

# 8/25/2020

Figure 1:  $y = x^4$  with  $sd = 100$

Figure 2:  $y = \sin(x)$  with  $sd = 1$

- The optimal bandwidth does not have the lowest MSE due to the tail behavior (plot 2)
- The lowest MSE is given when bandwidth =  $10^{-1}$ . Compare this with the optimal curve
- Compare the simulated MSE with the theoretical MSE (Simulation  $L = 100000$ , bandwidth = 0.1)
- Find some symmetric pattern in the MSE difference (diff = simulated MSE - theoretical MSE)
- Simulated MSE < Theoretical MSE?

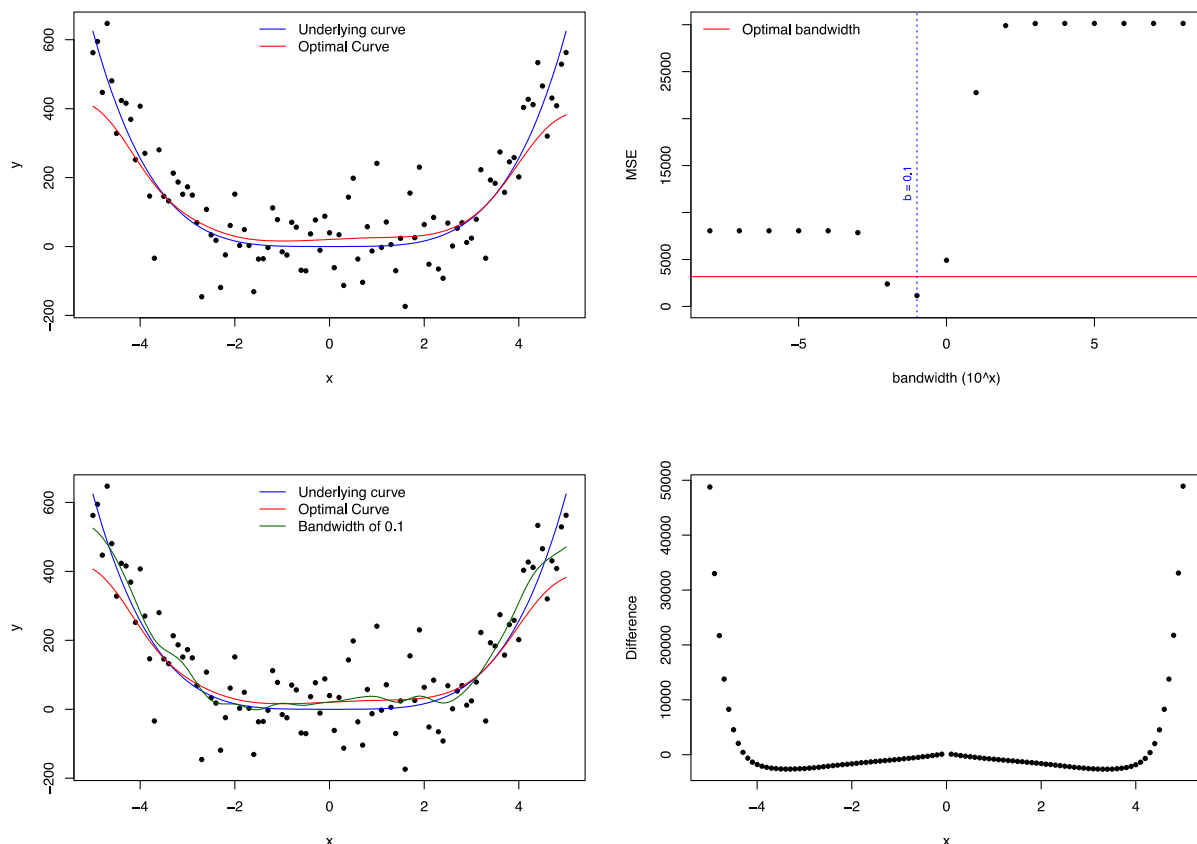


Figure 1:  $y = x^4$

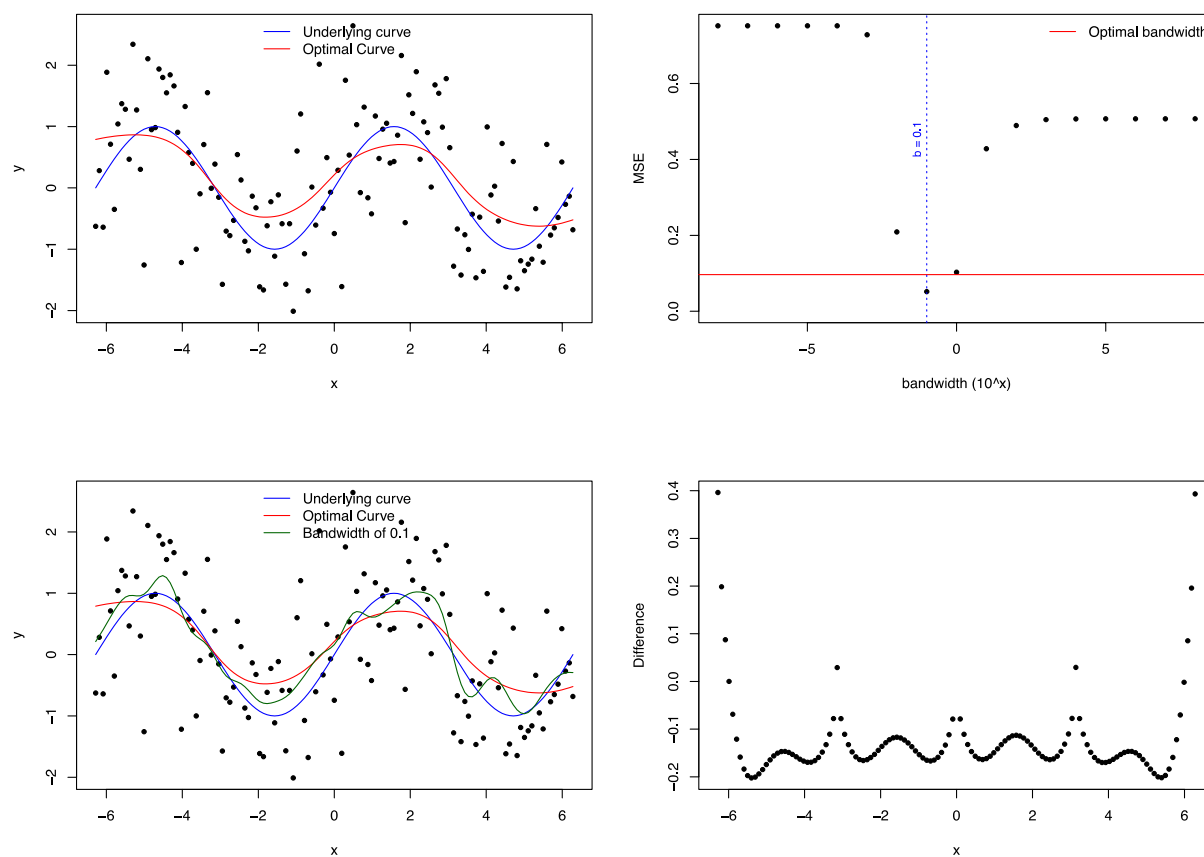


Figure 2:  $y = \sin(x)$

Other Question:

$$Y_i = g(x_i) + \epsilon_i$$

$$MSE = \sum_{i=1}^N (\hat{Y}_i - Y_i)^2 = \sum_{i=1}^N (\hat{Y}_i - g(x_i))^2$$

$$MISE = \int_1^5 [\hat{g}(x) - g(x)]^2 dx = \int_1^5 [\hat{Y}_i - g(x)]^2 dx = \sum_{i=1}^N [\hat{Y}_i - g(x)]^2 \cdot dx$$

