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MTH083 - Advanced Programming for Artificial Intelligence

**Slot 06-
Numpy**

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Numpy

- NumPy is a Python library used for working with arrays
- One of the most important foundational packages for numerical computing in Python.
- Most computational packages providing scientific functionality use NumPy's array objects as the lingua franca for data exchange.
- Providing fast array-oriented operations and flexible broadcasting capabilities

Array

- NumPy is used to work with arrays. The array object in NumPy is called **ndarray**
- Create a NumPy **ndarray** object by using the **array()** function

```
import numpy as np
```

```
arr = np.array([1, 2, 3, 4, 5])
```

```
print(arr) # [1 2 3 4 5]
```

```
print(type(arr)) # <class 'numpy.ndarray'>
```

Array

```
import numpy as np

# from list
print(np.array([1, 2, 3])) # [1 2 3]

# from tuple
print(np.array((1, 2, 3))) # [1 2 3]
print(np.array((1, 2, 3))[2]) # 3

# from set
print(np.array({1, 2, 3})) # {1, 2, 3}
print(np.array({1, 2, 3})[2])

# IndexError: too many indices for array:
# array is 0-dimensional,
# but 1 were indexed
```

Dimensions in Arrays

- A dimension in arrays is one level of array depth (nested arrays)
- 0-D array or Scalars, are the elements in an array
- 1-D array has 0-D arrays as its elements, called uni-dimensional
- 2-D array has 1-D arrays as its elements, called 2-d matrix
- 3-D array has 2-D matrices as its elements

Dimensions in Arrays

```
import numpy as np

arr2d_1 = np.array([[1, 2, 3], [4, 5, 6]])
arr3d_2 = np.array([1, 2, 3, 4], ndmin=3)
print(arr2d_1) # [[1 2 3] [4 5 6]]
print(arr3d_2) # [[[1 2 3 4]]]
print(arr2d_1.ndim, arr3d_2.ndim) # 2 3
```

Shape & Type of ndarray

- Attribute: `ndarray.shape` – Tuple of array dimensions

```
a = np.array([[1, 2],[3, 4], [5, 6]])  
print(a) # [[1 2]  
          #  [3 4]  
          #  [5 6]]  
print(a.shape) # (3, 2)
```

- Attribute: `ndarray.dtype` – Data-type of the array's elements

```
a = np.array([0.5, 1, 2])  
print(a.dtype) # float64
```

Create Array

Function	Description
<code>array</code>	Convert input data (list, tuple, array, or other sequence type) to an ndarray either by inferring a dtype or explicitly specifying a dtype; copies the input data by default
<code>asarray</code>	Convert input to ndarray, but do not copy if the input is already an ndarray
<code>arange</code>	Like the built-in <code>range</code> but returns an ndarray instead of a list
<code>ones</code> , <code>ones_like</code>	Produce an array of all 1s with the given shape and dtype; <code>ones_like</code> takes another array and produces a ones array of the same shape and dtype
<code>zeros</code> , <code>zeros_like</code>	Like <code>ones</code> and <code>ones_like</code> but producing arrays of 0s instead
<code>empty</code> , <code>empty_like</code>	Create new arrays by allocating new memory, but do not populate with any values like <code>ones</code> and <code>zeros</code>
<code>full</code> , <code>full_like</code>	Produce an array of the given shape and dtype with all values set to the indicated “fill value” <code>full_like</code> takes another array and produces a filled array of the same shape and dtype
<code>eye</code> , <code>identity</code>	Create a square $N \times N$ identity matrix (1s on the diagonal and 0s elsewhere)

Example:

```
print(np.zeros(5)) # [0. 0. 0. 0. 0.]
```

```
print(np.ones((2, 3))) # [[1. 1. 1.]  
                        #  [1. 1. 1.]]
```


Type	Type code	Description
int8, uint8	i1, u1	Signed and unsigned 8-bit (1 byte) integer types
int16, uint16	i2, u2	Signed and unsigned 16-bit integer types
int32, uint32	i4, u4	Signed and unsigned 32-bit integer types
int64, uint64	i8, u8	Signed and unsigned 64-bit integer types
float16	f2	Half-precision floating point
float32	f4 or f	Standard single-precision floating point; compatible with C float
float64	f8 or d	Standard double-precision floating point; compatible with C double and Python float object
float128	f16 or g	Extended-precision floating point
complex64, complex128, complex256	c8, c16, c32	Complex numbers represented by two 32, 64, or 128 floats, respectively
bool	?	Boolean type storing True and False values
object	O	Python object type; a value can be any Python object
string_	S	Fixed-length ASCII string type (1 byte per character); for example, to create a string dtype with length 10, use 'S10'
unicode_	U	Fixed-length Unicode type (number of bytes platform specific); same specification semantics as string_ (e.g., 'U10')

Type & Type cast

```
[3] #type cast
arr = np.array([1.5,2,3,4.5,5], dtype=np.float64) #dtype = float64
int_arr = arr.astype(np.int64) #dtype = int64
int_arr

array([1, 2, 3, 4, 5])
```

numpy.arange()

- `arange([start,] stop[, step,][, dtype])`

Parameters :

start : [optional] start of interval range. By default start = 0
stop : end of interval range
step : [optional] step size of interval. By default step size = 1,
For any output out, this is the distance between two adjacent values, out[i+1] - out[i].
dtype : type of output array

Return:

Array of evenly spaced values.
Length of array being generated = `Ceil((Stop - Start) / Step)`

numpy.arange()

```
a1 = np.arange(10)
print(a1, "dim = %d" % a1.ndim)
# [0 1 2 3 4 5 6 7 8 9] dim = 1
a2 = np.arange(2, 10, 3)
print(a2, "dim = %d" % a2.ndim)
# [2 5 8] dim = 1
```

numpy.random.randn

- `random.randn(d0, d1, ..., dn)`: Return a sample (or samples) from the “standard normal” distribution.

If positive `int_like` arguments are provided, `randn` generates an array of shape `(d0, d1, ..., dn)`, filled with random floats sampled from a univariate “normal” (Gaussian) distribution of mean 0 and variance 1. A single float randomly sampled from the distribution is returned if no argument is provided.

Parameters: `d0, d1, ..., dn : int, optional`

The dimensions of the returned array, must be non-negative. If no argument is given a single Python float is returned.

Returns: `Z : ndarray or float`

A `(d0, d1, ..., dn)`-shaped array of floating-point samples from the standard normal distribution, or a single such float if no parameters were supplied.

numpy.random.randn

```
a1 = np.random.randn()
print(type(a1), a1) # <class 'float'> 1.3338705849916304

a2 = np.random.randn(1)
print(type(a2), a2) # <class 'numpy.ndarray'> [1.80212745]

a3 = np.random.randn(2, 3)
print(type(a3), a3.shape) # <class 'numpy.ndarray'> (2, 3)
print(a3) # [[-0.2903103    0.03688071 -0.1302092 ]
           # [-1.27259517  0.69088078  1.98388177]]
```

Numerical operations on arrays

- Elementwise operations:
 - With scalars:

```
a = np.array([1, 2, 3, 4])  
  
print(a + 1) # [2 3 4 5]  
  
print(3 - a) # [ 2  1  0 -1]  
  
print(a*2) # [2 4 6 8]  
  
print(2**a) # [ 2  4  8 16]  
  
print(a//2) # [0 1 1 2]
```

Numerical operations on arrays

- Elementwise operations: With array (same dimension):

```
a = np.array([1, 2, 3, 4])
```

```
b = np.array([5, 1, 7, 4])
```

```
print(a + b) # [ 6  3 10  8]
```

```
print(a - b) # [-4  1 -4  0]
```

```
print(a * b) # [ 5  2 21 16]
```

```
print(a % b) # [1 0 3 0]
```

```
print(2**a - b) # [-3  3  1 12]
```


Numerical operations on arrays

- Matrix multiplication

```
a = np.array([1, 2, 3, 4])
b = np.array([1, 2, 2, 1])
print(a * b) # element-wise multiplication
# [1 4 6 4]
print(a.dot(b)) # matrix multiplication
# 15
print(a.shape, b.shape) # (4,) (4,)
```

Numerical operations on arrays

Comparisons:

```
a = np.array([1, 2, 3, 4])
b = np.array([4, 2, 2, 4])
print(a == b) # [False True False True]
print(a > b) # [False False True False]
```

Array-wise
Comparisons:

```
a = np.array([1, 2, 3, 4])
b = np.array([4, 2, 2, 4])
print(np.array_equal(a, b)) # False
print(np.array_equal(a, a)) # True
```

Numerical operations on arrays

- Logical operations

```
a = np.array([1, 0, 3, 0])
b = np.array([4, 0, 2, 4])
print(np.logical_or(a, b))
# [ True False True  True]
print(np.logical_and(a, b))
# [ True False True  False]
```

List vs numpy array in Math operation

```
[ ] #Multidimensional array object  
my_np_data = np.random.randn(2,3)  
print(my_np_data)
```

```
[[ -0.08221029  0.36287271  0.44168154]  
 [  0.639073    0.52044355 -1.09013561]]
```

```
[ ] my_list = [[-0.14660949,  0.10938535 , 0.73807359],  
               [ 0.23479429, -0.18461008 , -1.22907498]]
```

```
[ ] my_np_data * 10
```

```
array([[ -0.82210292,   3.62872709,   4.41681535],  
       [  6.39073001,   5.20443547, -10.90135605]])
```

```
[ ] my_list * 2
```

```
[[ -0.14660949,  0.10938535,  0.73807359],  
 [ 0.23479429, -0.18461008, -1.22907498],  
 [ -0.14660949,  0.10938535,  0.73807359],  
 [ 0.23479429, -0.18461008, -1.22907498]]
```

Indexing & Slicing

```
# One dimensions
```

```
arr = np.arange(10) # array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

```
arr[5] # 5
```

```
arr[5:8] # array([5, 6, 7])
```

```
arr[5:8] = 12 # array([ 0,  1,  2,  3,  4, 12, 12, 12,  8,  9])
```

```
# Two dimensions
```

```
arr2d = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
```

```
arr2d[2] #array([7, 8, 9])
```

```
arr2d[0][2] # 3
```

```
arr2d[0,2] # 3
```

```
arr2d[:2,1:] # array([[2, 3], [5, 6]])
```

Indexing & Slicing

```
# Three dimensions
```

```
a = np.array([[[1, 2, 3], [4, 5, 6]], [[7, 8, 9], [10, 11, 12]]])
```

```
print(a.shape) # (2, 2, 3)
```

```
temp = a[0] # [[1 2 3]
             #  [4 5 6]]
```

```
temp[:] = 0
```

```
# Explain the result if using the code line "temp = 0"
```

```
print(a) # [[[ 0  0  0]
```

```
          #  [ 0  0  0]]
```

```
          #  [[ 7  8  9]
```

```
          #  [10 11 12]]]
```

Indexing & Slicing

```
temp = 0
```

```
# Explain the result if using the code line "temp = 0"
```

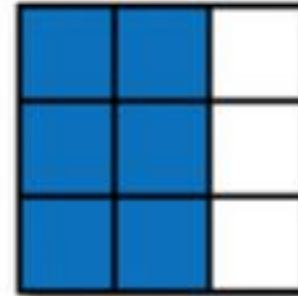
```
print(a) # [[[ 1  2  3]
             #    [ 4  5  6]]
          #    [[ 7  8  9]
          #    [10 11 12]]]
```

Indexing & Slicing



Expression
`arr[:2, 1:]`

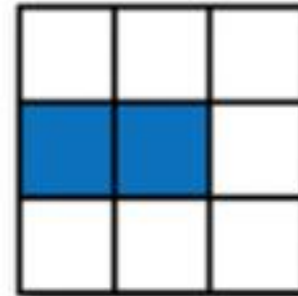
Shape
`(2, 2)`



`arr[:, :2]` `(3, 2)`



`arr[2]` `(3,)`
`arr[2, :]` `(3,)`
`arr[2:, :]` `(1, 3)`



`arr[1, :2]` `(2,)`
`arr[1:2, :2]` `(1, 2)`

Indexing & Slicing

```
>>> a[0, 3:5]
```

```
array([3, 4])
```

```
>>> a[4:, 4:]
```

```
array([[44, 55],  
       [54, 55]])
```

```
>>> a[:, 2]
```

```
a([2, 12, 22, 32, 42, 52])
```

```
>>> a[2::2, ::2]
```

```
array([[20, 22, 24],  
       [40, 42, 44]])
```

0	1	2	3	4	5
10	11	12	13	14	15
20	21	22	23	24	25
30	31	32	33	34	35
40	41	42	43	44	45
50	51	52	53	54	55

Copies & Views in ndarray

```
# View of ndarray via assignment operator  
a = np.array([[1, 2, 3], [4, 5, 6]])  
b = a[0] # creates a view  
print(b) # [1 2 3]  
a[0][0] = 0  
print(b) # [0 2 3]
```

Copies & Views in ndarray

```
# Copy of ndarray  
a = np.array([[1, 2, 3], [4, 5, 6]])  
b = a[0].copy() # creates a copy  
print(b) # [1 2 3]  
a[0][0] = 0  
print(a[0]) # [0 2 3]  
print(b) # [1 2 3]
```

Boolean indexing

- Numpy arrays support a feature called **conditional selection** to generate a new array of boolean values that state whether each element within the array satisfies a particular if statement.

```
arr = np.array([0.69, 0.94, 0.66, 0.73, 0.83])  
index = arr > 0.7 # [False True False True True]  
print(arr[index]) # [0.94 0.73 0.83]
```

Boolean indexing

```
names = np.array(['Bob', 'Will', 'Joe', 'Bob', 'Will'])
data = np.random.randn(5, 3)
print(data)
# [[ 1.64303      -0.91901438 -0.46691434]
#   [ 0.5523564   -1.29891734 -0.76211524]
#   [ 0.3985253    0.60424701  1.68980142]
#   [ 0.82260643   1.74365049 -0.01960414]
#   [ 0.94043782  -1.19145099  0.50533676]]
print(data[names == 'Bob'])
# [[ 1.64303      -0.91901438 -0.46691434]
#   [ 0.82260643   1.74365049 -0.01960414]]
print(data[names == 'Bob', 1:])
# [[-0.91901438 -0.46691434]
#   [ 1.74365049 -0.01960414]]
print(data[names == 'Bob'][1:]) # [[ 0.82260643  1.74365049 -0.01960414]]
```

Boolean indexing

```
names = np.array(['Bob', 'Will', 'Joe', 'Bob', 'Will'])
data = np.random.randn(5, 3)
print(data)
# [[ 1.64303      -0.91901438 -0.46691434]
#  [ 0.5523564   -1.29891734 -0.76211524]
#  [ 0.3985253    0.60424701  1.68980142]
#  [ 0.82260643   1.74365049 -0.01960414]
#  [ 0.94043782  -1.19145099  0.50533676]]
print(data[names != 'Bob'])
# [[-1.71144185  1.04257142  2.49841375]
#  [ 0.32656577  0.30792468  1.18419888]
#  [-0.55027386  0.80837473 -2.06744318]]
# Negative condition
print(data[~(names != 'Bob')])
# [[-1.65340362  0.20757075  0.97750883]
#  [-0.9188661  -1.23559978  0.13120124]]
```

Fancy Index

- Besides using indexing & slicing, NumPy provides you with a convenient way to index an array called fancy indexing.
- Fancy indexing allows you to index a numpy array using the following:
 - Another numpy array
 - A Python list
 - A sequence of integers

Fancy Index

```
a = np.arange(1, 10)
print(a) # [1 2 3 4 5 6 7 8 9]
indices = np.array([2, 3, 4])
print(a[indices]) # [3 4 5]
```


Fancy Index

```
[ ] arr = np.array([[ 0,  1,  2,  3],  
                    [ 4,  5,  6,  7],  
                    [ 8,  9, 10, 11],  
                    [12, 13, 14, 15],  
                    [16, 17, 18, 19],  
                    [20, 21, 22, 23],  
                    [24, 25, 26, 27],  
                    [28, 29, 30, 31]])
```

```
arr[[1,4,7]]
```

```
array([[ 4,  5,  6,  7],  
       [16, 17, 18, 19],  
       [28, 29, 30, 31]])
```

```
[ ] arr[[1,4, 7], [0, 0, 1]]
```

```
array([ 4, 16, 29])
```

```
[ ] arr[[1, 5, 7, 2]][:,[0, 3, 1, 2]]
```

```
array([[ 4,  7,  5,  6],  
       [20, 23, 21, 22],  
       [28, 31, 29, 30],  
       [ 8, 11,  9, 10]])
```

Reshape

- Reshaping means changing the shape of an array

```
arr = np.array([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12])
newArr = arr.reshape(4, 3)
print(newArr)
# [[ 1  2  3]
#   [ 4  5  6]
#   [ 7  8  9]
#  [10 11 12]]
```

Reshape

- Reshaping returns the view of the original array

```
arr = np.array([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12])
newArr = arr.reshape(4, 3)
print(newArr)
# [[ 1  2  3]
#   [ 4  5  6]
#   [ 7  8  9]
#  [10 11 12]]
arr[1] = 10
print(newArr)
# [[ 1 10  3]
#   [ 4  5  6]
#   [ 7  8  9]
#  [10 11 12]]
```

Reshape: Unknown Dimension

- Pass -1 as the value, and NumPy will calculate this number for you

```
arr = np.array([1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12])
newArr = arr.reshape(2, 3, -1)
print(newArr)
# [[[ 1  2]
#    [ 3  4]
#    [ 5  6]]
#   [[ 7  8]
#    [ 9 10]
#   [11 12]]]
```

Exercise

- Ex1: Given an integer matrix of $N \times M$, set negative values in the matrix to 0
- Ex2: Given an integer matrix of $N \times M$, set negative values in even rows to 0

Exercise

Ex3: Create a checkboard matrix NxN as follows:

```
[[0 1 0 1 0 1 0 1]
 [1 0 1 0 1 0 1 0]
 [0 1 0 1 0 1 0 1]
 [1 0 1 0 1 0 1 0]
 [0 1 0 1 0 1 0 1]
 [1 0 1 0 1 0 1 0]
 [0 1 0 1 0 1 0 1]
 [1 0 1 0 1 0 1 0]]
```

Exercise

Ex4: Create a matrix NxM with 1 in borders and 0 for inside:

$$\begin{bmatrix} [1 & 1 & 1 & 1 & 1] \\ [1 & 0 & 0 & 0 & 1] \\ [1 & 0 & 0 & 0 & 1] \\ [1 & 0 & 0 & 0 & 1] \\ [1 & 1 & 1 & 1 & 1] \end{bmatrix}$$

Exercise

Ex5: Create a NxN matrix as follows:

N = 4

```
[[100    1    2    3]
 [  4 100    6    7]
 [  8    9 100   11]
 [ 12   13   14 100]]
```


Exercise

Ex6: Write a function to multiply two matrices $N \times N$ without using `np.dot()`

THANK YOU
for YOUR ATTENTION