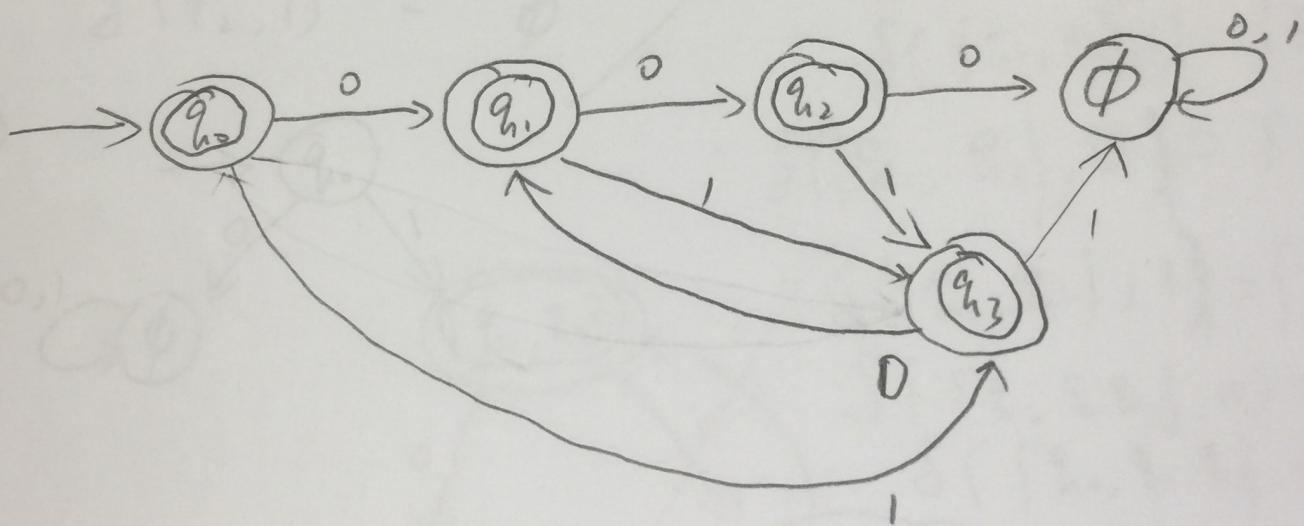
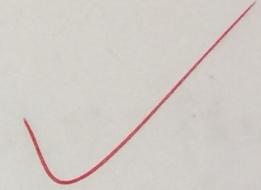
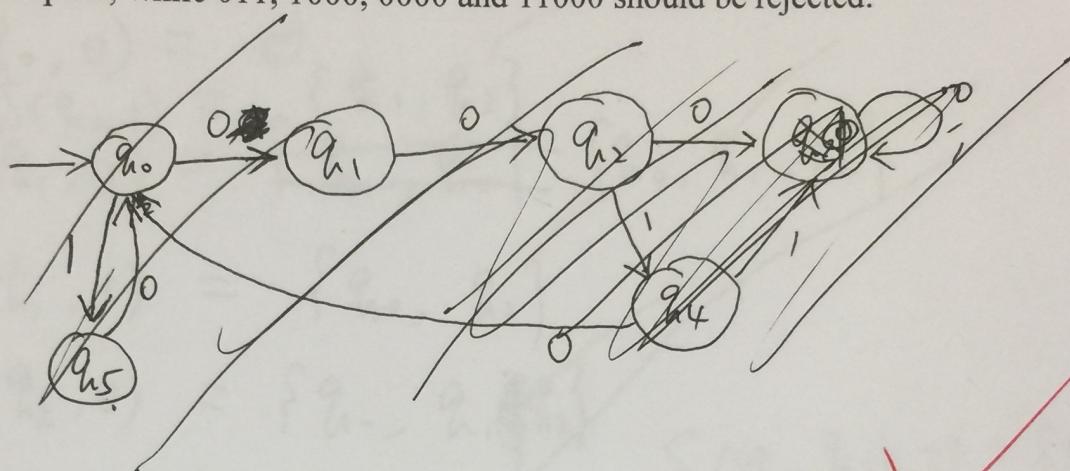


# Test # 2

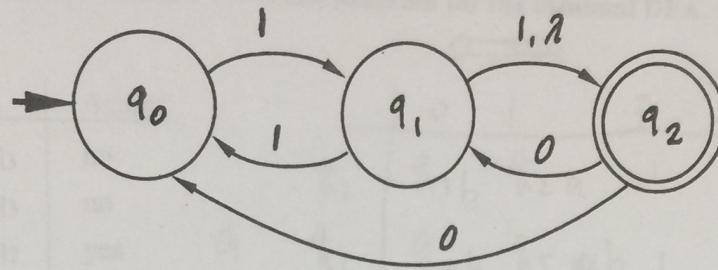
March 29, 2018

25 pts

1. Find a deterministic finite acceptor that accepts all strings on  $\{0, 1\}$ , except those containing substrings 11 or 000. For example,  $\lambda, 0, 1, 00$  and  $0101$  should be accepted; while  $011, 1000, 0000$  and  $11000$  should be rejected.



2. For the following non-deterministic finite acceptor:



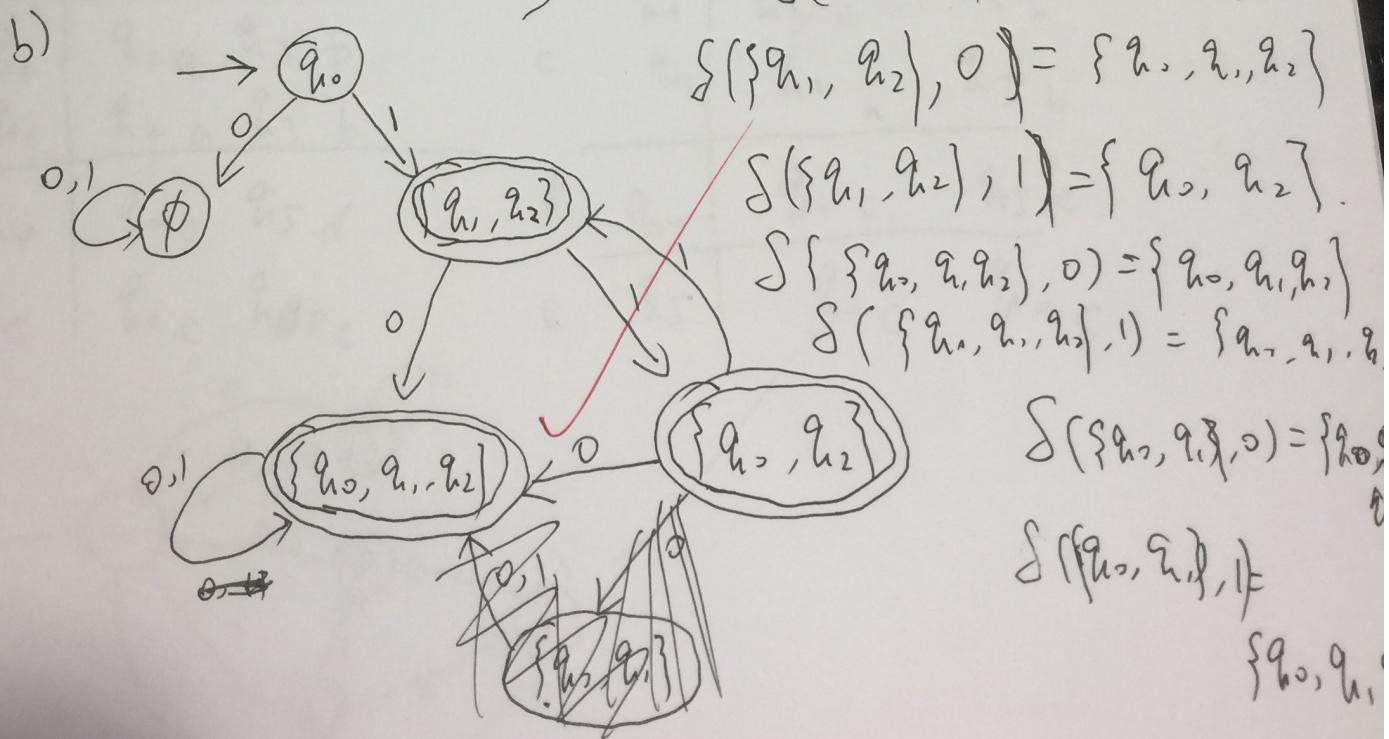
$$0, \lambda = \emptyset \\ \pi \cdot 0 \cdot \lambda = \emptyset$$

- 15 pts. (a) find  $\delta(q_0, 0)$ ,  $\delta(q_0, 1)$ ,  $\delta(q_1, 0)$ ,  $\delta(q_1, 1)$ ,  $\delta(q_2, 0)$  and  $\delta(q_2, 1)$ ,  
10 pts. (b) convert it into a deterministic finite acceptor. **Show your work.**

a)

$$\begin{aligned} \delta(q_0, 0) &= \emptyset \\ \delta(q_0, 1) &= \{q_1, q_2\} \\ \delta(q_1, 0) &= \cancel{\{q_0, q_1, q_2\}} \quad \{q_0, q_1, q_2\} \\ \delta(q_1, 1) &= \{q_0, q_2\} \\ \delta(q_2, 0) &= \{q_0, q_1, \cancel{q_2}\} \\ \delta(q_2, 1) &= \emptyset \end{aligned}$$

$$\begin{aligned} \delta(\{q_0, q_2\}, 0) &= \{q_0, q_1\} \\ \delta(\{q_0, q_2\}, 1) &= \{q_1, q_2\} \end{aligned}$$



20 pts.

3. Minimize the following deterministic finite acceptor using the k-equivalence algorithm. State  $q_0$  is initial. Show the diagram for the minimal DFA. Show your work.

 $\delta$ -equiv

	0	1	Accept
$q_0$	$q_2$	$q_3$	no
$q_1$	$q_2$	$q_3$	no
$q_2$	$q_1$	$q_2$	yes
$q_3$	$q_4$	$q_5$	yes
$q_4$	$q_0$	$q_5$	no
$q_5$	$q_0$	$q_0$	no

check:

$$[q_2, q_3] \quad [q_0, q_1, q_4, q_5]$$

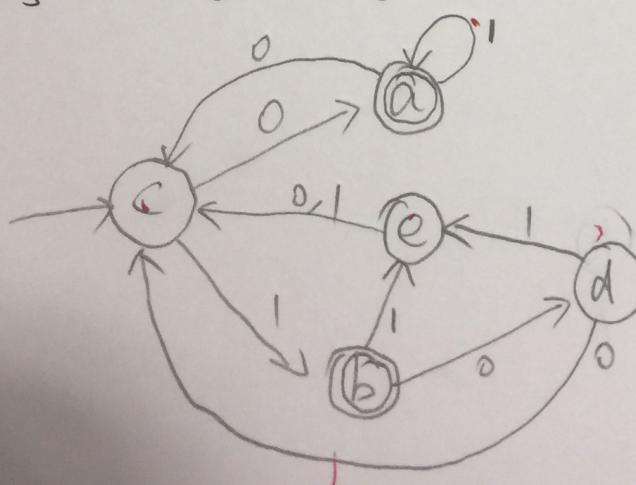
$$[q_2] \quad [q_3] \quad [q_0, q_1] \quad [q_4, q_5]$$

$$[q_2] \quad [q_3] \quad [q_0, q_1] \quad [q_4] \quad [q_5]$$

	0	1	F
$q_2$	$q_1, b$	$q_2, a$	1
$q_3$	$q_4, b$	$q_5, \cancel{b}$	1
$q_0$	$q_2, a$	$q_3, a$	0
$q_1$	$q_2, a$	$q_3, a$	0
$q_4$	$q_2, b$	$q_5, b$	0
$q_5$	$q_1, b$	$q_0, b$	0

	0	1	
a	$q_2$	$q_{1,c}$	$q_{2,a}$
b	$q_3$	$q_{4,d}$	$q_{5,d}$
c	$q_5$	$q_{2,a}$	$q_{3,b}$
d	$q_1$	$q_{2,a}$	$q_{3,b}$
e	$q_4$	$q_{1,c}$	$q_{5,d}$
	$q_5$	$q_{1,c}$	$q_{1,c}$

	0	1	
a	$q_2$	$q_{1,c}$	$q_{2,a}$
b	$q_3$	$q_{4,d}$	$q_{5,e}$
c	$q_5$	$q_{2,a}$	$q_{3,b}$
d	$q_1$	$q_{2,a}$	$q_{3,b}$
e	$q_4$	$q_{1,c}$	$q_{5,e}$
	$q_5$	$q_{1,c}$	$q_{1,c}$



50 pts.

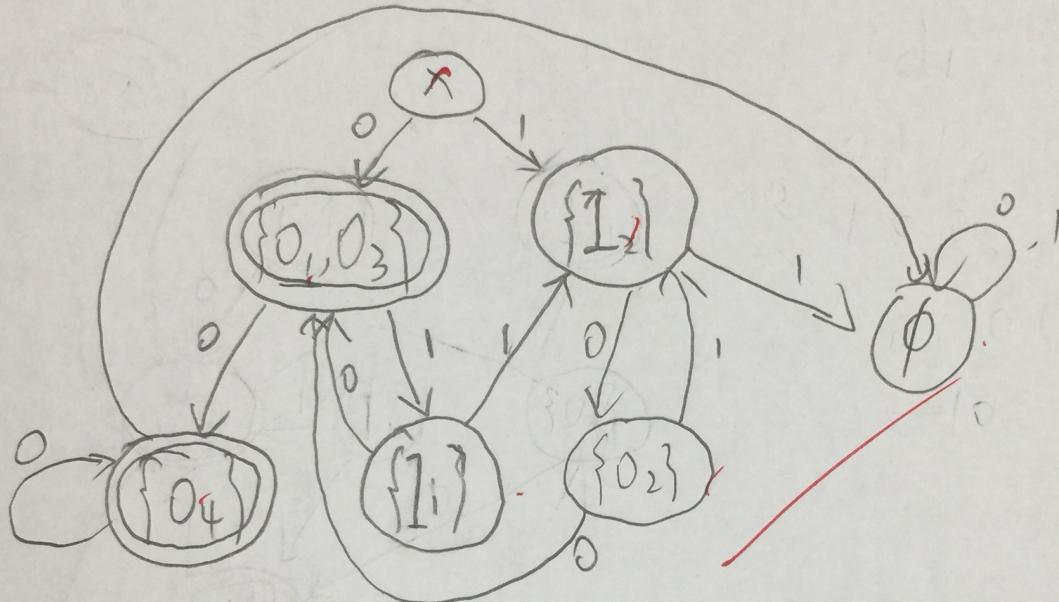
DFA

4. Find the deterministic finite acceptor, using McNaughton-Yamada algorithm, that accepts the language over  $\Sigma = \{0, 1\}$  defined by the following regular expression

$$(01 + 10)^* (0(0^*)) .$$

Show your work.

$$r = (0_1 1_1 + 1_2 0_2)^* (0_3 (0_4^*))$$



0 1 0 1 0 1 0<sub>3</sub>

① 0 1 0 1 0 1 0 0<sub>3</sub>.

② 0 1 0 0 0

1 0 0 0 0

③ ~~0 0 0 0~~

④