

# Qrlew: Differentially Private SQL Query Rewriting

Anonymous submission

## Abstract

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## Introduction

In recent years, the importance of safeguarding privacy when dealing with personal data has continuously increased. Traditional anonymization techniques have proven vulnerable to re-identification, as demonstrated by numerous works (Archie et al. 2018; Dwork et al. 2017; Narayanan and Shmatikov 2008; Sweeney, Abu, and Winn 2013). The total cost of data breaches has also significantly increased (IBM 2023) and governments have introduced stricter data protection laws. Yet, the collection, sharing, and utilization of data hold the potential to generate significant value across various industries, including healthcare, finance, transportation, and energy distribution.

To realize these benefits while managing privacy risks, researchers have turned to *differential privacy* (DP) (Wood et al. 2018; Dwork, Roth et al. 2014), which has become the gold standard in academia since its introduction by Dwork et al. in 2006 (Dwork et al. 2006) due to its provable and automatic privacy guarantees.

Despite the availability of open-source tools, DP adoption remains limited. One of the reasons for this lack of adoption is the relative complexity of the existing tools considered the utility of the results. *Qrlew* has been designed to solve these problems by providing the following features:

### **Qrlew provides automatic output privacy guarantees**

With *Qrlew* a *data owner* can let an analyst (*data practitioner*) with no expertise in privacy protection run arbitrary SQL queries with strong privacy guarantees on the output.

**Qrlew leverages existing infrastructures** *Qrlew* rewrites a SQL query into a *differentially private* SQL query that can be run on any data-store with a SQL interface from lightweight DB to big-data stores. This removes the need for a custom execution engine and enables *differentially private analytics with virtually no technical integration*.

**Qrlew leverages synthetic data** . Synthetic data are an increasingly popular way of *privatizing* a dataset. Using

jointly *differentially private* mechanisms and *differentially private* synthetic data can be a simple, yet powerful, way of managing a privacy budget and reaching better utility-privacy tradeoffs.

## Assumptions and Design Goals

In this work, we assume the *central model of differential privacy* (Near 2020), where a trusted central organization: Hospital, Insurance Company, Utility Provider, called the *data owner*, collects and stores personal data in a secured database. and wishes to let untrusted *data-practitioners* run SQL queries on its data. Furthermore, the *Qrlew* was designed to ease the

## General architecture

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## Paul on compilation

### Privacy algorithms

At this stage, we examine a *Relation* that takes one or two protected *Relation* inputs, where the entity to be protected is specified. To secure the outcome of the SQL query, it is imperative to protect not only the results obtained from aggregation functions but also the grouping keys. We will briefly describe these two steps in the following section, more technical details can be found in the appendix .

**Protecting aggregation results** The protection of aggregation functions is carried out in three sequential steps. Given that all currently supported aggregations (COUNT, SUM, AVG, VARIANCE STDDEV) can be expressed as compositions of sums, our focus will be on the SUM aggregation. Let's consider the scenario where we aim to compute the sum of a column.

1. **Limit the contribution per user:** For each user, we calculate the  $\ell_2$  norm of the observations associated with that user. Subsequently, we constrain the contribution of

a specific user by scaling  $\mathbf{x}$  with a factor chosen to maintain the original observations if the  $\ell_2$  norm of the user's observations does not exceed the clipping factor  $c$ . Conversely, if the  $\ell_2$  norm surpasses  $c$ , the  $\ell_2$  norm of the rescaled observations is restricted to  $c$ .

2. **Add random noise:** The sum of the original data is substituted with the sum of the scaled data with the addition of Gaussian noise. The level of noise is parameterized by the clipping and privacy parameters.
3. **Restrict differentially private aggregation:** The final operation involves confining the differentially private aggregation within the bounds automatically computed for the  $\text{SUM}(\mathbf{x})$ .

**Protecting grouping keys** As explained by Wilson et al., making grouping keys public could result in privacy breaches. The treatment of grouping keys varies depending on whether the analyst knows them.

- **Public Grouping Keys.** We categorize grouping keys as public when the analyst specifies them in the WHERE clause. In this scenario, all user-specified keys must be disclosed, even if they do not exist in the database. If a key is absent in the database, differentially private results will include these missing keys, and the corresponding aggregations will be random noise.
- **Revealing Private Keys through  $\tau$ -Thresholding** As introduced by Wilson et al., tau-thresholding involves releasing keys whose differentially private noise surpasses a threshold determined by privacy parameters.

When the SQL query involves both public and private grouping keys, we perform cross joins on the grouping keys obtained through the two algorithms.

## Comparison to other systems

### Known limitations

*Qrlew* relies on the random number generator of the SQL engine used. It is usually not a cryptographic noise.

*Qrlew* uses the floating-point numbers of the host SQL engine, therefore our system is liable to the vulnerabilities described in

### Useful links

#### PPAI

Last year papers: <https://aaai-ppai23.github.io/#sp2> This year program: <https://ppai-workshop.github.io/>

#### Comparable open-source projects

- Paszke et al. 2017 - Automatic differentiation in PyTorch <https://openreview.net/pdf?id=BJJsrnfCZ>
- Frostig et al. 2018 - Compiling machine learning programs via high-level tracing <https://mlsys.org/Conferences/2019/doc/2018/146.pdf>

## Comparable DP SQL papers

- Lessons Learned: Surveying the Practicality of Differential Privacy in the Industry (Garrido et al. 2022)
- Tumult Analytics: a robust, easy-to-use, scalable, and expressive framework for differential privacy (Berghel et al. 2022)
- Differentially Private SQL with Bounded User Contribution (Wilson et al. 2019)
- CHORUS: a Programming Framework for Building Scalable Differential Privacy Mechanisms (Johnson et al. 2020)
- Towards Practical Differential Privacy for SQL Queries (Johnson, Near, and Song 2018)

## Reference Examples

$$\tilde{\mathbf{X}} = \begin{bmatrix} \tilde{x}_1 \\ \tilde{x}_2 \\ \vdots \\ \tilde{x}_n \end{bmatrix} \text{ with } \forall i, \tilde{x}_i = \frac{1}{\max(1, \frac{1}{\Delta \tilde{\mathbf{x}}} \sqrt{\sum_{k \in \Sigma_i} x_k^2})} \quad (1)$$

$\Sigma_i$  denotes all the indices that correspond to the  $i^{th}$  group.  $\Delta \tilde{\mathbf{x}}$  is the absolute upper bound of the column

$$\Delta \tilde{\mathbf{x}} = \max(|\min \mathbf{x}|, |\max \mathbf{x}|) \quad (2)$$

In the case of the count, the ve

All the aggregations can be rewritten as SUM or COUNT.

$$\text{COUNT}(\mathbf{x}) \rightarrow \text{COUNT}(\tilde{\mathbf{I}}) + \text{Gaussian}(\sigma(\tilde{\mathbf{I}})) \quad (3)$$

$$\text{SUM}(\mathbf{x}) \rightarrow \text{SUM}(\tilde{\mathbf{x}}) + \text{Gaussian}(\sigma(\tilde{\mathbf{x}})) \quad (4)$$

$$\text{SUM}(\mathbf{x}) \rightarrow \text{SUM}(\tilde{\mathbf{x}}) + \text{Gaussian}(\sqrt{2 \ln(\frac{1.25}{\delta})} \times \frac{c}{\epsilon}) \quad (5)$$

$$\sigma(\tilde{\mathbf{x}}) = \quad (6)$$

Thank you for reading these instructions carefully. We look forward to receiving your electronic files!

## References

- Archie, M.; Gershon, S.; Katcoff, A.; and Zeng, A. 2018. Who's watching? de-anonymization of netflix reviews using amazon reviews.
- Berghel, S.; Bohannon, P.; Desfontaines, D.; Estes, C.; Haney, S.; Hartman, L.; Hay, M.; Machanavajjhala, A.; Magerlein, T.; Miklau, G.; et al. 2022. Tumult Analytics: a robust, easy-to-use, scalable, and expressive framework for differential privacy. *arXiv preprint arXiv:2212.04133*.
- Dwork, C.; McSherry, F.; Nissim, K.; and Smith, A. 2006. Calibrating noise to sensitivity in private data analysis. In *Theory of Cryptography: Third Theory of Cryptography Conference, TCC 2006, New York, NY, USA, March 4-7, 2006. Proceedings 3*, 265–284. Springer.
- Dwork, C.; Roth, A.; et al. 2014. The algorithmic foundations of differential privacy. *Foundations and Trends® in Theoretical Computer Science*, 9(3–4): 211–407.

- Dwork, C.; Smith, A.; Steinke, T.; and Ullman, J. 2017. Exposed! a survey of attacks on private data. *Annual Review of Statistics and Its Application*, 4: 61–84.
- Garrido, G. M.; Liu, X.; Matthes, F.; and Song, D. 2022. Lessons learned: Surveying the practicality of differential privacy in the industry. *arXiv preprint arXiv:2211.03898*.
- IBM. 2023. Cost of a Data Breach Report 2023.
- Johnson, N.; Near, J. P.; Hellerstein, J. M.; and Song, D. 2020. Chorus: a programming framework for building scalable differential privacy mechanisms. In *2020 IEEE European Symposium on Security and Privacy (EuroS&P)*, 535–551. IEEE.
- Johnson, N.; Near, J. P.; and Song, D. 2018. Towards Practical Differential Privacy for SQL Queries. *Proc. VLDB Endow.*, 11(5): 526–539.
- Narayanan, A.; and Shmatikov, V. 2008. Robust de-anonymization of large sparse datasets. In *2008 IEEE Symposium on Security and Privacy (sp 2008)*, 111–125. IEEE.
- Near, J. 2020. Threat Models for Differential Privacy.
- Sweeney, L.; Abu, A.; and Winn, J. 2013. Identifying participants in the personal genome project by name (a re-identification experiment). *arXiv preprint arXiv:1304.7605*.
- Wilson, R. J.; Zhang, C. Y.; Lam, W.; Desfontaines, D.; Simmons-Marengo, D.; and Gipson, B. 2019. Differentially private SQL with bounded user contribution. *arXiv preprint arXiv:1909.01917*.
- Wood, A.; Altman, M.; Bembenek, A.; Bun, M.; Gaboardi, M.; Honaker, J.; Nissim, K.; O’Brien, D. R.; Steinke, T.; and Vadhan, S. 2018. Differential privacy: A primer for a non-technical audience. *Vand. J. Ent. & Tech. L.*, 21: 209.