

# OPEN QUESTIONS

---

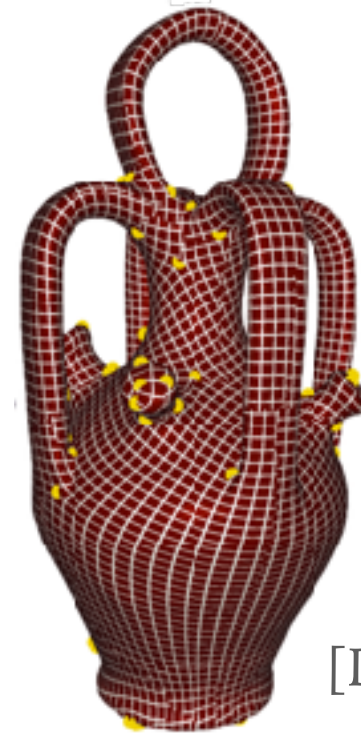
*Amir Vaxman*

*Department of Information and Computing Sciences  
Utrecht University*

# OPEN QUESTIONS: TOPOLOGY CONTROL

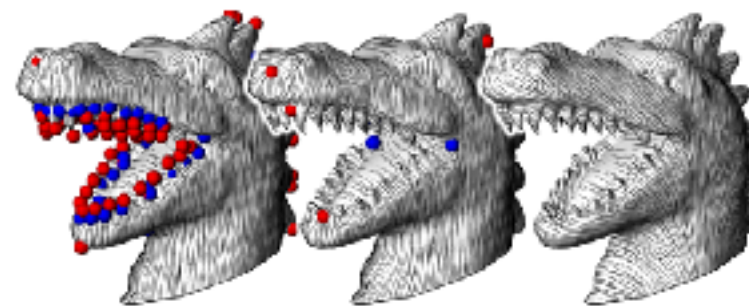
---

- Implicit Methods
  - Unpredictable singularities
    - Usually many low-degree.



[Diamanti *et al.* 2015]

- Explicit Methods
  - Specifying singularities
  - Direction fields
  - ...but nonconvex



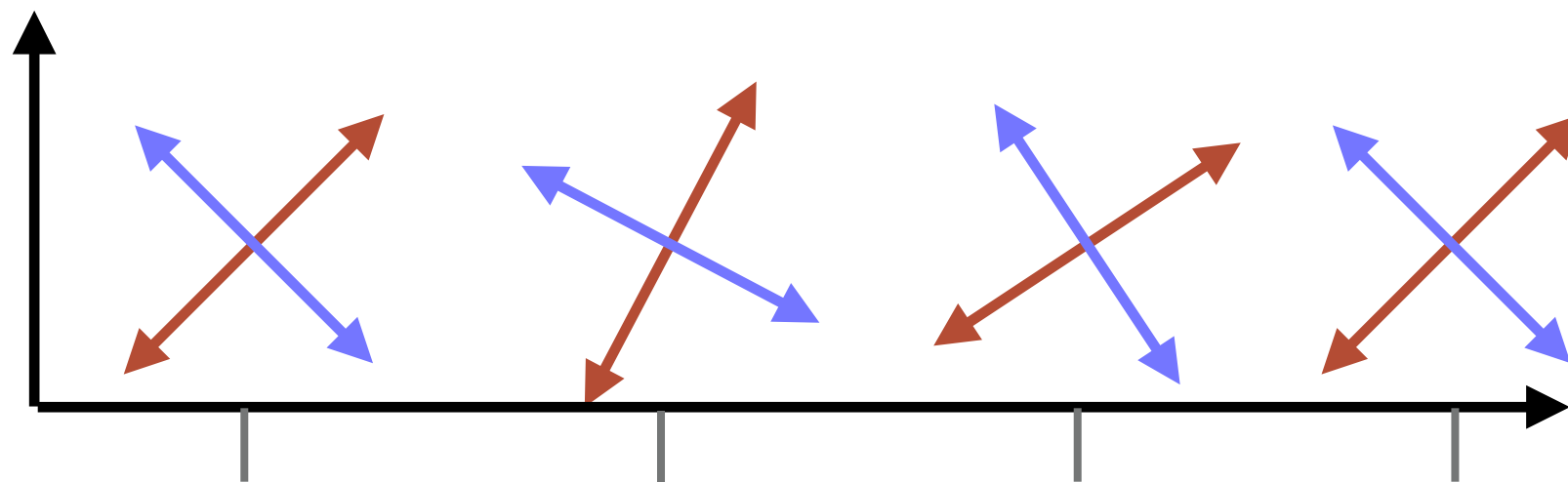
[Ray *et al.* 2009]

- **Current attempts:** alternatives to as-parallel-as-possible.

# OPEN QUESTIONS: SAMPLING & CONVERGENCE

---

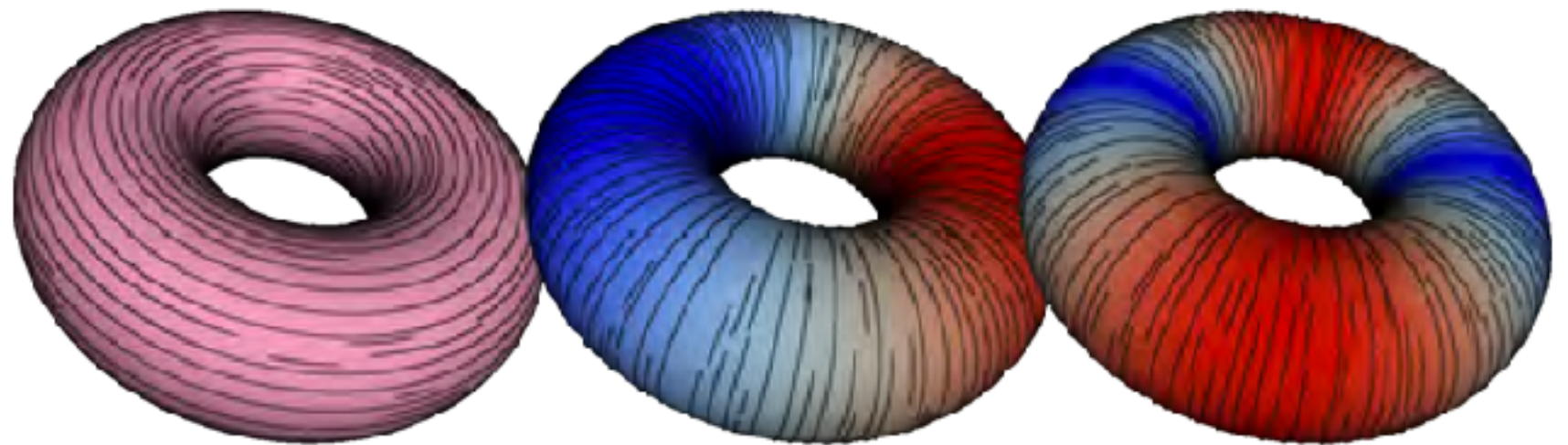
- **Discrete animals:** matching, period jumps.
- Bridge the gap between the continuous and the discrete.
- What is a good sampling?



# OPEN QUESTIONS: GEOMETRY

---

- Lie Bracket
  - [Azencot *et al.* 2013, de Goes *et al.* 2014, Azencot *et al.* 15].
  - Local and directly on vector fields
- Differential geometry of directional fields
  - Calculus
  - Operators

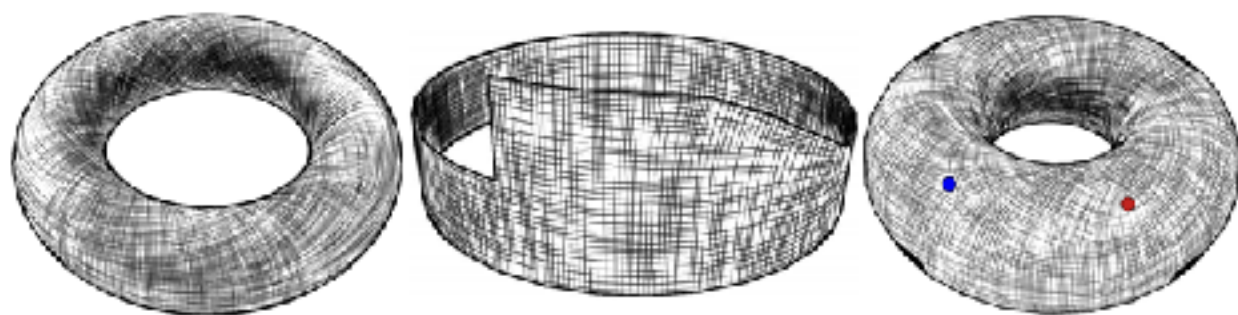


[de Goes *et al.* 2014]

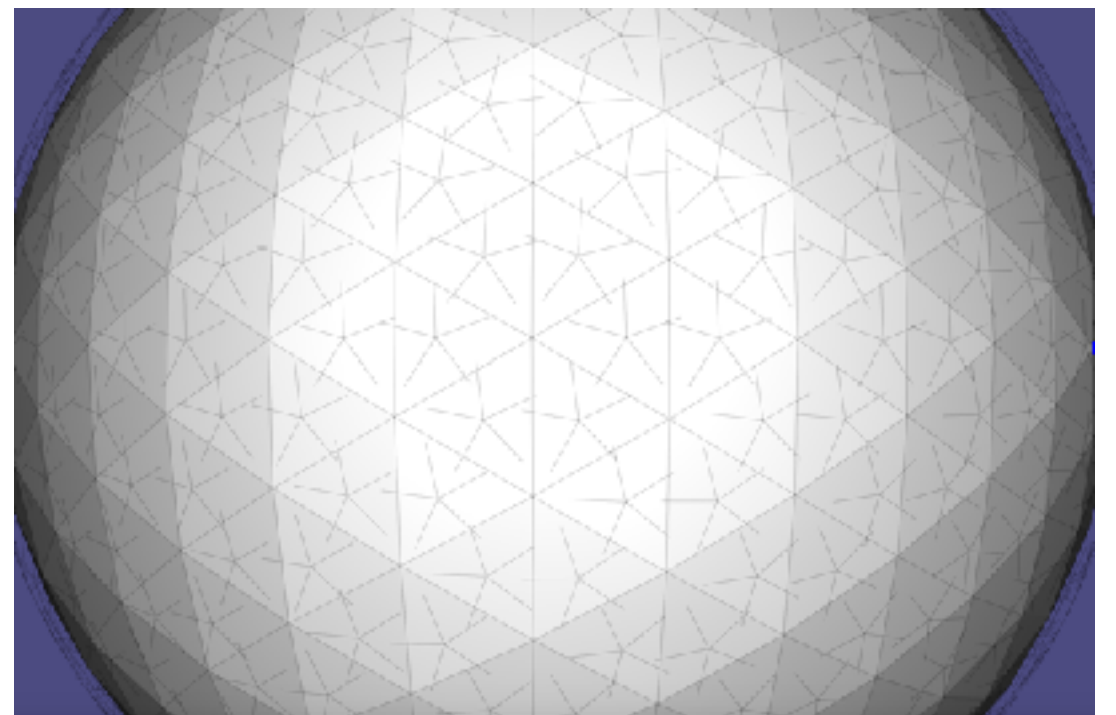
# OPEN QUESTIONS: PARAMETRIZATION

---

- Branched functions are more restricted than directionals.
- **Param**  $\rightarrow$  **vectors**: always possible.
- **Vectors**  $\rightarrow$  **Params**: *generally* impossible.
  - [Kälberer *et al.* 2007, Izmetiev *et al.* 2012, Myles *et al.* 2014]
- What is the space of parametrizing directionals?



[Myles *et al.* 2014]

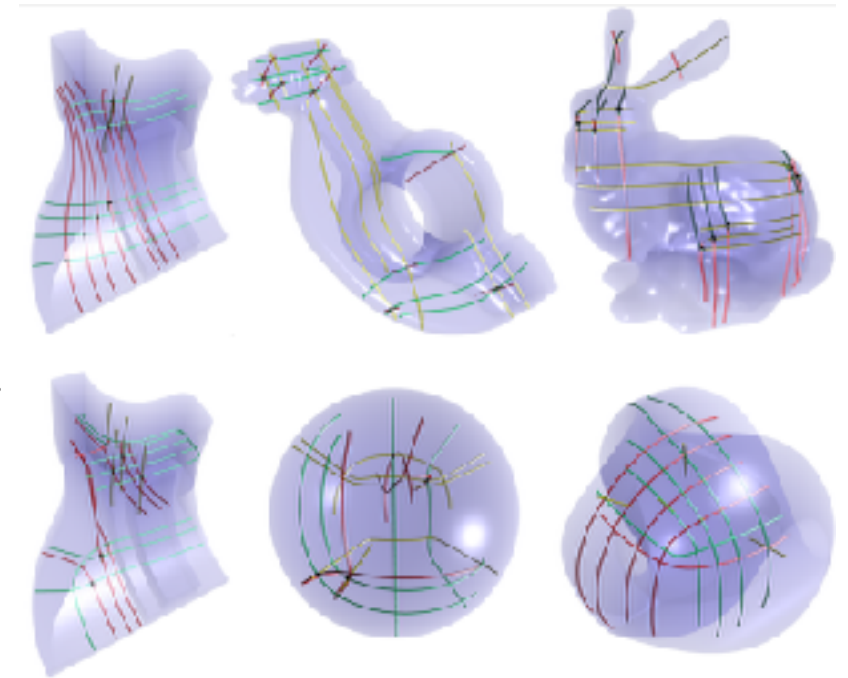




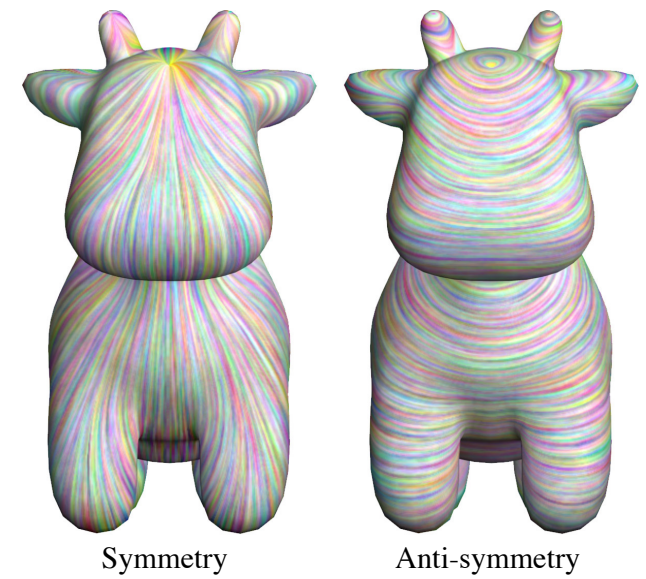
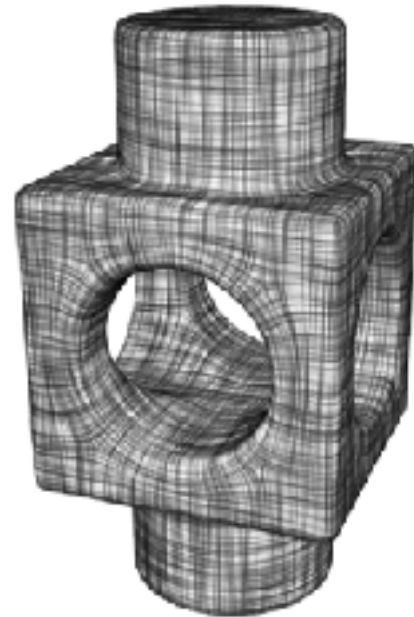
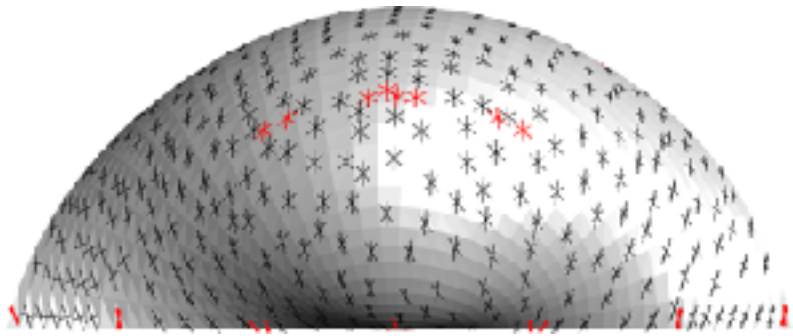
# OPEN QUESTIONS: THREE DIMENSIONS

---

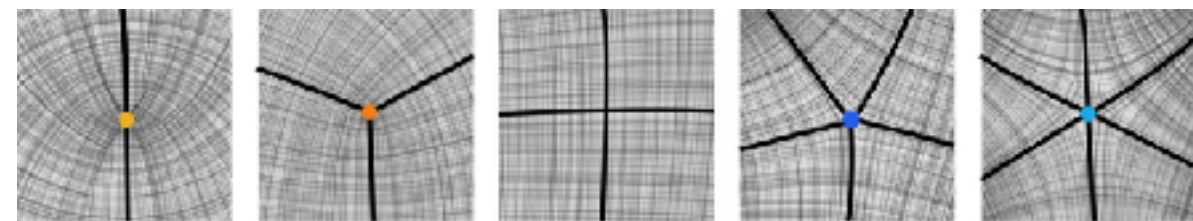
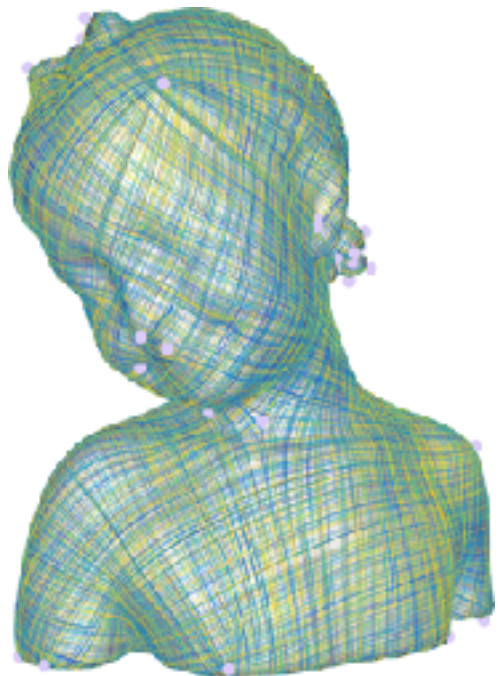
- Generalization is difficult:
  - Rotations are not commutative.
  - No notion of angle-based representation.
- **Singularities:** curves and nodes.
  - Index theorem?
- **Current attempts:**
  - Quaternions [Kowalski *et al.* 2014]
  - Tensors [Paris *et al.* 08]
  - Spherical Harmonics [Huang *et al.* 2011, Ray *et al.* 2016  
Solomon *et al.* 2016]



[Huang *et al.* 2011]



# THANK YOU!



\*Course repository: <https://github.com/avaxman/DirectionalFieldSynthesis>