

Affiliation Recommendation using Auxiliary Networks

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February 18, 2018

Abstract

Many social networks today, beside friendships, contain various groups and communities users associate with. Therefore, we can distinguish many co-existent structures within given network, such as user-to-user and user-to-group connections. The goal of this work is to calculate group affiliation recommendation for each user. Implications of those calculations span beyond social networks and can be applied to a wide range of problems.

I. INTRODUCTION

Predicting the future state of social networks has become a major occupation of scientists in recent years, thus data science as a discipline is growing more rapidly each day. Furthermore, there is a lot of interest in affiliation recommendation in today's over more competitive market. Nonetheless, approaches mentioned in this paper can even be extended to a variety of non-social problems such as the problem of identifying genes affecting certain traits from observed genes-to-genes and genes-to-traits connections.

Our network. Today's social networks have a lot of restrictions on their public API as well as strict laws against content crawling, so we decided to build our own social network of virtual users and groups. It is composed of users and groups, each having their capabilities which will be briefly described here and can, together with models calculations, be closely observed in our GitHub repository. Our network is created in distinct steps; groups creation, users creation, groups initial population, users be-friending. Last step is the most interesting one. User adds number of friends from list of all friends dependant on its popularity. There exist 1% of "super-popular" users who

are at least 2 times more popular than regular users. Friendship is symmetrical, that is, when an user adds new friend, this friend also adds him. This can easily be changed to be non-symmetrical. Users, except their initial group memberships also decide to join groups which their friends are members of and they do that 25% of the time.

Method described above yields a very good and "real-structured" social-network from which existant user connections and group affiliations are easily extracted in the form of later mentioned matrices A and S .

II. MODELS

In this section, we will establish the notation used in models that follow.

Notation. Let the N_u be the number of users and N_g be the number of groups. We define matrix $A \in \mathbb{R}^{N_u \times N_g}$ which denotes user \times group matrix or adjacency matrix of affiliation network and matrix $S \in \mathbb{R}^{N_u \times N_u}$ which denotes user \times user matrix or adjacency matrix of friendship.

The task is to recommend affiliations to a given user, we tackled all the users simultaneously. The problem can be posed as a

problem of ranking affiliations in order of the users interest in joining them. Methods that will be introduced later solve the problem by assigning scores to various affiliations in order to rank them.

Consider the adjacency matrices A and S . We assume S is symmetric, if user i is friend to user j then user j is friend to user i . Matrix S corresponds to undirected graph among users and $\begin{bmatrix} 0 & A \\ A^T & 0 \end{bmatrix}$ corresponds to undirected bipartite graph between users and groups. We will also define a graph C between all users and groups, with the combined adjacency matrix $C = \begin{bmatrix} \lambda S & A \\ A^T & 0 \end{bmatrix}$. Parametar λ controls the ratio of the weight of friendship to the weight of group membership. If $\lambda = 0$ we have bipartite affiliations graph.

Models we are introducing are Graph proximity model and Latent factors model to calculate score matrices.

i. Graph proximity model

We start by assuming that the graph is known and the prediction of new links between nodes is going to be examined by calculating proximity. As we mentioned, the affiliation network can be modeled by a graph, so the basic idea is that there is possible link between two nodes based on the proximity between them. Proximity can be calculated as sum of number of paths that connect them, paths of different lengths. We are going to use Katz measure for calculating proximity. Katz measure is used to measure the relative degree of influence of a node in a network.

$$Katz(S; \beta) = \sum_{n=1}^{\infty} \beta^n S^n = \beta S + \beta^2 S^2 + \beta^3 S^3 + \dots$$

We extend the Katz measure to the bipartite graph A

$$Katz(A; \beta) = \beta A A^T A + \beta^2 (A A^T)^2 A + \dots$$

where in the co-occurrence matrix $A A^T$, two users i and j are considered connected if i

and j belong to at least one same group, i.e. $(A A^T)_{i,j} > 0$. We consider paths from user i to user j by $A A^T$, and then user j to some other user k by $A A^T$ and then user k to some group by A . Idea is that if user i shares some community with j it is more likely i will join some community j belongs to.

We will now expand Katz measure on the combined graph C

$$Katz(C; \beta) = \beta C + \beta^2 C^2 + \dots$$

$$Katz(C; \beta) = \beta A + \beta^2 \lambda S A + \beta^3 (\lambda^2 S^2 A + A A^T A) + \dots$$

This Katz measure generalizes the normal Katz measure by also considering some paths from user i to user j by matrix S , then user j to some group by matrix A . And also user i to user j by S , user j to user k by $A A^T$ then again user k to user j by A and finally user j to some group by A . The matrix given by $Katz(C; \beta)$ can be used as score matrix. In case of higher dimension of matrices you work with, truncated Katz is preferred, but for our problems we stick to normal Katz because matrices for testing are not high dimensional.

We will just roughly discuss which β and λ we should take. In our algorithms β is calculated as reciprocal of the maximum absolute value of eigenvalues of matrix A . Usually we take $\lambda = 0.2$ but the point of that parametar is to factor the significance of user to user matrix and the connections between users itself.

ii. Latent factors model

III. DISCUSSION

i. Results

REFERENCES

[Figueredo and Wolf, 2009] Figueredo, A. J. and Wolf, P. S. A. (2009). Assortative pairing and life history strategy - a cross-cultural study. *Human Nature*, 20:317–330.