

First simulation       $\text{Cov } X = \text{diag}(n \times X)$

→ STRONG effects

Data :  $Y = \alpha + \beta X + \varepsilon$

→  $\alpha = 3$

→  $\beta = (3, 3, \dots, 3)$

→  $X = [\underbrace{x_1, x_2, \dots, x_5}_{\text{seen}}, \underbrace{x_6, \dots, x_{10}}_{\text{hidden}}]$

→  $\varepsilon \sim N(0, 1)$

Fit Model  $\text{lm}(Y \sim x_1 + \dots + x_5)$

$n_{\text{sample}} = (5, 10, 15, \dots, 150)$

$n_{\text{sim}} = 100$

Average RMSE.

→ Tapering effects

$\beta = \exp\left(\text{seq}(\log(3), \log(0.005), \text{length} = 21)\right)$

$\beta = 3 \quad 2.17 \quad 1.58 \quad \dots \quad 0.06 \quad 0.05$

$\beta_1 \quad \beta_2 \dots \beta_5 \quad \beta_6 \quad \beta_7 \dots \beta_{10} \quad \beta_{11} \quad \beta_{12} \dots \beta_{15} \quad \beta_{16} \quad \beta_{17} \dots \beta_{20} \quad \beta_{21}$   
 $\downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow$   
 $\text{seen} \quad \text{unseen} \quad \text{seen} \quad \text{seen} \quad \text{seen} \quad \text{seen} \quad \text{seen}$

Second simulation       $\text{Cov } X = \text{matrix}(\text{rep}(0.5, 21 * 21), ncol = 21)$   
 $\text{diag}(\text{Cov } X) = 1$