Macroeconomic Modeling with Julia

 ${\sf QuantEcon-RBA\ Workshop}$

March 2017





Thanks

- Adam Cagliarini and the RBA
- Marco del Negro and the FRBNY
- Julia Computing
- Sponsors of QuantEcon







NumFOCUS





Team

Pearl Li

Research Analyst at the FRBNY

Erica Moszkowski

Research Analyst at the FRBNY

John Stachurski

Academic, interests in computation, stochastic modeling

Pablo Winant

• Bank of England, macroeconomist, lead author of dolo





Schedule

Lecture 1

• Introduction and overview (John)

Lecture 2

The Julia language (Pearl)

Lecture 3

Julia for economists – libraries and features (Pablo)

Lecture 4

• DSGE modeling with Julia (Erica)





Aims and Assumptions

Assumptions

- Participants are programmers but new to Julia
- Interested in macroeconomics

Aims

- Background, overview and comparisons
- Lower fixed costs to getting started
- Provide resources for further study





Resources

Workshop homepage:

• https://github.com/QuantEcon/RBA_RBNZ_Workshops

Further resources listed there...



Software Options

Install

- 1. Julia
- 2. Packages such as IJulia, QuantEcon.jl
- 3. IDE (if you like) such as Juno

Or

1. JuliaPro



Overview of Scientific Computing

Tasks

- Solve numerical problems
- Produce figures and graphs
- Manipulate data
- Explore (simulate, plot, visualize, etc.)

And sometimes we need speed





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The Need for Speed

Maximum speed:

- Optimal use of hardware
- High level of control over calculations / logic

First best = assembly / machine code

Individual instructions at the CPU level

For example, let's add 1+2



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```
.cfi_startproc
              %rbp
pushq
.cfi_def_cfa_offset 16
.cfi_offset 6, -16
            %rsp, %rbp
movq
.cfi_def_cfa_register 6
movl
             1, -12(\%rbp)
movl
             $2, -8(\%rbp)
movl
            -12(\%rbp), %edx
            -8(\%rbp), \%eax
movl
addl
            %edx, %eax
            \%eax, -4(\%rbp)
movl
movl
             -4(\%rbp), \%eax
             %rbp
popq
.cfi_def_cfa 7, 8
ret
.cfi_endproc
```



Now imagine a heterogeneous agent model with 5 state variables...

And then optimizing for specific hardware

- pipelining
- cache hierarchies
- branch prediction
- coprocessors
- etc.

And then Intel brings out a new processor..



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Conclusion: There's a trade off

Low level languages give us

- speed
- fine grained control

High level languages give us

- abstraction
- automation of some tasks
- natural language representations





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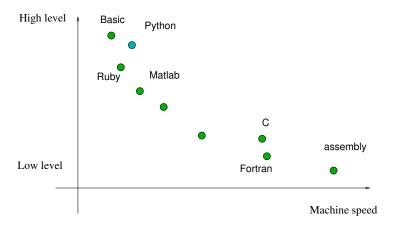
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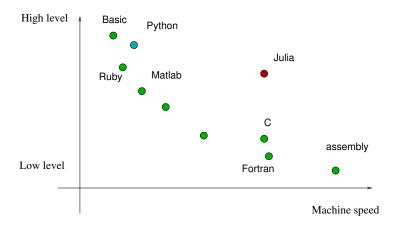






That said, the curve is starting to shift...









A Horse Race

Task:

- 1. compute X_1, X_2, \ldots, X_n via $X_{t+1} = \beta + \alpha X_t + W_{t+1}$ $W_t \sim N(0,1)$
- 2. calculate and return $\frac{1}{n} \sum_{t=1}^{n} X_t$

Set
$$n = 10^7$$

• RBA_RBNZ_Workshops/john/fast_loop_examples



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Modern, high level, open source, scientific programming language

Strengths

- High productivity...
- and high performance!

Negatives

- Still under development
- The "rabbit hole" of advanced features (plus or minus?)





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Why Open Source?

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Interacting with Julia

Options

- 1. The REPL + a text editor (e.g., Atom or Sublime)
- 2. IDEs like Juno
- 3. Jupyter notebooks





Jupyter Notebooks

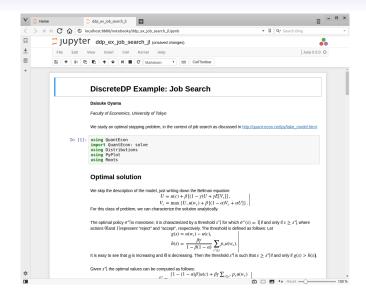
A browser based front end to Python, Julia, R, etc.

- Allows for rich text, graphics, etc.
- Easy to run remotely on servers / in cloud

Examples: http://notebooks.quantecon.org/











Let's try it out

• RBA_RBNZ_Workshops/john/ar1_plots_julia.ipynb

