DaSE CV Assignment1 Part1

助教: 孙秋实

数据科学与工程学院

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Outline

- KNN
- Cross-Validation
- Multiclass Support Vector Machine
- Softmax

KNN

加载 Cifar-10 数据集

```
X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
print('Training data shape: ', X_train.shape)
print('Training labels shape: ', y_train.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

查看数据维度

```
Training data shape: (50000, 32, 32, 3)
Training labels shape: (50000,)
Test data shape: (10000, 32, 32, 3)
Test labels shape: (10000,)
```

K-Nearest Neighbors

Instead of copying label from nearest neighbor, take **majority vote** from K closest points

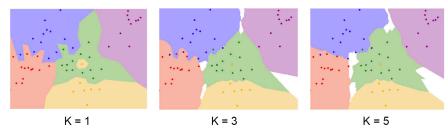


Figure: KNN Demo

KNN 算法实现

两层嵌套循环,遍历测试点,求其到全部训练样本点的距离

- 输入 X, (num_test,D) 维的数组
- 返回 dists (num_test, num_train) 维的 numpy 数组, dists[i, j] 表示 测试样本 i 到训练样本 j 的距离

KNN 算法实现

单层循环,遍历测试点,求其到全部训练样本点的距离

• 输入输出同上

```
def compute_distances_one_loop(self, X):
   num test = X.shape[0]
   num train = self.X train.shape[0]
   dists = np.zeros((num_test, num_train))
   for i in range (num test):
      ******************
      # TODO.
      # Compute the 12 distance between the ith test point and all training #
      # points, and store the result in dists[i, :].
      # Do not use np.linalg.norm().
      # ****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
      difference = self.X_train - X[i] #broadcast
      distance = np.sum(difference ** 2,axis = 1) #按行求和
      dists[i,:] = np.sqrt(distance)
      # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
   return dists
```

KNN 算法实现

完全向量化运行,求其到全部训练样本点的距离

● 输入输出同上

Cross Validation

交叉验证

将数据集划分3个部分,两两之间没有交集

- 训练集 Training Set
- 验证集 Validation Set
- 测试集 Test Set

fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test
fold 1	fold 2	fold 3	fold 4	fold 5	test

Figure: K-Fold Cross Validation

Cross Validation Cont'd

Cross Validation 实现

实现交叉验证,帮助选取超参数

Cross Validation Cont'd

Cross Validation 实现

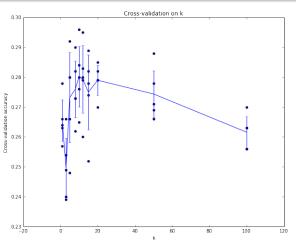
实现交叉验证,帮助选取超参数

```
k to accuracies = {} # Store the accuracies for all fold and all values of k
#TODO#
# Perform k-fold cross validation to find the best value of k. For each
# possible value of k, run the k-nearest-neighbor algorithm num folds times,
# where in each case you use all but one of the folds as training data and the
# last fold as a validation set.
for k in k choices:
  k to accuracies.setdefault(k . [])
for i in range (num folds):
  classifier = KNearestNeighbor()
  X val train = np.vstack(X train folds[0:i] + X train folds[i+1:])
  y_val_train = np.vstack(y_train_folds[0:i] + y_train_folds[i+1:])
  v val train = v val train[:,0]
  classifier.train(X val train, v val train)
   for k in k choices:
     v val pred = classifier.predict(X train folds[i], k=k)
      num_correct = np.sum(y_val_pred == y_train_folds[i][:,0])
      accuracy = float(num_correct) / len(y_val_pred)
      k to accuracies[k ] = k to accuracies[k] + [accuracy]
                         END OF YOUR CODE
```

Cross Validation Cont'd

Error bar

基于可视化结果,直观地选取超参



Multiclass Support Vector Machine

Suppose: 3 training examples, 3 classes. With some W the scores f(x,W)=Wx are:



cat **3.2**

car 5.1

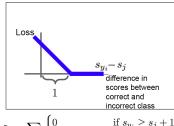
frog -1.7

1.3

4.9 2.5

2.0 **-3.1**

Interpreting Multiclass SVM loss:



$$\begin{split} L_i &= \sum_{j \neq y_i} \begin{cases} 0 & \text{if } s_{y_i} \geq s_j + 1 \\ s_j - s_{y_i} + 1 & \text{otherwise} \end{cases} \\ &= \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + 1) \end{split}$$

Figure: Hinge Loss

2.2

Multiclass Support Vector Machine

Multiclass SVM Loss

$$L_{i} = \sum_{j \neq y_{i}} \max \left(0, S_{j} - S_{y_{i}} + \Delta\right) \tag{1}$$

- L_i 第 i 个样本的 Hinge Loss
- S_v, 第 i 个样本分类标签分数
- S_i 第 i 个样本对应的标签

Regularized Multiclass SVM Loss Cont'd

$$L_i = \sum_{j \neq y_i} \max \left(0, S_j - S_{y_i} + \Delta\right) + \frac{\lambda}{2} \|\boldsymbol{w}\|^2$$
 (2)



Multiclass Support Vector Machine Cont'd

SVM 算法实现

Naive SVM Loss

```
def svm loss naive (W, X, v, reg):
 dW = np.zeros(W.shape) # initialize the gradient as zero
 # compute the loss and the gradient
 num classes = W.shape[1]
 num train = X.shape[0]
 loss = 0.0
 for i in xrange(num train):
   scores = X[i].dot(W)
   correct class score = scores[v[i]]
   for j in xrange(num_classes):
    if j == v[i]:
      continue
    margin = scores[i] - correct class score + 1 # note delta = 1
    if margin > 0:
     loss += margin
      dW[:,i] += X[i].T
      dW[:,v[i]] += -X[i].T
 # Right now the loss is a sum over all training examples, but we want it
 # to be an average instead so we divide by num train.
 loss /= num train
 dW /= num train
 # Add regularization to the loss.
 loss += 0.5 * reg * np.sum(W * W)
 dW += req * W
 return loss, dW
```

Multiclass Support Vector Machine Cont'd

SVM 算法实现

Vectorized SVM Loss

```
num_train = X.shape[0] # 得到样本的数目 scores = np.dot(X, W) # 计算所有的符分 y_score = scores[np.arange(num_train), y].reshape((-1, 1)) # 得到每个样本对应label的得分 mask = (scores - y_score + 1) > 0 # >0 loss 下标 scores = (scores - y_score + 1) * mask loss = (np.sum(scores) - num_train * 1) / num_train # 去掉每个样本多加的对应label得分,然后平均 loss += reg * np.sum(W * W)

# dw = x.T * dl/ds ds = np.ones_like(scores) # 初始化ds ds *= mask # >0 ->1, <0 ->0 ds[np.arange(num_train), y] = -1 * (np.sum(mask, axis=1) - 1) # # 负非0项个数 dW = np.dot(X.T, ds) / num_train dW += 2 * reg * W # add regularization
```

Softmax

Softmax Classifier (Multinomial Logistic Regression)

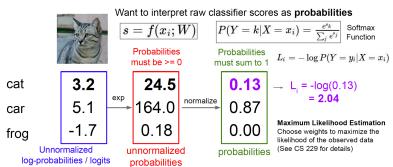


Figure: Softmax

Softmax Cont'd

Softmax 的各分量

$$\rho_k = \frac{e^{f_k}}{\sum_j e^{f_j}} \tag{3}$$

- k:某个特定类别
- f: 分值向量
- *j*:任意一个类别
- p_k: k 类别的概率大小

Regularized Softmax Loss

$$L = \underbrace{\frac{1}{N} \sum_{i} L_{i}}_{\text{data loss}} + \underbrace{\frac{1}{2} \lambda \sum_{k} \sum_{l} W_{k,l}^{2}}_{\text{regularization loss}}$$

(4)

Softmax

Softmax 算法实现

Naive Softmax

```
def softmax_loss_naive(W, X, y, reg):
loss = 0.0
dW = np.zeros like(W)
for i in range(X.shape[0]):
   score = np.dot(X[i], W)
   score -= max(score) # stability
   score = np.exp(score) # exp
   softmax sum = np.sum(score) # get den
   score /= softmax sum
   # calc gradient
   for j in range (W.shape[1]):
      if | != v[i]:
         dW[:, j] += score[j] * X[i]
      else:
         dW[:, j] = (1 - score[j]) * X[i]
   loss -= np.log(score[y[i]]) # cross entropy
loss /= X.shape[0]
dW /= X.shape[0]
loss += reg * np.sum(W * W) # add reg
dW += 2 * reg * W
return loss, dW
```

Softmax Cont'd

Softmax 算法实现

Vectorized Softmax

```
def softmax loss vectorized (W, X, v, reg):
Softmax loss function, vectorized version.
Inputs and outputs are the same as softmax loss naive.
. . .
# Initialize the loss and gradient to zero.
loss = 0.0
dW = np.zeros like(W)
scores = np.dot(X, W) # calc score
scores -= np.max(scores, axis=1, keepdims=True) # stability
scores = np.exp(scores) # exp
scores /= np.sum(scores, axis=1, keepdims=True) # softmax
ds = np.copy(scores) # init grad
ds[np.arange(X.shape[0]), v] -= 1 # get grad
dW = np.dot(X.T, ds) # get grad for w
loss = scores[np.arange(X.shape[0]), y] # compute loss
loss = -np.log(loss).sum() #get cross entropy
loss /= X.shape[0]
dW /= X.shape[0]
loss += reg * np.sum(W * W)
dW += 2 * reg * W
return loss, dW
```

问答环节

Questions!