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# Parallel Programming

## Data-Parallel Programming with CUDA

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<http://www.cs.nctu.edu.tw/~ypyou/>



# Acknowledgement

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- This set of slides is adapted from lectures by
  - ✿ Prof. Wen-mei Hwu (University of Illinois, Urbana-Champaign) and Dr. David Kirk (NVIDIA)
  - ✿ Dr. Erich Elsen (Consulting Assistant Professor at Stanford University)
  - ✿ Prof. Patrick Cozzi (University of Pennsylvania)
  - ✿ Prof. Henk Corporaal and Dr. Bart Mesman (Technische Universiteit Eindhoven)



# Outline

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- GPUs as Compute Engines
- GPU Architectures
  - ✿ GPU Threading Model
  - ✿ Separation of Memory Spaces
- Introduction to CUDA
  - ✿ Parallel Computing Platform
  - ✿ Programming Model
    - ◆ Built-in Data Types and Functions
    - ◆ Thread Model
    - ◆ Memory Model
  - ✿ Case Study: Matrix Multiplication
  - ✿ Thread Synchronization
  - ✿ Advanced Features



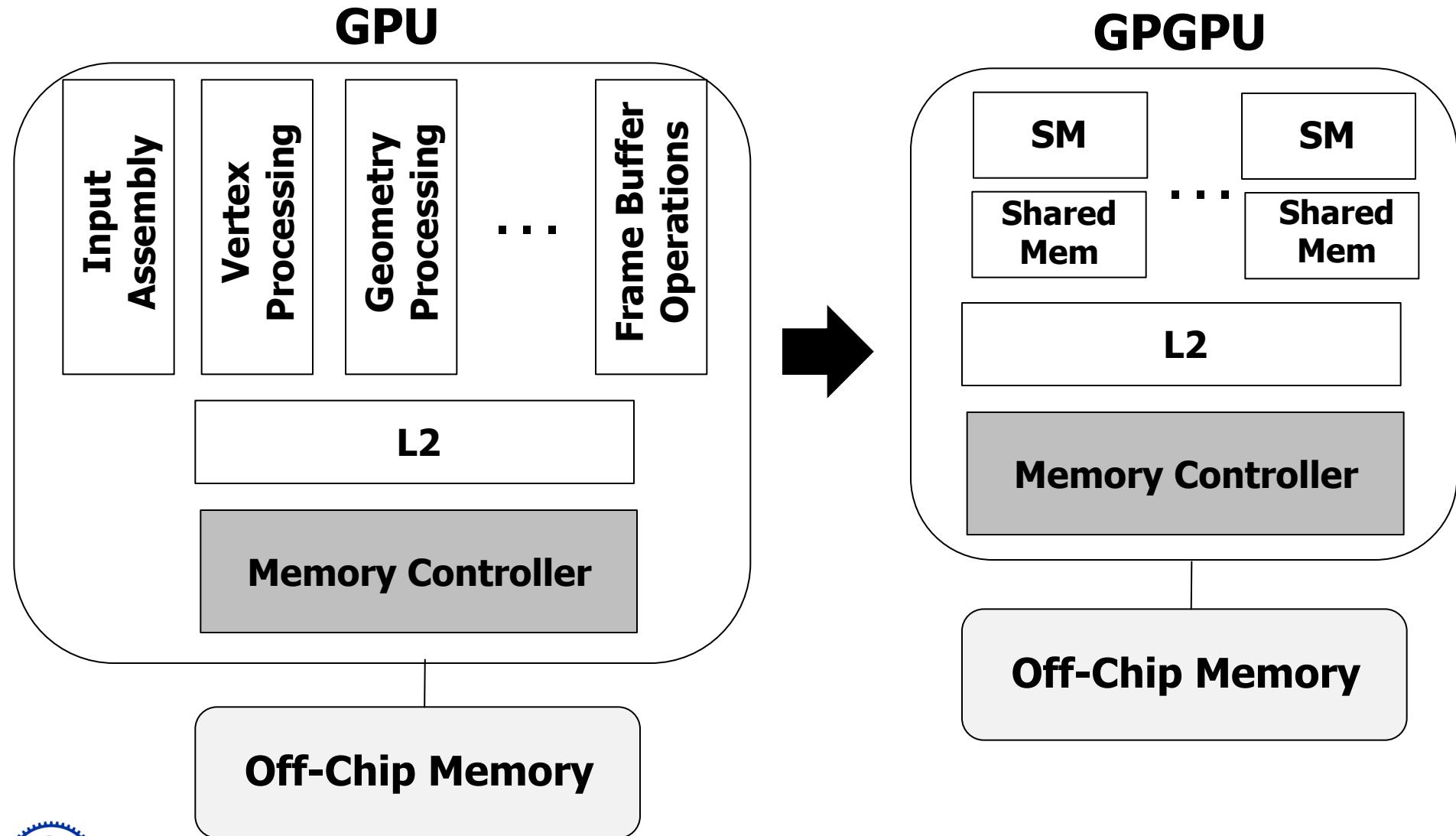
# GPU Computing History

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- 2001/2002 - researchers see GPU as data-parallel coprocessor
  - ✿ The **GPGPU** field is born
- 2007 - NVIDIA releases CUDA
  - ✿ **CUDA** - Compute Uniform Device Architecture
  - ✿ GPGPU shifts to **GPU Computing**
- 2008 - Khronos releases **OpenCL** specification

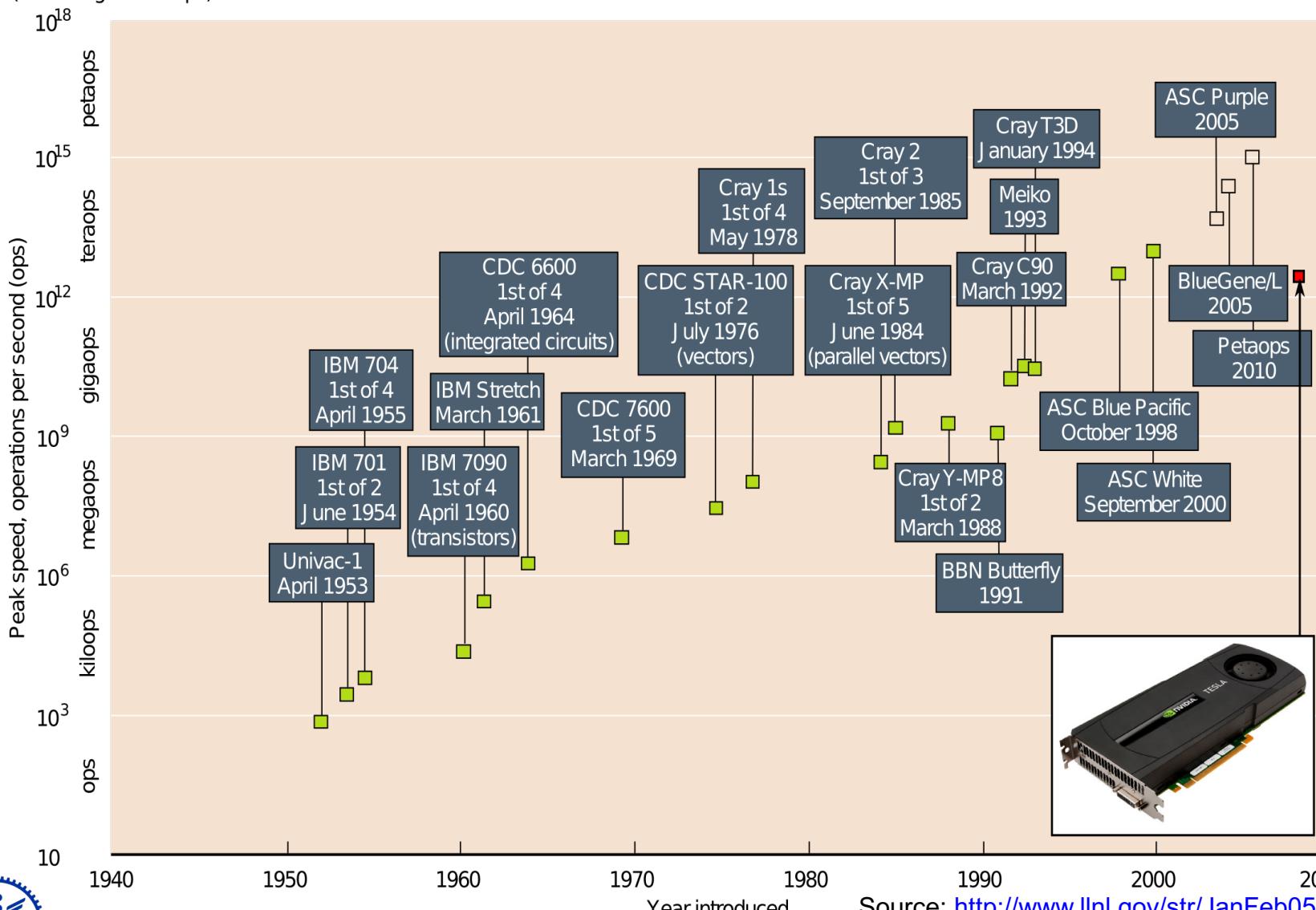


# From GPU to GPGPU



# Single-Chip GPU vs Fastest Supercomputers

(Next range is exaops)



# Single-Chip GPU vs Supercomputers



Nvidia A100 (2020)  
(Ampere)  
19.5 TFlop/s



IBM BlueGene/L (2007)  
(with 131,072 CPU cores)  
367 TFlop/s

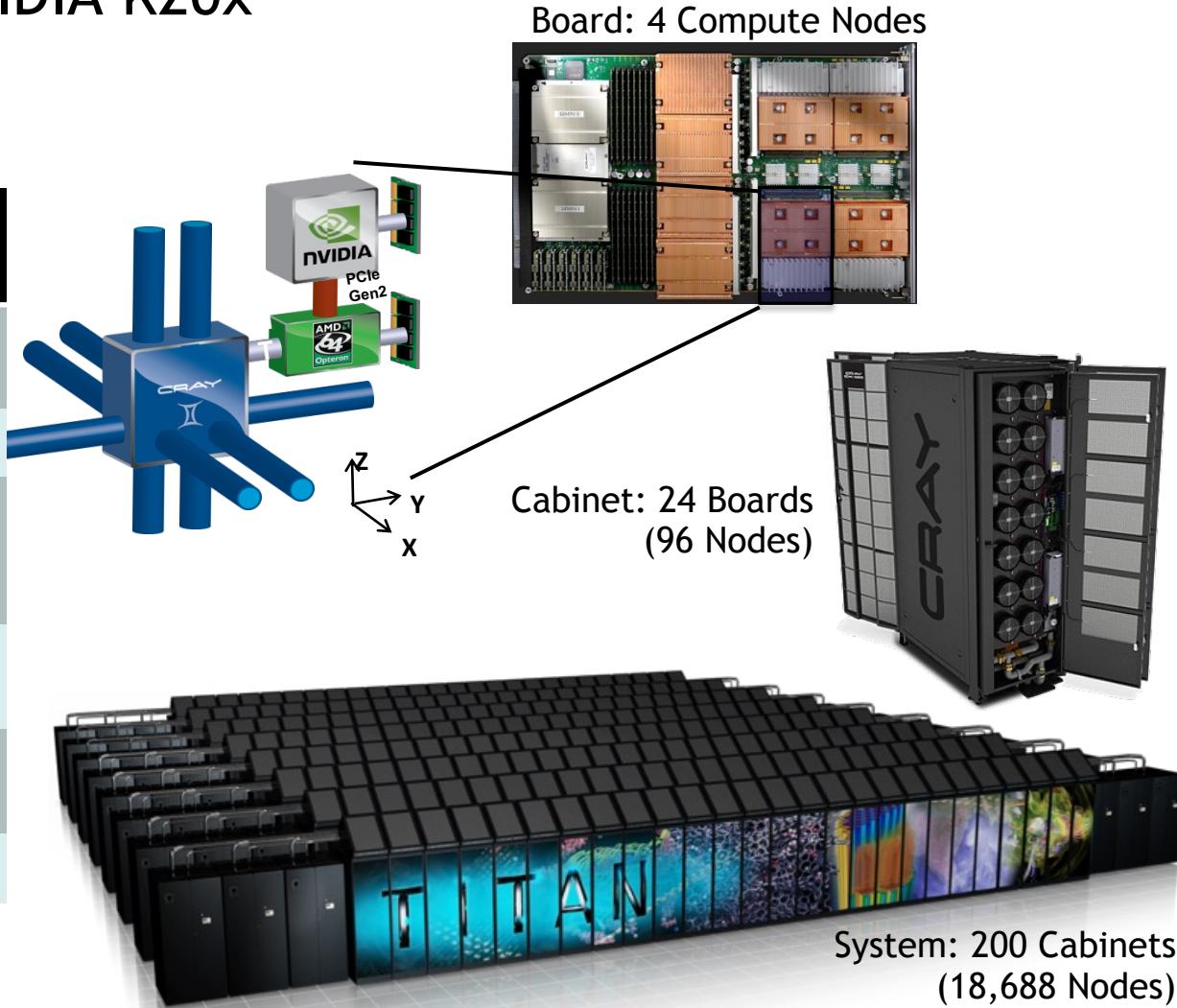


# Titan (#2, 06/2015)



- Cray XK7, Opteron 6274 16C 2.200GHz, Cray Gemini interconnect, NVIDIA K20x
- 560,640 cores

XK7 Compute Node Characteristics
AMD Series 6200 (Interlagos) 16 cores
NVIDIA Kepler
Host Memory 32GB 1600 MT/s DDR3
NVIDIA Tesla X2090 Memory 6GB GDDR5 capacity
Gemini High Speed Interconnect
Keplers in final installation



# Summit (#1, 06/2018)

- 2,282,544 CPU cores
  - 103,752 IBM POWER9 22-core CPUs
- 27,648 Nvidia Tesla V100 GPUs
- Site: DOE(Department of Energy)/SC(Office of Science)/Oak Ridge National Laboratory

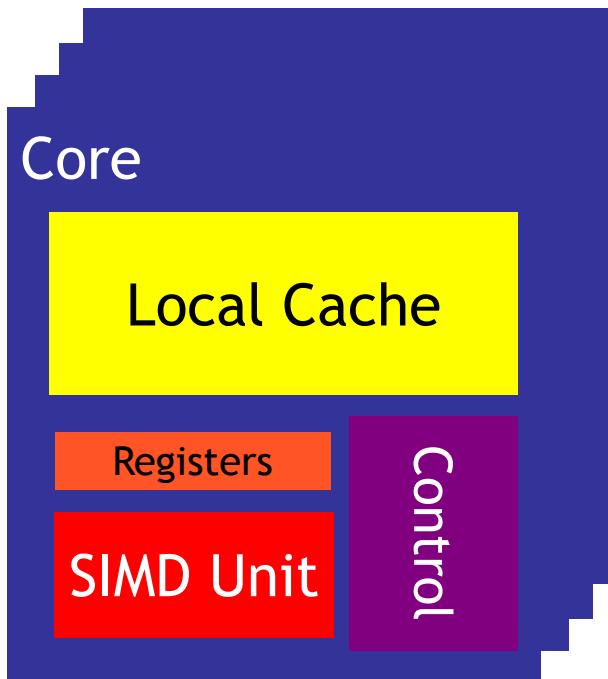


Rpeak: 187,659 TFlop/s

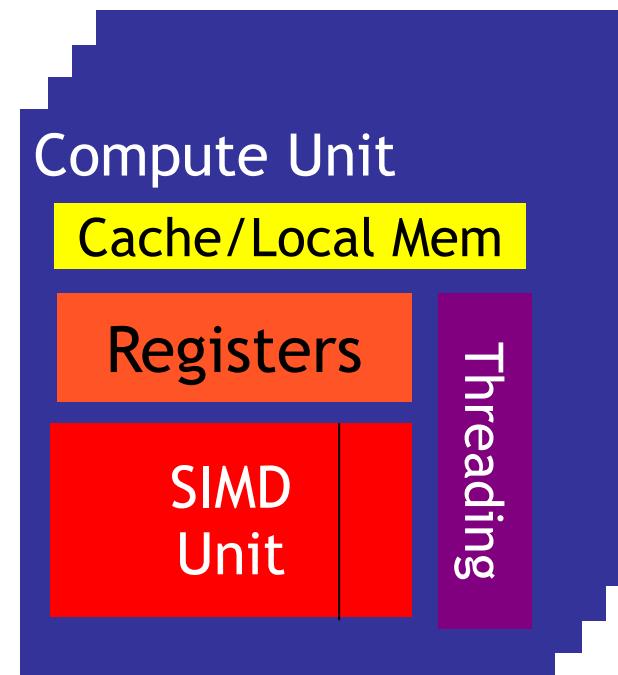


# CPU and GPU have very different design philosophy

CPU  
Latency-Oriented Cores

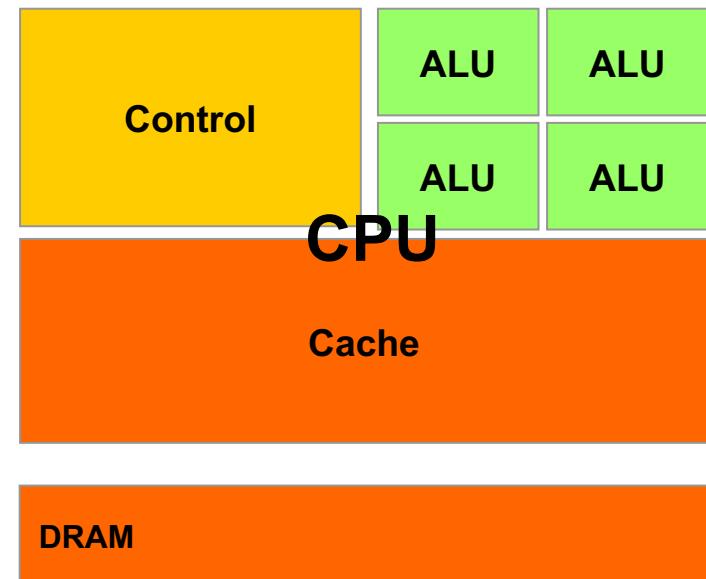


GPU  
Throughput-Oriented Cores



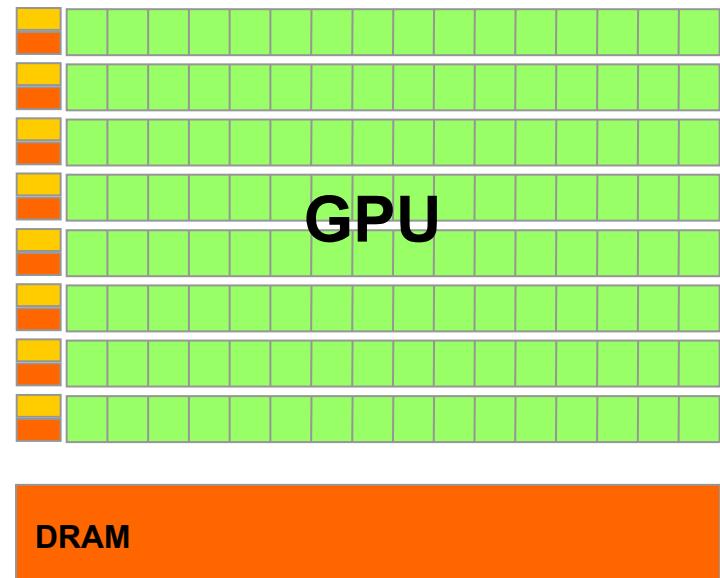
# CPUs: Latency-Oriented Design

- Large caches
  - ✿ Convert long latency memory accesses to short latency cache accesses
- Sophisticated control
  - ✿ Branch prediction for reduced branch latency
  - ✿ Data forwarding for reduced data latency
- Powerful ALU
  - ✿ Reduced operation latency



# GPUs: Throughput-Oriented Design

- Small caches
  - ✿ To boost memory throughput
- Simple control
  - ✿ No branch prediction
  - ✿ No data forwarding
- Energy efficient ALUs
  - ✿ Many, long latency but heavily pipelined for high throughput
- Require massive number of threads to tolerate latencies



# Winning Applications Use Both CPU and GPU

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- CPUs for sequential parts where latency matters
  - ✿ CPUs can be 10+X faster than GPUs for sequential code
- GPUs for parallel parts where throughput wins
  - ✿ GPUs can be 10+X faster than CPUs for parallel code



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# GPU Has 10x Compute Density

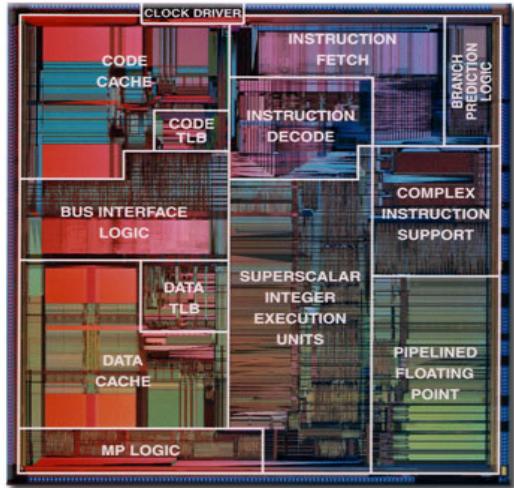
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- Given the same chip area, the achievable performance of GPU is 10x higher than that of CPU.

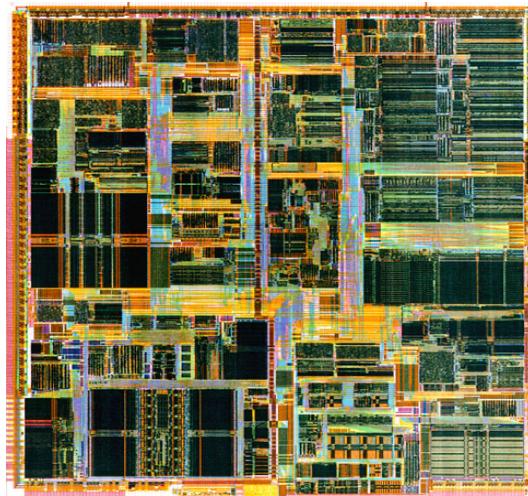


# Evolution of Intel Pentium

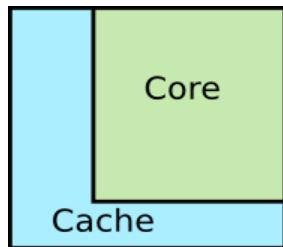
Pentium I



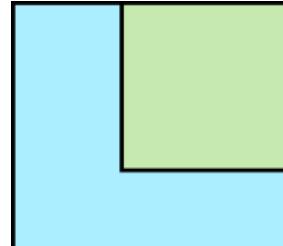
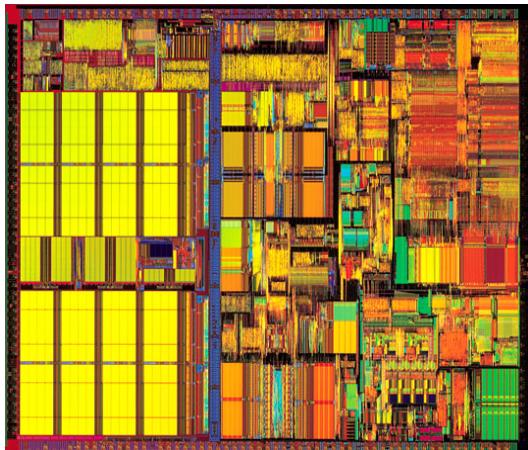
Pentium II



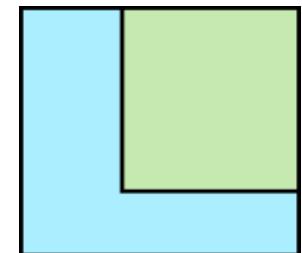
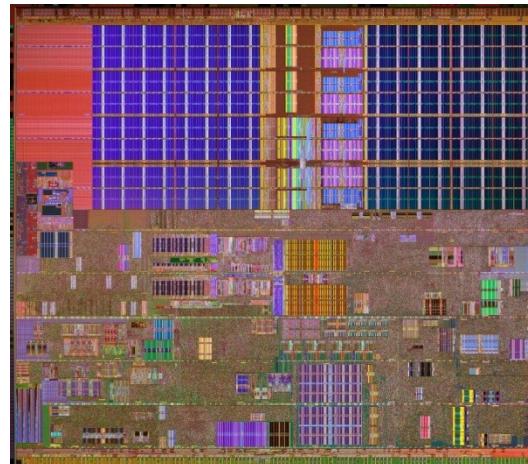
Chip area  
breakdown



Pentium III

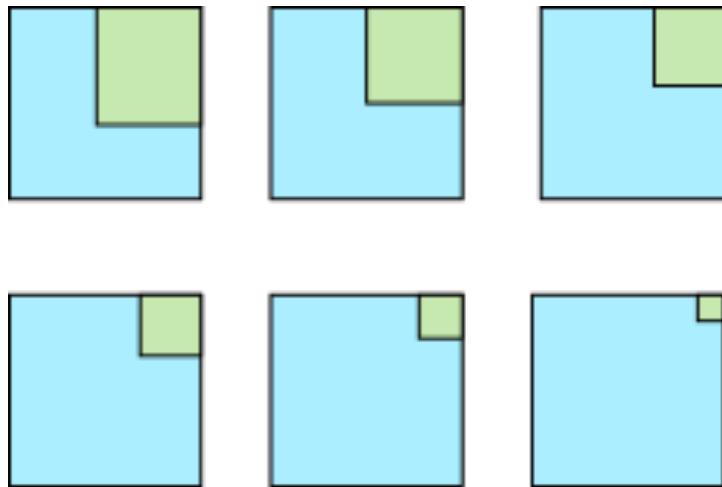


Pentium IV



# Extrapolation of Single Core CPU

- If we extrapolate the trend, in a few generations, Pentium will look like:



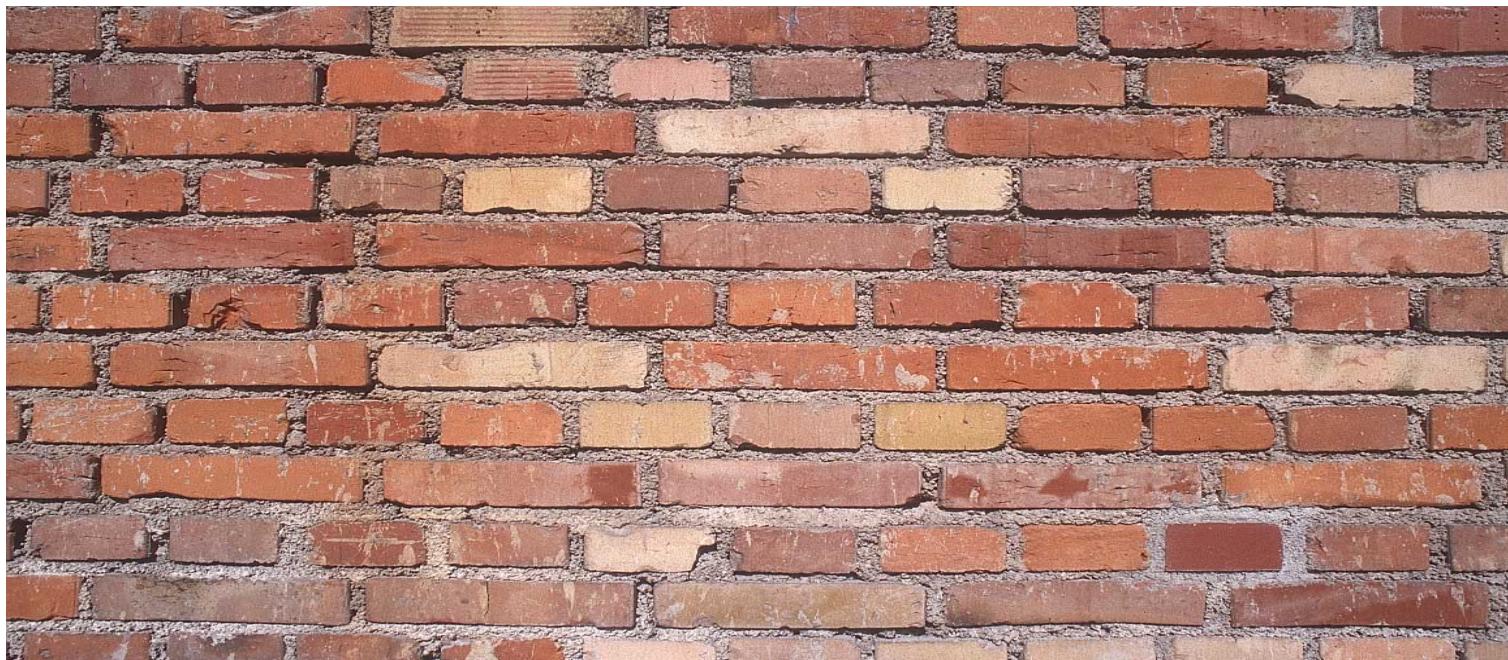
- Of course, we know it did not happen.
- Q: What happened instead? Why?



# The Brick Wall -- UC Berkeley's View

- Memory Wall: Memory slow, multiplies fast
- ILP Wall: diminishing returns on more ILP HW
- Power Wall: power expensive, transistors free

Power Wall + Memory Wall + ILP Wall = **Brick Wall**

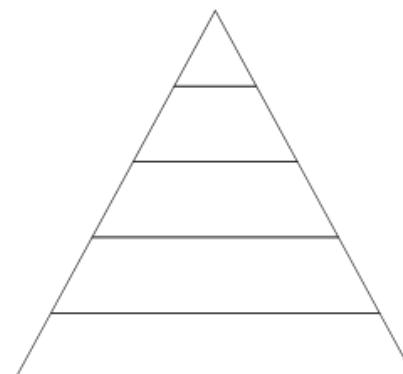


David Patterson, "Computer Architecture is Back - The Berkeley View of the Parallel Computing Research Landscape", Stanford EE Computer Systems Colloquium, Jan 2007,



# How to Break the Brick Wall?

	Size (Byte)	Energy (pJ)	Delay (cycles)	Bandwidth (GB/s)
Reg	1K	10	1	1000
L1	32K	20	5	100
L2	256K	100	10	100
L3	8M	200	50	100
Off-chip	4G	2000	100	10



Hint: how to exploit the parallelism inside the application?  
(GPUs need tons of parallel threads)



# Step 1: Trade Latency with Throughput

	Size (Byte)	Energy (pJ)	Delay (cycles)	Bandwidth (GB/s)
Reg	1K	16K	10~20	1~2~3
L1	32K	20	5	100
L2	256K	100	10	100
L3	8M	200	50	100
Off-chip	4G	2000	100	10

Hind the memory latency through fine-grained interleaved threading.



# Interleaved Multithreading

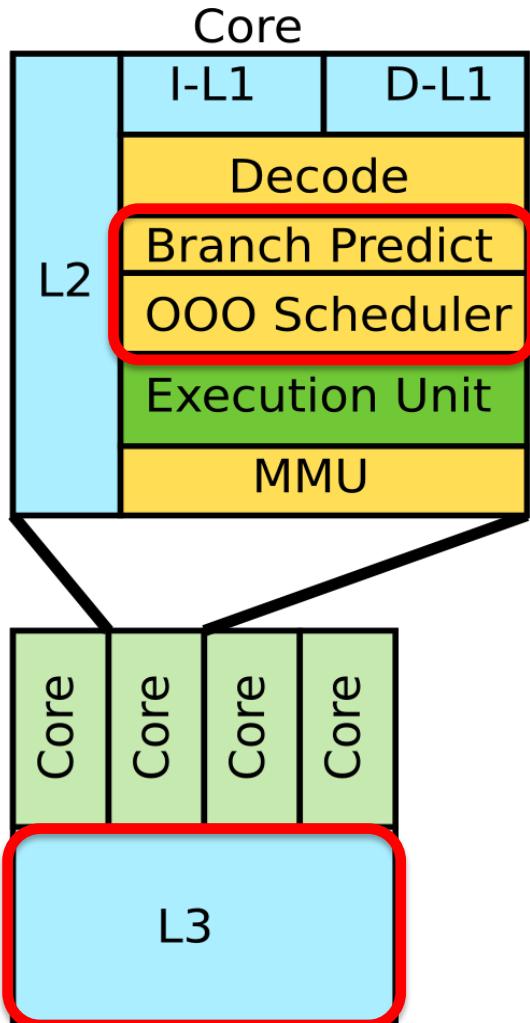


- Fine-grained interleaved multi-threading:
  - ✿ Pros: remove branch predictor, 000 scheduler, large cache
  - ✿ Cons: register pressure, thread scheduler, require huge parallelism, etc.

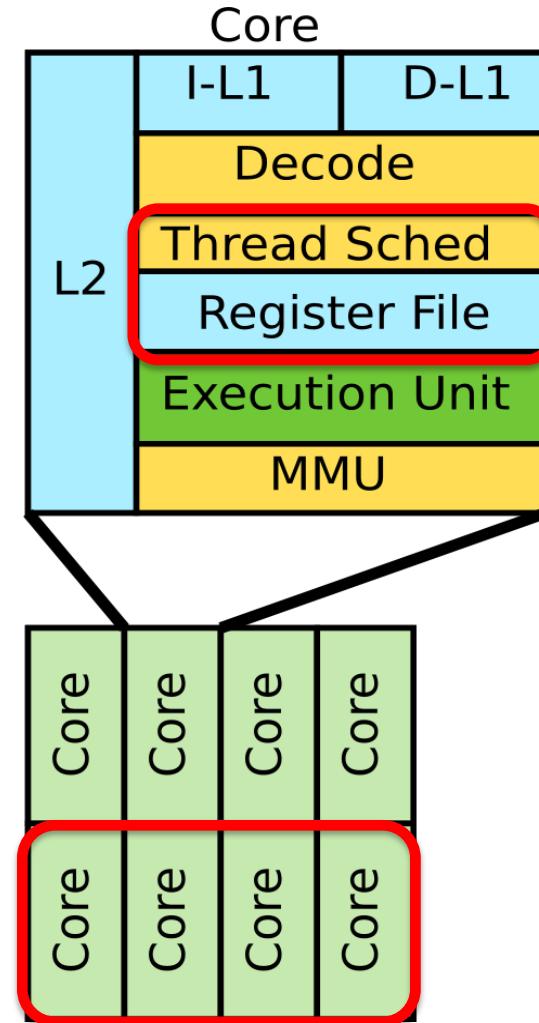


# Fine-Grained Interleaved Threading

Without fine-grained interleaved threading

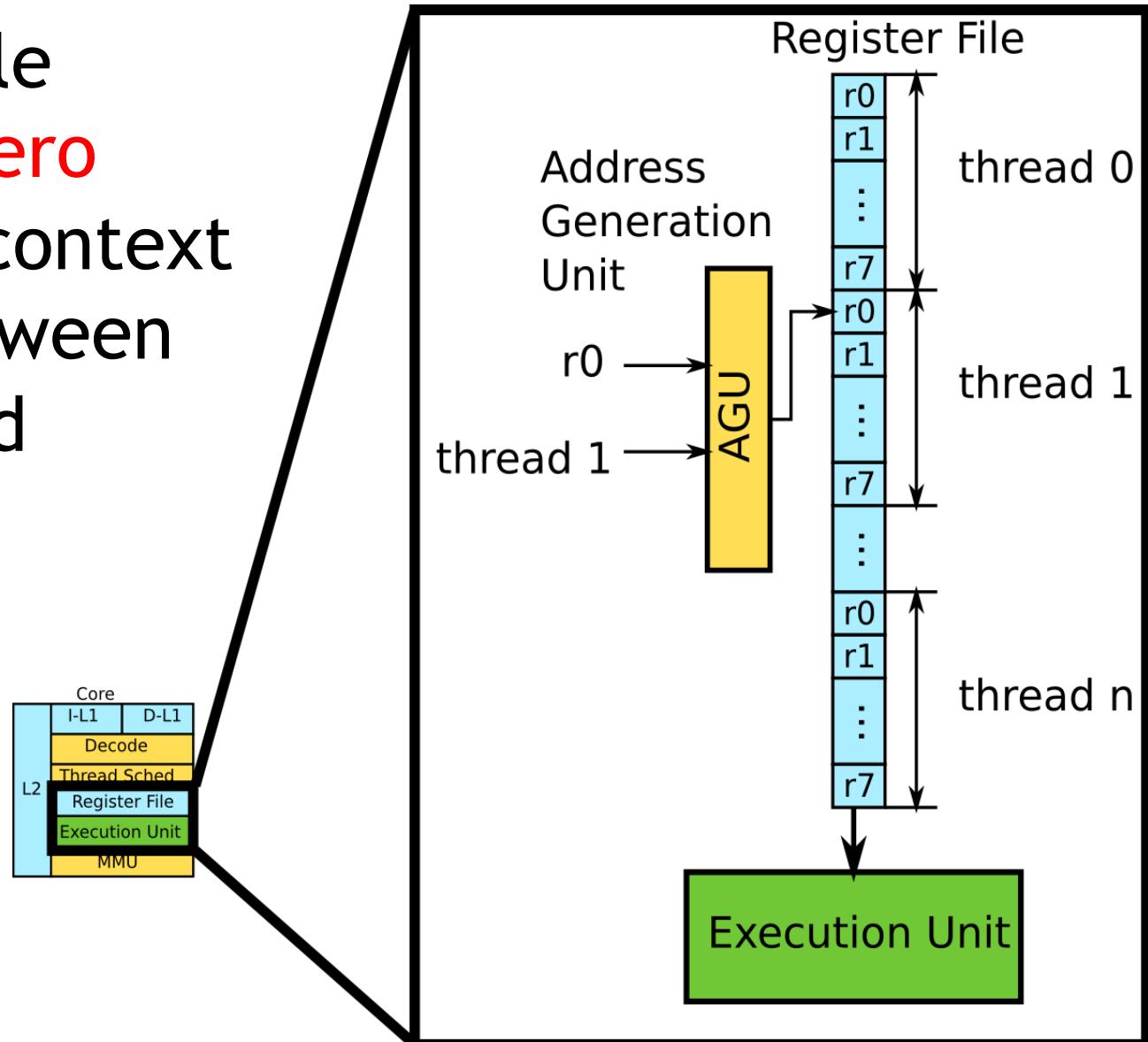


With fine-grained interleaved threading



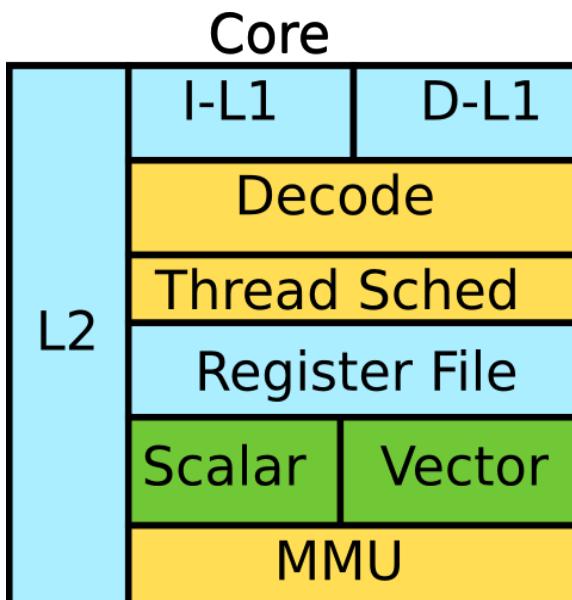
# Hardware Support

- Register file supports **zero overhead** context switch between interleaved threads



# Can We Make Further Improvement?

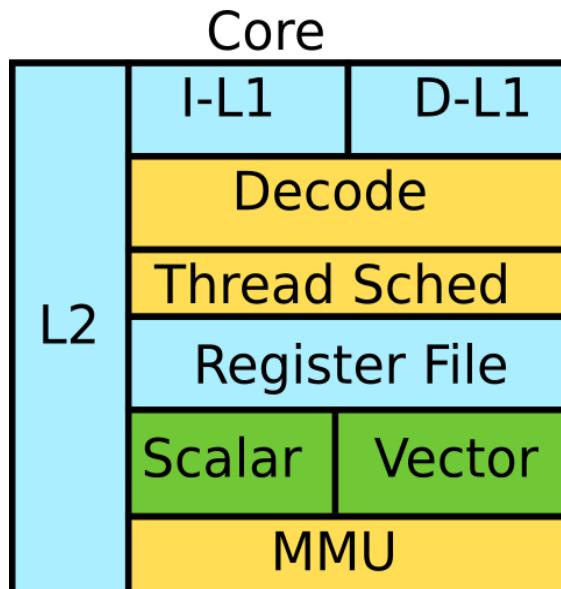
- Reducing large cache gives 2x computational density
- Q: Can we make further improvements?
  - ✳ Hint: We have only utilized thread level parallelism (TLP) so far



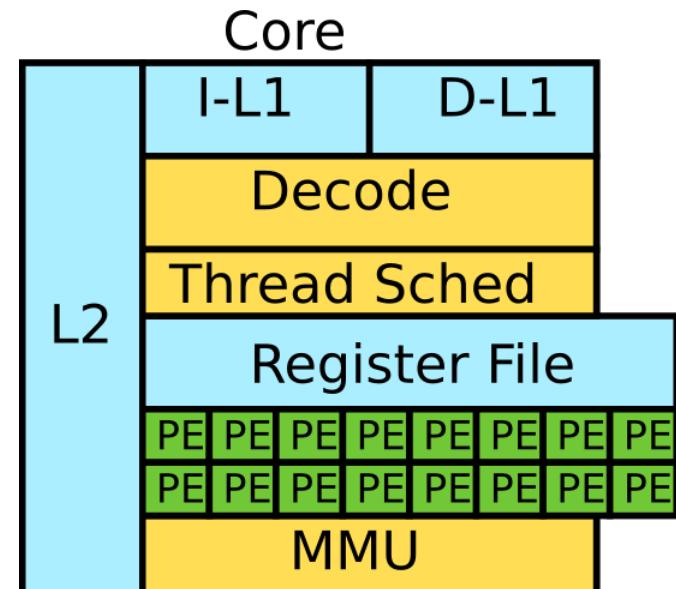
# Step 2: Single Instruction Multiple Data

- GPU uses wide SIMD: 8/16/24/32/64/... processing elements (PEs)
  - CPU uses short SIMD: usually has vector width of 4

SSE has 4 data lanes

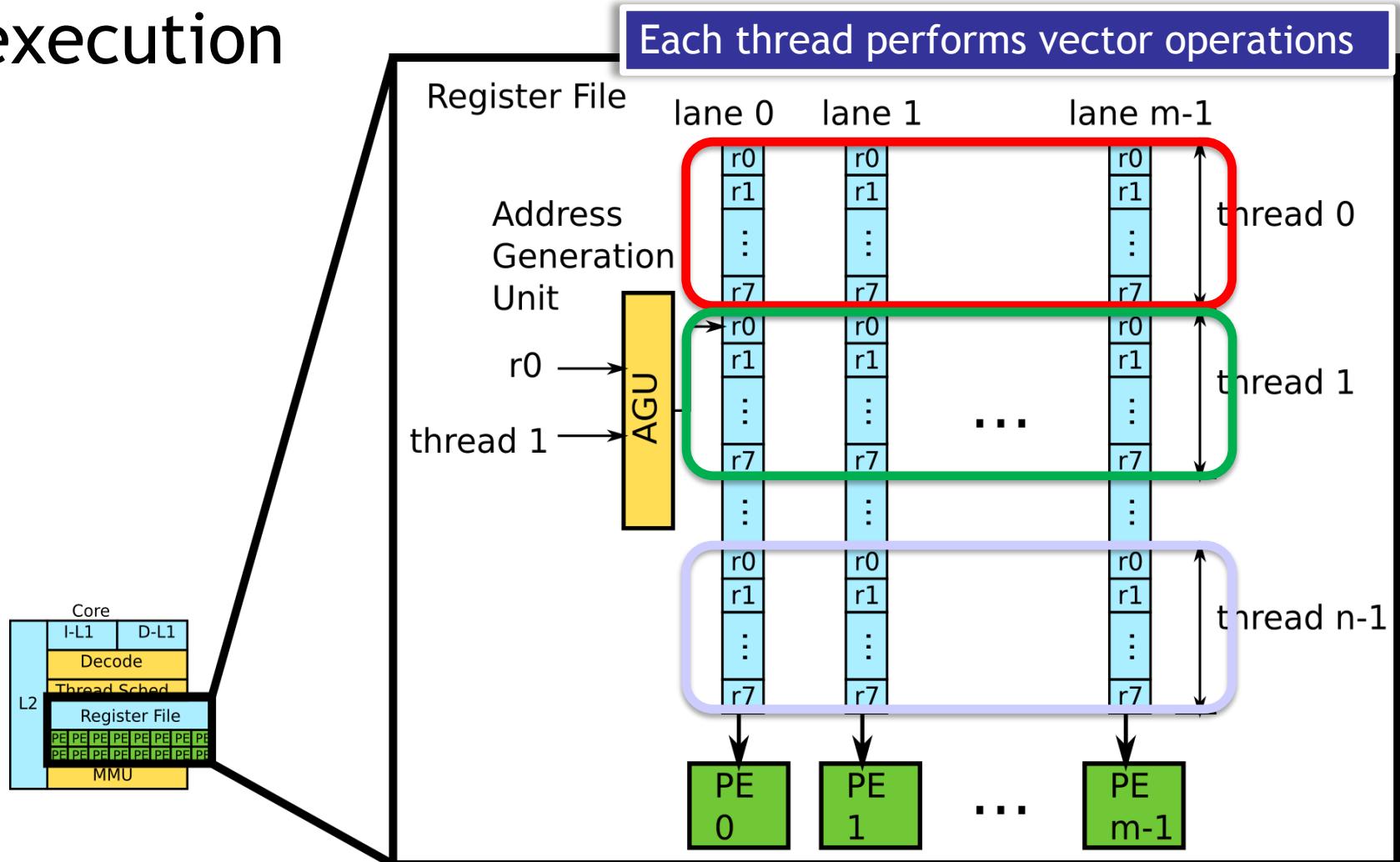


GPU has 8/16/24/... data lanes



# Hardware Support

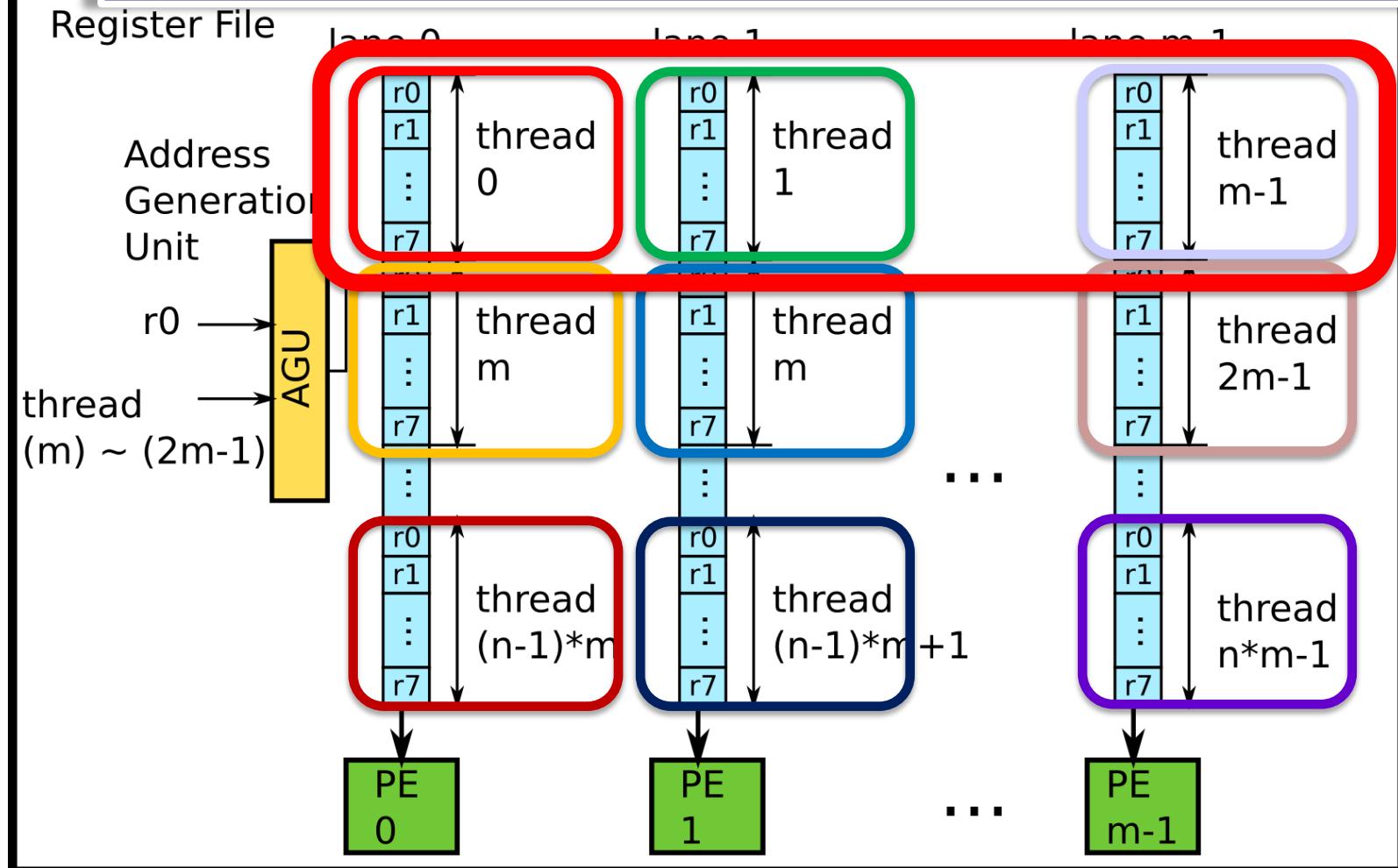
- Supporting interleaved threading + SIMD execution



# Single Instruction Multiple Thread (SIMT)

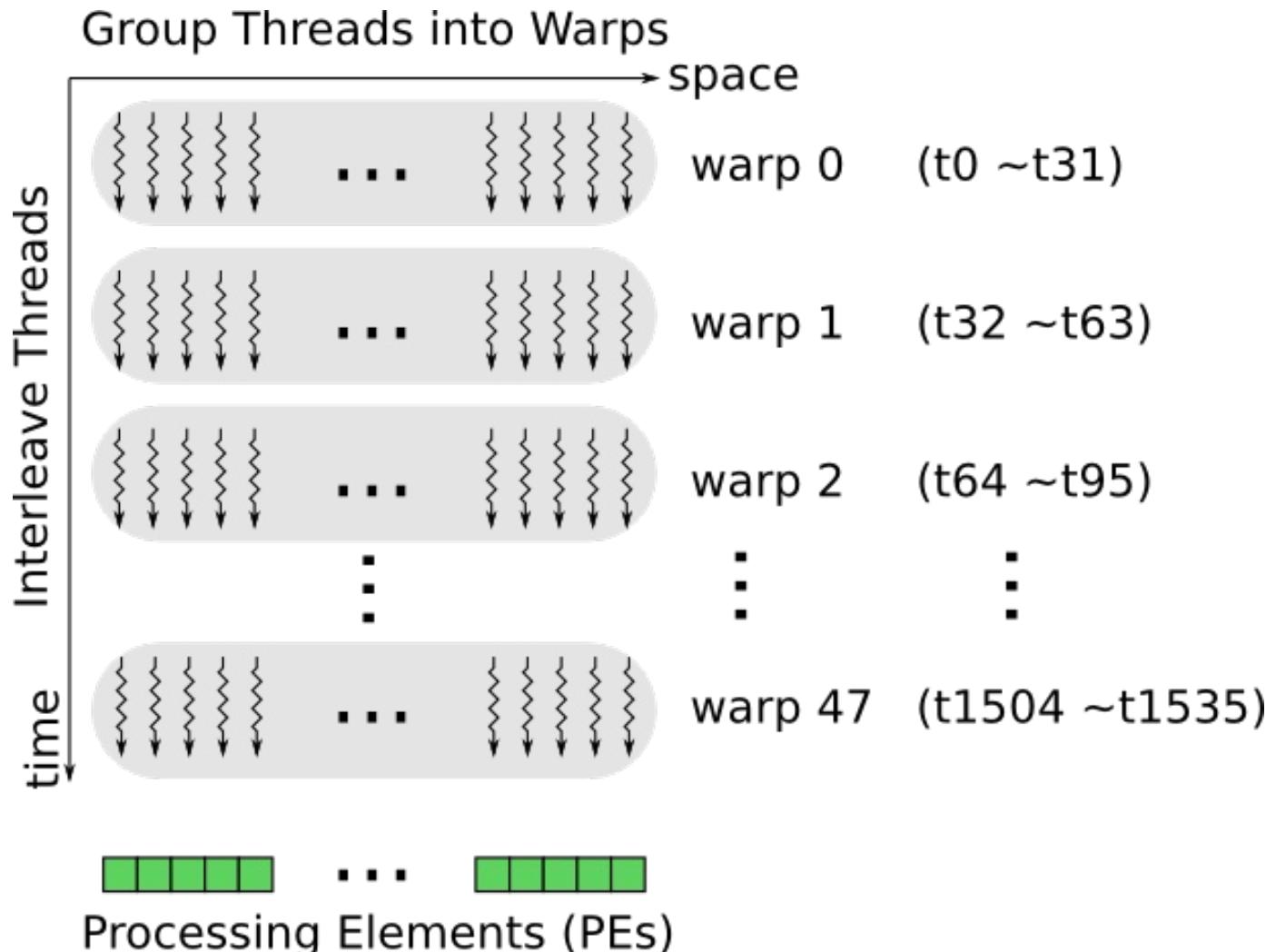
## Hide vector width using scalar threads

Each thread performs scalar operations, and a group of threads share a PC



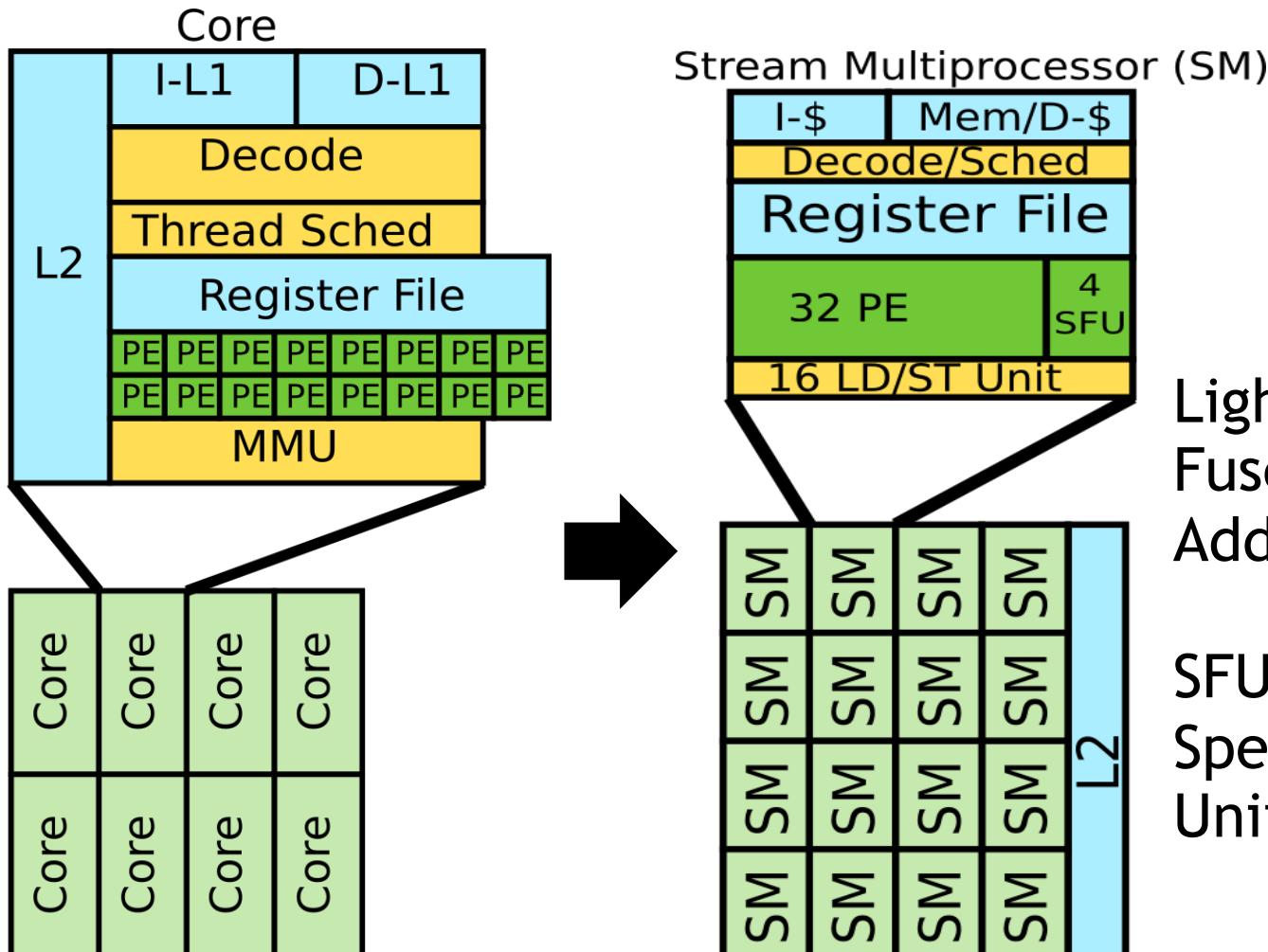
# Example of SIMT Execution

- Assume 32 threads are grouped into one warp



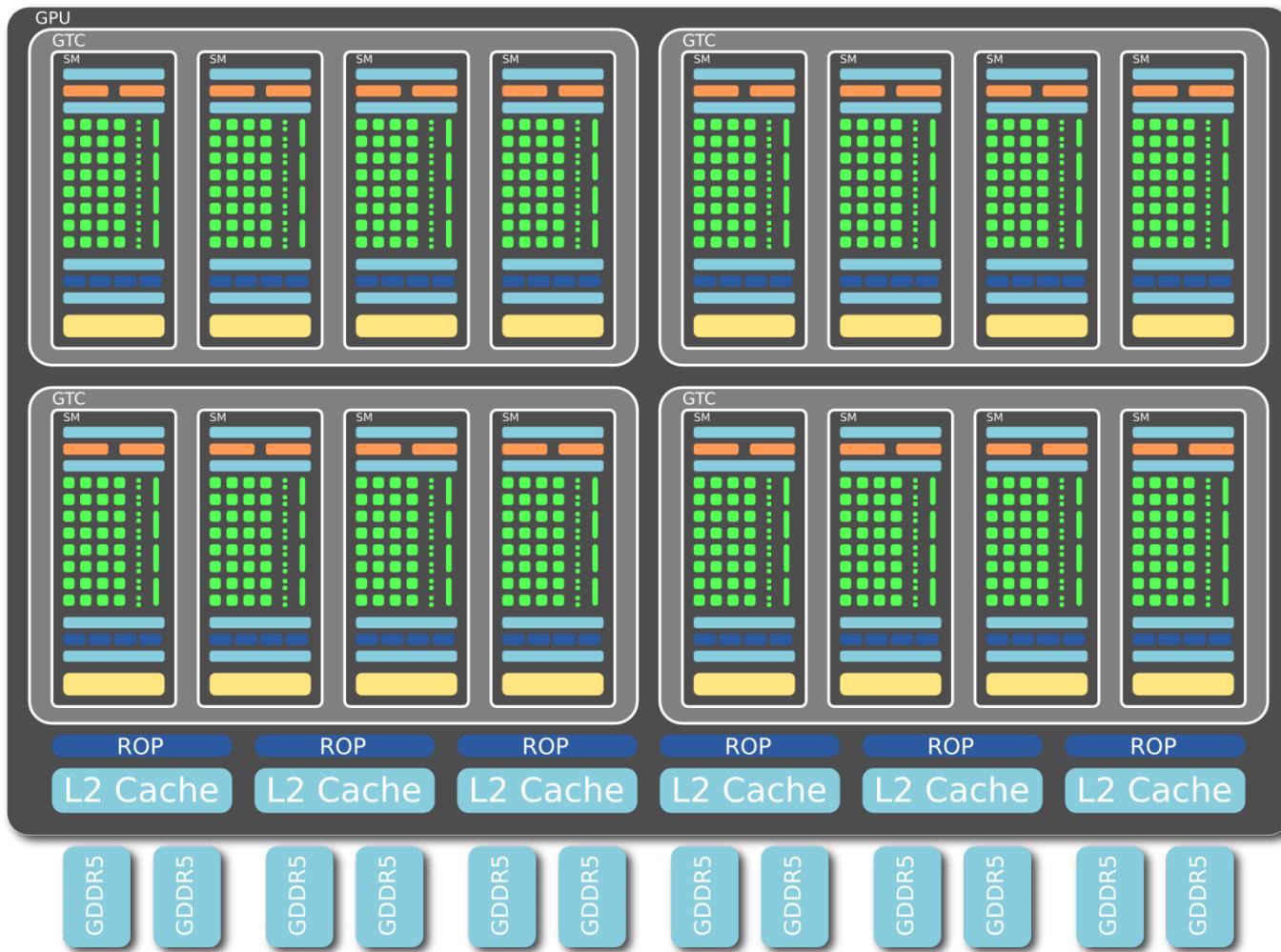
# Step 3: Simple Core

The Stream Multiprocessor (SM) is a light weight core compared to IA core

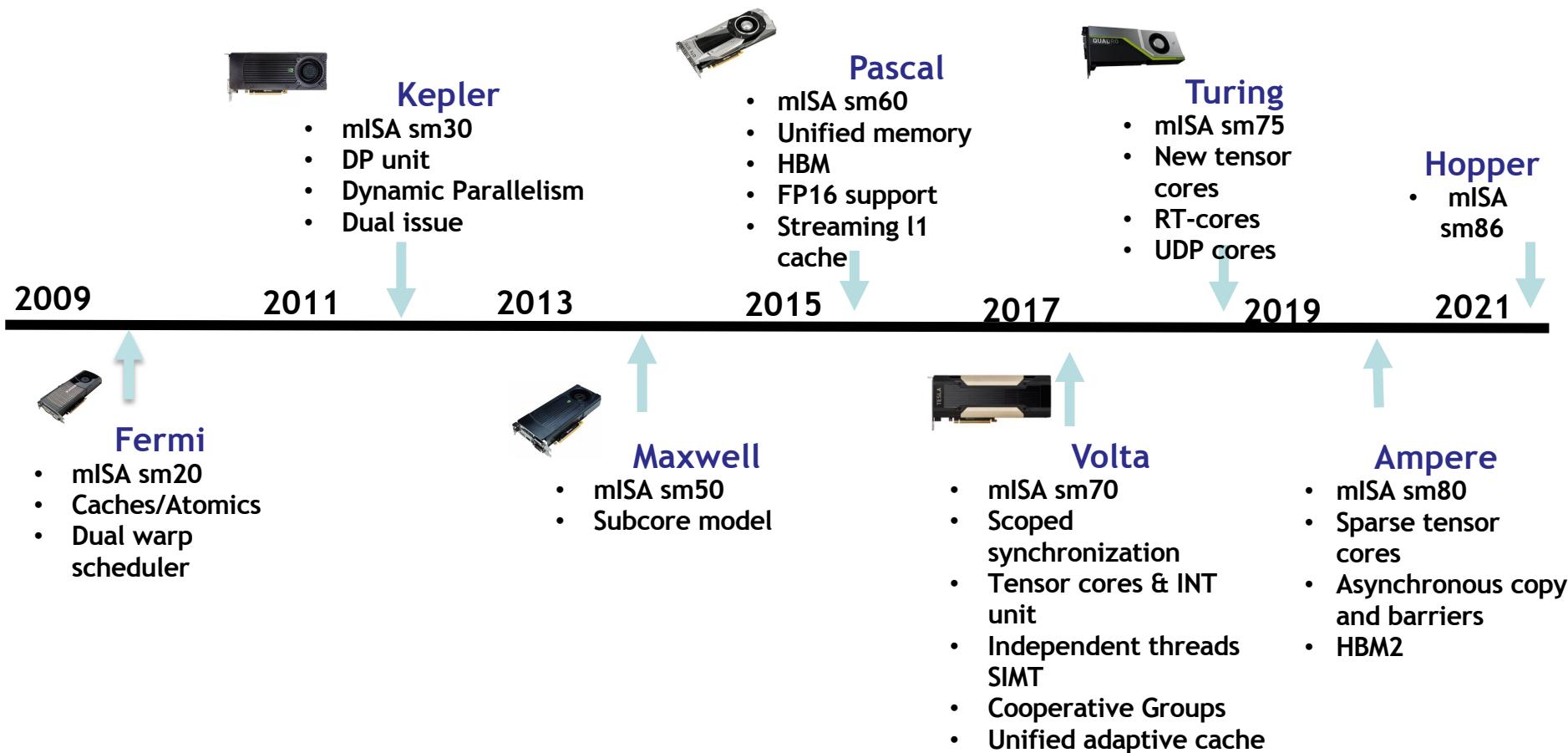


# NVIDIA Fermi

## ■ 512 Processing Elements (PEs)



# GPU Accelerators are Evolving Rapidly!



New machine ISA and architecture designs every 1-2 years!



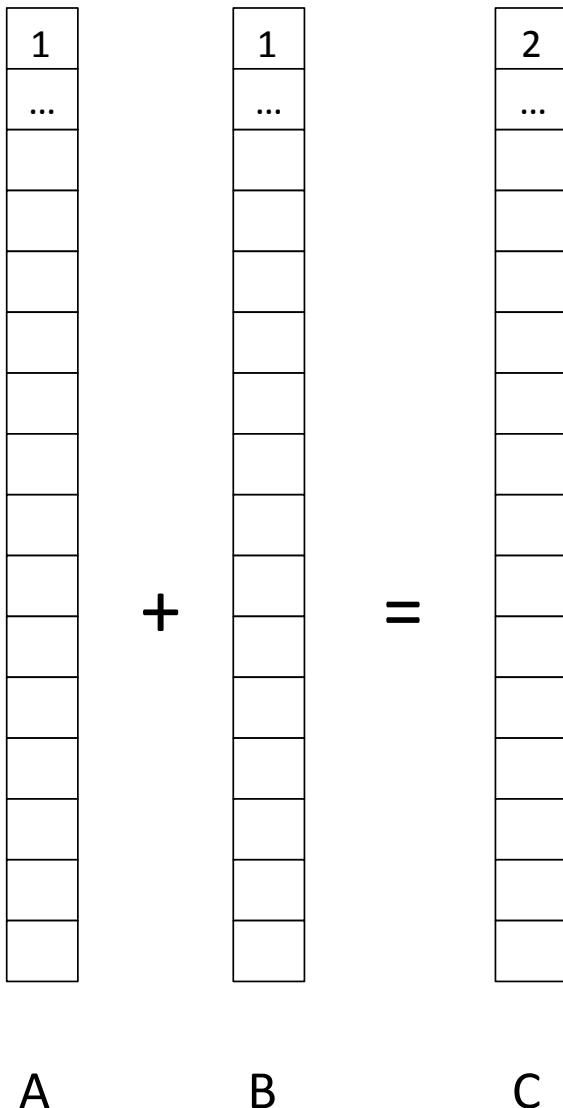
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# Threading Model: Serial Code

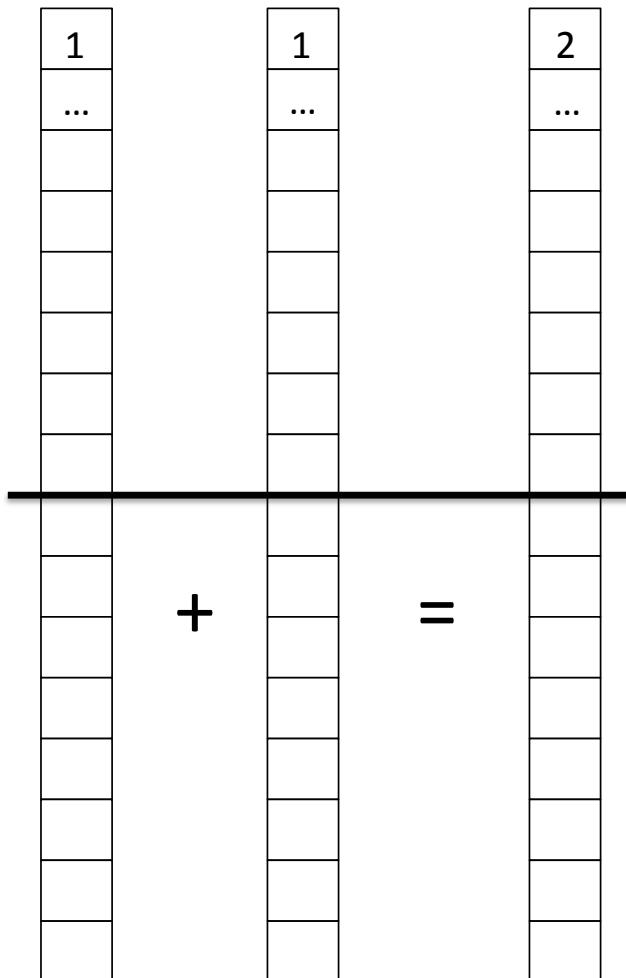


Thread 0

```
for (int i = 0; i < 1000; ++i)  
    c[i] = a[i] + b[i];
```



# Threading Model: Dual-core Parallelism (2 Threads)



Thread 0

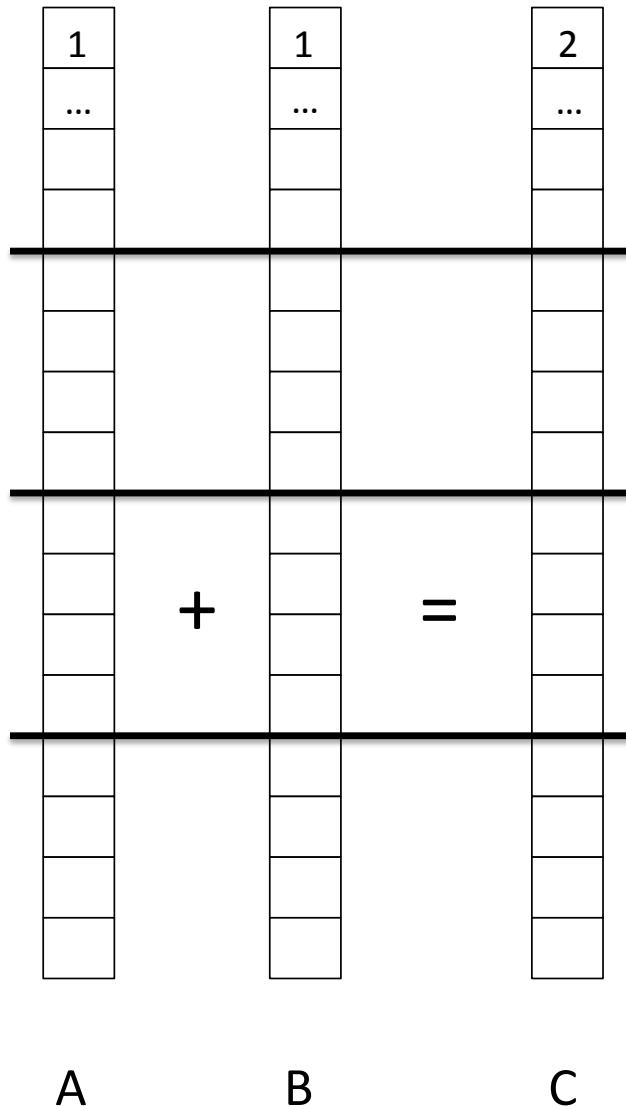
```
for (int i = 0; i < 500; ++i)  
    c[i] = a[i] + b[i];
```

Thread 1

```
for (int i = 500; i < 1000; ++i)  
    c[i] = a[i] + b[i];
```



# Threading Model: Quad-core Parallelism (4 Threads)



Thread 0

```
for (int i = 0; i < 250; ++i)  
    c[i] = a[i] + b[i];
```

Thread 1

```
for (int i = 250; i < 500; ++i)  
    c[i] = a[i] + b[i];
```

Thread 2

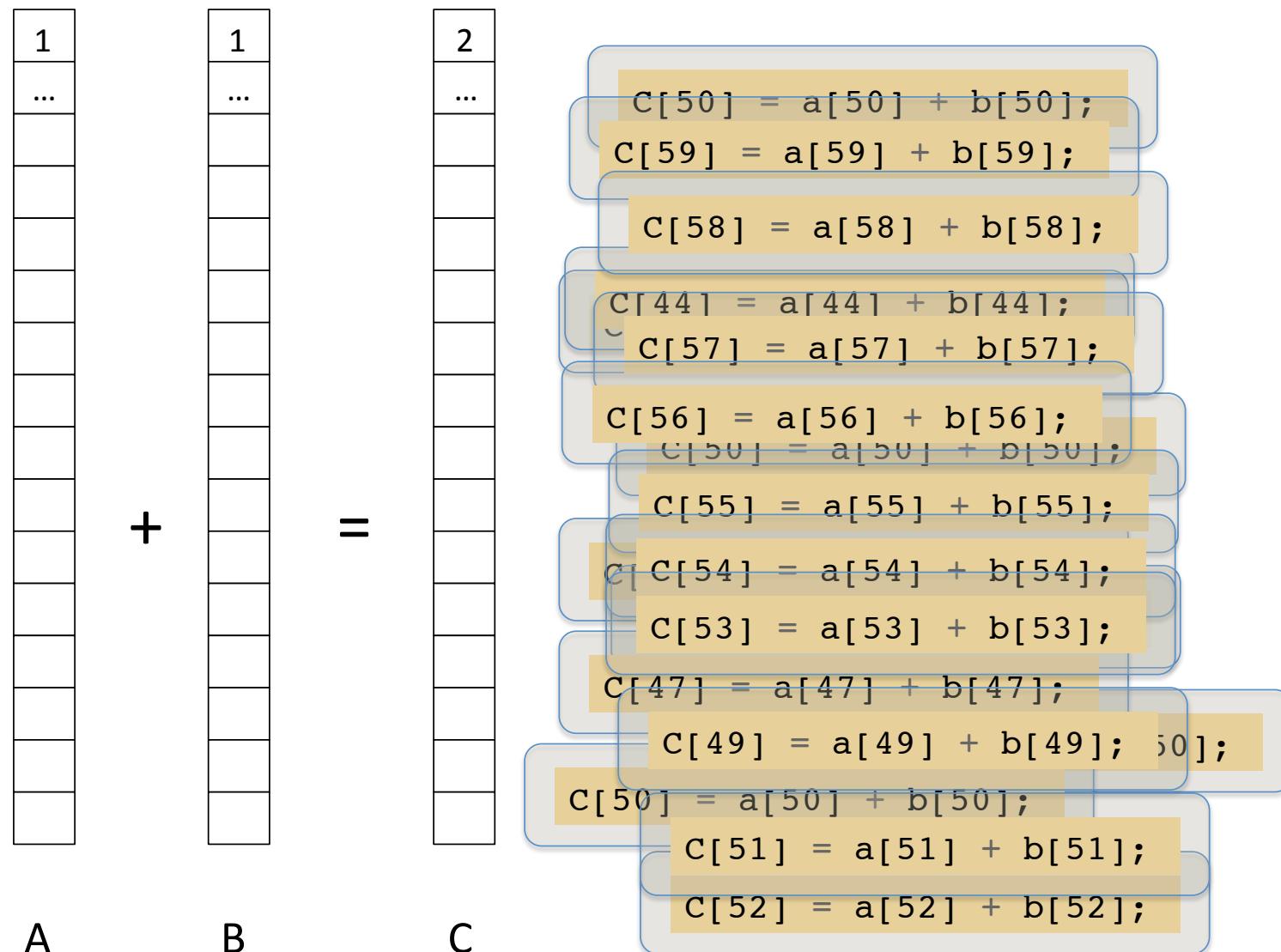
```
for (int i = 500; i < 750; ++i)  
    c[i] = a[i] + b[i];
```

Thread 3

```
for (int i = 750; i < 1000; ++i)  
    c[i] = a[i] + b[i];
```



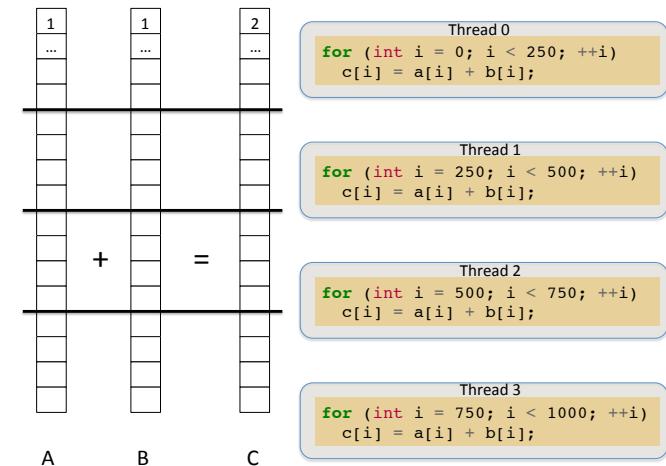
# Threading Model: GPU Parallelism (N Threads)



# Threading Model

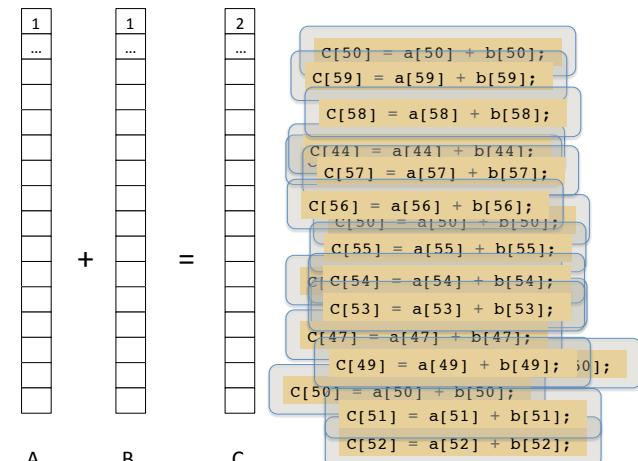
## CPU

- Number of Threads  
~ Physical Cores



## GPU

- Number of Threads  
~ Amount of Data
- Single instruction,  
multiple threads (SIMT)



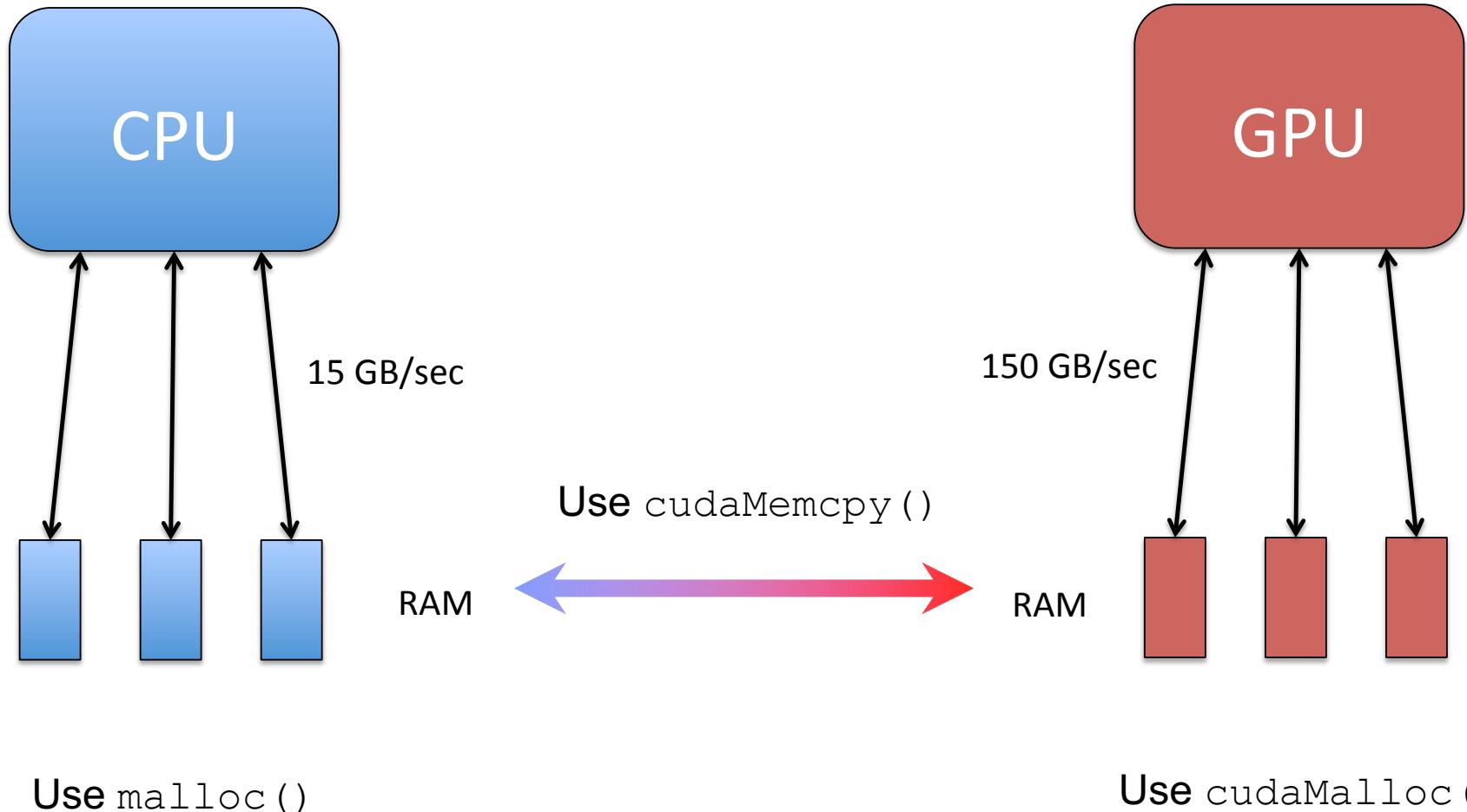
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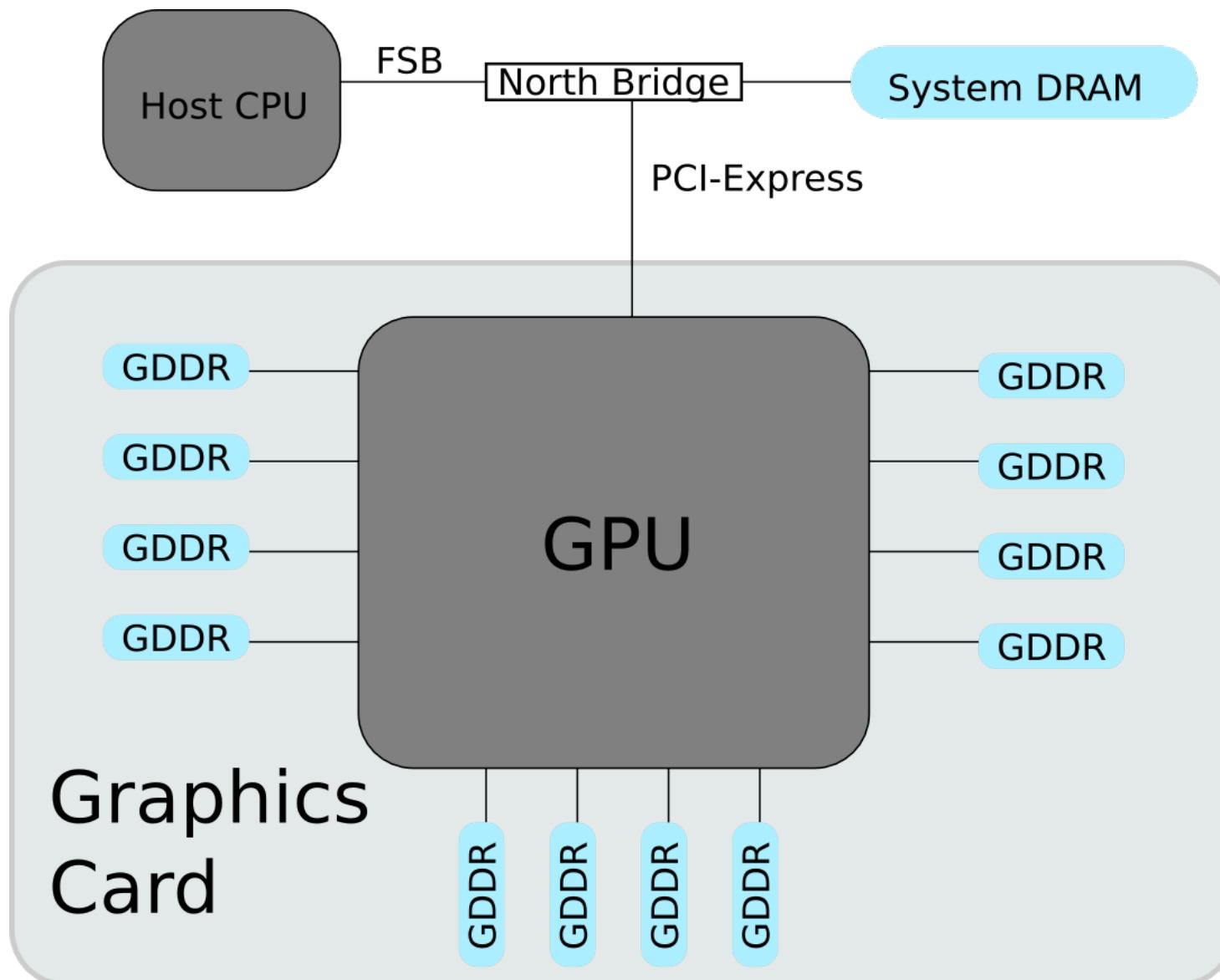
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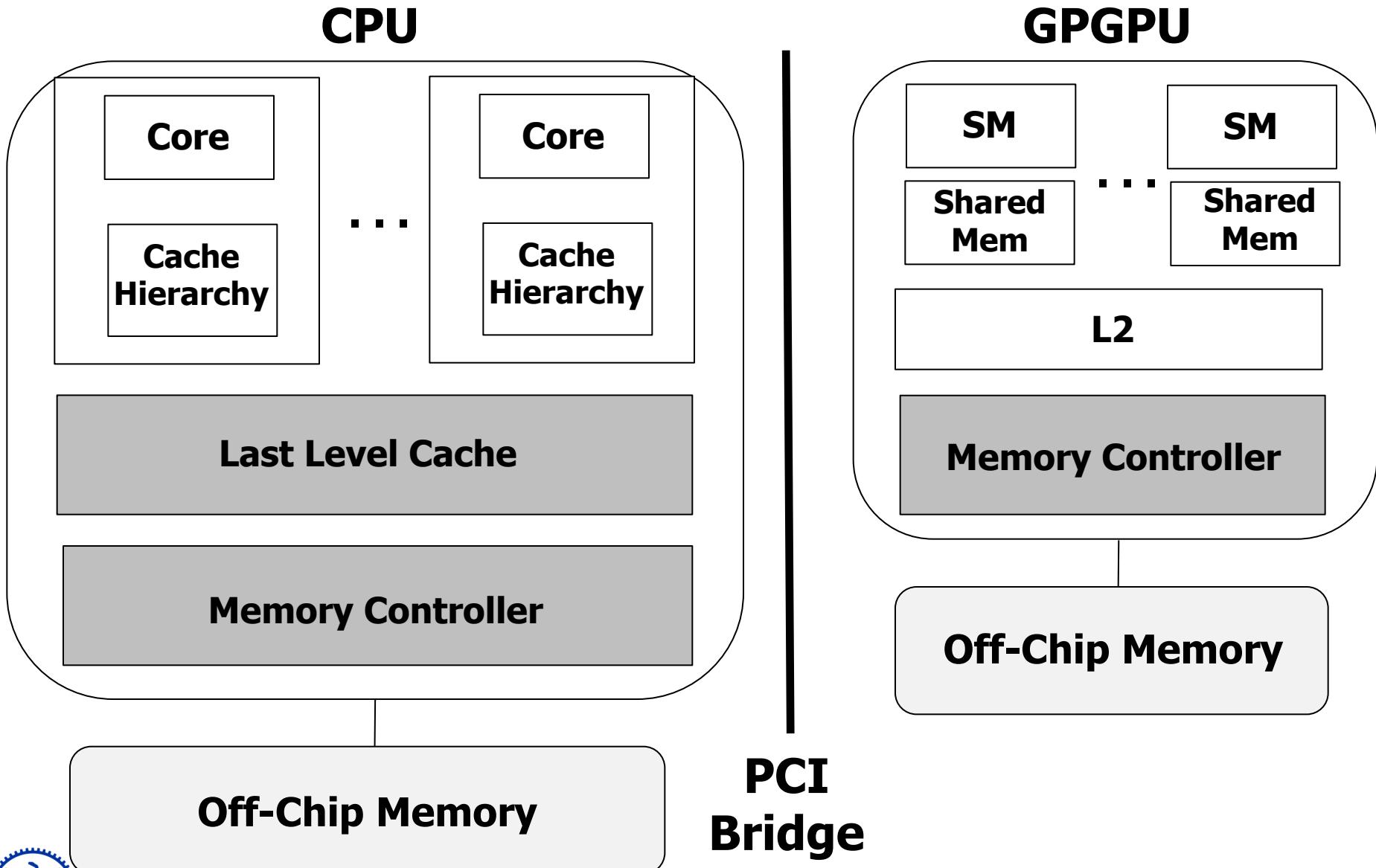
# Memory Separation



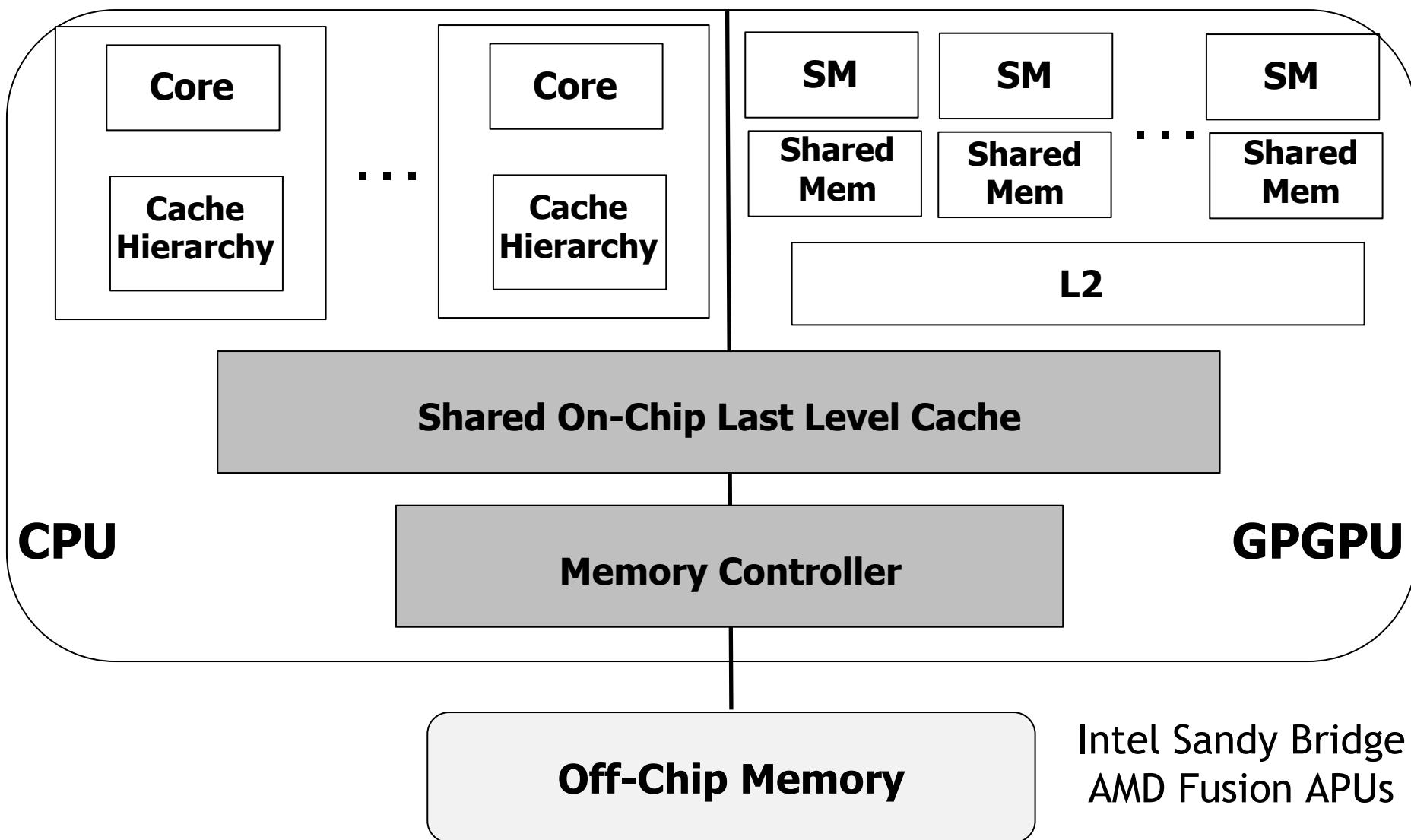
# System Architecture



# Discrete GPUs



# Integrated CPUs-GPUs



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# CUDA

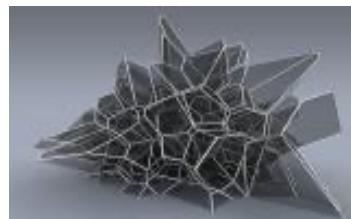
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- Compute Unified Device Architecture
- In November 2006, NVIDIA introduced CUDA™, a general-purpose **parallel computing platform and programming model**
- Leverages the parallel compute engine in NVIDIA GPUs to solve many complex computational problems in a more efficient way than on a CPU



# GPU as a General-Purpose Computing Platform

- Speedups are impressive and ever increasing!



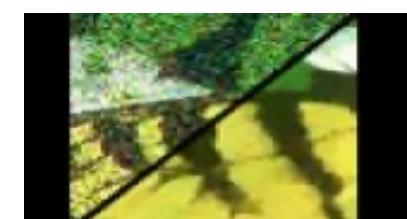
Genetic Algorithm  
**2600 X**



Real Time Elimination  
of Undersampling Artifacts  
**2300 X**



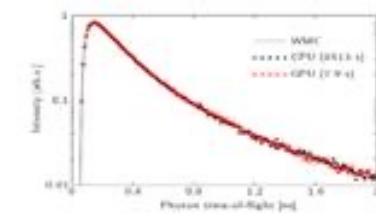
Lattice-Boltzmann Method  
for Numerical Fluid Mechanics  
**1840 X**



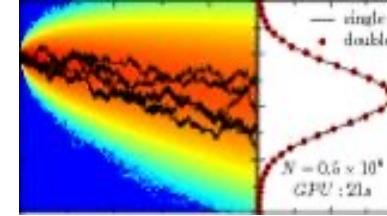
Total Variation Modeling  
**1000 X**



Fast Total Variation for  
Computer Vision  
**1000 X**



Monte Carlo Simulation  
Of Photon Migration  
**1000 X**



Stochastic Differential  
Equations  
**675 X**



K-Nearest Neighbor  
Search  
**470 X**

Source: CUDA Zone at [www.nvidia.com/cuda/](http://www.nvidia.com/cuda/)



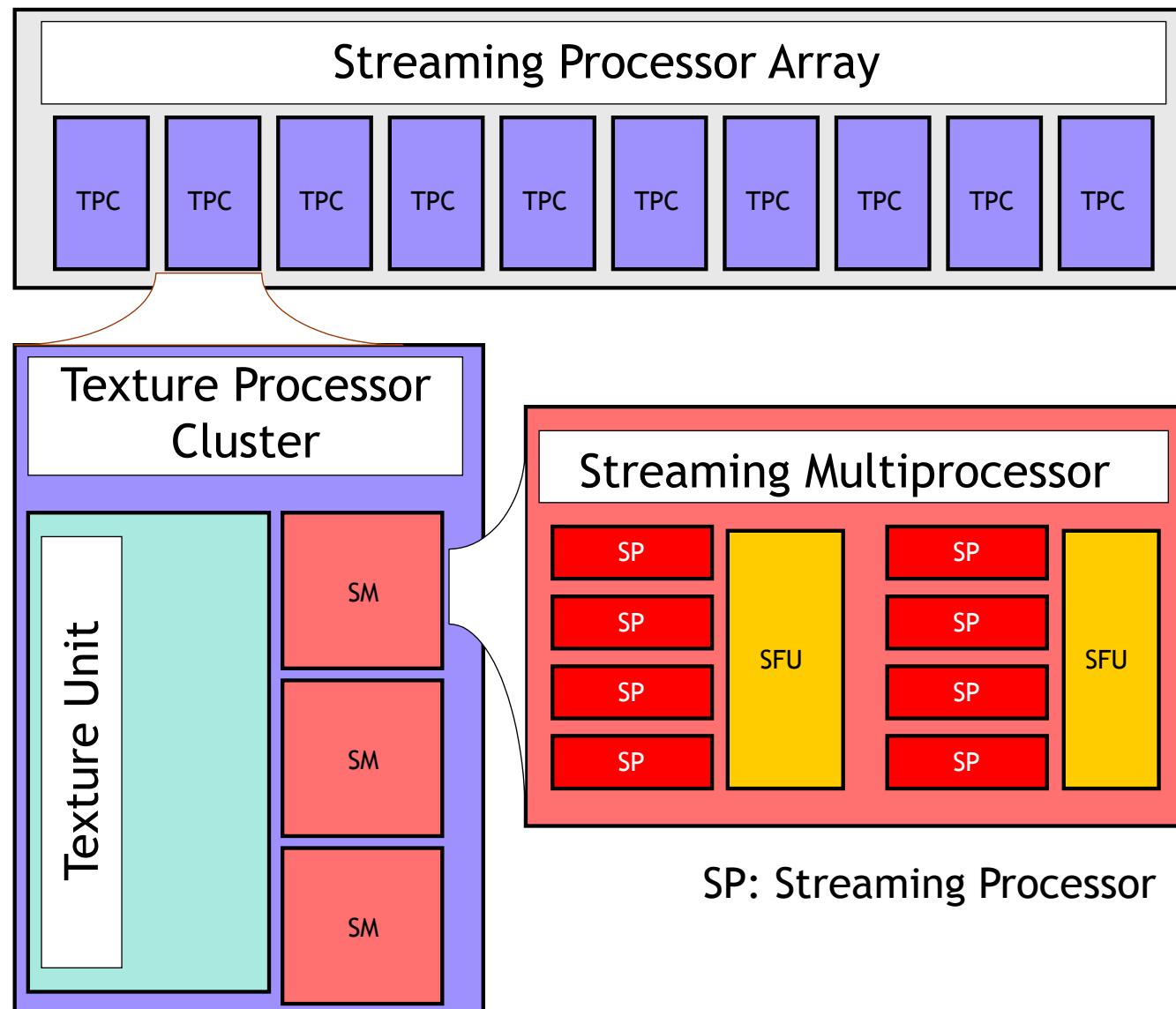
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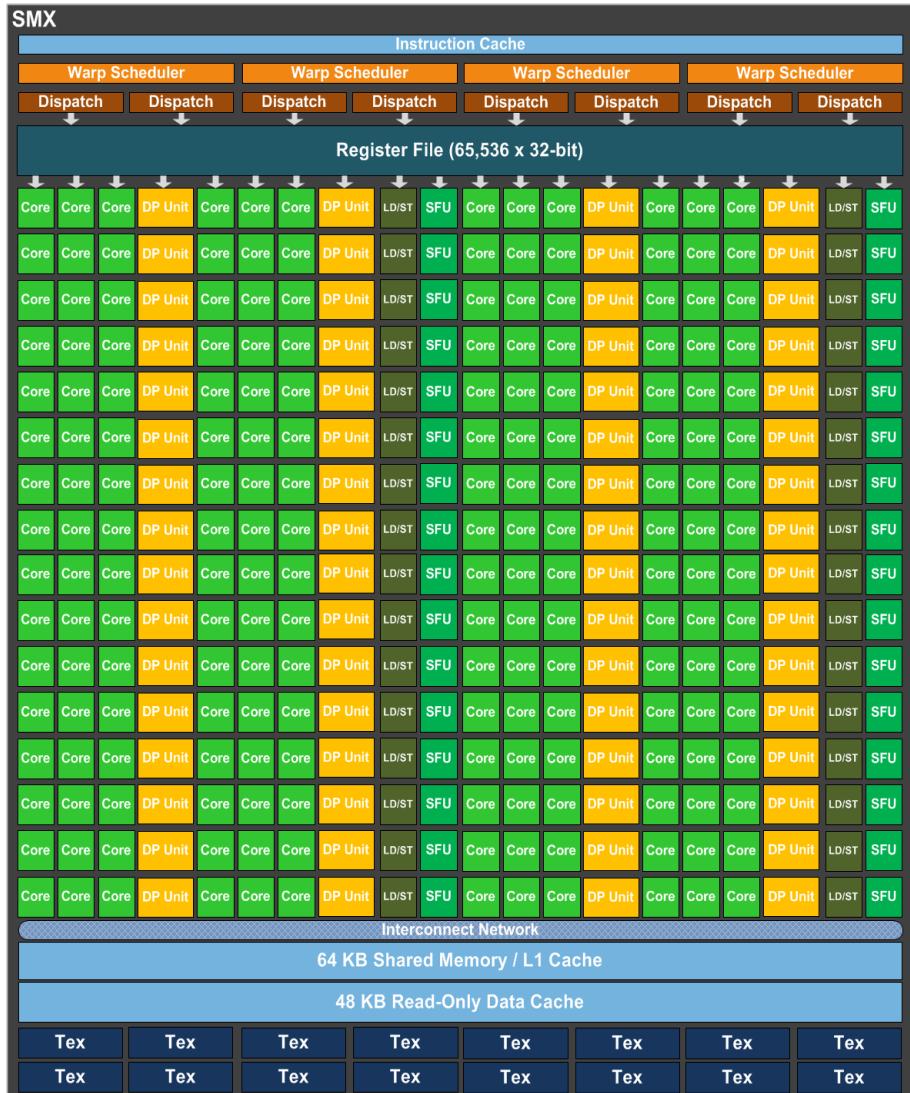


# CUDA: Parallel Computing Platform



# Kepler GK110

- New streaming multiprocessor (now called SMX)
  - Contains 192 single-precision CUDA cores, 64 double-precision units, 32 special function units (SFU), and 32 load/store units (LD/ST)
- Full Kepler GK110 has 15 SMXs
  - Some products may have 13 or 14 SMXs



Source: <http://www.nvidia.com/content/PDF/kepler/NVIDIA-Kepler-GK110-Architecture-Whitepaper.pdf>



# Hopper GH100



- A full GH100 GPU with 144 SMs
  - ❖ 128 FP32 CUDA Cores per SM
  - ❖ 18432 FP32 CUDA Cores per full GPU

Source: <https://resources.nvidia.com/en-us-tensor-core>



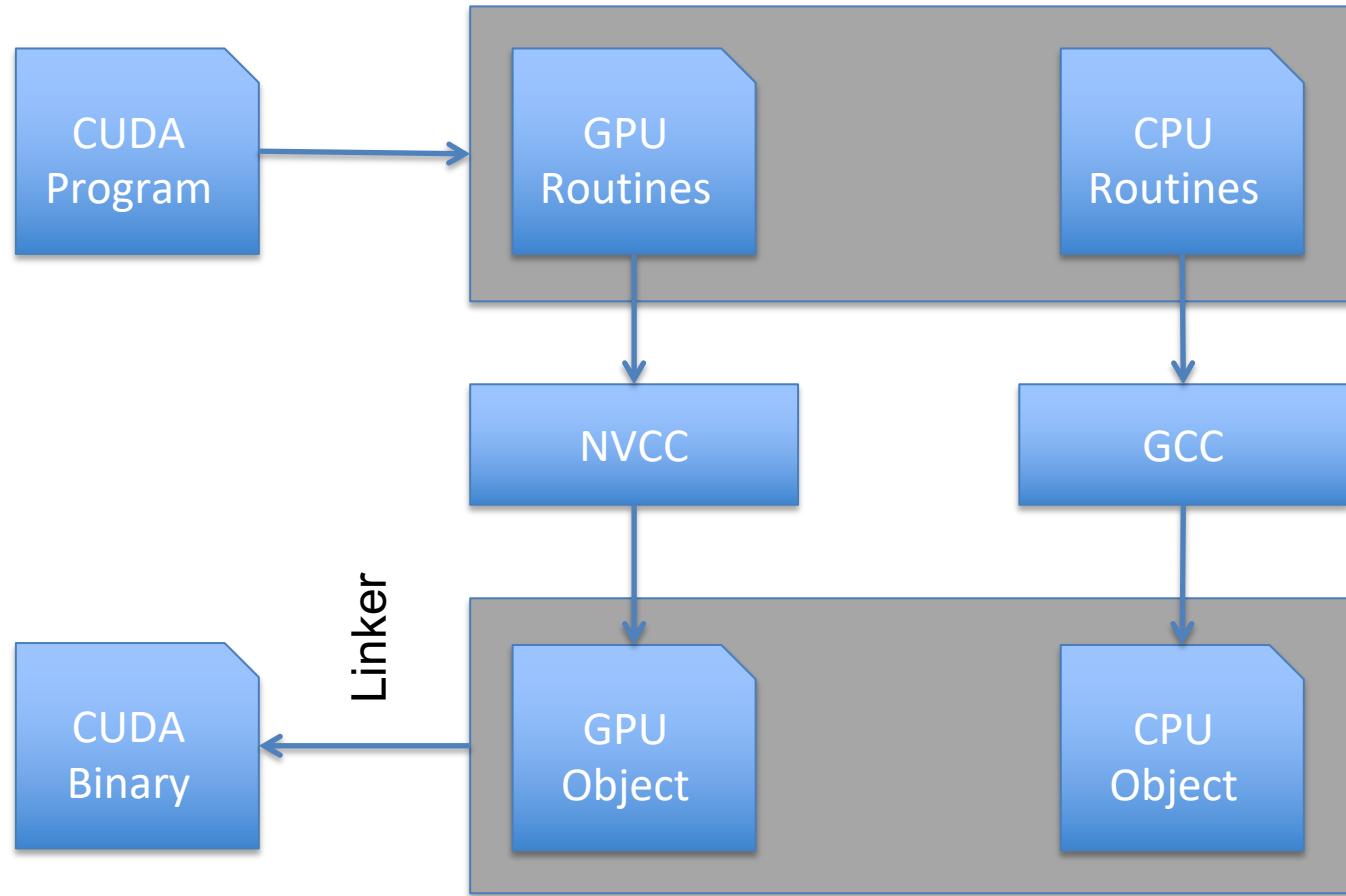
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# Heterogeneous Programming: CPU/GPU Code



# CUDA Program: An Example

mycode.cu

```
int main_data;
__shared__ int sdata;

Main() { }
__host__ hfunc () {
    int hdata;
    cudaMemcpy();
    gfunc<<<gs,bs>>>();
    cudaMemcpy();
}
__global__ gfunc() {
    int gdata;
    dfunc();
}
__device__ dfunc() {
    int ddata;
}
```

Host Only  
Interface  
Device Only

**Compiled by native compiler: gcc, icc, cc**

```
int main_data;
Main() {}
__host__ hfunc () {
    int hdata;
    cudaMemcpy();
    gfunc<<<gs,bz>>>();
    cudaMemcpy();
}
```

**Compiled by nvcc compiler**

```
__shared__ sdata;
__global__ gfunc() {
    int gdata;
    dfunc();
}
```

```
__device__ dfunc() {
    int ddata;
}
```



# CUDA: Minimal Extensions to C + API

## ■ Declaration specifiers

- ⊕ global, device, shared,  
local, constant

```
__device__ float filter[N];  
  
__global__ void convolve (float *image) {  
    __shared__ float region[M];  
    ...  
    region[threadIdx] = image[i];  
    ...  
    __syncthreads();  
    ...  
    image[j] = result;  
}  
  
int main() {  
    // Allocate GPU memory  
    void *myimage = cudaMalloc(...);  
  
    // 100 blocks, 10 threads per block  
    convolve<<<100, 10>>> (myimage);  
}
```

## ■ Keywords

- ⊕ threadIdx, blockIdx

## ■ Intrinsics

- ⊕ \_\_syncthreads

## ■ Runtime API

- ⊕ Memory, symbol,  
execution management

## ■ Function launch



# CUDA Programming Model: A Highly Multithreaded Coprocessor

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- The GPU is viewed as a compute **device** that:
  - ⊕ Is a coprocessor to the CPU or **host**
  - ⊕ Has its own DRAM (**device memory**)
  - ⊕ Runs many **threads in parallel**
- Data-parallel portions of an application are executed on the device as **kernels** which run in parallel on many threads
- Differences between GPU and CPU threads
  - ⊕ GPU threads are extremely lightweight
    - ◆ Very little creation overhead
  - ⊕ GPU needs 1000s of threads for full efficiency
    - ◆ Multi-core CPU needs only a few



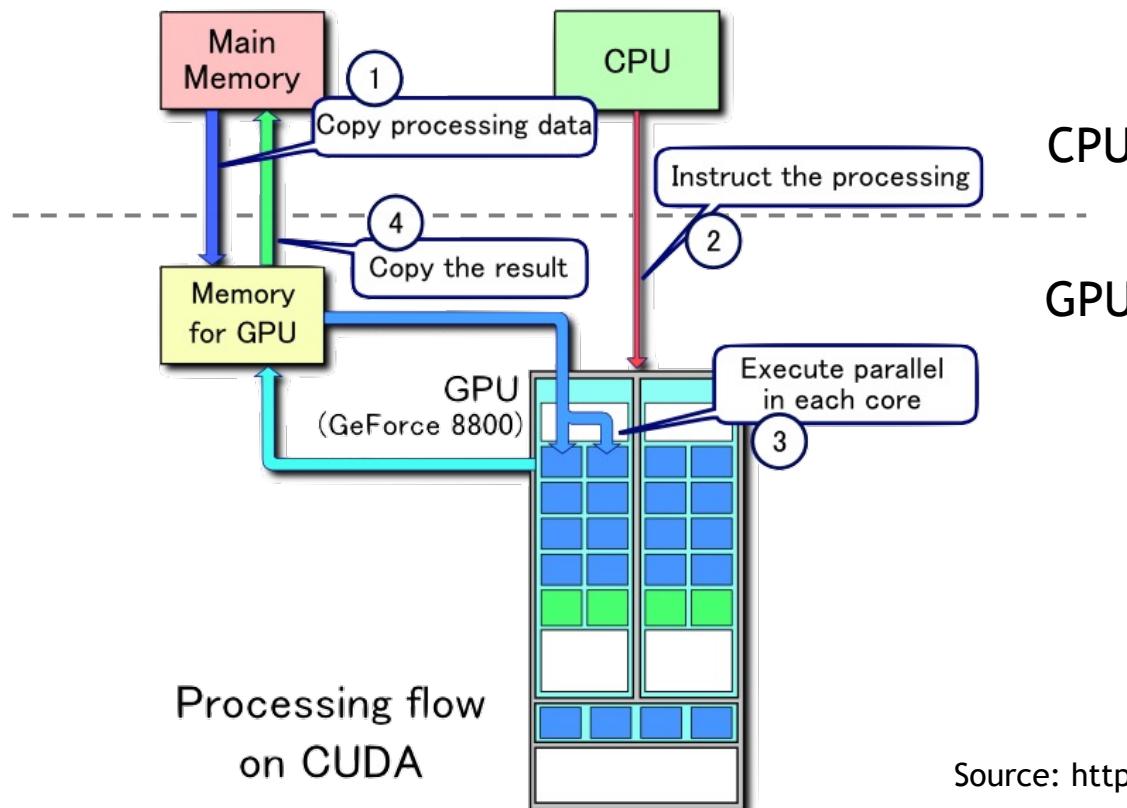
# What Programmer Expresses in CUDA

- Computation partitioning (where does computation occur?)
  - ⊕ Declarations on functions `__host__`, `__global__`, `__device__`
  - ⊕ Mapping of thread programs to device:  
`compute <<<gs, bs>>>(<args>)`
- Data partitioning (where does data reside, who may access it and how?)
  - ⊕ Declarations on data `__shared__`, `__device__`, `__constant__`, ...
- Data management and orchestration
  - ⊕ Copying to/from host: e.g.,  
`cudaMemcpy(h_obj, d_obj, cudaMemcpyDeviceToHost)`
- Concurrency management
  - ⊕ E.g. `__syncthreads()`



# Processing Flow on CUDA

1. Copy data from main mem to GPU mem
2. CPU instructs the process to GPU
3. GPU execute parallel in each core
4. Copy the result from GPU mem to main mem



Source: <http://en.wikipedia.org/wiki/CUDA>



# CUDA: A Scalable Programming Model

---

- A low learning curve for programmers familiar with standard programming languages such as C
- Three key abstractions
  - 1) A hierarchy of thread groups
  - 2) Shared memories
  - 3) Barrier synchronization



# CUDA Terminology

---

- **Host** - typically the CPU
  - ◆ Code written in ANSI C
    - ◆ Written in *extended* ANSI C when interacting with devices
- **Device** - typically the GPU (data-parallel)
  - ◆ Code written in *extended* ANSI C
- Host and device have separate memories
- CUDA Program
  - ◆ Contains both host and device code



# CUDA Terminology (Cont'd)

---

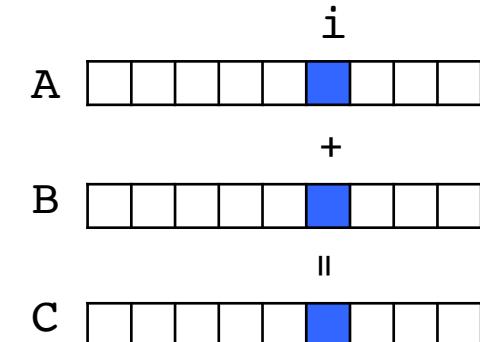
- ***Kernel*** - data-parallel function
  - ◆ Invoking a kernel creates lightweight threads on the device
    - ◆ Threads are generated and scheduled with hardware
- Similar to a ***shader*** in OpenGL



# CUDA Kernels

- Executed N times in parallel by N different *CUDA threads*

```
for (int i = 0; i < N; i++)  
    C[i] = A[i] + B[i];
```



Declaration  
Specifier

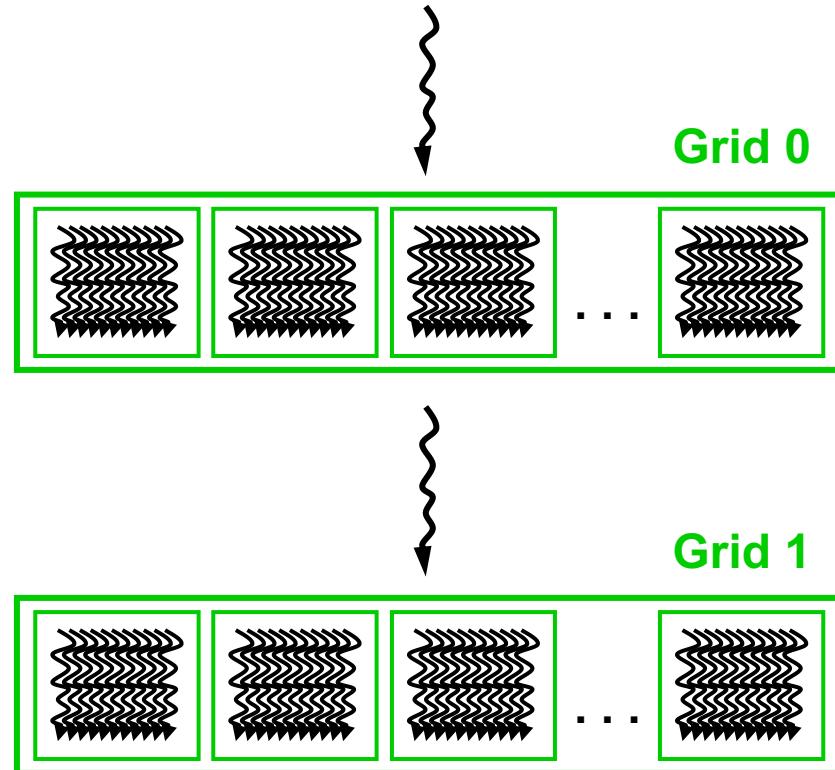
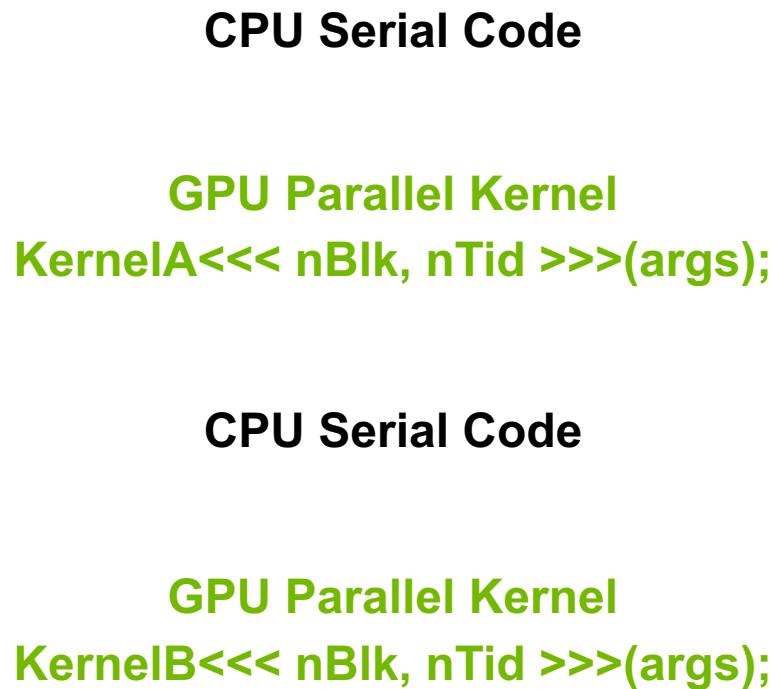
```
// Kernel definition  
__global__ void VecAdd(float* A, float* B, float* C)  
{  
    int i = threadIdx.x;  
    C[i] = A[i] + B[i];  
}  
  
int main()  
{  
    ...  
    // Kernel invocation with N threads  
    VecAdd<<<1, N>>>(A, B, C);  
}
```

Thread ID

Execution  
Configuration



# CUDA Program Execution



# Outline

---

- GPUs as Compute Engines
- GPU Architectures
  - ✿ GPU Threading Model
  - ✿ Separation of Memory Spaces
- Introduction to CUDA
  - ✿ Parallel Computing Platform
  - ✿ Programming Model
    - ◆ Built-in Data Types and Functions
    - ◆ Thread Model
    - ◆ Memory Model
  - ✿ Case Study: Matrix Multiplication
  - ✿ Thread Synchronization
  - ✿ Advanced Features



# Functional Declarations

	Executed on the:	Only callable from the:
<code>__global__ void KernelFunc()</code>	device	host
<code>__device__ float DeviceFunc()</code>	device	device
<code>__host__ float HostFunc()</code>	host	host

- `__global__`
  - Must return `void`
- `__device__`
  - Inlined by default for compute capability 1.x



# Functional Declarations

---

- What do these do?



`global host void func()`



`device host void func()`



# Functional Declarations

- What do these do?



~~`__global__ __host__ void func()`~~

~~`__device__ __host__ void func()`~~

```
__host__ __device__ func()
{
    #if __CUDA_ARCH__ == 100
        // Device code path for compute capability 1.0
    #elif __CUDA_ARCH__ == 200
        // Device code path for compute capability 2.0
    #elif !defined(__CUDA_ARCH__)
        // Host code path
    #endif
}
```



# Functional Declarations

---

- Global and device functions
  - No recursion (made available after Fermi)
  - No static variables
  - No malloc () (made available after Fermi)
  - Careful with function calls through pointers
    - Can't take the address of a \_\_device\_\_ function in host code



# Vector Types

---

- `char[1-4], uchar[1-4]`
- `short[1-4], ushort[1-4]`
- `int[1-4], uint[1-4]`
- `long[1-4], ulong[1-4]`
- `longlong[1-4], ulonglong[1-4]`
- `float[1-4]`
- `double1, double2`



# Vector Types

---

- Available in host and device code
- Construct with `make_<type name>`

```
int2 i2 = make_int2(1, 2);  
float4 f4 = make_float4(  
    1.0f, 2.0f, 3.0f, 4.0f);
```



# Vector Types

---

- Access with `.x`, `.y`, `.z`, and `.w`

```
int2 i2 = make_int2(1, 2);  
int x = i2.x;  
int y = i2.y;
```

- No `.r`, `.g`, `.b`, `.a`, etc. like GLSL



# Math Functions

---

- **double** and **float** overloads
  - ⊕ No vector overloads
- On the host, functions use the C runtime implementation if available
- On the device, SFU are likely used

```
// addition
inline __host__ __device__ int2 operator+(int2 a, int2 b){
    return make_int2(a.x + b.x, a.y + b.y);
}
```



# Math Functions

---

## ■ Partial list:

- ◆ `sqrt`, `rsqrt`
- ◆ `exp`, `log`
- ◆ `sin`, `cos`, `tan`, `sincos`
- ◆ `asin`, `acos`, `atan2`
- ◆ `trunc`, `ceil`, `floor`



# Math Functions

---

## ■ *Intrinsic* function

- Device only
- Faster, but less accurate
- Prefixed with `_`
- `_exp`, `_log` , `_sin` , `_pow` , ...



# Outline

---

- GPUs as Compute Engines
- GPU Architectures
  - ✿ GPU Threading Model
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- Introduction to CUDA
  - ✿ Parallel Computing Platform
  - ✿ Programming Model
    - ◆ Built-in Data Types and Functions
    - ◆ **Thread Model**
    - ◆ Memory Model
  - ✿ Case Study: Matrix Multiplication
  - ✿ Thread Synchronization
  - ✿ Advanced Features



# Thread Hierarchies

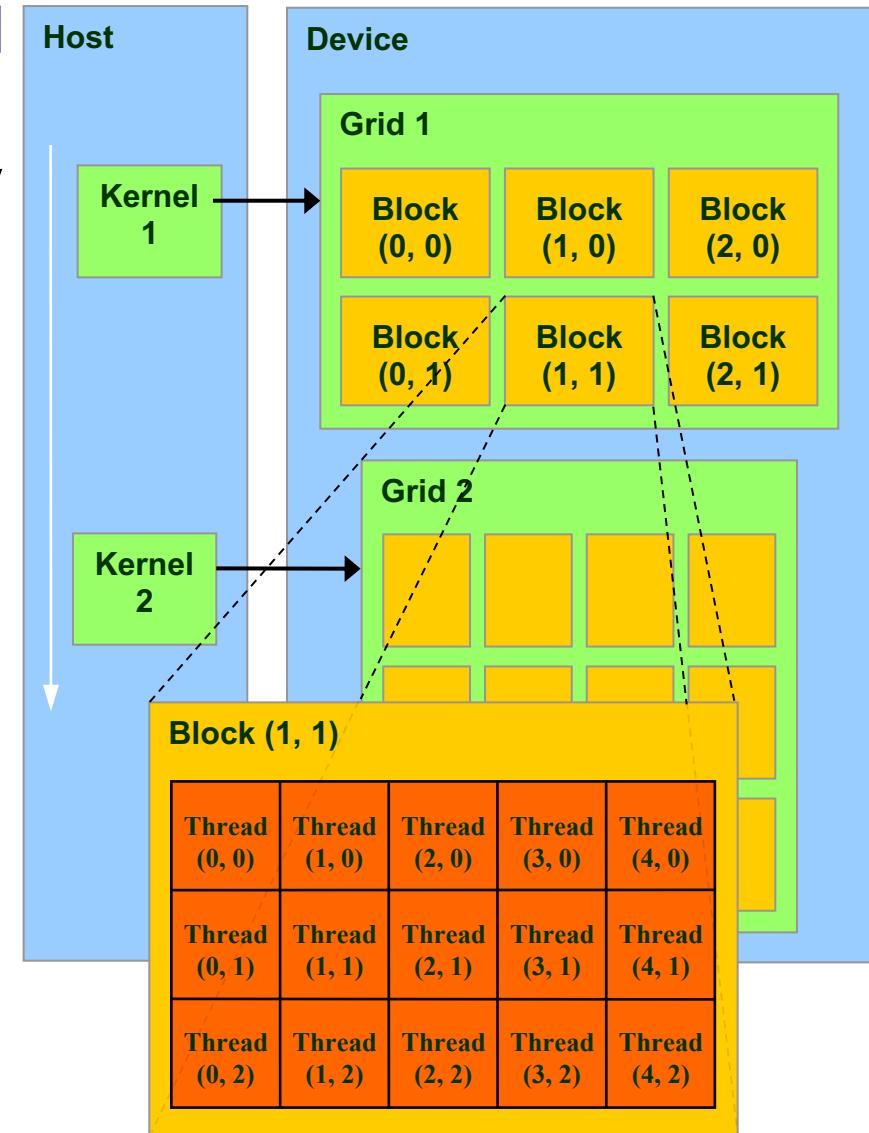
- A kernel is executed as a grid of thread blocks

- All threads share data memory space

- A **thread block** is a batch of threads that can **cooperate** with each other by:

- Synchronizing their execution
  - For hazard-free shared memory accesses
- Efficiently sharing data through a low latency **shared memory**

- Two threads from two different blocks cannot cooperate



# Thread Hierarchies

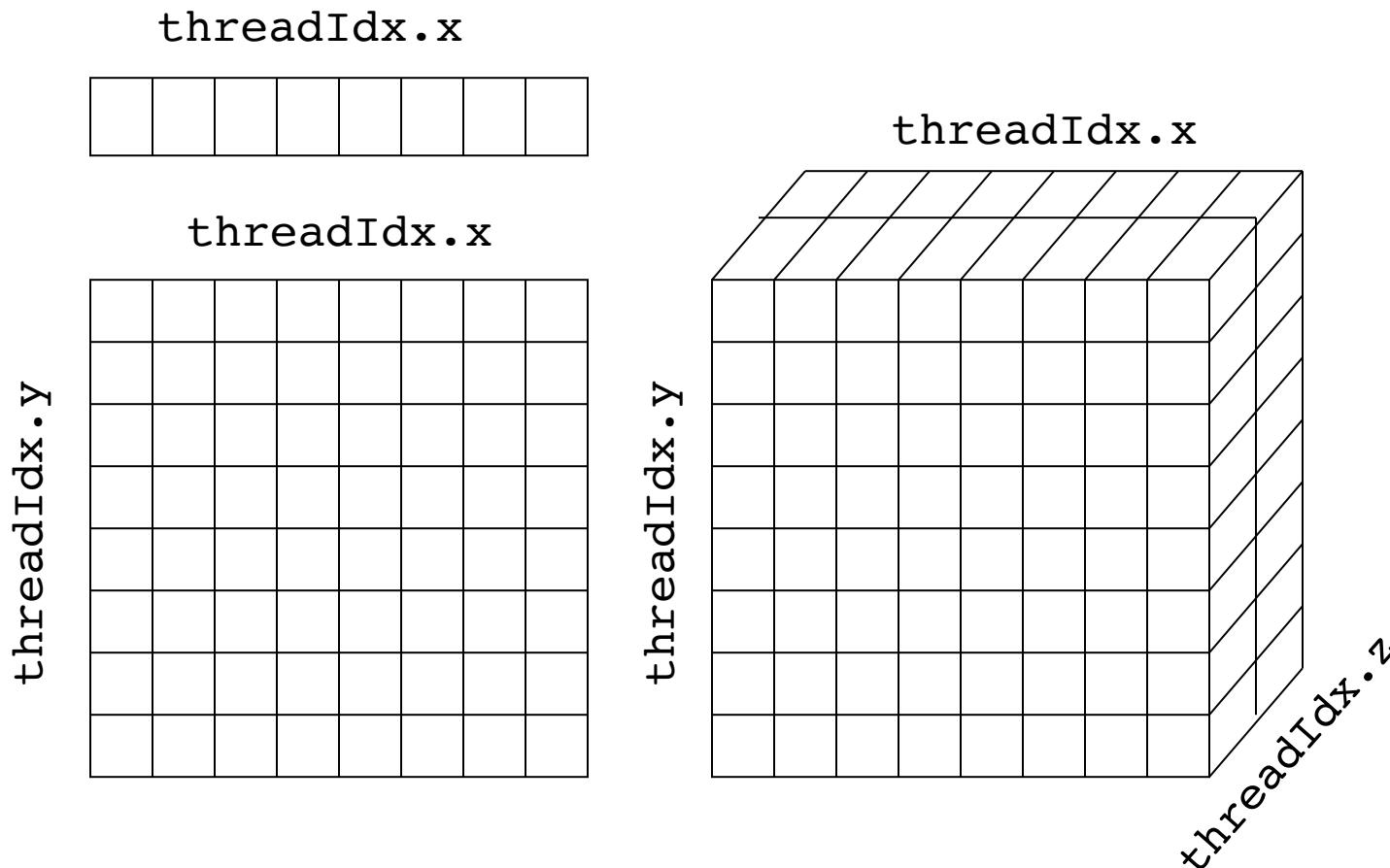
---

- ***Grid*** - one or more thread blocks
  - ◆ 1D or 2D
- ***Block*** - array of threads
  - ◆ 1D, 2D, or 3D
  - ◆ Each block in a grid has the same number of threads
  - ◆ Each thread in a block can
    - ◆ Synchronize
    - ◆ Access shared memory

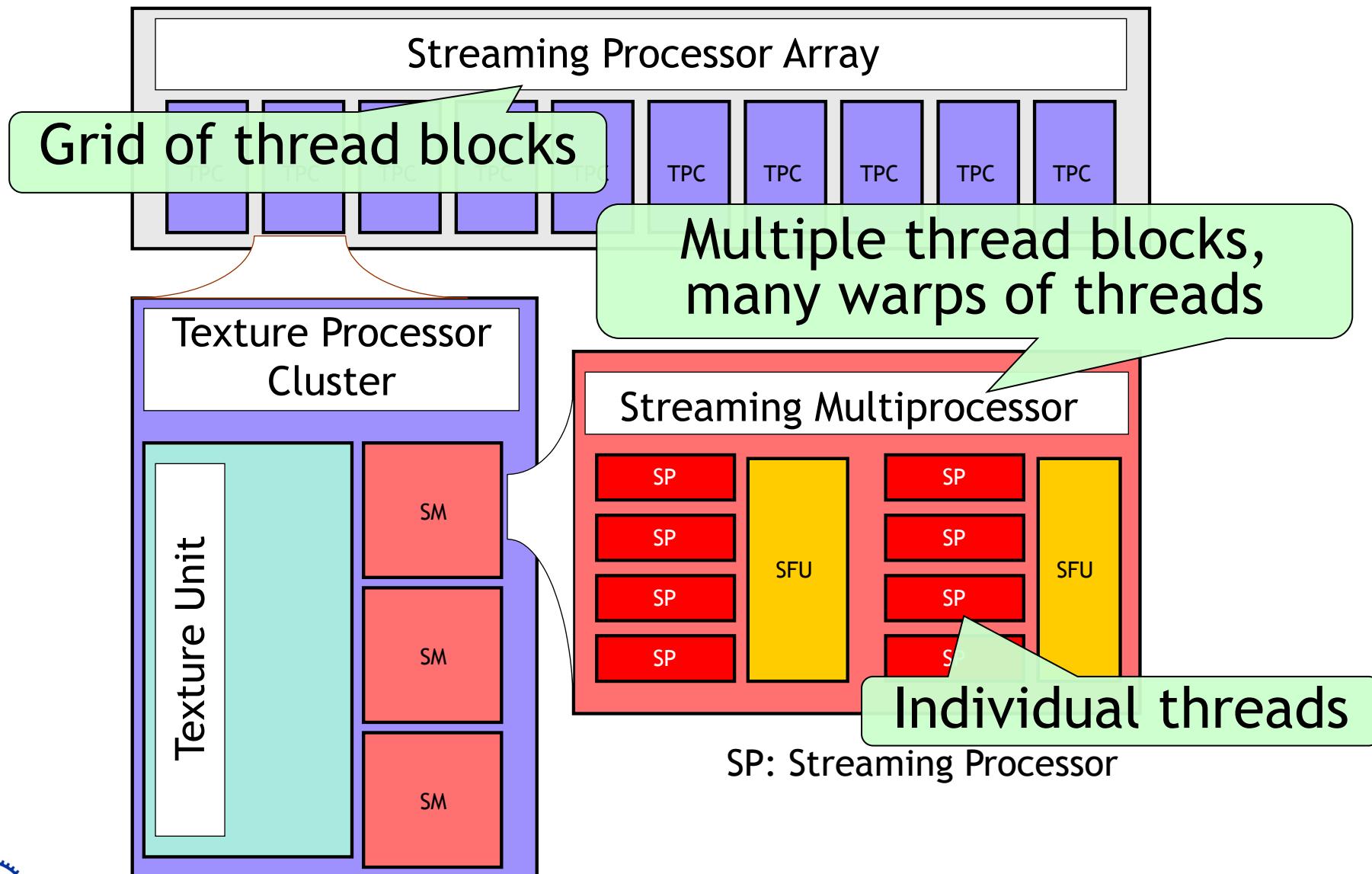


# Thread Hierarchies

- **Block** - 1D, 2D, or 3D
  - ✿ Example: Index into vector, matrix, volume



# CUDA: Parallel Computing Platform



# Thread ID

- *Thread ID*: Scalar thread identifier
- Thread Index: `threadIdx`

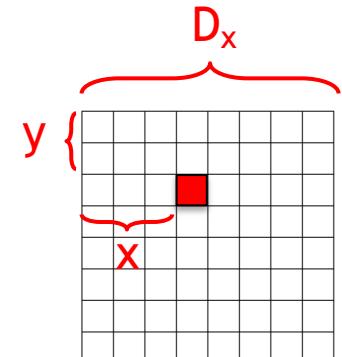
- 1D: Thread ID == Thread Index

- 2D with size ( $D_x, D_y$ )

- ⊕ Thread ID of index  $(x, y) == x + y D_x$

- 3D with size ( $D_x, D_y, D_z$ )

- ⊕ Thread ID of index  $(x, y, z) == x + y D_x + z D_x D_y$

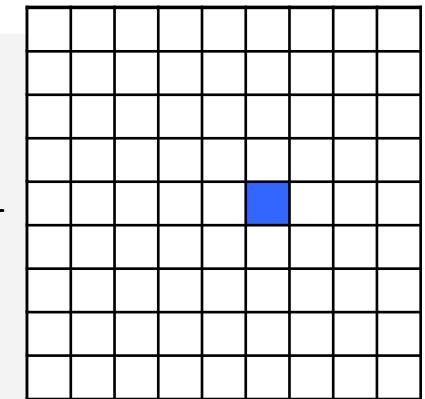


# Thread ID

```
for (int i = 0; i < N; i++)
    for (int j = 0; j < N; j++)
        C[i][j] = A[i][j] + B[i][j];
```

```
// Kernel definition
__global__ void MatAdd(float A[N][N], float B[N][N],
                      float C[N][N])
{
    int j = threadIdx.x;
    int i = threadIdx.y;
    C[i][j] = A[i][j] + B[i][j];
}

int main()
{
    ...
    // Kernel invocation with one block of N * N * 1 threads
    int numBlocks = 1;
    dim3 threadsPerBlock(N, N);
    MatAdd(<<numBlocks, threadsPerBlock>>(A, B, C));
}
```



1 Thread Block

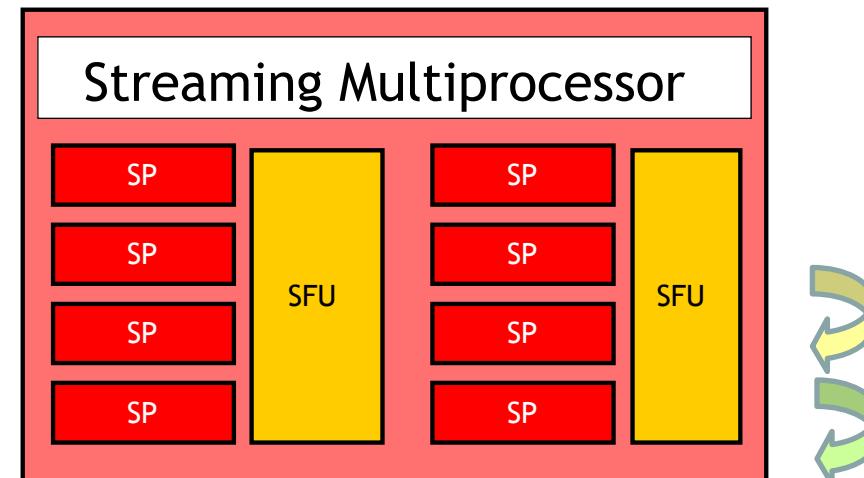
2D Block



# Thread Hierarchies

## Thread Block

- ❖ Group of threads
  - ◆ Size is defined by programmer
  - ◆ G80 and GT200: Up to 512 threads
  - ◆ Fermi and Kepler: Up to 1024 threads
- ❖ Reside on same SM
- ❖ Share memory of that core



# Block ID

---

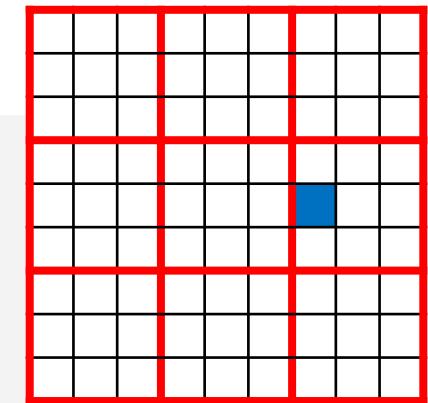
- **Block Index:** `blockIdx`
- **Dimension:** `blockDim`
  - ⊕ 1D or 2D



# Thread Hierarchies

```
// Kernel definition
__global__ void MatAdd(float A[N][N], float B[N][N],
                      float C[N][N])
{
    int j = blockIdx.x * blockDim.x + threadIdx.x;
    int i = blockIdx.y * blockDim.y + threadIdx.y;
    if (i < N && j < N)
        C[i][j] = A[i][j] + B[i][j];
}

int main()
{
    ...
    // Kernel invocation
    dim3 threadsPerBlock(16, 16);
    dim3 numBlocks(N / threadsPerBlock.x, N / threadsPerBlock.y);
    MatAdd<<<numBlocks, threadsPerBlock>>>(A, B, C);
}
```



16x16  
Threads per block

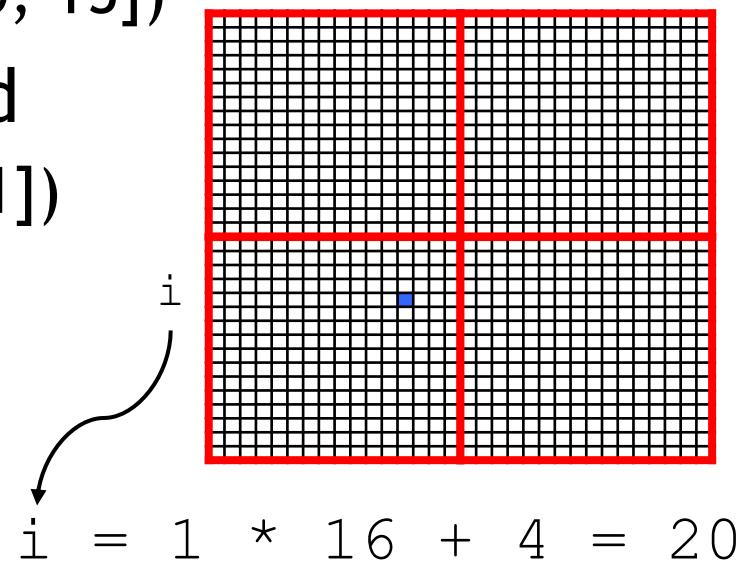
2D Thread Block



# Thread Hierarchies

## ■ Example: $N = 32$

- ✿ 16x16 threads per block (independent of  $N$ )
  - ◆ `threadIdx` ( $[0, 15], [0, 15]$ )
- ✿ 2x2 thread blocks in grid
  - ◆ `blockIdx` ( $[0, 1], [0, 1]$ )
  - ◆ `blockDim` = 16



```
int j = blockIdx.x * blockDim.x + threadIdx.x;
int i = blockIdx.y * blockDim.y + threadIdx.y;
```

■  $i = [0, 1] * 16 + [0, 15]$



# Thread Hierarchies

---

- Blocks execute independently
  - ✿ Each thread block is assigned to an SM to execute
  - ✿ In any order:
    - ◆ parallel (interleaved or not) or
    - ◆ series
  - ✿ Scheduled in any order by any number of cores
    - ◆ Allows code to scale with core count



# Review: Thread Hierarchies

```
int threadID = blockIdx.x *  
blockDim.x + threadIdx.x;
```

```
float x = input[threadID];  
float y = func(x);  
output[threadID] = y;
```

Use grid and block position to  
compute a thread id



# Review: Thread Hierarchies

```
int threadID = blockIdx.x *  
blockDim.x + threadIdx.x;
```

```
float x = input[threadID];
```

```
float y = func(x);
```

```
output[threadID] = y;
```

Use thread id to read from input



# Review: Thread Hierarchies

```
int threadID = blockIdx.x *  
blockDim.x + threadIdx.x;  
float x = input[threadID];  
float y = func(x);  
output[threadID] = y;
```

Run function on input: data-parallel!



# Review: Thread Hierarchies

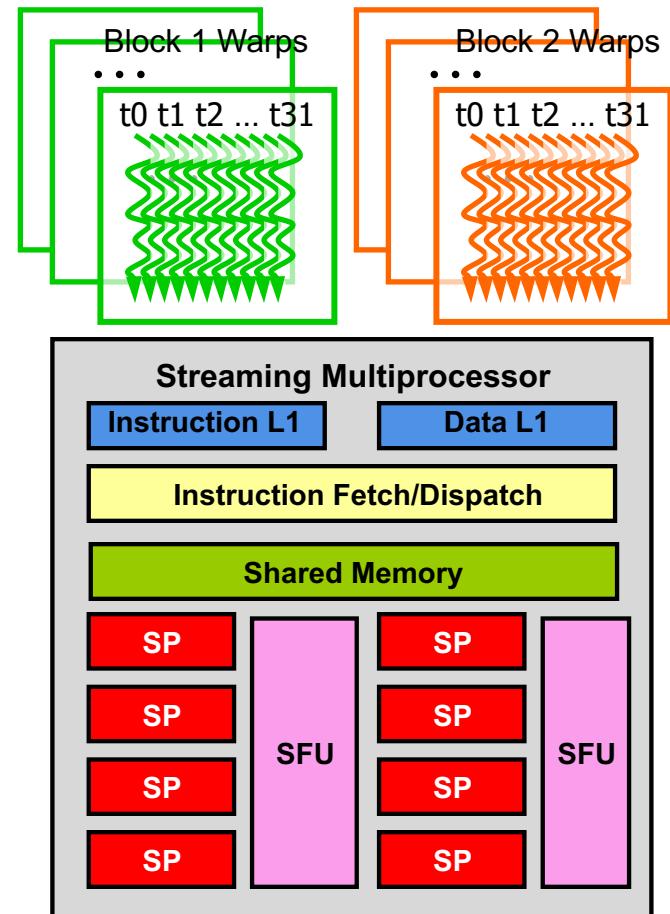
```
int threadID = blockIdx.x *  
    blockDim.x + threadIdx.x;  
float x = input[threadID];  
float y = func(x);  
output[threadID] = y;
```

Use thread id to output result



# Scheduling Threads

- Each Thread Block is divided in 32-thread **Warps**
  - ◆ This is an implementation decision, not part of the CUDA programming model
- Warps are the basic scheduling units in SM
- Example (draws on figure at right):
  - ◆ Assume 2 Blocks are processed by an SM and each Block has 512 threads, how many Warps are managed by the SM?
    - ◆ Each Block is divided into  $512/32 = 16$  Warps
    - ◆ There are  $16 * 2 = 32$  Warps
    - ◆ At any point in time, only *\*one\** of the 32 Warps will be selected for instruction fetch and execution.

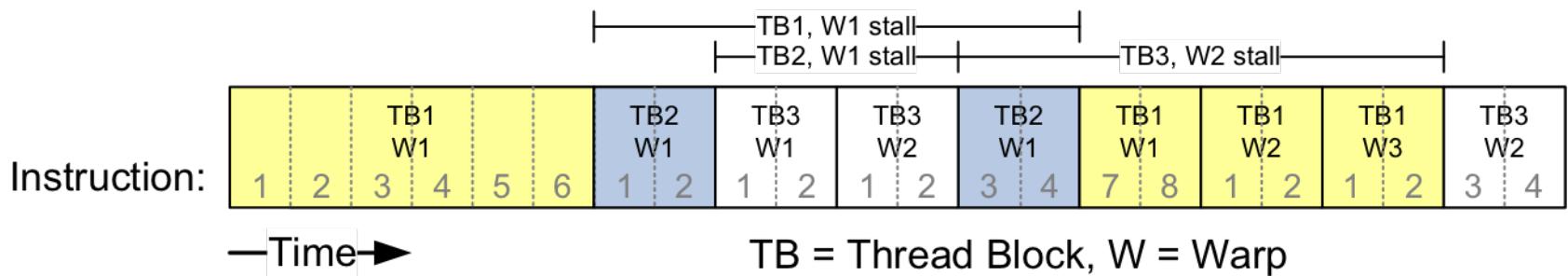


Fermi+ GPUs: each SM has two warp schedulers

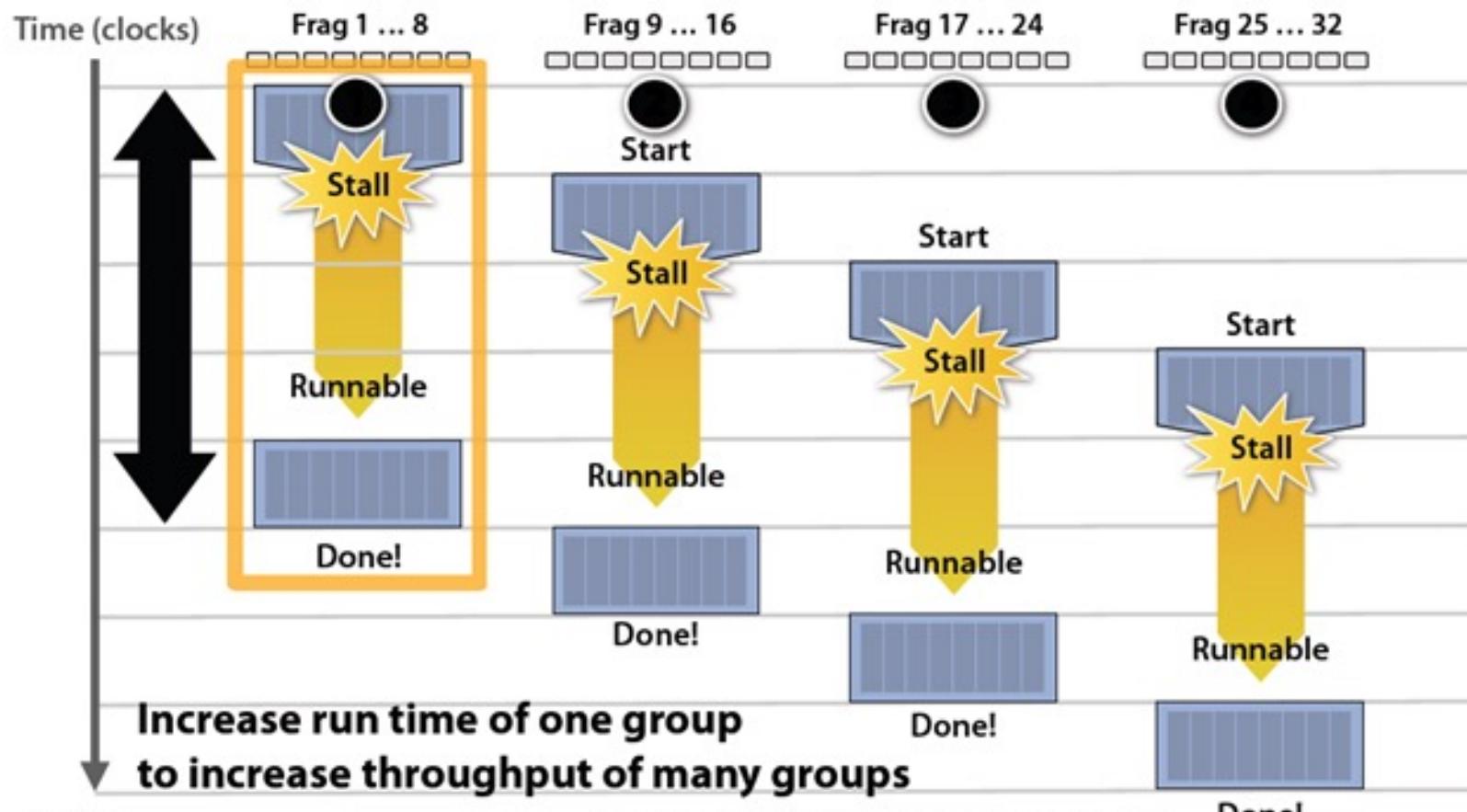


# SM Warp Scheduling

- SM implements zero-overhead warp scheduling
  - At any time, only one of the warps is executed by SM
  - Warps whose next instruction has its operands ready for consumption are eligible for execution
  - Eligible warps are selected for execution on a prioritized scheduling policy
  - All threads in a warp execute the same instruction when selected



# SM Warp Scheduling



07/29/10

Beyond Programmable Shading Course, ACM SIGGRAPH 2010



Image from: [http://bps10.idav.ucdavis.edu/talks/03-fatahalian\\_gpuArchTeraflop\\_BPS\\_SIGGRAPH2010.pdf](http://bps10.idav.ucdavis.edu/talks/03-fatahalian_gpuArchTeraflop_BPS_SIGGRAPH2010.pdf)



# Scheduling Threads

- What happens if branches in a warp diverge?

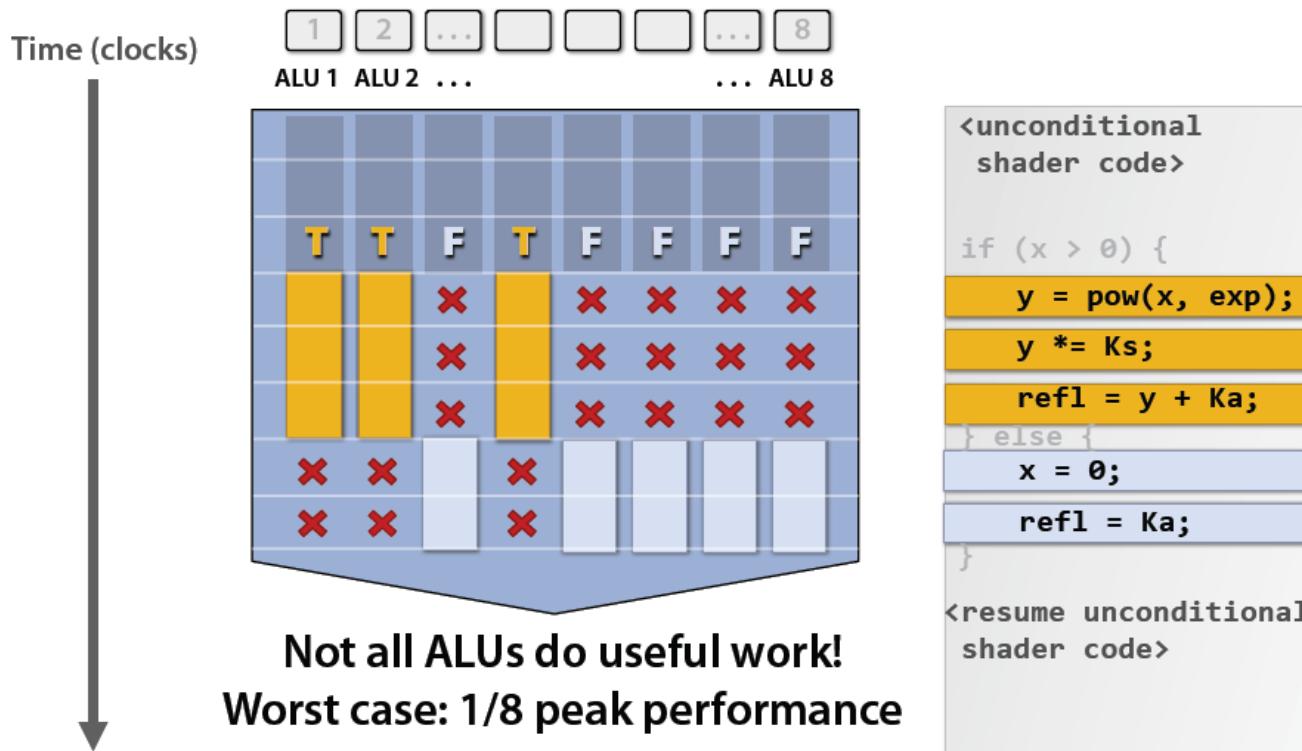


Image from: [http://bps10.idav.ucdavis.edu/talks/03-fatahalian\\_gpuArchTeraflop\\_BPS\\_SIGGRAPH2010.pdf](http://bps10.idav.ucdavis.edu/talks/03-fatahalian_gpuArchTeraflop_BPS_SIGGRAPH2010.pdf)



# Outline

---

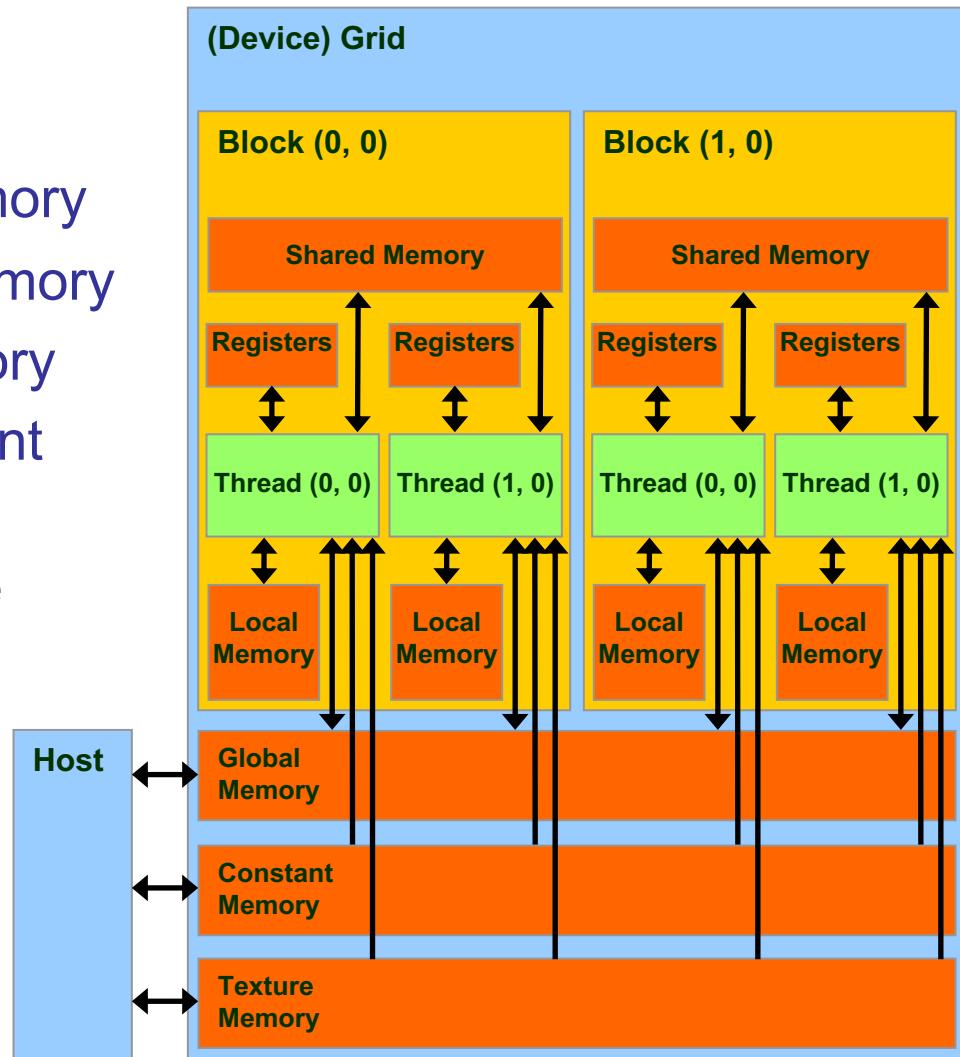
- GPUs as Compute Engines
- GPU Architectures
  - ✿ GPU Threading Model
  - ✿ Separation of Memory Spaces
- Introduction to CUDA
  - ✿ Parallel Computing Platform
  - ✿ Programming Model
    - ◆ Built-in Data Types and Functions
    - ◆ Thread Model
    - ◆ **Memory Model**
  - ✿ Case Study: Matrix Multiplication
  - ✿ Thread Synchronization
  - ✿ Advanced Features



# CUDA Memory Model

## Each thread can:

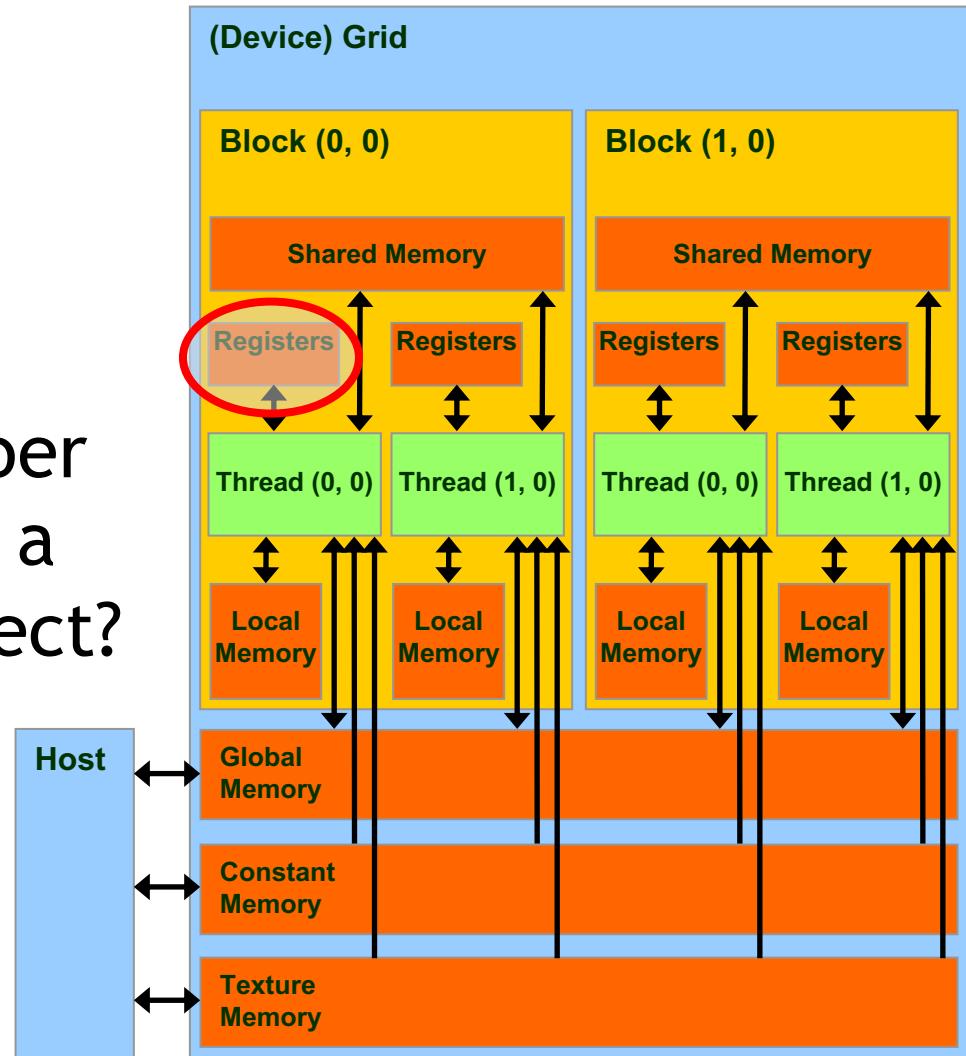
- R/W per-thread registers
- R/W per-thread local memory
- R/W per-block shared memory
- R/W per-grid global memory
- Read only per-grid constant memory
- Read only per-grid texture memory



# Memory Model

## Registers

- Per thread
- Fast, on-chip, read/write access
- Increasing the number of registers used by a kernel has what affect?



# Memory Model

---

## ■ Registers - G80

- ◆ Per SM
  - ◆ Up to 768 threads to interleavingly execute
  - ◆ 8K registers
- ◆ How many registers per thread?



# Memory Model

---

## ■ Registers - G80

- ◆  $8K / 768 = 10$  registers per thread
- ◆ Exceeding limit reduces threads by the block
- ◆ Example: Each thread uses 11 registers, and each block has 256 threads
  - ◆ How many threads can an SM host?
  - ◆ How many warps can an SM host?
  - ◆ What does having less warps mean?

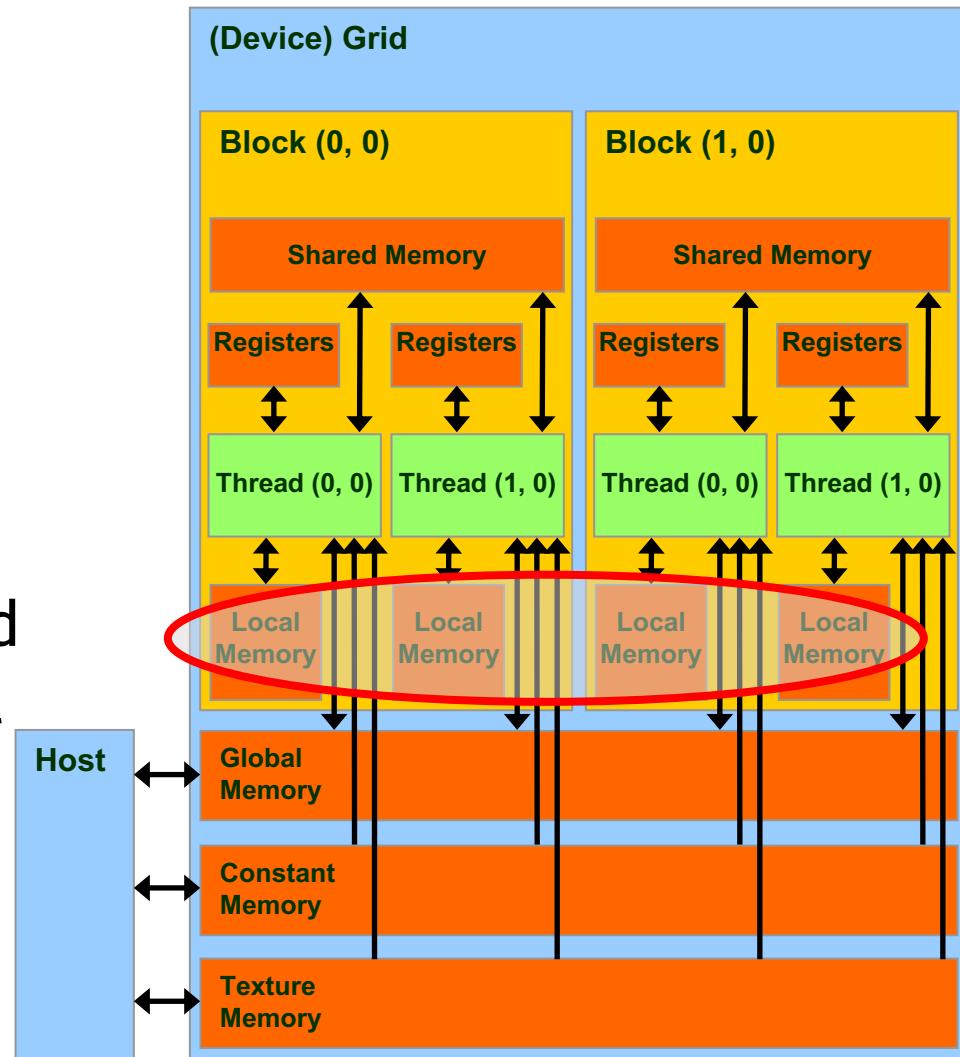
[https://docs.nvidia.com/cuda/cuda-occupancy-calculator/CUDA\\_Occupancy\\_Calculator.xls](https://docs.nvidia.com/cuda/cuda-occupancy-calculator/CUDA_Occupancy_Calculator.xls)



# Memory Model

## Local Memory

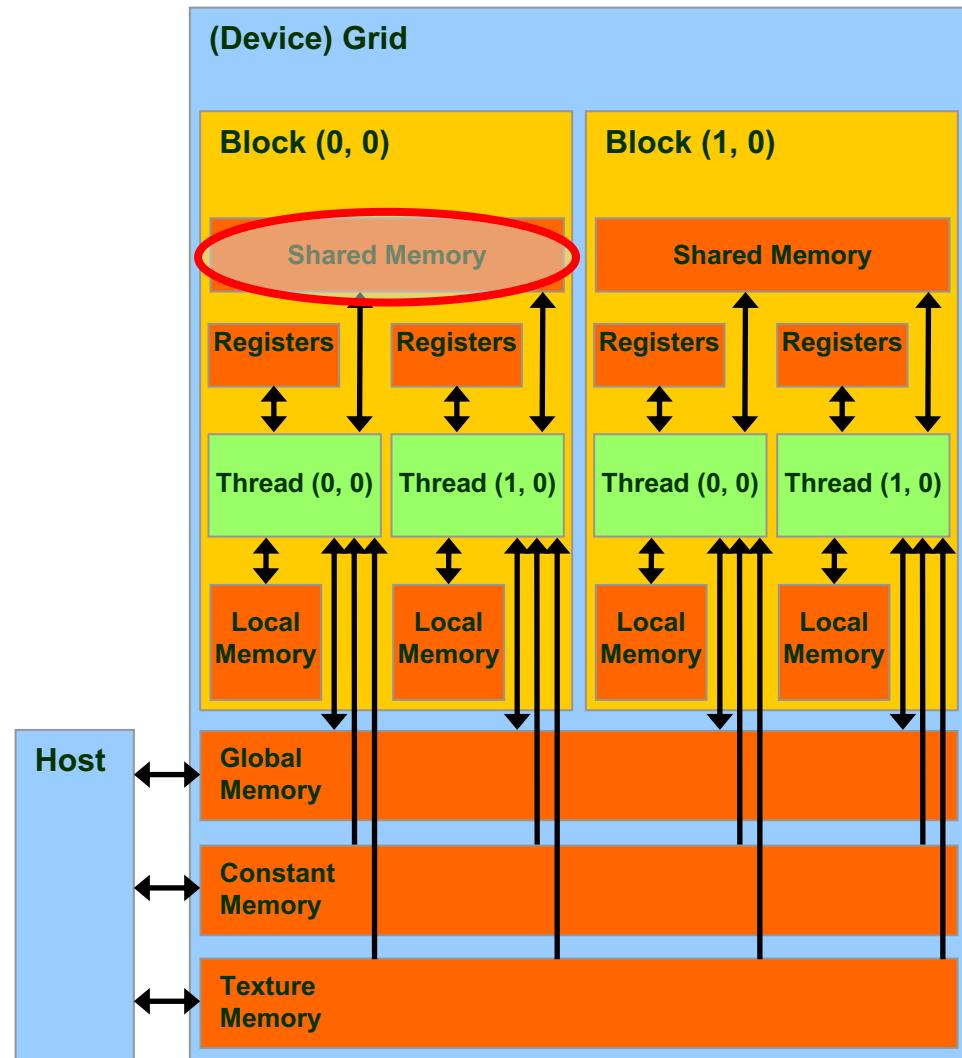
- Stored in global memory
  - Copy per thread
- Used for automatic arrays
  - Unless all accessed with only constant indices



# Memory Model

## ■ Shared Memory

- Per block
- Fast, on-chip, read/write access
- Full speed random access



# Memory Model

---

- Shared Memory - G80
  - ✿ Per SM
    - ◆ Up to 8 blocks
    - ◆ 16 KB
  - ✿ How many KB per block



# Memory Model

---

## ■ Shared Memory - G80

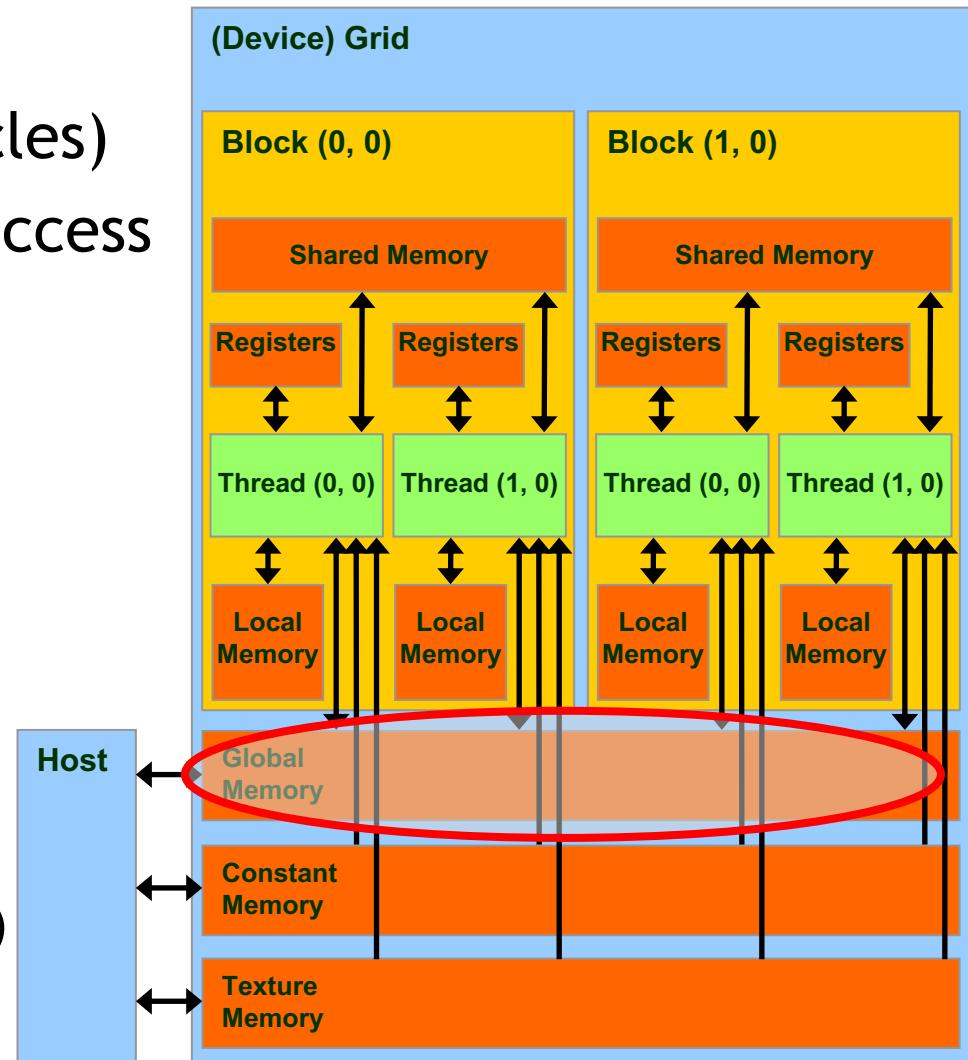
- ◆  $16\text{ KB} / 8 = 2\text{ KB}$  per block
- ◆ Example
  - ◆ If each block uses 5 KB, how many blocks can a SM host?



# Memory Model

## Global Memory

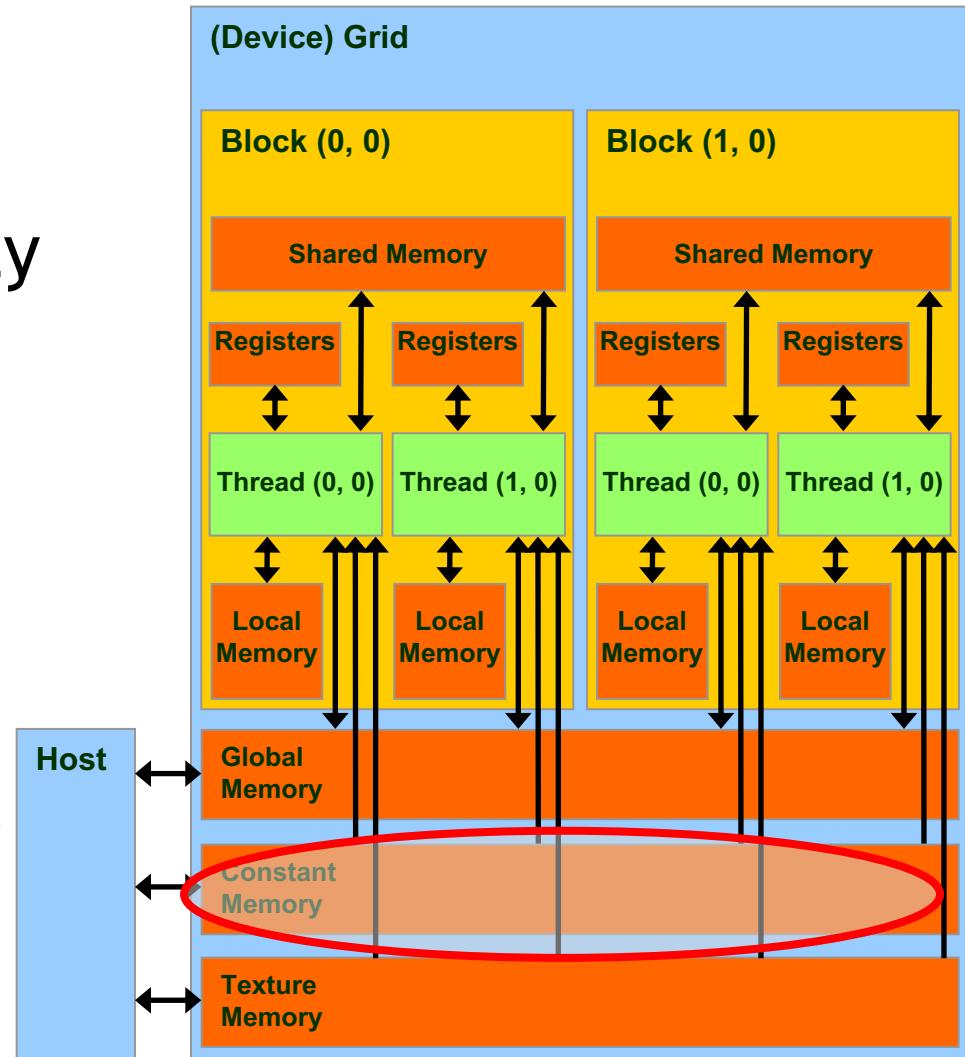
- Long latency (100s cycles)
- Off-chip, read/write access
- Random access causes performance hit
- Host can read/write
- G80 - 86.4 GB/s
- GT200
  - ◆ 150 GB/s
  - ◆ Up to 4 GB
- Tesla K20 (Kepler GK110)
  - ◆ Up to 208 GB/s
  - ◆ Up to 5GB



# Memory Model

## Constant Memory

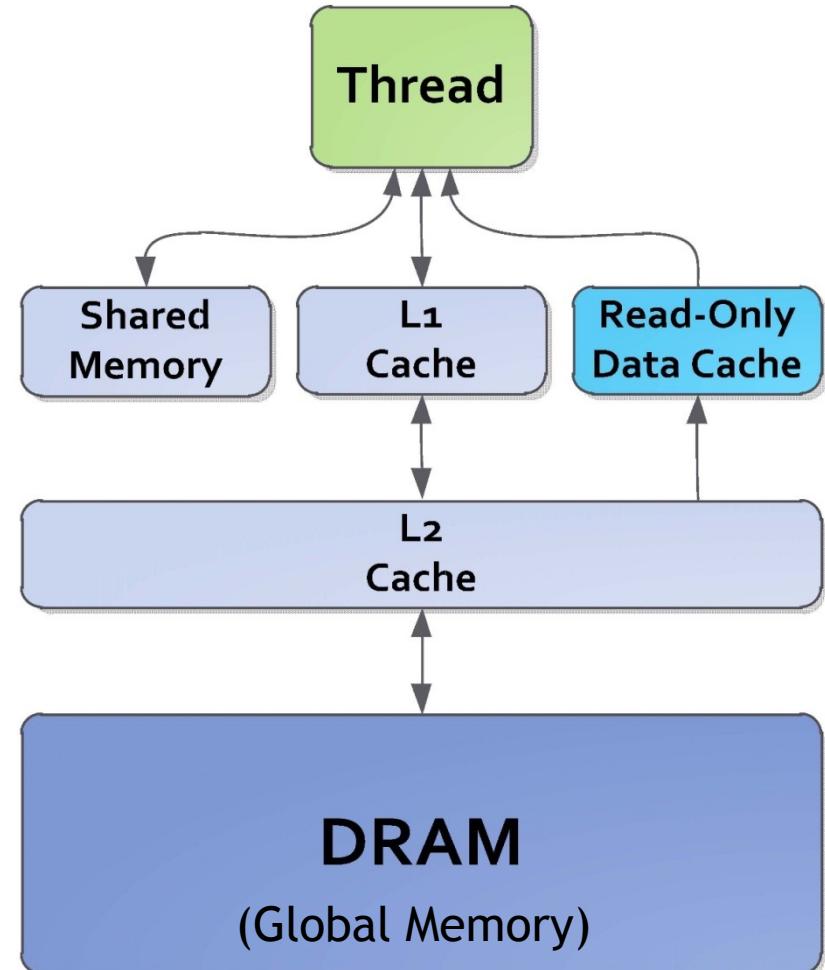
- Short latency, high bandwidth, read only access when all threads access the same location
- Stored in global memory but cached
- Host can read/write
- Up to 64 KB



# Kepler Memory Hierarchy

- Shared memory/L1 cache split
- Each SMX has 64 KB on-chip memory, that can be configured as:
  - 48 KB of shared memory with 16 KB of L1 cache,
  - 16 KB of shared memory with 48 KB of L1 cache, or
  - (new) a 32KB / 32KB split between shared memory and L1 cache.

## Kepler Memory Hierarchy



Source: <http://www.nvidia.com/content/PDF/kepler/NVIDIA-Kepler-GK110-Architecture-Whitepaper.pdf>



# Memory Model

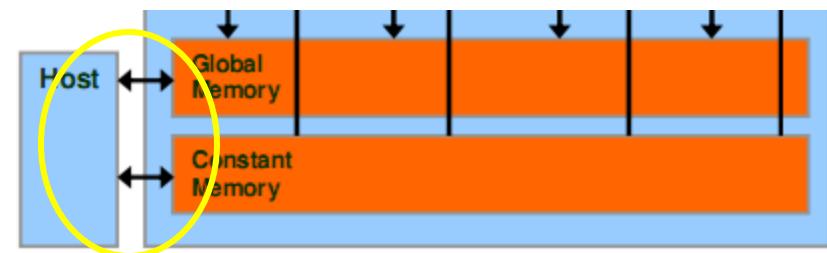
Variable Declaration	Memory	Scope	Lifetime
Automatic variables other than arrays	register	thread	kernel
Automatic array variables	local	thread	kernel
<code>__shared__ int sharedVar;</code>	shared	block	kernel
<code>__device__ int globalVar;</code>	global	grid	application
<code>__constant__ int constantVar;</code>	constant	grid	application

- `__shared__` is used within kernels
- `__device__` and `__constant__` is used outside kernels



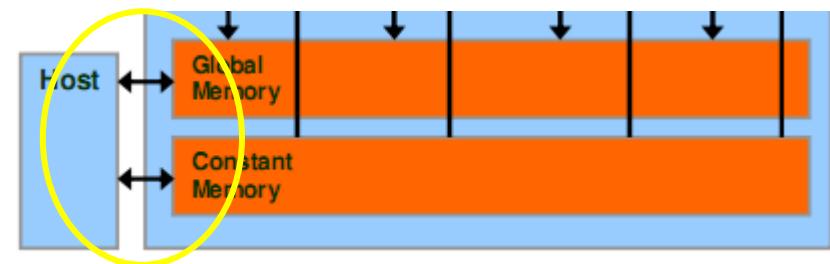
# CUDA Memory Transfers

- Host can transfer to/from device
  - ✳ *Global* memory
  - ✳ *Constant* memory



# CUDA Memory Transfers

- `cudaMalloc()`
  - ❖ To allocate global memory on device
- `cudaFree()`
  - ❖ To free memory
- Can only be called by the host
  - ❖ Starting from compute capability 3.5, they can be used in a kernel



# CUDA Memory Transfers

---

```
float *Md  
int size = Width * Width * sizeof(float);  
cudaMalloc( (void**) &Md, size);  
...  
cudaFree(Md);
```



# CUDA Memory Transfers

```
float *Md  
int size = Width * Width * sizeof(float);  
  
cudaMalloc( (void**) &Md, size );  
...  
cudaFree(Md);
```

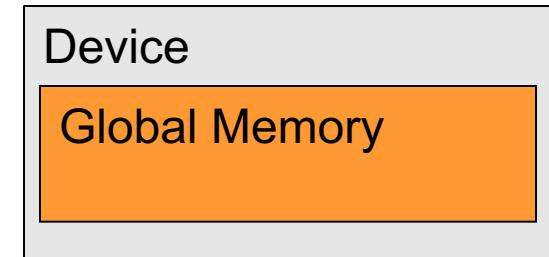
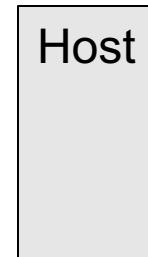
Pointer to device memory

Size in bytes



# CUDA Memory Transfers

- `cudaMemcpy()`
  - Memory transfer
    - ◆ Host to host
    - ◆ Host to device
    - ◆ Device to host
    - ◆ Device to device



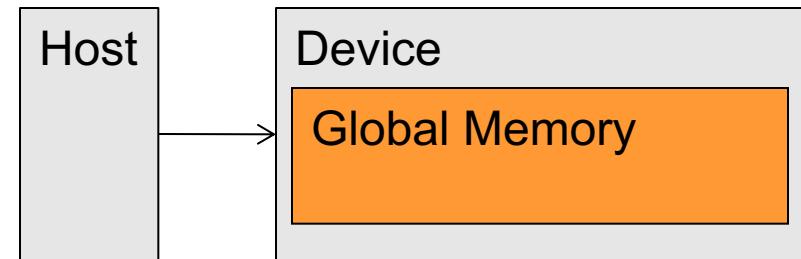
# CUDA Memory Transfers

- `cudaMemcpy()`
  - Memory transfer
    - ◆ Host to host
    - ◆ Host to device
    - ◆ Device to host
    - ◆ Device to device



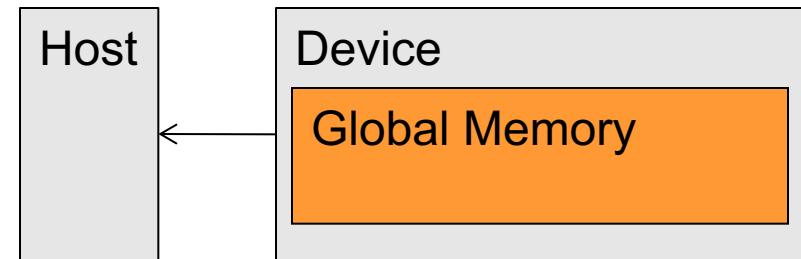
# CUDA Memory Transfers

- `cudaMemcpy()`
  - Memory transfer
    - ◆ Host to host
    - ◆ **Host to device**
    - ◆ Device to host
    - ◆ Device to device



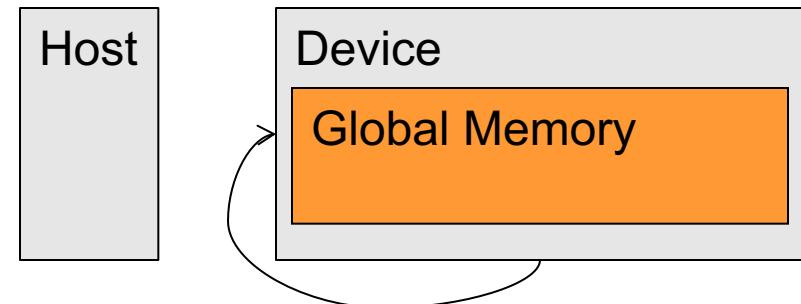
# CUDA Memory Transfers

- `cudaMemcpy()`
  - Memory transfer
    - ◆ Host to host
    - ◆ Host to device
    - ◆ Device to host
    - ◆ Device to device

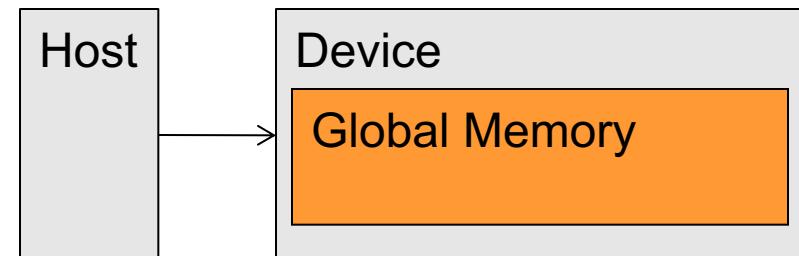
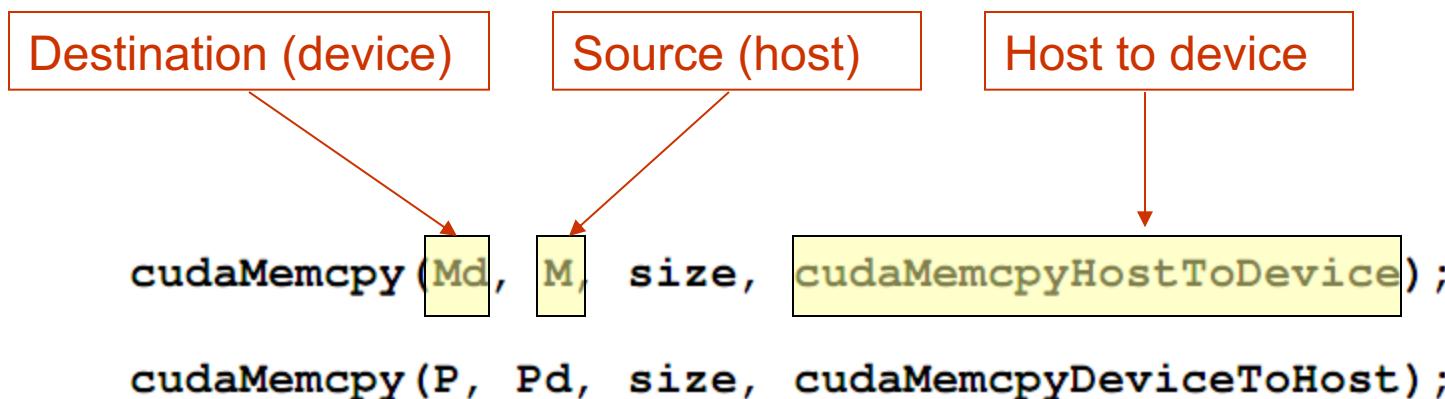


# CUDA Memory Transfers

- `cudaMemcpy()`
  - Memory transfer
    - ◆ Host to host
    - ◆ Host to device
    - ◆ Device to host
    - ◆ Device to device

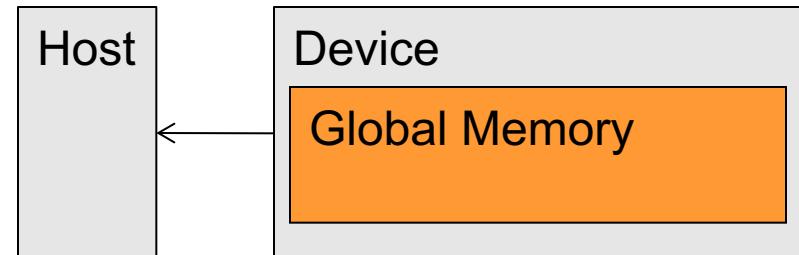


# CUDA Memory Transfers



# CUDA Memory Transfers

```
cudaMemcpy (Md, M, size, cudaMemcpyHostToDevice) ;  
cudaMemcpy (P, Pd, size, cudaMemcpyDeviceToHost) ;
```



# Unified Virtual Addressing (UVA)

- CUDA 4.0 introduced one (virtual) address space for all CPU and GPUs memory:
  - automatically detects physical memory location from pointer value
  - enables libraries to simplify their interfaces (e.g. cudaMemcpy)

Pre-UVA	UVA
Each source-destination permutation has its own option	Same interface
cudaMemcpyHostToHost cudaMemcpyHostToDevice cudaMemcpyDeviceToHost cudaMemcpyDeviceToDevice	cudaMemcpyDefault

```
cudaMemcpy(gpu0_buf, gpu1_buf, buf_size, cudaMemcpyDefault);
```



# Unified Memory

---

- Data are moved between CPU and GPU RAM on demand
  - ✿ It's similar to manual copying before/after kernel call, but automatically managed by the CUDA
- Allocate memory using `cudaMallocManaged`
  - ✿ The CUDA runtime will take care of the transfers
  - ✿ No need to call `cudaMemcpy` any more
  - ✿ Behaves as if you had a single memory space
- Suboptimal performance: software-managed coherency
  - ✿ Still call `cudaMemcpy` when you can
- Requires CUDA  $\geq 6.0$ , CC  $\geq 3.0$  (preferably 5.x), 64-bit Linux or Windows



# Explicit vs Unified Memory

## Explicit Memory Management

```
void *data, *d_data;  
data = malloc(N);  
cudaMalloc(&d_data, N);  
cpu_func1(data, N);  
cudaMemcpy(d_data, data, N, ...);  
gpu_func2<<<...>>>(d_data, N);  
cudaMemcpy(data, d_data, N, ...);  
cudaFree(d_data);  
cpu_func3(data, N);  
free(data);
```

## GPU code w/ Unified Memory

```
void *data;  
cudaMallocManaged(&data, N);  
  
cpu_func1(data, N);  
  
gpu_func2<<<...>>>(data, N);  
cudaDeviceSynchronize();  
  
cpu_func3(data, N);  
cudaFree(data);
```



# WHAT YOU CAN DO WITH UNIFIED MEMORY

See it in action at the end of the talk!

Works everywhere today

```
int *data;  
cudaMallocManaged(&data, sizeof(int) * n);  
kernel<<<grid, block>>>(data);
```

Works on Power9 + ATS in CUDA 9.2  
Will work in the future on x86 + HMM

```
int *data = (int*)malloc(sizeof(int) * n);  
kernel<<<grid, block>>>(data);
```

```
int data[1024];  
kernel<<<grid, block>>>(data);
```

```
int *data = (int*)alloca(sizeof(int) * n);  
kernel<<<grid, block>>>(data);
```

```
extern int *data;  
kernel<<<grid, block>>>(data);
```

ATS: Address Translation Service  
HMM: Heterogeneous Memory Management

47 NVIDIA.

Source: Nikolay Sakharnykh, “EVERYTHING YOU NEED TO KNOW ABOUT UNIFIED MEMORY”, 3/27/2018



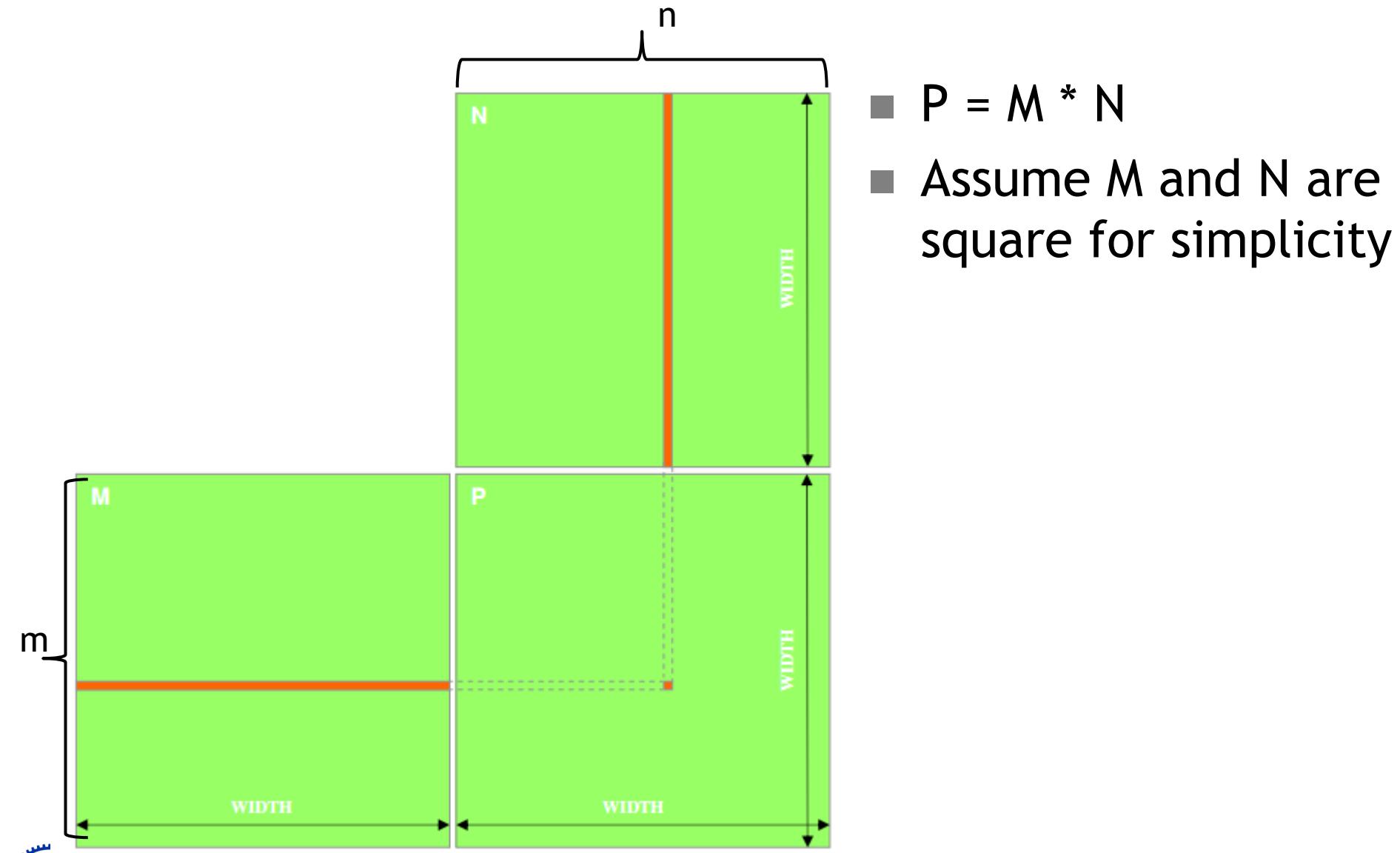
# Outline

---

- GPUs as Compute Engines
- GPU Architectures
  - ✿ GPU Threading Model
  - ✿ Separation of Memory Spaces
- Introduction to CUDA
  - ✿ Parallel Computing Platform
  - ✿ Programming Model
    - ◆ Built-in Data Types and Functions
    - ◆ Thread Model
    - ◆ Memory Model
  - ✿ Case Study: Matrix Multiplication
  - ✿ Thread Synchronization
  - ✿ Advanced Features



# Matrix Multiplication



# Matrix Multiplication

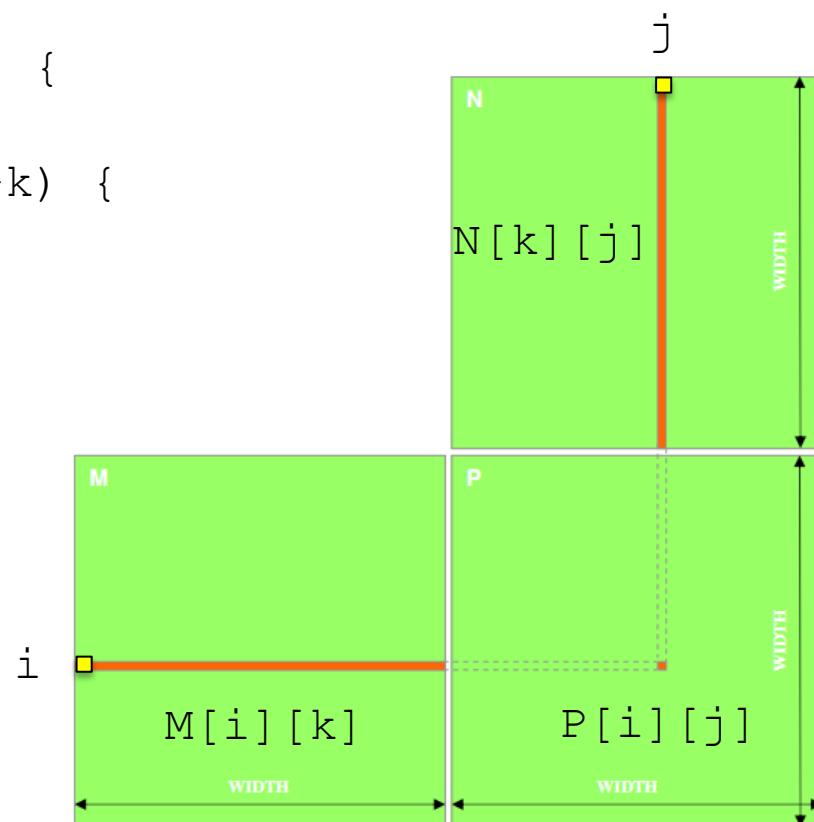
---

- 1,000 x 1,000 matrix
  - 1,000,000 dot products
    - Each 1,000 multiples and 1,000 adds



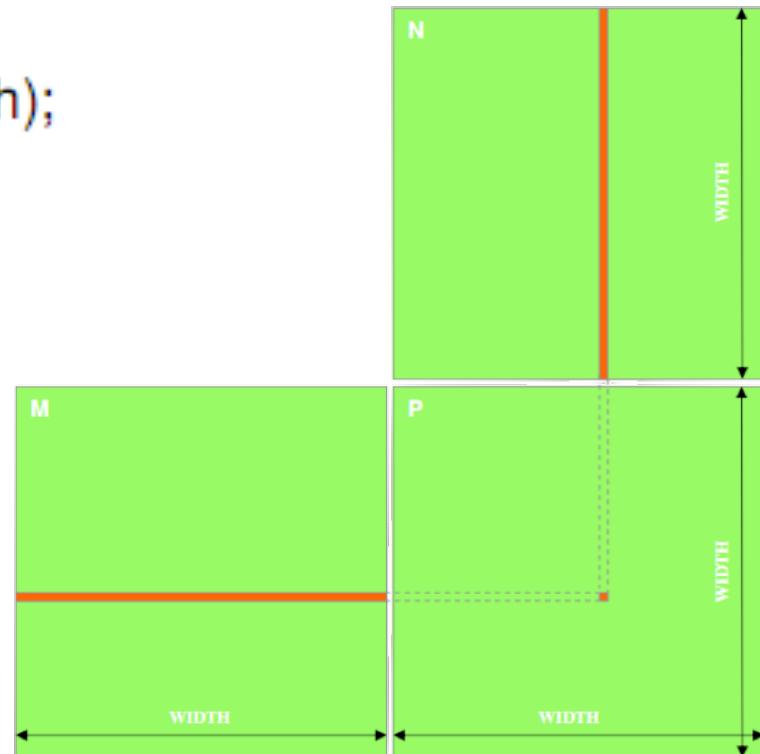
# Matrix Multiplication: CPU Implementation

```
void MatrixMulOnHost(float* M, float* N, float* P, int width)
{
    for (int i = 0; i < width; ++i) {
        for (int j = 0; j < width; ++j) {
            float sum = 0;
            for (int k = 0; k < width; ++k) {
                float a = M[i * width + k];
                float b = N[k * width + j];
                sum += a * b;
            }
            P[i * width + j] = sum;
        }
    }
}
```



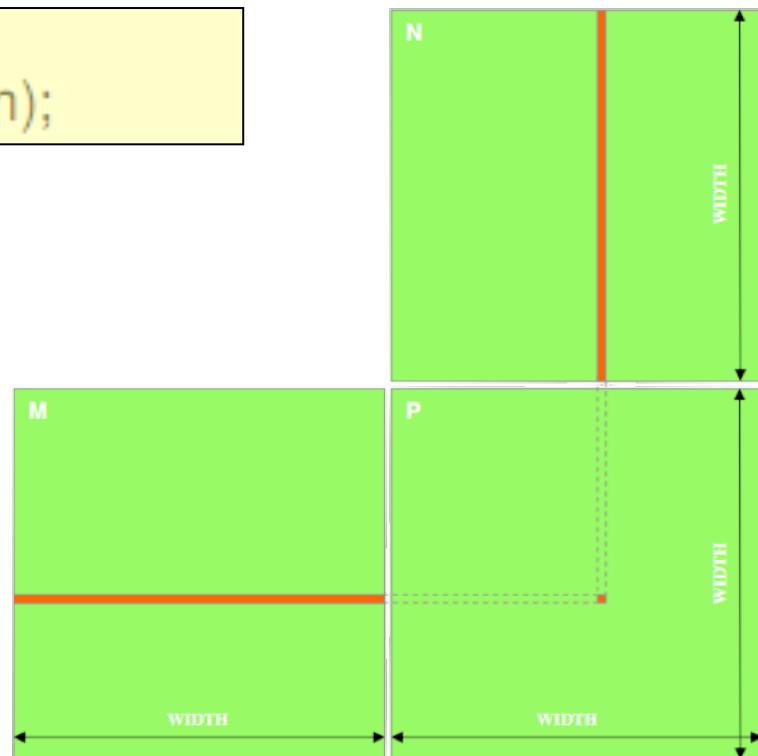
# Matrix Multiplication: CUDA Skeleton

```
int main(void) {  
    1. // Allocate and initialize the matrices M, N, P  
        // I/O to read the input matrices M and N  
  
    ....  
  
    2. // M * N on the device  
        MatrixMulOnDevice(M, N, P, width);  
  
    3. // I/O to write the output matrix P  
        // Free matrices M, N, P  
  
    ....  
    return 0;  
}
```



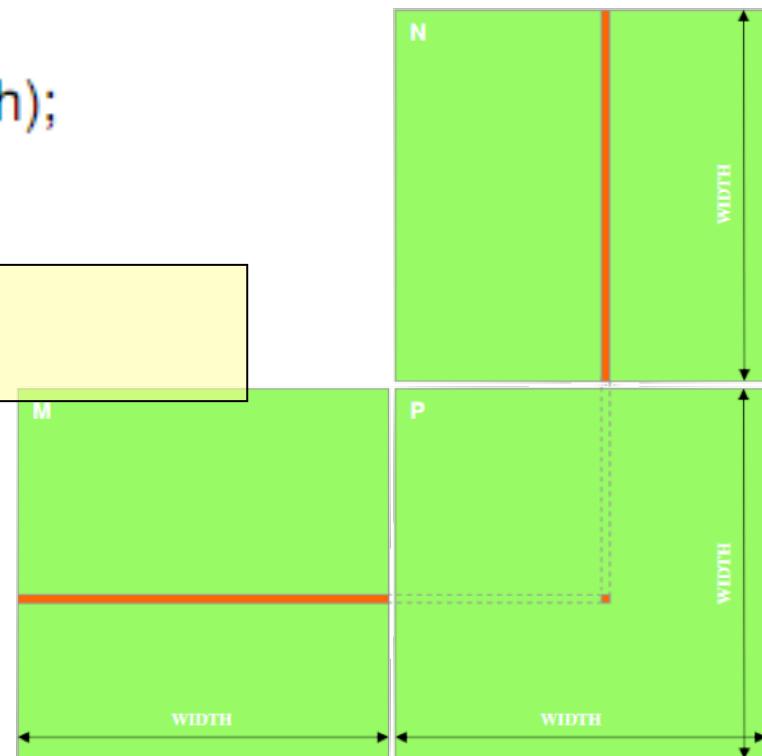
# Matrix Multiplication: CUDA Skeleton

```
int main(void) {  
    1. // Allocate and initialize the matrices M, N, P  
        // I/O to read the input matrices M and N  
    ....  
  
    2. // M * N on the device  
        MatrixMulOnDevice(M, N, P, width);  
  
    3. // I/O to write the output matrix P  
        // Free matrices M, N, P  
    ....  
    return 0;  
}
```



# Matrix Multiplication: CUDA Skeleton

```
int main(void) {
    1. // Allocate and initialize the matrices M, N, P
        // I/O to read the input matrices M and N
    ....
    2. // M * Non the device
        MatrixMulOnDevice(M, N, P, width);
    ...
    3. // I/O to write the output matrix P
        // Free matrices M, N, P
    ...
    return 0;
}
```



# Matrix Multiplication

---

- Step 1

- ⊕ Add *CUDA memory transfers* to the skeleton



# Matrix Multiplication: Data Transfer

```
void MatrixMulOnDevice(float* M, float* N, float* P, int Width)
{
    int size = Width * Width * sizeof(float);    float *Md, *Nd, *Pd;

    1. // Load M and N to device memory
        cudaMalloc(&Md, size);
        cudaMemcpy(Md, M, size, cudaMemcpyHostToDevice);
        cudaMalloc(&Nd, size);
        cudaMemcpy(Nd, N, size, cudaMemcpyHostToDevice);

    // Allocate P on the device
    cudaMalloc(&Pd, size);

    2. // Kernel invocation code – to be shown later
    ...
    3. // Read P from the device
        cudaMemcpy(P, Pd, size, cudaMemcpyDeviceToHost);
        // Free device matrices
        cudaFree(Md); cudaFree(Nd); cudaFree (Pd);
}
```

Allocate input



# Matrix Multiplication: Data Transfer

```
void MatrixMulOnDevice(float* M, float* N, float* P, int Width)
{
    int size = Width * Width * sizeof(float);    float *Md, *Nd, *Pd;

    1. // Load M and N to device memory
        cudaMalloc(&Md, size);
        cudaMemcpy(Md, M, size, cudaMemcpyHostToDevice);
        cudaMalloc(&Nd, size);
        cudaMemcpy(Nd, N, size, cudaMemcpyHostToDevice);

        // Allocate P on the device
        cudaMalloc(&Pd, size);
```

←      **Allocate output**

```
    2. // Kernel invocation code – to be shown later
        ...
    3. // Read P from the device
        cudaMemcpy(P, Pd, size, cudaMemcpyDeviceToHost);
        // Free device matrices
        cudaFree(Md); cudaFree(Nd); cudaFree(Pd);
}
```



# Matrix Multiplication: Data Transfer

```
void MatrixMulOnDevice(float* M, float* N, float* P, int Width)
{
    int size = Width * Width * sizeof(float);    float *Md, *Nd, *Pd;

    1. // Load M and N to device memory
        cudaMalloc(&Md, size);
        cudaMemcpy(Md, M, size, cudaMemcpyHostToDevice);
        cudaMalloc(&Nd, size);
        cudaMemcpy(Nd, N, size, cudaMemcpyHostToDevice);

        // Allocate P on the device
        cudaMalloc(&Pd, size);

    2. // Kernel invocation code – to be shown later
        ...
    3. // Read P from the device
        cudaMemcpy(P, Pd, size, cudaMemcpyDeviceToHost);
        // Free device matrices
        cudaFree(Md); cudaFree(Nd); cudaFree(Pd);
}
```



# Matrix Multiplication: Data Transfer

```
void MatrixMulOnDevice(float* M, float* N, float* P, int Width)
{
    int size = Width * Width * sizeof(float);    float *Md, *Nd, *Pd;

    1. // Load M and N to device memory
        cudaMalloc(&Md, size);
        cudaMemcpy(Md, M, size, cudaMemcpyHostToDevice);
        cudaMalloc(&Nd, size);
        cudaMemcpy(Nd, N, size, cudaMemcpyHostToDevice);

        // Allocate P on the device
        cudaMalloc(&Pd, size);

    2. // Kernel invocation code – to be shown later

    3. // Read P from the device
        cudaMemcpy(P, Pd, size, cudaMemcpyDeviceToHost);
        // Free device matrices
        cudaFree(Md); cudaFree(Nd); cudaFree (Pd);
}
```

Read back  
from device



# Matrix Multiplication

---

- Step 2
  - ✳ Implement the *kernel* in CUDA C



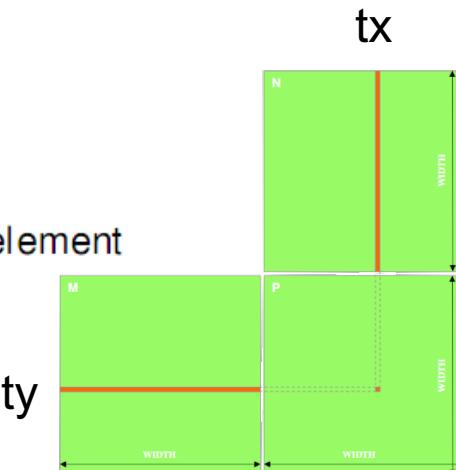
# Matrix Multiplication: CUDA Kernel

```
// Matrix multiplication kernel – thread specification
__global__ void MatrixMulKernel(float* Md, float* Nd, float* Pd, int Width)
{
    // 2D Thread ID
    int tx = threadIdx.x;
    int ty = threadIdx.y; ← Accessing a matrix, so using a 2D block

    // Pvalue stores the Pd element that is computed by the thread
    float Pvalue = 0;

    for (int k = 0; k < Width; ++k)
    {
        float Mdelement = Md[ty * Md.width + k];
        float Ndelement = Nd[k * Nd.width + tx];
        Pvalue += Mdelement * Ndelement;
    }

    // Write the matrix to device memory each thread writes one element
    Pd[ty * Width + tx] = Pvalue;
}
```



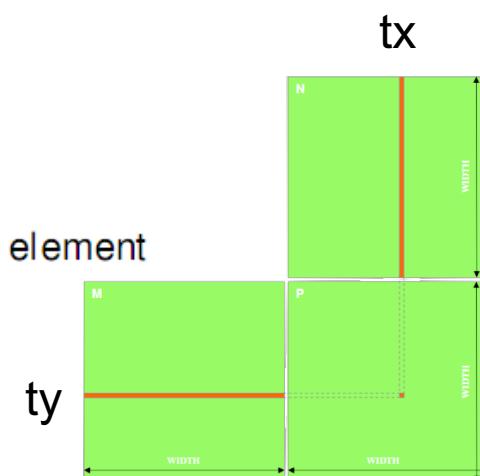
# Matrix Multiplication: CUDA Kernel

```
// Matrix multiplication kernel – thread specification
__global__ void MatrixMulKernel(float* Md, float* Nd, float* Pd, int Width)
{
    // 2D Thread ID
    int tx = threadIdx.x;
    int ty = threadIdx.y;

    // Pvalue stores the Pd element that is computed by the thread
    float Pvalue = 0; ←
    Each kernel computes one output

    for (int k = 0; k < Width; ++k)
    {
        float Mdelement = Md[ty * Md.width + k];
        float Ndelement = Nd[k * Nd.width + tx];
        Pvalue += Mdelement * Ndelement;
    }

    // Write the matrix to device memory each thread writes one element
    Pd[ty * Width + tx] = Pvalue;
}
```



# Matrix Multiplication: CUDA Kernel

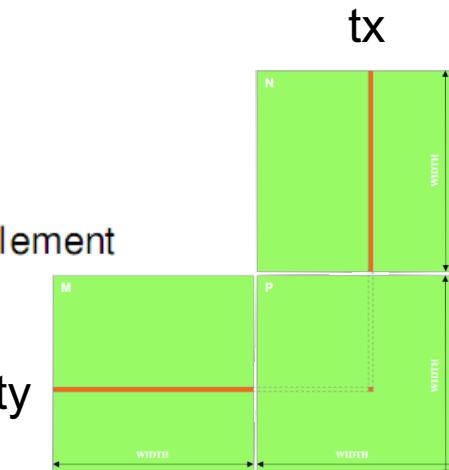
```
// Matrix multiplication kernel – thread specification
__global__ void MatrixMulKernel(float* Md, float* Nd, float* Pd, int Width)
{
    // 2D Thread ID
    int tx = threadIdx.x;
    int ty = threadIdx.y;

    // Pvalue stores the Pd element that is computed by the thread
    float Pvalue = 0;

    for (int k = 0; k < Width; ++k)
    {
        float Mdelement = Md[ty * Md.width + k];
        float Ndelement = Nd[k * Nd.width + tx];
        Pvalue += Mdelement * Ndelement;
    }

    // Write the matrix to device memory each thread writes one element
    Pd[ty * Width + tx] = Pvalue;
}
```

Where did the two outer for loops  
in the CPU implementation go?



# Matrix Multiplication: CUDA Kernel

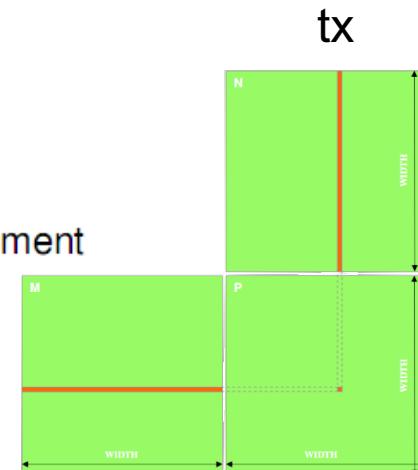
```
// Matrix multiplication kernel – thread specification
__global__ void MatrixMulKernel(float* Md, float* Nd, float* Pd, int Width)
{
    // 2D Thread ID
    int tx = threadIdx.x;
    int ty = threadIdx.y;

    // Pvalue stores the Pd element that is computed by the thread
    float Pvalue = 0;

    for (int k = 0; k < Width; ++k)
    {
        float Mdelement = Md[ty * Md.width + k];
        float Ndelement = Nd[k * Nd.width + tx];
        Pvalue += Mdelement * Ndelement;
    }

    // Write the matrix to device memory each thread writes one element
    Pd[ty * Width + tx] = Pvalue;
}
```

No locks or synchronization, why?



# Matrix Multiplication

---

- Step 3
  - ✳ Invoke the *kernel* in CUDA C



# Matrix Multiplication: Invoke Kernel

```
void MatrixMulOnDevice(float* M, float* N, float* P, int Width)
{
    int size = Width * Width * sizeof(float);    float *Md, *Nd, *Pd;

    1. // Load M and N to device memory
        cudaMalloc(&Md, size);
        cudaMemcpy(Md, M, size, cudaMemcpyHostToDevice);
        cudaMalloc(&Nd, size);
        cudaMemcpy(Nd, N, size, cudaMemcpyHostToDevice);

    // Allocate P on the device
    cudaMalloc(&Pd, size);

    2. // Kernel invocation code – to be shown later
    ...
    3. // Read P from the device
        cudaMemcpy(P, Pd, size, cudaMemcpyDeviceToHost);
    // Free device matrices
    cudaFree(Md); cudaFree(Nd); cudaFree(Pd);
}
```

// Setup the execution configuration  
dim3 dimBlock(WIDTH, WIDTH);  
dim3 dimGrid(1, 1);

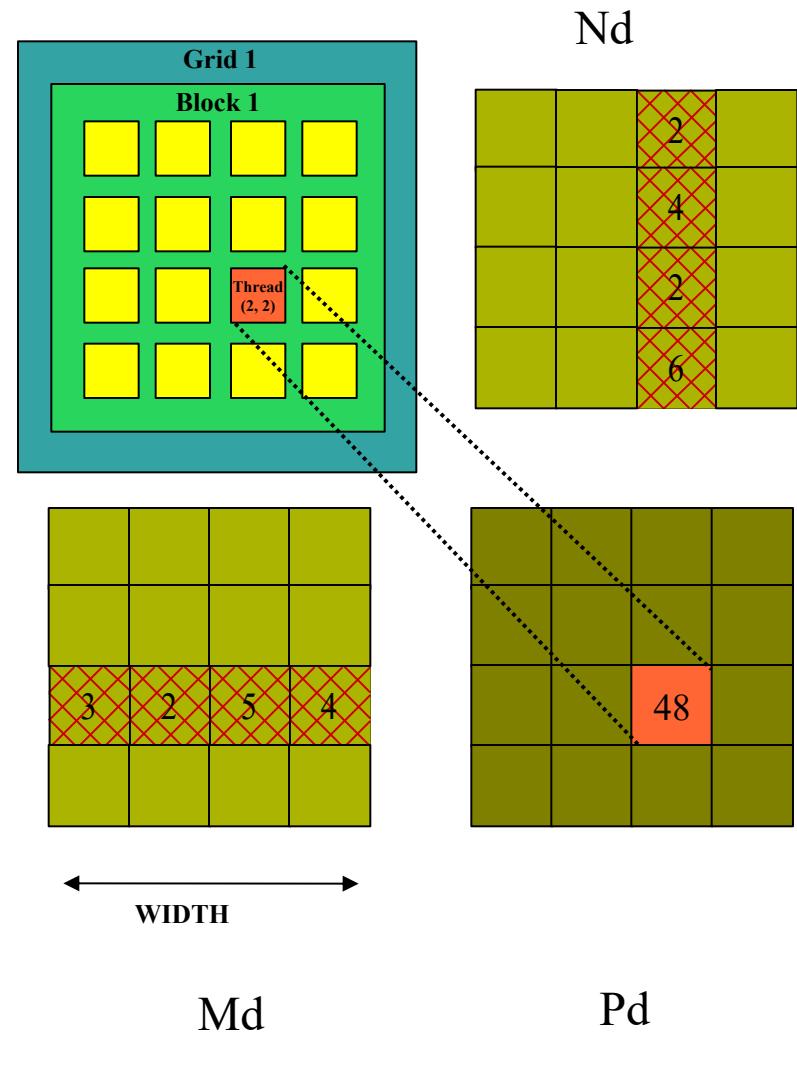
One block with width by width threads

// Launch the device computation threads!  
MatrixMulKernel<<<dimGrid, dimBlock>>>(Md, Nd, Pd);



# Matrix Multiplication

- One Block of threads compute matrix  $P_d$ 
  - Each thread computes one element of  $P_d$
- Each thread
  - Loads a row of matrix  $M_d$
  - Loads a column of matrix  $N_d$
  - Perform one multiply and addition for each pair of  $M_d$  and  $N_d$  elements
  - Compute to off-chip memory access ratio close to 1:1 (not very high)
- Size of matrix limited by the number of threads allowed in a thread block



# Matrix Multiplication

---

## ■ Problems

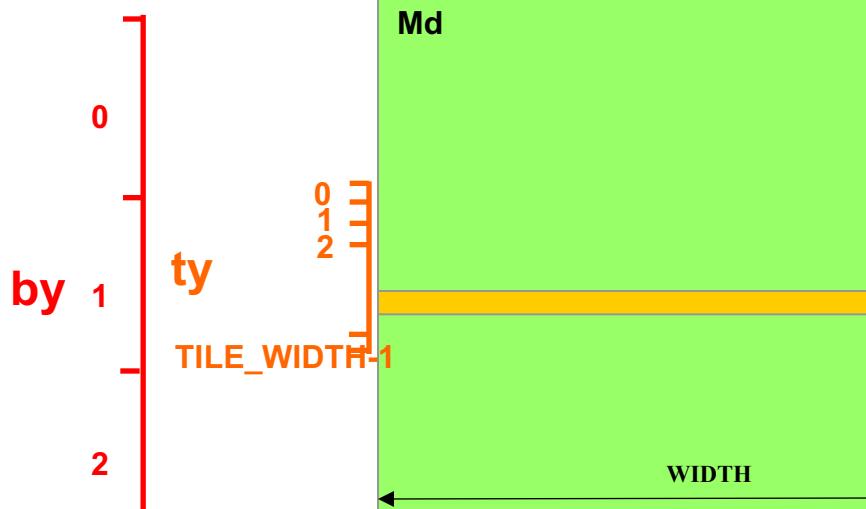
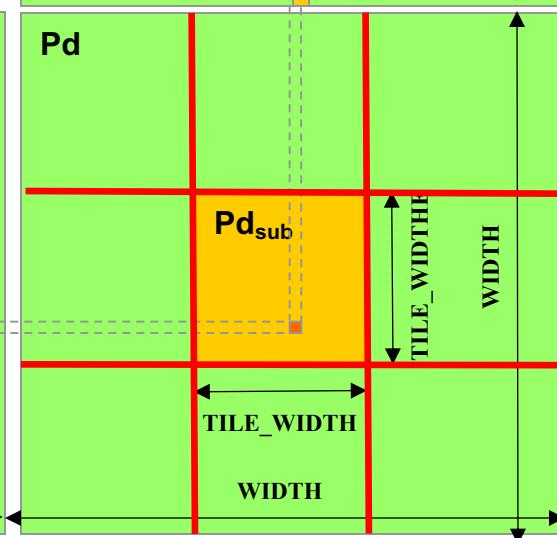
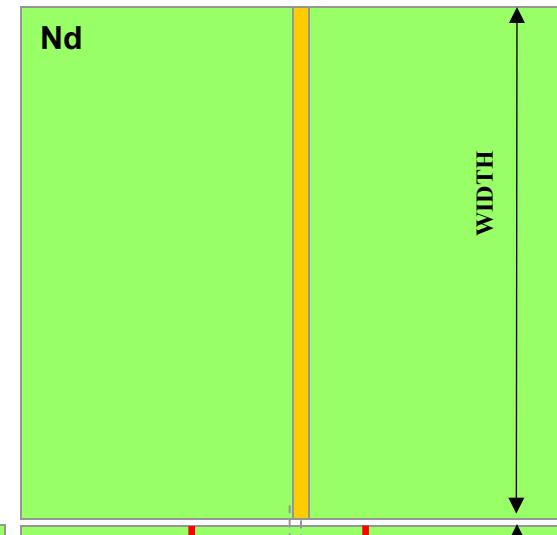
- ✳ Limited matrix size
  - ◆ Only uses one block
  - ◆ G80 and GT200 - up to 512 threads per block
- ✳ Lots of global memory access



# Matrix Multiplication

## ■ Remove size limitation

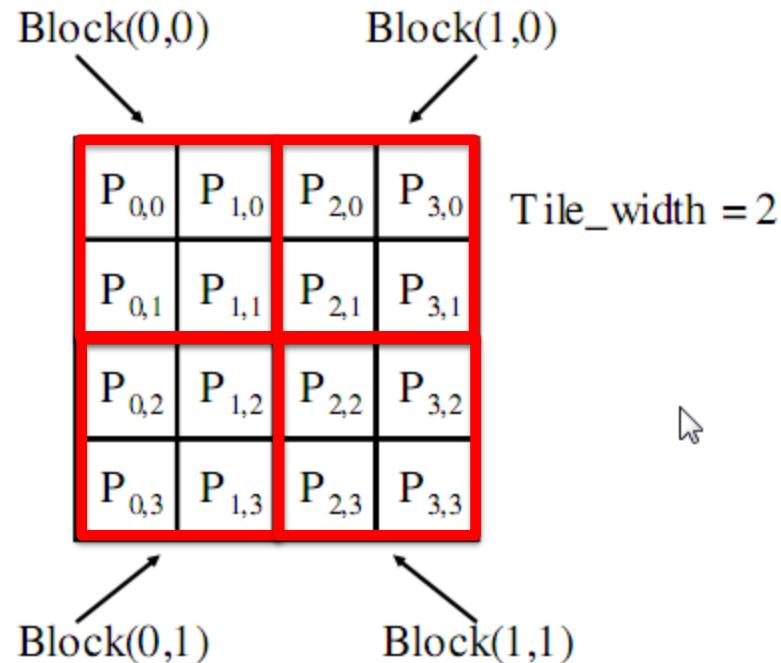
- Break  $P_d$  matrix into tiles
- Assign each tile to a block
- Use `threadIdx` and `blockIdx` for indexing



# Matrix Multiplication

## Example

- Matrix: 4x4
  - TILE\_WIDTH = 2
- =>
- Grid size: 2x2 blocks
  - Block size: 2x2 threads



# Matrix Multiplication

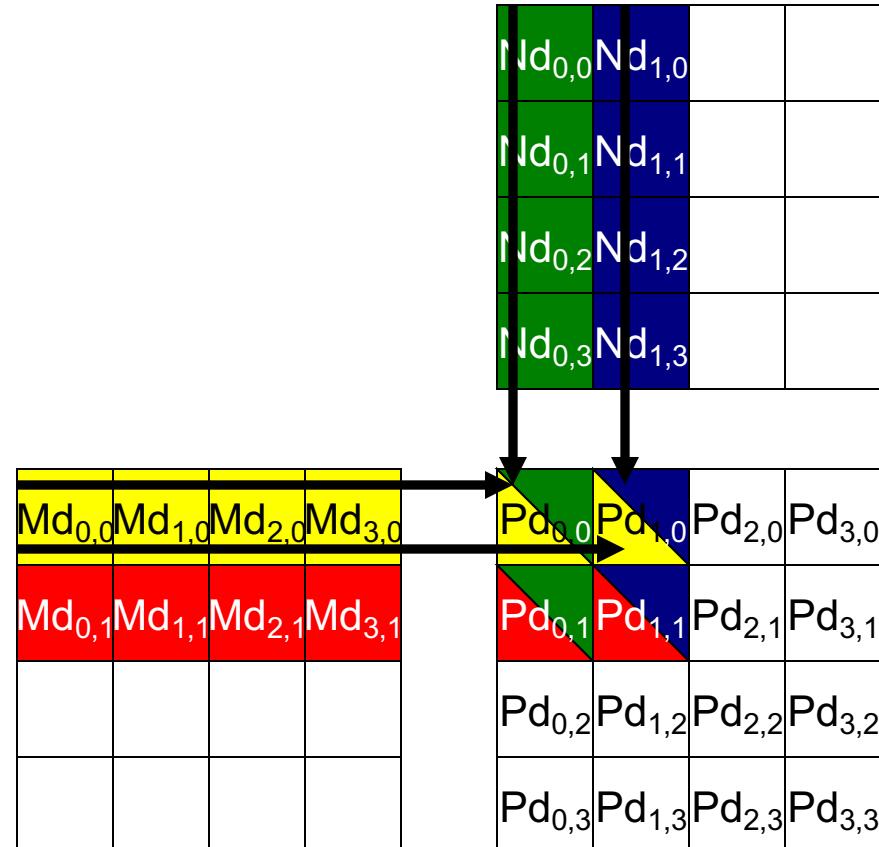
## Example

- Matrix: 4x4

- TILE\_WIDTH = 2

=>

- Grid size: 2x2 blocks
- Block size: 2x2 threads



# Matrix Multiplication

---

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    int Row = blockIdx.y * blockDim.y + threadIdx.y;
    int Col = blockIdx.x * blockDim.x + threadIdx.x;

    float Pvalue = 0;
    for (int k = 0; k < Width; ++k)
        Pvalue += Md[Row * Width + k] * Nd[k * Width + Col];

    Pd[Row * Width + Col] = Pvalue;
}
```



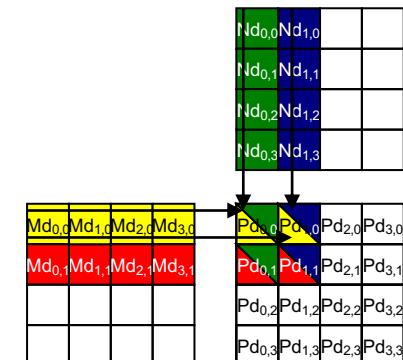
# Matrix Multiplication

Calculate the row index of the Pd element and M

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    int Row = blockIdx.y * blockDim.y + threadIdx.y;
    int Col = blockIdx.x * blockDim.x + threadIdx.x;

    float Pvalue = 0;
    for (int k = 0; k < Width; ++k)
        Pvalue += Md[Row * Width + k] * Nd[k * Width + Col];

    Pd[Row * Width + Col] = Pvalue;
}
```



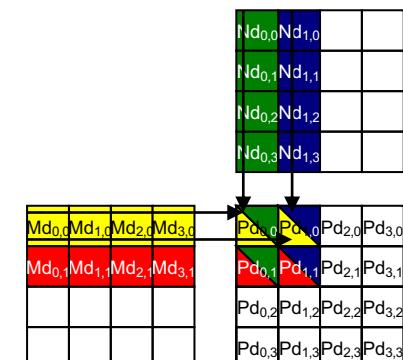
# Matrix Multiplication

Calculate the column index of Pd and Nd

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    int Row = blockIdx.y * blockDim.y + threadIdx.y;
    int Col = blockIdx.x * blockDim.x + threadIdx.x;

    float Pvalue = 0;
    for (int k = 0; k < Width; ++k)
        Pvalue += Md[Row * Width + k] * Nd[k * Width + Col];

    Pd[Row * Width + Col] = Pvalue;
}
```



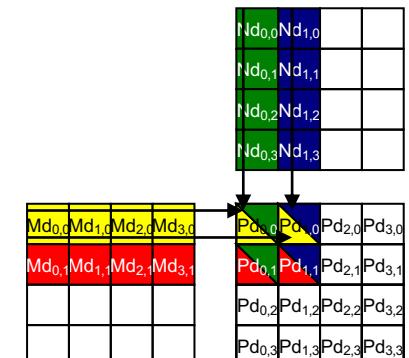
# Matrix Multiplication

Each thread computes one element  
of the block sub-matrix

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    int Row = blockIdx.y * blockDim.y + threadIdx.y;
    int Col = blockIdx.x * blockDim.x + threadIdx.x;

    float Pvalue = 0;
    for (int k = 0; k < Width; ++k)
        Pvalue += Md[Row * Width + k] * Nd[k * Width + Col];

    Pd[Row * Width + Col] = Pvalue;
}
```



# Matrix Multiplication

---

- Invoke kernel:

```
dim3 dimGrid(Width / TILE_WIDTH, Height / TILE_WIDTH);  
dim3 dimBlock(TILE_WIDTH, TILE_WIDTH);  
  
MatrixMulKernel<<<dimGrid, dimBlock>>>(  
Md, Nd, Pd, WIDTH);
```



---

# What about global memory access?



# Matrix Multiplication

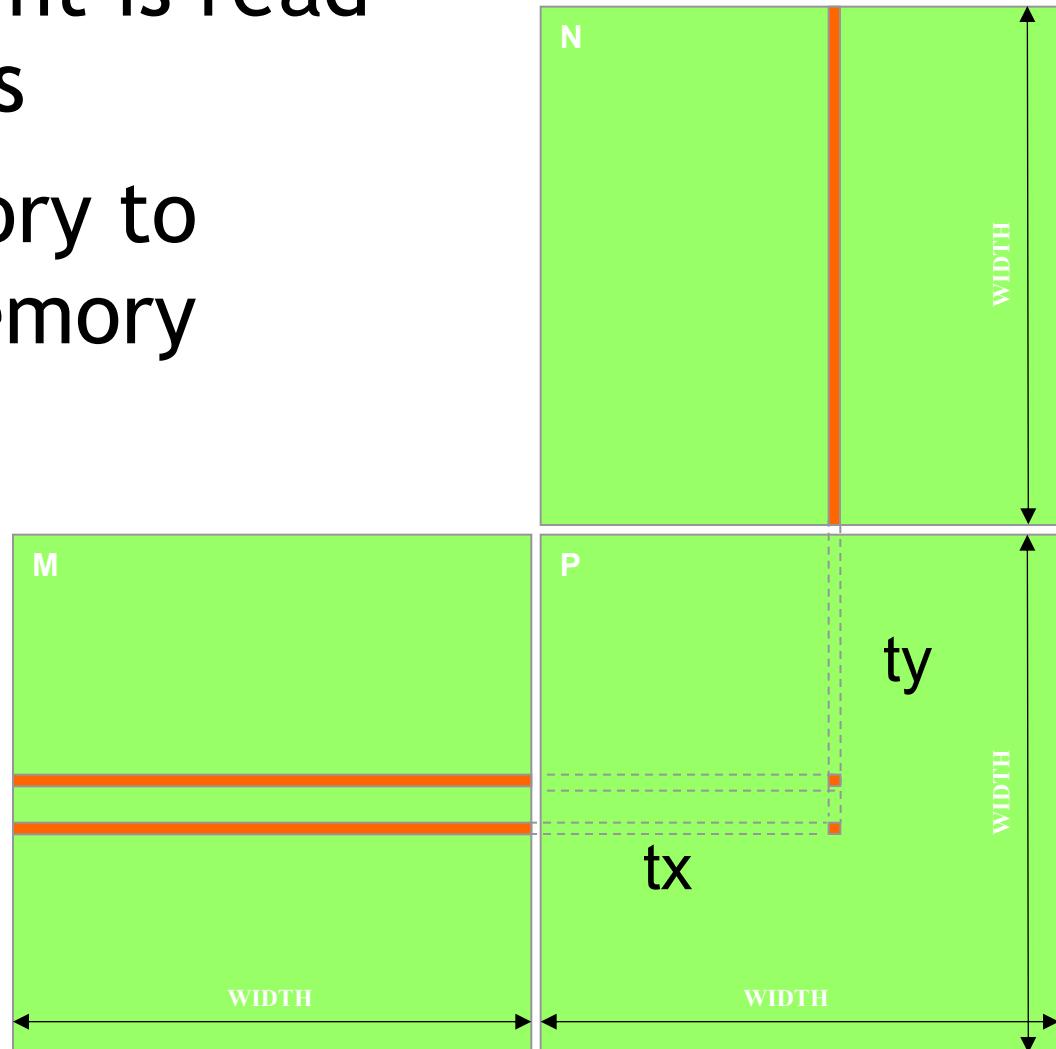
---

- Limited by global memory bandwidth
  - ✿ G80 peak GFLOPS: 346.5
  - ✿ Require 1386 GB/s to achieve this
  - ✿ G80 memory bandwidth: 86.4 GB/s
    - ◆ Limits code to 21.6 GFLOPS
    - ◆ In practice, code runs at 15 GFLOPS
  - ✿ Must drastically reduce global memory access



# Matrix Multiplication

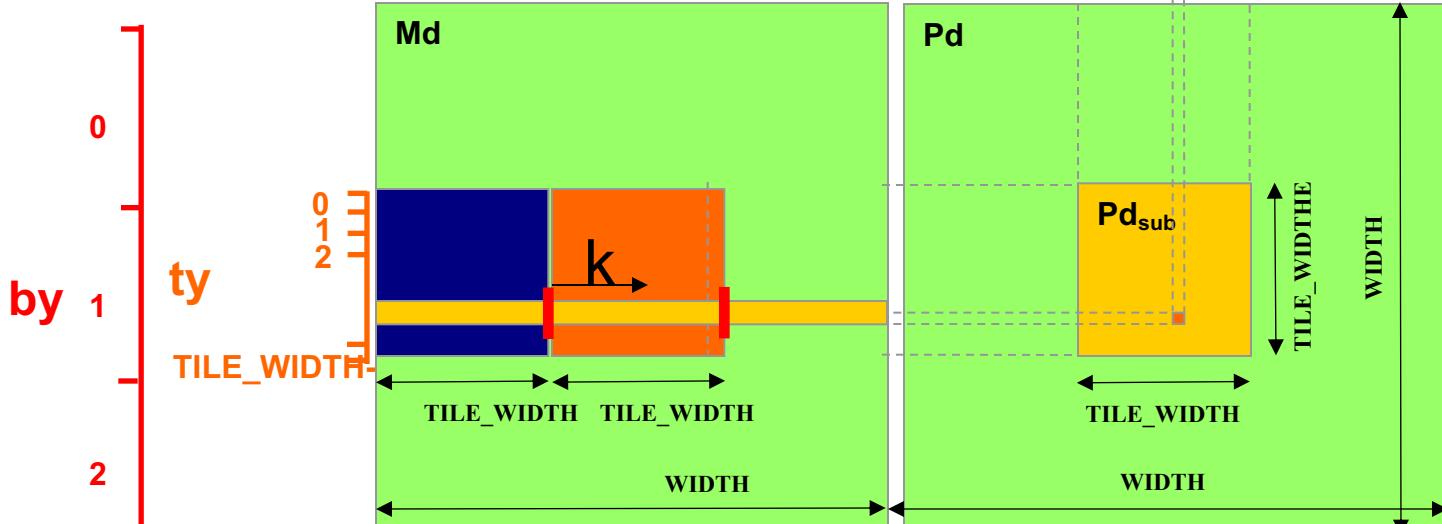
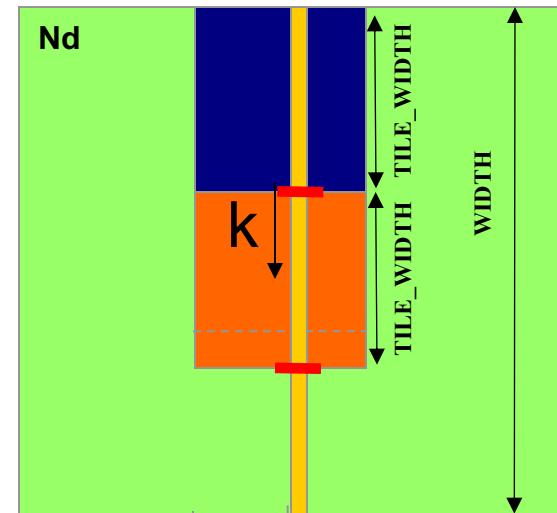
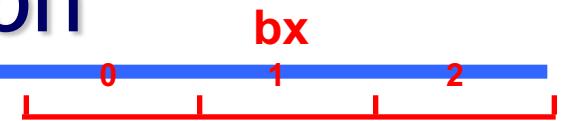
- Each input element is read by  $\text{WIDTH}$  threads
- Use shared memory to reduce global memory bandwidth



# Matrix Multiplication

## ■ Break kernel into phases

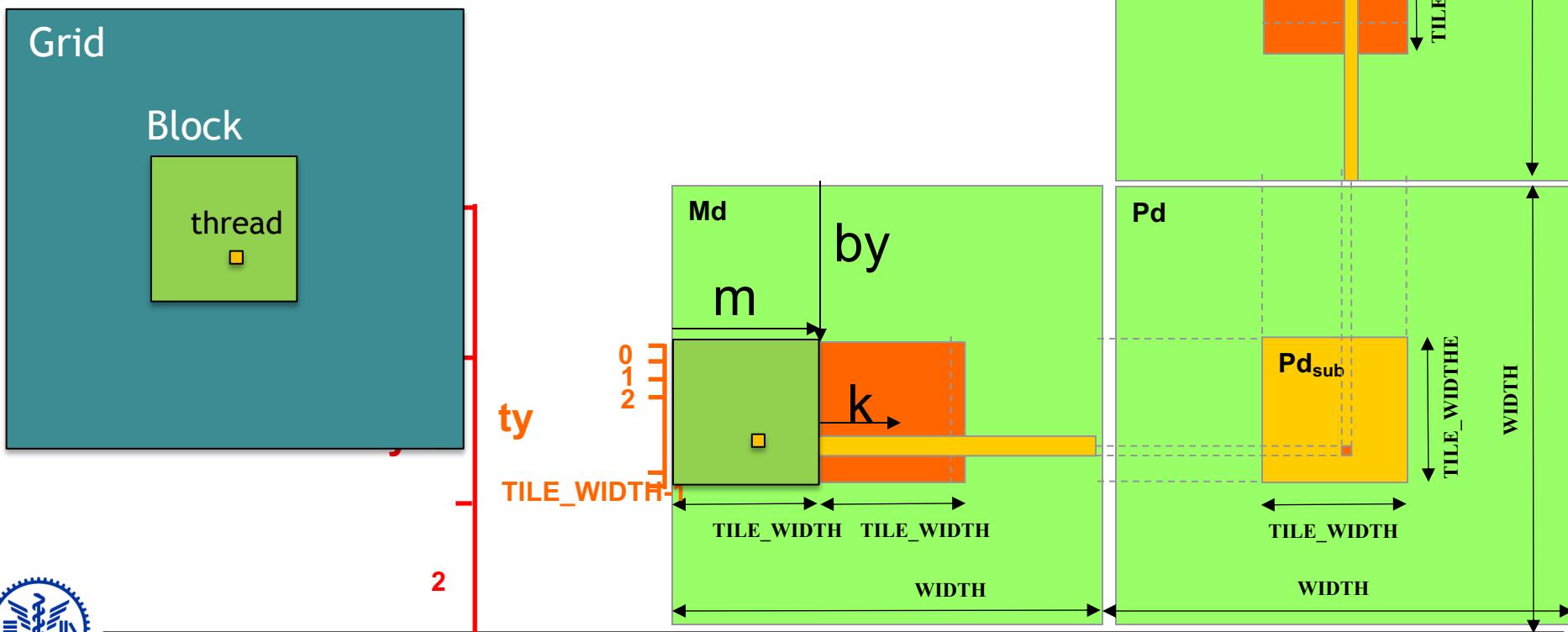
- Each phase accumulates  $P_d$  using a subset of  $M_d$  and  $N_d$
- Each phase has good data locality



# Matrix Multiplication

## Each thread

- loads one element of  $M_d$  and  $N_d$  in the tile into shared memory



# Matrix Multiplication

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

    int bx = blockIdx.x;    int by = blockIdx.y;
    int tx = threadIdx.x;  int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
        __syncthreads();

        for (int k = 0; k < TILE_WIDTH; ++k)
            Pvalue += Mds[ty][k] * Nds[k][tx];
        __syncthreads();
    }
    Pd[Row*Width+Col] = Pvalue;
}
```

Shared mem allocation

Indexing process

Filling data into shared mem

Partial dot product



# Matrix Multiplication

```

__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

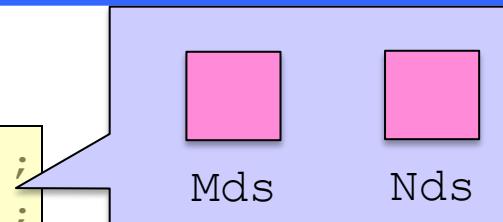
    int bx = blockIdx.x;    int by = blockIdx.y;
    int tx = threadIdx.x;  int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

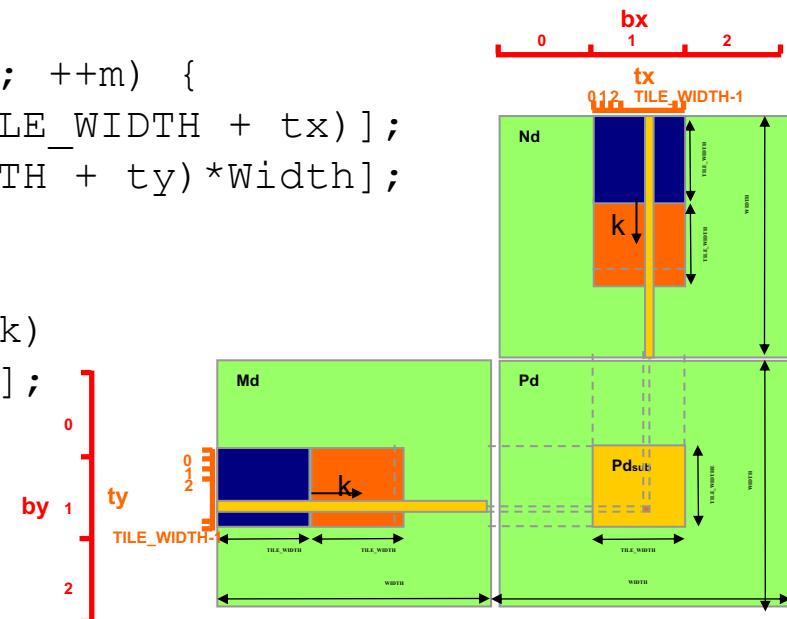
    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
        __syncthreads();

        for (int k = 0; k < TILE_WIDTH; ++k)
            Pvalue += Mds[ty][k] * Nds[k][tx];
        __syncthreads();
    }
    Pd[Row*Width+Col] = Pvalue;
}

```



Shared memory for a subset of Md and Nd



# Matrix Multiplication

```

__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

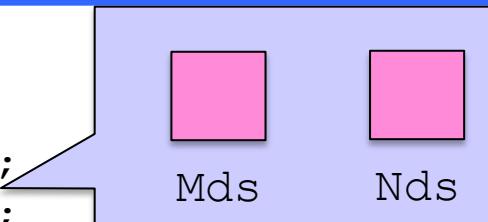
    int bx = blockIdx.x;  int by = blockIdx.y;
    int tx = threadIdx.x; int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
        __syncthreads();

        for (int k = 0; k < TILE_WIDTH; ++k)
            Pvalue += Mds[ty][k] * Nds[k][tx];
        __syncthreads();
    }
    Pd[Row*Width+Col] = Pvalue;
}

```

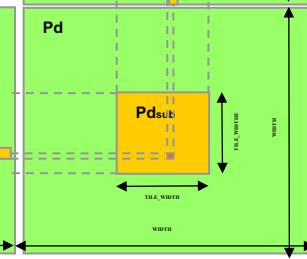
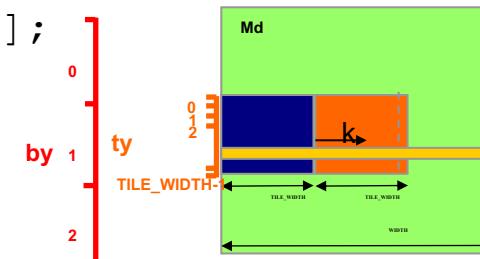
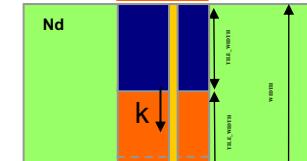


Width/TILE\_WIDTH

- Number of phases

m

- Index for current phase



# Matrix Multiplication

```

__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

    int bx = blockIdx.x;  int by = blockIdx.y;
    int tx = threadIdx.x; int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
    }

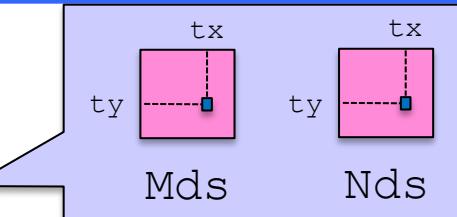
    __syncthreads();

    Nd[m*TILE_WIDTH+ty][Col]

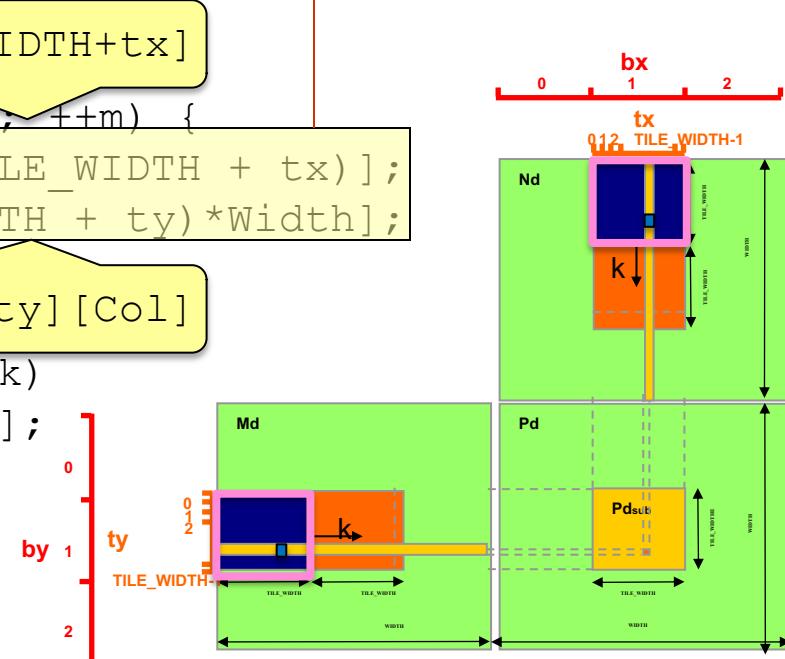
    for (int k = 0; k < TILE_WIDTH; ++k)
        Pvalue += Mds[ty][k] * Nds[k][tx];
    __syncthreads();
}

Pd[Row*Width+Col] = Pvalue;
}

```



Bring one element each from Md and Nd into shared memory



# Matrix Multiplication

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

    int bx = blockIdx.x;    int by = blockIdx.y;
    int tx = threadIdx.x;  int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
        __syncthreads(); // Wait for every thread in the block, i.e., wait for the tile to be in shared memory

        for (int k = 0; k < TILE_WIDTH; ++k)
            Pvalue += Mds[ty][k] * Nds[k][tx];
        __syncthreads();
    }
    Pd[Row*Width+Col] = Pvalue;
}
```

Wait for every thread in the block, i.e., wait for the tile to be in shared memory



# Matrix Multiplication

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

    int bx = blockIdx.x;  int by = blockIdx.y;
    int tx = threadIdx.x; int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
        __syncthreads();

        for (int k = 0; k < TILE_WIDTH; ++k)
            Pvalue += Mds[ty][k] * Nds[k][tx];
        __syncthreads();
    }
    Pd[Row*Width+Col] = Pvalue;
}
```

Accumulate subset of dot product



# Matrix Multiplication

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

    int bx = blockIdx.x;    int by = blockIdx.y;
    int tx = threadIdx.x;  int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
        __syncthreads();

        for (int k = 0; k < TILE_WIDTH; ++k)
            Pvalue += Mds[ty][k] * Nds[k][tx];
        __syncthreads();
    }

    Pd[Row*Width+Col] = Pvalue;
}
```

Why?



# Matrix Multiplication

```
__global__ void MatrixMulKernel(
    float* Md, float* Nd, float* Pd, int Width)
{
    __shared__ float Mds[TILE_WIDTH][TILE_WIDTH];
    __shared__ float Nds[TILE_WIDTH][TILE_WIDTH];

    int bx = blockIdx.x;    int by = blockIdx.y;
    int tx = threadIdx.x;  int ty = threadIdx.y;

    int Row = by * TILE_WIDTH + ty;
    int Col = bx * TILE_WIDTH + tx;

    float Pvalue = 0;
    for (int m = 0; m < Width/TILE_WIDTH; ++m) {
        Mds[ty][tx] = Md[Row*Width + (m*TILE_WIDTH + tx)];
        Nds[ty][tx] = Nd[Col + (m*TILE_WIDTH + ty)*Width];
        __syncthreads();

        for (int k = 0; k < TILE_WIDTH; ++k)
            Pvalue += Mds[ty][k] * Nds[k][tx];
        __syncthreads();
    }

    Pd[Row*Width+Col] = Pvalue;
}
```

Write final answer  
to global memory



# Matrix Multiplication

---

- How do you pick TILE\_WIDTH?
  - ✿ How can it be too large?



# Matrix Multiplication

---

- How do you pick TILE\_WIDTH?
  - ◆ How can it be too large?
    - ◆ By exceeding the maximum number of threads/block
      - G80 and GT200 - 512 (TILE\_WIDTH = 22)
      - Fermi - 1024 (TILE\_WIDTH = 32)
      - Pascal - 4096 (TILE\_WIDTH = 64)



# Matrix Multiplication

---

- How do you pick TILE\_WIDTH?
  - ◆ How can it be too large?
    - ◆ By exceeding the maximum number of threads/block
      - G80 and GT200 - 512 (TILE\_WIDTH = 22)
      - Fermi - 1024 (TILE\_WIDTH = 32)
      - Pascal - 4096 (TILE\_WIDTH = 64)
    - ◆ By exceeding the shared memory limitations
      - G80: 16KB per SM and up to 8 blocks per SM
        - » 2 KB per block
        - » 1 KB for Nds and 1 KB for Mds ( $16 * 16 * 4$ )
        - » TILE\_WIDTH = 16
        - » A larger TILE\_WIDTH will result in less blocks



# Matrix Multiplication

---

- Shared memory tiling benefits
  - ✿ Reduces global memory access by a factor of TILE\_WIDTH
    - ◆ 16x16 tiles reduces by a factor of 16
  - ✿ G80
    - ◆ Now global memory supports 345.6 GFLOPS
      - $21.6 \text{ GFLOPS} * 16 = 345.6 \text{ GFLOPS}$
    - ◆ Close to maximum of 346.5 GFLOPS



# Outline

---

- GPUs as Compute Engines
- GPU Architectures
  - ✿ GPU Threading Model
  - ✿ Separation of Memory Spaces
- Introduction to CUDA
  - ✿ Parallel Computing Platform
  - ✿ Programming Model
    - ◆ Built-in Data Types and Functions
    - ◆ Thread Model
    - ◆ Memory Model
  - ✿ Case Study: Matrix Multiplication
  - ✿ Thread Synchronization
  - ✿ Advanced Features



# Thread Synchronization

- Threads in a block can synchronize
  - call `_syncthreads` to create a barrier
  - A thread waits at this call until **all threads in the block** reach it, then all threads continue

```
Mds [ i ] = Md [ j ] ;  
_syncthreads() ;  
func (Mds [ i ] , Mds [ i + 1 ] ) ;
```



# Thread Synchronization

- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Time: 0



# Thread Synchronization

- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Time: 1



# Thread Synchronization

- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Threads 0 and 1 are blocked at barrier

Time: 1



# Thread Synchronization

- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Time: 2



# Thread Synchronization

- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Time: 3



# Thread Synchronization

- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

All threads in block have reached barrier, any thread can continue

Time: 3



# Thread Synchronization

- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Time: 4



# Thread Synchronization

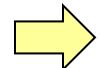
- Assume that the warp size is 2 and the block size is 4.

Thread 0

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 1

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```



Thread 2

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Thread 3

```
Mds[i] = Md[j];  
__syncthreads();  
func(Mds[i], Mds[i+1]);
```

Time: 5



# Atomic Functions

---

- What is the value of count if 8 threads execute `++count`?

```
__device__ unsigned int count = 0;  
// ...  
  
__global__ kernel(...) {  
    // ...  
    ++count;  
    // ...  
}
```



# Atomic Functions

---

- Read-modify-write atomic operation
  - ✿ Guaranteed no interference from other threads
  - ✿ No guarantee on order
- Shared or global memory
- Requires compute capability 1.1 (> G80)



# Atomic Functions

---

- What is the value of count if 8 threads execute `atomicAdd` below?

```
__device__ unsigned int count = 0;  
// ...  
  
__global__ kernel(...) {  
    // ...  
    // atomic ++count  
    atomicAdd(&count, 1);  
    // ...  
}
```



# Atomic Functions

---

- How do you implement `atomicAdd`?

```
__device__ int atomicAdd(  
    int *address, int val);
```



# Atomic Functions

---

- How do you implement `atomicAdd`?

```
__device__ int atomicAdd(  
    int *address, int val)  
{ // Made up keyword:  
    __lock (address) {  
        *address += val;  
    }  
}
```



# Atomic Functions

---

- How do you implement `atomicAdd` without locking?



# Atomic Functions

- How do you implement `atomicAdd` without locking?
- What if you were given an atomic **compare and swap**?

```
int atomicCAS(int *address, int  
compare, int val);
```

- Compare the value (old value) pointed by the pointer and the given compare value
- If old value is the same as the compare value, make the value pointed by the pointer as the new given value,
- Return the old value

There are PTX instructions for CAS and other atomics.

[http://developer.download.nvidia.com/compute/DevZone/docs/html/C/doc/ptx\\_isa\\_3.0.pdf](http://developer.download.nvidia.com/compute/DevZone/docs/html/C/doc/ptx_isa_3.0.pdf)



# Atomic Functions

---

## ■ atomicCAS pseudo implementation

```
int atomicCAS(int *address,
    int compare, int val)
{ // Made up keyword
    _lock(address) {
        int old = *address;
        *address = (old == compare) ? val : old;
        return old;
    }
}
```



# Atomic Functions

## ■ atomicCAS pseudo implementation

```
int atomicCAS(int *address,
              int compare, int val)
{ // Made up keyword
    _lock(address) {
        int old = *address;
        *address = (old == compare) ? val : old;
        return old;
    }
}
```



# Atomic Functions

## ■ atomicCAS pseudo implementation

```
int atomicCAS(int *address,
    int compare, int val)
{ // Made up keyword
    _lock(address) {
        int old = *address;
        *address = (old == compare) ? val : old;
    return old;
}
}
```



# Atomic Functions

---

## ■ Example:

```
*addr = 1;
```

```
atomicCAS(addr, 1, 2);
```

```
atomicCAS(addr, 1, 3);
```

```
atomicCAS(addr, 2, 3);
```



# Atomic Functions

## ■ Example:

```
*addr = 1;
```

```
atomicCAS(addr, 1, 2);
```

```
// returns 1
```

```
atomicCAS(addr, 1, 3);
```

```
// *addr = 2
```

```
atomicCAS(addr, 2, 3);
```



# Atomic Functions

## ■ Example:

```
*addr = 1;
```

```
atomicCAS(addr, 1, 2);
```

```
atomicCAS(addr, 1, 3);
```

```
atomicCAS(addr, 2, 3);
```

```
// returns 2
```

```
// *addr = 2
```



# Atomic Functions

## ■ Example:

```
*addr = 1;
```

```
atomicCAS(addr, 1, 2);
```

```
atomicCAS(addr, 1, 3);
```

```
atomicCAS(addr, 2, 3);
```

```
// returns 2
```

```
// *addr = 3
```



# Atomic Functions

---

- Again, how do you implement `atomicAdd` given `atomicCAS`?

```
_device_ int atomicAdd(  
    int *address, int val);
```



# Atomic Functions

---

```
__device__ int atomicAdd(int *address, int val)
{
    int old = *address, assumed;
    do {
        assumed = old;
        old = atomicCAS(address,
                        assumed, val + assumed);
    } while (assumed != old);
    return old;
}
```



# Atomic Functions

```
__device__ int atomicAdd(int *address, int val)
{
    int old = *address, assumed;
    do {
        assumed = old;
        old = atomicCAS(address,
                        assumed, val + assumed);
    } while (assumed != old);
    return old;
}
```

Read original value at  
\*address.



# Atomic Functions

```
__device__ int atomicAdd(int *address, int val)
{
    int old = *address, assumed;
    do {
        assumed = old;
        old = atomicCAS(address,
                        assumed, val + assumed);
    } while (assumed != old);
    return old;
}
```

If the value at  
\*address didn't  
change, increment it.



# Atomic Functions

```
__device__ int atomicAdd(int *address, int val)
{
    int old = *address, assumed;
    do {
        assumed = old;
        old = atomicCAS(address,
                        assumed, val + assumed);
    } while (assumed != old);
    return old;
}
```

Otherwise, loop until  
atomicCAS succeeds.

The value of \*address after this function  
returns is not necessarily the original value  
of \*address + val, why?



# Atomic Functions

---

## ■ Lots of atomics:

// Arithmetic  
atomicAdd()  
atomicSub()  
atomicExch()  
atomicMin()  
atomicMax()  
atomicAdd()  
atomicDec()  
atomicCAS()

// Bitwise  
atomicAnd()  
atomicOr()  
atomicXor()

<http://docs.nvidia.com/cuda/cuda-c-programming-guide/index.html#atomic-functions>



# Atomic Functions

---

- How can threads from different blocks work together?
- Use atomics sparingly. Why?



# Outline

---

- GPUs as Compute Engines
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- Introduction to CUDA
  - ✿ Parallel Computing Platform
  - ✿ Programming Model
    - ◆ Built-in Data Types and Functions
    - ◆ Thread Model
    - ◆ Memory Model
  - ✿ Case Study: Matrix Multiplication
  - ✿ Thread Synchronization
  - ✿ Advanced Features



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---

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  - ✿ Prof. Barry Wilkinson, University of North Carolina at Charlotte
  - ✿ Dr. Steve Rennich, Nvidia



# Advanced Features

---

- Pinned Host Memory
- Asynchronous Memory Copy
- CUDA Streams and Concurrency
- CUDA Events
- CUDA Timing
- Device Management



# Pinned (Page-Locked) Host Memory

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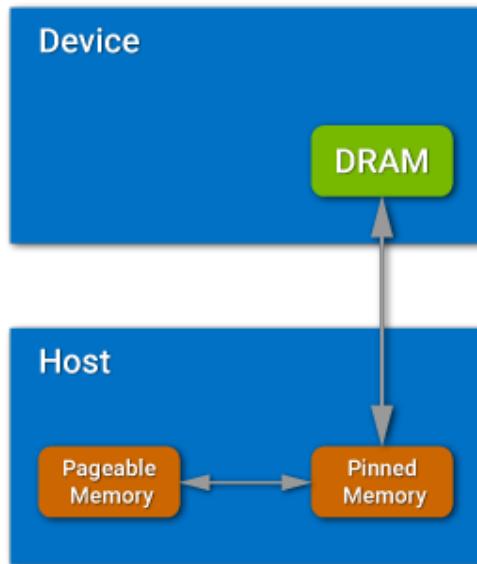
- A main memory area that is not pageable by the operating system; guaranteed to actually be in memory
- Two main advantages
  - ◆ Ensures faster transfers (the DMA engine can work without CPU intervention)
  - ◆ Allows CUDA asynchronous operations (including Zero Copy) to work correctly
    - ◆ Zero copy: memory on the host that is mapped to device's address space and thus accessible directly by a kernel



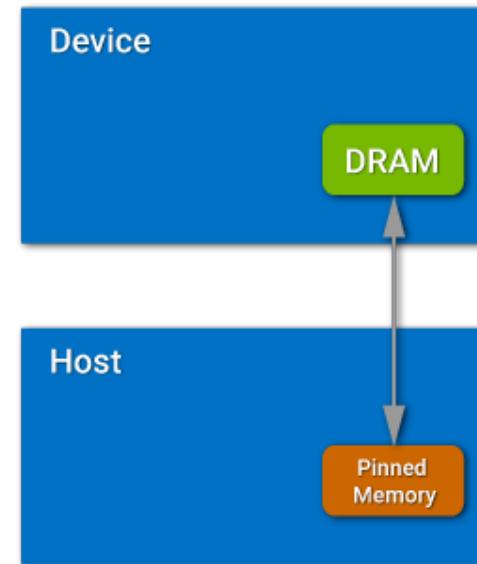
# Faster Pinned Data Transfer

- Whenever the data transfer function is called, the CUDA driver allocates a temporary pinned memory and copies the data to the pinned memory and then transfers the data from the pinned memory to the device

Pageable Data Transfer



Pinned Data Transfer



# Pinned Host Memory - How to use it?

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- Two ways to get pinned host memory
  - ⊕ Using `cudaMallocHost/cudaFreeHost` to allocate new memory
  - ⊕ Using `cudaHostRegister/cudaHostUnregister` to pin memory after allocation
- `cudaMemcpy` makes automatic use of it
- `cudaMemcpyAsync` can be used to **issue asynchronous memory copies**
- Can be directly accessed from Kernels (**zero-copy access**) - use `cudaHostGetDevicePointer`



# Examples of Allocating Pinned Memory

```
// allocate page-locked memory  
cudaMallocHost(&area, sizeof(double) * N);  
// free page-locked memory  
cudaFreeHost(area);
```

```
// allocate regular memory  
area = (double*) malloc( sizeof(double) * N );  
// lock area pages (CUDA >= 4.0)  
cudaHostRegister( area, sizeof(double) * N,  
                  cudaHostRegisterPortable );  
// unlock area pages (CUDA >= 4.0)  
cudaHostUnregister(area);  
// free regular memory  
cudaFreeHost(area);
```

- **Warning:** page-locked memory is a scarce resource.  
Use with caution: allocating too much page-locked memory can reduce overall system performance
- **But:** nVidia guys allocate up to 95% of a Linux compute node memory as ‘pinned’ memory in real world applications «without much problems» they say...



# Zero-Copy Access

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- Beginning with CUDA 2.2, a kernel can directly access host page-locked memory - no copy to device needed
  - Useful when you can't predetermine what data is needed
  - Less efficient if all data will be needed anyway
  - Could be worthwhile for pointer-based data structures as well



# Example of Zero-Copy Access

- CUDA allows to map a page-locked host memory area to the device's address space

```
// allocate page-locked and mapped memory
cudaHostAlloc(&area, sizeof(double) * N, cudaHostAllocMapped);
// invoke retrieving device pointer for mapped area
cudaHostGetDevicePointer( &dev_area, area, 0 );
my_kernel<<< g, b >>>( dev_area );
// free page-locked and mapped memory
cudaFreeHost(area);
```

- The only way to provide on-the-fly data that doesn't fit into the device's global memory
- Very convenient for large data with sparse access pattern



# Advanced Features

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- Pinned Host Memory
- Asynchronous Memory Copy
- CUDA Streams and Concurrency
- CUDA Events
- CUDA Timing
- Device Management



# Asynchronous CPU/GPU Operations

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- Asynchronous operations: control is returned to the host thread before the device has completed the requested task
  - ✿ Kernel calls are asynchronous by default
  - ✿ Memory copies from host to device of a memory block of 64 KB or less
  - ✿ Memory set function calls
- Remember: standard memory transfers and copybacks are **blocking**
  - ✿ The `cudaMemcpy()` has an asynchronous version (`cudaMemcpyAsync`)



# cudaMemcpyAsync

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- `cudaError_t cudaMemcpy( void* dst, const void* src, size_t count, enum cudaMemcpyKind kind )`
- `cudaError_t cudaMemcpyAsync( void* dst, const void* src, size_t count, enum cudaMemcpyKind kind, cudaStream_t stream )`
  - ⊕ Requires pinned host memory



# Example of Asynchronous CPU/GPU Operations (1/2)

```
cudaMemcpyAsync(data_d, data_h, size, cudaMemcpyHostToDevice, 0);  
cpuFunction();
```

Overlapped

- The last `cudaMemcpyAsync()` argument is the stream ID
- By default the kernel stream ID is zero
- `cudaMemcpyAsync()` allows the data transfer in asynchronous mode
- The execution of `cpuFunction()` can be overlapped with `cudaMemcpyAsync()`



# Example of Asynchronous CPU/GPU Operations (2/2)

```
cudaMemcpyAsync(data_d, data_h, size, cudaMemcpyHostToDevice, 0); }  
kernel<<<grid , block>>>(data_d);  
cpuFunction();
```

Overlapped

- Since the data transfer and the kernel uses the same stream, then these calls are sequential
- The execution of `cpuFunction()` can be overlapped with `cudaMemcpyAsync()` and `kernel()`



# Advanced Features

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# CUDA Streams

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- A CUDA stream is a sequence of commands (possibly issued by different host threads) that execute in order
- Different streams, on the other hand, may execute their commands out of order with respect to one another or concurrently



# Simple Example: Synchronous

```
cudaMalloc ( &dev1, size ) ;
double* host1 = (double*) malloc ( &host1, size ) ;
...
cudaMemcpy ( dev1, host1, size, H2D ) ;
kernel2 <<< grid, block, 0 >>> ( ..., dev2, ... ) ;
kernel3 <<< grid, block, 0 >>> ( ..., dev3, ... ) ;
cudaMemcpy ( host4, dev4, size, D2H ) ;
...
}
```

} Completely synchronous

- The third kernel launch argument specifies the number of bytes in shared memory that is dynamically allocated **per block** for this call in addition to the statically allocated memory
- All CUDA operations in the default stream are synchronous



# Simple Example: Asynchronous, No Streams

```
cudaMalloc ( &dev1, size ) ;
double* host1 = (double*) malloc ( &host1, size ) ;
...
cudaMemcpy ( dev1, host1, size, H2D ) ;
kernel2 <<< grid, block >>> ( ..., dev2, ... ) ;
some_CPU_method () ;
kernel3 <<< grid, block >>> ( ..., dev3, ... ) ;
cudaMemcpy ( host4, dev4, size, D2H ) ;
...
```

Potentially overlapped

- GPU kernels are asynchronous with host by default



# CUDA Streams (Cont'd)

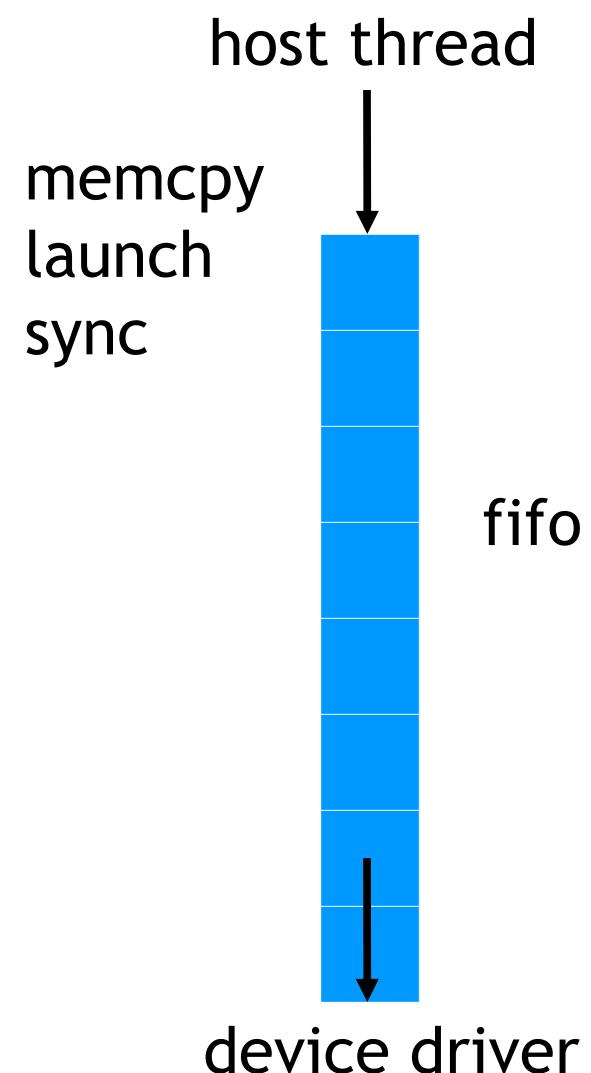
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- CUDA Streams are work queues to express concurrency between different tasks, e.g.
  - host to device memory copies
  - device to host memory copies
  - kernel execution
- To overlap different tasks just launch them in different streams
  - All tasks launched into the same stream are executed in order
  - Tasks launched into different streams might execute concurrently (depending on available resources: two copy engines, compute resources)



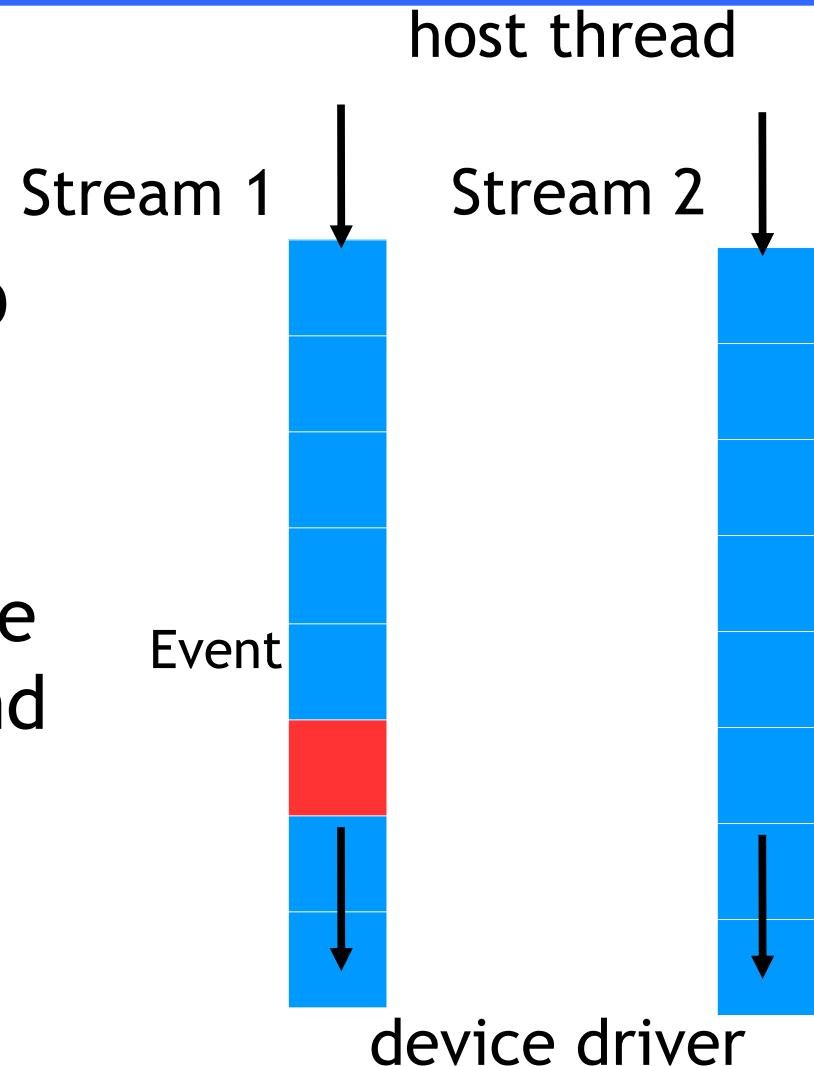
# Single CUDA Stream

- All device requests made from the host code are put into a queue
  - Queue is read and processed asynchronously by the driver and device
  - Driver ensures that commands in the queue are processed in sequence.
  - Memory copies end before kernel launch, etc.



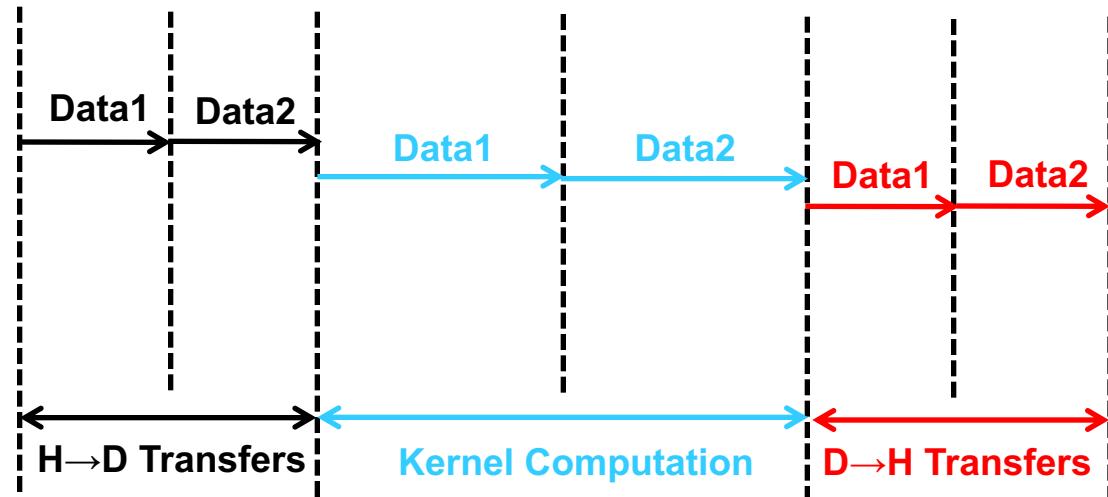
# Multiple CUDA Streams

- To allow concurrent copying and kernel execution, you need to use multiple queues, called “streams”
  - Cuda “events” allow the host thread to query and synchronize with the individual queues.



# Single Stream vs Multiple Streams

- Sequence of commands that execute serially

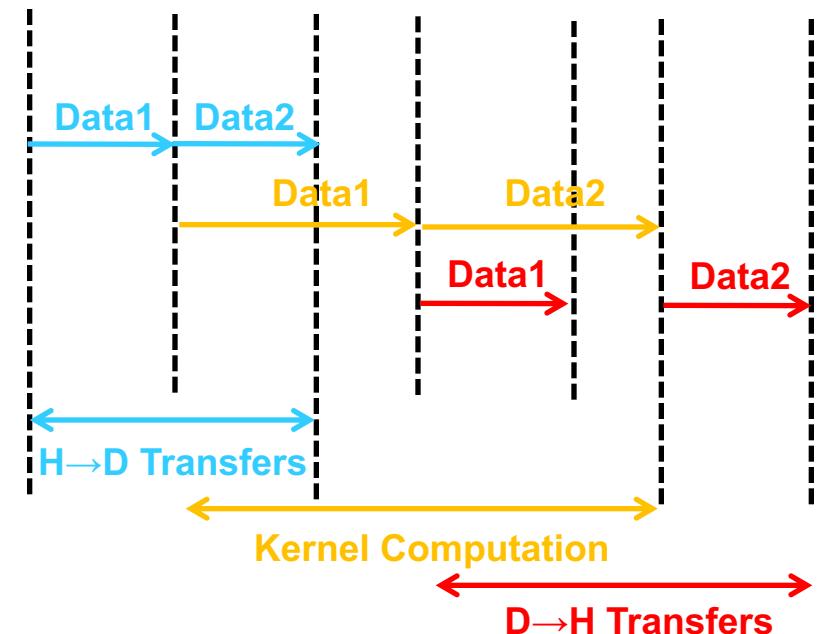


- Allow overlapping of memory transfers and kernel computations from different streams

  - Hides data transfer cost

- Implementable in CUDA devices with compute capability  $\geq 1.1$

- Host memory must be of type 'pinned'



# CUDA Streams - How to use them?

## ■ Create/destroy

```
cudaStream_t stream;  
cudaStreamCreate( &stream );  
cudaStreamDestroy( stream );
```

## ■ Launch

```
my_kernel<<<grid,block,0,stream>>>( . . . );  
cudaMemcypAsync( . . . , stream );
```

## ■ Synchronize

- Blocks until stream has completed all operations

```
cudaStreamSynchronize( stream );
```



# Simple Example: Asynchronous, With Streams

```
cudaStream_t stream1, stream2, stream3, stream4 ;
cudaStreamCreate ( &stream1 ) ;
...
cudaMalloc ( &dev1, size ) ;
cudaMallocHost ( &host1, size ) ; // pinned memory required
...
cudaMemcpyAsync ( dev1, host1, size, H2D, stream1 ) ;
kernel2 <<< grid, block, 0, stream2 >>> ( ..., dev2, ... ) ;
kernel3 <<< grid, block, 0, stream3 >>> ( ..., dev3, ... ) ;
cudaMemcpyAsync ( host4, dev4, size, D2H, stream4 ) ;
some_CPU_method () ;
...

```

Potentially overlapped

- Fully asynchronous / concurrent
  - Data used by concurrent operations should be independent



# Explicit Synchronization

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## ■ Synchronize everything

- `cudaDeviceSynchronize ()`
- Blocks host until all issued CUDA calls are complete

## ■ Synchronize w.r.t. a specific stream

- `cudaStreamSynchronize ( streamid )`
- Blocks host until all CUDA calls in `streamid` are complete

## ■ Synchronize using Events

- Create specific 'Events', within streams, to use for synchronization
- `cudaEventRecord ( event, streamid )`
- `cudaEventSynchronize ( event )`
- `cudaStreamWaitEvent ( stream, event )`
- `cudaEventQuery ( event )`



# Requirements for Concurrency

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- CUDA operations must be in different, non-0, streams
- `cudaMemcpyAsync` with host from 'pinned' memory
  - ✿ Page-locked memory allocated using `cudaMallocHost()` or `cudaHostAlloc()`
- Sufficient resources must be available
  - ✿ `cudaMemcpyAsync` in different directions
  - ✿ Device resources (SMEM, registers, blocks, etc.)



# Advanced Features

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# CUDA Events

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- CUDA Events are synchronization markers that can be used to:
  - ⊕ Time asynchronous tasks in streams
  - ⊕ Allow fine grained synchronization within a stream
  - ⊕ Allow inter stream synchronization (e.g., let a stream wait for an event in another stream)



# CUDA Events - How to use them?

## ■ Create/Destroy

```
cudaEvent_t event;  
cudaEventCreate( &event );  
cudaEventDestroy( event );
```

## ■ Record (records a given stream)

```
cudaEventRecord( event, stream );
```

## ■ Query (reports if the event was recorded)

```
cudaEventQuery( event );
```

## ■ Synchronize (waits until named event actually recorded)

```
cudaEventSynchronize( event );
```

## ■ Timing (returns the total time in miliseconds between the events start and end)

```
cudaEventElapsedTime( &time, start, end );
```



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# Measuring Performance of CUDA Programs

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- Generally instrument code. Measure time at two places and get difference
- Routines to use to measure time:
  - ✳ C `clock()` or `time()` routines
  - ✳ CUDA “events” (seems the best way)
  - ✳ CUDA SDK timer



# Timing with clock()

- If program uses cudaMemcpy, which is synchronous and waits for previous operations to complete and returns when it is complete, could use clock():

```
#include <time.h> // needed for clock()
int main() {
    clock_t start, stop;           // return types are clock_t, int's
    ...
    start = clock();      // number of clock ticks since prog launched
    cudaMemcpy(...);
    mykernel<<<B,T>>>(...);    // kernel call
    cudaMemcpy(...);
    stop = clock();
    ...
    printf("Execution time is %f seconds\n",
           (float) (stop-start)/(CLOCKS_PER_SEC) );
    return 0;
}
```



## If just measuring time of asynchronous kernel with `clock()`

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- Important to remember that kernel calls asynchronous and return immediately and before kernels have fully executed
- Hence need to wait for kernel to complete
- Can be achieved using `cudaThreadSynchronize()`:

```
start = clock();
mykernel<<<B, T>>>(....);
cudaThreadSynchronize();
stop = clock();
```



# CUDA Event Timer

- In general, better to use CUDA event timer

```
float time_ms = 0.0f;  
cudaEvent_t start , stop ;  
cudaEventCreate( &start );  
cudaEventCreate( &stop );  
  
cudaEventRecord( start , 0 );  
kernel<<< ... , ... , 0, 0 >>>( ... );  
cudaEventRecord( stop , 0 );  
  
cudaEventSynchronize(start ); //optional  
cudaEventSynchronize( stop );  
cudaEventElapsedTime( &time_ms, start , stop );  
  
cudaEventDestroy( start );  
cudaEventDestroy( stop );
```



# Advanced Features

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# Device Management

## ■ CPU can query and select GPU devices

- ◆ `cudaGetDeviceCount( int* count )`
- ◆ `cudaSetDevice( int device )`
- ◆ `cudaGetDevice( int *current_device )`
- ◆ `cudaGetDeviceProperties( cudaDeviceProp* prop, int device )`
- ◆ `cudaChooseDevice( int *device, cudaDeviceProp* prop )`

## ■ Multi-GPU setup:

- ◆ device 0 is used by default
- ◆ one CPU thread can control one GPU
  - ◆ multiple CPU threads can control the same GPU
    - calls are serialized by the driver



# Summary

## ■ CUDA brings C to a multiprocessor architecture

- ❖ Pros:

- ❖ It's easy to use and program
- ❖ Extensive, responsive support base, including developers
- ❖ NVIDIA is actively supporting the project
- ❖ Some applications are remarkably successful
- ❖ Handmade SIMD code yields impressive results

- ❖ Cons:

- ❖ Performance depends heavily on the algorithm
- ❖ Handmaking SIMD code requires learning a “new” style
- ❖ Mostly exploiting capabilities is easy, but fully exploiting capabilities is difficult

