# Among Site (Beta) Diversity

Z620: Quantitative Biodiversity, Indiana University
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## **OVERVIEW**

In this excercise, we move beyond the investigation of within-site  $\alpha$ -diversity. We will explore  $\beta$ -diversity, which is defined as the diversity that occurs among sites. This requires that we examine the compositional similarity of assemblages that vary in space or time.

After completing this exercise you will know how to:

- 1. formally quantify  $\beta$ -diversity
- 2. visualize  $\beta$ -diversity with heatmaps, cluster analysis, and ordination
- 3. test hypotheses about  $\beta$ -diversity using multivariate statistics

# 1) SETUP

# A. Retrieve and Set Your Working Directory

```
rm(list = ls())
getwd()
setwd("~/GitHub/QB-2017/Week3-Beta/")
```

### B. Load Packages

We will be using the vegan package again; let's load it now.

```
require("vegan")
```

# 2) LOADING DATA

## A. Description of Data Set

To date, we have analyzed biodiversity data sets for freshwater zooplankton, tropical trees, and soil bacteria. In this exercise, we introduce a new dataset containing information on stream fish assemblages from the Doubs river, which runs near the France-Switzerland boarder in the Jura Mountains. The data set (doubs) includes fish abundances, environmental variables, and spatial cooridinates for 30 sites. The data set has previously been used to demonstrate that fish communities can be good indicators of ecological zones in rivers and streams.

Let's load the ade package, which contains the doubs data set.

```
require("ade4")
data(doubs)
```

### B. Introduction to a New Data Structure: Lists

While working in R this semester, we have learned about vectors, matrices, and data frames. Here we introduce another data structure: a **list**. In R, a list is an object that contains a collection of other objects of similar or different types.

# C. Exploring the Doubs River Data Set

We can use the str() function to describe the attributes of doubs, which is a list. Because this dataset is somewhat complex, we can pass the "max.level = 1" argument to minimize the str() output. Also, you can use the dollar sign (\$) between the list name (doubs) and objects within the list (e.g., env) to explore the data set. For example, to access the site-by-environment matrix, you would pass doubs\$env to the R console. Last, recall that you can use help() to learn more about a dataset contained in a package.

str(doubs, max.level = 1)

Question 1: Describe some of the attributes of the doubs dataset.

- a. How many objects are in doubs?
- b. What types of data structures are contained in doubs?
- c. What are the units of nitrate ("nit") in the stream water?
- d. How many fish species are there in the doubs data set?

Answer 1a:

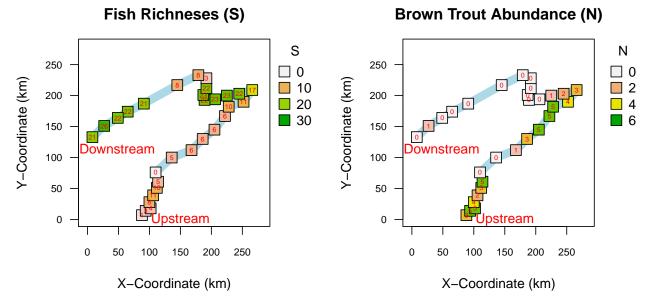
Answer 1b:

Answer 1c:

Answer 1d:

#### D. Visualizing the Doubs River Dataset

There is a wealth of information in the doubs dataset that can be used to address various issues related to  $\beta$ -diversity. For example, we might use the environmental or spatial data to develop or test a hypothesis. Below we have generated two plots of the doubs fish data. The first plot shows fish richness at each site in the stream. The second plot shows the abundance of a particular fish species, Brown Trout (Salmo trutta), at each site in the stream.



**Question 2:** Answer the following questions based on the spatial patterns of richness (i.e.,  $\alpha$ -diversity) and Brown Trout (Salmo trutta) abundance in the Doubs River.

- a. How does fish richness vary along the sampled reach of the Doubs River?
- b. How does Brown Trout (Salmo trutta) abundance vary along the sampled reach of the Doubs River?
- c. What do these patterns say about the limitations of using richness when examining patterns of biodiversity?

Answer 2a: Answer 2b: Answer 2c:

# 3) QUANTIFYING BETA-DIVERSITY BETWEEN TWO SAMPLES

There are various ways to quantify  $\beta$ -diversity. Perhaps one of the simplest metrics is **Whittaker's**  $\beta$ -**Diversity**, which was developed by Robert Whittaker (1960). This classic index is useful for comparing  $\beta$ -diversity between two samples. The equation for Whittaker's  $\beta$ -Diversity is as follows:  $\beta_W = \frac{S}{\bar{\alpha}} - 1$ , where  $S = \text{the total number of species recorded across sites (i.e., <math>\gamma$ -diversity) and  $\bar{\alpha}$  is the mean richness (i.e.,  $\alpha$  diversity) among sites. Subtracting 1 scales  $\beta_w$  from 0 (minimum  $\beta$ -diversity) to 1 (maximum  $\beta$ -diversity).

We can write  $\beta_W$  as a function in R as follows:

Question 3: Using the beta.w function above, answer the following questions:

- a. What is the  $\beta$ -diversity for fish assemblages sampled from site 1 and site 2 of the doubs data set?
- b. Based on the formula for  $\beta_w$ , what does this value represent?

Answer 3a: Answer 3b:

# 4) QUANTIFYING BETA-DIVERSITY FOR TWO OR MORE SAMPLES

Often, we often want to compare the diversity of more than just a pair of samples. For example, it would be nice to be able to compare fish assemblages for *all* of sites in the Doubs River. In this section we will estimate  $\beta$ -diversity for multiple samples. During this process, you will learn how to generate similarity and dissimilarity matrices for different data sets that will be needed for visualizing and quantifying  $\beta$ -diversity.

# A. Introducing the Resemblance Matrix

In order to quantify  $\beta$ -diversity for more than two samples, we need to introduce our second primary ecological data structure: the **Resemblance Matrix**. In the context of biodiversity, a resemblance matrix is a data structure that calculates the pairwise **similarity** or **dissimiliarity** for all samples in a site-by-species matrix. The resemblance matrix can be generated from a site-by-species matrix containing incidence (presence-absence) data or abundance data. In the sections below, we describe some of the similarity and dissimilarity metrics that are commonly used for constructing a resemblance matrix. Throughout this handout, we adopt the

notations of Table 7.2 in Legendre & Legendre (2012); this book can be electronically accessed via the IU library (see the course syllabus [http://goo.gl/y4oK7c]).

## B. Incidence-Based Measures of Similarity and Dissimilarity

When you are working with presence-absence data, you can use the following metrics for generating a similarity or dissimilarity matrix.

Index	Equation	Properties
Jaccard	$S_7 = \frac{a}{a+b+c}$	Compares the number of shared species to the number of species in the combined assemblages (global view)
Sørensen	$S_8 = \frac{2a}{(2a+b+c)}$	Compares the number of shared species to the mean number of species in a single assemblage (local view)

In the above table, a = the number of species shared between assemblages, b = the number of unique species in the first assemblage, and c = the number of unique species in the second assemblage.

Question 4: Answer the following questions about incidence-based measures of similarity:

- a. What are the differences between Jaccard and Sørensen metrics?
- b. When might you use one instead of the other?
- c. In what situations would these metrics of  $\beta$ -diversity fail?

Answer 4a:

Answer 4b:

Answer 4c:

Notes on incidence-based similarity: Jacard and Sørensen are perhaps the two most commonly used incidence-based measures of similarity. Others include Ochiai, Kulczynski-Cody, and Lennon, which can be found in Table 6.1 of Magurran & McGill (2011). The differences in these measures include how means are calculated (Sørensen = harmonic mean, Ochiai = geometric mean, and Kulczynski-Cody = arithmetic mean), and how unique species are dealt with if only one sample has unique species (Lennon). Also, it is important to note that these metrics calculate similarity, but can (and in many cases should) be converted to dissimilarity (D). In vegan, disimilarities (D) are usually returned from functions instead of similarities (S). The conversion between similarity and dissimilarity is calculated as D = 1 - S.

## C. Abundance-Based Measures of Similarity and Dissimilarity

When you are working with abundance data, you can use the following metrics for generating a similarity or dissimilarity matrix.

Index	Equation	Properties
Bray-Curtis Dissimilarity	$D_{14} = \frac{\sum_{j=1}^{p}  y_{1j} - y_{2j} }{\sum_{j=1}^{p} (y_{1j} + y_{2j})}$	A quantitative version of the Sørensen index. Commonly used measure of similarity. Also known as the <i>percentage difference</i> .
Morisita-Horn	$S_{MH} = \frac{2\sum_{j=1}^{p} y_{1j} \cdot y_{2j}}{\left(\sum_{j=1}^{p} y_{1j}^2 + \sum_{j=1}^{p} y_{2j}^2\right)}$	A measure of <i>compositional overlap</i> . Uses squared differences in relative abundance and thus is influenced by abundant species. Resistant to undersampling.

In the above table  $y_{1j}$  is the abundance of each species (1:p) in site 1 and  $y_{2j}$  is the abundance of each species (1:p) in site 2. As with incidence-based measures, there are many other options for calculating similarity or dissimilarity between communities, including Mean Character Difference, Canberra, Coefficient of Divergence, and Gower.

### D. A Cautionary Note on Other Measures of Distance

There are other distance measures that you are likely to encounter because they are widely used. It is important to note that some of these should *not* be used for abundance-based data in biodiversity analyses. This is because they lead to the **Species Abundance Paradox**, which is a phenomenon that occurs when the distance between two sites that have no species in common is smaller than the distance between sites with shared species. In particular, the paradox described above arises when Euclidean Distance and Manhattan Distance are used:

**Euclidean Distance**: 
$$D_1 = \sqrt{\sum_{j=1}^{p} (y_{1j} - y_{2j})^2}$$

Manhattan Distance: 
$$D_7 = \sum_{j=1}^p |y_{ij} - y_{2j}|$$

Methods exist to transform species abundance data prior to implementing metrics like Euclidean Distance and Manhattan Distance (e.g., Chord transformation and Chi-Square transformation). It is recommended that you read more about these distance metrics if you are interested in implementing them to address your research questions.

# E. Constructing the Resemblance Matrix

Conveniently, vegan includes many of the similarity metrics used to construct a resemblance matrix. These metrics can be calcualted using the vegdist() function. Let's use vegdist to create a resemblance matrix for the fish assemblages in the Doubs River. Before that, we'll need to remove site 8 from doubs because for some reason it has no observations.

```
fish <- doubs$fish
fish <- fish[-8, ] # Remove site 8 from data

# Calculate Jaccard
fish.dj <- vegdist(fish, method = "jaccard", binary = TRUE)

# Calculate Bray-Curtis
fish.db <- vegdist(fish, method = "bray")</pre>
```

Now that we've created a resemblance matrix, it would be nice to visualize the fish assemblages of the Doubs River. As a start, we can print the Bray-Curtis-based resemblance matrix in the console:

```
fish.db
```

From this, you will see a large diagonal matrix. Typically, resemblance matrices just show the upper or lower triangle of values. This is because the two triangles have the same information. However, you can generate a square resemblance matrix with the following command:

```
fish.db <- vegdist(fish, method = "bray", upper = TRUE, diag = TRUE)</pre>
```

**Question 5**: Does the resemblance matrix (fish.db) represent similarity or dissimilarity? What information in the resemblance matrix led you to arrive at your answer?

Answer 5:

# 5) VISUALIZING BETA-DIVERSITY

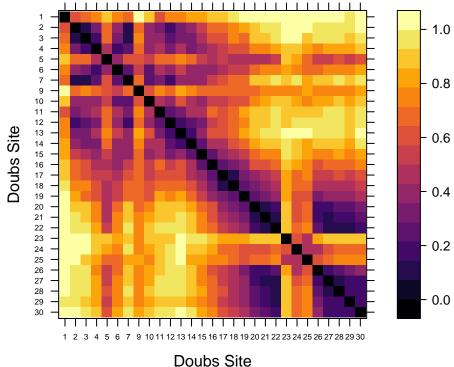
# A. Heatmaps

One way to visualize  $\beta$ -diversity is to plot the data in our resemblance matrix using a **heatmap**. Heatmaps are a two-dimensional, color representation of a data matrix. Here we are going to use the levelplot() function in the lattice package of R. This function will allow us to make a basic heatmap of our resemblance matrix. First, there are a few things we need to do:

- 1. Define a color palette. R includes many predefined color palettes; however, we are going to use another color palette. The package viridis includes four color palettes, each of which are perceptually uniform and both colorblind- and black-and-white-friendly.
- 2. Ensure that our resemblance matrix is plotted correctly. In particular, we need specify the order in which we want our sites to be plotted in the heatmap.

```
# Get a Color Palette
# install.packages("viridis")
require(viridis)
## Loading required package: viridis
# Define Order of Sites
order <- rev(attr(fish.db, "Labels"))</pre>
# Plot Heatmap
levelplot(as.matrix(fish.db)[, order], aspect = "iso", col.regions = inferno,
          xlab = "Doubs Site", ylab = "Doubs Site", scales = list(cex = 0.5),
          main = "Bray-Curtis Distance")
```

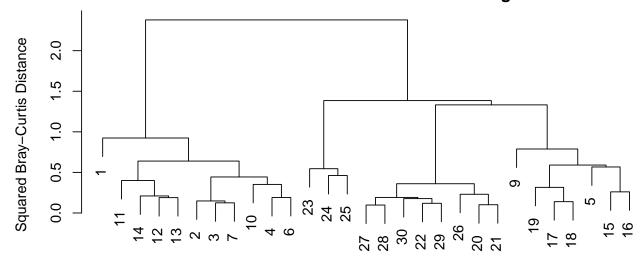
# **Bray-Curtis Distance**



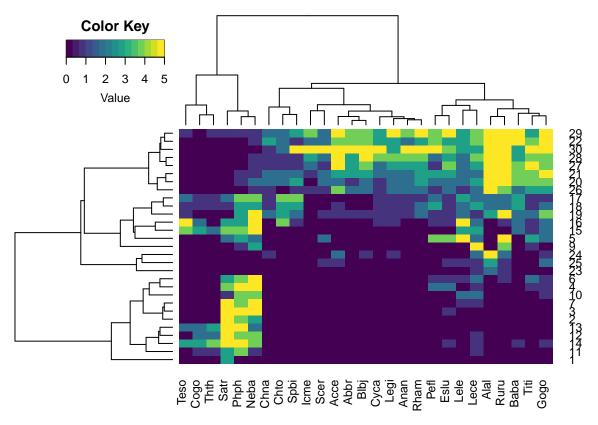
# B. Cluster Analysis

Another common way to visualize  $\beta$ -diversity is through cluster analysis. Cluster analysis is an exploratory technique that assigns objects to groups based on their similarity to one another. In this exercise, we will use hierarchical clustering, specifically **Ward's Clustering**. Ward's Clustering (a.k.a., Ward's minimum variance method) is an agglomerative clustering technique based on the linear model criterion of least squares. The method minimizes within-cluster sums-of-squared distances between sites. However, there are numerous methods for clustering (e.g., Single Linkage, UPGMA, UPGMC), which can influence the conclusions that you draw from your analysis. See chapter 8 of Legendre and Legendre (2012) for more information on the various clustering methods that can be used.

# **Doubs River Fish: Ward's Clustering**



Another clustering tool that aids in visualization for exploratory purposes is heatmap.2(), which is a function in the gplots package. This tool generates a cluster diagram that allows one to examine the abundance of different fish species in different sites.



**Question 6**: Based on cluster analyses and the introdutory plots that we generated after loading the data, develop a hypothesis for the doubs data set?

### Answer 6:

### C. Ordination

The primary aim of ordination is to represent multiple objects in a reduced number of orthogonal (i.e., independent) axes. The first axis of an ordination explains the most variation in the data set, followed by the second axis, then the third, and so on, where the total number of axes is less than or equal to the number of objects. Ordination plots are particularly useful for visualizing the similarity among objects. For example, in the context of  $\beta$  diversity, sites that are closer in ordination space have species assemblages that are more similar to one another than sites that are further apart in ordination space.

There are various ordination techniques that can be applied to multivariate biodiversity data. Common methods include: Principal Components Analysis (PCA), Correspondence Analysis (CA), Principal Coordinates Analysis (PCoA), Factor Analysis (FA), and Nonmetric Multidemensional Scaling (NMDS). When choosing an ordination technique, careful consideration should be given to the data type (continuous vs. categorical), model assumptions, and the underlying mathematical procedures that are invovled.

### i. An Overview of Principal Coordinates Analysis (PCoA)

In this exercise, we focus on Principal Coordinates Analysis (PCoA), which is sometimes referred to as metric multidimensional scaling. PCoA starts with creating a matrix,  $\boldsymbol{A}$ , which is a transformed and centered version of distance matrix,  $\boldsymbol{D}$ . Because these steps preserve all distances, PCoA is a flexible ordination technique that allows us to use virtually any distance metric (e.g., Jaccard, Bray-Curtis, Gower, Euclidean, etc.). The dimensionality of  $\boldsymbol{A}$  is then reduced by determining each eigenvector,  $\boldsymbol{u}_i$ , and eigenvalue,  $\lambda_i$ , that solve the

following equation:  $\mathbf{A}\mathbf{u}_i = \lambda_i \mathbf{u}_i$ . Finally, each eigenvector,  $\mathbf{u}_i$ , is scaled to length  $\sqrt{\lambda_i}$  to obtain the principal coordinates.

To conduct a PCoA, we will use the cmdscale() function from the stats package, which performs PCoA. The input for this function is our resemblance matrix (Bray-Curtis distances for the doubs dataset). In addition, we are going to set k = 3 (number of dimensions we want returned) and eig = TRUE (which saves the eigenvalues).

```
fish.pcoa <- cmdscale(fish.db, eig = TRUE, k = 3)
```

### ii. Interpetting PCoA Output

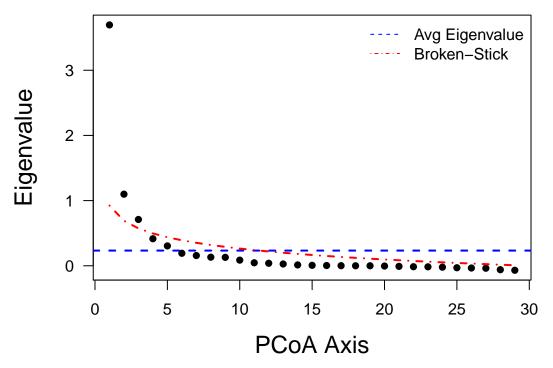
The cmdscale function produces a list of output. The first item *points* contains the coordinates for each site in each reduced dimension. The second item *eig* contains the eigenvalues. The last three items pertain to other options of the analysis that we will not cover here.

First, we want to examine the eigenvalues. The eigenvalues are the scaling factors that allowed us to reduce the dimensionality of a data set. The eigenvalues can also be used to calcualte the amount of variation that is explained by each orthogonal axis. To do this, we divide the eigenvalue of each axis by the sum of all eigenvalues. In the following chunk of R code, we quantify the percent variation in the doubs data set that is explained by the first three axes of the PCoA.

```
explainvar1 <- round(fish.pcoa$eig[1] / sum(fish.pcoa$eig), 3) * 100
explainvar2 <- round(fish.pcoa$eig[2] / sum(fish.pcoa$eig), 3) * 100
explainvar3 <- round(fish.pcoa$eig[3] / sum(fish.pcoa$eig), 3) * 100
sum.eig <- sum(explainvar1, explainvar2, explainvar3)</pre>
```

Another way to evaluate our analysis is to assess whether or not the first few PCoA axes capture a disproportionately large amount of the total explained variation. First, the eigenvalues associated with the first few axes should be larger than the average of all the eigenvalues (Kaiser- $Guttman\ criterion$ ). Second, we can compare the eigenvalues associated with the first few axes to the expectations of the broken- $stick\ model$ , which we introduced in the  $\alpha$ -diversity exercise when discussing species abundance distributions (SAD). In the current context, the broken stick model assumes that the total sum of eigenvalues decreases sequentially with ordered PCoA axes.

We will evaluate these two criteria with the following plots:



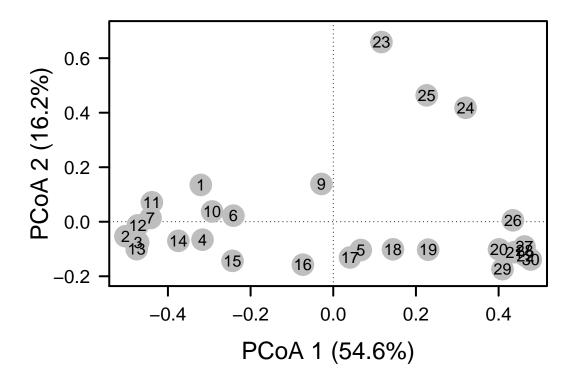
**Question 7**: Based on the three criteria described above, does the PCoA do a good job of explaining variation in the doubs data set? Please justify.

Answer 7:

# iii. Creating a PCoA Ordination Plot

Having evaluated the PCoA output, now we will create an ordination plot. We will plot all of the fish assemblages of the Doubs River for the first two PCoA axes.

```
# Define Plot Parameters
par(mar = c(5, 5, 1, 2) + 0.1)
# Initiate Plot
plot(fish.pcoa$points[ ,1], fish.pcoa$points[ ,2], ylim = c(-0.2, 0.7),
     xlab = paste("PCoA 1 (", explainvar1, "%)", sep = ""),
     ylab = paste("PCoA 2 (", explainvar2, "%)", sep = ""),
     pch = 16, cex = 2.0, type = "n", cex.lab = 1.5, cex.axis = 1.2, axes = FALSE)
# Add Axes
axis(side = 1, labels = T, lwd.ticks = 2, cex.axis = 1.2, las = 1)
axis(side = 2, labels = T, lwd.ticks = 2, cex.axis = 1.2, las = 1)
abline(h = 0, v = 0, lty = 3)
box(lwd = 2)
# Add Points & Labels
points(fish.pcoa$points[ ,1], fish.pcoa$points[ ,2],
       pch = 19, cex = 3, bg = "gray", col = "gray")
text(fish.pcoa$points[ ,1], fish.pcoa$points[ ,2],
     labels = row.names(fish.pcoa$points))
```



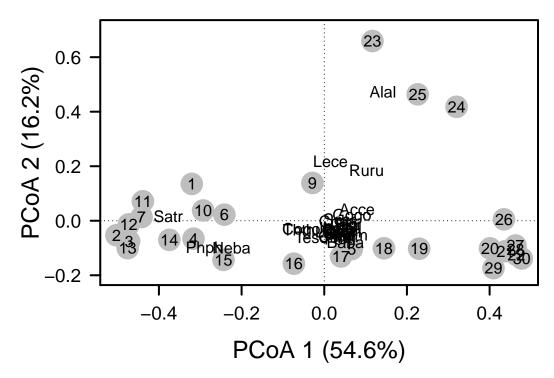
# iv. Identifying and Visualizing Influential Species in PCoA

Basic ordination plots allow us to see how samples separate from one another. A logical follow-up is to ask what features of the data set are driving the observed divergence among points. In the Doubs River example, sites are separating along the PCoA axes owing to variation in the abundance of different fish species. We can get a better sense of "who" is contributing to this trend by plotting explanatory vectors (i.e., species coordinates) in ordination space. We can obtain this information using the add.spec.scores() function in the BiodiversityR package. These coordinates reflect the strength and direction that each species has on the ordination of the different sites.

```
require("BiodiversityR")

# Calculating Relative Abundance
fishREL <- fish
  for(i in 1:nrow(fish)){
    fishREL[i, ] = fish[i, ] / sum(fish[i, ])
    }

# Calculate and Add Species Scores
fish.pcoa <- add.spec.scores(fish.pcoa,fishREL,method = "pcoa.scores")
text(fish.pcoa$cproj[ ,1], fish.pcoa$cproj[ ,2],
    labels = row.names(fish.pcoa$cproj), col = "black")</pre>
```



A more quantitative way of identifying influential species involves determining the correlation of each species along the PCoA axes. To do this, we will use the add.spec.scores function again. Then we can identify a correlation-coefficient cutoff (e.g. r = 0.70) to pull out important species. Finally, we will use the envfit() function from the vegan pacakee, to conduct a permutation test on these correlations.

```
spe.corr <- add.spec.scores(fish.pcoa, fishREL, method = "cor.scores")$cproj
corrcut <- 0.7  # user defined cutoff
imp.spp <- spe.corr[abs(spe.corr[, 1]) >= corrcut | abs(spe.corr[, 2]) >= corrcut, ]

# Permutation Test for Species Abundances Across Axes
fit <- envfit(fish.pcoa, fishREL, perm = 999)</pre>
```

Question 9: Address the following questions about the ordination results of the doubs data set:

- a. Generate a hypothesis about the grouping of sites in the Doubs River based on fish community composition.
- b. Generate a hypothesis about which fish species are potential indicators of river quality.
- c. Do the different approaches described in the ordination section agree or disagree? Explain.

Answer 9a: Answer 9b: Answer 9c:

# 6) HYPOTHESIS TESTING

The visualization tools that we just learned about (i.e., heatmaps, cluser analysis, and ordination) are powerful for exploratory analysis and for *generating* hypotheses. In this section we introduce some methods that are better suited for *testing* hypotheses and predictions related to  $\beta$ -diversity.

# A. Multivariate Procedures for Categorical Designs

PERMANOVA stands for permutational multivariate analysis of variance (Anderson 2001). It is a multivariate analog to univariate ANOVA and has less restrictions than parametric multivariate analysis of variance (MANOVA). As the name suggests, it evaluates differences according to a specified model by randomly permuting the data. PERMANOVA can easily handle simple designs, but also accommodates nested and higher-order studies. In addition, it can deal with missing values and unbalanced designs. The PERMANOVA output is similar to the output of classic ANOVA; it includes (pseudo) F-tests, p-values, and  $R^2$  values. We will implement PERMANOVA with the adonis() function in the vegan package.

To run adonis, you first need a factor vector or matrix that specifies your treatments and replicates. This vector or matrix can either be provided in the form of a file that you open in R (e.g. read.table()) or a user-specified vector or matrix that you write within R.

Earlier work done in the Doubs River suggested that the river can be broken into four distinct regions based on fish habitat quality. The first region (sites 1-14) has been rated as being "high quality". The second (sites 15 - 19) and fourth (sites 26 - 30) regions have been rated as being "moderate quality". And the third region (sites 20 - 25) has been rated has being "low quality".

Even though the Doubs River is not a controlled experiment, let's test the hypothesis that fish community composition is affected by river quality rankings.

```
# Create "Factors"" vector
quality <- c(rep("HQ", 13), rep("MQ", 5), rep("LQ", 6), rep("MQ", 5))
# Run PERMANOVA with adonis function
adonis(fish ~ quality, method = "bray", permutations = 999)</pre>
```

Question 10: Based on the PERMANOVA results, evaluate the prediction that river quality influences fish community composition.

### Answer 10:

To determine whether any species can be used as indicators of habitat quality, we can calculate each species' Indicator Value (Dufrene and Legendre 1997), which measures the associated between a species and a site group.

```
require(indicspecies)

## Loading required package: indicspecies
indval <- multipatt(fish, cluster = quality, control = how(nperm=999))
summary(indval)</pre>
```

```
##
##
   Multilevel pattern analysis
##
##
   Association function: IndVal.g
##
##
   Significance level (alpha): 0.05
##
   Total number of species: 27
##
##
   Selected number of species: 23
##
   Number of species associated to 1 group: 1
##
   Number of species associated to 2 groups: 22
##
##
   List of species associated to each combination:
##
   Group MQ #sps. 1
```

```
##
         stat p.value
## Teso 0.686
                 0.02 *
##
##
   Group HQ+MQ #sps.
##
         stat p.value
## Satr 0.860
               0.005 **
## Phph 0.859
                0.014 *
##
##
   Group LQ+MQ #sps. 20
##
         stat p.value
## Alal 0.935
                0.001 ***
## Gogo 0.933
                0.001 ***
## Ruru 0.916
                0.001 ***
## Legi 0.901
                0.001 ***
## Baba 0.895
                0.001 ***
## Chna 0.866
                0.003 **
## Spbi 0.866
                0.001 ***
## Cyca 0.866
                0.001 ***
## Acce 0.866
                0.001 ***
## Lele 0.863
                0.004 **
## Titi 0.853
                0.010 **
## Chto 0.829
                0.002 **
## Rham 0.829
                0.003 **
## Anan 0.829
                0.002 **
## Eslu 0.827
                0.026 *
## Pefl 0.806
                0.016 *
## Blbj 0.791
                0.003 **
## Scer 0.766
                0.008 **
## Abbr 0.750
                0.006 **
                0.028 *
## Icme 0.661
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Although none of our species is a good indicator of high quality habitat, many are strong indicators of low-to-middle quality habitat. If you observe a community with Alal, Gogo, or Ruru species, the community is likely not of the highest quality.

To test for species preferences, we can calculate Pearson's phi coefficient of association (fidelity).

```
fish.pa <- decostand(fish, method = "total")
phi <- multipatt(fish.pa, cluster = quality, func = "r.g", control = how(nperm=999))
summary(phi)</pre>
```

```
##
##
   Multilevel pattern analysis
##
   _____
##
##
   Association function: r.g
   Significance level (alpha): 0.05
##
##
##
   Total number of species: 27
   Selected number of species: 18
##
   Number of species associated to 1 group: 9
   Number of species associated to 2 groups: 9
##
##
   List of species associated to each combination:
```

```
##
##
   Group HQ #sps. 3
##
         stat p.value
## Phph 0.802
                0.001 ***
  Neba 0.734
                0.001 ***
  Satr 0.650
                0.001 ***
##
##
   Group LQ #sps.
##
         stat p.value
                0.001 ***
## Alal 0.693
  Ruru 0.473
                0.043 *
##
##
   Group MQ
              #sps.
##
         stat p.value
## Anan 0.571
                0.007 **
  Spbi 0.557
                0.004 **
  Chto 0.542
                0.008 **
##
  Icme 0.475
                0.029 *
##
##
   Group LQ+MQ #sps.
##
         stat p.value
## Legi 0.658
                0.004 **
## Baba 0.645
                0.003 **
## Rham 0.600
                0.004 **
## Acce 0.594
                0.006 **
## Cyca 0.586
                0.009 **
## Chna 0.571
                0.005 **
## Blbj 0.571
                0.013 *
## Gogo 0.523
                0.011 *
                0.028 *
## Abbr 0.499
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

From this analysis, we can see that Phph, Neba, and Satr species strongly prefer high quality habitats, while Alal tends to be more often found in low quality habitats.

## B. Mutivariate Procedures for Continuous Designs

### i. Mantel Test

A Mantel test is essentially a multivariate correlation analysis. It produces an r value that is analogous to the Pearson's correlation coefficient. In addition, it produces a p-value that is derived from the deviation of observed correlation to that of correlations derived from randomizations of the two matrices.

In the following section, we will perform a Mantel test using the mantel() function in vegan. This requires that we first have two distance matrices to compare. Here, we will compare the Bray-Curtis distance matrix we created earlier with a new distance matrix of environmental factors (doubs\$env). After creating the distance matrices, we will test the hypothesis that fish assemblages are correlated with stream environmental variables.

```
# Define Matrices
fish.dist <- vegdist(doubs$fish[-8, ], method = "bray")
env.dist <- vegdist(scale(doubs$env[-8,]),method = "euclid")</pre>
```

```
#Mantel Test
mantel(fish.dist,env.dist)
```

**Question 11**: What do the results from our Mantel test suggest about fish diversity and stream environmental conditions? How might this relate to your hypothesis about stream quality influencing fish communities?

Answer 11:

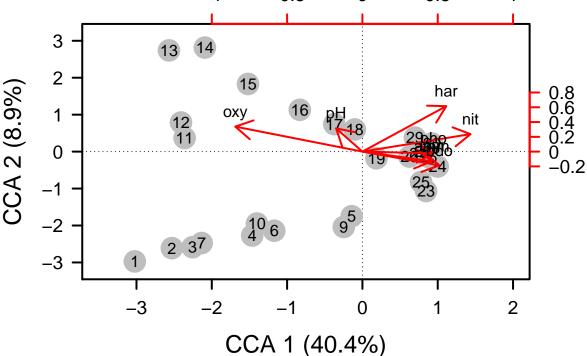
### ii. Constrained Ordination

Another way we can test hypotheses with continuous data is to use **constrained ordination**, which is sometimes referred to as canonical ordination. Constrained ordination explores the relationships between two matrices: an **explanatory matrix** and a **response matrix**. Canonical correspondence analysis (CCA) and redundancy analysis (RDA) are two types of constrained ordination. These techniques are based on the linear model framework and thus can be used to formally test hypotheses. Constrained ordination works by first conducting multivariate multiple linear regression followed either by correspondence analysis (CA) with CCA or Principal Components Analysis (PCA) with RDA, while using the matrix of fitted values to obtain a constrained ordination. A permutation test can then be used to test for overall significance.

Here, we will use environmental data to conduct a CCA on the fish assemblages of the Doubs River. We will start by creating an explanatory matrix that contains water chemistry data. We will then use the cca() function from the vegan package. Note, we have to specify that we want the cca function in the vegan package because there are cca functions in both vegan and ade4! We will then use permutation tests to evaluate the significance of our model. Finally, we will test the influence of each environmental variable on the constrained axes.

```
# Define Environmental Matrix
env.chem <- as.matrix(doubs$env[-8 , 5:11])</pre>
# Conduct CCA
doubs.cca <- vegan::cca(fish ~ env.chem)</pre>
# Permutation Tests
anova(doubs.cca, by = "axis")
cca.fit <- envfit(doubs.cca, env.chem, perm = 999)</pre>
cca.fit
# Calculate Explained Variation
cca.explainvar1 <- round(doubs.cca$CCA$eig[1] /</pre>
                          sum(c(doubs.cca$CCA$eig, doubs.cca$CA$eig)), 3) * 100
cca.explainvar2 <- round(doubs.cca$CCA$eig[2] /</pre>
                          sum(c(doubs.cca$CCA$eig, doubs.cca$CA$eig)), 3) * 100
# Define Plot Parameters
par(mar = c(5, 5, 4, 4) + 0.1)
# Initiate Plot
plot(scores(doubs.cca, display = "wa"), xlim = c(-3.5, 2), ylim = c(-3.2, 3.2),
     xlab = paste("CCA 1 (", cca.explainvar1, "%)", sep = ""),
     ylab = paste("CCA 2 (", cca.explainvar2, "%)", sep = ""),
     pch = 16, cex = 2.0, type = "n", cex.lab = 1.5, cex.axis = 1.2, axes = FALSE)
# Add Axes
axis(side = 1, labels = T, lwd.ticks = 2, cex.axis = 1.2, las = 1)
axis(side = 2, labels = T, lwd.ticks = 2, cex.axis = 1.2, las = 1)
```

```
abline(h = 0, v = 0, lty = 3)
box(lwd = 2)
# Add Points & Labels
points(scores(doubs.cca, display = "wa"),
       pch = 19, cex = 3, bg = "gray", col = "gray")
text(scores(doubs.cca, display = "wa"),
     labels = row.names(scores(doubs.cca, display = "wa")))
# Add Environmental Vectors
vectors <- scores(doubs.cca, display = "bp")</pre>
row.names(vectors) <- c("pH", "har", "pho", "nit", "amm", "oxy", "bdo")</pre>
arrows(0, 0, vectors[,1] * 2, vectors[, 2] * 2,
       lwd = 2, lty = 1, length = 0.2, col = "red")
text(vectors[,1] * 2, vectors[, 2] * 2, pos = 3,
     labels = row.names(vectors))
axis(side = 3, lwd.ticks=2, cex.axis=1.2, las = 1, col = "red", lwd = 2.2,
     at = pretty(range(vectors[, 1])) * 2, labels = pretty(range(vectors[, 1])))
axis(side = 4, lwd.ticks=2, cex.axis=1.2, las = 1, col = "red", lwd = 2.2,
     at = pretty(range(vectors[, 2])) * 2, labels = pretty(range(vectors[, 2])))
                                       -0.5
                                                              0.5
       3
       2
                                                               har
```



Question 12: Based on the CCA, what are the environmental variables that seem to be contributing to stream water quality for fish assemblages?

Answer 12:

### iii. Variation Partitioning

As seen in the site-by-species matrix, fish species abundances vary across sites. From the above analyses, we have shown that spatial variation in fish community structure in the Doubs River can be explained by

(1) a qualitative description of site habitat quality (PERMANOVA), with certain fish preferring particular habitats over over (Phi Coefficient of Fidelity); (2) environmental dissimilarity between sites, tested via pairwise correlations between elements of two distance matrices (Mantel tests); and (3) variation in individual environmental variables measured across sites (constrained ordination). However, the environmental variables we have identified as important drivers of community structure also vary across space. A major question in the study of  $\beta$ -diversity is whether variation in community structure is more strongly driven by changes in underlying environmental variables (after controlling for spatial variation in those variables), by changes in spatial position alone (after controlling for environmental variation), by spatially structured environmental variation, or by other factors. A common approach to answering these types of question is variation partitioning, which determines the amount of variation in a response variable that can be explained by two or more explanatory matrices, jointly and independently. For more detailed explanation of the application of variation partition in ecology, see Borcard et al. (1992), Legendre et al. (2005), and Peres-Neto et al. (2006).

First, we will perform Principal Coordinates of Neighbor Matrices (Borcard and Legendre 2002), a special form of distance based Moran's Eigenvector Maps (Dray et al. 2006). This approach decomposes spatial variation into different sine waves to model broad scale (long wavelengths) to fine scale (short wavelengths) spatial structures.

```
rs <- rowSums(fish)/sum(fish)
doubs.pcnmw <- pcnm(dist(doubs$xy[-8,]), w = rs, dist.ret = T)</pre>
doubs.pcnmw$values < 0 # Only the positive eigenvalues are meaningful
    [1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [12] FALSE FALSE FALSE FALSE FALSE TRUE TRUE
```

TRUE TRUE

This analysis returns many eigenvalues, but some of them are redundant. So we will perform model selection (forwards and backwards) to determine which eigenvalues create the most informative model with the fewest parameters (Blanchet et al. 2008).

```
doubs.space <- as.data.frame(scores(doubs.pcnmw))</pre>
doubs.pcnm.mod0 <- dbrda(fish.db ~ 1, doubs.space)</pre>
doubs.pcnm.mod1 <- dbrda(fish.db ~ ., doubs.space)</pre>
step.pcnm <- ordiR2step(doubs.pcnm.mod0, doubs.pcnm.mod1, perm.max = 200)</pre>
```

The object step.pcnm now contains the selected model. We can now construct a spatial model using only the selected PCNM axes.

# step.pcnm\$anova

TRUE TRUE TRUE TRUE

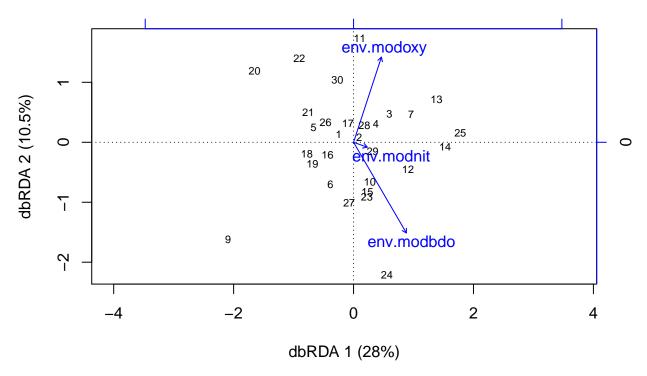
```
##
                    R2.adj Df
                                          F Pr(>F)
                                 AIC
## + PCNM2
                   0.23537
                            1 49.574 9.6190
                                            0.002 **
## + PCNM3
                   0.34293
                           1 46.083 5.4196
                                             0.002 **
## + PCNM5
                   0.40760
                           1 43.941 3.8385
                                             0.004 **
## + PCNM1
                   0.47215
                            1 41.411 4.0570
                                             0.008 **
## + PCNM13
                   0.52124
                            1 39.346 3.4612
                                             0.016 *
## + PCNM16
                            1 36.480 4.0192
                   0.57680
                                             0.012 *
## + PCNM6
                   0.60431
                           1 35.182 2.5296
                                            0.050 *
## <All variables> 0.62601
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Our new model uses a subset of the PCNM axes and has an R2 of 0.63.
space.mod <- model.matrix(~ PCNM2 + PCNM3 + PCNM5 + PCNM1 + PCNM13 + PCNM16 + PCNM6, doubs.space)[,-1]
```

Now, let's repeat the model selection for the environmental dataset.

```
doubs.env.mod0 <- dbrda(fish.db ~ 1, as.data.frame(env.chem))</pre>
doubs.env.mod1 <- dbrda(fish.db ~ ., as.data.frame(env.chem))</pre>
step.env <- ordiR2step(doubs.env.mod0, doubs.env.mod1, perm.max = 200)</pre>
## Step: R2.adj= 0
## Call: fish.db ~ 1
##
##
                   R2.adjusted
## <All variables> 0.53032584
## + oxy
                    0.27727176
## + nit
                    0.25755208
## + bdo
                    0.17477787
## + pho
                    0.14568614
## + har
                    0.14174915
## + amm
                    0.14142804
## <none>
                    0.00000000
## + pH
                   -0.01827054
##
##
        Df
               AIC
                        F Pr(>F)
## + oxy 1 47.939 11.742 0.002 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Step: R2.adj= 0.2772718
## Call: fish.db ~ oxy
##
##
                   R2.adjusted
## <All variables>
                     0.5303258
## + bdo
                     0.4009000
## + amm
                     0.3474192
## + pho
                     0.3452702
                     0.3331357
## + har
## + nit
                     0.3316120
## <none>
                     0.2772718
## + pH
                     0.2586983
                     0.000000
## - oxy
##
##
               AIC
                        F Pr(>F)
        Df
## + bdo 1 43.404 6.5716 0.002 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Step: R2.adj = 0.4009
## Call: fish.db ~ oxy + bdo
##
##
                   R2.adjusted
## <All variables>
                     0.5303258
## + nit
                     0.4980793
## + har
                     0.4695121
## <none>
                     0.4009000
                     0.3938042
## + pho
## + amm
                     0.3869134
## + pH
                     0.3865240
## - bdo
                     0.2772718
```

```
## - oxy
                     0.1747779
##
##
         Df
               AIC
                       F Pr(>F)
## + nit 1 39.134 6.034 0.004 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Step: R2.adj = 0.4980793
## Call: fish.db ~ oxy + bdo + nit
##
##
                   R2.adjusted
                     0.5415705
## + amm
## <All variables>
                     0.5303258
## + pho
                     0.5277128
## + har
                     0.5218852
## <none>
                     0.4980793
## + pH
                     0.4843267
## - nit
                     0.4009000
## - oxy
                     0.3420426
## - bdo
                     0.3316120
step.env$anova
                    R2.adj Df
                                            F Pr(>F)
##
                                  AIC
## + oxy
                   0.27727 1 47.939 11.7421 0.002 **
                   0.40090 1 43.404 6.5716 0.002 **
## + bdo
## + nit
                   0.49808 1 39.134 6.0340 0.004 **
## <All variables> 0.53033
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Our new environmental model contains oxy, bdo, and nit; with R2 of 0.53
env.mod <- model.matrix(~ oxy + bdo + nit, as.data.frame(env.chem))[,-1]</pre>
Now we wish to determine the independent and joint explanatory power of the environmental and spatial
datasets using variation partitioning.
# First, we perform partial canonical ordination controlling for spatial and environmental datasets
doubs.pure.env <- dbrda(fish.db ~ env.mod + Condition(space.mod))</pre>
doubs.pure.space <- dbrda(fish.db ~ space.mod + Condition(env.mod))</pre>
doubs.total.env <- dbrda(fish.db ~ env.mod)</pre>
doubs.total.space <- dbrda(fish.db ~ space.mod)</pre>
We test for significance of the dbRDA fractions.
permutest(doubs.pure.env, permutations = 999)
##
## Permutation test for dbrda
##
## Permutation: free
## Number of permutations: 999
## Call: dbrda(formula = fish.db ~ env.mod + Condition(space.mod))
## Permutation test for all constrained eigenvalues
## Pseudo-F:
                 4.423025 (with 3, 18 Degrees of Freedom)
## Significance:
                     0.001
```

```
permutest(doubs.pure.space, permutations = 999)
## Permutation test for dbrda
##
## Permutation: free
## Number of permutations: 999
## Call: dbrda(formula = fish.db ~ space.mod + Condition(env.mod))
## Permutation test for all constrained eigenvalues
## Pseudo-F:
                 4.174109 (with 7, 18 Degrees of Freedom)
## Significance:
                     0.001
permutest(doubs.total.env, permutations = 999)
## Permutation test for dbrda
##
## Permutation: free
## Number of permutations: 999
## Call: dbrda(formula = fish.db ~ env.mod)
## Permutation test for all constrained eigenvalues
## Pseudo-F:
                 10.2619 (with 3, 25 Degrees of Freedom)
## Significance:
                     0.001
permutest(doubs.total.space, permutations = 999)
## Permutation test for dbrda
## Permutation: free
## Number of permutations: 999
## Call: dbrda(formula = fish.db ~ space.mod)
## Permutation test for all constrained eigenvalues
## Pseudo-F:
                 7.108896 (with 7, 21 Degrees of Freedom)
## Significance:
                     0.001
Just like we did before with CCA, we can visualize each of these partial constrained ordinations.
dbrda.explainvar1 <- round(doubs.pure.env$CCA$eig[1] /</pre>
                              sum(c(doubs.pure.env$CCA$eig, doubs.pure.env$CA$eig)), 3) * 100
dbrda.explainvar2 <- round(doubs.pure.env$CCA$eig[2] /</pre>
                              sum(c(doubs.pure.env$CCA$eig, doubs.pure.env$CA$eig)), 3) * 100
plot(doubs.pure.env,
     xlab = paste("dbRDA 1 (",dbrda.explainvar1,"%)",sep=""),
     ylab = paste("dbRDA 2 (",dbrda.explainvar2,"%)",sep=""))
```



We can see that ofter controlling for space, we still have a high amount of variation explained by environmental variables in our model.

```
doubs.varpart <- varpart(fish.db, env.mod, space.mod)
par(mar = c(2,2,2,2))
plot(doubs.varpart)
text(1, 0.25, "Space")
text(0, 0.25, "Env")</pre>
```

