## Minimal Constraint Subsets Detected for differential trail in Table 8 DDH21+

```
the 0 Th Minimal constraint set is:
 y^0_0 + x^1_4 + k_1_0 + k_2_0 = 0
 y^0_0 + y^0_1 + x^1_1 + k_1 + k_2 = 0
 y^0_2 + x^1_6 + k_1_2 + k_2_0 = 0
 y^0_2 + [y^0_8] + [x^1_14] + k_1_2 + k_2_0 = 0
 y^0 5 + [y^0 8] + x^1 10 + k1 5 + k2 5 0 = 0
 y^1_0 + y^1_1 + x^2_1 + k_1_9 + k_2_9_0 = 0
 v^1 1 + v^1 11 + [v^1 14] + [x^2 1] + k1 15 + k2 15 0 = 0
 y^1_1 + x^2_5 + k_1_1 + k_2_1 = 0
 y^1 3 + y^1 9 + y^1 12 + [x^2 3] + k1 13 + k2 13 0 = 0
 y^1_3 + y^1_9 + [x^2_{15}] + k_{113} + k_{2130} = 0
 y^1_4 + y^1_11 + x^2_9 + k_{11}0 + k_{21}0_0 = 0
 y^1_6 + y^1_9 + x^2_{11} + k_{112} + k_{2120} = 0
 [y^2_1] + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
 y^2_2 + y^2_8 + [y^2_15] + [x^3_2] + k_1_0 + k_2_1 = 0
 y^2_2 + x^3_6 + k_1_0 + k_2_1 = 0
 [y^2 3] + y^2 9 + y^2 12 + x^3 3 + k1 5 + k2 5 1 = 0
 y^2_5 + y^2_8 + x^3_10 + k_16 + k_261 = 0
 y^3_0 + y^3_10 + y^3_13 + x^4_0 + k_115 + k_215_1 = 0
 y^3_0 + x^4_4 + k_{115} + k_{2151} = 0
 [y^3_2] + [x^4_6] + k_1_9 + k_2_9_1 = 0
 y^3 + y^3 + y^4 
 y^3_6 + y^3_9 + x^4_11 + k_1_10 + k_2_10_1 = 0
 y^4_0 + [x^5_4] + k_1^7 + k_2^7_2 = 0
 y^4_2 + y^4_8 + y^4_15 + x^5_2 + k_11 + k_21_2 = 0
 y^4 2 + y^4 8 + x^5 14 + k1 1 + k2 1 2 = 0
 y^4 3 + x^5 7 + k1 6 + k2 6 2 = 0
 y^4 3 + y^4 9 + x^5 15 + k1 6 + k2 6 2 = 0
 y^4_4 + y^4_11 + x^5_9 + k_10 + k_202 = 0
 [y^4_6] + y^4_9 + [x^5_11] + k_1_2 + k_2_2_2 = 0
 y^5_0 + x^6_4 + k_{111} + k_{2112} = 0
 y^5_0 + y^5_10 + x^6_12 + k_111 + k_211_2 = 0
 y^5_1 + [y^5_11] + y^5_14 + [x^6_1] + k_{11}3 + k_{2132} = 0
 y^5_1 + [y^5_1] + [x^6_1] + k_1_1 + k_2_1_2 = 0
 y^5_2 + y^5_8 + y^5_15 + x^6_2 + k_1_15 + k_2_15_2 = 0
 y^5_2 + x^6_6 + k_1_15 + k_2_15_2 = 0
 y^5_2 + y^5_8 + x^6_14 + k_1_15 + k_2_15_2 = 0
 y^5_3 + x^6_7 + k_{112} + k_{2122} = 0
 y^5_3 + y^5_9 + x^6_{15} + k_{112} + k_{212}^2 = 0
 [y^5_4] + [y^5_11] + x^6_9 + k_1_9 + k_2_9_2 = 0
 y^5_7 + y^5_10 + x^6_8 + k_1_14 + k_2_14_2 = 0
 y^6_0 + y^6_10 + [y^6_13] + [x^7_0] + k_1_3 + k_2_3_3 = 0
 y^6 0 + x^7 4 + k1 3 + k2 3 3 = 0
```

```
[y^6_1] + y^6_1 + y^6_1 + y^6_1 + x^7_1 + k_1^5 + k_2^5_3 = 0
y^6 2 + y^6 8 + y^6 15 + x^7 2 + k1 7 + k2 7 3 = 0
y^6_3 + y^6_9 + y^6_12 + x^7_3 + k_14 + k_24_3 = 0
y^6_3 + y^6_9 + x^7_15 + k_14 + k_24_3 = 0
y^6_4 + y^6_11 + x^7_9 + k_11 + k_21_3 = 0
y^6_6 + y^6_9 + x^7_11 + k_10 + k_20_3 = 0
y^6 7 + y^6 10 + x^7 8 + k1 6 + k2 6 3 = 0
[y^7_0] + x^8_4 + k_{113} + k_{2133} = 0
v^7 1 + x^8 5 + k1 14 + k2 14 3= 0
y^7_2 + y^7_8 + y^7_15 + x^8_2 + k_1_11 + k_2_11_3 = 0
y^7 3 + y^7 9 + x^8 15 + k1 10 + k2 10 3 = 0
y^7_4 + y^7_11 + x^8_9 + k_{115} + k_{215}3 = 0
y^8_2 + y^8_8 + y^8_15 + x^9_2 + k_1^3 + k_2^4_0
y^8_3 + x^9_7 + k_1_2 + k_2_4 = 0
y^8_3 + y^8_9 + x^9_15 + k_1_2 + k_2_4 = 0
v^8 4 + v^8 11 + x^9 9 + k1 7 + k2 7 4 = 0
y^8_5 + y^8_8 + x^9_10 + k_10 + k_204 = 0
y^9 2 + y^9 8 + y^9 15 + [x^10 2] + k1 13 + k2 13 4 = 0
y^9_3 + x^10_7 + k_{18} + k_{284} = 0
y^9_3 + y^9_9 + x^10_15 + k_18 + k_28_4 = 0
y^9_5 + y^9_8 + x^10_10 + k_19 + k_29_4 = 0
y^9_7 + y^9_10 + x^10_8 + k_110 + k_210_4 = 0
[y^10 2] + y^10 8 + y^10 15 + x^11 2 + k1 5 + k2 5 5 = 0
y^10_7 + y^10_10 + x^11_8 + k_12 + k_25= 0
y^1_1_2 + y^1_1_8 + y^1_1_5 + x^1_2_2 + k_1_4 + k_2_4_5 = 0
y^14_1 + x^15_5 + k_10 + k_207 = 0
y^14_2 + y^14_8 + y^14_15 + x^15_2 + k_14 + k_24_7 = 0
y^14 6 + y^14 9 + x^15 11 + k1 5 + k2 5 7 = 0
S(x^0 1) + y^0 1 = 0
S(x^0_3) + y^0_3 = 0
S(x^0_5) + y^0_5 = 0
S(x^0_9) + y^0_9 = 0
S(x^0_12) + y^0_12 = 0
S(x^1_3) + y^1_3 = 0
S(x^1_6) + y^1_6 = 0
S(x^1_10) + y^1_10 = 0
S(x^2_4) + y^2_4 = 0
S(x^2_6) + y^2_6 = 0
S(x^2_11) + y^2_11 = 0
S([x^2_15]) + [y^2_15] = 0
S([x^3_2]) + [y^3_2] = 0
S(x^3_4) + y^3_4 = 0
S(x^3_1) + y^3_1 = 0
S(x^3 9) + y^3 9 = 0
```

```
S(x^3_11) + y^3_11 = 0
```

$$S(x^3 14) + y^3 14 = 0$$

$$S(x^3_15) + y^3_15 = 0$$

$$S(x^4_1) + y^4_1 = 0$$

$$S(x^4_2) + y^4_2 = 0$$

$$S(x^4_4) + y^4_4 = 0$$

$$S([x^4 6]) + [y^4 6] = 0$$

$$S(x^4_7) + y^4_7 = 0$$

$$S(x^4_8) + y^4_8 = 0$$

$$S(x^4_9) + y^4_9 = 0$$

$$S(x^4 12) + y^4 12 = 0$$

$$S(x^4_13) + y^4_13 = 0$$

$$S(x^4_14) + y^4_14 = 0$$

$$S(x^4_15) + y^4_15 = 0$$

$$S(x^5_0) + y^5_0 = 0$$

$$S(x^5_1) + y^5_1 = 0$$

$$S(x^5_3) + y^5_3 = 0$$

$$S([x^5_4]) + [y^5_4] = 0$$

$$S(x^5_8) + y^5_8 = 0$$

$$S(x^5_9) + y^5_9 = 0$$

$$S([x^5_11]) + [y^5_11] = 0$$

$$S(x^5_15) + y^5_15 = 0$$

$$S(x^6 2) + y^6 2 = 0$$

$$S(x^6_4) + y^6_4 = 0$$

$$S(x^6_5) + y^6_5 = 0$$

$$S(x^6_9) + y^6_9 = 0$$

$$S(x^6_15) + y^6_15 = 0$$

$$S(x^7_2) + y^7_2 = 0$$

$$S(x^7_1) + y^7_1 = 0$$

$$S(x^7_9) + y^7_9 = 0$$

$$S(x^7_10) + y^7_10 = 0$$

$$S(x^7_15) + y^7_15 = 0$$

$$S(x^8_2) + y^8_2 = 0$$

$$S(x^8_7) + y^8_7 = 0$$

$$S(x^8_8) + y^8_8 = 0$$

$$S(x^8_10) + y^8_10 = 0$$

$$S(x^8_15) + y^8_15 = 0$$

$$S(x^9_2) + y^9_2 = 0$$

$$S(x^9_8) + y^9_8 = 0$$

the 1 Th Minimal constraint set is:

$$y^0_2 + x^1_6 + k_1_2 + k_2_0 = 0$$

$$y^0_2 + [y^0_8] + [x^1_14] + k_1_2 + k_2_0 = 0$$

$$y^0_5 + [y^0_8] + x^1_10 + k_15 + k_25_0 = 0$$

$$y^1 0 + y^1 10 + x^2 12 + k1 9 + k2 9 0 = 0$$

```
y^1_1 + y^1_1 + [y^1_14] + [x^2_1] + k_{115} + k_{215}0 = 0
y^1 1 + y^1 11 + x^2 13 + k1 15 + k2 15 0 = 0
y^1_6 + y^1_9 + x^2_{11} + k_{112} + k_{212} = 0
y^2_0 + y^2_10 + y^2_13 + x^3_0 + k_11 + k_211 = 0
y^2_0 + y^2_10 + x^3_12 + k_11 + k_211 = 0
[y^2_1] + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
[y^2 3] + y^2 9 + y^2 12 + x^3 3 + k1 5 + k2 5 1 = 0
[y^2_3] + y^2_9 + x^3_15 + k_1_5 + k_2_5_1 = 0
y^2_4 + y^2_11 + x^3_9 + k_1^2 + k_2^1 = 0
y^3_0 + y^3_10 + y^3_13 + x^4_0 + k_{115} + k_{215} = 0
y^3 0 + x^4 4 + k1 15 + k2 15 1 = 0
y^3 0 + y^3 10 + x^4 12 + k1 15 + k2 15 1 = 0
y^3_1 + x^4_5 + k_{111} + k_{2111} = 0
[y^3_2] + [y^3_8] + y^3_15 + x^4_2 + k_1_9 + k_2_9_1 = 0
[y^3_2] + [x^4_6] + k_1_9 + k_2_9_1 = 0
[y^3_2] + [y^3_8] + x^4_14 + k_19 + k_29_1 = 0
y^3_3 + y^3_9 + y^3_{12} + x^4_3 + k_{114} + k_{2141} = 0
y^4 1 + y^4 11 + y^4 14 + x^5 1 + k1 3 + k2 3 2 = 0
y^4_1 + x^5_5 + k_1_3 + k_2_3_2 = 0
y^4_2 + y^4_8 + x^5_14 + k_11 + k_21_2 = 0
y^4_3 + y^4_9 + y^4_12 + x^5_3 + k_1_6 + k_2_6_2 = 0
y^4_4 + y^4_11 + x^5_9 + k_10 + k_20_2 = 0
y^4 5 + y^4 8 + x^5 10 + k1 4 + k2 4 2 = 0
[y^4_6] + y^4_9 + [x^5_11] + k_1_2 + k_2_2_2 = 0
y^5_0 + x^6_4 + k_1_1 + k_2_1_2 = 0
y^5_0 + y^5_1 + x^6_1 + k_1 + k_2 + k_2 = 0
y^5_1 + [y^5_1] + y^5_1 + [x^6_1] + k_{11} + k_{2132} = 0
y^5 2 + x^6 6 + k1 15 + k2 15 2 = 0
y^5_2 + y^5_8 + x^6_14 + k_1_15 + k_2_15_2 = 0
y^5_3 + y^5_9 + x^6_{15} + k_{112} + k_{212}^2 = 0
y^5_5 + y^5_8 + x^6_10 + k_110 + k_2102 = 0
y^6_0 + x^7_4 + k_1^3 + k_2^3_3 = 0
y^6_0 + y^6_10 + x^7_12 + k_1^3 + k_2^3_3 = 0
[y^6_1] + y^6_11 + y^6_14 + x^7_1 + k_1^5 + k_2^3 = 0
y^6_2 + y^6_8 + y^6_15 + x^7_2 + k_1^7 + k_2^3 = 0
y^6_2 + y^6_8 + x^7_14 + k_1^7 + k_2^3 = 0
y^6_3 + y^6_9 + y^6_12 + x^7_3 + k_14 + k_24_3 = 0
y^6_3 + x^7_7 + k_1_4 + k_2_4_3 = 0
y^6_4 + y^6_11 + x^7_9 + k_11 + k_21_3 = 0
y^6_6 + y^6_9 + x^7_11 + k_10 + k_203 = 0
[y^7_0] + x^8_4 + k_{113} + k_{2133} = 0
[y^7_0] + y^7_10 + x^8_12 + k_113 + k_213_3 = 0
y^7_1 + y^7_1 + y^7_1 + y^7_1 + x^8_1 + k_114 + k_214_3 = 0
y^7 1 + x^8 5 + k1 14 + k2 14 3 = 0
```

$$y^8_0 + y^8_10 + y^8_13 + x^9_0 + k_1^5 + k_2^5_4 = 0$$

$$y^8_0 + y^8_1 + x^9_1 + k_1^5 + k_2^4 = 0$$

$$y^8_3 + y^8_9 + y^8_{12} + x^9_3 + k_{12} + k_{224} = 0$$

$$y^8_4 + y^8_11 + x^9_9 + k_1^7 + k_2^7_4 = 0$$

$$y^8_5 + y^8_8 + x^9_10 + k_10 + k_204 = 0$$

$$y^9_0 + y^9_1 + x^1_1 + k_1_1 + k_2_1 = 0$$

$$y^9 3 + y^9 9 + y^9 12 + x^10 3 + k1 8 + k2 8 4 = 0$$

$$y^10_3 + y^10_9 + y^10_12 + x^11_3 + k_10 + k_20_5 = 0$$

$$y^14_2 + y^14_8 + y^14_15 + x^15_2 + k_14 + k_24_7 = 0$$

$$y^14_6 + y^14_9 + x^15_11 + k_15 + k_25_7 = 0$$

$$S(x^0_1) + y^0_1 = 0$$

$$S(x^0_12) + y^0_12 = 0$$

$$S(x^0_13) + y^0_13 = 0$$

$$S(x^1_0) + y^1_0 = 0$$

$$S(x^1_3) + y^1_3 = 0$$

$$S(x^1_9) + y^1_9 = 0$$

$$S(x^1_12) + y^1_12 = 0$$

$$S(x^1_15) + y^1_15 = 0$$

$$S(x^2 2) + y^2 2 = 0$$

$$S([x^2_3]) + [y^2_3] = 0$$

$$S(x^2_4) + y^2_4 = 0$$

$$S(x^2_5) + y^2_5 = 0$$

$$S(x^2_6) + y^2_6 = 0$$

$$S(x^2_12) + y^2_12 = 0$$

$$S(x^2_14) + y^2_14= 0$$

$$S(x^3_1) + y^3_1 = 0$$

$$S(x^3_3) + y^3_3 = 0$$

$$S(x^3_5) + y^3_5 = 0$$

$$S(x^3_9) + y^3_9 = 0$$

$$S(x^3_10) + y^3_10 = 0$$

$$S(x^3_11) + y^3_11 = 0$$

$$S(x^3_14) + y^3_14= 0$$

$$S(x^4_1) + y^4_1 = 0$$

$$S(x^4_4) + y^4_4 = 0$$

$$S([x^4_6]) + [y^4_6] = 0$$

$$S([x^4_10]) + [y^4_10] = 0$$

$$S(x^4_12) + y^4_12 = 0$$

$$S(x^4_14) + y^4_14=0$$

$$S(x^4_15) + y^4_15 = 0$$

$$S(x^5 1) + y^5 1 = 0$$

```
S(x^5_3) + y^5_3 = 0
 S([x^5 4]) + [y^5 4] = 0
 S(x^5_-7) + y^5_-7 = 0
 S(x^5_9) + y^5_9 = 0
 S([x^5_11]) + [y^5_11] = 0
 S(x^5_12) + y^5_12 = 0
 S(x^6 3) + y^6 3 = 0
 S(x^6_4) + y^6_4 = 0
 S(x^6_5) + y^6_5 = 0
 S(x^6_8) + y^6_8 = 0
 S(x^6 9) + y^6 9 = 0
 S(x^6_12) + y^6_12 = 0
 S([x^6_13]) + [y^6_13] = 0
 S([x^7_0]) + [y^7_0] = 0
 S(x^7_3) + y^7_3 = 0
 S(x^7_9) + y^7_9 = 0
 S(x^7_10) + y^7_10 = 0
 S(x^7 12) + y^7 12 = 0
 S(x^8_3) + y^8_3 = 0
 S(x^8_12) + y^8_12 = 0
the 2 Th Minimal constraint set is:
y^0_0 + x^1_4 + k_1_0 + k_2_0_0 = 0
y^0 0 + y^0 10 + x^1 12 + k1 0 + k2 0 0 = 0
y^0_2 + x^1_6 + k_1_2 + k_2_0 = 0
y^0_2 + [y^0_8] + [x^1_14] + k_1^2 + k_2^0 = 0
y^0_5 + [y^0_8] + x^1_10 + k_15 + k_250 = 0
y^1_1 + y^1_1 + [y^1_14] + [x^2_1] + k_{115} + k_{215}0 = 0
y^1 1 + x^2 5 + k1 15 + k2 15 0 = 0
y^1 4 + y^1 11 + x^2 9 + k1 10 + k2 10 0 = 0
y^1_6 + y^1_9 + x^2_{11} + k_{112} + k_{212} = 0
[y^2_1] + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
y^2_2 + y^2_8 + [y^2_15] + [x^3_2] + k_1_0 + k_2_1 = 0
y^2_2 + x^3_6 + k_1_0 + k_2_1 = 0
 [y^2_3] + x^3_7 + k_1^5 + k_2^5_1 = 0
 [y^2_3] + y^2_9 + x^3_{15} + k_{15} + k_{25}1 = 0
y^2_4 + y^2_11 + x^3_9 + k_1^2 + k_2^1 = 0
y^2_5 + y^2_8 + x^3_10 + k_16 + k_261 = 0
[y^3_2] + [y^3_8] + y^3_15 + x^4_2 + k_1_9 + k_2_9_1 = 0
 [y^3_2] + [x^4_6] + k_1_9 + k_2_9_1 = 0
 [y^3_2] + [y^3_8] + x^4_14 + k_1_9 + k_2_9_1 = 0
y^3_6 + y^3_9 + x^4_11 + k_1_10 + k_2_10_1 = 0
y^3-7 + y^3-10 + x^4-8 + k_1-13 + k_2-13-1=0
y^4_1 + y^4_1 + y^4_1 + x^5_1 + k_3 + k_3^2 = 0
y^4 1 + x^5 5 + k1 3 + k2 3 2 = 0
```

```
y^4_2 + y^4_8 + x^5_14 + k_11 + k_21_2 = 0
y^4 3 + x^5 7 + k1 6 + k2 6 2 = 0
y^4_3 + y^4_9 + x^5_15 + k_16 + k_26_2 = 0
[y^4_6] + y^4_9 + [x^5_11] + k_1_2 + k_2_2_2 = 0
y^5_0 + x^6_4 + k_1_1 + k_2_1_2 = 0
y^5_0 + y^5_10 + x^6_12 + k_111 + k_211_2 = 0
y^5_1 + [y^5_11] + y^5_14 + [x^6_1] + k_{11}3 + k_{2132} = 0
y^5_2 + y^5_8 + y^5_15 + x^6_2 + k_1_15 + k_2_15_2 = 0
v^5 2 + x^6 6 + k1 15 + k2 15 2 = 0
y^5_5 + y^5_8 + x^6_10 + k_110 + k_2102 = 0
y^5 7 + y^5 10 + x^6 8 + k1 14 + k2 14 2 = 0
y^6 0 + x^7 4 + k1 3 + k2 3 3 = 0
y^6_0 + y^6_10 + x^7_12 + k_1^3 + k_2^3_3 = 0
[y^6_1] + y^6_11 + x^7_13 + k_15 + k_25_3 = 0
y^6_2 + y^6_8 + x^7_14 + k_1^7 + k_2^3 = 0
v^6 3 + v^6 9 + v^6 12 + x^7 3 + k1 4 + k2 4 3 = 0
y^6_3 + x^7_7 + k_1_4 + k_2_4_3 = 0
y^6 4 + y^6 11 + x^7 9 + k1 1 + k2 1 3 = 0
y^6_6 + y^6_9 + x^7_11 + k_10 + k_203 = 0
[y^7_0] + y^7_10 + y^7_13 + x^8_0 + k_{113} + k_{2133} = 0
[y^7_0] + x^8_4 + k_1_13 + k_2_13_3 = 0
y^7_1 + y^7_1 + y^7_1 + y^7_1 + x^8_1 + k_{114} + k_{214} = 0
y^7 1 + y^7 11 + x^8 13 + k1 14 + k2 14 3 = 0
y^7_3 + y^7_9 + y^7_{12} + x^8_3 + k_{110} + k_{2103} = 0
y^7_3 + x^8_7 + k_1_10 + k_2_10_3 = 0
y^7_3 + y^7_9 + x^8_{15} + k_{110} + k_{2103} = 0
y^7_4 + y^7_11 + x^8_9 + k_{115} + k_{215}3 = 0
y^7 6 + y^7 9 + x^8 11 + k1 9 + k2 9 3 = 0
y^7 7 + y^7 10 + x^8 8 + k1 12 + k2 12 3 = 0
y^8_0 + y^8_10 + y^8_13 + x^9_0 + k_15 + k_25_4 = 0
y^8_2 + y^8_8 + y^8_15 + x^9_2 + k_1^3 + k_2^4_0
y^8_2 + x^9_6 + k_1_3 + k_2_3_4 = 0
y^8_3 + y^8_9 + x^9_15 + k_1^2 + k_2^4 = 0
y^8 4 + y^8 11 + x^9 9 + k1 7 + k2 7 4 = 0
y^8_7 + y^8_10 + x^9_8 + k_14 + k_244 = 0
y^9_0 + x^1_0_4 + k_1_1_4 + k_2_1_4_4 = 0
y^9_2 + y^9_8 + y^9_15 + [x^10_2] + k_{11}3 + k_{21}4 = 0
y^9_6 + y^9_9 + x^10_{11} + k_{115} + k_{2154} = 0
[y^10_2] + x^11_6 + k_15 + k_25_5 = 0
y^10_4 + y^10_11 + x^11_9 + k_13 + k_23_5 = 0
y^11_6 + y^11_9 + x^12_11 + k_11 + k_21_5 = 0
y^14_1 + x^15_5 + k_10 + k_20_7 = 0
y^14_2 + y^14_8 + y^14_15 + x^15_2 + k_14 + k_24_7 = 0
y^14 6 + y^14 9 + x^15 11 + k1 5 + k2 5 7 = 0
```

- $S(x^0_1) + y^0_1 = 0$
- $S(x^0_5) + y^0_5 = 0$
- $S(x^0_9) + y^0_9 = 0$
- $S(x^1_6) + y^1_6 = 0$
- $S(x^1_7) + y^1_7 = 0$
- $S(x^1_9) + y^1_9 = 0$
- $S(x^1_10) + y^1_10 = 0$
- $S(x^1_15) + y^1_15 = 0$
- $S(x^2_2) + y^2_2 = 0$
- $S(x^2_6) + y^2_6 = 0$
- $S(x^2_8) + y^2_8 = 0$
- $S(x^2_11) + y^2_11 = 0$
- $S(x^2_14) + y^2_14= 0$
- $S(x^3_1) + y^3_1 = 0$
- $S(x^3_5) + y^3_5 = 0$
- $S(x^3_7) + y^3_7 = 0$
- $S(x^3_11) + y^3_11 = 0$
- $S(x^3_14) + y^3_14 = 0$
- $S(x^3_15) + y^3_15 = 0$
- $S(x^4_1) + y^4_1 = 0$
- $S(x^4_2) + y^4_2 = 0$
- $S(x^4_4) + y^4_4 = 0$
- $S([x^4 6]) + [y^4 6] = 0$
- $S(x^4_8) + y^4_8 = 0$
- $S([x^4_10]) + [y^4_10] = 0$
- $S(x^4_12) + y^4_12 = 0$
- $S(x^5_3) + y^5_3 = 0$
- $S([x^5_4]) + [y^5_4] = 0$
- $S(x^5_7) + y^5_7 = 0$
- $S(x^5_9) + y^5_9 = 0$
- $S([x^5_11]) + [y^5_11] = 0$
- $S(x^5_12) + y^5_12 = 0$
- $S(x^5_13) + y^5_13 = 0$
- $S(x^6_0) + y^6_0 = 0$
- $S(x^6_3) + y^6_3 = 0$
- $S(x^6_4) + y^6_4 = 0$
- $S(x^6_7) + y^6_7 = 0$
- $S(x^6_8) + y^6_8 = 0$
- $S(x^6_9) + y^6_9 = 0$
- $S([x^6_13]) + [y^6_13] = 0$
- $S(x^6_15) + y^6_15 = 0$
- $S([x^7_0]) + [y^7_0] = 0$
- $S(x^7_2) + y^7_2 = 0$
- $S(x^{7}_6) + y^{7}_6 = 0$

```
S(x^7_8) + y^7_8 = 0
 S(x^7 9) + y^7_9 = 0
 S(x^7_15) + y^7_15 = 0
 S(x^8_2) + y^8_2 = 0
 S(x^8_4) + y^8_4 = 0
 S(x^8_11) + y^8_11 = 0
 S(x^9 6) + y^9 6 = 0
 S(x^9_9) + y^9_9 = 0
the 3 Th Minimal constraint set is:
y^0_1 + x^1_5 + k_11 + k_210 = 0
y^0 1 + y^0 11 + x^1 13 + k1 1 + k2 1 0 = 0
y^0_4 + y^0_11 + x^1_9 + k_1_4 + k_2_4_0 = 0
y^1_0 + y^1_1 + y^1_1 + y^1_1 + x^2_0 + k_1_9 + k_2_9_0 = 0
y^1_0 + y^1_1 + x^2_1 + k_1_9 + k_2_9_0 = 0
y^1_2 + x^2_6 + k_1_8 + k_2_8_0 = 0
v^1 2 + v^1 8 + x^2 14 + k1 8 + k2 8 0 = 0
y^1_3 + y^1_9 + y^1_12 + [x^2_3] + k_1_13 + k_2_13_0 = 0
y^1 3 + y^1 9 + [x^2 15] + k1 13 + k2 13 0 = 0
y^1_5 + y^1_8 + x^2_{10} + k_{114} + k_{2140} = 0
y^2_0 + y^2_10 + x^3_12 + k_11 + k_21_1 = 0
 [y^2_1] + y^2_1 + y^2_1 + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
 [y^2_1] + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
[y^2 3] + y^2 9 + y^2 12 + x^3 3 + k1 5 + k2 5 1 = 0
y^2_6 + y^2_9 + x^3_{11} + k_{14} + k_{24} = 0
y^3_0 + y^3_10 + y^3_13 + x^4_0 + k_{115} + k_{215} = 0
y^3_0 + y^3_1 + x^4_1 + k_{115} + k_{215} = 0
y^3_1 + x^4_5 + k_{111} + k_{2111} = 0
y^3 1 + y^3 11 + x^4 13 + k1 11 + k2 11 1 = 0
y^3_3 + y^3_9 + y^3_{12} + x^4_3 + k_{114} + k_{214} = 0
y^3_3 + x^4_7 + k_1_14 + k_2_14_1 = 0
y^3_3 + y^3_9 + x^4_{15} + k_{114} + k_{2141} = 0
y^4_0 + [y^4_10] + y^4_13 + x^5_0 + k_17 + k_27_2 = 0
y^4_2 + y^4_8 + y^4_15 + x^5_2 + k_11 + k_21_2 = 0
y^4_2 + x^5_6 + k_1_1 + k_2_1_2 = 0
y^4_3 + y^4_9 + y^4_12 + x^5_3 + k_16 + k_26_2 = 0
y^4_3 + x^5_7 + k_1_6 + k_2_6_2 = 0
y^4_3 + y^4_9 + x^5_15 + k_1_6 + k_2_6_2 = 0
y^4_5 + y^4_8 + x^5_10 + k_14 + k_24_2 = 0
y^4_7 + [y^4_10] + x^5_8 + k_1^5 + k_2^5_2 = 0
y^5 0 + x^6 4 + k1 11 + k2 11 2 = 0
y^5_2 + y^5_8 + y^5_15 + x^6_2 + k_1_15 + k_2_15_2 = 0
y^5_3 + y^5_9 + x^6_{15} + k_{112} + k_{2122} = 0
y^5_6 + y^5_9 + x^6_{11} + k_{18} + k_{28_2} = 0
y^5 7 + y^5 10 + x^6 8 + k1 14 + k2 14 2 = 0
```

```
y^6_2 + y^6_8 + y^6_15 + x^7_2 + k_1^7 + k_2^7_3 = 0
y^6 4 + y^6 11 + x^7 9 + k1 1 + k2 1 3 = 0
y^7_6 + y^7_9 + x^8_11 + k_19 + k_29_3 = 0
y^14_1 + [y^14_1] + x^15_13 + k_10 + k_207 = 0
y^14_5 + y^14_8 + x^15_10 + k_13 + k_23_7 = 0
 S(x^0_0) + y^0_0 = 0
 S(x^0 3) + y^0 3 = 0
 S(x^0_6) + y^0_6 = 0
 S(x^0_10) + y^0_10 = 0
 S(x^0_12) + y^0_12 = 0
 S(x^0 14) + y^0 14= 0
 S(x^1_3) + y^1_3 = 0
 S(x^1_1) + y^1_1 = 0
 S(x^1_12) + y^1_12 = 0
 S([x^2_3]) + [y^2_3] = 0
 S(x^2_5) + y^2_5 = 0
 S([x^2_1]) + [y^2_1] = 0
 S(x^2 12) + y^2 12 = 0
 S(x^2_13) + y^2_13 = 0
 S([x^2_15]) + [y^2_15] = 0
 S(x^3_0) + y^3_0 = 0
 S([x^3_2]) + [y^3_2] = 0
 S(x^3 3) + y^3 3 = 0
 S(x^3_6) + y^3_6 = 0
 S(x^3_1) + y^3_1 = 0
 S([x^3_8]) + [y^3_8] = 0
 S(x^3_10) + y^3_10 = 0
 S(x^3_15) + y^3_15 = 0
 S(x^4_2) + y^4_2 = 0
 S(x^4_4) + y^4_4 = 0
 S(x^4_8) + y^4_8 = 0
 S(x^4_11) + y^4_11 = 0
 S(x^4_15) + y^4_15 = 0
 S(x^5 9) + y^5 9 = 0
the 4 Th Minimal constraint set is:
y^0_1 + x^1_5 + k_1_1 + k_2_1_0 = 0
y^0_1 + y^0_1 + x^1_1 + k_1 + k_2_0 = 0
y^0_2 + x^1_6 + k_1_2 + k_2_0 = 0
y^0_2 + [y^0_8] + [x^1_14] + k_1_2 + k_2_0 = 0
y^0_4 + y^0_11 + x^1_9 + k_1_4 + k_2_4_0 = 0
y^0_5 + [y^0_8] + x^1_10 + k_1_5 + k_2_5_0 = 0
y^1_0 + y^1_1 + y^1_1 + y^1_1 + x^2_0 + k_1_9 + k_2_9_0 = 0
y^1_0 + y^1_1 + x^2_1 + k_1_9 + k_2_9_0 = 0
y^1 1 + y^1 11 + [y^1 14] + [x^2 1] + k1 15 + k2 15 0 = 0
```

```
y^1_1 + y^1_1 + x^2_1 + k_1_1 + k_2_1 = 0
y^1 2 + x^2 6 + k1 8 + k2 8 0 = 0
y^1_2 + y^1_8 + x^2_14 + k_1_8 + k_2_8_0 = 0
y^1_3 + [x^2_7] + k_1_13 + k_2_13_0 = 0
y^1_3 + y^1_9 + [x^2_{15}] + k_{113} + k_{2130} = 0
y^1_5 + y^1_8 + x^2_{10} + k_{114} + k_{2140} = 0
y^1 6 + y^1 9 + x^2 11 + k1 12 + k2 12 0 = 0
y^2_0 + y^2_10 + y^2_13 + x^3_0 + k_11 + k_211 = 0
v^2 0 + x^3 4 + k1 1 + k2 1 1 = 0
y^2_0 + y^2_10 + x^3_12 + k_11 + k_211 = 0
[y^2_1] + y^2_1 + y^2_1 + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
y^2_2 + y^2_8 + [y^2_15] + [x^3_2] + k_1_0 + k_2_1 = 0
y^2_2 + y^2_8 + x^3_14 + k_1_0 + k_2_1=0
[y^2_3] + y^2_9 + y^2_12 + x^3_3 + k_1_5 + k_2_5_1 = 0
[y^2_3] + x^3_7 + k_1_5 + k_2_5_1 = 0
v^2 4 + v^2 11 + x^3 9 + k1 2 + k2 2 1 = 0
y^2_6 + y^2_9 + x^3_{11} + k_1_4 + k_2_4_1 = 0
[y^2 7] + y^2 10 + [x^3 8] + k1 3 + k2 3 1 = 0
y^3_0 + y^3_1 + x^4_1 + k_{115} + k_{215} = 0
y^3_1 + y^3_1 + y^3_1 + y^3_1 + x^4_1 + k_{111} + k_{2111} = 0
y^3_1 + x^4_5 + k_1_1 + k_2_1_1 = 0
y^3_1 + y^3_1 + x^4_1 + k_11 + k_21_1 = 0
[y^3 2] + [x^4 6] + k1 9 + k2 9 1 = 0
[y^3_2] + [y^3_8] + x^4_14 + k_1_9 + k_2_9_1 = 0
y^3_3 + y^3_9 + y^3_{12} + x^4_3 + k_{114} + k_{2141} = 0
y^3_4 + y^3_11 + x^4_9 + k_18 + k_28_1 = 0
y^3_7 + y^3_10 + x^4_8 + k_{113} + k_{2131} = 0
y^4 0 + [y^4 10] + y^4 13 + x^5 0 + k1 7 + k2 7 2 = 0
y^4_0 + [y^4_10] + x^5_12 + k_17 + k_27_2 = 0
y^4_1 + y^4_1 + y^4_1 + x^5_1 + k_3 + k_2_2 = 0
y^4_1 + x^5_5 + k_1_3 + k_2_3_2 = 0
y^4_1 + y^4_1 + x^5_1 + k^1_3 + k^2_3_2 = 0
y^4_3 + y^4_9 + y^4_12 + x^5_3 + k_1_6 + k_2_6_2 = 0
y^4_3 + x^5_7 + k_1_6 + k_2_6_2 = 0
y^4_3 + y^4_9 + x^5_15 + k_1_6 + k_2_6_2 = 0
y^4_5 + y^4_8 + x^5_10 + k_14 + k_24_2 = 0
[y^4_6] + y^4_9 + [x^5_11] + k_1_2 + k_2_2_2 = 0
y^5_0 + y^5_10 + y^5_13 + x^6_0 + k_{111} + k_{2112} = 0
y^5_0 + x^6_4 + k_{111} + k_{2112} = 0
y^5 0 + y^5 10 + x^6 12 + k1 11 + k2 11 2 = 0
y^5_1 + [y^5_1] + [x^6_1] + k_1_1 + k_2_1_2 = 0
y^5_2 + y^5_8 + y^5_15 + x^6_2 + k_1_15 + k_2_15_2 = 0
y^5_2 + x^6_6 + k_1_15 + k_2_15_2 = 0
y^5 3 + y^5 9 + y^5 12 + x^6 3 + k1 12 + k2 12 2 = 0
```

```
y^5_3 + x^6_7 + k_{112} + k_{2122} = 0
v^5 3 + v^5 9 + x^6 15 + k1 12 + k2 12 2 = 0
y^5_5 + y^5_8 + x^6_10 + k_110 + k_2102 = 0
y^5_7 + y^5_10 + x^6_8 + k_1_14 + k_2_14_2 = 0
y^6_0 + y^6_10 + [y^6_13] + [x^7_0] + k_1_3 + k_2_3_3 = 0
y^6_0 + x^7_4 + k_1_3 + k_2_3_3 = 0
y^6 0 + y^6 10 + x^7 12 + k1 3 + k2 3 3 = 0
[y^6_1] + x^7_5 + k_1^5 + k_2^3 = 0
[v^6 1] + v^6 11 + x^7 13 + k1 5 + k2 5 3 = 0
y^6_2 + y^6_8 + y^6_15 + x^7_2 + k_1^7 + k_2^3 = 0
y^6 3 + y^6 9 + y^6 12 + x^7 3 + k1 4 + k2 4 3 = 0
y^6 4 + y^6 11 + x^7 9 + k1 1 + k2 1 3 = 0
y^6_6 + y^6_9 + x^7_11 + k_10 + k_20_3 = 0
y^6_7 + y^6_10 + x^7_8 + k_16 + k_26_3 = 0
[y^7_0] + y^7_10 + y^7_13 + x^8_0 + k_{113} + k_{213_3} = 0
[v^7 \ 0] + x^8 \ 4 + k1 \ 13 + k2 \ 13 \ 3 = 0
[y^7_0] + y^7_10 + x^8_12 + k_113 + k_213_3 = 0
y^7 3 + y^7 9 + y^7 12 + x^8 3 + k1 10 + k2 10 3 = 0
y^7_4 + y^7_11 + x^8_9 + k_{115} + k_{215} = 0
y^7_5 + y^7_8 + x^8_10 + k_18 + k_28_3 = 0
y^8_0 + y^8_10 + x^9_12 + k_15 + k_25_4 = 0
y^8_3 + y^8_9 + y^8_{12} + x^9_3 + k_{12} + k_{22}4 = 0
y^8 4 + y^8 11 + x^9 9 + k1 7 + k2 7 4 = 0
y^9_3 + y^9_9 + y^9_12 + x^10_3 + k_18 + k_28_4 = 0
y^10_3 + y^10_9 + x^11_15 + k_10 + k_20_5 = 0
y^14_1 + [y^14_1] + x^15_13 + k_10 + k_207 = 0
y^14_2 + y^14_8 + y^14_15 + x^15_2 + k_14 + k_24_7 = 0
y^14 5 + y^14 8 + x^15 10 + k1 3 + k2 3 7 = 0
y^14_6 + y^14_9 + x^15_11 + k_15 + k_2 5 7 = 0
S(x^0_0) + y^0_0 = 0
S(x^0_1) + y^0_1 = 0
S(x^0_6) + y^0_6 = 0
S([x^0_7]) + [y^0_7] = 0
S(x^0_10) + y^0_10 = 0
S(x^0_12) + y^0_12 = 0
S(x^0_13) + y^0_13 = 0
S(x^0_14) + y^0_14= 0
S(x^1_0) + y^1_0 = 0
S(x^1_3) + y^1_3 = 0
S(x^1 4) + y^1 4 = 0
S(x^1_-7) + y^1_-7 = 0
S(x^1_8) + y^1_8 = 0
S(x^1_9) + y^1_9 = 0
S(x^1 11) + y^1 11 = 0
```

$$S(x^1_12) + y^1_12 = 0$$

$$S([x^1_14]) + [y^1_14] = 0$$

$$S([x^2_1]) + [y^2_1] = 0$$

$$S([x^2_3]) + [y^2_3] = 0$$

$$S(x^2_5) + y^2_5 = 0$$

$$S(x^2_6) + y^2_6 = 0$$

$$S(x^2_8) + y^2_8 = 0$$

$$S(x^2_9) + y^2_9 = 0$$

$$S(x^2_12) + y^2_12 = 0$$

$$S(x^2_13) + y^2_13 = 0$$

$$S(x^2_14) + y^2_14= 0$$

$$S(x^3_0) + y^3_0 = 0$$

$$S(x^3_1) + y^3_1 = 0$$

$$S(x^3_3) + y^3_3 = 0$$

$$S(x^3_5) + y^3_5 = 0$$

$$S(x^3_7) + y^3_7 = 0$$

$$S(x^3_10) + y^3_10 = 0$$

$$S(x^3_11) + y^3_11 = 0$$

$$S(x^3_12) + y^3_12 = 0$$

$$S(x^3_13) + y^3_13 = 0$$

$$S(x^3_15) + y^3_15 = 0$$

$$S(x^4_0) + y^4_0 = 0$$

$$S(x^4 2) + y^4 2 = 0$$

$$S(x^4_3) + y^4_3 = 0$$

$$S(x^4_4) + y^4_4 = 0$$

$$S([x^4_6]) + [y^4_6] = 0$$

$$S(x^4_7) + y^4_7 = 0$$

$$S(x^4_8) + y^4_8 = 0$$

$$S([x^4_10]) + [y^4_10] = 0$$

$$S(x^4_12) + y^4_12 = 0$$

$$S(x^4_13) + y^4_13 = 0$$

$$S(x^4_15) + y^4_15 = 0$$

$$S(x^5_0) + y^5_0 = 0$$

$$S(x^5_3) + y^5_3 = 0$$

$$S([x^5_4]) + [y^5_4] = 0$$

$$S(x^5_5) + y^5_5 = 0$$

$$S(x^5_8) + y^5_8 = 0$$

$$S(x^5_9) + y^5_9 = 0$$

$$S([x^5_11]) + [y^5_11] = 0$$

$$S(x^5_12) + y^5_12 = 0$$

$$S(x^5_13) + y^5_13 = 0$$

$$S(x^6_0) + y^6_0 = 0$$

$$S(x^6_3) + y^6_3 = 0$$

$$S(x^6_4) + y^6_4 = 0$$

```
S(x^6_9) + y^6_9 = 0
 S(x^6_10) + y^6_10 = 0
 S(x^6_12) + y^6_12 = 0
 S(x^7_3) + y^7_3 = 0
 S(x^7_9) + y^7_9 = 0
 S(x^7_12) + y^7_12 = 0
 S(x^8 3) + y^8 3 = 0
the 5 Th Minimal constraint set is:
y^0 0 + x^1 4 + k1 0 + k2 0 0 = 0
y^0_0 + y^0_1 + x^1_1 + k_1 + k_2 = 0
y^0 1 + x^1 5 + k1 1 + k2 1 0 = 0
y^0 1 + y^0 11 + x^1 13 + k1 1 + k2 1 0 = 0
y^0_2 + x^1_6 + k_1_2 + k_2_0 = 0
y^0_2 + [y^0_8] + [x^1_14] + k_1_2 + k_2_0 = 0
y^0_4 + y^0_11 + x^1_9 + k_14 + k_24_0 = 0
v^0 5 + [v^0 8] + x^1 10 + k1 5 + k2 5 0 = 0
y^1_0 + y^1_1 + y^1_1 + y^1_1 + x^2_0 + k_1_9 + k_2_9_0 = 0
y^1 1 + y^1 11 + [y^1 14] + [x^2 1] + k1 15 + k2 15 0 = 0
y^1_1 + x^2_5 + k_1_1 + k_2_1 = 0
y^1_2 + x^2_6 + k_1_8 + k_2_8_0 = 0
y^1_2 + y^1_8 + x^2_14 + k_1_8 + k_2_8_0 = 0
y^1_3 + y^1_9 + y^1_12 + [x^2_3] + k_{113} + k_{213}0 = 0
y^1 3 + [x^2 7] + k1 13 + k2 13 0 = 0
y^1_4 + y^1_11 + x^2_9 + k_{110} + k_{2100} = 0
y^1_5 + y^1_8 + x^2_10 + k_1_14 + k_2_14_0 = 0
y^1_6 + y^1_9 + x^2_{11} + k_{112} + k_{212} = 0
y^2_0 + x^3_4 + k_1_1 + k_2_1_1 = 0
[y^2_1] + y^2_1 + y^2_1 + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
y^2_2 + y^2_8 + [y^2_15] + [x^3_2] + k_10 + k_201 = 0
y^2_2 + x^3_6 + k_1_0 + k_2_1 = 0
[y^2_3] + x^3_7 + k_1_5 + k_2_5_1 = 0
y^2_4 + y^2_11 + x^3_9 + k_1_2 + k_2_1 = 0
y^2_5 + y^2_8 + x^3_10 + k_1_6 + k_2_6_1 = 0
y^2 6 + y^2 9 + x^3 11 + k1 4 + k2 4 1 = 0
[y^2_1] + y^2_10 + [x^3_8] + k_1_3 + k_2_1=0
y^3_0 + y^3_10 + y^3_13 + x^4_0 + k_{115} + k_{215} = 0
y^3_0 + y^3_10 + x^4_12 + k_1_15 + k_2_15_1 = 0
[y^3_2] + [x^4_6] + k_1_9 + k_2_9_1 = 0
 [y^3_2] + [y^3_8] + x^4_14 + k_1_9 + k_2_9_1 = 0
y^3 4 + y^3 11 + x^4 9 + k1 8 + k2 8 1 = 0
y^3_6 + y^3_9 + x^4_11 + k_1_10 + k_2_10_1 = 0
y^3-7 + y^3-10 + x^4-8 + k_1-13 + k_2-13-1=0
y^4_0 + [x^5_4] + k_1^7 + k_2^7_2 = 0
y^4 1 + y^4 11 + y^4 14 + x^5 1 + k1 3 + k2 3 2 = 0
```

```
y^4_1 + x^5_5 + k_1^3 + k_2^3_2 = 0
v^4 2 + x^5 6 + k1 1 + k2 1 2 = 0
y^4_2 + y^4_8 + x^5_14 + k_11 + k_21_2 = 0
y^4_3 + y^4_9 + y^4_12 + x^5_3 + k_16 + k_26_2 = 0
y^4_3 + y^4_9 + x^5_15 + k_16 + k_26_2 = 0
[y^4_6] + y^4_9 + [x^5_11] + k_1_2 + k_2_2_2 = 0
y^5_1 + [y^5_11] + y^5_14 + [x^6_1] + k_{11}3 + k_{2132} = 0
y^5_1 + x^6_5 + k_{11} + k_{21} = 0
v^5 1 + [v^5 11] + [x^6 13] + k1 13 + k2 13 2 = 0
y^5_2 + y^5_8 + y^5_15 + x^6_2 + k_1_15 + k_2_15_2 = 0
y^5 2 + x^6 6 + k1 15 + k2 15 2 = 0
y^5 3 + y^5 9 + x^6 15 + k1 12 + k2 12 2 = 0
[y^5_4] + [y^5_11] + x^6_9 + k_1_9 + k_2_9_2 = 0
y^5_5 + y^5_8 + x^6_10 + k_110 + k_2102 = 0
y^5_6 + y^5_9 + x^6_{11} + k_{18} + k_{28_2} = 0
y^6_0 + y^6_10 + [y^6_13] + [x^7_0] + k_1_3 + k_2_3_3 = 0
y^6_0 + x^7_4 + k_1^3 + k_2^3_3 = 0
y^6_2 + y^6_8 + y^6_15 + x^7_2 + k_1^7 + k_2^3 = 0
y^6_5 + y^6_8 + x^7_10 + k_1^2 + k_2^3 = 0
y^6_6 + y^6_9 + x^7_11 + k_10 + k_203 = 0
[y^7_0] + y^7_10 + y^7_13 + x^8_0 + k_{113} + k_{213_3} = 0
y^7 2 + x^8 6 + k1 11 + k2 11 3 = 0
y^7_4 + y^7_11 + x^8_9 + k_{115} + k_{215}3 = 0
y^8_0 + x^9_4 + k_{15} + k_{254} = 0
y^8_6 + y^8_9 + x^9_11 + k_11 + k_21_4 = 0
y^9 4 + y^9 11 + x^10 9 + k1 11 + k2 11 4 = 0
y^14 1 + x^15 5 + k1 0 + k2 0 7 = 0
y^14_1 + [y^14_11] + x^15_13 + k_10 + k_207 = 0
y^14_2 + y^14_8 + y^14_15 + x^15_2 + k_14 + k_24_7 = 0
y^14_5 + y^14_8 + x^15_10 + k_13 + k_23_7 = 0
y^14_6 + y^14_9 + x^15_11 + k_{15} + k_{25}7 = 0
S(x^0_0) + y^0_0 = 0
S(x^0_1) + y^0_1 = 0
S(x^0_3) + y^0_3 = 0
S(x^0_5) + y^0_5 = 0
S(x^0_6) + y^0_6 = 0
S([x^0_7]) + [y^0_7] = 0
S(x^0_9) + y^0_9 = 0
S(x^0 10) + y^0 10 = 0
S(x^0_14) + y^0_14= 0
S(x^1_4) + y^1_4 = 0
S(x^1_6) + y^1_6 = 0
S(x^1 7) + y^1 7 = 0
```

```
S(x^1_8) + y^1_8 = 0
```

$$S(x^1_9) + y^1_9 = 0$$

$$S(x^1_10) + y^1_10 = 0$$

$$S(x^1_1) + y^1_1 = 0$$

$$S(x^2_6) + y^2_6 = 0$$

$$S(x^2_8) + y^2_8 = 0$$

$$S(x^2_9) + y^2_9 = 0$$

$$S(x^2_11) + y^2_11 = 0$$

$$S(x^2_12) + y^2_12 = 0$$

$$S(x^2_14) + y^2_14= 0$$

$$S(x^3 1) + y^3 1 = 0$$

$$S(x^3_3) + y^3_3 = 0$$

$$S(x^3_4) + y^3_4 = 0$$

$$S(x^3_5) + y^3_5 = 0$$

$$S(x^3_6) + y^3_6 = 0$$

$$S(x^3_11) + y^3_11 = 0$$

$$S(x^3_14) + y^3_14= 0$$

$$S(x^3_15) + y^3_15 = 0$$

$$S(x^4_1) + y^4_1 = 0$$

$$S(x^4_2) + y^4_2 = 0$$

$$S(x^4_5) + y^4_5 = 0$$

$$S([x^4_6]) + [y^4_6] = 0$$

$$S(x^4 9) + y^4 9 = 0$$

$$S([x^4_10]) + [y^4_10] = 0$$

$$S(x^4_11) + y^4_11 = 0$$

$$S(x^4_13) + y^4_13 = 0$$

$$S(x^4_15) + y^4_15 = 0$$

$$S(x^5_0) + y^5_0 = 0$$

$$S([x^5_4]) + [y^5_4] = 0$$

$$S(x^5_10) + y^5_10 = 0$$

$$S([x^5_11]) + [y^5_11] = 0$$

$$S(x^5_13) + y^5_13 = 0$$

$$S(x^6_0) + y^6_0 = 0$$

$$S(x^6_6) + y^6_6 = 0$$

$$S(x^6_9) + y^6_9 = 0$$

$$S(x^7_4) + y^7_4 = 0$$

$$S(x^7_11) + y^7_11 = 0$$

## the 6 Th Minimal constraint set is:

$$y^0_0 + x^1_4 + k_1 + k_2 = 0$$

$$y^0_0 + y^0_1 + x^1_1 + k_1 + k_2 = 0$$

$$y^0_1 + x^1_5 + k_1_1 + k_2_1_0 = 0$$

$$y^0_1 + y^0_1 + x^1_1 + k_1 + k_2_0 = 0$$

$$y^0_4 + y^0_11 + x^1_9 + k_1_4 + k_2_4_0 = 0$$

$$y^1 0 + y^1 10 + y^1 13 + x^2 0 + k1 9 + k2 9 0 = 0$$

```
y^1_0 + y^1_1 + x^2_1 + k_1_9 + k_2_9_0 = 0
v^1 1 + x^2 5 + k1 15 + k2 15 0 = 0
y^1_1 + y^1_1 + x^2_1 + k_1_5 + k_2_5 = 0
y^1_2 + x^2_6 + k_1_8 + k_2_8_0 = 0
y^1_2 + y^1_8 + x^2_14 + k_1_8 + k_2_8_0 = 0
y^1_4 + y^1_11 + x^2_9 + k_{11}0 + k_{21}0_0 = 0
y^1 5 + y^1 8 + x^2 10 + k1 14 + k2 14 0 = 0
y^2_0 + y^2_10 + y^2_13 + x^3_0 + k_11 + k_211 = 0
[v^2 1] + v^2 11 + v^2 14 + v^3 1 + k1 7 + k2 7 1 = 0
[y^2_1] + y^2_1 + x^3_1 + k_1^7 + k_2^7_1 = 0
y^2 2 + x^3 6 + k1 0 + k2 0 1 = 0
y^2_2 + y^2_8 + x^3_14 + k_1_0 + k_2_1= 0
[y^2_3] + y^2_9 + y^2_12 + x^3_3 + k_1_5 + k_2_5_1 = 0
[y^2_3] + y^2_9 + x^3_{15} + k_{15} + k_{25}1 = 0
y^2_5 + y^2_8 + x^3_10 + k_1_6 + k_2_6_1 = 0
v^2 6 + v^2 9 + x^3 11 + k1 4 + k2 4 1 = 0
y^3_0 + y^3_10 + x^4_12 + k_1_15 + k_2_15_1 = 0
y^3 1 + y^3 11 + y^3 14 + x^4 1 + k1 11 + k2 11 1 = 0
[y^3_2] + [y^3_8] + y^3_15 + x^4_2 + k_19 + k_29_1 = 0
[y^3_2] + [y^3_8] + x^4_14 + k_1_9 + k_2_9_1 = 0
y^3_3 + y^3_9 + x^4_{15} + k_{114} + k_{214} = 0
y^3_6 + y^3_9 + x^4_{11} + k_{11} + k_{210} = 0
y^4 0 + [x^5 4] + k1 7 + k2 7 2 = 0
y^4_1 + y^4_1 + y^4_1 + x^5_1 + k_3 + k_2_2 = 0
y^4_2 + y^4_8 + y^4_15 + x^5_2 + k_11 + k_21_2 = 0
y^4_2 + x^5_6 + k_1_1 + k_2_1_2 = 0
y^4 2 + y^4 8 + x^5 14 + k1 1 + k2 1 2 = 0
y^4_3 + y^4_9 + y^4_12 + x^5_3 + k_1_6 + k_2_6_2 = 0
y^4_3 + y^4_9 + x^5_15 + k_1_6 + k_2_6_2 = 0
y^5_1 + [y^5_1] + y^5_1 + [x^6_1] + k_113 + k_2132 = 0
y^5_2 + y^5_8 + y^5_15 + x^6_2 + k_1_15 + k_2_15_2 = 0
y^5_2 + x^6_6 + k_1_15 + k_2_15_2 = 0
y^5_2 + y^5_8 + x^6_14 + k_1_15 + k_2_15_2 = 0
y^5_3 + y^5_9 + x^6_{15} + k_{112} + k_{2122} = 0
[y^5_4] + [y^5_11] + x^6_9 + k_1_9 + k_2_9_2 = 0
y^5_6 + y^5_9 + x^6_11 + k_18 + k_28_2 = 0
[y^6_1] + y^6_11 + y^6_14 + x^7_1 + k_15 + k_25_3 = 0
y^6_2 + y^6_8 + y^6_15 + x^7_2 + k_1^7 + k_2^3 = 0
y^6_2 + x^7_6 + k_1^7 + k_2^3 = 0
y^6_2 + y^6_8 + x^7_14 + k_1^7 + k_2^7_3 = 0
y^6_6 + y^6_9 + x^7_11 + k_10 + k_203 = 0
y^7_1 + y^7_1 + y^7_1 + y^7_1 + x^8_1 + k_114 + k_214_3 = 0
y^14_1 + x^15_5 + k_10 + k_20_7 = 0
y^14 1 + [y^14 11] + x^15 13 + k1 0 + k2 0 7 = 0
```

```
y^14_5 + y^14_8 + x^15_10 + k_13 + k_23_7 = 0
```

$$S(x^0 0) + y^0 0 = 0$$

$$S(x^0_5) + y^0_5 = 0$$

$$S(x^0_6) + y^0_6 = 0$$

$$S(x^0_9) + y^0_9 = 0$$

$$S(x^0_10) + y^0_10 = 0$$

$$S(x^0_12) + y^0_12 = 0$$

$$S(x^0_13) + y^0_13 = 0$$

$$S(x^0_14) + y^0_14= 0$$

$$S(x^1_0) + y^1_0 = 0$$

$$S(x^1_3) + y^1_3 = 0$$

$$S(x^1_6) + y^1_6 = 0$$

$$S(x^1_10) + y^1_10 = 0$$

$$S(x^1_1) + y^1_1 = 0$$

$$S([x^1_14]) + [y^1_14] = 0$$

$$S(x^1_15) + y^1_15 = 0$$

$$S([x^2_1]) + [y^2_1] = 0$$

$$S(x^2_2) + y^2_2 = 0$$

$$S(x^2_11) + y^2_11 = 0$$

$$S(x^2_12) + y^2_12 = 0$$

$$S(x^2_14) + y^2_14= 0$$

$$S([x^2_15]) + [y^2_15] = 0$$

$$S(x^3 1) + y^3 1 = 0$$

$$S([x^3_2]) + [y^3_2] = 0$$

$$S(x^3_3) + y^3_3 = 0$$

$$S(x^3_4) + y^3_4 = 0$$

$$S(x^3_6) + y^3_6 = 0$$

$$S(x^3_14) + y^3_14 = 0$$

$$S(x^3_15) + y^3_15 = 0$$

$$S(x^4_1) + y^4_1 = 0$$

$$S(x^4_2) + y^4_2 = 0$$

$$S([x^4_6]) + [y^4_6] = 0$$

$$S(x^4_9) + y^4_9 = 0$$

$$S(x^4_11) + y^4_11 = 0$$

$$S(x^4_14) + y^4_14=0$$

$$S(x^4_15) + y^4_15 = 0$$

$$S(x^5_1) + y^5_1 = 0$$

$$S([x^5_11]) + [y^5_11] = 0$$

the 7 Th Minimal constraint set is:

$$y^1_0 + x^2_4 + k_{19} + k_{290} = 0$$

the 8 Th Minimal constraint set is:

$$y^8_1 + x^9_5 + k_{16} + k_{264} = 0$$