

Homework 4

UNI: qy2205

Name: Quan Yuan

Email: qy2205@columbia.edu

```
debt <- read.csv("debt.csv", as.is = TRUE)
dim(debt)
```

```
## [1] 1171    4
```

```
head(debt)
```

```
##      Country Year   growth   ratio
## 1 Australia 1946 -3.557951 190.41908
## 2 Australia 1947  2.459475 177.32137
## 3 Australia 1948  6.437534 148.92981
## 4 Australia 1949  6.611994 125.82870
## 5 Australia 1950  6.920201 109.80940
## 6 Australia 1951  4.272612  87.09448
```

1

```
# (a)
library(plyr)
mean.growth <- function (data){
  return(mean(data$growth))
}
# (b)
country.ave.growth <- signif(daply(debt, .(Country), mean.growth), 3)
country.ave.growth
```

```
##      Australia      Austria      Belgium      Canada      Denmark      Finland
##          3.72          4.44          3.18          3.65          2.66          3.57
##      France      Germany      Greece      Ireland      Italy      Japan
##          3.78          3.31          2.93          3.93          3.25          4.45
## Netherlands New Zealand      Norway      Portugal      Spain      Sweden
##          3.03          3.07          3.83          4.00          3.20          3.07
##          UK          US
##          2.41          3.00
```

```
country.ave.growth[c("Australia", "Netherlands")]
```

```
##      Australia Netherlands
##          3.72          3.03
```

Report: the average GDP growth rates is highest in Japan and lowest in UK. Austria, Jpan and Portugal have high average GPA growth rate (above 4). UK, Greece and Denmark have low GPA growth rate (below 3).

2

```
each.year.ave.growth <- signif(daply(debt, .(Year), mean.growth), 3)
each.year.ave.growth
```

```
##      1946      1947      1948      1949      1950      1951      1952      1953      1954      1955
```

```
## 2.620 5.410 5.560 4.740 6.320 4.920 3.400 4.090 4.880 5.140
## 1956 1957 1958 1959 1960 1961 1962 1963 1964 1965
## 4.230 3.910 2.240 5.310 5.860 4.890 4.960 4.830 6.370 4.720
## 1966 1967 1968 1969 1970 1971 1972 1973 1974 1975
## 4.310 4.040 5.270 6.250 4.610 4.070 5.630 5.970 1.990 0.830
## 1976 1977 1978 1979 1980 1981 1982 1983 1984 1985
## 4.170 2.630 3.320 4.190 1.870 0.992 0.876 2.040 4.060 3.520
## 1986 1987 1988 1989 1990 1991 1992 1993 1994 1995
## 2.890 2.450 2.920 3.190 2.570 1.330 1.590 1.020 3.860 3.630
## 1996 1997 1998 1999 2000 2001 2002 2003 2004 2005
## 3.390 4.070 3.090 3.480 4.060 2.040 1.970 1.870 3.290 2.620
## 2006 2007 2008 2009
## 3.140 3.140 0.798 -3.370
```

```
each.year.ave.growth[c("1972", "1989")]
```

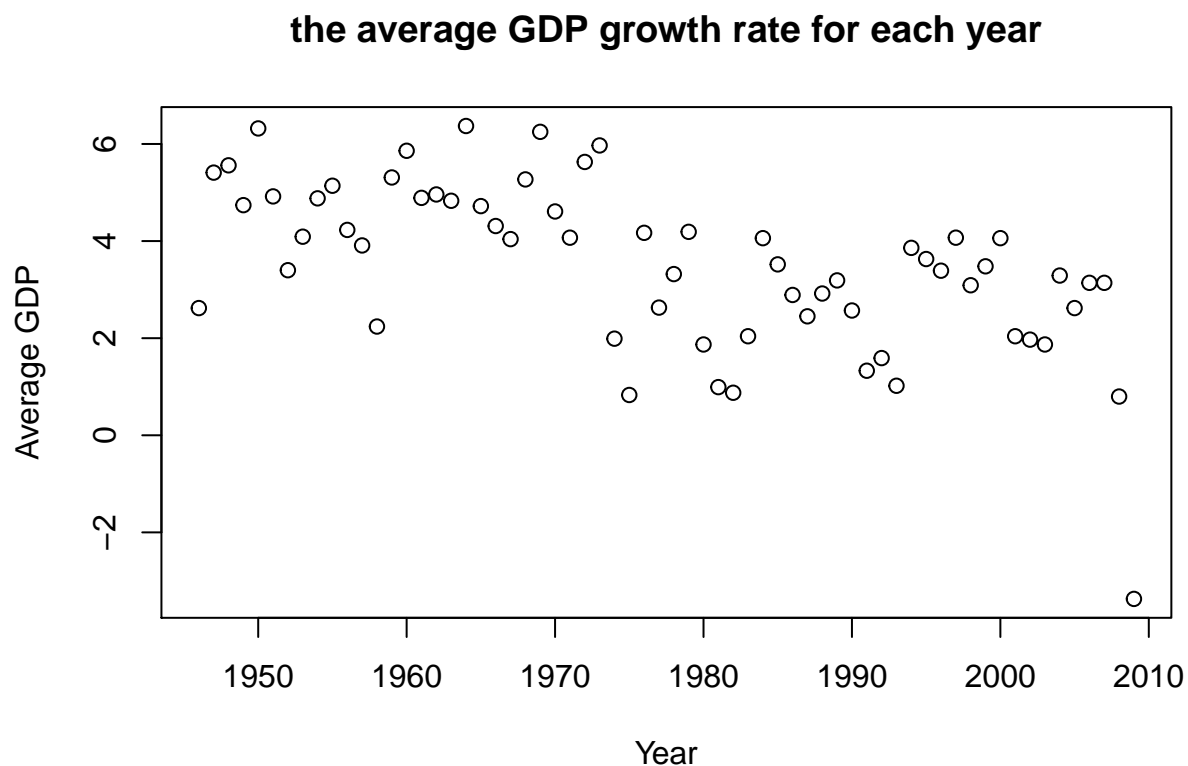
```
## 1972 1989
```

```
## 5.63 3.19
```

```
year <- as.numeric(names(each.year.ave.growth))
```

```
year.ave.gdp <- unname(each.year.ave.growth)
```

```
plot(year, year.ave.gdp, xlab = 'Year', ylab = 'Average GDP', main = 'the average GDP growth rate for each year')
```



```
### 3
```

```
# (a)
```

```
cat('the correlation coefficient between GDP growth and the debt ratio over the whole data set', signif(
```

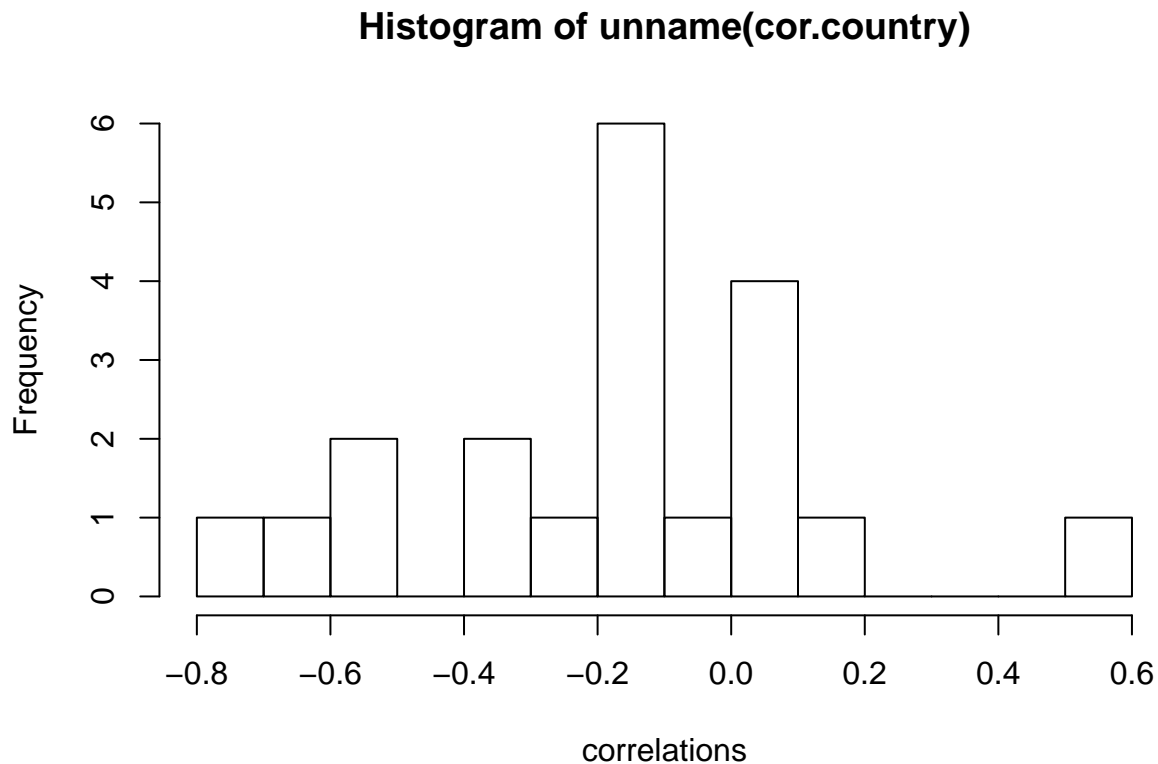
```
## the correlation coefficient between GDP growth and the debt ratio over the whole data set -0.1995
```

```
# (b)
debt.gdp.cor <- function (data) {
  return(cor(data$growth, data$ratio))
}
cor.country <- dapply(debt, .(Country), debt.gdp.cor)
signif(cor.country, 3)

##      Australia      Austria      Belgium      Canada      Denmark      Finland
##      0.025200    -0.253000    -0.192000     0.075000    -0.168000     0.000581
##      France      Germany      Greece      Ireland      Italy      Japan
##     -0.502000    -0.576000    -0.093500    -0.140000    -0.645000    -0.702000
## Netherlands New Zealand      Norway      Portugal      Spain      Sweden
##     -0.199000     0.161000     0.563000    -0.352000     0.081400    -0.161000
##           UK           US
##     -0.137000    -0.341000

cat('The mean of correlations (country):', signif(mean(cor.country),4), '3 digits:', signif(mean(cor.country),3))

## The mean of correlations (country): -0.1778 3 digits: -0.178
hist(unname(cor.country), breaks = 10, xlab = 'correlations')
```



```
# (c)
cor.year <- dapply(debt, .(Year), debt.gdp.cor)
signif(cor.year, 3)

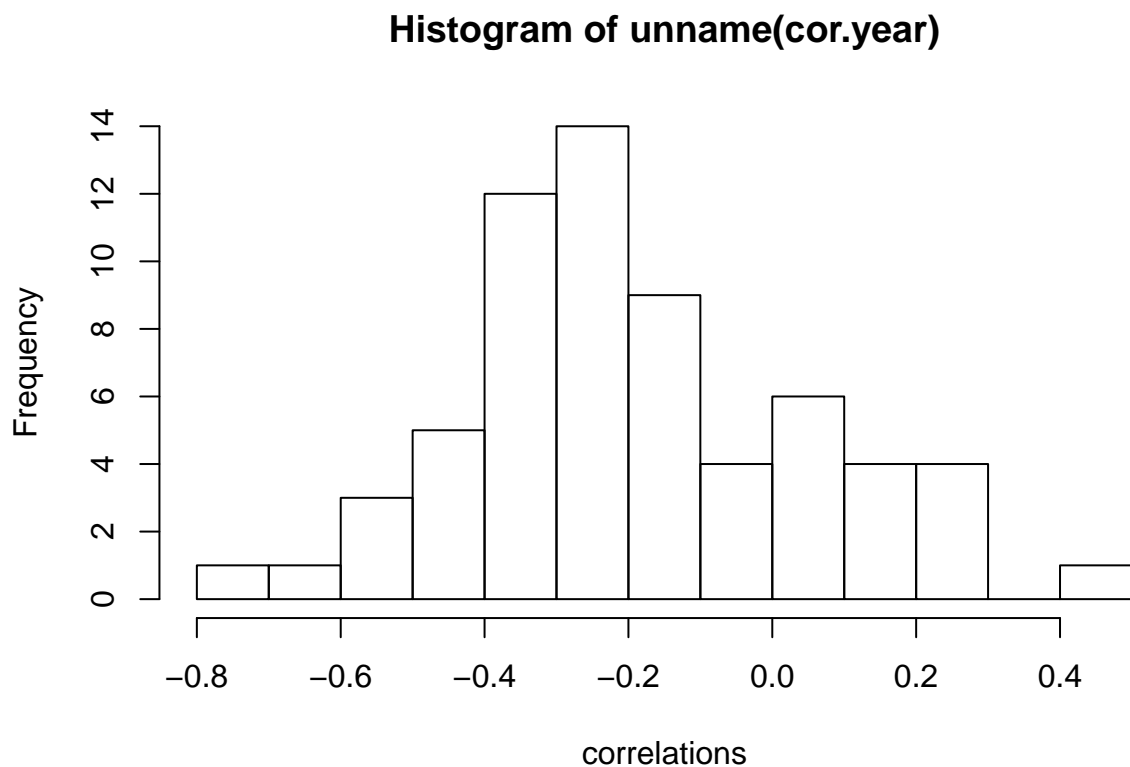
##      1946      1947      1948      1949      1950      1951      1952      1953
##     -0.62000 -0.27400 -0.34000 -0.20000  0.03980 -0.41600 -0.27700 -0.20500
```

```
##      1954      1955      1956      1957      1958      1959      1960      1961
## -0.27500 -0.22700 -0.45800 -0.75500 -0.45400 -0.28500 -0.50400 -0.53900
##      1962      1963      1964      1965      1966      1967      1968      1969
## -0.38300  0.12800 -0.36100 -0.31100 -0.31100 -0.27800 -0.18100 -0.25000
##      1970      1971      1972      1973      1974      1975      1976      1977
## -0.51200  0.00872 -0.19600  0.11400  0.26000  0.27100 -0.17100  0.16400
##      1978      1979      1980      1981      1982      1983      1984      1985
##  0.43100 -0.42900 -0.12700  0.03040  0.23900 -0.36200 -0.15600 -0.44900
##      1986      1987      1988      1989      1990      1991      1992      1993
## -0.35800 -0.06890  0.07970  0.06640  0.15600  0.20200 -0.00222 -0.37200
##      1994      1995      1996      1997      1998      1999      2000      2001
## -0.22400  0.05190 -0.35700 -0.11100 -0.26500 -0.25800 -0.13400 -0.23800
##      2002      2003      2004      2005      2006      2007      2008      2009
## -0.34900 -0.06790 -0.17100 -0.31400 -0.19600 -0.34400 -0.09450 -0.20500
```

```
cat('The mean of correlations (year):', signif(mean(cor.year),4), '3 digits:', signif(mean(cor.year),3))
```

```
## The mean of correlations (year): -0.1906 3 digits: -0.191
```

```
hist(unname(cor.year), breaks = 10, xlab = 'correlations')
```



```
# (d)
```

```
cat('Country: Norway has very high positive corr, Jpan and Germany have high negative corr')
```

```
## Country: Norway has very high positive corr, Jpan and Germany have high negative corr
```

```
cat('Year: 1946 and 1957 have high negative corr, 1978 has high positive corr')
```

```
## Year: 1946 and 1957 have high negative corr, 1978 has high positive corr
```

4

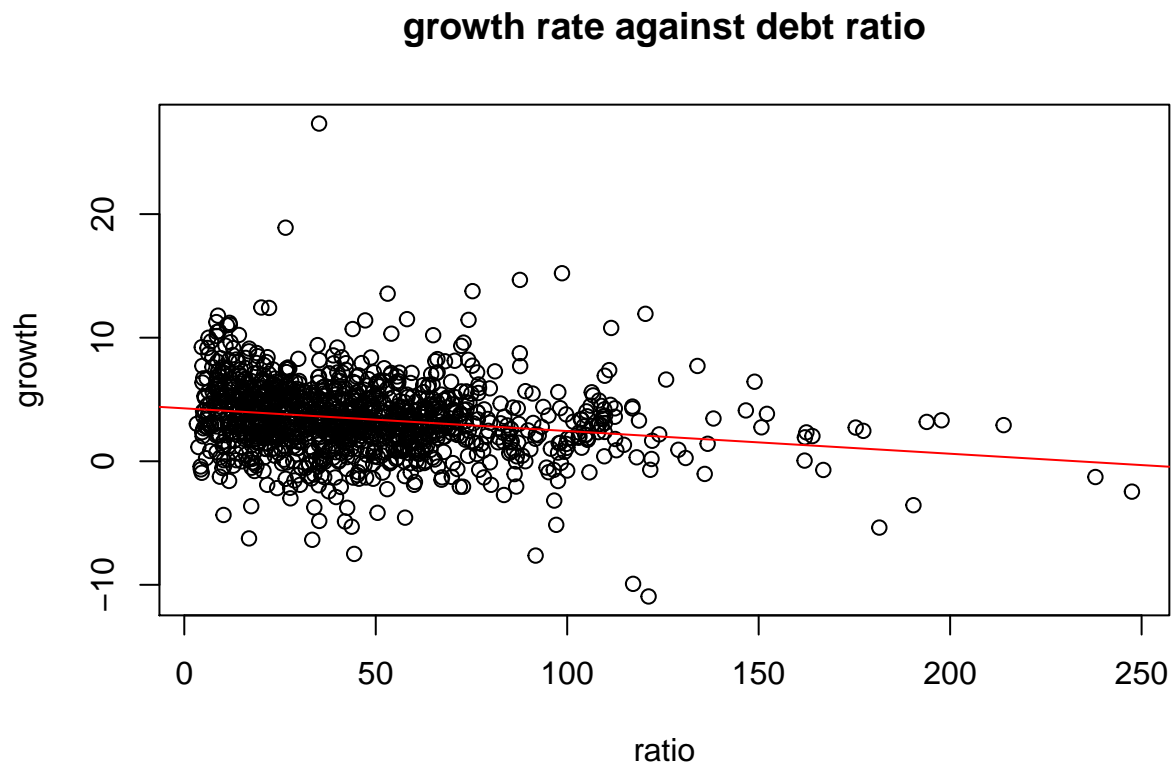
```
lm0 <- lm(debt$growth ~ debt$ratio, data = debt)
cat('slope is ', signif(lm0$coefficients[2], 3))

## slope is -0.0184

cat('intercept is ', signif(lm0$coefficients[1], 3))

## intercept is 4.28

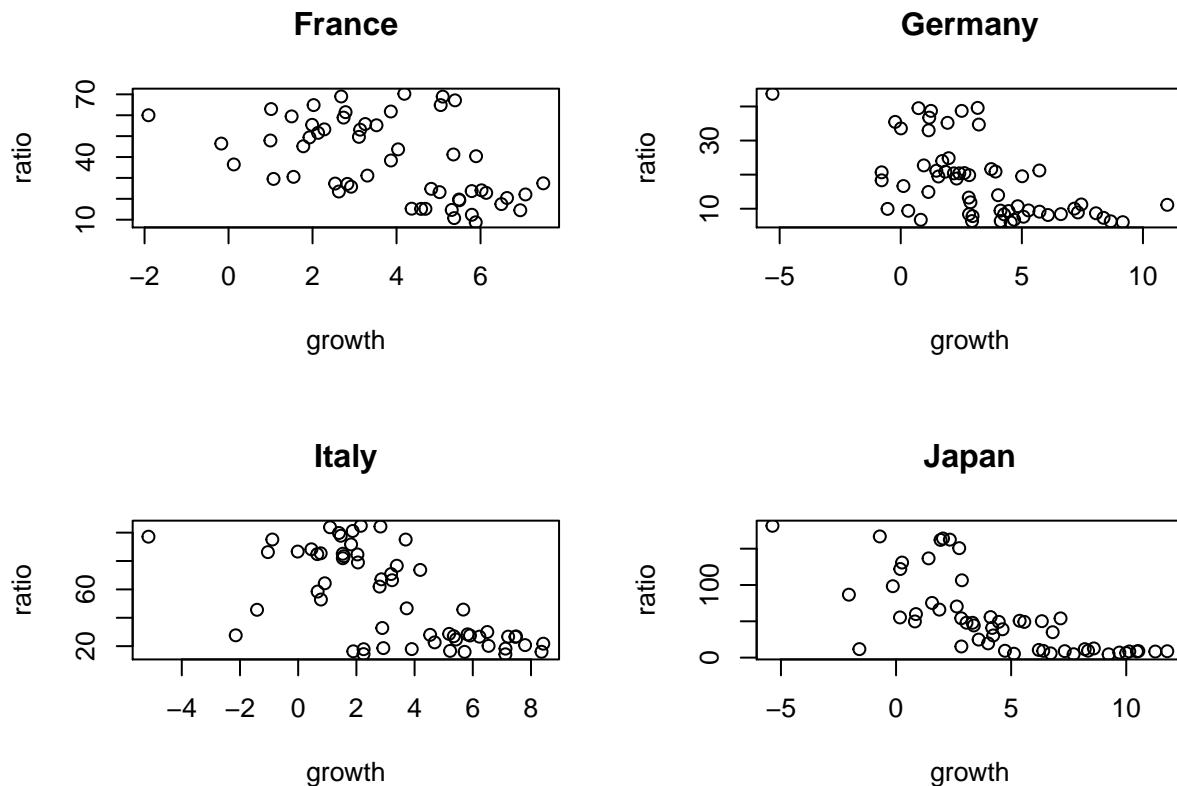
plot(debt$ratio, debt$growth, xlab = 'ratio', ylab = 'growth', main = 'growth rate against debt ratio')
abline(lm0, col = 'red')
```



```
### 5

four.countries <- names(cor.country[cor.country < -0.5])
country.plot <- function (data){
  plot(data$growth, data$ratio, main = unique(data$Country), xlab = 'growth', ylab = 'ratio')
  return(NA)
}

par(mfrow = c(2,2))
dapply(debt[debt$Country %in% four.countries, ], .(Country), country.plot)
```



```
## France Germany Italy Japan
##      NA      NA      NA      NA
```

6

```
# (a)
France <- debt[debt$Country == 'France', ]
dim(France)

## [1] 54  4

# (b)
France$judge <- ifelse((c(France$Year[2:nrow(France)] - 1, NA) == c(France$Year)) == TRUE, 0, NA)
France$next.growth <- c(France$growth[2:nrow(France)], NA) + France$judge
France <- subset(France, select = -judge)
cat('Year 1971:', signif(France[France$Year == 1971,]$next.growth, 3))

## Year 1971: 5.89

cat('Year 1972:', France[France$Year == 1972,]$next.growth)

## Year 1972: NA
```

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```
get.next.growth <- function (data) {
  data$judge <- ifelse((c(data$Year[2:nrow(data)] - 1, NA) == c(data$Year)) == TRUE, 0, NA)
  data$next.growth <- c(data$growth[2:nrow(data)], NA) + data$judge
```

```

data <- subset(data, select = -judge)
return(data)
}
data.list <- ddply(debt, .(Country), get.next.growth)
cat('France Year 2009:', data.list[(data.list$Country == 'France') & (data.list$Year == 2009), ]$next.growth)

## France Year 2009: NA

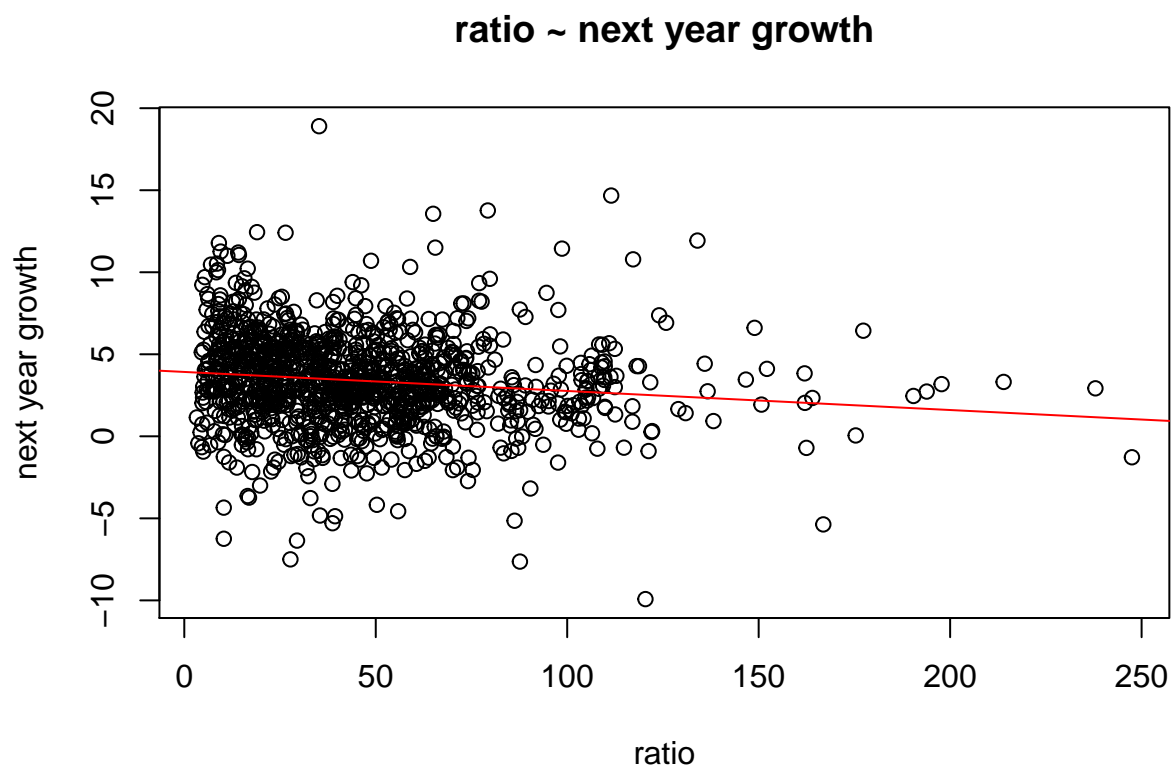
8

```

```

plot(data.list$ratio, data.list$next.growth, xlab = 'ratio', ylab = 'next year growth', main = 'ratio ~ next year growth')
lm1 <- lm(data.list$next.growth ~ data.list$ratio)
abline(lm1, col = 'red')

```



```

cat('Intercept is:', signif(lm1$coefficients[1], 3))

```

```
## Intercept is: 3.92
```

```

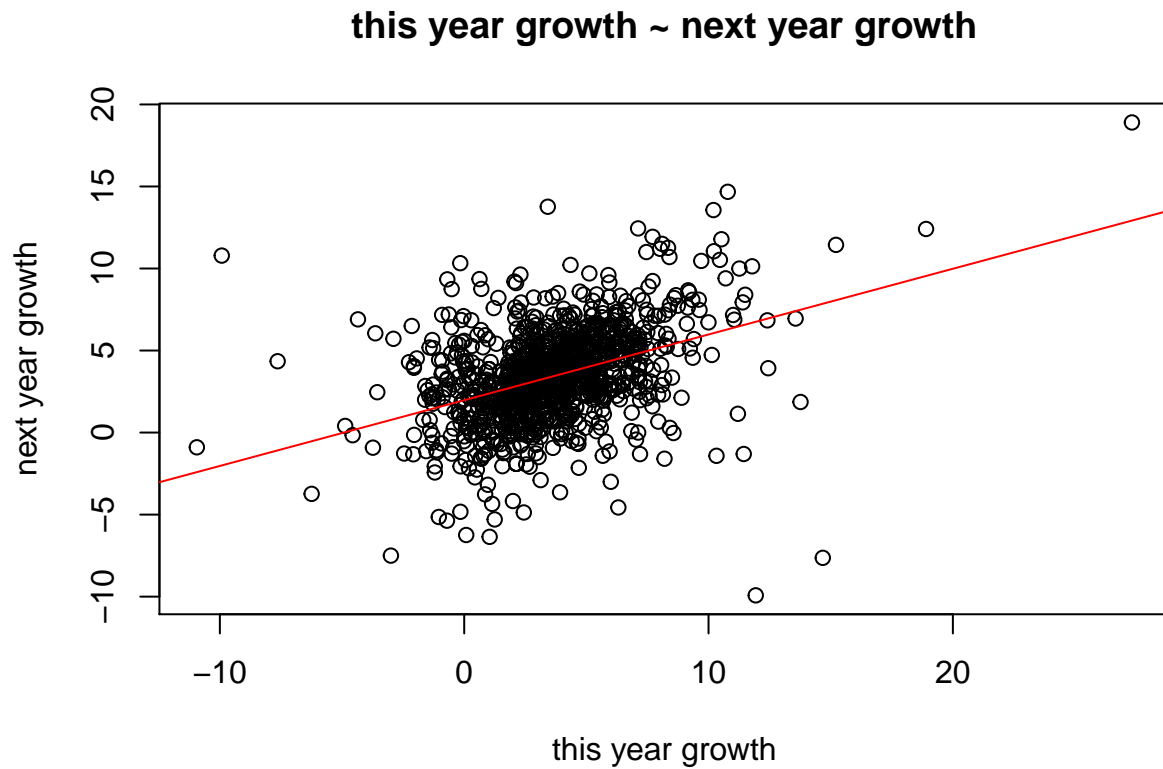
cat('Slope is:', signif(lm1$coefficients[2], 3))

```

```
## Slope is: -0.0116
```

the slope becomes closer to zero, which means the the next year GDP growth is less related to the current debt ratio. The intercept becomes samller, which means the next year GDP growth is likely to be lower than this year if debt ratio is 0

```
plot(data.list$growth, data.list$next.growth, xlab = 'this year growth', ylab = 'next year growth', main = 'this year growth ~ next year growth')
lm2 <- lm(data.list$next.growth ~ data.list$growth)
abline(lm2, col = 'red')
```



Answer: current growth is a better predictor of future growth since it has a more significant slope.