## XIIS Math

$$\pi(n) = \sum_{m=2}^{n} \left[ \left( \sum_{k=1}^{m-1} \lfloor (m/k) / \lceil m/k \rceil \rfloor \right)^{-1} \right]$$

$$\pi(n) = \sum_{k=2}^{n} \left[ \frac{\phi(k)}{k-1} \right]$$

$$1 + \left( \frac{1}{1-x^2} \right)^3$$

$$1 + \left( \frac{1}{\frac{x^2}{1-\frac{x^2}{y^3}}} \right)^3$$

$$\frac{a+1}{b} / \frac{c+1}{d}$$

$$\left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) |\phi(x+iy)|^2$$

$$\sum_{\substack{0 \le i \le m \\ 0 < j < n}} P(i,j)$$

$$0 < j < n$$

$$\int_0^3 9x^2 + 2x + 4 \, dx = 3x^3 + x^2 + 4x + C \Big]_0^3 = 102$$

$$e^{x+iy} = e^x(\cos y + i \sin y)$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

 $f(x) = \begin{cases} x, & \text{if } 0 \le x \le \frac{1}{2} \\ 1 - x, & \text{if } \frac{1}{2} \le x \le 1 \end{cases}$ 

$$\sqrt{1 + \sqrt{1 + \sqrt{1 + \sqrt{1 + \sqrt{1 + \sqrt{1 + x}}}}}}$$

$$S^{-1}TS = dg(\omega_1, ..., \omega_n) = \Lambda$$

$$Pr(m = n \mid m + n = 3)$$

$$\sin 18^* = \frac{1}{4}(\sqrt{5} - 1)$$

$$k = 1.38 \times 10^{-16} \text{ erg } / \text{ K}$$

$$\tilde{\Phi} \subset NL_1^* / N = \tilde{L}_1^* \subseteq \cdots \subseteq NL_n^* / N = \tilde{L}_n^*$$

$$I(\lambda) = \iint_D g(x, y) e^{i\lambda h(x, y)} dx dy$$

$$\int_0^1 \cdots \int_0^1 f(x_1, ..., x_n) dx_1 ... dx_n$$

$$x_{2m} \equiv \begin{cases} Q(X_m^2 - P_2 W_m^2) - 2S^2 & (m \text{ odd}) \\ P_2^2 (X_m^2 - P_2 W_m^2) - 2S^2 & (m \text{ even}) \end{cases}$$

$$(1 + x_1 z + x_1^2 z^2 + \cdots) ... (1 + x_n z + x_n^2 z^2 + \cdots) = \frac{1}{(1 - x_1 z) ... (1 - x_n z)}$$

$$\prod_{j \ge 0} \left( \sum_{k \ge 0} a_{jk} z^k \right) = \sum_{n \ge 0} z^n \left( \sum_{k_0, k_1, ..., k_n \ge 0 \atop k_0 + k_1 + \cdots = n} a_{0k_0} a_{1k_1} ... \right)$$

$$\sum_{n = 0}^{\infty} a_n z^n \quad \text{converges if} \quad |z| < \left( \limsup_{n \to \infty} \sqrt[4]{a - n} \right)$$

$$\frac{f(x + \Delta x) - f(x)}{\Delta x} \to f'(x) \quad \text{as } \Delta x \to 0$$

$$||u_i|| = 1, \qquad u_i \cdot u_j = 0 \quad \text{if } i \ne j$$

$$\prod_{k\geq 0} \frac{1}{(1-q^k z)} = \sum_{n\geq 0} z^n / \prod_{1\leq k\leq n} (1-q^k).$$
 (16')

$$T(n) \le T(2^{\lceil \lg n \rceil}) \le c(3^{\lceil \lg n \rceil} - 2^{\lceil \lg n \rceil})$$

$$< 3c \cdot 3^{\lg n}$$

$$= 3cn^{\lg n}$$

$$P(x) = a_0 + a_1 x + a_2 x^2 + \dots + a_n x^2,$$
  

$$P(-x) = a_0 - a_1 x + a_2 x^2 - \dots + (-1)^n a_n x^2.$$
(30)

(9) 
$$\gcd(u, v) = \gcd(v, u);$$

(10) 
$$\gcd(u, v) = \gcd(-u, v).$$

$$\left(\int_{-\infty}^{\infty} e^{-x^2} dx\right)^2 = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{-(x^2 + y^2)} dx dy$$

$$= \int_{0}^{2\pi} \int_{0}^{\infty} e^{-r^2} r dr d\theta$$

$$= \int_{0}^{2\pi} \left(-\frac{e^{-r^2}}{2}\Big|_{r=0}^{r=\infty}\right) d\theta$$

$$= \pi. \tag{11}$$