

1: due on Mar 1st 11:59pm
2: follow the instruction !!!
* "Title of your email"
* program name (file name) "Stable-matching-[KUID].py."
* Input format
* tie-breaking rule.

3 (num. of persons)	1,2
1,2,3 2,1,3 3,2,1 (men's list)	2,3 3,1
1,2,3 2,3,1 (women's list)	



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The G-S algorithm

Initialize each person to be free.

while (some man is free and has not proposed to every woman) {

 Choose such a man m .

$w = 1$ st woman in m 's list who m has not proposed to.

 if (w is free): engage m and w .

* else if (w prefers m over her fiance' m'): engage m and w , free m' .
else: w rejects m .

A \cap B
A
B

(F)
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Does the G-S algorithm terminate?

"When all men have proposed to all women."

" $O(n^2)$ "

Does everyone get paired up? 每个人都配对嘛

Observation: A woman only trades up, but never becomes free again.

Proof: by contradiction.

* If we assume there is a man m who is unmatched upon termination, then there is also a woman who is free, let the woman be w .



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- * Since w is free, she is never proposed to.
- * m is free, so he has proposed to every woman.
- * It contradicts with the fact that w has not been proposed.
- * --- Conclusion.

Proposition. There exists no unstable matching upon the termination of the algorithm.

Proof: by contradiction.

Assume an unstable matching exists. i.e. (m, w') , and let m paired with w (m, w)
and let w' paired with m' (m', w')

- * In the first case, m has proposed to w' .
Since woman only trades up. so w' likes her current partner m' better than m .

So there is no instability.

- * In the second case, m has not proposed to w' .
Since men propose in descending order.
It means m prefers w over w' .
So there is no instability.



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The G-S algorithm

Initialize each person to be free.

while (Some man is free and has not proposed to every woman) { $O(n^2)$

 Choose such a man m . \star (linked list)

$w =$ 1st woman in m 's list who m has not proposed to. \star

 if (w is free): engage m and w .

* else if (w prefers m over her fiancé m'): engage m and w , free m' .

else: w rejects m .

A \cap B
A
B

(F)
(T)
(F)

	1st	2nd	3rd		1st	2nd	3rd
x	a ↗	b	c	a	y	x	z
y	b	a ↗	c	b	x	y	z
z	a ↗	b	c	c	x	y	z

1. Pick x . x proposes to a , and engage $x-a$.
2. Pick z . z proposes to a , a rejects z
3. Pick y . y proposes to b , engage $y-b$
4. Pick z . z proposes to b . b rejects z .
5. Pick z . z proposes to c , engage $z-c$



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