

# embedded Quantum ESPRESSO

Michele Pavanello  
@MikPavanello

Department of Chemistry  
Rutgers, the State University of New Jersey  
Newark, NJ

#QE2018

# A glance at Pavanello Research Group @ Rutgers

# A glance at Pavanello Research Group @ Rutgers



*PRG @ Rutgers-Newark since 2012*

# A glance at Pavanello Research Group @ Rutgers



PRG accepting PhD students!

PRG @ Ru

# A glance at Pavanello Research Group @ Rutgers



PRG @ Ru

PRG accepting PhD students!

- Work alongside
  - 3 postdocs
  - 2 PhD students

# A glance at Pavanello Research Group @ Rutgers



PRG @ Ru

PRG accepting PhD students!

- Work alongside
  - 3 postdocs
  - 2 PhD students
- Work on
  - New ways to use TDDFT for molecule–surface interactions
  - Nonadiabatic dynamics based on Constrained DFT
  - Orbital-free DFT ...

# A glance at Pavanello Research Group @ Rutgers



PRG @ Ru

PRG accepting PhD students!

- Work alongside
  - 3 postdocs
  - 2 PhD students
- Work on
  - New ways to use TDDFT for molecule–surface interactions
  - Nonadiabatic dynamics based on Constrained DFT
  - Orbital-free DFT ...that actually works

# Some theoretical aspects of embedding

## Outline

# Some theoretical aspects of embedding

## Outline

- Nature is made of interacting subsystems

# Some theoretical aspects of embedding

## Outline

- Nature is made of interacting subsystems
- Multiscale models of ground electronic states
  - Materials modeling: Periodic Subsystem DFT
    - embedded Quantum-ESPRESSO (eQE)
    - Dynamics of liquid, solvated and layered systems
  - Details of the eQE algorithm
  - Details of the eQE parallelization
- One example of excited states calculation

Krishtal, A.; Sinha, D.; Genova, A. & Pavanello, M.

*Subsystem Density-Functional Theory as an Effective Tool for Modeling Ground and Excited States, their Dynamics, and Many-Body Interactions*

J. Phys.: Condens. Matter, **27**, 183202 (2015)

# Introduction to subsystem DFT (FDE)

# Introduction to subsystem DFT (FDE)

- Split the system into (smaller) interacting subsystems

# Introduction to subsystem DFT (FDE)

- Split the system into (smaller) interacting subsystems
- Partition of the total electron density into subsystem contributions

$$\rho(\mathbf{r}) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r}) \quad \rho_I(\mathbf{r}) = \sum_i^{\infty} n_i^I |\phi_{(i)_I}(\mathbf{r})|^2$$

# Introduction to subsystem DFT (FDE)

- Split the system into (smaller) interacting subsystems
- Partition of the total electron density into subsystem contributions

$$\rho(\mathbf{r}) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r}) \quad \rho_I(\mathbf{r}) = \sum_i^{\infty} n_i^I |\phi_{(i)_I}(\mathbf{r})|^2$$

- The energy functional is almost additive:  $E[\rho] \simeq E[\rho_I] + E[\rho_{II}]$

Senatore 1986, Cortona 1991, Wesolowski 1993; Jacob, Neugebauer, Carter, ...

# Introduction to subsystem DFT (FDE)

- Split the system into (smaller) interacting subsystems
- Partition of the total electron density into subsystem contributions

$$\rho(\mathbf{r}) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r}) \quad \rho_I(\mathbf{r}) = \sum_i^{\infty} n_i^I |\phi_{(i)_I}(\mathbf{r})|^2$$

- The energy functional is almost additive:  $E[\rho] \simeq E[\rho_I] + E[\rho_{II}]$

$$E_{\text{FDE}}[\rho] = E[\rho_I] + E[\rho_{II}] + T_s^{\text{nadd}}[\rho_I, \rho_{II}] + E_{xc}^{\text{nadd}}[\rho_I, \rho_{II}] + V_{\text{Coul}}^{\text{nadd}}[\rho_I, \rho_{II}]$$

Senatore 1986, Cortona 1991, Wesolowski 1993; Jacob, Neugebauer, Carter, ...

# Introduction to subsystem DFT (FDE)

- Split the system into (smaller) interacting subsystems
- Partition of the total electron density into subsystem contributions

$$\rho(\mathbf{r}) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r}) \quad \rho_I(\mathbf{r}) = \sum_i^{\infty} n_i^I |\phi_{(i)_I}(\mathbf{r})|^2$$

- The energy functional is almost additive:  $E[\rho] \simeq E[\rho_I] + E[\rho_{II}]$

$$E_{\text{FDE}}[\rho] = E[\rho_I] + E[\rho_{II}] + T_s^{\text{nadd}}[\rho_I, \rho_{II}] + E_{xc}^{\text{nadd}}[\rho_I, \rho_{II}] + V_{\text{Coul}}^{\text{nadd}}[\rho_I, \rho_{II}]$$

$$F^{\text{nadd}}[\rho_I, \rho_{II}] = F[\rho] - F[\rho_I] - F[\rho_{II}]$$

Senatore 1986, Cortona 1991, Wesolowski 1993; Jacob, Neugebauer, Carter, ...

# Introduction to subsystem DFT (FDE)

- Split the system into (smaller) interacting subsystems
- Partition of the total electron density into subsystem contributions

$$\rho(\mathbf{r}) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r}) \quad \rho_I(\mathbf{r}) = \sum_i^{\infty} n_i^I |\phi_{(i)_I}(\mathbf{r})|^2$$

- The energy functional is almost additive:  $E[\rho] \simeq E[\rho_I] + E[\rho_{II}]$

$$E_{\text{FDE}}[\rho] = E[\rho_I] + E[\rho_{II}] + T_s^{\text{nadd}}[\rho_I, \rho_{II}] + E_{xc}^{\text{nadd}}[\rho_I, \rho_{II}] + V_{\text{Coul}}^{\text{nadd}}[\rho_I, \rho_{II}]$$

$$F^{\text{nadd}}[\rho_I, \rho_{II}] = F[\rho] - F[\rho_I] - F[\rho_{II}]$$

- **Frozen Density Embedding (FDE):** Coupled Kohn–Sham equations for each subsystem

$$\frac{\delta E_{\text{FDE}}[\rho_I + \rho_{II}]}{\delta \rho_I} = 0 \rightarrow \left[ -\frac{1}{2} \nabla^2 + v_{KS}^I(\mathbf{r}) + v_{emb}^I(\mathbf{r}) \right] \phi_{(i)_I}(\mathbf{r}) = \varepsilon_i^I \phi_{(i)_I}(\mathbf{r})$$

Senatore 1986, Cortona 1991, Wesolowski 1993; Jacob, Neugebauer, Carter, ...

# Orbital-free DFT interaction between subsystems

# Orbital-free DFT interaction between subsystems

The nonadditive functional for two subsystems

$$F^{\text{nadd}}[\rho_I, \rho_{II}] = F[\rho] - F[\rho_I] - F[\rho_{II}]$$

considering that  $\rho(r) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r})$ .

# Orbital-free DFT interaction between subsystems

The nonadditive functional for two subsystems

$$F^{\text{nadd}}[\rho_I, \rho_{II}] = F[\rho] - F[\rho_I] - F[\rho_{II}]$$

considering that  $\rho(r) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r})$ .

Homework :)

- Compute  $T_s^{\text{nadd}}[\rho_I, \rho_{II}]$  in the Thomas-Fermi approximation,  
 $T_s[\rho] = C_{TF} \int \rho^{5/3}(\mathbf{r}) d\mathbf{r}$
- Compute  $E_x^{\text{nadd}}[\rho_I, \rho_{II}]$  in the Dirac approximation,  $E_x[\rho] = C_x \int \rho^{4/3}(\mathbf{r}) d\mathbf{r}$
- Compute  $E_H^{\text{nadd}}[\rho_I, \rho_{II}]$ ,  $E_H[\rho] = \frac{1}{2} \int \int \rho(\mathbf{r}) \frac{\rho(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} d\mathbf{r} d\mathbf{r}'$

# Orbital-free DFT interaction between subsystems

The nonadditive functional for two subsystems

$$F^{\text{nadd}}[\rho_I, \rho_{II}] = F[\rho] - F[\rho_I] - F[\rho_{II}]$$

considering that  $\rho(r) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r})$ .

Homework :)

- Compute  $T_s^{\text{nadd}}[\rho_I, \rho_{II}]$  in the Thomas-Fermi approximation,  
 $T_s[\rho] = C_{TF} \int \rho^{5/3}(\mathbf{r}) d\mathbf{r}$
- Compute  $E_x^{\text{nadd}}[\rho_I, \rho_{II}]$  in the Dirac approximation,  $E_x[\rho] = C_x \int \rho^{4/3}(\mathbf{r}) d\mathbf{r}$
- Compute  $E_H^{\text{nadd}}[\rho_I, \rho_{II}]$ ,  $E_H[\rho] = \frac{1}{2} \int \int \rho(\mathbf{r}) \frac{\rho(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} d\mathbf{r} d\mathbf{r}'$

The embedding potential is given by  $\frac{\delta E^{\text{nadd}}}{\delta \rho_I(\mathbf{r})}$ .

# Orbital-free DFT interaction between subsystems

The nonadditive functional for two subsystems

$$F^{\text{nadd}}[\rho_I, \rho_{II}] = F[\rho] - F[\rho_I] - F[\rho_{II}]$$

considering that  $\rho(r) = \rho_I(\mathbf{r}) + \rho_{II}(\mathbf{r})$ .

Homework :)

- Compute  $T_s^{\text{nadd}}[\rho_I, \rho_{II}]$  in the Thomas-Fermi approximation,  
 $T_s[\rho] = C_{TF} \int \rho^{5/3}(\mathbf{r}) d\mathbf{r}$
- Compute  $E_x^{\text{nadd}}[\rho_I, \rho_{II}]$  in the Dirac approximation,  $E_x[\rho] = C_x \int \rho^{4/3}(\mathbf{r}) d\mathbf{r}$
- Compute  $E_H^{\text{nadd}}[\rho_I, \rho_{II}]$ ,  $E_H[\rho] = \frac{1}{2} \int \int \rho(\mathbf{r}) \frac{\rho(\mathbf{r}')}{|\mathbf{r}-\mathbf{r}'|} d\mathbf{r} d\mathbf{r}'$

The embedding potential is given by  $\frac{\delta E^{\text{nadd}}}{\delta \rho_I(\mathbf{r})}$ .

... more homework!

- $T_s$  contribution to  $v_{emb}(\mathbf{r})$
- $E_x$  contribution to  $v_{emb}(\mathbf{r})$
- $E_H$  contribution to  $v_{emb}(\mathbf{r})$

# Other types of embedding

# Other types of embedding

## Density-based embedding

## Density-based embedding

- Density Functional Embedding Theory [Carter]  
*via KS inversion*

## Density-based embedding

- Density Functional Embedding Theory [Carter]  
*via KS inversion*
- Partition DFT [Wasserman]  
*via KS inversion*

## Density-based embedding

- Density Functional Embedding Theory [Carter]  
*via KS inversion*
- Partition DFT [Wasserman]  
*via KS inversion*
- Potential Functional Embedding Theory [Carter]  
*via OEP / KS inversion*

# Other types of embedding

## Density-based embedding

- Density Functional Embedding Theory [Carter]  
*via KS inversion*
- Partition DFT [Wasserman]  
*via KS inversion*
- Potential Functional Embedding Theory [Carter]  
*via OEP / KS inversion*

## Wavefunction, density matrix, and others

# Other types of embedding

## Density-based embedding

- Density Functional Embedding Theory [Carter]  
*via KS inversion*
- Partition DFT [Wasserman]  
*via KS inversion*
- Potential Functional Embedding Theory [Carter]  
*via OEP / KS inversion*

## Wavefunction, density matrix, and others

- WFT densities in DFT densities [Carter, Wesolowski, Neugebauer]  
 $\rho_I(\mathbf{r}) = \langle \Psi_I | \hat{\rho}(\mathbf{r}) | \Psi_I \rangle$

# Other types of embedding

## Density-based embedding

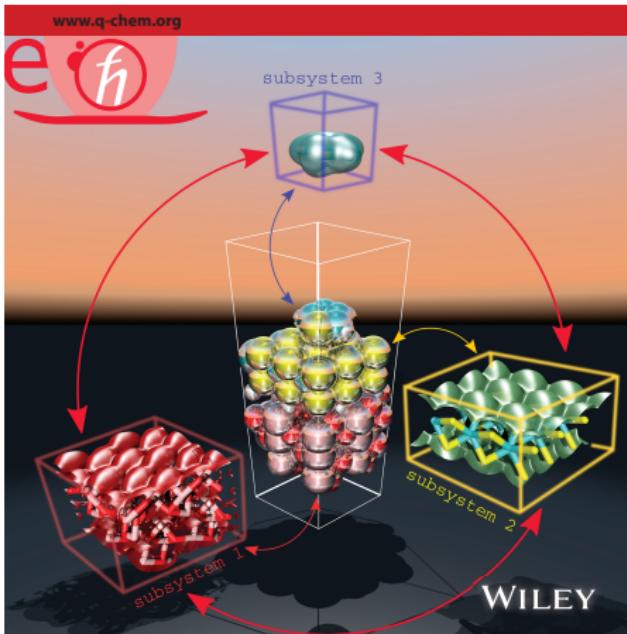
- Density Functional Embedding Theory [Carter]  
*via KS inversion*
- Partition DFT [Wasserman]  
*via KS inversion*
- Potential Functional Embedding Theory [Carter]  
*via OEP / KS inversion*

## Wavefunction, density matrix, and others

- WFT densities in DFT densities [Carter, Wesolowski, Neugebauer]  
 $\rho_I(\mathbf{r}) = \langle \Psi_I | \hat{\rho}(\mathbf{r}) | \Psi_I \rangle$
- WFT density matrices in DFT density matrices [Manby, Miller, Goodpaster]  
 $\gamma_I(\mathbf{r}, \mathbf{r}') = \langle \Psi_I^{HF} | \hat{\gamma}(\mathbf{r}, \mathbf{r}') | \Psi_I^{HF} \rangle$



# International Journal of QUANTUM CHEMISTRY



*eQE: An open-source density functional embedding theory code for the condensed phase*  
International Journal of Quantum Chemistry, **117**, e25401 (2017)



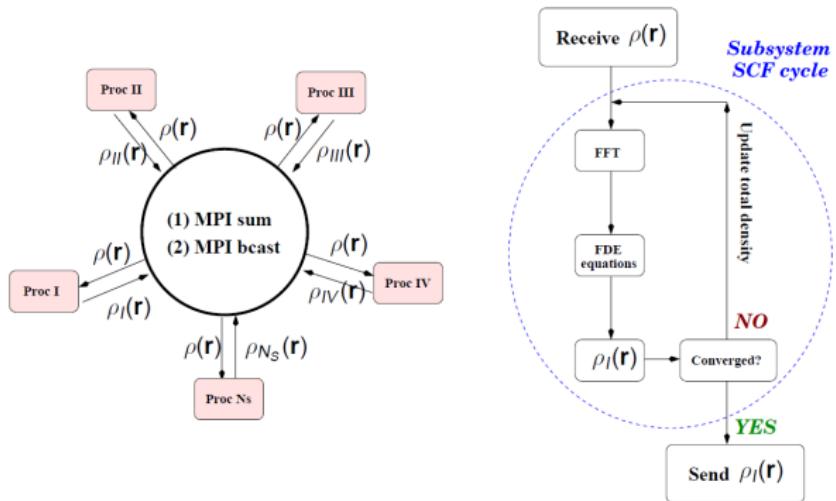


[eqe.rutgers.edu](http://eqe.rutgers.edu)

# eQE — embedded Quantum ESPRESSO

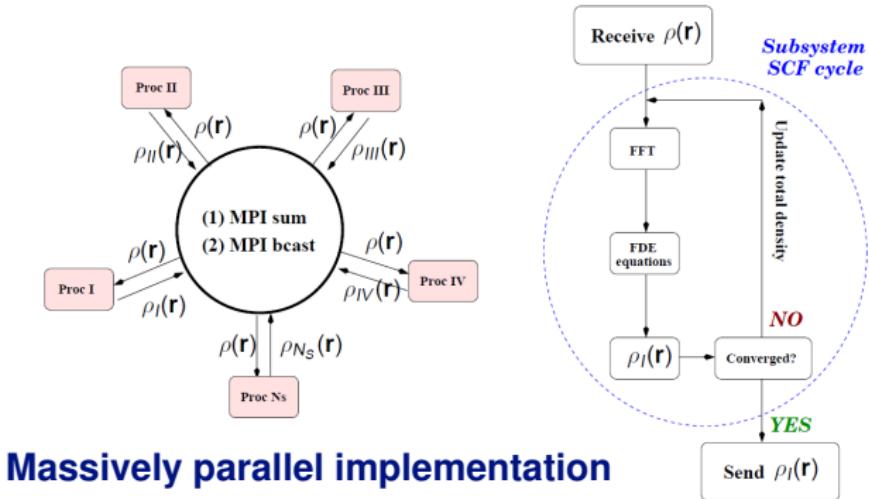


eqe.rutgers.edu



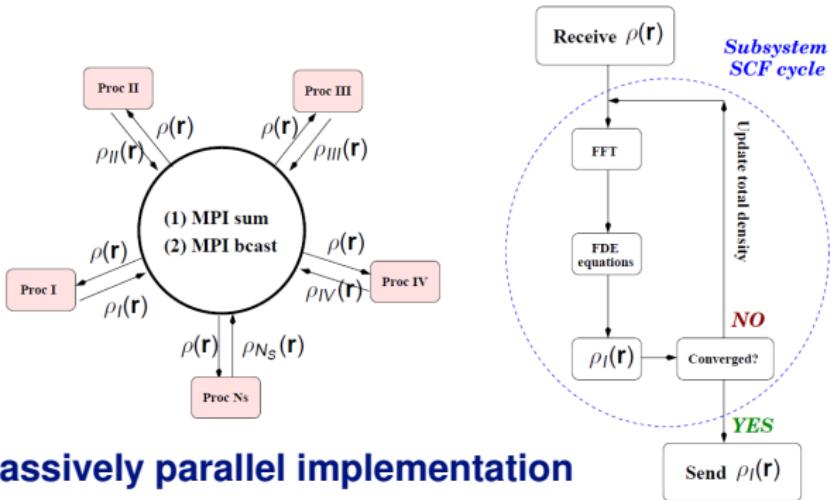


eqe.rutgers.edu





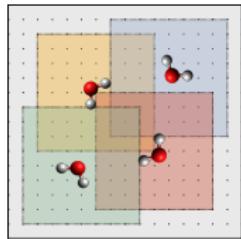
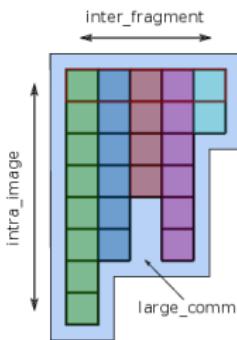
[eQE.rutgers.edu](http://eQE.rutgers.edu)



## Massively parallel implementation

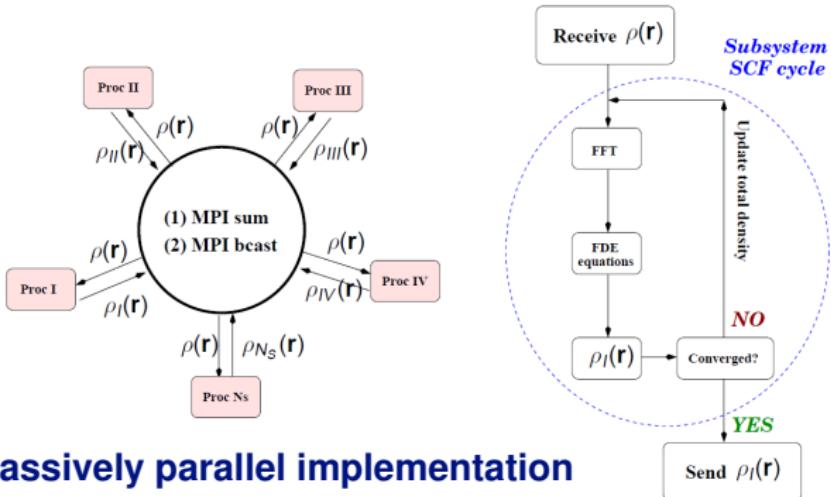
### Rewrite the MPI module of QE

- Subsystem-specific # of CPUs
- Improved latencies (processes wait for others to complete)
- Nested DIIS for  $\{\rho_I(\mathbf{r})\}$





eqe.rutgers.edu



## Rewrite the MPI module of QE

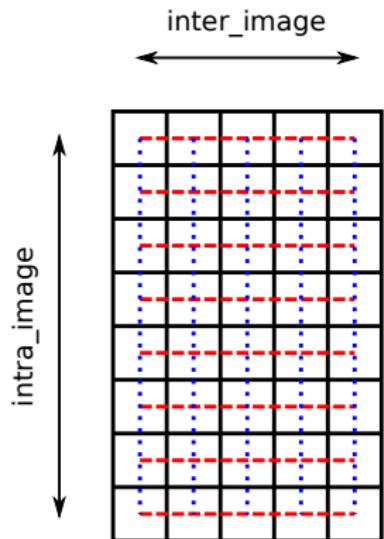
- Subsystem-specific # of CPUs
- Improved latencies (processes wait for others to complete)
- Nested DIIS for  $\{\rho_I(\mathbf{r})\}$

## BZ sampling ( $k$ -points)

- $K$ -point sampling for (semi)conductors.
- $\Gamma$ -point for molecules/insulators.

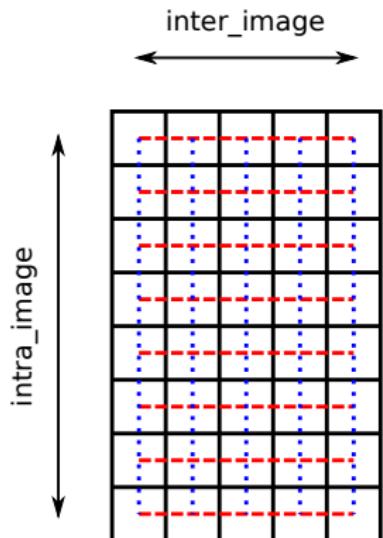
# eQE: a note on parallelization

## Regular QE

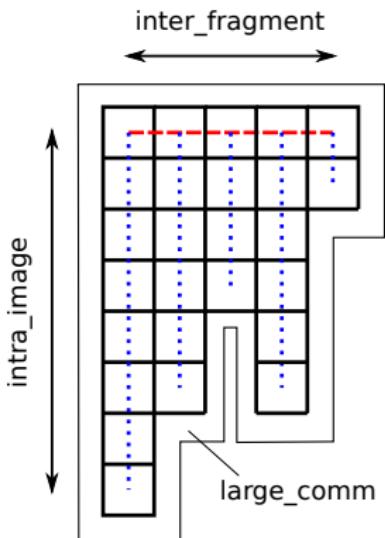


# eQE: a note on parallelization

## Regular QE

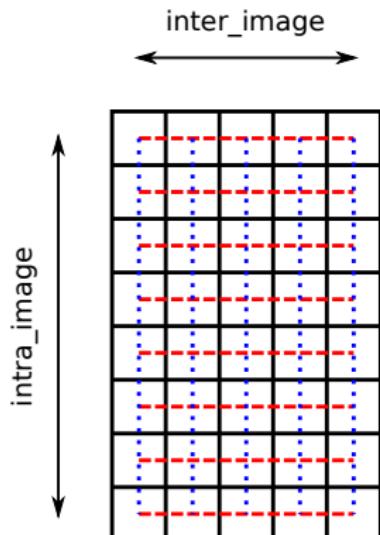


## eQE

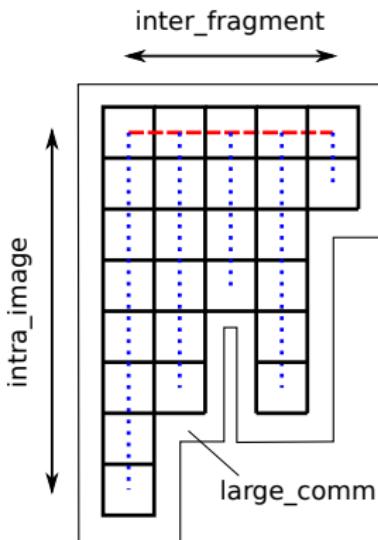


# eQE: a note on parallelization

## Regular QE



## eQE

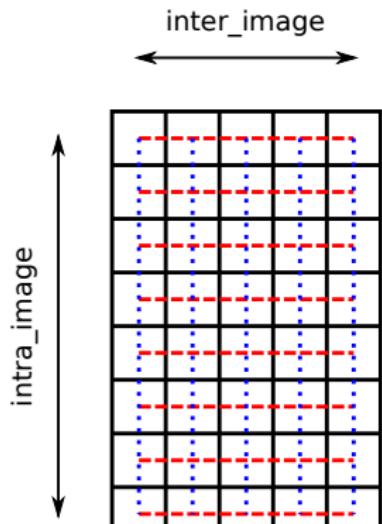


### pros & cons

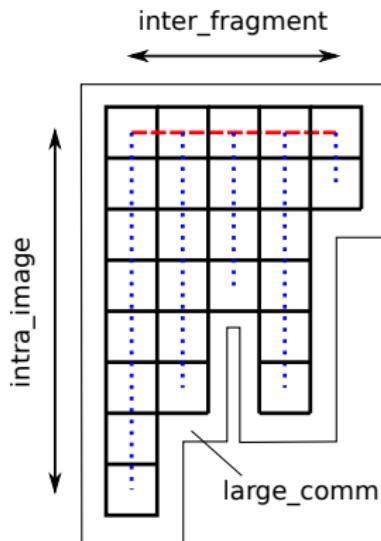
- distributed data communication
- non-polymorphic

# eQE: a note on parallelization

## Regular QE



## eQE



### pros & cons

- distributed data communication
- non-polymorphic

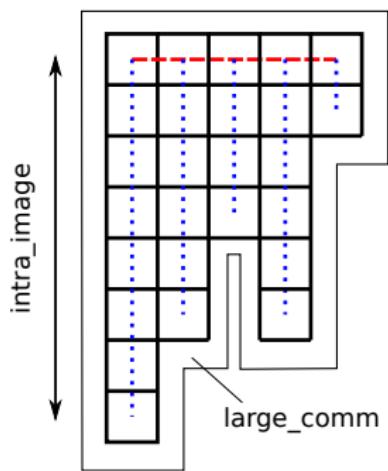
### pros & cons

- polymorphic
- gathered data communication

# eQE: a note on coding it

eQE

inter\_fragment



```
! dfftp          :: the fft descriptor of the subsystem electron cell
! diffpt         :: the fft descriptor of the supersystem simulation cell
! rho%of_r(dfftp%nnr)   :: the subsystem density in the subsystem cell
! (grid is distributed over the processes in intra_image_comm)
! rho_fde%of_r(dfftp%nnr) :: the supersystem density in the subsystem cell
! (grid is distributed over the processes in intra_image_comm)
! rho_fde_large%of_r(dfftl%nnr) :: the supersystem density in the supersystem cell
! (grid is distributed over the processes in large_comm)
! %of_g(:)        :: same quantity in reciprocal space
! aux(dfftp%nnr)  :: auxiliary vector of the subsystem cell real space
! (grid is distributed over the processes in intra_image_comm)
! gaux(ngm)       :: auxiliary vector of the subsystem cell reciprocal space
! raux(nr1*nr2*nr3) :: subsystem cell real space auxiliary vector
! auxl(dfftl%nnr) :: auxiliary vector of the supersystem cell real space
! (whole grid is collected on the ionode proc of intra_image_comm)
! gauxl(ngml)     :: auxiliary vector of the supersystem cell reciprocal space
! rauxl(nr1*nr2l*nr3l) :: supersystem (large) cell real space gathered auxiliary vector
! (whole grid is collected on the ionode proc of large_comm)
! f2l(nr1*nr2*nr3) :: subsystem cell to supersystem cell mapping vector.
```

```
call grid_gather(rho_fde%of_r(:,is), raux)
```

```
if (ionode) then
```

```
    rauxl = 0.d0
    rauxl(f2l(:)) = raux(:)
```

```
call mp_sum(rauxl, inter_fragment_comm)
```

```
raux = 0.d0
raux(:) = rauxl(f2l(:))
```

```
endif
```

```
call grid_scatter_large(raux, rho_fde_large%of_r(:,is))
call grid_scatter(raux, rho_fde%of_r(:,is))
```

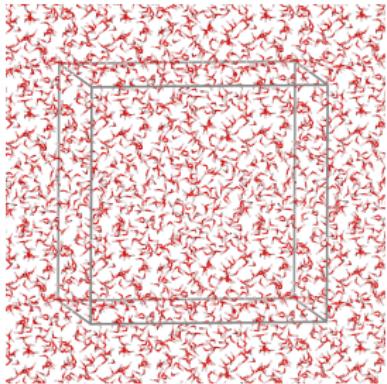
```
gauxl(:) = cmplx(rho_fde_large%of_r(:,is), 0.d0, kind=dp)
call fwfft ('Custom', gauxl, dfftl)
rho_fde_large%of_g(1:ngml,is) = gauxl(nll(1:ngml))
```

```
gaux(:) = cmplx(rho_fde%of_r(:,is), 0.d0, kind=dp)
call fwfft ('Dense', gaux, dfftp)
```

# eQE: Performance for molecular periodic systems

# eQE: Performance for molecular periodic systems

Water 1024



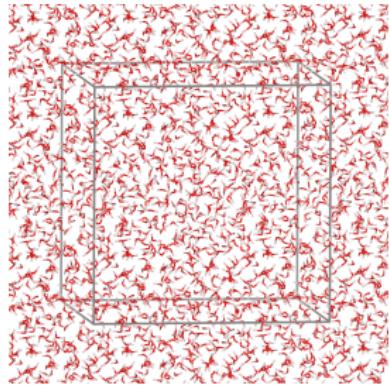
$30726 \text{ \AA}^3$

**Speedup compared to regular QE (all PBE)**

**24.5 ×**

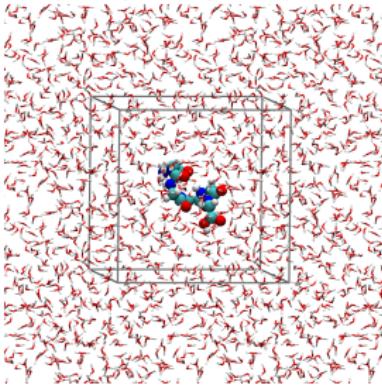
# eQE: Performance for molecular periodic systems

Water 1024



$30726 \text{ \AA}^3$

(GLY)<sub>6</sub> in (H<sub>2</sub>O)<sub>395</sub>



$12656 \text{ \AA}^3$

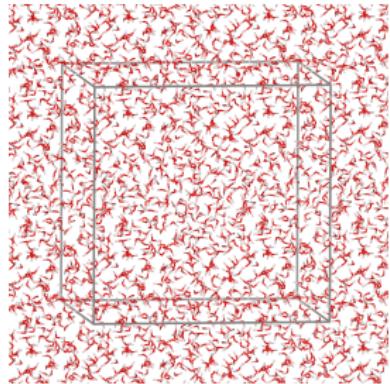
**Speedup compared to regular QE (all PBE)**

**24.5 ×**

**36.5 ×**

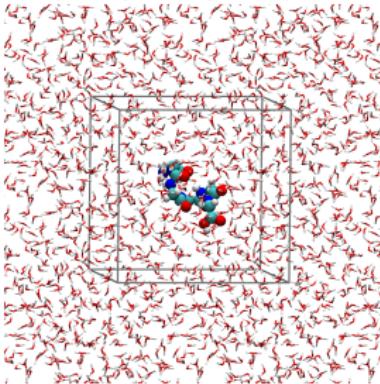
# eQE: Performance for molecular periodic systems

Water 1024



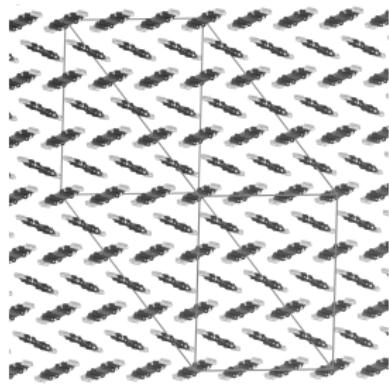
$30726 \text{ \AA}^3$

(GLY)<sub>6</sub> in (H<sub>2</sub>O)<sub>395</sub>



$12656 \text{ \AA}^3$

Pentacene  $3 \times 3 \times 3$



$18243 \text{ \AA}^3$

**Speedup compared to regular QE (all PBE)**

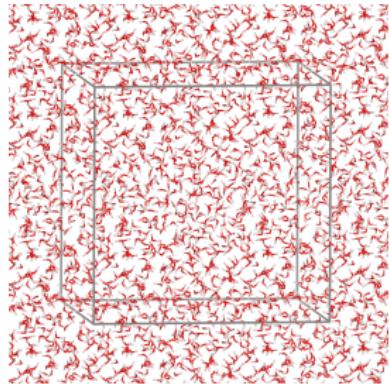
**24.5 ×**

**36.5 ×**

**12.5 ×**

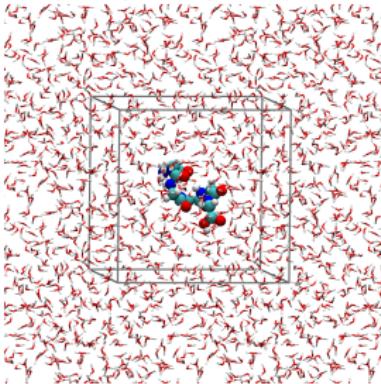
# eQE: Performance for molecular periodic systems

Water 1024



30726 Å<sup>3</sup>

(GLY)<sub>6</sub> in (H<sub>2</sub>O)<sub>395</sub>



12656 Å<sup>3</sup>

Pentacene 3 × 3 × 3



18243 Å<sup>3</sup>

**Speedup compared to regular QE (all PBE)**

**24.5 ×**

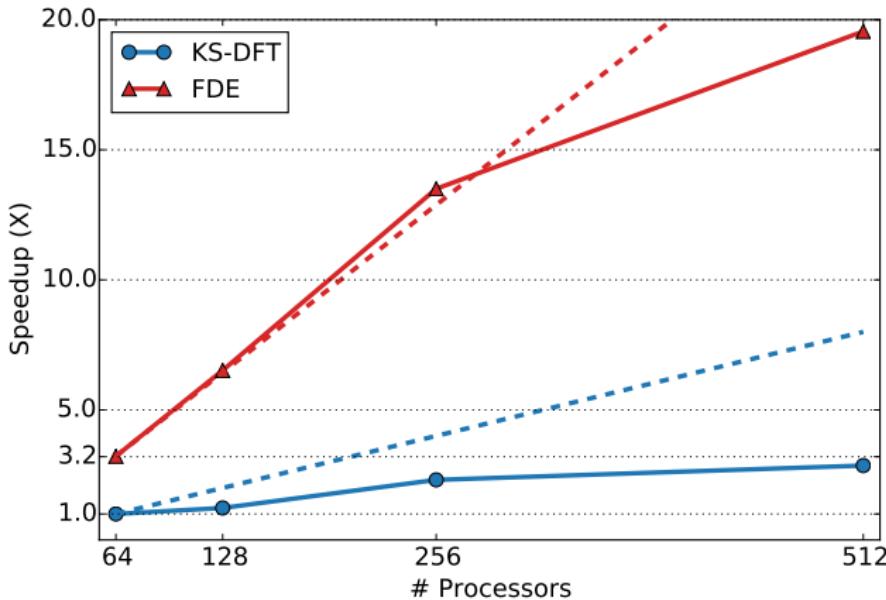
**36.5 ×**

**12.5 ×**

**Well over one order of magnitude speedup!**

# eQE vs QE: Parallel scaling for water 256

Water 256, 256 subsystems

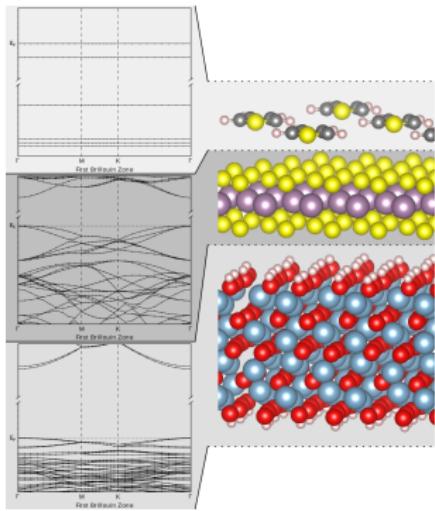


**QE–eQE gap widens with increasing # of CPUs**

# eQE: Computational savings for truly periodic systems

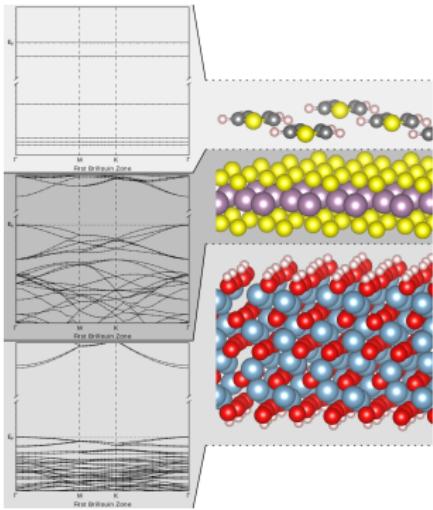
# eQE: Computational savings for truly periodic systems

System relevant for catalysis:



# eQE: Computational savings for truly periodic systems

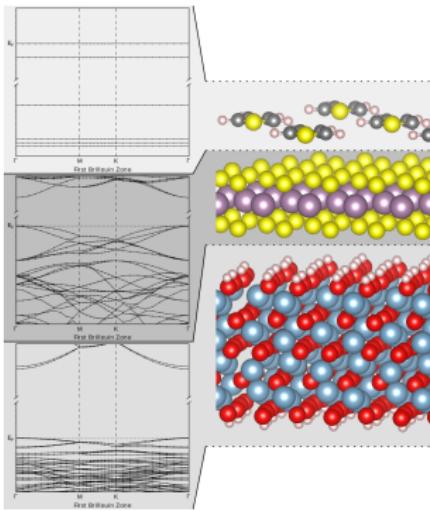
System relevant for catalysis:



How low can we go with  $k$ -points?

# eQE: Computational savings for truly periodic systems

System relevant for catalysis:

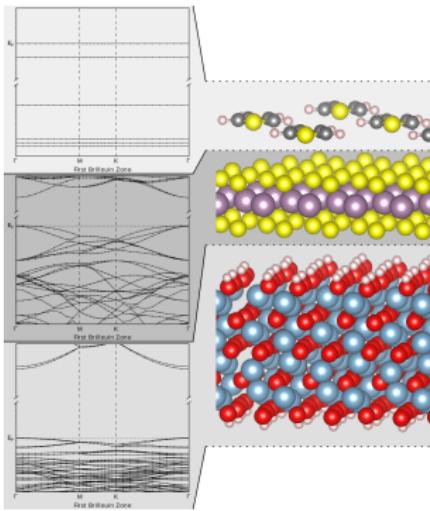


How low can we go with  $k$ -points?

		<Δp> (e <sup>-</sup> )			
		8x8	3.9 x 10 <sup>-3</sup>	3.2 x 10 <sup>-3</sup>	3.0 x 10 <sup>-3</sup>
MoS <sub>2</sub> k mesh	4x4	6.4 x 10 <sup>-2</sup>	3.9 x 10 <sup>-3</sup>	3.2 x 10 <sup>-3</sup>	3.1 x 10 <sup>-3</sup>
	2x2	7.5 x 10 <sup>-2</sup>	1.5 x 10 <sup>-2</sup>	1.4 x 10 <sup>-2</sup>	1.4 x 10 <sup>-2</sup>
	1x1	4.9 x 10 <sup>-1</sup>	4.3 x 10 <sup>-1</sup>	4.3 x 10 <sup>-1</sup>	4.3 x 10 <sup>-1</sup>
	Al <sub>2</sub> O <sub>3</sub> k mesh	1x1	2x2	4x4	8x8

# eQE: Computational savings for truly periodic systems

System relevant for catalysis:



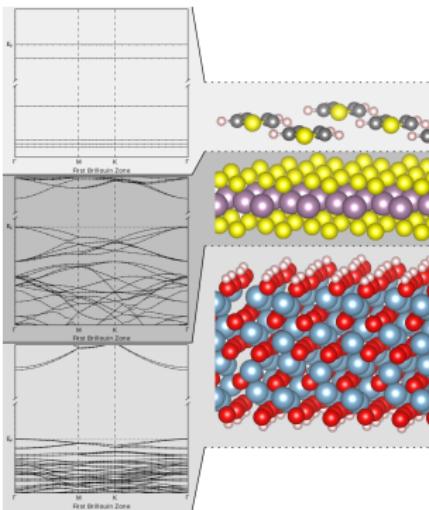
How low can we go with  $k$ -points?

		$\langle \Delta p \rangle (\text{e}^-)$				
		8x8	$3.9 \times 10^{-3}$	$3.2 \times 10^{-3}$	$3.0 \times 10^{-3}$	
MoS <sub>2</sub> k mesh	4x4	$6.4 \times 10^{-2}$	$3.9 \times 10^{-3}$	$3.2 \times 10^{-3}$	$3.1 \times 10^{-3}$	
	2x2	$7.5 \times 10^{-2}$	$1.5 \times 10^{-2}$	$1.4 \times 10^{-2}$	$1.4 \times 10^{-2}$	
	1x1	$4.9 \times 10^{-1}$	$4.3 \times 10^{-1}$	$4.3 \times 10^{-1}$	$4.3 \times 10^{-1}$	
		Al <sub>2</sub> O <sub>3</sub> k mesh	1x1	2x2	4x4	8x8

The MoS<sub>2</sub> layer must be well sampled!

# eQE: Computational savings for truly periodic systems

System relevant for catalysis:



How low can we go with  $k$ -points?

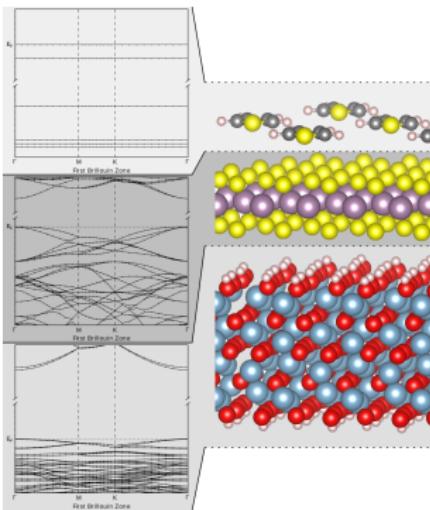
		$\langle \Delta p \rangle (\text{e}^-)$			
		8x8	$3.9 \times 10^{-3}$	$3.2 \times 10^{-3}$	$3.0 \times 10^{-3}$
MoS <sub>2</sub> k mesh	4x4	$6.4 \times 10^{-2}$	$3.9 \times 10^{-3}$	$3.2 \times 10^{-3}$	$3.1 \times 10^{-3}$
	2x2	$7.5 \times 10^{-2}$	$1.5 \times 10^{-2}$	$1.4 \times 10^{-2}$	$1.4 \times 10^{-2}$
	1x1	$4.9 \times 10^{-1}$	$4.3 \times 10^{-1}$	$4.3 \times 10^{-1}$	$4.3 \times 10^{-1}$
	Al <sub>2</sub> O <sub>3</sub> k mesh	1x1	2x2	4x4	8x8

The MoS<sub>2</sub> layer must be well sampled!

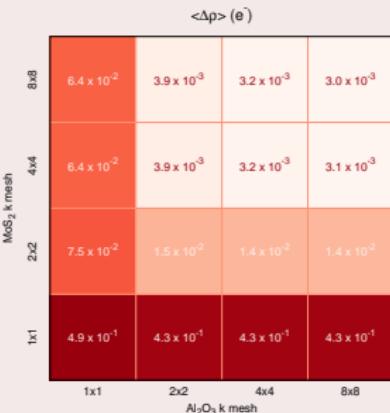
Computational complexity [Genova & Pavanello JPCM (2015)]

# eQE: Computational savings for truly periodic systems

System relevant for catalysis:



How low can we go with  $k$ -points?



The MoS<sub>2</sub> layer must be well sampled!

Computational complexity [Genova & Pavanello JPCM (2015)]

	KS	FDE (bare)	FDE (optimized)
Speedup	1.0×	0.9×	6.2×
Time / Cycle (s)	195	220	31
# of Cycles	17	88	24

# eQE for periodic systems: does it work?

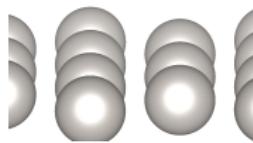
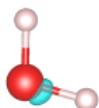
## Water on Pt(100)

---

<sup>a</sup>Genova, Ceresoli, & MP, J. Chem. Phys., **141**, 174101 (2014)

# eQE for periodic systems: does it work?

## Water on Pt(100)



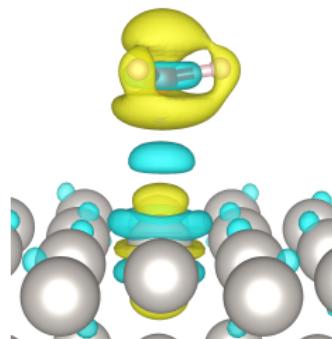
$$\langle \Delta\rho \rangle = 0.02$$
$$\Delta E_{\text{int}} = -0.2 \text{ kcal/mol}$$
$$(-0.5)$$

---

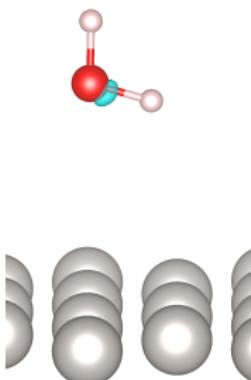
<sup>a</sup>Genova, Ceresoli, & MP, J. Chem. Phys., **141**, 174101 (2014)

# eQE for periodic systems: does it work?

## Water on Pt(100)



$$\langle \Delta\rho \rangle = 0.2$$
$$\Delta E_{\text{int}} = +0.04 \text{ kcal/mol}$$
$$(-3.2)$$

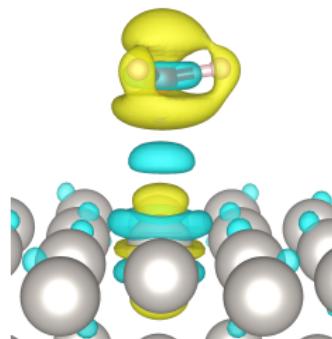


$$\langle \Delta\rho \rangle = 0.02$$
$$\Delta E_{\text{int}} = -0.2 \text{ kcal/mol}$$
$$(-0.5)$$

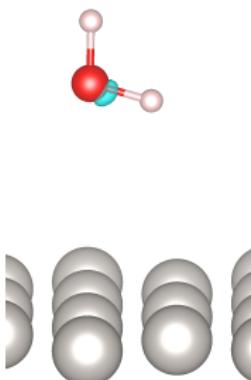
<sup>a</sup>Genova, Ceresoli, & MP, J. Chem. Phys., **141**, 174101 (2014)

# eQE for periodic systems: does it work?

## Water on Pt(100)



$$\langle \Delta\rho \rangle = 0.2$$
$$\Delta E_{\text{int}} = +0.04 \text{ kcal/mol}$$
$$(-3.2)$$

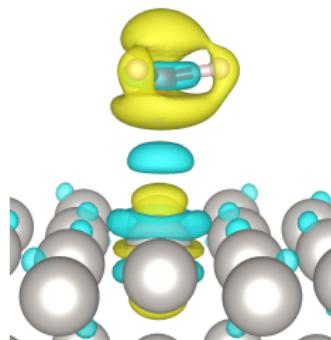


$$\langle \Delta\rho \rangle = 0.02$$
$$\Delta E_{\text{int}} = -0.2 \text{ kcal/mol}$$
$$(-0.5)$$

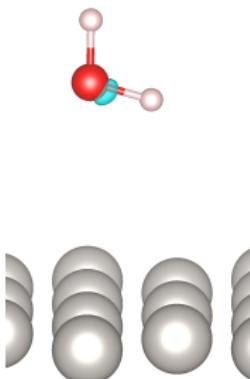
<sup>a</sup>Genova, Ceresoli, & MP, J. Chem. Phys., **141**, 174101 (2014)

# eQE for periodic systems: does it work?

## Water on Pt(100)



$$\langle \Delta\rho \rangle = 0.2$$
$$\Delta E_{\text{int}} = +0.04 \text{ kcal/mol}$$
$$(-3.2)$$

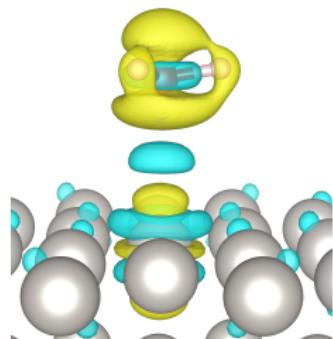


■ Weak interactions → OK

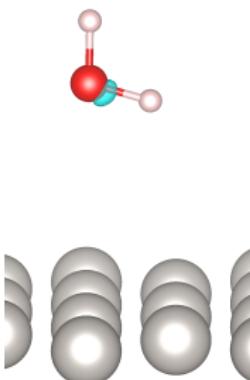
<sup>a</sup>Genova, Ceresoli, & MP, J. Chem. Phys., **141**, 174101 (2014)

# eQE for periodic systems: does it work?

## Water on Pt(100)



$$\langle \Delta\rho \rangle = 0.2$$
$$\Delta E_{\text{int}} = +0.04 \text{ kcal/mol}$$
$$(-3.2)$$



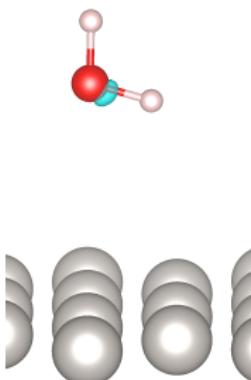
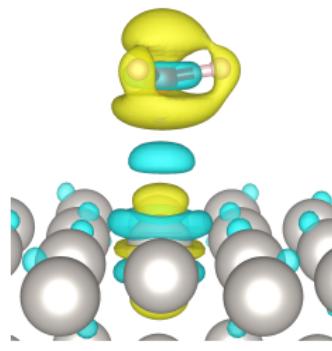
$$\langle \Delta\rho \rangle = 0.02$$
$$\Delta E_{\text{int}} = -0.2 \text{ kcal/mol}$$
$$(-0.5)$$

- Weak interactions → OK
- Covalent bonds → Not OK

<sup>a</sup>Genova, Ceresoli, & MP, J. Chem. Phys., **141**, 174101 (2014)

# eQE for periodic systems: does it work?

## Water on Pt(100)



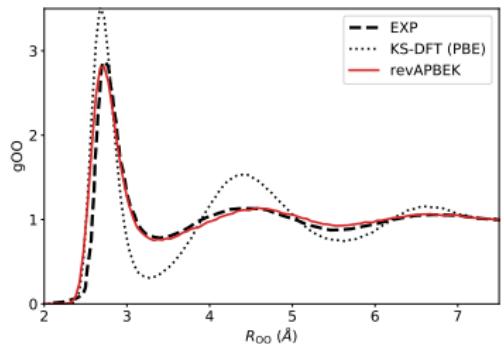
- Weak interactions → OK
- Covalent bonds → Not OK
- ... not until more accurate  $T_s[\rho]$  functionals are developed

<sup>a</sup>Genova, Ceresoli, & MP, J. Chem. Phys., **141**, 174101 (2014)

# Liquid Water – does eQE get the structure right?

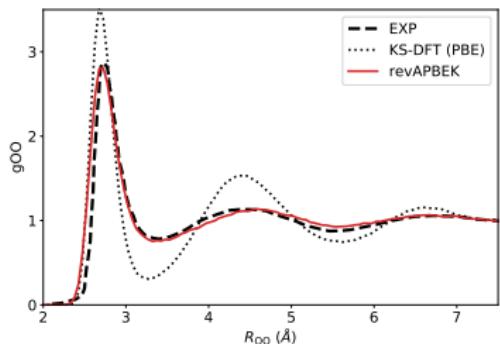
# Liquid Water – does eQE get the structure right?

## Oxygen–Oxygen RDF

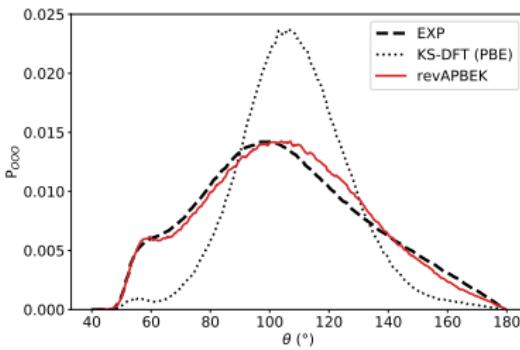


# Liquid Water – does eQE get the structure right?

Oxygen–Oxygen RDF

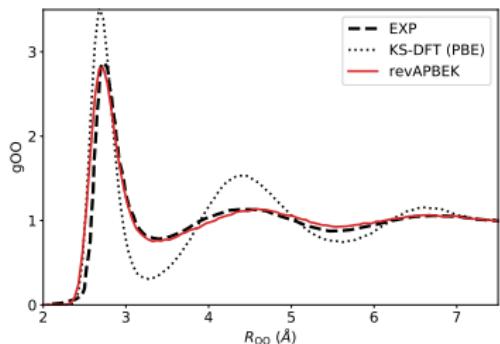


O–O–O ADF

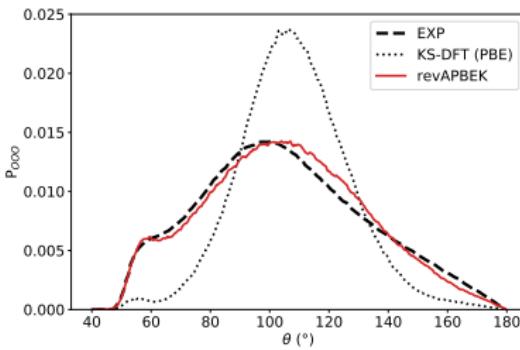


# Liquid Water – does eQE get the structure right?

## Oxygen–Oxygen RDF



## O–O–O ADF

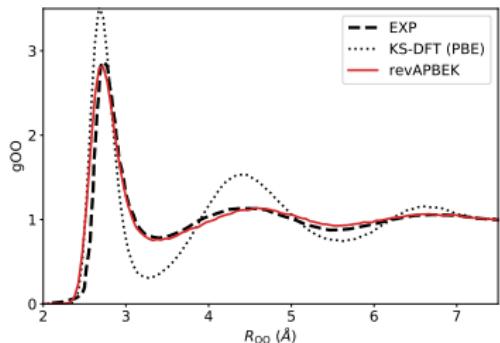


## Diffusion coefficient and dipole moment

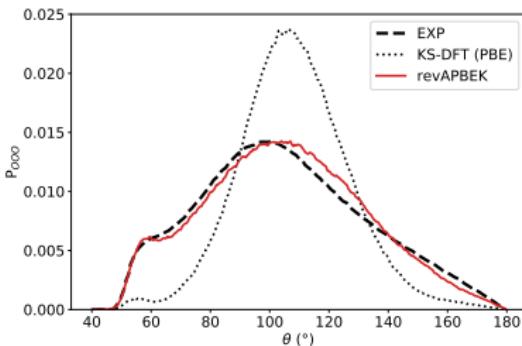
$$\begin{aligned}\langle D \rangle &= 2.97(0.4) \cdot 10^{-5} \text{ cm}^2 \text{s}^{-1} \\ \langle \mu \rangle &= 2.8(0.2)D\end{aligned}$$

# Liquid Water – does eQE get the structure right?

Oxygen–Oxygen RDF



O–O–O ADF



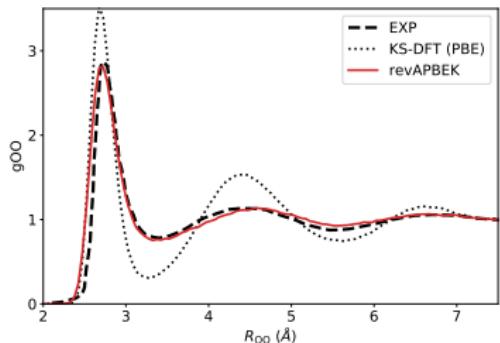
Diffusion coefficient and dipole moment

$$\begin{aligned}\langle D \rangle &= 2.97(0.4) \cdot 10^{-5} \text{ cm}^2 \text{s}^{-1} \\ \langle \mu \rangle &= 2.8(0.2)D\end{aligned}$$

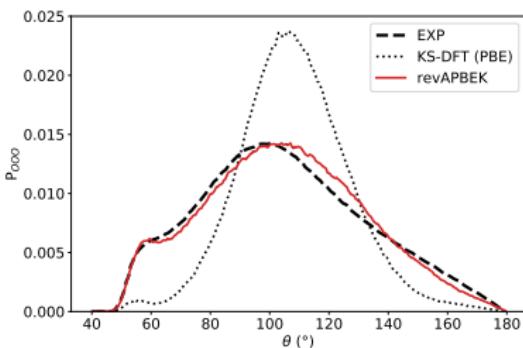
- eQE recovers correct structure
- eQE recovers correct dynamics
- eQE recovers correct  $e^-$  structure

# Liquid Water – does eQE get the structure right?

Oxygen–Oxygen RDF



O–O–O ADF



## Diffusion coefficient and dipole moment

$$\begin{aligned}\langle D \rangle &= 2.97(0.4) \cdot 10^{-5} \text{ cm}^2 \text{s}^{-1} \\ \langle \mu \rangle &= 2.8(0.2)D\end{aligned}$$

- eQE recovers correct structure
- eQE recovers correct dynamics
- eQE recovers correct  $e^-$  structure
- **How about  $e^-$  excited states?**

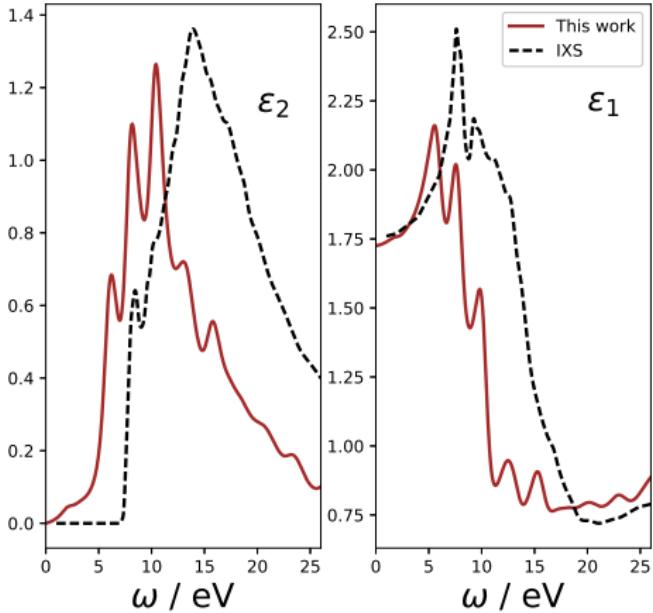
# Optical Properties of Liquid Water: $\epsilon_1$ & $\epsilon_2$

## Computation of $\epsilon$

# Optical Properties of Liquid Water: $\epsilon_1$ & $\epsilon_2$

## Computation of $\epsilon$

- 10 snapshots of water 64
- Average of 640 spectra

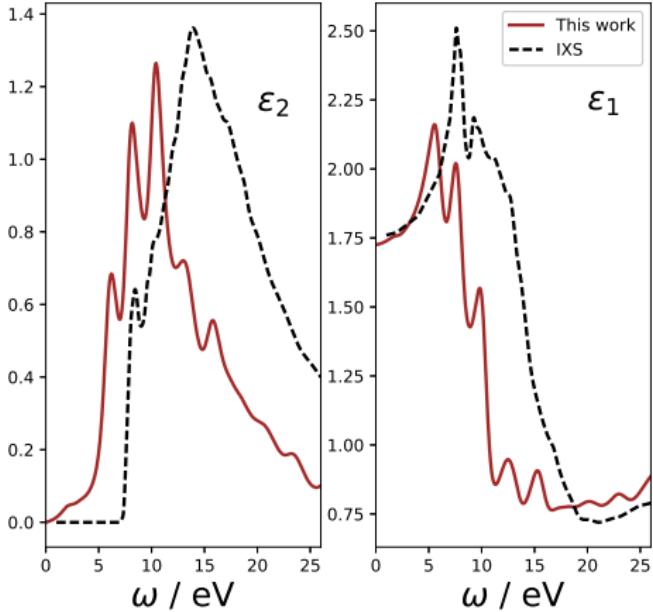


Kumar P, S. & Genova, A. & MP, J. Phys. Chem. Lett., 8 (20), pp 5077-5083 (2017)

# Optical Properties of Liquid Water: $\epsilon_1$ & $\epsilon_2$

## Computation of $\epsilon$

- 10 snapshots of water 64
- Average of 640 spectra
- Match experimental sum-rule in 0-25 eV window



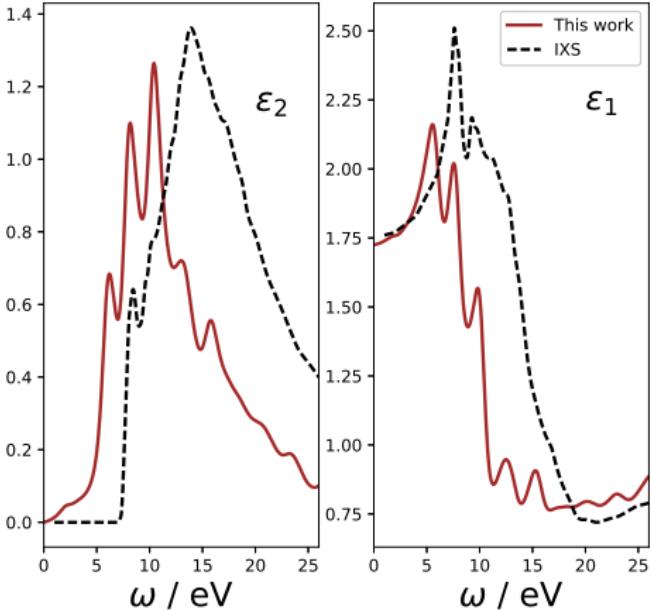
Kumar P, S. & Genova, A. & MP, J. Phys. Chem. Lett., 8 (20), pp 5077-5083 (2017)

# Optical Properties of Liquid Water: $\epsilon_1$ & $\epsilon_2$

## Computation of $\epsilon$

- 10 snapshots of water 64
- Average of 640 spectra
- Match experimental sum-rule in 0-25 eV window

We find...



Kumar P. S. & Genova, A. & MP, J. Phys. Chem. Lett., 8 (20), pp 5077-5083 (2017)

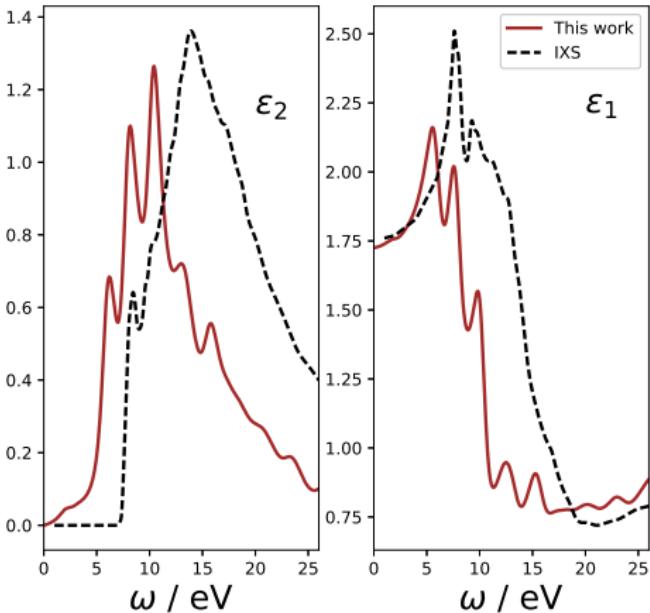
# Optical Properties of Liquid Water: $\epsilon_1$ & $\epsilon_2$

## Computation of $\epsilon$

- 10 snapshots of water 64
- Average of 640 spectra
- Match experimental sum-rule in 0-25 eV window

We find...

- Overall good agreement across wide window of  $\omega$



Kumar P. S. & Genova, A. & MP, J. Phys. Chem. Lett., 8 (20), pp 5077-5083 (2017)

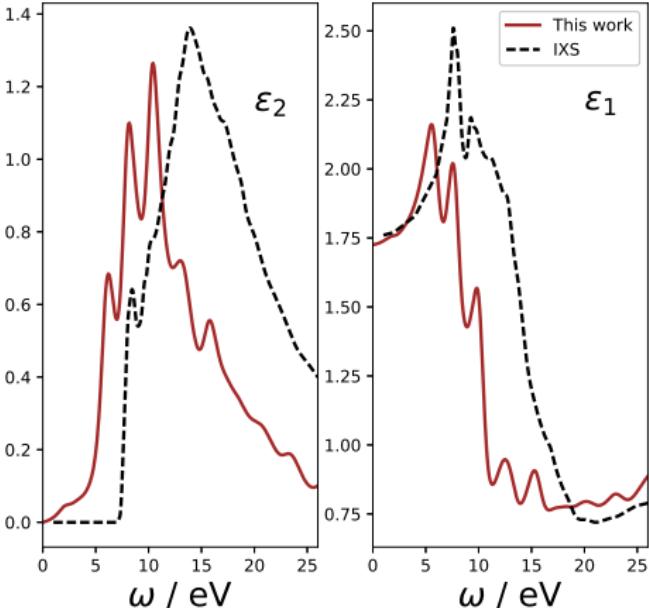
# Optical Properties of Liquid Water: $\epsilon_1$ & $\epsilon_2$

## Computation of $\epsilon$

- 10 snapshots of water 64
- Average of 640 spectra
- Match experimental sum-rule in 0-25 eV window

## We find...

- Overall good agreement across wide window of  $\omega$
- KS Exciton binding energy
  - $\rightarrow$  KS gap  $\sim 7.0$  eV
  - $\rightarrow$  Optical gap  $\sim 6.4$  eV



Kumar P, S. & Genova, A. & MP, J. Phys. Chem. Lett., 8 (20), pp 5077-5083 (2017)

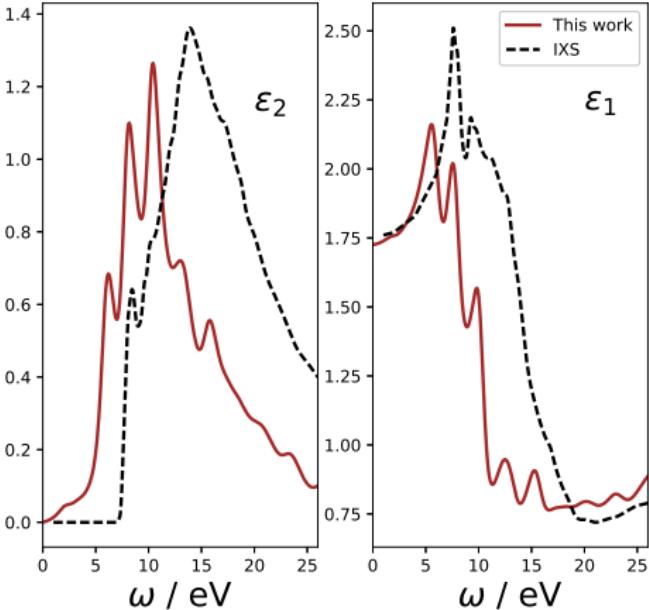
# Optical Properties of Liquid Water: $\epsilon_1$ & $\epsilon_2$

## Computation of $\epsilon$

- 10 snapshots of water 64
- Average of 640 spectra
- Match experimental sum-rule in 0-25 eV window

We find...

- Overall good agreement across wide window of  $\omega$
- KS Exciton binding energy
  - $\rightarrow$  KS gap  $\sim 7.0$  eV
  - $\rightarrow$  Optical gap  $\sim 6.4$  eV
- Index of refraction  $n = 1.68$



Kumar P., S. & Genova, A. & MP, J. Phys. Chem. Lett., 8 (20), pp 5077-5083 (2017)

# Acknowledgments

## Postdocs, Students & Collaborators

- Dr. Wenhui Mi
- Dr. Muhammed Acikgoz
- Pablo Ramos
- Alessandro Genova
- Rupali Chawla
- Sudheer Kumar P.
- Alina Umerbekova
- Johannes Tölle (visitor)
- Prof. Alisa Krishtal (@ NJIT)
- Dr. Debalina Sinha (@ L'Oreal)
- Dr. Davide Ceresoli (CNR)
- Prof. Oliviero Andreussi (North Texas)
- Dr. Andre Gomes (CNRS)
- Prof. Rob DiStasio (Cornell)
- Prof. Henk Eshuis (Montclair State)
- Dr. Damien Riedel (CNRS)

## Funding

- ACS PRF
- NSF (CHE, DMR, CBET)
- DOE CTC
- ELF fund – State of New Jersey
- AMSTERDAM DENSITY FUNCTIONAL