COMP9414: Artificial Intelligence Tutorial 4: Propositional Logic

1. Translate the following sentences into Propositional Logic.

- (i) If Jane and John are not in town we will play tennis [do both of them have to be away?]
- (ii) It will either rain today or it will be dry today [is "dry" the same as "not raining"?]
- (iii) You will not pass this course unless you study [this means "if you do not study"]

To do the translation

- (a) Identify a scheme of abbreviation for basic sentences
- (b) Identify logical connectives between variables

2. Convert the following formulae into Conjunctive Normal Form (CNF).

(i)
$$P \to Q$$

(ii)
$$(P \to \neg Q) \to R$$

(iii)
$$\neg (P \land \neg Q) \rightarrow (\neg R \lor \neg Q)$$

3. Show using the truth table method that the corresponding inferences are valid.

(i)
$$P \to Q, \neg Q \models \neg P$$

(ii)
$$P \to Q \models \neg Q \to \neg P$$

(iii)
$$P \to Q, Q \to R \models P \to R$$

Check your answers using the Python program tableau_prover.py.

4. Repeat Question 3 using resolution. In this case, show

(i)
$$P \to Q, \neg Q \vdash \neg P$$

(ii)
$$P \to Q \vdash \neg Q \to \neg P$$

(iii)
$$P \to Q, Q \to R \vdash P \to R$$

5. Determine whether the following sentences are valid (i.e. tautologies) using truth tables.

(i)
$$((P \lor Q) \land \neg P) \to Q$$

(ii)
$$((P \to Q) \land \neg (P \to R)) \to (P \to Q)$$

(iii)
$$\neg(\neg P \land P) \land P$$

(iv)
$$(P \lor Q) \to \neg(\neg P \land \neg Q)$$

Check your answers using the Python program tableau_prover.py.

6. Repeat Question 5 using resolution. In this case, try to show

(i)
$$\vdash ((P \lor Q) \land \neg P) \to Q$$

(ii)
$$\vdash ((P \rightarrow Q) \land \neg (P \rightarrow R)) \rightarrow (P \rightarrow Q)$$

(iii)
$$\vdash \neg(\neg P \land P) \land P$$

(iv)
$$\vdash (P \lor Q) \to \neg(\neg P \land \neg Q)$$