

Answer Set Solving in Practice

Torsten Schaub, Javier Romero, Etienne Tignon
University of Potsdam — Winter Semester 2020/2021

Quiz 1

Answer

- | | | |
|--|-------------|--------------|
| 1. Each positive logic program has some model. | true | false |
| 2. Each positive logic program has some stable model. | true | false |
| 3. If P is a positive logic program and $A(P)$ are the atoms occurring in P then $A(P)$ is a model of P . | true | false |
| 4. If P is a positive logic program and $A(P)$ are the atoms occurring in P then $A(P)$ is a stable model of P . | true | false |
| 5. If a positive rule is satisfied by a set of atoms, then each of its supersets satisfies the rule as well. | true | false |
| 6. The stable model of a positive logic program is contained in each model of the program. | true | false |

Quiz 2**Answer**

- | | | |
|--|-------------|--------------|
| 1. Each normal logic program has some model. | true | false |
| 2. Each normal logic program has some stable model. | true | false |
| 3. Given a normal logic program P , the reduct P^X is contained in P^Y for each subset X of a set Y of atoms. | true | false |
| 4. If a set X of atoms is a model of a normal logic program P , then X is a model of the reduct P^Y for each superset Y of X . | true | false |
| 5. Given a normal logic program P , each stable model of P is a \subseteq -minimal model of P . | true | false |

Exercise 1 (Positive Logic Programs)

Determine the models of the following positive logic programs and decide which models are stable.

$$1\text{-a} \quad P = \left\{ \begin{array}{l} \textit{rain} \leftarrow \\ \textit{wet} \leftarrow \textit{rain} \\ \textit{wet} \leftarrow \textit{sprinkler} \end{array} \right\}$$

$$1\text{-b} \quad P = \left\{ \begin{array}{l} \textit{coffee} \leftarrow \\ \textit{lemon} \leftarrow \textit{tea} \\ \textit{sugar} \leftarrow \textit{coffee} \\ \textit{milk} \leftarrow \textit{coffee}, \textit{sugar} \\ \textit{tea} \leftarrow \textit{lemon} \\ \textit{tea} \leftarrow \textit{diet} \end{array} \right\}$$

$$1\text{-c} \quad P = \left\{ \begin{array}{l} \textit{shirt} \leftarrow \\ \textit{sneakers} \leftarrow \\ \textit{pants} \leftarrow \textit{sneakers} \\ \textit{skirt} \leftarrow \textit{shirt}, \textit{sandals} \\ \textit{sandals} \leftarrow \textit{dress} \end{array} \right\}$$

$$1\text{-d} \quad P = \left\{ \begin{array}{l} \textit{red} \leftarrow \\ \textit{meat} \leftarrow \textit{cabbage} \\ \textit{meat} \leftarrow \textit{red} \\ \textit{fish} \leftarrow \textit{asparagus} \\ \textit{asparagus} \leftarrow \textit{fish}, \textit{white} \\ \textit{white} \leftarrow \textit{fish} \end{array} \right\}$$

Exercise 2 (Normal Logic Programs)

Determine the stable models of the following normal logic programs.

$$\begin{array}{ll}
 2\text{-a} & P = \left\{ \begin{array}{l} \textit{sprinkler} \leftarrow \neg \textit{rain} \\ \textit{rain} \leftarrow \neg \textit{sprinkler} \\ \textit{wet} \leftarrow \textit{rain} \\ \textit{wet} \leftarrow \textit{sprinkler} \end{array} \right\} \\
 2\text{-b} & P = \left\{ \begin{array}{l} \textit{diet} \leftarrow \neg \textit{sugar} \\ \textit{coffee} \leftarrow \neg \textit{tea} \\ \textit{lemon} \leftarrow \textit{tea} \\ \textit{sugar} \leftarrow \textit{coffee} \\ \textit{milk} \leftarrow \textit{coffee}, \textit{sugar} \\ \textit{tea} \leftarrow \textit{lemon} \\ \textit{tea} \leftarrow \textit{diet} \end{array} \right\} \\
 2\text{-c} & P = \left\{ \begin{array}{l} \textit{dress} \leftarrow \neg \textit{shirt} \\ \textit{shirt} \leftarrow \neg \textit{dress} \\ \textit{sandals} \leftarrow \neg \textit{sneakers} \\ \textit{sneakers} \leftarrow \neg \textit{sandals} \\ \textit{pants} \leftarrow \textit{sneakers} \\ \textit{skirt} \leftarrow \textit{shirt}, \textit{sandals} \\ \textit{sandals} \leftarrow \textit{dress} \end{array} \right\} \\
 2\text{-d} & P = \left\{ \begin{array}{l} \textit{asparagus} \leftarrow \neg \textit{cabbage} \\ \textit{cabbage} \leftarrow \neg \textit{asparagus} \\ \textit{red} \leftarrow \neg \textit{white} \\ \textit{meat} \leftarrow \textit{cabbage} \\ \textit{meat} \leftarrow \textit{red} \\ \textit{fish} \leftarrow \textit{asparagus} \\ \textit{asparagus} \leftarrow \textit{fish}, \textit{white} \\ \textit{white} \leftarrow \textit{fish} \end{array} \right\}
 \end{array}$$

Exercise 3 (Positive Logic Programs with Variables)

Determine the Herbrand universe \mathcal{T} , the Herbrand base \mathcal{A} , the ground instantiation, and the stable models of the following positive logic programs with variables.

$$\begin{array}{ll}
 \text{3-a} & P = \left\{ \begin{array}{l} \text{fish}(\text{blinky}) \leftarrow \\ \text{bird}(\text{tweety}) \leftarrow \\ \text{flies}(X) \leftarrow \text{bird}(X) \end{array} \right\} \\
 \text{3-b} & P = \left\{ \begin{array}{l} \text{next}(0, 1) \leftarrow \\ \text{next}(1, 0) \leftarrow \\ \text{even}(0) \leftarrow \\ \text{even}(Y) \leftarrow \text{next}(X, Y), \text{odd}(X) \\ \text{odd}(Y) \leftarrow \text{next}(X, Y), \text{even}(X) \end{array} \right\} \\
 \text{3-c} & P = \left\{ \begin{array}{l} \text{friend}(\text{alice}, \text{bob}) \leftarrow \\ \text{friend}(\text{bob}, \text{alice}) \leftarrow \\ \text{friend}(\text{eve}, \text{alice}) \leftarrow \\ \text{invite}(\text{alice}) \leftarrow \\ \text{invite}(Y) \leftarrow \text{invite}(X), \text{friend}(X, Y) \end{array} \right\} \\
 \text{3-d} & P = \left\{ \begin{array}{l} \text{next}(0, 1) \leftarrow \\ \text{next}(1, 2) \leftarrow \\ \text{before}(X) \leftarrow \text{next}(X, Y) \\ \text{between}(Y) \leftarrow \text{next}(X, Y), \text{before}(Y) \end{array} \right\}
 \end{array}$$

Exercise 4 (Normal Logic Programs with Variables)

Determine the ground instantiation and the stable models of the following normal logic programs with variables.

$$4\text{-a} \quad P = \left\{ \begin{array}{l} \textit{sparrow}(\textit{jack}) \leftarrow \\ \textit{penguin}(\textit{tweety}) \leftarrow \\ \textit{bird}(X) \leftarrow \textit{sparrow}(X) \\ \textit{bird}(X) \leftarrow \textit{penguin}(X) \\ \textit{flies}(X) \leftarrow \textit{bird}(X), \neg \textit{penguin}(X) \end{array} \right\}$$

$$4\text{-b} \quad P = \left\{ \begin{array}{l} \textit{next}(0, 1) \leftarrow \\ \textit{next}(1, 0) \leftarrow \\ \textit{even}(X) \leftarrow \neg \textit{odd}(X) \\ \textit{odd}(Y) \leftarrow \textit{next}(X, Y), \textit{even}(X) \end{array} \right\}$$

$$4\text{-c} \quad P = \left\{ \begin{array}{l} \textit{next}(0, 1) \leftarrow \\ \textit{next}(1, 2) \leftarrow \\ \textit{next}(2, 0) \leftarrow \\ \textit{select}(X) \leftarrow \textit{next}(X, Y), \neg \textit{select}(Y) \end{array} \right\}$$

$$4\text{-d} \quad P = \left\{ \begin{array}{l} \textit{friend}(\textit{alice}, \textit{bob}) \leftarrow \\ \textit{friend}(\textit{bob}, \textit{alice}) \leftarrow \\ \textit{friend}(\textit{eve}, \textit{alice}) \leftarrow \\ \textit{refuse}(X) \leftarrow \neg \textit{invite}(X) \\ \textit{invite}(X) \leftarrow \neg \textit{refuse}(X) \\ \textit{invite}(Y) \leftarrow \textit{invite}(X), \textit{friend}(X, Y) \end{array} \right\}$$

Exercise 5 (Safety)

Determine which rules of the following programs are not safe.

$$\begin{array}{ll}
 \text{5-a} & P = \left\{ \begin{array}{l} \textit{sparrow}(\textit{jack}) \leftarrow \\ \textit{penguin}(\textit{tweety}) \leftarrow \\ \textit{bird}(X) \leftarrow \textit{sparrow}(X) \\ \textit{bird}(X) \leftarrow \textit{penguin}(X) \\ \textit{animal}(X) \leftarrow \\ \textit{flies}(X) \leftarrow \neg \textit{penguin}(X) \end{array} \right\} \\
 \text{5-b} & P = \left\{ \begin{array}{l} \textit{next}(0, 1) \leftarrow \\ \textit{next}(1, 0) \leftarrow \\ \textit{greater_equal}(1, X) \leftarrow \\ \textit{even}(X) \leftarrow \neg \textit{odd}(X) \\ \textit{odd}(Y) \leftarrow \textit{next}(X, Y), \textit{even}(X), \neg \textit{odd}(X) \end{array} \right\} \\
 \text{5-c} & P = \left\{ \begin{array}{l} \textit{next}(0, 1) \leftarrow \\ \textit{next}(1, 2) \leftarrow \\ \textit{next}(2, 0) \leftarrow \\ \textit{select}(X) \leftarrow \neg \textit{next}(X, Y), \neg \textit{select}(Y) \end{array} \right\} \\
 \text{5-d} & P = \left\{ \begin{array}{l} \textit{friend}(\textit{alice}, \textit{bob}) \leftarrow \\ \textit{friend}(\textit{bob}, \textit{alice}) \leftarrow \\ \textit{friend}(\textit{eve}, X) \leftarrow \\ \textit{refuse}(X) \leftarrow \neg \textit{invite}(X) \\ \textit{invite}(X) \leftarrow \neg \textit{refuse}(X) \\ \textit{invite}(Y) \leftarrow \textit{invite}(X), \neg \textit{friend}(X, Y) \end{array} \right\}
 \end{array}$$

Solution**Quiz 1****Answer**

- | | |
|--|--------------|
| 1. Each positive logic program has some model. | true |
| 2. Each positive logic program has some stable model. | true |
| 3. If P is a positive logic program and $A(P)$ are the atoms occurring in P then $A(P)$ is a model of P . | true |
| 4. If P is a positive logic program and $A(P)$ are the atoms occurring in P then $A(P)$ is a stable model of P . | false |
| 5. If a positive rule is satisfied by a set of atoms, then each of its supersets satisfies the rule as well. | false |
| 6. The stable model of a positive logic program is contained in each model of the program. | true |

Solution**Quiz 2****Answer**

- | | |
|--|--------------|
| 1. Each normal logic program has some model. | true |
| 2. Each normal logic program has some stable model. | false |
| 3. Given a normal logic program P , the reduct P^X is contained in P^Y for each subset X of a set Y of atoms. | false |
| 4. If a set X of atoms is a model of a normal logic program P , then X is a model of the reduct P^Y for each superset Y of X . | true |
| 5. Given a normal logic program P , each stable model of P is a \subseteq -minimal model of P . | true |

Solution 1

1-a Models:

- $\{rain, wet\}$
- $\{rain, wet, sprinkler\}$

Stable Model: $\{rain, wet\}$

1-b Models:

- $\{coffee, sugar, milk\}$
- $\{coffee, sugar, milk, tea, lemon\}$
- $\{coffee, sugar, milk, tea, lemon, diet\}$

Stable Model: $\{coffee, sugar, milk\}$

1-c Models:

- $\{shirt, sneakers, pants\}$
- $\{shirt, sneakers, pants, skirt\}$

- $\{shirt, sneakers, pants, skirt, sandals\}$
- $\{shirt, sneakers, pants, skirt, sandals, dress\}$

Stable Model: $\{shirt, sneakers, pants\}$

1-d Models:

- $\{red, meat\}$
- $\{red, meat, cabbage\}$
- $\{red, meat, white\}$
- $\{red, meat, white, cabbage\}$
- $\{red, meat, white, fish, asparagus\}$
- $\{red, meat, white, fish, asparagus, cabbage\}$

Stable Model: $\{red, meat\}$

Solution 2

2-a Stable Models:

- $\{rain, wet\}$
- $\{sprinkler, wet\}$

2-b Stable Models:

- $\{coffee, sugar, milk\}$
- $\{tea, lemon, diet\}$

2-c Stable Models:

- $\{shirt, sneakers, pants\}$
- $\{shirt, sandals, skirt\}$
- $\{dress, sandals\}$

2-d Stable Models:

- $\{red, meat, cabbage\}$
- $\{white, fish, asparagus\}$

Solution 3

3-a Herbrand Universe $\mathcal{T} = \{blinky, tweety\}$
Herbrand Base:

$$\mathcal{A} = \left\{ \begin{array}{l} fish(blinky), fish(tweety), \\ bird(blinky), bird(tweety), \\ flies(blinky), flies(tweety) \end{array} \right\}$$

Ground instantiation:

$$ground(P) = \left\{ \begin{array}{l} fish(blinky) \leftarrow \\ bird(tweety) \leftarrow \\ flies(blinky) \leftarrow bird(blinky) \\ flies(tweety) \leftarrow bird(tweety) \end{array} \right\}$$

Stable Models:

- $\{fish(blinky), bird(tweety), flies(tweety)\}$

3-b Herbrand Universe $\mathcal{T} = \{0, 1\}$
Herbrand Base:

$$\mathcal{A} = \left\{ \begin{array}{l} next(0, 0), next(0, 1), next(1, 0), next(1, 1) \\ even(0), even(1), odd(0), odd(1) \end{array} \right\}$$

Ground instantiation:

$$\text{ground}(P) = \left\{ \begin{array}{l} \text{next}(0, 1) \leftarrow \\ \text{next}(1, 0) \leftarrow \\ \text{even}(0) \leftarrow \\ \text{even}(0) \leftarrow \text{next}(0, 0), \text{odd}(0) \\ \text{even}(1) \leftarrow \text{next}(0, 1), \text{odd}(0) \\ \text{even}(0) \leftarrow \text{next}(1, 0), \text{odd}(1) \\ \text{even}(1) \leftarrow \text{next}(1, 1), \text{odd}(1) \\ \text{odd}(0) \leftarrow \text{next}(0, 0), \text{even}(0) \\ \text{odd}(1) \leftarrow \text{next}(0, 1), \text{even}(0) \\ \text{odd}(0) \leftarrow \text{next}(1, 0), \text{even}(1) \\ \text{odd}(1) \leftarrow \text{next}(1, 1), \text{even}(1) \end{array} \right\}$$

Stable Models:

- $\{\text{next}(0, 1), \text{next}(1, 0), \text{even}(0), \text{odd}(1)\}$

3-c Herbrand Universe $\mathcal{T} = \{\text{alive}, \text{bob}, \text{eve}\}$

Herbrand Base:

$$\mathcal{A} = \left\{ \begin{array}{l} \text{friend}(\text{alice}, \text{alice}), \text{friend}(\text{alice}, \text{bob}), \text{friend}(\text{alice}, \text{eve}), \\ \text{friend}(\text{bob}, \text{alice}), \text{friend}(\text{bob}, \text{bob}), \text{friend}(\text{bob}, \text{eve}), \\ \text{friend}(\text{eve}, \text{alice}), \text{friend}(\text{eve}, \text{bob}), \text{friend}(\text{eve}, \text{eve}), \\ \text{invite}(\text{alice}), \text{invite}(\text{bob}), \text{invite}(\text{eve}) \end{array} \right\}$$

Ground instantiation:

$$\text{ground}(P) = \left\{ \begin{array}{l} \text{friend}(\text{alice}, \text{bob}) \leftarrow \\ \text{friend}(\text{bob}, \text{alice}) \leftarrow \\ \text{friend}(\text{eve}, \text{alice}) \leftarrow \\ \text{invite}(\text{alice}) \leftarrow \\ \text{invite}(\text{alice}) \leftarrow \text{invite}(\text{alice}), \text{friend}(\text{alice}, \text{alice}) \\ \text{invite}(\text{bob}) \leftarrow \text{invite}(\text{alice}), \text{friend}(\text{alice}, \text{bob}) \\ \text{invite}(\text{eve}) \leftarrow \text{invite}(\text{alice}), \text{friend}(\text{alice}, \text{eve}) \\ \text{invite}(\text{alice}) \leftarrow \text{invite}(\text{bob}), \text{friend}(\text{bob}, \text{alice}) \\ \text{invite}(\text{bob}) \leftarrow \text{invite}(\text{bob}), \text{friend}(\text{bob}, \text{bob}) \\ \text{invite}(\text{eve}) \leftarrow \text{invite}(\text{bob}), \text{friend}(\text{bob}, \text{eve}) \\ \text{invite}(\text{alice}) \leftarrow \text{invite}(\text{eve}), \text{friend}(\text{eve}, \text{alice}) \\ \text{invite}(\text{bob}) \leftarrow \text{invite}(\text{eve}), \text{friend}(\text{eve}, \text{bob}) \\ \text{invite}(\text{eve}) \leftarrow \text{invite}(\text{eve}), \text{friend}(\text{eve}, \text{eve}) \end{array} \right\}$$

Stable Models:

- $\left\{ \begin{array}{l} \text{friend}(\text{alice}, \text{bob}), \text{friend}(\text{bob}, \text{alice}), \text{friend}(\text{eve}, \text{alice}), \\ \text{invite}(\text{alice}), \text{invite}(\text{bob}) \end{array} \right\}$

3-d Herbrand Universe $\mathcal{T} = \{0, 1, 2\}$

Herbrand Base:

$$\mathcal{A} = \left\{ \begin{array}{l} \text{next}(0, 0), \text{next}(0, 1), \text{next}(0, 2), \\ \text{next}(1, 0), \text{next}(1, 1), \text{next}(1, 2), \\ \text{next}(2, 0), \text{next}(2, 1), \text{next}(2, 2), \\ \text{before}(0), \text{before}(1), \text{before}(2), \\ \text{between}(0), \text{between}(1), \text{between}(2) \end{array} \right\}$$

Ground instantiation:

$$ground(P) = \left\{ \begin{array}{l} next(0, 1) \leftarrow \\ next(1, 2) \leftarrow \\ before(0) \leftarrow next(0, 0) \\ before(0) \leftarrow next(0, 1) \\ before(0) \leftarrow next(0, 2) \\ before(1) \leftarrow next(1, 0) \\ before(1) \leftarrow next(1, 1) \\ before(1) \leftarrow next(1, 2) \\ before(2) \leftarrow next(2, 0) \\ before(2) \leftarrow next(2, 1) \\ before(2) \leftarrow next(2, 2) \\ between(0) \leftarrow next(0, 0), before(0) \\ between(1) \leftarrow next(0, 1), before(1) \\ between(2) \leftarrow next(0, 2), before(2) \\ between(0) \leftarrow next(1, 0), before(0) \\ between(1) \leftarrow next(1, 1), before(1) \\ between(2) \leftarrow next(1, 2), before(2) \\ between(0) \leftarrow next(2, 0), before(0) \\ between(1) \leftarrow next(2, 1), before(1) \\ between(2) \leftarrow next(2, 2), before(2) \end{array} \right\}$$

Stable Models:

- $\{next(0, 1), next(1, 2), before(0), before(1), between(1)\}$

Solution 4

$$4-a \quad ground(P) = \left\{ \begin{array}{l} sparrow(jack) \leftarrow \\ penguin(tweety) \leftarrow \\ bird(jack) \leftarrow sparrow(jack) \\ bird(tweety) \leftarrow sparrow(tweety) \\ bird(jack) \leftarrow penguin(jack) \\ bird(tweety) \leftarrow penguin(tweety) \\ flies(jack) \leftarrow bird(jack), \neg penguin(jack) \\ flies(tweety) \leftarrow bird(tweety), \neg penguin(tweety) \end{array} \right\}$$

Stable Models:

- $\{sparrow(jack), penguin(tweety), bird(jack), bird(tweety), flies(jack)\}$

$$4-b \quad ground(P) = \left\{ \begin{array}{l} next(0, 1) \leftarrow \\ next(1, 0) \leftarrow \\ even(0) \leftarrow \neg odd(0) \\ even(1) \leftarrow \neg odd(1) \\ odd(0) \leftarrow next(0, 0), even(0) \\ odd(1) \leftarrow next(0, 1), even(0) \\ odd(0) \leftarrow next(1, 0), even(1) \\ odd(1) \leftarrow next(1, 1), even(1) \end{array} \right\}$$

Stable Models:

- $\{next(0, 1), next(1, 0), even(0), odd(1)\}$
- $\{next(0, 1), next(1, 0), even(1), odd(0)\}$

$$4-c \quad ground(P) = \left\{ \begin{array}{l} next(0, 1) \leftarrow \\ next(1, 2) \leftarrow \\ next(2, 0) \leftarrow \\ select(0) \leftarrow next(0, 0), \neg select(0) \\ select(0) \leftarrow next(0, 1), \neg select(1) \\ select(0) \leftarrow next(0, 2), \neg select(2) \\ select(1) \leftarrow next(1, 0), \neg select(0) \\ select(1) \leftarrow next(1, 1), \neg select(1) \\ select(1) \leftarrow next(1, 2), \neg select(2) \\ select(2) \leftarrow next(2, 0), \neg select(0) \\ select(2) \leftarrow next(2, 1), \neg select(1) \\ select(2) \leftarrow next(2, 2), \neg select(2) \end{array} \right\}$$

Stable Models: None

$$4-d \quad \text{ground}(P) = \left\{ \begin{array}{l} \text{friend}(\text{alice}, \text{bob}) \leftarrow \\ \text{friend}(\text{bob}, \text{alice}) \leftarrow \\ \text{friend}(\text{eve}, \text{alice}) \leftarrow \\ \text{refuse}(\text{alice}) \leftarrow \neg \text{invite}(\text{alice}) \\ \text{refuse}(\text{bob}) \leftarrow \neg \text{invite}(\text{bob}) \\ \text{refuse}(\text{eve}) \leftarrow \neg \text{invite}(\text{eve}) \\ \text{invite}(\text{alice}) \leftarrow \neg \text{refuse}(\text{alice}) \\ \text{invite}(\text{bob}) \leftarrow \neg \text{refuse}(\text{bob}) \\ \text{invite}(\text{eve}) \leftarrow \neg \text{refuse}(\text{eve}) \\ \text{invite}(\text{alice}) \leftarrow \text{invite}(\text{alice}), \text{friend}(\text{alice}, \text{alice}) \\ \text{invite}(\text{bob}) \leftarrow \text{invite}(\text{alice}), \text{friend}(\text{alice}, \text{bob}) \\ \text{invite}(\text{eve}) \leftarrow \text{invite}(\text{alice}), \text{friend}(\text{alice}, \text{eve}) \\ \text{invite}(\text{alice}) \leftarrow \text{invite}(\text{bob}), \text{friend}(\text{bob}, \text{alice}) \\ \text{invite}(\text{bob}) \leftarrow \text{invite}(\text{bob}), \text{friend}(\text{bob}, \text{bob}) \\ \text{invite}(\text{eve}) \leftarrow \text{invite}(\text{bob}), \text{friend}(\text{bob}, \text{eve}) \\ \text{invite}(\text{alice}) \leftarrow \text{invite}(\text{eve}), \text{friend}(\text{eve}, \text{alice}) \\ \text{invite}(\text{bob}) \leftarrow \text{invite}(\text{eve}), \text{friend}(\text{eve}, \text{bob}) \\ \text{invite}(\text{eve}) \leftarrow \text{invite}(\text{eve}), \text{friend}(\text{eve}, \text{eve}) \end{array} \right\}$$

Stable Models:

- $\left\{ \text{friend}(\text{alice}, \text{bob}), \text{friend}(\text{bob}, \text{alice}), \text{friend}(\text{eve}, \text{alice}), \right. \\ \left. \text{refuse}(\text{alice}), \text{refuse}(\text{bob}), \text{refuse}(\text{eve}) \right\}$
- $\left\{ \text{friend}(\text{alice}, \text{bob}), \text{friend}(\text{bob}, \text{alice}), \text{friend}(\text{eve}, \text{alice}), \right. \\ \left. \text{invite}(\text{alice}), \text{invite}(\text{bob}), \text{refuse}(\text{eve}) \right\}$
- $\left\{ \text{friend}(\text{alice}, \text{bob}), \text{friend}(\text{bob}, \text{alice}), \text{friend}(\text{eve}, \text{alice}), \right. \\ \left. \text{invite}(\text{alice}), \text{invite}(\text{bob}), \text{invite}(\text{eve}) \right\}$

Solution 5

5-a The following rules are not safe:

$$\begin{array}{l} \text{animal}(X) \leftarrow \\ \text{flies}(X) \leftarrow \neg \text{penguin}(X) \end{array}$$

5-b The following rules are not safe:

$$\begin{array}{l} \text{greater_equal}(1, X) \leftarrow \\ \text{even}(X) \leftarrow \neg \text{odd}(X) \end{array}$$

5-c The following rule is not safe:

$$\text{select}(X) \leftarrow \neg \text{next}(X, Y), \neg \text{select}(Y)$$

5-d The following rules are not safe:

$$\begin{array}{l} \text{friend}(\text{eve}, X) \leftarrow \\ \text{refuse}(X) \leftarrow \neg \text{invite}(X) \\ \text{invite}(X) \leftarrow \neg \text{refuse}(X) \\ \text{invite}(Y) \leftarrow \text{invite}(X), \neg \text{friend}(X, Y) \end{array}$$