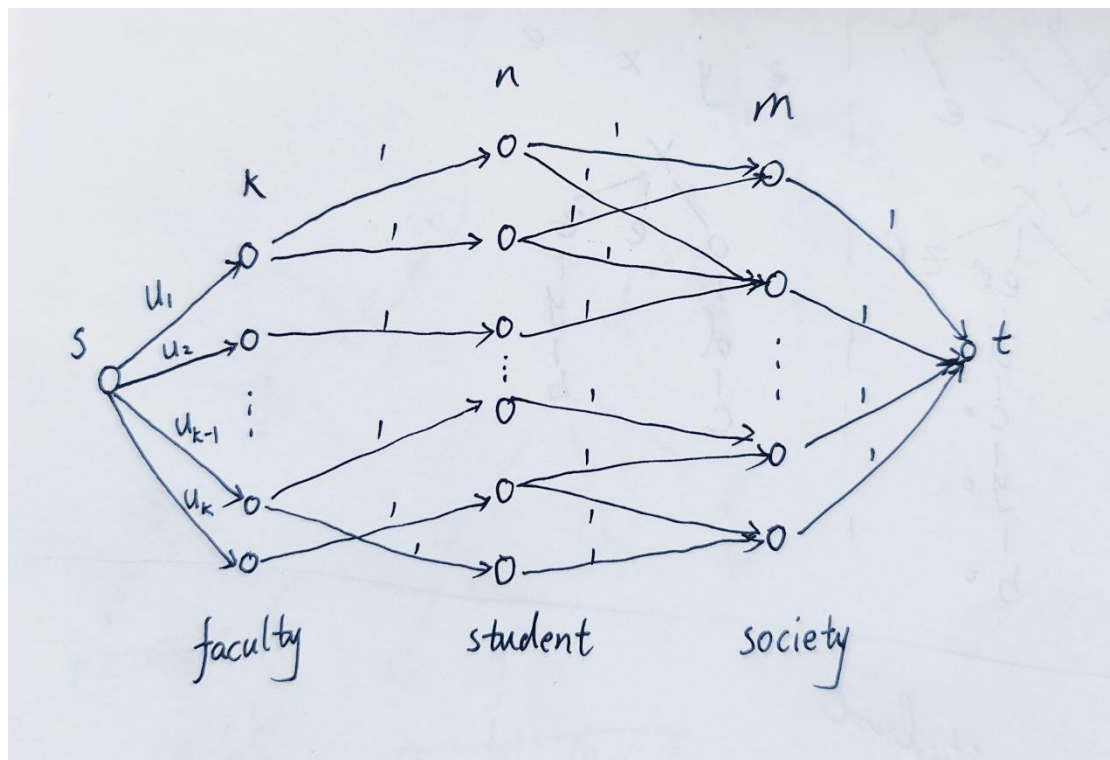


**Qiyao Zhou**

**Z5379852**

## **Question 1**

We begin by constructing a flow network using the input data. The network is showed in the diagram below:



- source  $s$  and sink  $t$ ,
- The combinations of vertices from left to right represent faculty, students and societies in that order,
- connect  $s$  to each faculty vertex( $i$ ) with capacity equal to  $u_i$ ,
- The student vertices are connected to the corresponding faculties and societies according to the input, with a capacity of 1 for all connections,
- connect  $s$  to each society vertex with capacity equal to 1.

From this flow network construction, we run Ford-Fulkerson to find the

maximum flow. If the maximum flow is less than  $m$ , then we output “no solution”. Otherwise, a selection is possible. We can deduce a selection of students by examining which of the student vertices are in the max flow. If student vertex  $i$  is in the max flow, then the student  $i$  is selected to attend the event.

The time complexity is  $O(|V||F|)$  where  $V = k + m + n + 2$  and  $F \leq 3m + k \leq 3m + n$ , so the algorithm runs in  $O(nm)$ .