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Optimal Non-uniform Deployments in Ultra-Dense Finite-Area Cellular Networks

Pete Pratt¹, Carl P. Dettmann¹, and Orestis Georgiou²

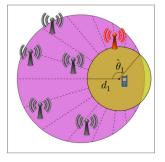
¹School of Mathematics, University of Bristol, University Walk, Bristol, BS8 1TW, UK ²Toshiba Telecommunications Research Laboratory, 32 Queens Square, Bristol, BS1 4ND, UK

Abstract—Network densification and heterogenisation through the deployment of small cellular access points (picocells and femtocells) are seen as key mechanisms in handling the exponential increase in cellular data traffic. Modelling such networks by leveraging tools from Stochastic Geometry has proven particularly useful in understanding the fundamental limits imposed on network coverage and capacity by co-channel interference. Most of these works however assume infinite sized and uniformly distributed networks on the Euclidean plane. In contrast, we study finite sized non-uniformly distributed networks, and find the optimal non-uniform distribution of access points which maximises network coverage for a given non-uniform distribution of mobile users, and vice versa.

I. Introduction

The rapid growth in cellular data traffic presents unprecedented strain on current cellular infrastructures. One technology that can alleviate this is extreme network densification of cellular access points (APs) and also the heterogenisation of the conventional macrocell architecture with smaller picocells and femtocells. Through the efficient exploitation of spatial frequency reuse, such dense heterogeneous cellular networks (HetNets) are expected to deliver higher data rates as well as the ubiquitous wireless coverage needed in this internet age. Therefore, network performance under spatial densification is an area of active academic and industrial research and standardisation with the view that the deployment of a multitier architecture can help facilitate the transition into 5G [1].

The modelling and analysis of HetNets has been greatly facilitated by the development of Stochastic Geometry tools [2], and through the establishment of meaningful performance metrics such as capacity, throughput, spectral efficiency, and coverage [3], [4]. The main outcome of these research efforts has been the unveiling of engineering insights and a tractable framework for tackling network optimisation, e.g., designing Coordinated Multipoint (CoMP) transmission schemes [5]. As this research area matures however, some insights have been revisited and new complexities uncovered. For instance, the celebrated result of [6] that coverage does not depend on network density when thermal noise is negligible has been overturned (by the same author) when considering multi-slope path loss models [7]. A similar result was obtained by [8] who studied the impact of AP density in finite-area networks. It is therefore desirable to understand how Access Points (AP) should be deployed in order to maximise Mobile User (MU) coverage; to this end, and motivated by the aforementioned findings in [5]–[8], we revisit the coverage problem in dense, finite area, cellular networks and analyse the optimal deployment of APs for a non-uniform distribution of MU.



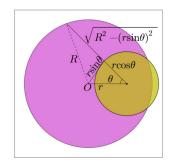


Fig. 1. Left: Simplified schematic of the system set up. A MU is located at r, and is served by its nearest AP (the red one) which is located a distance d_1 away. Other APs are randomly distributed in the finite deployment region $\mathcal V$ according to a non-uniform density $\lambda(t)$, and act as sources of interference. Right: A schematic for the shift in coordinate system used to calculate (7).

We model the AP locations using a non-uniform Poisson Point Process (PPP) in a circular deployment region, and, assuming a closest AP user association model (as usually done when modelling cellular networks [6]), and derive novel analytic expressions for the probability density function (pdf) of the nearest neighbour distribution (NND). By leveraging tools from stochastic geometry, and assuming Rayleigh fading, we calculate the position dependent interference field and outage probability, and use the NND to calculate a position dependent coverage probability, i.e., the probability that a mobile user (MU) located at $r \in \mathcal{V}$ can achieve a Signal-to-Interference-plus-Noise-Ratio (SINR) in the downlink greater than a threshold q. Finally, we optimise the average coverage probability with respect to non-uniform AP and MU spatial distributions. The main contributions of this letter are:

- we analyse network coverage in a finite domain with nonuniform AP deployment for the first time, and highlight how border effects improve network coverage for convex AP deployments whilst the converse is true for the concave case.
- we study the optimal AP deployment in finite regions which maximizes network coverage and show that for non-uniform MU spatial distributions the optimal AP deployment is non-trivial.

These results provide insight into how AP should be deployed or operated by highlighting the impact of non-uniform MU distributions, along with border and interference effects. Note that even though we discuss a simplified non-uniform AP/MU distribution within a circular domain, our analysis provides

insight for more complex AP/MU distributions and domains. We proceed by formally defining the system model, along with the NND and the connection model used in our main analysis in Section III.

II. SYSTEM MODEL

A. Network Model

We consider a non-uniform PPP of density $\lambda(t) = (t,\phi)$ in a circular disk $\mathcal{V} \subset \mathbb{R}^2$ of area $|\mathcal{V}| = \pi R^2$ and zero intensity elsewhere. Each point in our process corresponds to a cellular AP, transmitting at constant power \mathcal{P} . For simplicity we restrict the analysis to quadratic radially symmetric AP distributions in polar coordinates such that the intensity function is

$$\lambda(t) = \lambda_0 \left(a + bt^2 \right), \quad 0 \le t \le R \tag{1}$$

where t is the radial distance, $\lambda_0 > 0$, $a = 1 - bR^2/2$ and $b \in [-2/R^2, 2/R^2]$, such that there are, on average, $2\pi \int_0^R \lambda(t)t dt = \lambda_0 |\mathcal{V}|$ APs in \mathcal{V} . More specifically, the parameter b in (1) controls how the AP are deployed within \mathcal{V} , and allows us to interpolate between three different AP deployment distributions, in particular: uniform (b = 0), convex (b > 0 nodes located predominately near the border), and concave (b < 0 nodes located near the centre of the deployment region). Note that the concave distribution is akin to the Random Waypoint Mobility model¹ (RWPM) [9]–[11] which models mobile ad hoc networks. Note that by independently thinning a uniform PPP, one can easily obtain a non-uniform random access transmission scheme. The corresponding intensity would be $\lambda(t) \to \lambda_0 p(t)$ where $p \in [0, 1]$ is a position dependent thinning probability [2].

Let the Euclidean distance from a receiving MU located at $r = (r, \theta) \in \mathcal{V}$ and its distance to every other AP i located at $t_i \in \mathcal{V}$ in the PPP be denoted by $d_i = |r - t_i|$, where we order the distances as $0 \le d_1 \le d_2 \le \dots$ The assumption that a MU is served by its nearest AP is fairly intuitive since it is likely that the AP with the strongest signal will typically be the closest AP [6] (see Fig. 1).

B. Nearest Neighbour distribution

In our model where a MU connects to its nearest AP, the pdf of this NND $f(r, d_1)$ is given by the derivative of the contact distribution, or equivalently, minus the derivative of the void probability:

$$f(\mathbf{r}, d_1) = -\frac{\mathrm{d}}{\mathrm{d}d_1} \mathbb{P}\left[N(B(\mathbf{r}, d_1)) = 0\right]$$
 (2)

Intuitively, the pdf of the NND in (2) tells us the probability that the nearest AP will be a distance d_1 from a receiver located at r. Assuming the AP are distributed according to (1), the pdf of the NND in (2) becomes the radially symmetric and piecewise continuous function:

$$f(r,d_1) = \begin{cases} f_1(r,d_1) & \text{if } r \le R - d_1\\ f_2(r,d_1) & \text{if } r > R - d_1 \end{cases}$$
 (3)

 $^1\mathrm{In}$ the RWPM nodes are initially placed in $\mathcal V$ according to some point process, where they then independently travel from waypoint to waypoint in a sequential manner. A node selects its next waypoint from a uniform distribution in $\mathcal V$, travels toward it in a straight line at a constant speed chosen at random and pauses with a certain probability, and then repeats the process. This model gives rise to a stationary distribution with a higher density of nodes in the bulk of the domain due to the continual crossing of paths. The parameter $b=-2/R^2$ in (1) gives the RWPM in a disk with no pause time.

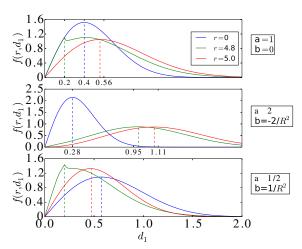


Fig. 2. Plot of the nearest neighbour pdf (3) for MUs at different off-centre distances $r \in [0, R]$ for different AP deployments: Uniform(top panel), Concave (middle), and Convex (bottom). We assume that R = 5.

$$f_{1}(r,d_{1}) = 2\pi d_{1}\lambda_{0} \left(a + b(d_{1}^{2} + r^{2})\right) e^{-\lambda_{0}\pi d_{1}^{2} \left(a + b\frac{d_{1}^{2} + 2r^{2}}{2}\right)}$$
(4)

$$f_{2}(r,d_{1}) = -\frac{d}{dd_{1}} \exp\left[-2\lambda_{0} \left\{a\tilde{r}\sqrt{d_{1}^{2} - \tilde{r}^{2}}\right\} + d_{1}^{2} \left(\arctan\left[\frac{\tilde{r}}{\sqrt{d_{1}^{2} - \tilde{r}^{2}}}\right] + \frac{\pi}{2}\right) \left(a + \frac{b(d_{1}^{2} + 2r^{2})}{2}\right) + \frac{b\tilde{r}}{12\sqrt{d_{1}^{2} - \tilde{r}^{2}}} \left(5d_{1}^{4} - 7d_{1}^{2}\tilde{r}^{2} + 2\tilde{r}^{4}\right) - \frac{b\sqrt{d_{1}^{2} - \tilde{r}^{2}}}{12} \left(d_{1}^{2}(13r + 3\hat{r}) + 2(r^{2} + r^{2}\hat{r} + r\hat{r}^{2} - 3\hat{r}^{3})\right) + R^{2}\left(a + \frac{bR^{2}}{2}\right) \left(\frac{\pi}{2} + \arctan\left[\frac{\hat{r}}{\sqrt{R^{2} - \hat{r}^{2}}}\right]\right) - \hat{r}\sqrt{R^{2} - \hat{r}^{2}} \left(a + \frac{b}{6}(R^{2} + 2\hat{r}^{2})\right)\right\}\right]$$
(5)

where we defined $\hat{r}=\frac{R^2+r^2-d_1^2}{2r}$ and $\tilde{r}=\hat{r}-r$. Fig. 2 highlights the piecewise nature of $f(r,d_1)$, for

Fig. 2 highlights the piecewise nature of $f(r,d_1)$, for the uniform (top panel), concave (middle panel) and convex (bottom panel) cases. If the receiver is off centre, as the ball of radius d_1 grows, it will eventually intersect the boundary of the domain giving rise to this piecewise nature. This has a direct effect on the mean separation distance to the serving AP, given by $\mathbb{E}[d_1] = \int_0^{d_{\max}} f(r,d_1)d_1dd_1$ which clearly depends on r and b. For uniform deployments, $\mathbb{E}[d_1]$ is smaller for a MU located near the centre $(r \approx 0)$, and bigger near the border $(r \approx R)$. This border effect is amplified in the concave case, and reversed in the convex AP deployment density.

C. Connection Model

The signal power received by a MU in the far field is inversely proportional to the separation distance x between source and destination. We adopt the following well-established pathloss attenuation function $g(x) = x^{-\eta}$, where $\eta \geq 2$ is the pathloss exponent. For free space $\eta = 2$ so the signal strength obeys exactly the inverse square law, and decays faster for more cluttered environments; $\eta = 4$ is typically taken for urban areas. In addition to pathloss attenuation, small-scale fading can affect the received signal power. We model this by a Rayleigh fading channel, such that the gain between

a transmitting AP i and the receiving MU is an independent random variable with a standard exponential distribution $|h_i|^2 \sim \exp(1)$, for $i=1,2,\ldots$ We therefore formulate the received SINR at the MU located at r in the downlink as SINR = $\frac{\mathcal{P}|h_1|^2g(d_1)}{\mathcal{N}+\mathcal{I}}$ where $\mathcal{I}=\mathcal{P}\sum_{k\geq 2}g(d_k)|h_k|^2$ is the aggregate interference from all other transmitters, \mathcal{P} is the transmit power (assumed the same for all AP), and \mathcal{N} is the average thermal noise power. For the sake of simplicity, we consider the quality of the received signal to be completely characterised by the SINR.

We assume that a MU can connect to its nearest AP if the SINR at the MU is greater than a threshold q, else it is said to be in outage. The connection probability is thus given by, $H_1(\mathbf{r}, d_1) = \mathbb{P}[\text{SINR} \ge q]$.

Conditioning on the interference we have that the connection probability is given by

$$H_{1}(\mathbf{r}, d_{1}) = \mathbb{E}_{\mathcal{I}} \Big[\mathbb{P} \Big[|h_{1}|^{2} \ge \frac{q(\mathcal{N} + \mathcal{I})}{g(d_{1})\mathcal{P}} \Big| \mathbf{r}, d_{1}, \mathcal{I} \Big] \Big]$$

$$= \exp \Big[-\frac{q\mathcal{N}}{\mathcal{P}g(d_{1})} \Big] \mathcal{L}_{\mathcal{I}}(q d_{1}^{\eta})$$
(6)

where $\mathcal{L}_{\mathcal{I}}(s)$ is the Laplace transform of the random variable \mathcal{I} . Assuming that $|h_k|^2 \sim \exp(1)$ and evoking the probability generating function for a PPP [2] we can express this as

$$\mathcal{L}_{\mathcal{I}}(q \, d_1^{\eta}) = \exp\left[-\int_{\mathcal{V}\setminus B(r, d_1)} \frac{\lambda(z)}{1 + \frac{d_k^{\eta}}{q \, d_1^{\eta}}} d_k \mathbf{d} d_k \mathbf{d} \theta\right] \tag{7}$$

where $z = \sqrt{r^2 + d_k^2 - 2rd_k \cos \theta}$. Notice that the integral is computed over the whole domain \mathcal{V} but excluding the ball $B(r, d_1)$, see Fig. 1. Moreover, the integral is over a non-uniform density $\lambda(z)$ where we have also used the cosine rule to shift the polar coordinate system from the centre of \mathcal{V} , to that centred on r. This shift in coordinates allows us to further simplify the Laplace functional and arrive at

$$\mathcal{L}_{\mathcal{I}}(q \, d_1^{\eta}) = \exp\left[-\lambda_0 \int_0^{\hat{\theta}_1} \phi(\hat{R}) - \phi(d_1) d\theta\right], \tag{8}$$

where, $\hat{\theta}_1 = \min\left[\arccos\left(\frac{r^2+d_1^2-R^2}{2rd_1}\right),\pi\right]$ is the angle of intersection shown in Fig. 1, $\hat{R}=r\cos\theta+\sqrt{R^2-r^2\sin^2\theta}$ is the radial distance from the MU to the domain border, and

$$\phi(x) = \frac{x^2}{6} \left[6(a + br^2) \,\psi(\frac{2}{\eta}, \frac{x^{\eta}}{q \, d_1^{\eta}}) + bx \left(3x \,\psi(\frac{4}{\eta}, \frac{x^{\eta}}{q \, d_1^{\eta}}) - 8r \cos\theta\psi(\frac{3}{\eta}, \frac{x^{\eta}}{q \, d_1^{\eta}}) \right) \right]$$
(9)

is the result after calculating the radial integral over d_k in (7), where we also have defined $\psi(x,y) = {}_2F_1\big(1,x,1+x,-y\big)$. Here ${}_2F_1$ is the Gauss hypergeometric function. Equation (8) can only be expressed in closed form for the special case of r=0, in which case we obtain

$$\mathcal{L}_{\mathcal{I}}(q \, d_1^{\eta}) = \exp\left[\frac{2d_1^2 q (2 + bd_1^2 - bR^2)}{4(1+q)} - 4R^2 \psi(\frac{2}{\eta}, \frac{R^{\eta}}{q \, d_1^{\eta}}) + bR^4 \psi(\frac{4}{\eta}, \frac{R^{\eta}}{q \, d_1^{\eta}})\right],\tag{10}$$

but can be computed numerically using standard libraries. Fig. 3 shows the calculation of (8) as a function of radial position of the MU r conditioning on different values of d_1 .

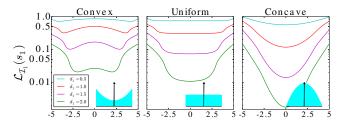


Fig. 3. The Laplace functional (8) plotted as a function of MU position r for all three cases with the distributions inset. Parameters used: $\eta=6$, $\mathcal{P}, q=1, \lambda_0=1$. Note: For $\eta<6$ we have a decrease in $\mathcal{L}_{\mathcal{I}_1}(q\, d_1^\eta)$.

Note how the interference is reduced, in all cases, when ris near the border. This is because the expected separation distance of the interfering APs $\mathbb{E}[d_k]$, k > 1, typically increases as a MU approaches the border, thus leading to a weaker interference field. This is purely a geometrical effect. Intuitively, when r=0 all interferers are located at distances $d_k \in [d_1, R]$. In contrast, when r = R all interferers are located at distances $d_k \in [d_1, 2R]$. Again, a non-uniform density of APs can amplify or counter this effect. Further, for areas of low density (e.g near the centre for the convex case), the interference field is also reduced. By increasing d_1 , $\mathcal{L}_{\mathcal{I}_1}(q d_1^{\eta})$ decreases, (interference increases); a consequence of $\frac{d_k}{d_1}$ (integrand of (7)) decaying to one. In other words, conditioning on the AP being further away the ratio $\mathbb{E}[\frac{d_k}{d_1}] \to 1$ which in turn will cause the average Signal-to-Interference-Ratio (SIR) \rightarrow 0. We proceed by using the aforementioned NND and connection model to analyse MU coverage and the optimal AP deployment.

III. OPTIMAL COVERAGE DEPLOYMENT

A. Mobile User Coverage

An important performance metric commonly used is the network coverage probability experienced by a MU given by,

$$C(\boldsymbol{r}, b, \lambda_0 \pi R^2) = \int_0^{d_{\text{max}}} H(\boldsymbol{r}, d_1) f(\boldsymbol{r}, d_1) dd_1$$
 (11)

where $H(\mathbf{r}, d_1)$ is the connection probability given in (9), $d_{\text{max}} = R + r$ is the maximum distance from the MU to the boundary, and $f(\mathbf{r}, d_1)$ is the pdf of the NND given in eq.(2).

More specifically, eq (11) tells us the probability that a MU at r can successfully decode a message from its nearest AP, and this probability depends on both the distribution of APs, $\lambda(t)$ controlled by b, and the location of the MU, see Fig 4. In fact, since the AP are deployed in a radially symmetric fashion, following eq (1), the coverage probability is also radially symmetric as a result.

B. Optimal Coverage Deployment

It is important to know how to deploy APs such that MU connectivity can be maximised. To this end, we introduce the average coverage probability for a radially symmetric non-uniform distribution of MUs given by $\rho(r) = 1 - \beta \frac{R^2}{2} + \beta r^2$, where β plays a similar role as b in (1) and $\int_{\mathcal{V}} \rho(r) r dr = |\mathcal{V}|$:

$$\bar{C}(b,\beta,\lambda_0\pi R^2) = \frac{2}{R^2} \int_0^R \rho(r)C(r,b,\lambda_0\pi R^2)r\mathrm{d}r \qquad (12)$$

Eq. (12) can be maximised to give the optimal value of b

$$b^*(\eta, \beta, \lambda_0 \pi R^2) = \arg\max_b \bar{C}(b, \beta, \lambda_0 \pi R^2), \quad (13)$$

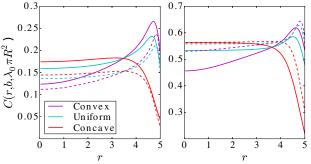


Fig. 4. The coverage probability, (11), as a function of position r from the centre to the boundary, with $\mathcal{P}=\mathcal{N}=q=1,\,R=5$ and $\eta=2,4$ for the left and right panel respectively. Solid line: $\lambda_0=1$; dashed line: $\lambda_0=5$.

conditioned on η , β and density of APs λ_0 in \mathcal{V} . Equation (13) is a maximization over a double integral of an exponential of another integral, and is therefore computationally taxing. The simplifications and analysis performed in the previous sections have alleviated this task to some extent.

C. Numerical Results

Fig 4 shows how the border effects result in a drop in coverage probability due to low $f(r,d_1)$, and the distance between the first and second nearest neighbour is likely to be much less compared with a MU located near the centre of $\mathcal V$. Similarly, away from the border, areas of high AP density mean that coverage decreases due to a higher interference field, regardless of the close proximity of the nearest neighbour. For the convex case we observe a "sweet spot" where the trade-off between the distribution of APs and border effects helps to maximise coverage probability.

Fig. 5 shows the optimal deployment of APs b^* as a function of the non-uniform MU distribution parameter β , for different values of η and λ_0 . Basically, these plots show that a convex spatial distribution of MUs (representing the demand of data in the downlink) should be met by a convex spatial distribution of active APs (representing the supply of data in the downlink). For a concave distribution of MUs in a finite domain however, the optimal AP distribution will depend on β , η , and λ_0 , and may vary from concave to convex. This is an interesting observation caused by the trade-off between interference and border effects, revealed for the first time in this paper. Note that the optimal distribution of APs in ultra-dense deployments, i.e., for $\lambda_0 \gg 1$, tends to be more uniform. A similar trend is observed for larger pathloss exponents $\eta \geq 2$. Finally, recall that a uniform deployment of APs can be made nonuniform via a non-uniform independent thinning process p(t)modelling a random access transmission scheme.

IV. CONCLUSION

In this letter we analyse network densification, a key aspect in providing the increased network performance promised by the fifth generation of wireless communications. Under a nearest neighbour association scheme we highlight the impact that the spatial distributions of APs and MUs have on network coverage in finite operating regions. Using tools from stochastic geometry, we investigate the trade-off in SINR and how this is affected by the position of MUs in a finite region, and also the spatial distribution of APs. Finally, we formulate an optimisation problem for the average network coverage by

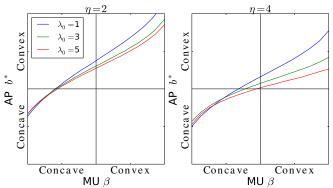


Fig. 5. The optimal distribution of AP given a deployment of MU for different λ_0 with R=5, and $\eta=2,4$ for the left and right panel respectively.

adapting the APs deployment method or transmission scheme according to the spatial distribution of MUs. An application where an adaptive transmission scheme could be used to achieve optimal MU coverage would be for cities where the MUs spatial distribution goes from concave during workhours, to convex at night-time. Collaborative AP transmission schemes where the k nearest APs collaborate in a maximum ratio transmission (MRT) or joint transmission scheme such as in CoMP could be studied in order to improve network performance.

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