

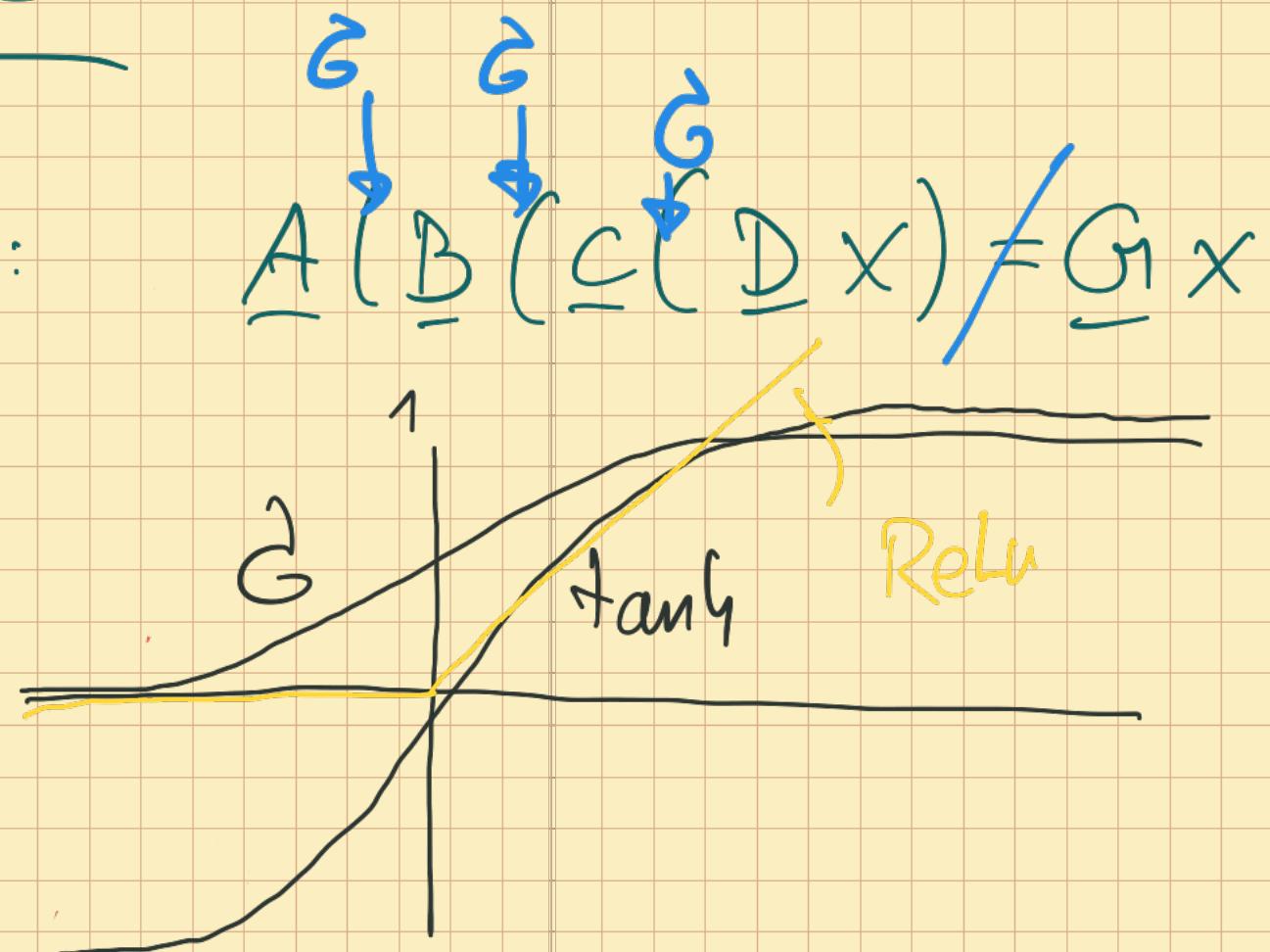
## Activation functions

$f(x) = x$  linear :

*sigmoid*  $f(x) = \frac{1}{1+e^{-x}}$

$f(x) = \tanh$

$f(x) = \max(x, 0) = \text{ReLU}$



## Vanishing - gradients

remember backprop, where we had  
factors of the form:

$$\frac{\partial \tilde{G}(z)}{\partial z}$$

For tanh,  $\tilde{G} : G(z) \rightarrow 1$  for  $z \rightarrow \infty$   
 $\Rightarrow \tilde{G}'(z) \rightarrow 0 - 11 -$

→ the error term becomes small: exponentially so  
in earlier layers in the net: stop of learning!

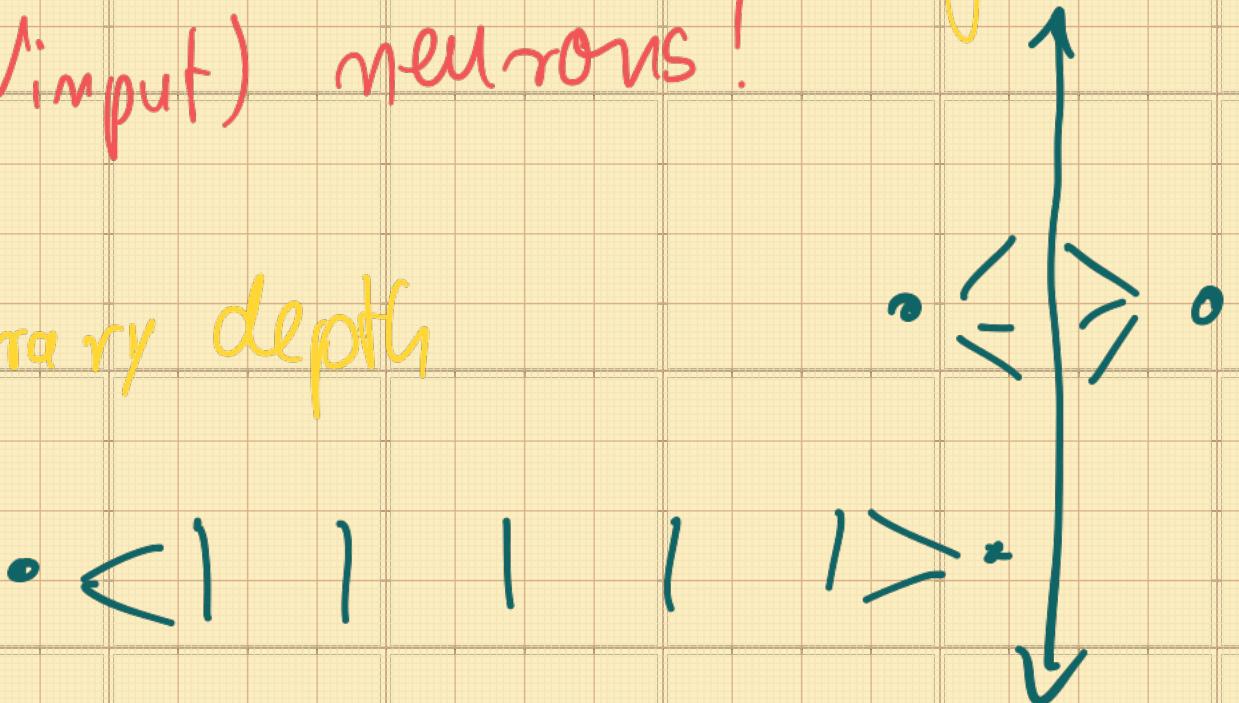
→ use other activations

→ use ReLUs with skip connectors!

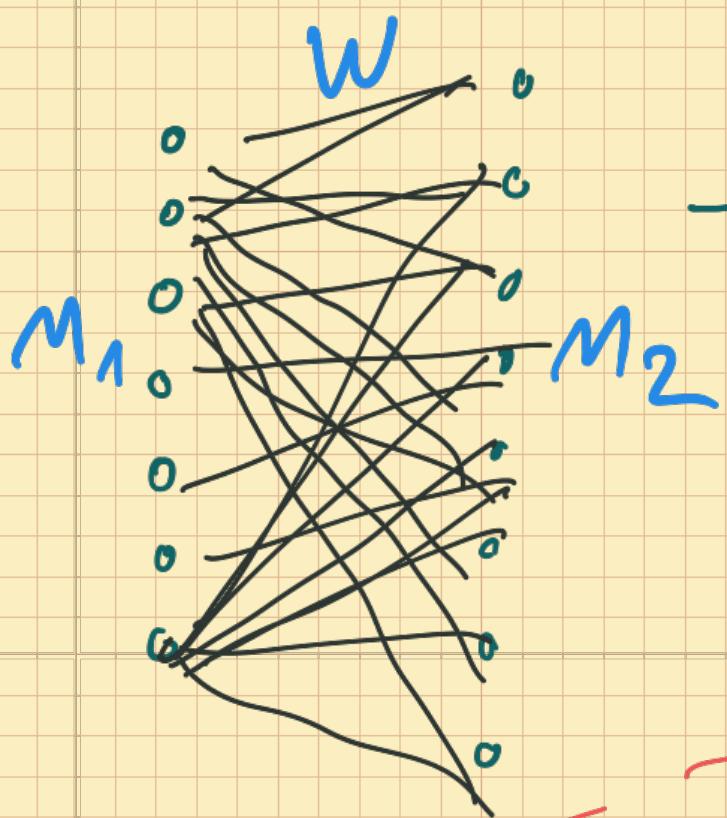
## Universal approximations:

A ANN with a single hidden layer can exactly represent any continuous function of multiple inputs:

- Cybenko, Hornik 1989: smooth activation function  
→ might need  $\exp(N_{\text{input}})$  neurons!
- Leshno 1993: ReLU
- Lu et al 2017: arbitrary depth

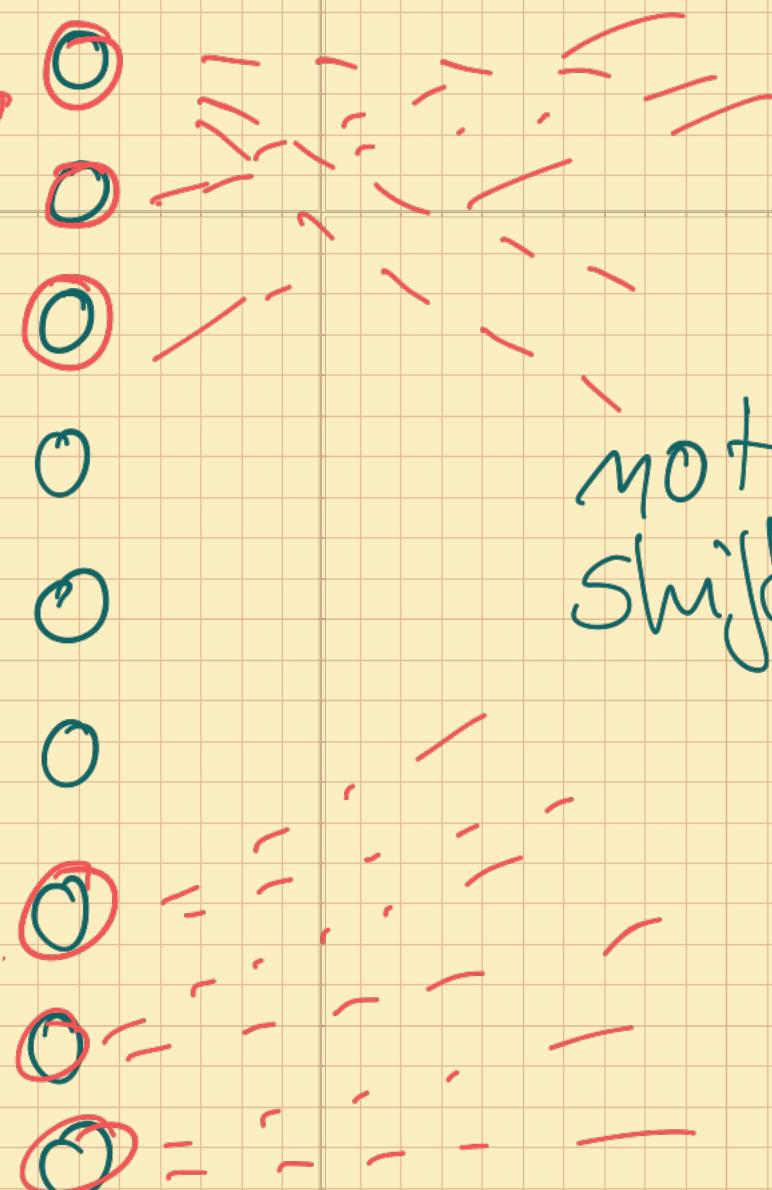
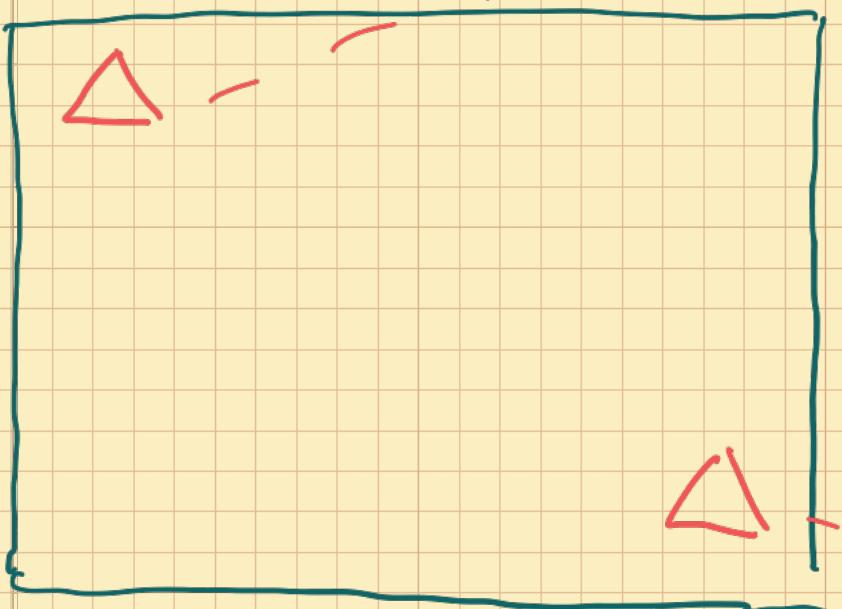


## The MLP - problem(s):



$\rightarrow N^2$  behaviour of neurons  
→ hard to train

parameters  $w$   
~~neurons~~



not  
shift-invariant!

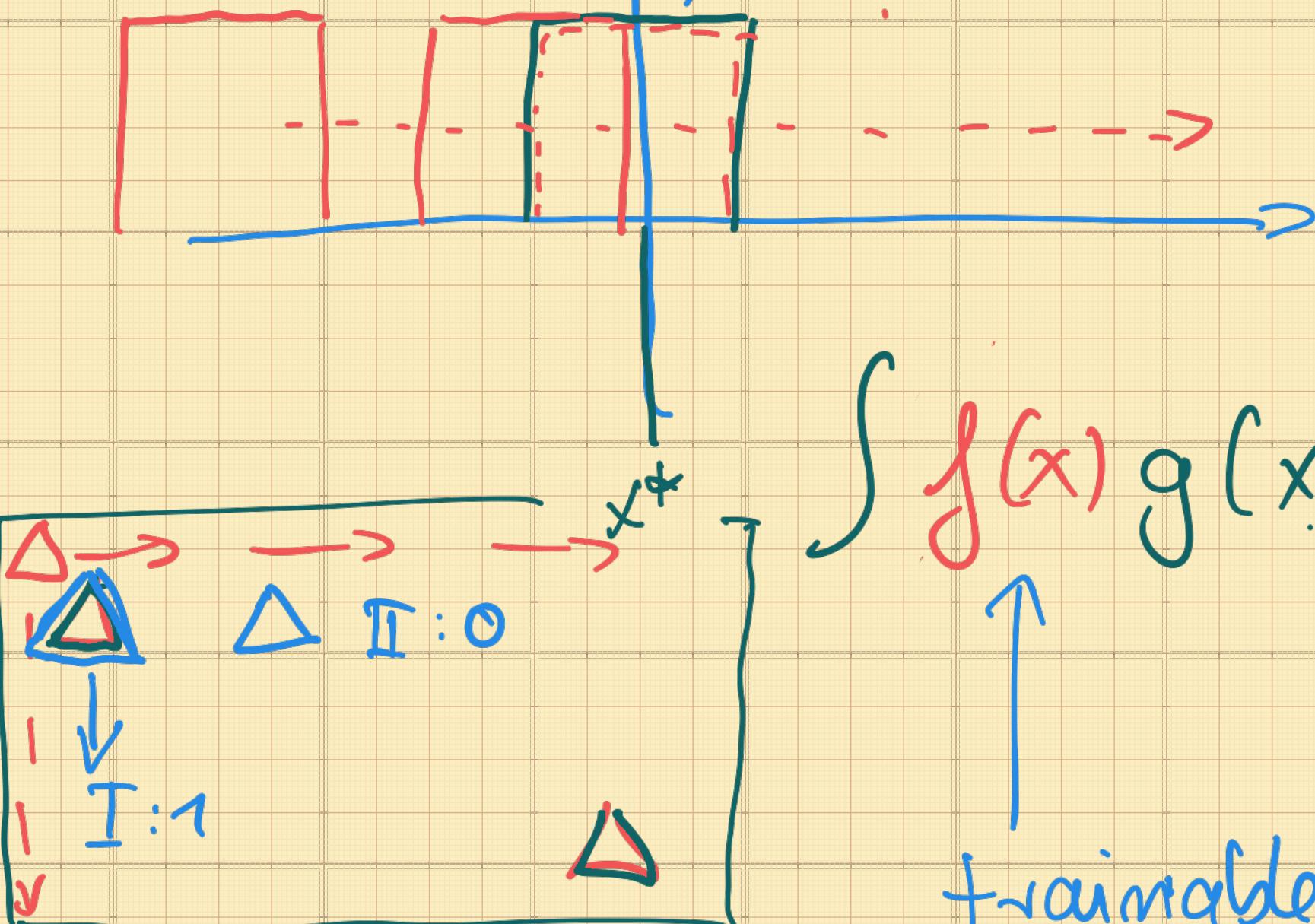
A better architecture?

- a trainable set of basis functions aka filters
- Convolutional NNs
- Convolution: a sliding projection:

continuous:  $\int f(x) g(x^* - x) dx = (f * g)(x^*)$

discrete:  $\sum_k f(k) g(k^* - k) = (f * g)(k^*)$

I: 0      II:  $\frac{1}{2}$       III: 1



+ trainable -  $\rightarrow w!$

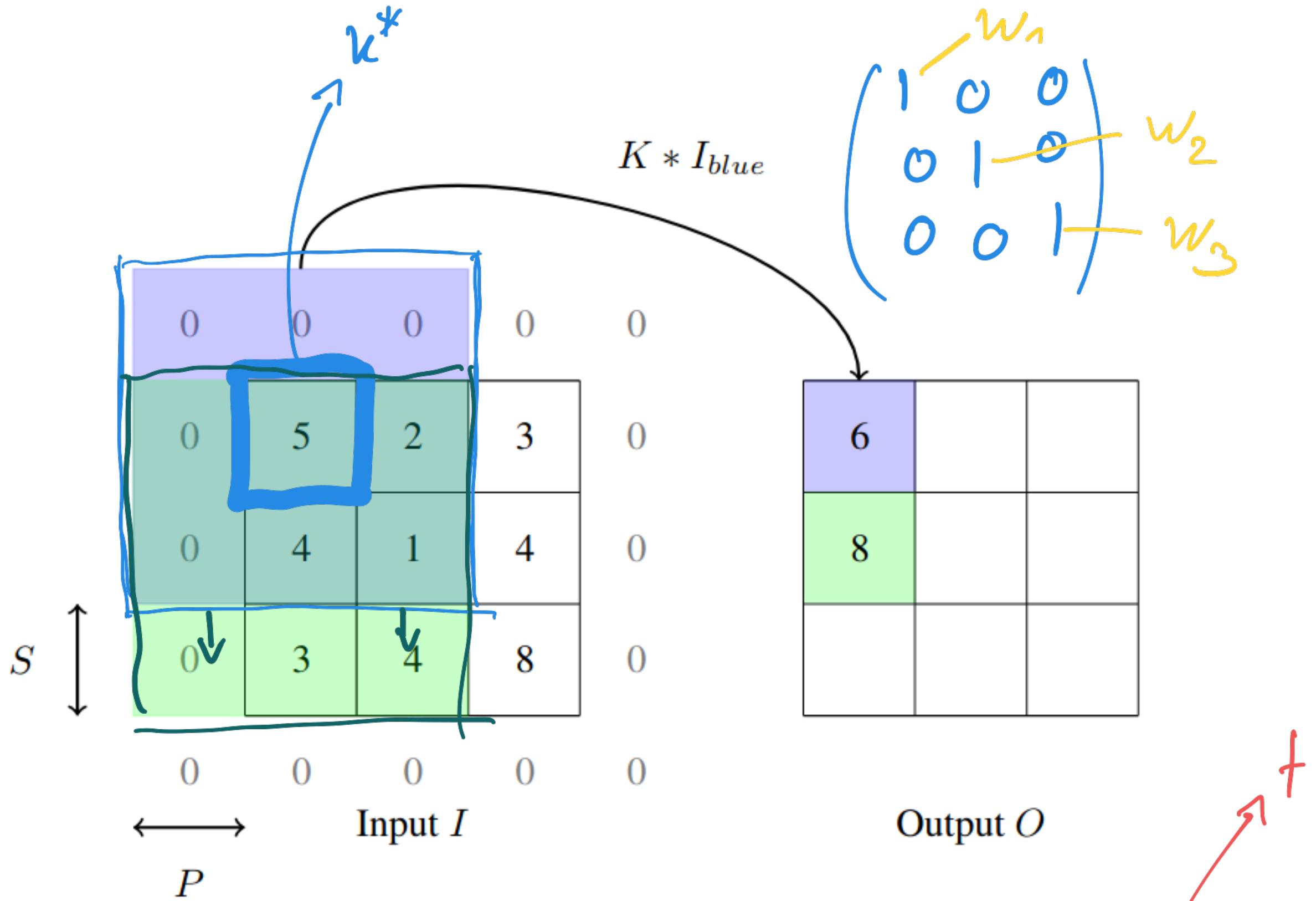
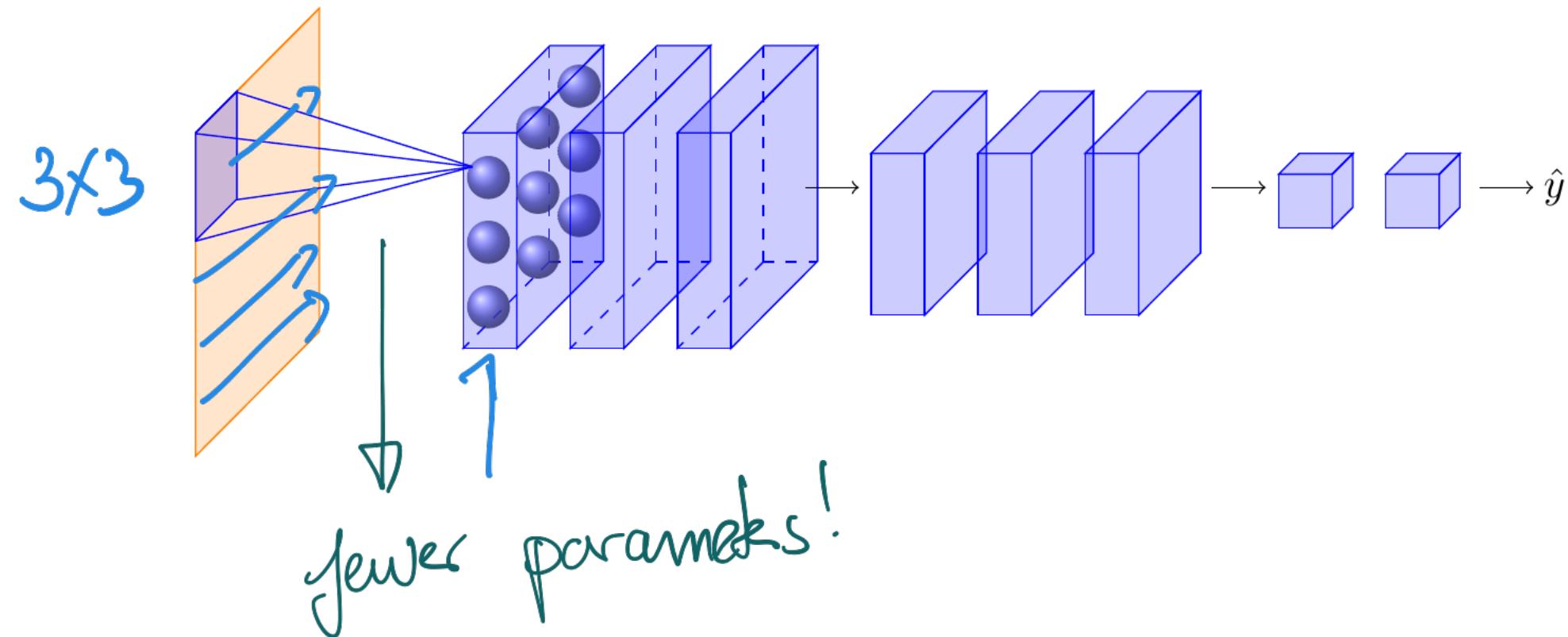


Figure 3: Illustration of a convolutional operation. The filter kernel  $K$  is of size  $3 \times 3$ , the colors indicate the corresponding filter input and output neurons. For demonstration purposes, the kernel is chosen the identity matrix, and for completeness stride ( $S$ ) and padding ( $P$ ) are chosen as  $S = P = 1$ .

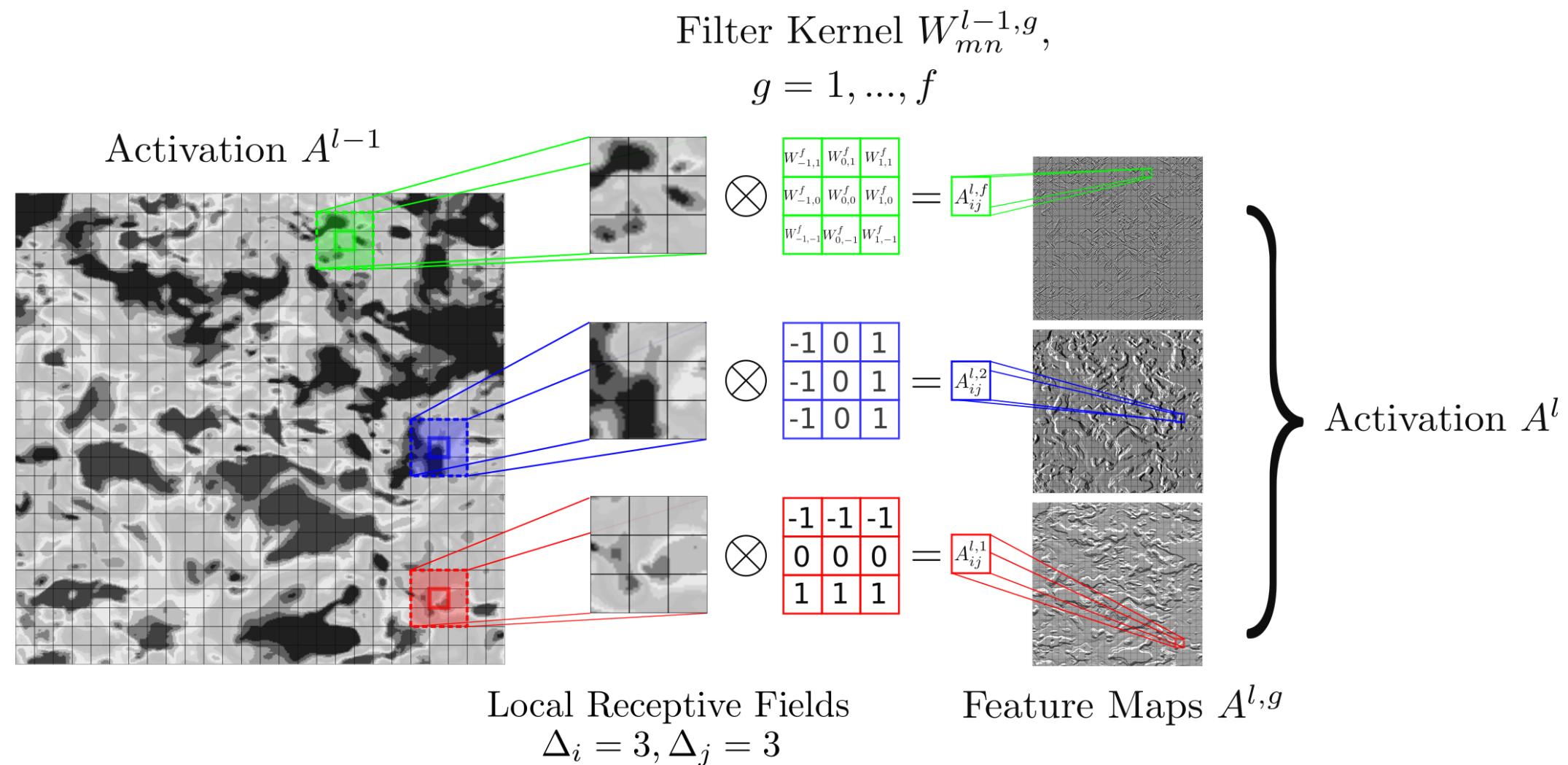
## Advanced Architectures

- Convolutional Neural Networks
  - Local connectivity, multidimensional trainable filter kernels, discrete convolution, shift invariance, hierarchical representation
  - Current state of the art for multi-D data and segmentation



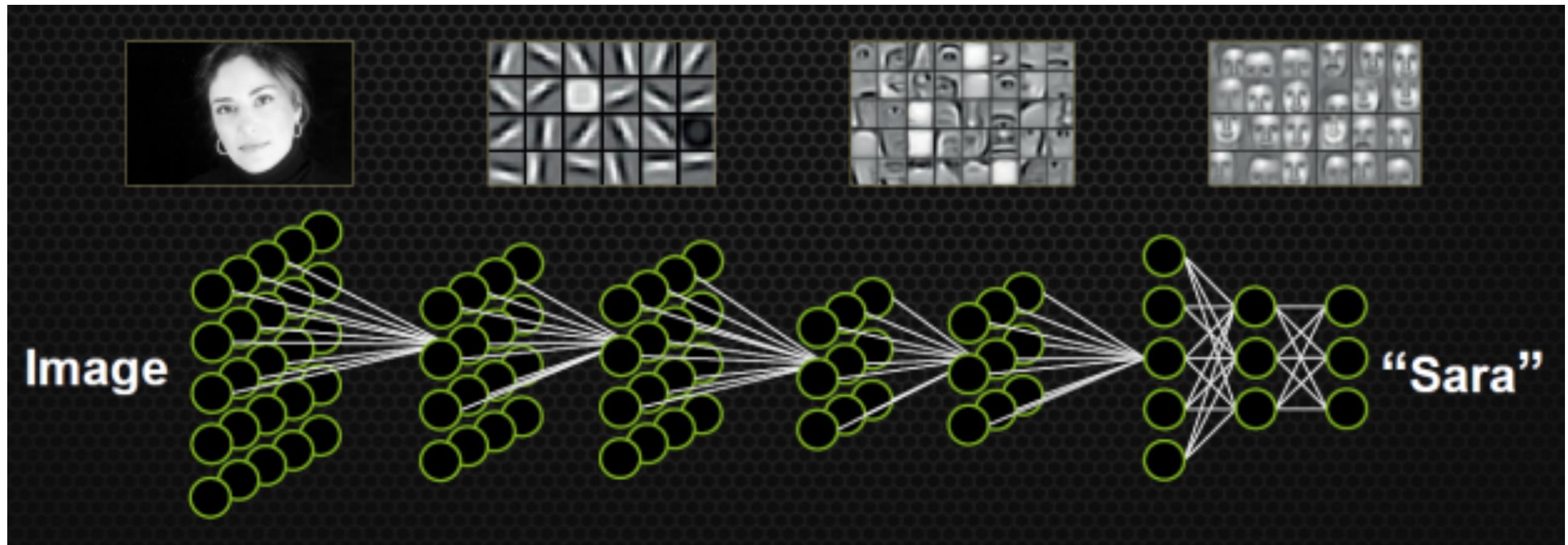
## Advanced Architectures

- Convolutional Neural Networks



## What does a CNN learn?

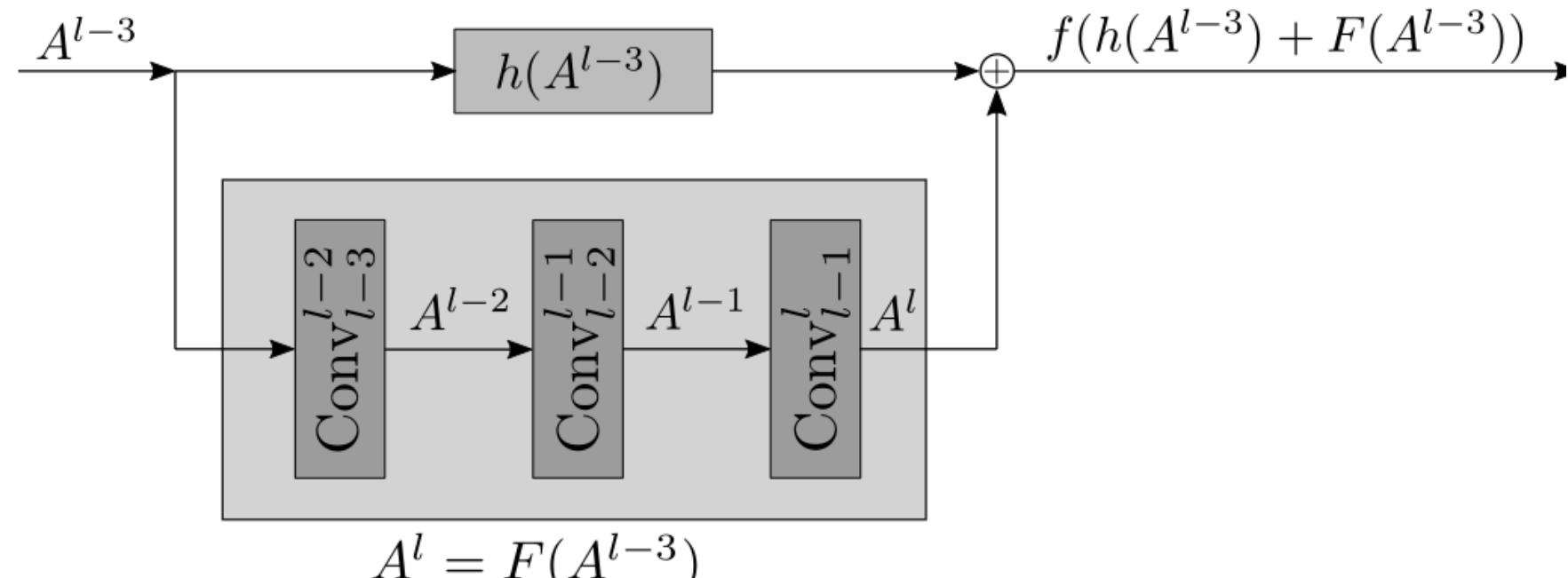
- Representation in hierarchical basis



from: H. Lee, R. Grosse, R. Ranganath, and A. Y. Ng. “Convolutional deep belief networks for scalable unsupervised learning of hierarchical representations.” In ICML 2009.

## Residual Neural Networks

- He et al. recognized that the prediction performance of CNNs may deteriorate with depths (not an overfitting problem)
- Introduction of **skip connectors** or **shortcuts**, most often identity mappings
- A sought mapping, e.g.  $G(A^{l-3})$  is split into a **linear** and non-linear (**residual**) part
- Fast passage of the linear part through the network: hundreds of CNN layers possible
- More robust identity mapping



He, Kaiming, et al. "Deep residual learning for image recognition." Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition. 2016.

# A mostly complete chart of Neural Networks

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