$$\tilde{u}_g = u_g \bar{e}_g = |u_g| \exp\left\{i(\theta_{u_g} - \theta_{e_g})\right\}$$