

**Instruction:** You must show all your calculations clearly for credit.

1. (8) Compute  $\sum_{i=28}^n (3i^2 - 4i + \frac{5}{7^i})$ . Do not simplify your solution.
2. (8) Compute  $\sum_{i=1}^n i(i+1)(i+2)$ . Simplify your solution.
3. (12) Compute  $\sum_{i=28}^n \sum_{j=i}^n (3i + 4j - 5ij)$ . Do not simplify your solution.
4. (12) Compute  $\sum_{i=1}^n \frac{i}{3^i}$ . Simplify your solution.
5. (12) Compute  $\sum_{i=1}^n \frac{i}{2^{n-i+1}}$ . Simplify your solution.
6. (12) Compute  $\frac{1}{2*5} + \frac{1}{3*6} + \frac{1}{4*7} + \dots + \frac{1}{(n-2)(n+1)} + \frac{1}{(n-1)(n+2)}$  using the technique of telescoping summation. Do not simplify your solution.
7. (12) Recall that  $\sum_{i=1}^n i = \frac{n(n+1)}{2}$  and  $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$ . Compute  $\sum_{i=1}^n i^3$  using the technique of telescoping summations.
8. (12) By concentrating on the dominating step(s) and also assuming that all basic operations are having the same constant cost C, compute  $T_w(n)$  in closed-form for the following program segment. Do not simplify your solution.
 

```

x = 210;
y = 560;
for i = 1 to n do
    for j = 1 to 2*i do
        x = 3*x + 1;
    endfor;
    for k = i to n*n do
        y = x*y/2;
    endfor;
endfor;
      
```

9. (12) By concentrating on the dominating step(s) and also assuming that all basic operations are having the same constant cost  $C$ , compute  $T_w(n)$  in closed-form for the following program segment. Do not simplify your solution.

```
x = 210;  
y = 560;  
for i = 1 to n do  
  for j = 1 to i do  
    x = 3 * x + 1;  
    for k = i to n do  
      y = x * y / 2;  
    endfor;  
  endfor;  
endfor;
```

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