A Plural Voting Design for Cardano's Delegated Representatives using Hyper-Plutocratic Deposits for Sybil Resistance

Analysis of a DReps votes as a function of Delegation, Deposit, and Wallets

by Kenric Nelson July 4, 2023

This is a draft document that has not been reviewed. It is being release to allow the Cardano community to examine the proposed design prior to the Voltaire Workshop on July 11, 2023.

CIP - 1694 proposes one coin one vote (1c1v) as the process for Delegated Representative (DRep) voting for Cardano governance. Unfortunately, 1c1v cannot support the claim that Cardano is building a decentralized governance, since power-law distributions of wealth and nonlinear increases in influence with votes result in centralized concentration of voting power. In fact, corporate governance research, which uses one share one vote (1s1v), indicates that only 10%-20% of widely held shares are necessary to control the decision-making; hence, the democratic requirement for disclosure of owners with greater than 10% of shares.

Glenn Weyl invented an alternative voting method known as Plural or Quadratic Voting. It has has been implemented in both democratic (one person one vote 1 p1v) and corporate (one share one vote 1 s1v) settings. Plural Voting offsets the nonlinear increases in voting power by weighting votes by the square-root of the resource, in Cardano's case ADA coins. The full implementation of Plural Voting involves additional procedures, but a preliminary implementation for Cardano's Voltaire governance would simply apply the square-root of the ADA delegated to a DRep.

Plural Voting requires control against splitting voting weight across multiple wallets. This is usually accomplished through identity validation; however, use of self-sovereign identity is not being considered for the Cardano Minimal Viable Governance (MVG). Therefore, there is a need to design a method of Sybil resistance that does not require identity. There is in fact research deweighting wallets that have a high degree of correlation; and measures of community contribution by wallet are possible. These methods have merit but would require lengthy analysis to properly implement.

Defined and analyzed here is a method of Sybil resistance using a DReps deposit to control against the benefit of wallet splitting. By limiting a DReps votes based on the square of their deposit, the deposit weight acts in a hyper-plutocratic manner. The DRep votes is the minimum of the Plural votes from the delegates and the hyper-plutocratic votes of their deposit. This creates a competitive situation in which delegates seek to spread their delegation across many wallets, while DReps seek to concentrate the delegation into one wallet.

Aligning these two factors toward a range of 100 votes (10⁴ADA delegates) and 10⁵votes (10¹⁰ADA delegates) requires a normalization of the deposit function. Thus votesDeposit = (10 (deposit per wallet)/(minimum Deposit))². In the examples below minDeposit = 500 ADA, like the current Catalyst program. The minimum deposit enables the DRep to have 100 votes if they have greater than 10,000 ADA delegated. Each increment of 10 ADA deposit adds another 100 votes which must be matched by an additional 10,000 ADA in delegation.

The analysis examines the effect of using multiple wallets. For modest deposits (~5000 ADA) and large delegates ($\sim 10^8$) splitting the wallet reduces the number of votes. For smaller delegates ($\sim 10^6$) there is some benefit to wallet splitting but only over a limited number of wallets after which there are diminishing votes. A solo Rep with assets of two billion who splits 10 million for deposits across ten thousand wallets and the rest into the delegate pools would achieve \sim 5 × 10⁶ rather than the one wallet plural votes of ~ 40,000 votes. However, the initial implementation of Voltaire governance, as specified in Cardano Improvement Proposal (CIP) 1694, will restrict the selection of DReps to the 10,000 with the most delegates. Thus, the wealthy solo DRep trying to exploit the system with just 200 000 delegates per wallet would have additional restrictions on their participation.

Definition of Voting Weight Function

In the defining functions, the delegate and deposit variables represent the totals across all the wallets used. minDelegate and minDeposit are the minimums for a wallet. For the examples shown, the minimums are set to 10 ADA and 500 ADA respectively. The delegatePower sets the type of voting process for the delegates; 0 is a democracy (1 wallet 1 vote), 1/2 is a Pluralism, and 1 is a plutocracy (1c1v). The default used in this analysis is Pluralism (1/2). The deposit power is powerDeposit/powerDelegate. The purpose of using the two variables is to allow powerDeposit =1 be the default, while providing the option to explore other possibilities. With powerDeposit = 1, the deposit is raised to the inverse power of the delegates. For the examples examined here this is 2; i.e. a hyper-plutocratic process.

The DRep Vote function is:

Votes = Min[DelegatedWeight, DepositWeight]

The delegate vote function is:

```
DelegateWeight =
       delegate \powerDelegate
                                    \frac{\text{delegate}}{\dots} \ge \text{minDelegate}
      \ wallets /
                                     wallets
                                    delegate < minDelegate
```

The deposit vote function is:

```
DepositWeight =
                \(\frac{10 \text{ deposit}}{\text{ wallets}}\)\)\(\frac{\text{powerDeposit}}{\text{powerDelegate}}\)
                                                                    \frac{\text{deposit}}{\text{wallets}} \ge \text{minDelegate}
                                                                                     < minDelegate
```

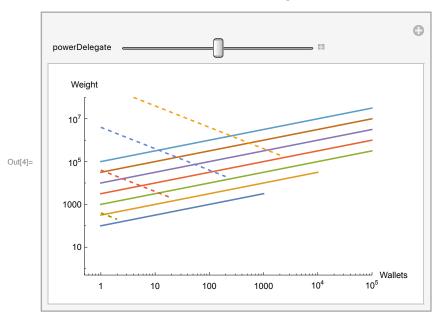
The factor 10 is a constant rather than a variable because strictly speaking its not required; however, it seems more pragmatic for the minimum deposit to enable 100 votes rather than 1 vote. This could be examined in the future and removed as long as the DRep community understands that more than the minimum will be required to enable voting.

Analysis of Delegate & Deposit Weight

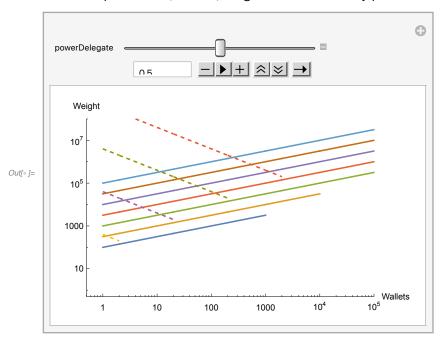
This log-log plot shows how the voting weight for the delegate and the deposit have opposite slopes as the number of wallets is increased. The intersection of a delegate and deposit line represents the maximum number of votes achievable by splitting delegate and deposit into multiple wallets.

The solid lines are the votes based on the delegate ADA. For 0 < powerDelegate < 1 these lines slope upward as the number wallets increases. The dashed lines are the votes based on the deposit ADA. For 0 < powerDelegate < 1 and powerDeposit = 1, these lines slope downward as the number of wallets increases.

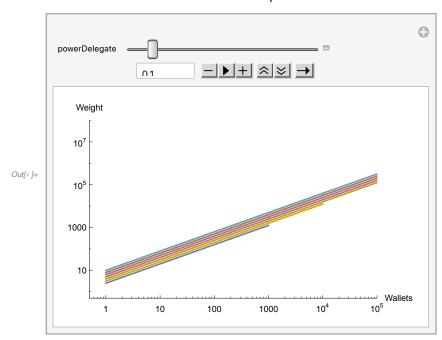
```
In[4]:= Manipulate LogLogPlot
    Evaluate[{
       Tooltip[DelegateWeight[#, 10, wallets, powerDelegate], #] & /@
         \{10^4, 10^5, 10^6, 10^7, 10^8, 10^9, 10^{10}\},
       Tooltip[DepositWeight[#, 500 (*minDeposit*), wallets, powerDelegate,
             1 (*powerDeposit*)], \#] & /@ {10, 10<sup>2</sup>, 10<sup>3</sup>, 10<sup>4</sup>, 10<sup>5</sup>, 10<sup>6</sup>}}],
    {wallets, 1, 100 000},
    AxesLabel → {"Wallets", "Weight"},
    (*PlotLegends→SwatchLegend[{10<sup>1</sup>,10<sup>2</sup>,10<sup>3</sup>,10<sup>4</sup>,10<sup>5</sup>},LegendLabel→"Deposited"],*)
    PlotRange \rightarrow \{\{5 \times 10^{-1}, 10^{5}\}, \{5 \times 10^{-1}, 10^{8}\}\},
    PlotStyle → Flatten[{Table[Line, 7], Table[Dashed, 6]}]],
   {{powerDelegate, 0.5}, 0.01, .99}]
```



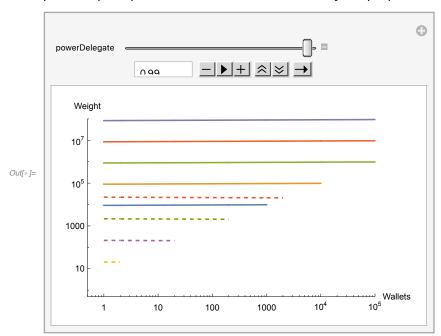
The default settings have overlap between the delegate and deposit weight, facilitating Sybil resistance in the range of 100 to 10^5 votes. The delegate lines (solid) shown range from 10^3 to 10^{10} by powers of 10. The deposit lines (dashed) range from 10³ to 10⁶ by powers of 10.



With powerDelegate = 0.1 the delegate voting is close to democratic (1w1v). The delegate line has a steeper slope and they are more closely spaced. The deposit lines are not visible in this plot but will have a close to vertical downward slope.

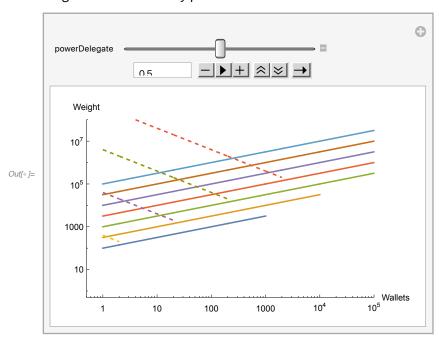


A powerDelegate = 0.99 is similar to 1c1v. In this design, the both the delegate deposit weight are plutocratic. Thus, the deposit is required to match the delegate. While this example isn't practical, the powerDeposit parameter could be used to modify the properties.



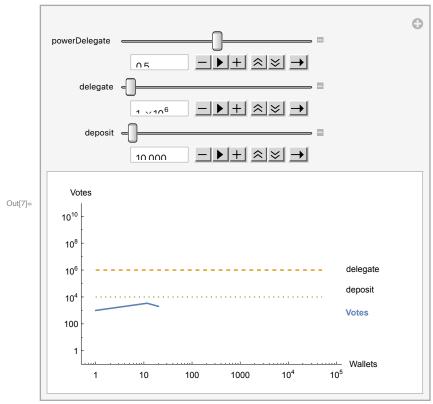
In this example, minDeposit = 10, removing the 10/minDeposit factor. Shown are deposits of $\{10^2,$ 10^3 , 10^4 , 10^5 }. In this case a modest deposit of 10,000 can be allocated over 10 wallets to increase the votes with a delegate of 1 million. Large delegate size have less of a benefit; nevertheless the 10/minDeposit factor with minDeposit = 500 reduces this effect, which is why it was added to the design.

The delegate lines (solid) shown are range from 10³ to 10¹⁰ by powers of 10. The deposit lines (dashed) range from 10^3 to 10^6 by powers of 10.

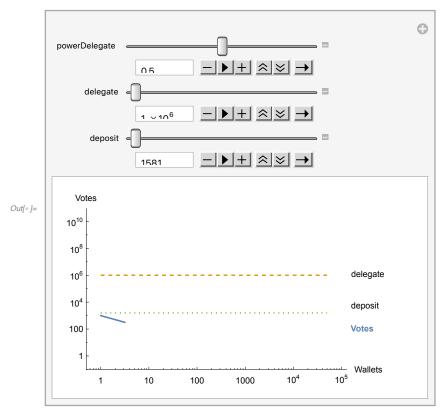


Analysis of DRep Votes using multiple wallets

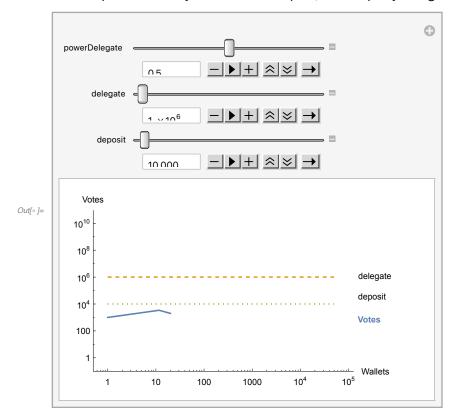
```
In[5]:= minDelegateforPlot = 10;
minDepositforPlot = 500;
Manipulate [LogLogPlot]
   {Labeled[
      Votes[delegate, deposit, minDelegateforPlot,
       minDepositforPlot, wallets, powerDelegate, 1],
      Text[Style["Votes", {ColorData[97, 1], Bold}]]],
     Labeled[delegate, "delegate"],
     Labeled[deposit, "deposit"]},
    {wallets, 1, 50000},
   AxesLabel → {"Wallets", "Votes"},
    (*PlotLegends→SwatchLegend[{10<sup>1</sup>,10<sup>2</sup>,10<sup>3</sup>,10<sup>4</sup>,10<sup>5</sup>},LegendLabel→"Deposited"],*)
   PlotRange \rightarrow \{\{5 \times 10^{-1}, 10^{5}\}, \{10^{-1}, 10^{10}\}\},\
   PlotStyle → {Line, Dashed, Dotted}],
  {{powerDelegate, 0.5}, 0.01, .99},
  \{\{delegate, 10^7\}, 10^4, 10^9\},
  \{\{\text{deposit}, 5 \times 10^3\}, \text{minDepositforPlot}, 10^6\}\}
```



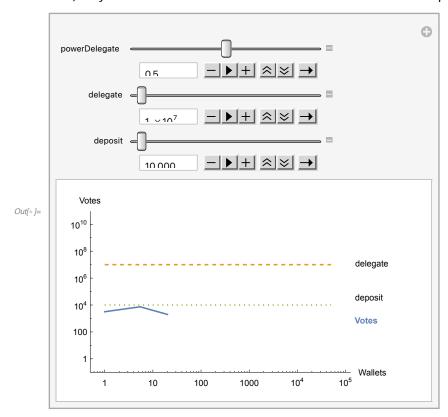
A DRep that can attract a modestly large delegation (10⁶ ADA) and uses the minimum required deposit to support this delegation (1581 ADA) has 1000 votes with one wallet. Their votes decrease to 500 if they split the deposit and delegation into two wallets. Beyond three wallets the deposit does not meet the minimum and the votes go to zero.



Even with an investment of 10,000 for the deposits, the maximum votes is limited to 10 wallets. In this case the delegates/wallet has dropped to 100,000 ADA which creates the risk that they will deselected as a DRep because they are not in the top 10,000 DReps by delegation.

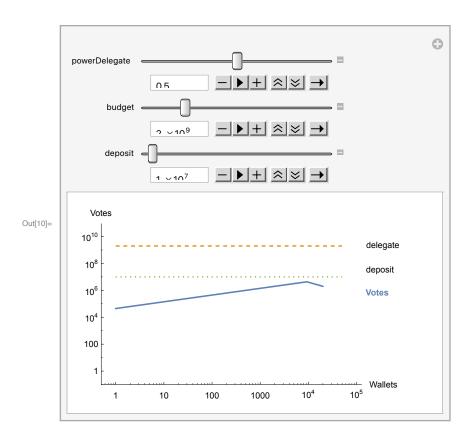


Furthermore, if this DRep investing 10,000 ADA in deposits could increase their delegate to 10 million ADA, they would have to reduce the number of wallets used to improve their votes.



Analysis of solo DRep

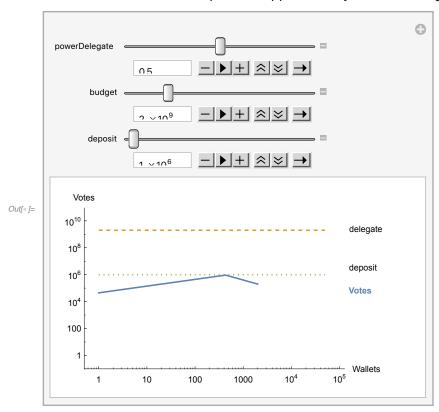
```
In[8]:= minDelegateforPlot = 10;
minDepositforPlot = 500;
Manipulate[
  delegate = budget - deposit;
  LogLogPlot[
   {Labeled[
     Votes[delegate, deposit, minDelegateforPlot,
       minDepositforPlot, wallets, powerDelegate, 1],
     Text[Style["Votes", {ColorData[97, 1], Bold}]]],
    Labeled[delegate, "delegate"],
    Labeled[deposit, "deposit"]},
   {wallets, 1, 50000},
   AxesLabel → {"Wallets", "Votes"},
   (*PlotLegends→SwatchLegend[{10¹,10²,10³,10⁴,10⁵},LegendLabel→"Deposited"],*)
   PlotRange \rightarrow \{\{5 \times 10^{-1}, 10^{5}\}, \{10^{-1}, 10^{10}\}\},\
   PlotStyle → {Line, Dashed, Dotted}],
  {{powerDelegate, 0.5}, 0.01, .99},
  \{\{\text{budget}, 10^6\}, 10^4, 10^{10}\},
  \left\{\left\{\text{deposit, 1} \times 10^{3}\right\},\, \text{minDepositforPlot, 10}^{9}\right\}
```



An important security question is whether a wealthy individual can run a large number of pools and thereby circumvent the Sybil resistance. The current supply of ADA is ~36 Billion. If there is 50% participation in DRep delegation and someone had 10% of the supply, that would be ~ 2 Billion ADA.

So let's examine an individual or institution with 2 billion ADA to place on the delegate pools and deposits across an unlimited number of DRep wallets.

If 1 million of the budget is applied to the deposits, the votes peaks at approximately 400 wallets. The one wallet votes of 10⁵ increases to approximately 10⁶. So there is only a factor of 10 increase despite the use of 400 wallets. Each pool has approximately 5 million delegate ADA.



If the investment in the deposit is increased to 10 million (and the delegate is therefore 2 billion - 10 million), the votes peak at approximately 10,000 wallets. The votes are ~5 million, a factor of ~x50 over the single wallet votes. Across 10,000 wallets the delegation per wallet has dropped to ~200,000.

If increased Sybil resistance is desired, this is easily achieved by increasing the minimum deposit. A minimum deposit of 1000 or even 5000 ADA may be desirable but it would put further restrictions on who in the community can afford the deposit.

