$$u_f = (u_f^x, u_f^y) \in \mathbb{R}^2$$