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Core turbulent transport in tokamak plasmas: bridging theory and experiment with QuaLiKiz

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Abstract

Nonlinear gyrokinetic codes allow for detailed understanding of tokamak core turbulent transport. However, their computational demand precludes their use for predictive profile modeling. An alternative approach is required to bridge the gap between theoretical understanding and prediction of experiments. A quasilinear gyrokinetic model, QuaLiKiz (Bourdelle *et al* 2007 *Phys. Plasmas* 14 112501), is demonstrated to be rapid enough to ease systematic interface with experiments. The derivation and approximation of this approach are reviewed. The quasilinear approximation is proven valid over a wide range of core plasma parameters. Examples of profile prediction using QuaLiKiz coupled to the CRONOS integrated modeling code (Artaud *et al* 2010 *Nucl. Fusion* 50 043001) are presented. QuaLiKiz is being coupled to other integrated modeling platforms such as ETS and JETTO. QuaLiKiz quasilinear gyrokinetic turbulent heat, particle and angular momentum fluxes are available to all users. It allows for extensive stand-alone interpretative analysis and for first principle based integrated predictive modeling.

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Keywords: tokamak, turbulence, modeling

1. Introduction

Understanding and predicting temperature, density and rotation profiles in the confined core of tokamak plasmas requires accurate and rapid turbulent transport codes.

The continuously expanding availability of high performance computing systems facilitates the use of gyrokinetic codes, either gradient driven such as GENE [1], GKW [2], GS2 [3], and GYRO [4] or flux driven such as GYSELA [5] or GT5D [6]. Fixed gradient codes were intensively applied over the past few years for quasilinear and nonlinear investigations of experimental profiles. The role of the particle convection in determining the density profile was identified and understood

[7–9]. The impurity transport level was successfully compared to quasilinear diffusive and convective coefficients [10–13], including W turbulent transport [14–16]. Angular momentum convective transport was also explored [17–19].

Despite impressive progress in comparing quasilinear gyrokinetic and measured fluxes, the main issue—predicting temperature, density, rotation profiles in future tokamaks such as ITER—remains highly challenging. This requires the dynamic solution of the transport equations. Beyond the fluxes, this includes energy, particle, and momentum source modeling, together with a self-consistent magnetic equilibrium. This system is characterized by numerous nonlinear interactions, e.g. between temperature and current diffusion, and density and radio frequency heating. To reach a stationary state, these interactions must be modeled for a few confinement times, i.e. $\sim\!1~{\rm s}$ for JET-scale plasmas. This necessitates approximately 10 000

⁵ See the appendix of Romanelli et al 2014 Proc. of the 25th IAEA Fusion Energy Conf. (Saint Petersburg, Russia, 2014)

Collisions

Table 1. Various core turbulence modeling tools are presented from the codes dedicated to detailed theoretical investigation of fundamental

turbulence mechanisms towa		uxes estimates for systematic experimental	comparison/prediction.						
	→lowards easing intern	face with experiments →							
ux driven Gradient driven									
Gyrokinetic full-f	Gyı	Gyro-Landau fluid							
Some examples are: GT5D [6], GYSELA [5]	Some examples are: GS2 [21], GENE [1], GYRO [4], GKW [22]	Additional approximations: electrostatic, $s - \alpha$, etc: QuaLiKiz [8]	Calibrated to gyrokinetic theory TGLF [23]						
Nonlinear	Nonlinear or quasilinear Quasil								
Estimated time to simulate 20 radial points and 10 wave numbers: around 10 Mh Estimated time to simulate 20 radial Estimated time to simulate 20 radial points and 10 wave number around 5 min. 50 000 h for nonlinear runs or 500 h for quasilinear runs									
	Table 2. Comparison of Qua	LiKiz and TGLF frameworks.							
Calculated fluxes	fluxes Energy, particle and momentum fluxes for unlimited number of ions and electrons								
Dispersion relation	Gyrokinetic Finds all unstable modes Use the ballooning representation Includes trapped and passing ions and e	Fluid: 12 moments for circulating trapped Finds the top two most unstable lectrons, i.e. ITG-TEM and ETG							
Eigenfunctions	Estimated in the fluid limit: shifted Gau	nated in the fluid limit: shifted Gaussians Hermite basis functions, Gauss							

Equilibrium $s-\alpha$ Bishop eikonal with Miller flux surface shape with elongation, triangularity [40] Saturated potential: level, k Three parameters saturation rule optimized to best fit 160 Mixing length: $\gamma / < k_{\perp}^2 >$ with k_{\perp} accounting for and frequency spectra nonlinear GYRO simulations the eigenfunction k_{θ} spectrum such that k_{θ}^{-3} above the maximum and k_{θ} below Frequency spectrum: a Lorentzian which width scales as γ adjusted for |s| < 0.6Self-consistently through modified Included in spectral shift of saturated potential based on $E \times B$ eigenfunctions GYRO nonlinear results Fitted parameters One, such that, for the GA standard case, All of the parameters were determined by fitting to linear QuaLiKiz ion energy flux matches the nonlinear and non-linear theory GYRO ion energy flux Verification Against nonlinear GYRO, GKW and GENE Against 1799 linear gyrokinetic GKS runs and 160 simulations see table 3 nonlinear GYRO runs

On electrons, use the Krook operator, energy

flux calculations. A severe constraint on the transport model calculation time per call of a few minutes is set to obtain the profiles evolution over 1 s of plasma within reasonable wall-clock times (e.g. <24h) and on an very easily accessible number of computing cores (e.g. ~30). Gradient driven gyrokinetic nonlinear simulations are too costly, taking typically 5000-50 000 CPU hours per flux calculation for a single radial position. While optimized multiscale coupling schemes do exist [20], routine profile calculations and sensitivity studies are still impractical. Therefore, the quasilinear approximation provides an avenue for tractable profile calculations. Table 1 situates quasilinear codes with respect to the more complete gyrokinetic nonlinear codes.

dependent

As summarized in table 1, the quasilinear approximation alone is not sufficient to reach the required level of tractability. Indeed, the quasilinear approximation alone provides only a factor 100 speedup compared with nonlinear. Hence, further approximations are necessary. In TGLF [23, 24], the fluid instead of the gyrokinetic dispersion relation is solved. In QuaLiKiz [8], the axisymmetric gyrokinetic problem is further simplified thanks to the use of the lowest order ballooning transform. Some integrals are reduced by treating separately trapped and passing particles. Finally, in QuaLiKiz, the eigenfunctions are not solved self-consistently together with the eigenvalues, but rather are calculated in the fluid limit. See

for 1-2 basis functions then refined to 4

dependent

On electrons, use a pitch-angle scattering operator, energy

table 2 for a general overview of QuaLiKiz and TGLF respective frameworks. Previously to TGLF, other fluid codes have been developed and widely used such as the Weiland model [25] (embedded in the MMM model [26, 27]), the IFS-PPPL model [21] and GLF23 [28] now extended in TGLF. TGLF has been extensively tested and its predicted profiles of electron and ion temperature have been shown to reproduce measured profiles from the core to $\rho = 0.8$ with an averaged RMS error around 15% [29]. Hybrid scenarios [30] and ITB were also modeled [31]. QuaLiKiz has also been extensively compared to nonlinear gyrokinetic codes and to TGLF itself as summarized in table 3 later in this paper. Despite these successes, numerous issues remain to be addressed, such as: the pedestal height prediction [32], the underestimated transport level in the deep core, the transport level in the L mode edge region [33], the combined role of MHD and turbulence on the confinement, the impact of finite β in particular in hybrid scenarios [34], etc. Nonetheless, the overall success of quasilinear turbulent transport models in reproducing tokamak plasma profiles demonstrates the validity of the quasilinear approach in multiple regimes.

In QuaLiKiz, recent efforts in improving the numerical schemes have optimized the dispersion relation solver [35] and the plasma dispersion functions [36]. Thanks to these further approximations, 20 radial positions and 10 wave numbers are modeled within 5 min, meaning that, as TGLF, in an integrated framework, QuaLiKiz can model 1 s of plasma over 30 processors within 24h. QuaLiKiz is embedded in CRONOS [37], and was applied for predictive simulations of energy and particle transport for JET H-mode scenarios [38, 39]. This article is focusing on QuaLiKiz development and results.

This paper aims at presenting QuaLiKiz in a brief and nonetheless exhaustive manner. References are provided throughout to allow the interested reader accessing the complete derivation, verification and validation of the code. Quasilinear fluxes, Γ , are sums over the wave number k and the frequency ω made of two essential parts: the linear response $R_{\text{lin}}(k,\omega)$ and the saturated electrostatic potential $|\phi_{k\omega}|^2$; it can be expressed schematically as $\Gamma \propto \sum_{k,\omega} R_{\text{lin}}(k,\omega) \times |\phi_{k\omega}|^2$. Therefore this paper review the gyrokinetic linear dispersion relation leading to $R_{\text{lin}}(k,\omega)$ in section 2, the rules and the validity of the saturated potential $|\phi_{k\omega}|^2$ in section 3 and finally, in section 4, the QuaLiKiz fluxes are compared to nonlinear gyrokinetic fluxes as well as experimentally measured profiles. Perspectives for further speed up while enlarging the validity domain are discussed in section 5.

2. QuaLiKiz linear gyrokinetic dispersion relation

In QuaLiKiz, the eigenvalues are solutions of a linear gyrokinetic equation and the eigenfunctions are solutions of the fluid limit of this equation. All unstable eigenvalues are found thanks to a Nyquist like method. Both the eigenvalues and the eigenfunctions have been benchmarked with more complete δf gyrokinetic codes. In the review spirit of this short paper, the main approximations are presented and, for more exhaustive explanations, the adequate references are provided.

2.1. The approximated QuaLiKiz linearized Vlasov equation

In the core of tokamak plasmas, the measured density fluctuation level is well below 10% [41]. This validates assuming a background Maxwellian distribution function f_0 with a small perturbation δf . Thus, for each species s, $f_s = f_{0,s} + \delta f_s$ with $f_{0,s} = n_s \frac{1}{(2\pi m_s T_s)^{3/2}} \mathrm{e}^{-E/T_s}$, with T_s the temperature, n_s the density and m_s the mass of the considered species. E is the kinetic energy of a particle at the thermodynamical equilibrium. When treating a rotating plasma in the laboratory frame, E writes $E = \frac{m_s (\nu_\parallel - U_\parallel)^2}{2} + \frac{m_s v_\perp^2}{2}$, with U_\parallel the bulk parallel rotation of the plasma. v_\parallel and v_\perp are respectively the velocities parallel and perpendicular to the magnetic field B. In QuaLiKiz, the low Mach number limit is assumed.

The electrostatic limit is assumed in QuaLiKiz. This limit is valid for low β plasmas. The total electrostatic potential is written as $\phi = \phi_0 + \delta \phi$.

The Vlasov equation is linearized assuming harmonic perturbations such that $\delta f = \sum_{\vec{n}\omega} f_{\vec{n}\omega}(\vec{J}) \mathrm{e}^{\mathrm{i}(\vec{n}\dot{-}\vartheta - \omega t)}$ and $\delta \phi = \sum_{\vec{n}\omega} \phi_{\vec{n}\omega}(\vec{J}) \mathrm{e}^{\mathrm{i}(\vec{n}\dot{-}\vartheta - \omega t)}$:

$$f_{\vec{n}\omega}(\vec{J}) = -\frac{f_0(\vec{J})}{T_s} \left(1 - \frac{\omega - \vec{n} \cdot \vec{\omega}_s^* - \vec{n} \cdot \vec{\omega}_E}{\omega - \vec{n} \cdot \vec{\Omega}_J + i0^+} \right) e_s \phi_{\vec{n}\omega}(\vec{J}) \quad (1)$$

 \vec{J} and $\vec{\vartheta}$ are respectively the action and angle variables [42, 43] and \vec{n} is the associated wave vector. ω is the frequency of the perturbation δf , e_s is the charge of the species s. The small positive imaginary part $i0^+$ is needed to insure the causality property such that the fluctuations cancel out for a time t tending towards $-\infty$. $\vec{n} \cdot \vec{\Omega}_J$ includes the effective Doppler frequency shifts (which can importantly lead to a resonant denominator) due to the perpendicular ∇B and curvature drifts, as well as the parallel dynamics $k_{\parallel} v_{\parallel} \cdot \vec{n} \cdot \vec{\omega}_E = \vec{n} \cdot \frac{e_s d\phi}{T_s d\vec{J}}$ is the $E \times B$ drift and $\vec{\omega}^*$ is the diamagnetic frequency which represents the instability drive term since it expresses the departures from thermodynamical equilibrium of the quantities T_s , n_s and U_{\parallel} such that:

$$\vec{\omega}_{s}^{*} = T_{s} \frac{1}{n_{s}} \frac{\mathrm{d}n_{s}}{\mathrm{d}\vec{J}} + T_{s} \left(\mathcal{E} - \frac{3}{2} - \frac{U_{\parallel}}{v_{T_{s}}} \left(\frac{2v_{\parallel} - U_{\parallel}}{v_{T_{s}}} \right) \right) \frac{1}{T_{s}} \frac{\mathrm{d}T_{s}}{\mathrm{d}\vec{J}} + 2T_{s} \left(\frac{v_{\parallel} - U_{\parallel}}{v_{T_{s}}} \right) \frac{\mathrm{d}U_{\parallel}}{\mathrm{d}\vec{J}} \frac{1}{v_{T_{s}}}$$

$$(2)$$

with $\mathcal{E} = \frac{\frac{m_s v_\parallel^2}{2} + \frac{m_s v_\perp^2}{2}}{T_s}$ and v_{T_s} such that $T_s = \frac{1}{2} m_s v_{T_s}^2$.

In the electrostatic case, relevant wavelengths being larger than the Debye length, the dispersion relation is closed by the weak formulation of the quasineutrality condition:

$$\sum_{s} \mathcal{L}_{s}(\omega, \vec{n}) = 0 \tag{3}$$

where \mathcal{L}_s is the particle Lagrangian defined for each species s by $\mathcal{L}_s(\omega, \vec{n}) = \int d^3\vec{x} (-\rho_s(\omega, \vec{n})\phi^*(\omega, \vec{n}))$. This quasineutrality weak formulation is exact in the case of a unique eigenfunction [44].

Combining the weak variational formulation, equation (3), to the linearized Vlasov equation (1), one obtains the dispersion relation:

$$\sum_{s} \frac{e_{s}^{2} f_{0}^{s}}{T_{s}} \left[\langle \phi_{\vec{n}} \omega \phi_{\vec{n}}^{*} \omega \rangle - \langle \frac{\omega - \vec{n} \cdot \vec{\omega}^{*} - \vec{n} \cdot \vec{\omega}_{E}}{\omega - \vec{n} \cdot \vec{\Omega} + i0^{+}} \phi_{\vec{n}} \omega \phi_{\vec{n}}^{*} \omega \rangle \right] = 0$$
(4

where $\langle ... \rangle = \mathrm{d}^3 \vec{\vartheta} \, \mathrm{d}^3 \vec{J} ...$, hence equation (4) leads to 6D integrals.

Here the abiabatic part is summed to the non-adiabatic one. An alternative formulation of the dispersion relation isolates the polarization term and the gyrocenter part [45].

The 6D dispersion relation can be reduced down to 5D by toroidal axisymmetry, and then down to 4D by the gyrokinetic approximation $\omega/\omega_c \ll 1$, where ω_c is the cyclotron frequency. This introduces a Bessel function in front of the nonadiabatic term and removes the gyroangle. Then, it reduces further down to 3 through the strong ballooning approximation. This approximation takes advantage of the fact that the dynamics along the field line is faster than the dynamics across the field line leading to $k_{\parallel} \ll k_{\perp}$ [43, 46, 47]. The fluctuating electrostatic potential is hence rewritten as the product of slowly and rapidly varying functions: $e^{-in(\varphi-q(x)\theta)}\phi_{n\omega}(\theta)$, where φ is the toroidal angle, θ and extended poloidal angle and q the safety factor. By utilizing the analytical Fried and Conte energy integrals the dispersion relation is further reduced to 2D. To simplify further, the trapped and passing particles are integrated separately using the circular concentric large aspect ratio magnetic equilibrium $s - \alpha$ [48, 49]. For passing particles, since $v_{\parallel} \gg v_{\perp}$, a pitch angle averaged transit frequency as well as curvature and ∇B drift frequencies are performed. For trapped particle, the bounce frequency being larger than ω , a bounced average is performed. The trapped curvature and ∇B drift frequency is averaged over θ . This approximation leads to an underestimation of Trapped Electron Modes in QuaLiKiz at intermediate wave numbers $(k_{\theta}\rho_{s} \simeq 0.5-10)$. A Krook type collision operator is taken into account [50, 51] for trapped electrons only. Collisions on trapped ions and passing particles are neglected. QuaLiKiz dispersion relation accounts for trapped and passing ions and electrons, i.e. it covers the ITG-TEM and ETG ranges. An arbitrary number of tracers or active ions can be accounted for [35]. The detailed dispersion relation can be found in [43].

2.2. Validating the fluid eigenfunctions

In the variational approach, an error ε in estimating the eigenfunction will lead to a smaller error, ϵ^2 , on the eigenvalue, allowing for a higher tolerance in approximations for the eigenfunction determination. The eigenfunction $\phi_{n\omega}(\theta)$ is hence derived separately in the fluid limit, which corresponds to: $\omega \gg \vec{n} \cdot \vec{\Omega}$. The fluid limit dispersion relation is developed analytically, details can be found in [17, 42, 43].

The validity of QuaLiKiz fluid eigenfunctions was successfully assessed by comparing to self-consistent gyrokinetic eigenfunctions. For consistency with QuaLiKiz, all direct comparisons are realized with the $s-\alpha$ equilibrium

using $\alpha=0$ in either GKW, GYRO or GENE. Without rotation and $\mathbf{E} \times \mathbf{B}$, the QuaLiKiz Gaussian width agrees within a few % with the gyrokinetic GYRO width [50]. Nonetheless, wide oscillating eigenfunctions are reported in GENE/GKW for simultaneously low magnetic shear and wave number [52] and in large k_{θ} TEM dominated regimes [17]. The influence of u_{\parallel} and ∇u_{\parallel} on the eigenfunction shift is also successfully benchmarked against GKW in [17]. Moreover, the $\mathbf{E} \times \mathbf{B}$ shear leading to the expected asymmetric eigenfunctions is observed in QuaLiKiz [17].

2.3. Searching for the eigenvalues

QuaLiKiz is written in Fortran 90. Open source modules are used for the Fried and Conte integrals, the Bessel functions, the elliptical integrals and the adaptive 1D and 2D integration methods.

To find the eigenvalues of the QuaLiKiz dispersion relation, the Davies method is used [53]. Within a given contour in the complex plane, this method can determine the number of eigenvalues as well as an estimate of their values. Their precise value is then refined using a standard Newton's method. This numerical scheme was recently further optimized [35].

2.4. Linear benchmark of the growth rates

The first benchmark was presented in [42] and showed that the stabilizing impact of $Z_{\rm eff}$ was found in both QuaLiKiz and GS2. Following the implementation of collisions on trapped electrons in QuaLiKiz [50], their stabilizing impact on TEM was tested against GS2 [54]. More recently, QuaLiKiz growth rates were compared to GENE over a magnetic shear (s) scan [52]. In QuaLiKiz the stabilization for negative values of s is overestimated. It could be due to the pitch angle averaged transit frequency for passing particles leading to an underestimation of the slab branch. In the presence of finite rotation and/or $E \times B$ shear QuaLiKiz was extensively benchmarked against GKW [17].

In most cases the order of magnitude of the growth rate is correct within a few tens of %. Overall, QuaLiKiz tends to underestimate the growth rates due to narrower eigenfunctions in θ .

3. The quasilinear formulation and its validity

In this section, the quasilinear flux formulation is briefly presented. Then the validity of the quasilinear approximation is extensively discussed. The QuaLiKiz formulation of the saturated potential is deduced from the quasilinear validity exploration. Note that, as previously, a brief and wide overview is proposed here. The reader interested in further details is guided towards additional references.

3.1. The quasilinear flux formulation

The quasilinear approach can be used if a time scale, τ , exists such that $1/\gamma < \tau < T_0$, where T_0 is the equilibrium time scale. The quasilinear flux, e.g. for particle flux, is defined as $\Gamma_s = \langle \delta n_s \delta V_{E \times B} \rangle$, where $\langle \dots \rangle$ is a flux surface average and time

average over τ . For electrostatic turbulence using the linearized Vlasov equation (1), the particle flux can be expressed as the product of a linear plasma response with a saturated electrostatic potential as follows:

$$\Gamma_{s} = \operatorname{Re}\langle \delta n_{s} \frac{\mathrm{i} k_{\theta} \delta \phi}{B} \rangle
= \sum_{\vec{n}, \omega} n \operatorname{Im} \langle \vec{n} \cdot \frac{\mathrm{d} f_{0,s}(\vec{J})}{\mathrm{d} \vec{J}} \frac{1}{\omega - \vec{n} \cdot \vec{\Omega}_{J} + \mathrm{i} 0^{+}} e_{s}^{2} |\phi_{\vec{n}\omega}(\vec{J})|^{2} \rangle
\propto \sum_{\vec{n}, \omega} \langle R_{\text{lin}}(\omega, \vec{n}) |\phi_{\vec{n}\omega}|^{2} \rangle$$
(5)

Note that energy, and momentum transport fluxes are similarly derived [17, 43]. Here the time averaging was carried out and the frequency ω is taken as the real part of the solution of the dispersion relation equation (4). Nonlinear effects tend to broaden the frequency spectrum, hence a finite value will be used instead of 0^+ , as discussed below. Equation (5) is valid if the two following linked assumptions hold: (i) the linear properties are maintained in the saturated phase and (ii) the random-walk assumption holds. In the following, both assumptions are shown to be valid over a large range of parameters. Nonetheless, the amplitude and spectral shape of the saturated potential in equation (5) is not set by linear physics. This needs to be tuned by nonlinear simulations, turbulence measurements, and physical intuition. This is a key attribute of all quasilinear transport models.

3.2. Testing the quasilinear approximation validity and building the saturated potential

3.2.1. The Kubo number. Historically, the standard quasilinear theory was elaborated for test particles [55]. A condition of validity for this quasilinear framework is that the particles should not be trapped in the field. This means that decorrelation time of the potential should be shorter than the eddy turn-over time. The ratio of these two times is known as the Kubo number [55, 56]. Using gyrokinetic nonlinear codes, these times were derived and compared to each other for ETG turbulence [57] and for ITG-TEM turbulence [52, 58]. For all cases, no field trapping is reported, hence a Kubo number below 1. Therefore, it is demonstrated that well developed turbulence for typical tokamak plasma parameters is such that random walk processes do take place and can be modeled by the quasilinear theory. This is an important feature of tokamak plasma turbulence. It is coherent with results reported in the introduction regarding the overall success of quasilinear models in reproducing temperature profiles within around 15% averaged RMS error [29].

3.2.2. The frequency spectrum. As mentioned in equation (5), a finite positive imaginary part at the denominator guarantees causality. In the case of $0^+ \to 0$, the term $\operatorname{Im}\left(\frac{1}{\omega - \vec{n} \cdot \vec{\Omega}_J + \mathrm{i}0^+}\right)$ tends towards a Dirac function $-\pi\delta(\omega - \vec{n} \cdot \vec{\Omega}_J)$. To avoid these singularities and obtain continuous frequency spectra, a finite positive imaginary part is required. This is often referred as the renormalized quasilinear theory, also called the resonance

broadening theory [59]. Indeed, if a finite imaginary part ν_{QL} is assumed instead of 0^+ , one obtains:

$$\operatorname{Im} \frac{1}{\omega - \vec{n} \cdot \vec{\Omega}_J + i\nu_{\text{QL}}} = \frac{\nu_{\text{QL}}}{(\omega - \vec{n} \cdot \vec{\Omega}_J)^2 + \nu_{\text{QL}}^2}$$
(6)

which is a Lorentzian of width ν_{QL} . Two questions have now to be answered: is the Lorentzian an appropriate shape, and what is the value of its width, ν_{QL} .

In tokamak plasmas, the frequency spectrum is measured by Doppler reflectometry and its shape can be compared to Lorentzian as well as Gaussian fits. The same procedure can carried out for a GYRO nonlinear frequency spectrum [60]. The density fluctuations are computed at the outboard midplane, according to the disgnostic line of sightNeither of the two shapes are correct, as illustrated by figure 1. The turbulence cannot be approximated by either a purely diffusive (Lorentzian) or convective (Gaussian) model. Nevertheless, both fits capture the majority of the spectrum (note that the figure is in a semi-log scale), and although not exact, a Lorentzian fit, as chosen in QuaLiKiz is acceptable.

The width ν_{QL} can be estimated from a crude approximation assuming that for each mode, the linear growth rate competes with the nonlinear damping. Within this picture, the nonlinear decorrelation takes place at the same rate that the free energy is replenished [62], leading to:

$$\nu_{\rm OL} = \gamma \tag{7}$$

This hypothesis was tested in nonlinear simulations [52, 60]. Figure 2 shows that for $k_y \simeq k_\theta \rho_s < 0.2$, the linear growth rate of the most unstable mode represents rather well the nonlinear width. Since most of the transport occurs at low k_θ , the QuaLiKiz choice if a Lorentzian of width γ is a reasonable assumption for most cases. Indeed, on the semilog plots of figure 1 more than 80% of the spectrum is captured by either a Lorentzian or a Gaussian shape. However, an increased frequency broadening at low magnetic shear was reported as being likely the result of non-linear decorrelation mechanisms, such as zonal flows [52]. This was dealt by including an additional shear dependent normalization factor to QuaLiKiz fluxes, as discussed in the following section, see equation (9).

The frequency around which the nonlinear spectrum is centered was also compared to the linear eigenmode frequency ω . As illustrated by figure 3, a very good agreement is observed at scales dominating the transport: $k_{\theta}\rho_{s} \leq 0.4$ [60].

Nonetheless, recently quasi-coherent modes were observed in reflectometry spectra [63] and successfully identified as a TEM signature in GENE nonlinear simulation [64]. Such modified frequency spectra should be accounted for in a revisited renormalized quasilinear fluxes.

3.2.3. Testing the validity of the linear response. By comparing nonlinear and linear fluxes in different ways, the validity of the linear Vlasov equation for $R_{\rm lin}$ in $\Gamma_s \propto \sum_{k,\omega} R_{\rm lin}(_k,\omega) \times |\phi_{k,\omega}|^2$ can be investigated. The two approaches are 1/ comparing the nonlinear and quasilinear phases between the transported quantities and the fluctuating potential; 2/ comparing the fluxes either quasilinear or nonlinear divided by the same saturated potential, typically the nonlinear saturated potential. Both are reviewed here.

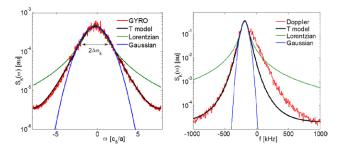


Figure 1. At $\rho = 0.7$, TS39596, experimental parameters given in [61]. Density fluctuation spectra at $k_\theta \rho_s = 0.82$ in red, compared to a Lorentzian fit in green, a Gaussian fit in blue and a model test T function [55] in black. Left hand side: frequency spectrum from GYRO nonlinear simulation. Right hand side: experimental Doppler reflectometry spectrum. From [60].

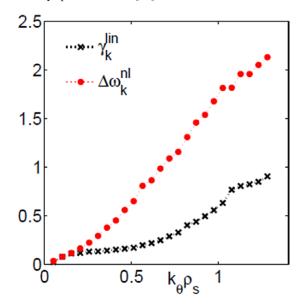


Figure 2. k_{θ} spectrum of the linear growth rates and of the nonlinear frequency widths. The results refer to nonlinear and linear (most unstable mode) simulations using GYRO on TS39596 at r/a = 0.7 [61].

A phase between a transported quantity and the fluctuating potential, for example between δn_s and $\delta \phi$ for particles, different from 0 or π is responsible for a finite level of transport. The nonlinear phases can be extracted from nonlinear simulations [58, 65]. The linear phase corresponds to the phase of the complex expression of $R_{\rm lin}(\omega,k)$. A good agreement has been reported for $k_\theta \rho_s \leqslant 0.4$ in the case of pure TEM turbulence [65] and for coupled ITG–TEM turbulence [58, 66]. It demonstrates that for low k_θ the linear response captures properly the phase between transported quantities and fluctuating potential.

In a nonlinear simulation, over a significant time window of the saturated phase, for each wave number k, the flux surface average nonlinear flux $\Gamma_k^{\rm NL}$ normalized to the saturated potential $|\delta\phi_k|_{\rm NL}^2$ on a flux surface can be defined as a nonlinear transport weight $w_k^{\rm NL}$ such that:

$$w_k^{\rm NL} = \frac{\Gamma_k^{\rm NL}}{\left|\delta\phi_k\right|_{\rm NL}^2} \tag{8}$$

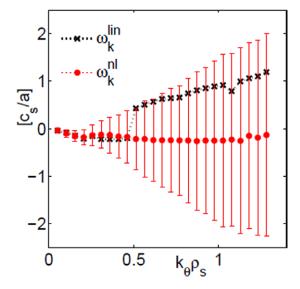


Figure 3. k_{θ} spectrum of the frequencies of the linear most unstable mode and of the nonlinear frequencies (the bars indicate the statistical variance from the mean value) [60]. The results refer to nonlinear and linear (most unstable mode) simulations using GYRO on TS39596 at r/a = 0.7 [61].

 $w_k^{\rm NL}$ amplitude can be compared to the quasilinear weight, w_k^{QL} , which is proportional the linearized Vlasov equation, $R_{\rm lin}$, as expressed in equation (5). The weight amplitudes are compared using the nonlinear saturated potential for both the nonlinear and quasilinear weights such that: $w_k^{\text{QL}} = \frac{\Gamma_k^{\text{QL}}}{|\delta\phi_k|_{\text{NL}}^2}$ [66]. It is found that the ratio $\frac{w_k^{\text{QL}}}{w_k^{\text{NL}}}$ is around 1.4 in various cases: the ITG dominated GA standard case as well as two TEM dominated regimes with GYRO [66], with adiabatic electrons for a Tore Supra L mode case at r/a = 0.4 using both GYSELA and GYRO [58]. This value is independent of $k_{\theta}\rho_{s}$ in the low k range dominating the transport. This comparison allows to further validates the linear response R_{lin} . Nonetheless, as s is reduced from 1 down to 0.1, the transport weight overage is increased from 1.4 up to larger values, even at low k_{θ} [52]. Another departure from 1.4 is observed in the case of strong inward particle fluxes with GYRO [66] and GKW [39] where the inward particle flux is stronger nonlinearly than quasilinearly. The origin of this 1.4 factor could be linked to nonlinear transfer of energy through zonal flows or through transfer towards stable eigenmodes [67]. To strengthen these hypotheses, a more theoretically robust renormalized quasilinear theory is required as the behavior at low s and strong inward particle fluxes reported above further illustrates. In the absence of more rigorous theory, an ad-hoc additional s dependent normalization factor was included on top of the 1.4 factor for |s| < 0.6, in the form of:

$$2.5(1-|s|)$$
 (9)

Despite the lack of understanding of the theoretical origin of the 1.4 factor adjusted for |s| < 0.6, it has allowed QuaLiKiz to robustly reproduce GENE, GYRO or GKW nonlinear fluxes over a wide range of parameters as summarized in table 3, including the vicinity of the temperature gradient threshold.

Table 3. Plasma parameters used in various comparisons of QuaLiKiz fluxes against nonlinear gyrokinetic codes (GYRO, GKW and GENE) and TGLF.

							$E \times B$						
Code	$\frac{R_0}{a}$	$\frac{r}{a}$	q	S	$\frac{T_i}{T_e}$	Z _{eff}	$\frac{c_s}{a}$	α	$\frac{\nu_{ei}}{c_s}$ in $\frac{c_s}{a}$	$\frac{R}{L_n}$	$\frac{R}{L_{Te}}$	$\frac{R}{L_{Ti}}$	Reference
GYRO, TGLF	3	0.5	2	1	1	1	0	0	0	3	$4.5 \rightarrow 18$	$=\frac{R}{L_{Te}}$	[38, 58]
GYRO, TGLF	3	0.5	2	1	1	1	0	0	0	3	9	$4.5 \rightarrow 18$	[38, 58]
GYRO, TGLF	3	0.5	2	1	$0.5 \rightarrow 2$	1	0	0	0	3	9	9	[38, 58]
GYRO	3	0.5	2	1	1	$1 \rightarrow 1.3$	0	0	0	3	9	9	[58]
GYRO, GENE, TGLF	3	0.5	2	$-1 \rightarrow 2.5$	1	1	0	0	0	3	9	9	[38, 52]
GYRO, TGLF	3	0.5	$1 \rightarrow 7$	1	1	1	0	0	0	3	9	9	[38, 52]
GYRO, TGLF	3.25	0.5	1.48	0.72	1	1	0	0	$0 \rightarrow 0.6$	2.5	6.5	8	[38, 58]
GENE	3	0.5	1.4	$-1 \rightarrow 2.5$	1.4	1	0	0	0	4	6.7	7.6	[52]
GENE	3	0.5	1.4	$-1 \rightarrow 2.5$	1.4	1	0	0	0	3.3	5.5	6.3	[52]
GENE	3	0.5	1	$-1 \rightarrow 2.5$	1.4	1	0	0	0	4	6.7	7.6	[52]
GYRO, GKW	3	0.5	2	1	1	1	$0 \rightarrow 0.5$	0	0	3	9	9	[17]
GYRO, TGLF	3	0.5	2	1	1	1	0	0	0	$0 \rightarrow 6$	9	9	[38]
GKW	3	0.5	1.2	0.58	1	1.7	0	0	0.0118	$-3 \rightarrow 3$	9	9	[39]
GYRO	2.8	0.5	1.4	0.78	1	1	0	0	0.03	2.24	$2 \rightarrow 8$	$=\frac{R}{L_{Te}}$	see figure 4

The only remaining identified disagreement between quasilinear and nonlinear fluxes occurs for the particle fluxes in cases of hollow density profiles [39]. See also the next section for further discussion of these comparisons.

3.2.4. The saturated potential level and k spectrum in QuaLiKiz. On most experiments [68–70], the density fluctuation wave-number spectrum: $S(k_{\perp}) = \left| \frac{\delta n(k_{\perp})}{n} \right|^2$ shows a decay for $k_{\perp} \rho_s \geqslant 0.2$ such that: $S(k_{\perp}) \simeq k_{\perp}^{\alpha_{\perp}}$ with $\alpha_{\perp} = -3.5 \pm 0.5$. This was also observed on a Tore Supra ohmic L mode pulse using two reflectometers which agreed well with nonlinear GYSELA and GYRO simulations confirming isotropic k spectra with a decay of $\alpha_{\perp} \simeq -3$ [61]. Moreover this decay is successfully recovered by the shell model [71]. This choice is hence retained in QuaLiKiz.

Now that the slope above the maximum potential is determined, it is necessary to set the k value of the maximum potential: k_{max} . It is chosen such that the effective diffusivity, D_{eff} , follows the mixing length rule:

$$\max \left(D_{\text{eff}} \simeq \frac{R\Gamma_s}{n_s} \right)_{k_{\text{max}}} = \frac{R}{n_s} \frac{k_{\theta}}{B} \frac{n_s e_s}{T_s} |\tilde{\phi}_{n\omega}|_{k_{\text{max}}}^2 = \max \left(\frac{\gamma}{\langle k_{\perp}^2 \rangle} \right)$$
(10)

 k_{max} corresponds to the k value at which $\frac{\gamma}{\langle k_{\perp}^2 \rangle}$ is maximum as proposed in [65].

Here $-\nabla n_s \simeq n_s/R$. By making use of the mixing length rule, a random Gaussian statistics for the saturated electrostatic potential is assumed [55]. This result is based on the picture that the nonlinear damping rate, $D_{\rm eff} \langle k_\perp^2 \rangle_{k_{\rm max}}$ balances the linear growth rate γ [72]. Hence $D_{\rm eff} \langle k_\perp^2 \rangle_{k_{\rm max}}$ is equal to the previously introduced $\nu_{\rm QL}$ and is modified in presence of zonal flows for example [73].

The choice for $\langle k_{\perp}^2 \rangle$ is based on both experimental observations and nonlinear simulation results. It should lead to a maximum $|\phi_{n\omega}|^2$ around $k_{\theta}\rho_s \simeq 0.2$ as reported by numerous nonlinear simulations [61], and as observed with Beam Emission Spectroscopy [74]. It should also depend on q as observed in nonlinear simulations [65, 75]. A pertinent choice for $\langle k_{\perp}^2 \rangle$ combining these two aspects was proposed by [7, 65, 76]. It is here extended to account for the MHD α parameter on the curvature drift as well as the magnetic shear s [8] such that:

$$\langle k_{\perp}^2 \rangle = k_{\theta}^2 [1 + (s - \alpha)^2 < \theta^2 >]$$
 (11)

with:

$$\langle \theta^2 \rangle = \frac{\int \theta^2 |\phi_{n\omega}(\theta)|^2 d\theta}{\int |\phi_{n\omega}(\theta)|^2 d\theta}$$
 (12)

The eigenfunction $|\phi_{n\omega}(\theta)|^2$ is a shifted Gaussian, accounting for finite $\mathbf{E} \times \mathbf{B}$ and rotation. Hence, symmetry breaking in $\langle k_{\perp}^2 \rangle$ is enacted through the imaginary part of the eigenfunction shift and the real part of the mode width, the latter being proportional to the growth rate found in the fluid model.

The expression for $\langle k_{\perp}^2 \rangle$, proposed in [8], was revisited in [52] to improve QuaLiKiz fluxes estimation at low magnetic shear. It reads:

$$\langle k_{\perp}^{2} \rangle = k_{\theta}^{2} + k_{r}^{2}$$

$$k_{r} = \sqrt{k_{\theta}^{2} \hat{s}^{2} \langle \theta^{2} \rangle} + \frac{0.4 \exp(-2\hat{s})}{\sqrt{q}} + 1.5(k_{\theta} - 0.2/\rho_{s})H(k_{\theta} - 0.2/\rho_{s})$$
(13)

At low magnetic shear, the $k_r^2 = k_\theta^2 \hat{s}^2 \langle \theta^2 \rangle$ resulting from magnetic field line shearing, is underestimated with respect to nonlinear k_r [52]. The factor $\frac{0.4 \exp(-2\hat{s})}{\sqrt{q}}$ was found to represent

well the non linear isotropization at low s. Finally, the term $1.5(k_{\theta} - 0.2l\rho_{s})H(k_{\theta} - 0.2l\rho_{s})^{2}$ (H is the Heaviside function) is present to correctly capture the approximate isotropy at high wave-numbers, but typically plays a negligible role in setting the maximum value of $\gamma/\langle k_{\perp}^{2} \rangle$.

To conclude, it should be stressed that the amplitude of the saturated potential peak is normalized in QuaLiKiz by a unique constant, such that the quasilinear ion energy flux for the GA-standard case reproduces the nonlinear result. This QuaLiKiz saturated potential level and k spectrum were successfully compared to GKW for three values of the $\mathbf{E} \times \mathbf{B}$ shear [17]. Despite some quantitative differences, the nonlinear flux quenching with $\mathbf{E} \times \mathbf{B}$ shear is captured qualitatively with a shifted eigenfunction calculated in the linear fluid limit. Moreover the linear k_{θ} dependence up to the maximum, the value of k_{max} and the slope in k_{θ}^{-3} above k_{max} all reproduce fairly well the nonlinearly saturated potential k spectra.

4. Comparing QuaLiKiz quasilinear fluxes

To construct QuaLiKiz fluxes, two elements are required: the linear response R_{lin} and the saturated electrostatic potential $|\phi_{k,j}|^2$. R_{lin} is the linear gyrokinetic dispersion relation developed in the framework discussed in section 2 and summarized in table 2. The saturated potential has its maximum value constrained by the mixing length rule see equation (10), and its k spectrum decreases as k^{-3} as reviewed in section 3. The Lorentzian frequency spectrum, equation (6), is obtained by replacing 0^+ in equation (5) by the linear growth rate γ . The sum over k is typically done over 20 values from $k_{\theta}\rho_{s} = 0.05$ up to 2. In QuaLiKiz, all eigenvalues contributions to the flux are summed. Finally, the saturated potential level is adjusted by equaling QuaLiKiz ion energy flux with GYRO nonlinear ion energy flux for the GA standard case. This only adjustment is done once and for all. The fact that QuaLiKiz fluxes reproduces well nonlinear fluxes for the ion energy fluxes using other sets of parameters, as well as electron energy fluxes, particle fluxes and angular momentum fluxes proves the validity of QuaLiKiz derivation as detailed further in this section. For a complete derivation of the quasilinear fluxes see [8] for particle, [17] for angular momentum and [43] for on overview.

4.1. QuaLiKiz fluxes compared to nonlinearly computed fluxes

QuaLiKiz ion and electron energy and particle fluxes without rotation nor $\mathbf{E} \times \mathbf{B}$ shear were extensively compared to nonlinear simulations as summarized in table 3. Over a wide range of normalized temperature gradients: $4.5 < R/L_{Ti} = R/L_{Te} < 13.5$ QuaLiKiz and GYRO agree within 15% [58, 60]. Showing that both the ratio between the transport channels and the parametric dependence are well captured by the quasilinear approach.

The collisionality impact on transport is a crucial test for quasilinear models. Indeed two effects are potentially at play: a collisional damping of zonal flows [77] not included in QuaLiKiz and a linear collisional TEM damping. Over an

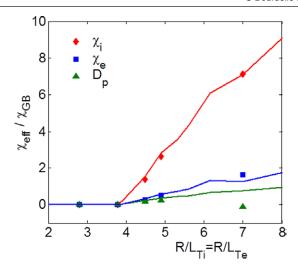


Figure 4. Ion energy, electron energy and particle effective diffusivities from GYRO (points) and QuaLiKiz (lines) for the parameters of table 4 plotted versus $R/L_T = R/L_{Te} = R/L_{Ti}$.

experimentally relevant range of collisionality [58], the linear TEM damping is found to be dominant and QuaLiKiz fluxes agree well with GYRO. In particular, the particle flux reverses direction as ν_* increases as expected [7].

A transition from TEM dominated to ITG dominated domains is realized by keeping fixed $R/L_{Te} = 9.0$ and varying only the ion gradient R/L_{Ti} from 1 to 18 [58]. The electron energy fluxes are well matched; discrepancies are instead observed on the particle fluxes for strong ITG turbulence and for the ion energy flux both in the deep TEM and deep ITG regimes. Above $R/L_{Ti} = 13$, the QuaLiKiz overestimation can be ascribed to a more pronounced effect of zonal flows in the nonlinear saturation.

When approaching the critical temperature threshold, the impact of zonal flows in pure ITG turbulence was shown to lead to an upshift of the threshold referred to as the 'Dimits upshift' [78]. It was, for the Cyclone base case and with adiabatic electrons, a shift in normalized temperature gradient units such that: $\Delta(R/L_T) \simeq 2$. In presence of kinetic electrons, it was reduced to $\Delta(R/L_T) \simeq 0.8$ [79]. To explore this region, a $R/L_T = R/L_{Te} = R/L_{Ti}$ scan down to the linear threshold is performed using QuaLiKiz and GYRO as illustrated by figure 4. The electrons are kinetic and the collisionality is finite as detailed in table 4. Close to the stability threshold the nonlinear runs are more demanding in term of resolution and their convergence should be carefully checked. Therefore, from figure 4, only an upper limit to the Dimits shift can be set such that $\Delta(R/L_T) \leq 0.7$. The reduced Dimits shift observed with kinetic electrons and finite collisionality is hence coherent with the overall success of quasilinear models in reproducing profiles within around 15% averaged RMS error [29, 38].

In [52], the impact of q and more specifically of magnetic shear s was extensively investigated. The RMS error on the particle and energy fluxes between QuaLiKiz and the nonlinear Gene and Gyro simulations are for the ion energy flux $\sigma = 0.26$, for electron energy flux $\sigma = 0.33$ and particle flux $\sigma = 1$. Where σ is the root of the ratio between the sum of the squares of the differences between the quasilinear and

Table 4. Plasma parameters of $R/L_T = R/L_{Te} = R/L_{Ti}$ scan of figure 4.

R_0/a	r/a	R/L_n	q	s	T_i/T_e	$Z_{ m eff}$	$ ho_*$	β	ν_{ei} in units of c_s/a
2.8	0.5	2.24	1.4	0.78	1.0	1.0	0.006	0	0.03

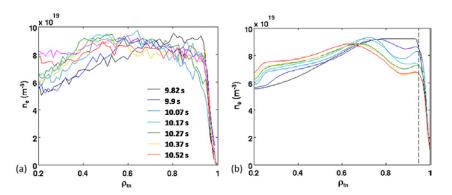


Figure 5. Evolution of the density profile (a) from HRTS in the experimental JET pulse 79676 and (b) as obtained by the QuaLiKiz simulation in CRONOS. Different colors correspond to the times of the legend of figure (a). The experimental density profile at 10.6 s, after the first sawtooth, is included in the graph (a) in purple. The dashed line of (b) corresponds to the radial location of the imposed boundary conditions. Reproduced with permission from [39], copyright 2015 EURATOM.

nonlinear fluxes divided by the sum of the squares of the nonlinear fluxes.

Quasilinear angular momentum fluxes were also validated [17]. For an $\mathbf{E} \times \mathbf{B}$ scan at zero U_{\parallel} , the angular momentum flux corresponds to the residual stress. In absolute value, the momentum flux increases at first with γ_E due the $\mathbf{E} \times \mathbf{B}$ shear asymmetrization of the eigenfunction. Then, as γ_E increases further, the momentum flux is slowly reduced due to the turbulence quenching by the $\mathbf{E} \times \mathbf{B}$ shear. This qualitative trend is found for GYRO, GKW and QuaLiKiz [17]. Quantitatively, QuaLiKiz overestimates the momentum flux found with GKW by \sim 50%. The discrepancy between QuaLiKiz and GKW is related to the overestimation of the saturated potential amplitude at lower $k_{\theta}\rho_{s}$ and intermediate values of γ_{F} in QuaLiKiz as presented in the previous section. In QuaLiKiz the $\mathbf{E} \times \mathbf{B}$ shear is estimated assuming that the $\nabla_r(\nabla_r(P_s))$ terms are negligible, hence assuming that $\nabla_r U_{\parallel}$ is the dominant contribution. This approximation is not always justified, as in [80], nonlinear GYRO simulations show that the neglected terms can provide a residual stress comparable to the profile velocity shear contribution. Depending on the respective signs, the two contributions can be additive or oppose each other [52].

The effect of ∇u_{\parallel} and u_{\parallel} on the momentum flux are analyzed with the aid of dimensionless quantities: the Prandtl number $\frac{\chi_{\parallel}}{\chi_i}$ and the pinch number $\frac{RV_{\parallel}}{\chi_{\parallel}}$. A normalized density gradient R/L_n scan is chosen to illustrate this comparison [81, 82]. In [17], the QuaLiKiz Prandtl number is found to be close to 0.7 agreeing with quasilinear [83] and nonlinear GKW simulations [82]. The QuaLiKiz pinch number $\frac{RV_{\parallel}}{\chi_{\parallel}}$ is found to vary from -2 to -5, with a strong correlation with R/L_n , as in [82]. This illustrates that the eigenfunction shift is a key element and that QuaLiKiz models correctly its impact on the momentum flux convective and diffusive parts.

4.2. quasilinear fluxes versus experiments

4.2.1. Electron particle flux. Following the overall success of quasilinear models in reproducing numerous features of the electron particle transport at a given time slice [8, 18, 84, 85], it is natural to now use such models in an integrated modeling framework to model density profile evolution. The experimental case on which the focus is made concerns high plasma current JET H-mode discharges ($I_p > 2.0-2.5$ MA, depending on plasma shape), with naturally higher plasma densities for which NBI penetration is poorer [86]. It leads to hollow density profiles persisting for timescales of several energy confinement times. When extrapolated towards ITER in D-T operation, such transient hollow density profiles lower the L to H power threshold and hence facilitates an early α central heating, necessary to maintain the H mode. To improve the accuracy of ITER extrapolation, the modeling of JET pulse by applying QuaLiKiz embedded in CRONOS was carried out [39]. Provided that the density pedestal is recovered, QuaLiKiz predicted hollow density profiles consistent with the experiment as illustrated by figure 5. The hollow profile is maintained since the diffusion—initially directed outward—is not counterbalanced by sufficient inward convection. Despite this success, more robust quasilinear models are required for hollow density profiles as mentioned earlier in this section, since in such cases the quasilinear fluxes underestimate the nonlinear inward fluxes. Also it is interesting to note that in an attempt to let evolve multiple transport channels simultaneously, a CRONOS simulation where the ion and electron energy fluxes were evolving together with the particles has also be performed. In this case, the hollow profile is filled faster in this case likely due to the fact that the temperatures are overestimated [39]. When investigating multiple transport channels at a time, the nonlinear interplay between them, with the sources and with the boundary conditions are extremely

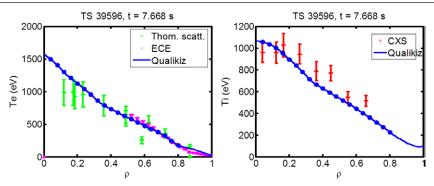


Figure 6. Left hand side: Electron temperature profile measured by ECE and Thomson Scattering and QuaLiKiz prediction. Right hand side: Charge Exchange measured ion temperature and QuaLiKiz prediction. Tore Supra pulse 39596 [61].

rich and complex. Thanks to faster first principle based tools such as TGLF and QuaLiKiz, this interplay should become a strong axis of research in the future.

4.2.2. Impurity particle transport. Impurity particle transport can be explored experimentally thanks to perturbation techniques [12, 87–89]. The impact of the impurity charge Z was studied [8, 11, 90, 91]. In Tore Supra, no dependence in Z was found on the diffusivities [88], in agreement with Qua-LiKiz. Concerning the inward convection, experimentally no Z dependence was reported whereas it was expected from the modeling.

For impurity transport dominated by TEM turbulent transport, an influence of R/L_{Te} is expected. This was studied in [12]. Within the uncertainties, QuaLiKiz reproduces the diffusion and convection of Nickel reasonably well as well as the increase of the diffusion with larger R/L_{Te} .

In ASDEX Upgrade, in the presence of central electron heating, average Z impurities had either a weak or even a positive convection. This leads to weaker core impurity accumulation. The theoretical understanding of this mechanism is thought to be due to the passing electron compressibility term, leading to an outward convection in case of dominant TEM as reported in [9, 92]. It is shown that an outward convection is obtained only if both R/L_{Ti} is low and R/L_{Te} is high. To reproduce ASDEX Upgrade's result R/L_{Te} has to be increased above its experimental value. This mechanism cannot explain results obtained in JET on Nickel transport [10]. It is important to note that such cases, deeply in the TEM regime, are accompanied by eigenfunctions extended along the field line (i.e. non-zero for $\theta = \pm \pi$, see appendix of [17]). In QuaLiKiz, the lowest order ballooning approximation, assuming null eigenfunctions at $\theta = \pm \pi$, is not adapted for such cases where complementary gyrokinetic simulations have to be carried out. It is also to note that, in Tore Supra dominantly electron heated pulses, such deep TEM regimes were not found and the experimentally measured impurity convection was never found directed outward.

4.2.3. Energy flux. For a wide range of parameter space the QuaLiKiz electrostatic assumption for ion energy flux is appropriate, including in L-modes as illustrated by figure 6 and in baseline H-modes [38] where the profiles predicted by QuaLiKiz and TGLF are shown to be similar. In the L mode

ohmic Tore Supra case, figure 6, the temperature profiles are predicted by QuaLiKiz in CRONOS from the core to a normalized radius of 0.8. In other cases, with high β and/or significant fast ion pressure, such as in the hybrid H modes, the plasma conditions are close to the Kinetic Ballooning Modes limit. Under such condition, the nonlinear electromagnetic stabilization will be important [17] and QuaLiKiz will overpredict the fluxes [38]. This can be accounted for by changing the saturated potential rather than the linear part, since it is mostly a nonlinear effect.

The L mode edge was also reported as a region where both nonlinear and quasilinear gyrokinetic models failed in reproducing systematically measured turbulent transport levels [93–95]. Resistive Ballooning Modes were proposed as potential key players [27, 96]. RBM are not accounted for in QuaLiKiz. More recently the role of the bulk rotation direction was pointed out [97]. This effect will be investigated in future work using QuaLiKiz.

Towards the magnetic axis, experimentally an electron heat diffusivity larger than the neoclassical predictions is reported whereas gyrokinetic codes are often below the linear stability threshold. For example, on figure 6, one can note that the modeled electron temperature values are above the measured ones for $r/a \le 0.2$. To reconcile the modeling with the experimental observations, nonlinear turbulence spreading [98] should be investigated. ETG might also be a candidate, since recent multiscale simulations show that high k ETG can nonlinearly be responsible for large increase of high k turbulent fluxes [99].

4.2.4. Angular momentum transport. To determine experimentally the momentum convective term, modulations of the momentum sources are necessary. Such experiments were carried out in JET H-mode pulses, where the momentum source was modulated using the Neutral Beam Injection [100]. It was demonstrated that both the amplitude and phase of the modulated toroidal velocity from the experiment are best reproduced when a momentum pinch is taken into account. In this analysis, the residual stress contribution was neglected. This JET pulse was analyzed by QuaLiKiz. The estimated Prandtl number lies within 0.8 and 1.4, close to both GKW and experimental values [100]. The pinch number calculated with QuaLiKiz ranges from -3 to -7, in good agreement with the experimental values. However a definitive conclusion would require smaller error bars. Moreover some significant

contributions to the residual stress reviewed in [80] are not taken into account in local models such as QuaLiKiz.

5. Conclusion and perspectives

The quasilinear approximation was demonstrated to be valid over a wide range of core tokamak parameters using both nonlinear gyrokinetic simulations and turbulence measurements [17, 43, 52, 58]. However, the construction of the saturated potential through nonlinear mechanisms needs to be further improved by revisiting renormalized quasilinear theory. Indeed for low magnetic shear, |s| < 0.6, ad-hoc formation had to be used. The QuaLiKiz particle fluxes for strongly inward fluxes do not reproduce well nonlinear fluxes. Recent observation of a quasi-coherent structure in measured frequency spectra linked to unstable TEM [63] is also pointing towards the need of a revisited renormalized quasilinear theory.

Moreover, now that QuaLiKiz can be used in an integrated framework, hence flux driven, its predicted profiles can be compared to nonlinear gyrokinetic flux driven codes such as GYSELA [101]. Such investigations should allow exploring further the validity domain of the quasilinear approximation. For example, it would be interesting to explore quantitatively the impact of reported avalanches [102] on the overall transport level and their parametric behavior.

Nonetheless, as demonstrated by TGLF and other quasilinear studies, over a wide range of parameters quasilinear energy, particle and momentum fluxes reproduce well nonlinear gyrokinetic fluxes while gaining a factor 106 on the computing time. In the case of QuaLiKiz, the turbulent fluxes for 20 radial positions and 10 wave numbers can be computed in less than 5 min. With such a code, 1-10 s of plasma evolution can be modeled within a 24h using a very easily accessible number of 30 CPUs. Note that such time scales are similar to TGLF [24]. QuaLiKiz imbedded in CRONOS [37] reproduces well temperature profiles of in JET baseline [38], ohmic L mode temperature in Tore Supra up to r/a = 0.8as well as slowly evolving hollow density profiles [39]. The L mode edge issue encounter on DIII-D cases [93, 95, 103] needs to be investigated with QuaLiKiz, as well as current ramp-up modeling which is challenging edge turbulent electron heat transport [104, 105]. To model high β hybrid H modes [38], QuaLiKiz which is presently electrostatic needs to be extended to included nonlinear electromagnetic stabilization [34]. Accounting for electromagnetic effects and general geometry is expected to slow down QuaLiKiz. It is presently marginally fast enough, therefore an alternative route is being explored to include richer physical effects while speeding up the calculation. This is based on using a Neural Network emulation on a large QuaLiKiz database at first, then a database including results from GKW, GENE, etc. The proof of principle of this idea was successfully demonstrated on 5D QuaLiKiz database with adiabatic electrons [106]. It is presently being extended to kinetic electrons and up to 10D.

Despite various open issues to be addressed, QuaLiKiz is an adequate quasilinear gyrokinetic turbulent transport code for integrated modeling of H mode baseline and L mode core. It is very rapid and, if used in stand alone, it can allow for extensive input scans which are essential when comparing the results to experimental fluxes. Indeed fixed gradient codes are highly sensitive to the uncertainties on its inputs such as the normalized temperature gradient for example. When used in a source driven integrated framework such as CRONOS, TGLF or QuaLiKiz model temperatures, densities and rotation profiles of few seconds of plasma. Hence now, two first principle based turbulent transport codes, bridging theory and experiments are available to all interested users. QuaLiKiz will be coupled in the European Transport Solver and JETTO by end of 2015. Documentation on code derivation details are available online [43]. For more information and to download the code, contact the two main authors of this article: clarisse. bourdelle@cea.fr or j.citrin@differ.nl.

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