



Transport

and

Dispersion

of

Exciton-Polariton

Arkajit Mandal and David R. Reichman

Experiment: Ding Xu and Milan Dilor

Xu[†] *Mandal*[†] Baxter Cheng Lee Su Liu Reichman* Delor*

Arxiv: 2205.01176 (2022)

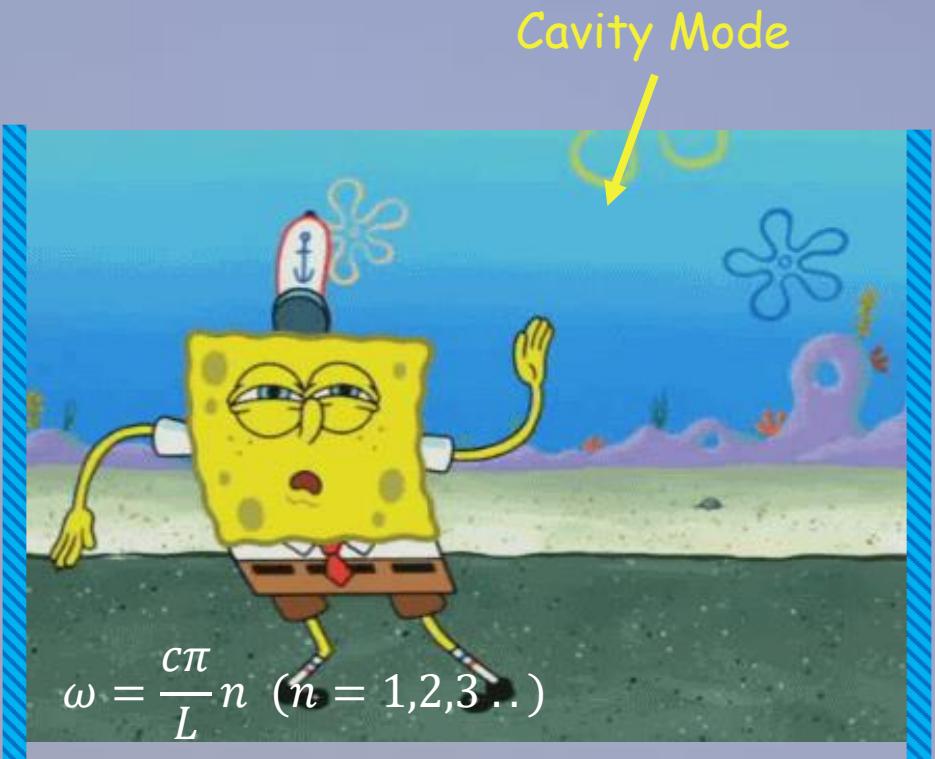
[†] Equal

*Mandal** Xu Mahajan Lee Delor Reichman*
Nano Lett. 2023

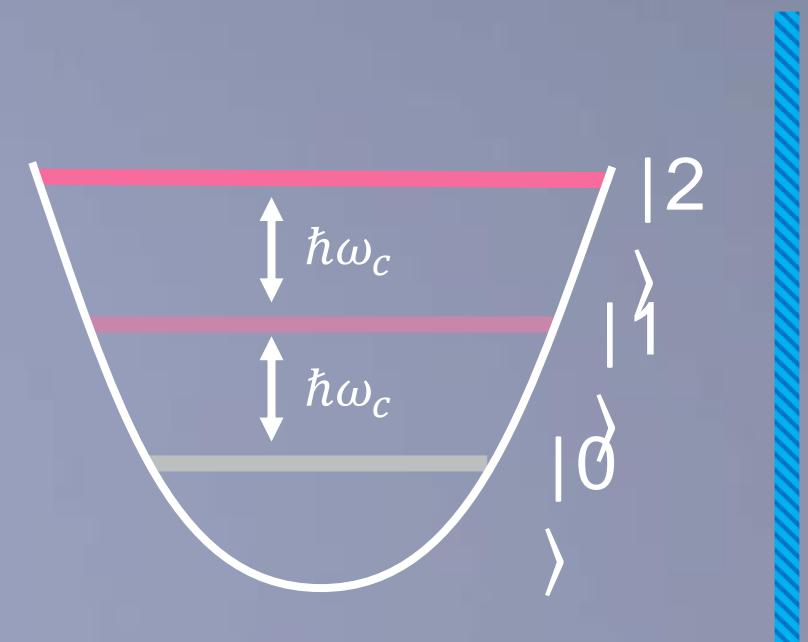


COLUMBIA UNIVERSITY
IN THE CITY OF NEW YORK

A Cavity

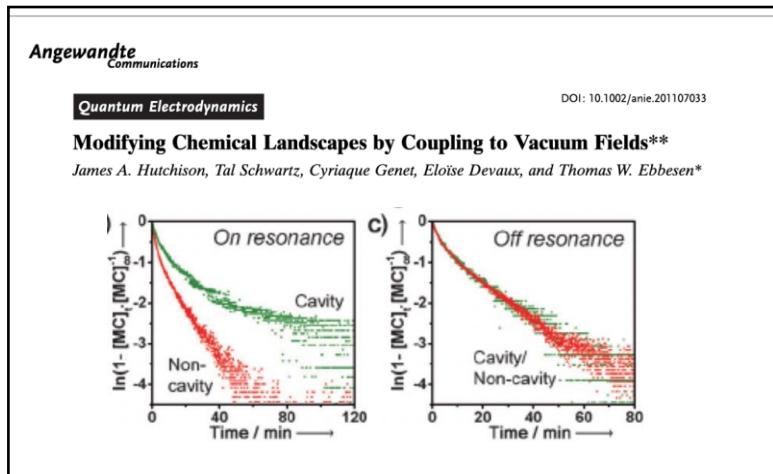


Quantization

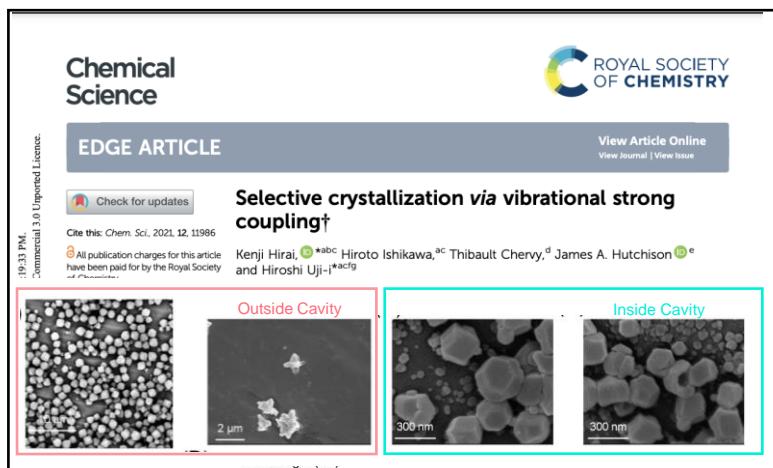


Polaritons

Photochemistry



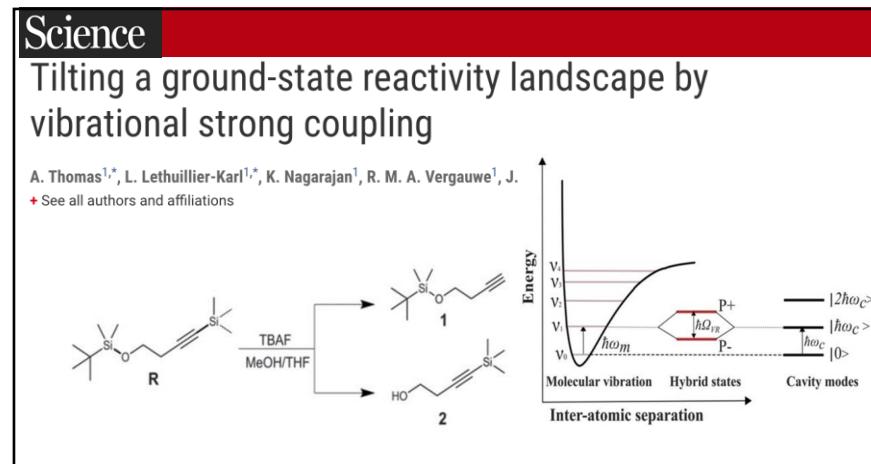
Crystallization



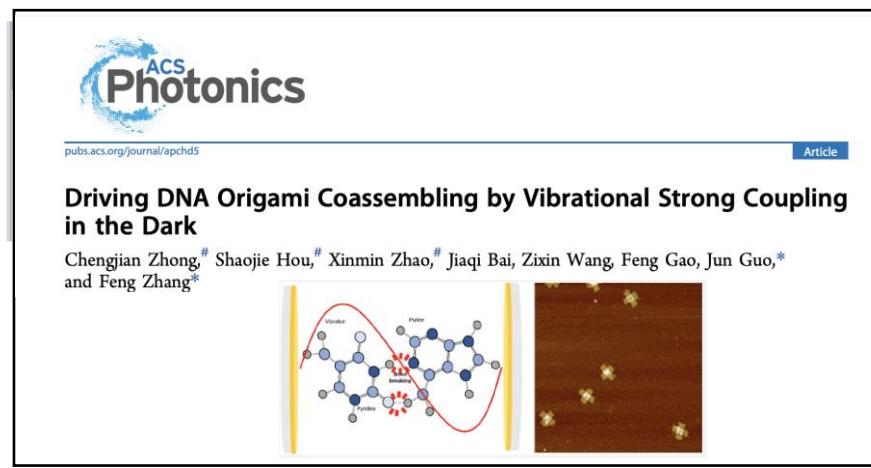
Theoretical Advances in Polariton Chemistry

Rubio (Max Planck), Mukamel (UCI), Huo (Rochester), Yuen-Zhou (UCSD), Herrera (U. Santiago), Groenhoff (U. Jyväskylä), Narang (UCLA), Keeling (St. Andrews), Rebeiro (Emory), Subotnik (UPenn), Feist (UAM), Nitzan (UPenn), Saalfrank (U. Potsdam), Vendrell (Heidelberg), Garcia-Vidal (UAM), Cederbaum (Heidelberg), Koch (NTNU), Kowalewski (Stockholm), Deprince (FSU), Vivok (U. Debrecen), Hammes-Schiffer (Yale), Scholes (Princeton), Foley (UNCC) and many more groups

Chemical Kinetics

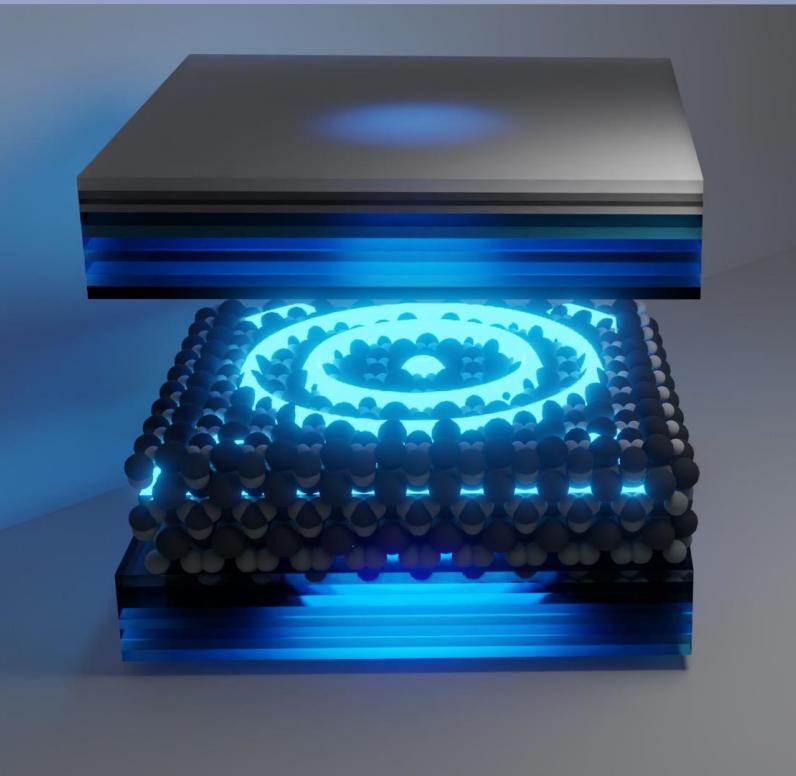


Biophysics



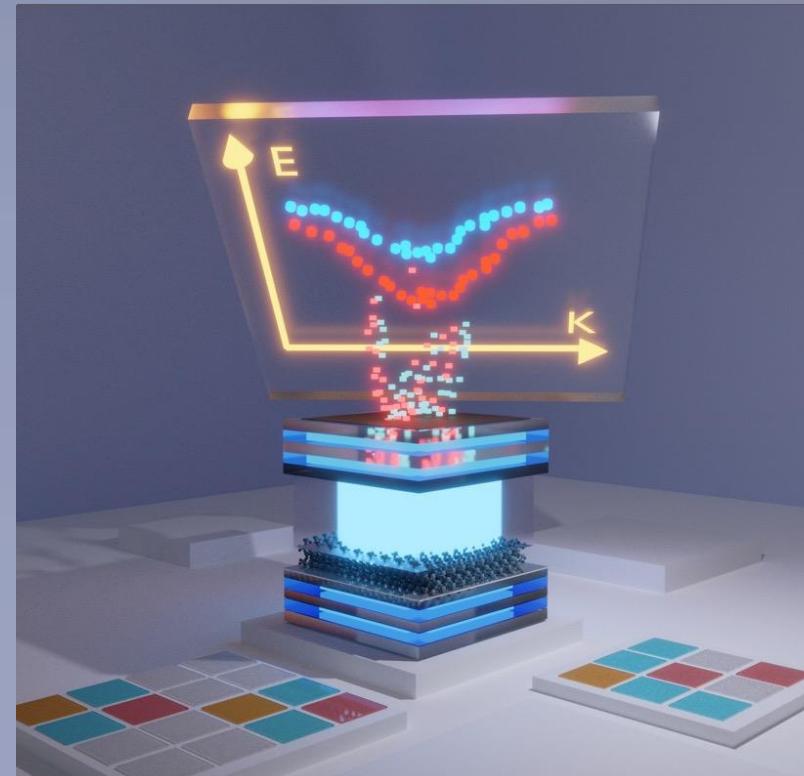
Experiments in Polariton Chemistry/Physics

Ebbesen (Strasbourg), Xiong (UCSD), Menon (CCNY), Schwartz (Tel Aviv), Giebink (Penn), George (IISER-M), Simpkins (NRL), Baumberg (St. Andrews), Vamivakas (Rochester), Krauss (Rochester), Haran (Weizmann), Witchman (Princeton), XYZ (Columbia), Delor (Columbia), Musser (Cornell) many more group...



Exciton-Polariton *Transport*

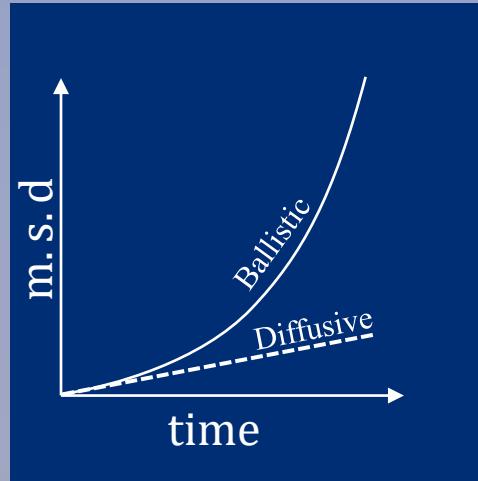
Xu^t **Mandal**^t Baxter Cheng Lee Su Liu Reichman* Delor*
Arxiv: 2205.01176 (2022) ^t Equal



Exciton-Polariton *Dispersion*

Mandal* Xu Mahajan Lee Delor Reichman*
Nano Lett. 2023

Outline



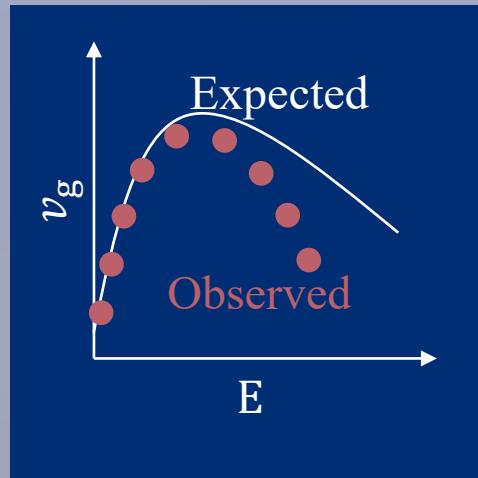
1

Introduce the key concepts
Coherent and Incoherent
Transport

$$\hat{c}\hat{a}^\dagger + \hat{c}^\dagger\hat{a}$$

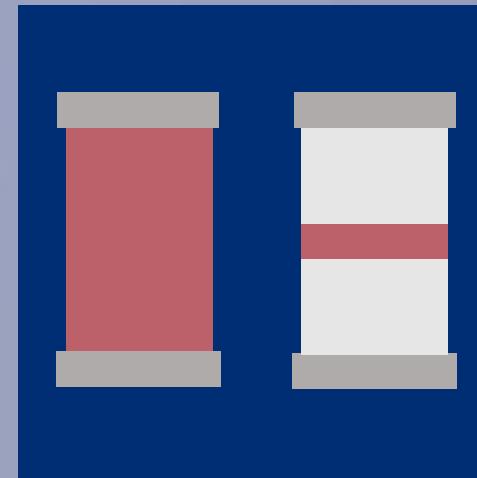
2

Light-Matter
Interactions



3

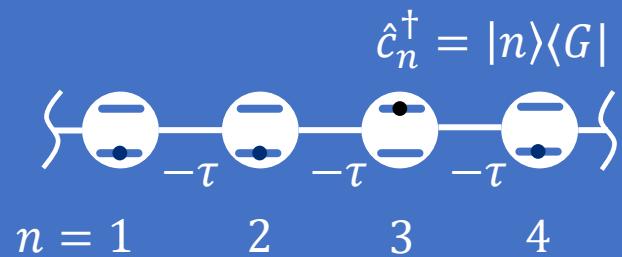
Simulation of Exciton
Polariton Transport
Ballistic and Diffusive
motion of Exciton-Polariton
Experiment + Theory



4

Microscopic theory of
Dispersion
Experiment + Theory

5



A set of two level systems with nearest neighbor coupling.

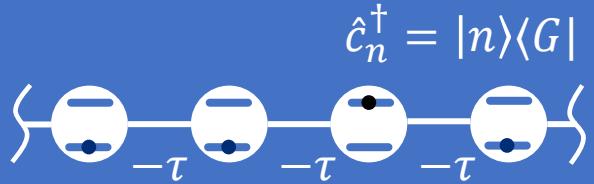
$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

$$|k\rangle = \frac{1}{\sqrt{N}} \sum_n e^{ikn} |n\rangle \quad \hat{c}_k = \frac{1}{\sqrt{N}} \sum_n e^{ikn} \hat{c}_n$$

$$\hat{H}_{1D} |k\rangle = (\epsilon_0 - 2\tau \cos k) |k\rangle$$

$$\hat{H}_{1D} = \sum_k (\epsilon_0 - 2\tau \cos k) \hat{c}_k^\dagger \hat{c}_k = \sum_k \epsilon_k \hat{c}_k^\dagger \hat{c}_k$$

1D Exciton (Group Velocity)



$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

$$|k\rangle = \frac{1}{\sqrt{N}} \sum_n e^{ikn} |n\rangle \quad \hat{c}_k = \frac{1}{\sqrt{N}} \sum_n e^{ikn} \hat{c}_n$$

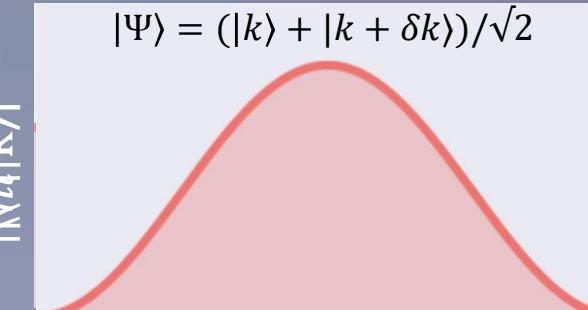
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$$\hat{H}_{1D} = \sum_k (\epsilon_0 - 2\tau \cos k) \hat{c}_k^\dagger \hat{c}_k = \sum_k \epsilon_k \hat{c}_k^\dagger \hat{c}_k$$

Energy

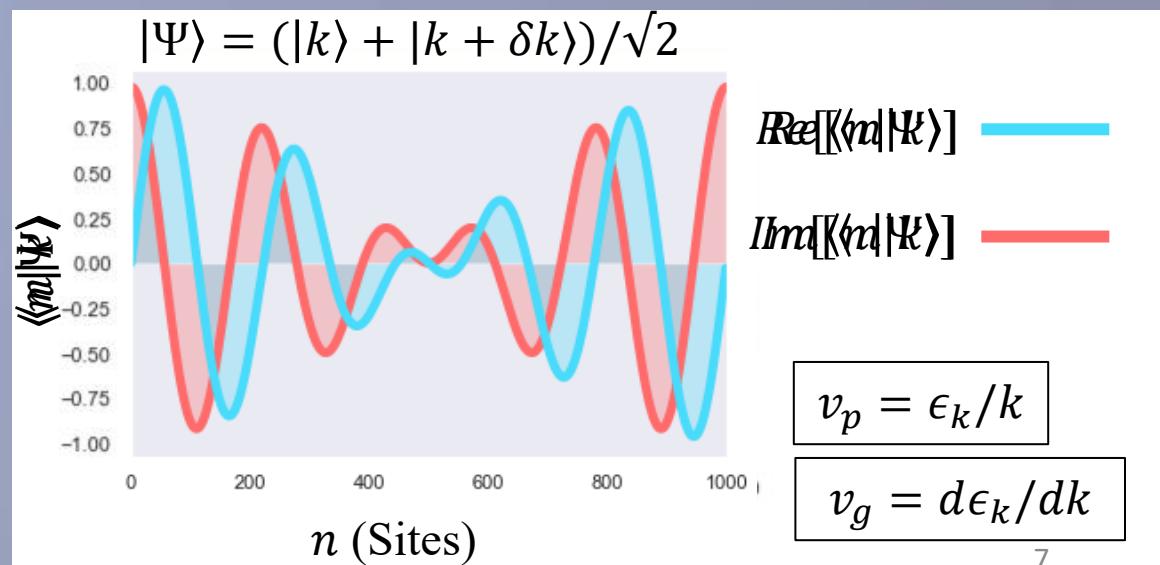


k

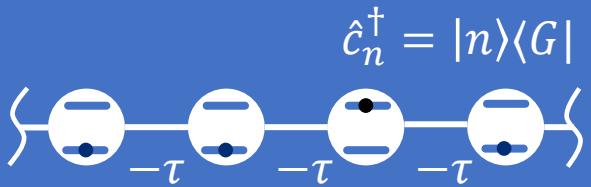


n (Sites)

Eigenfunctions are delocalized in site space.
Localized in reciprocal space.



Ballistic (Coherent) Transport



$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

$$|k\rangle = \frac{1}{\sqrt{N}} \sum_n e^{ikn} |n\rangle \quad \hat{c}_k = \frac{1}{\sqrt{N}} \sum_n e^{ikn} \hat{c}_n$$

$$\hat{H}_{1D} |k\rangle = (\epsilon_0 - 2\tau \cos k) |k\rangle$$

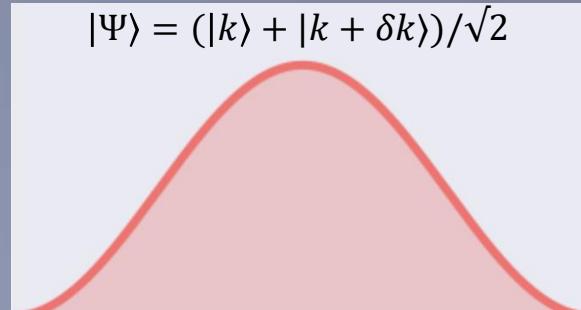
$$\hat{H}_{1D} = \sum_k (\epsilon_0 - 2\tau \cos k) \hat{c}_k^\dagger \hat{c}_k = \sum_k \epsilon_k \hat{c}_k^\dagger \hat{c}_k$$

Energy

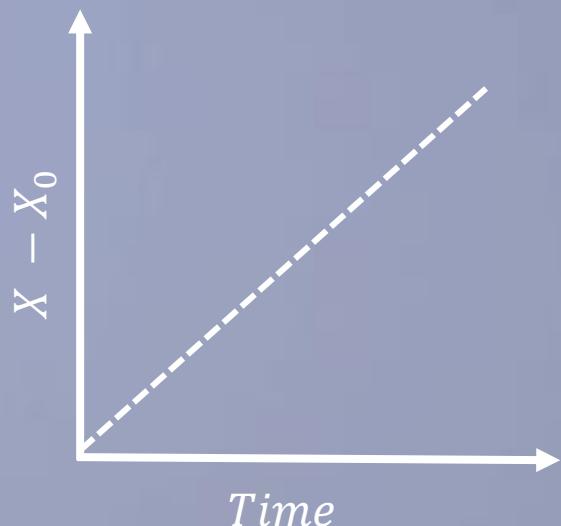


k

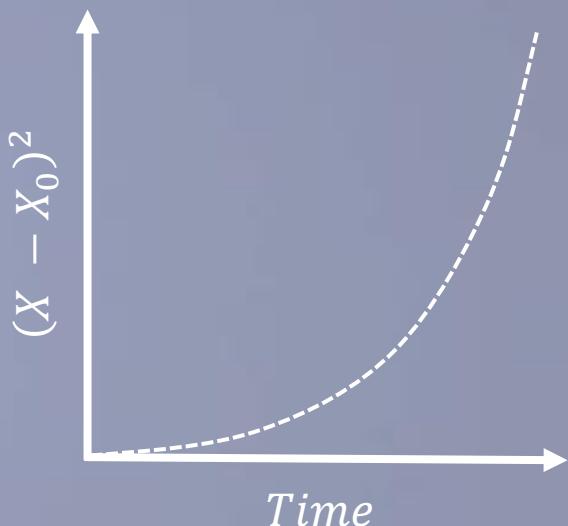
$|\langle n | \Psi \rangle|^2$



Ballistic (Coherent) Motion

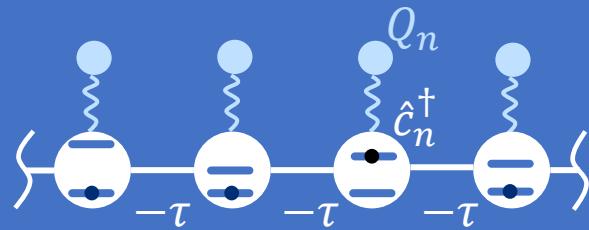


Time



Time

1D Exciton + Phonon



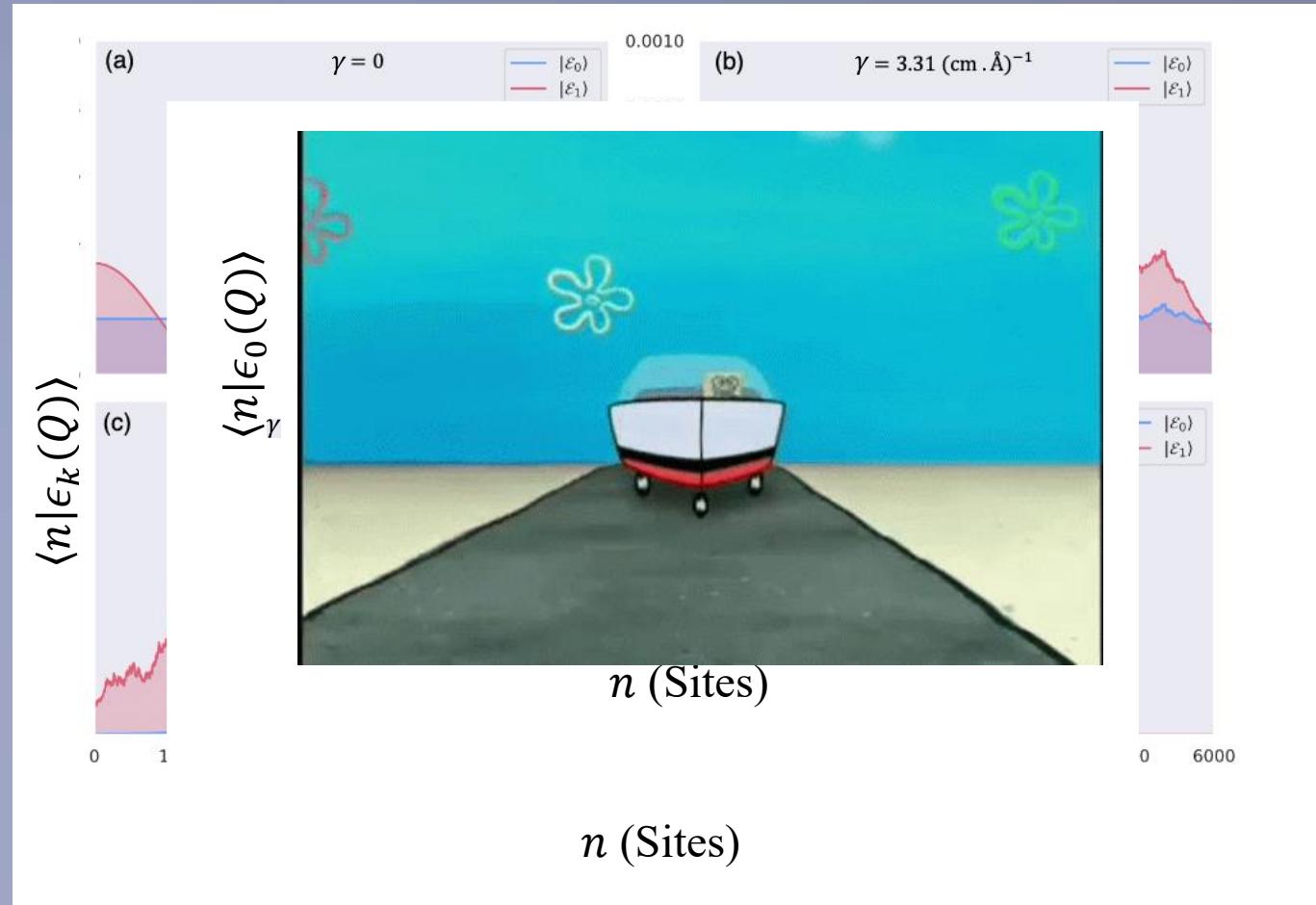
$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1})$$

$$+ \gamma \sum_n Q_n \hat{c}_n^\dagger \hat{c}_n + \frac{1}{2} \sum_n (P_n^2 + \omega_p^2 Q_n^2)$$

Electronic Hamiltonian

$$\hat{H}_{el} = \hat{H}_{1D} - \sum_n \frac{P_n^2}{2}$$

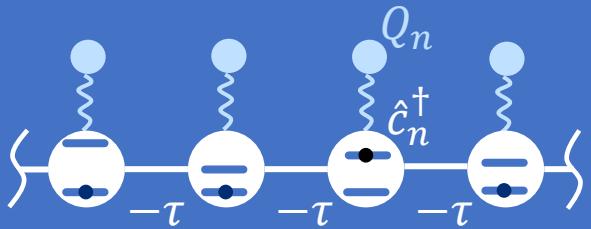
$$\hat{H}_{el} |\epsilon_k(Q)\rangle = \epsilon_k(Q) |\epsilon_k(Q)\rangle$$



Phonon fluctuation leads to energetic disorder which leads to localization of eigenstates

This disorder is dynamic, i.e. time-dependent

Exciton Diffusion (Ehrenfest Method)

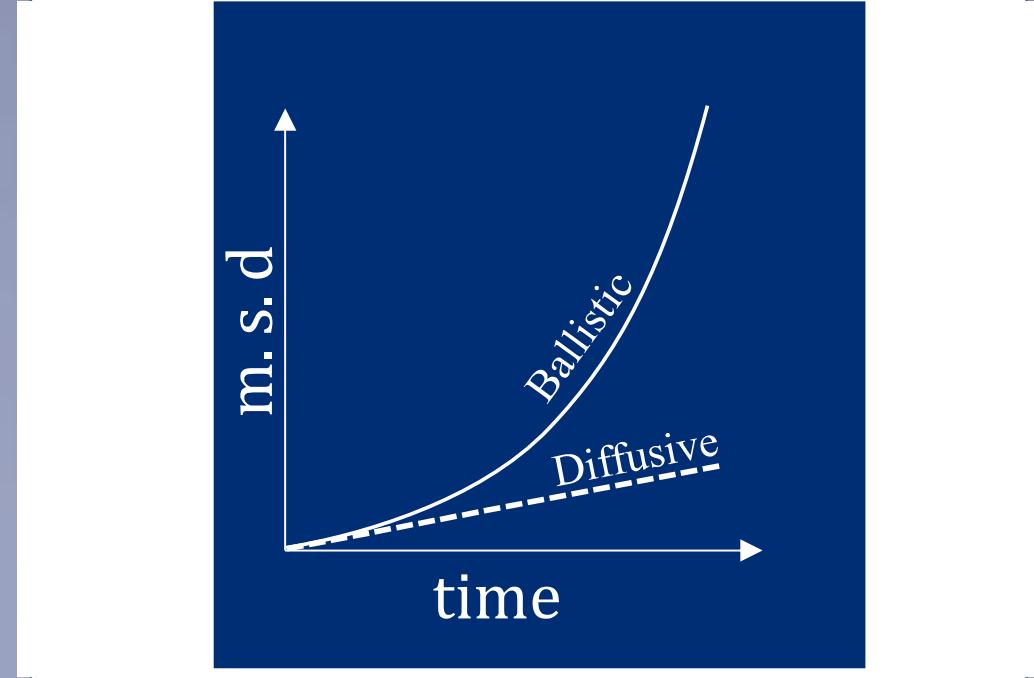


$$\hat{H}_{1D} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1}) + \gamma \sum_n Q_n \hat{c}_n^\dagger \hat{c}_n + \frac{1}{2} \sum_n (P_n^2 + \omega_p^2 Q_n^2)$$

Electronic Hamiltonian

$$\hat{H}_{el} = \hat{H}_{1D} - \sum_n \frac{P_n^2}{2}$$

$$\hat{H}_{el} |\epsilon_k(Q)\rangle = \epsilon_k(Q) |\epsilon_k(Q)\rangle$$



THE JOURNAL OF CHEMICAL PHYSICS 134, 244116 (2011)

Mixed quantum-classical simulations of charge transport in organic materials: Numerical benchmark of the Su-Schrieffer-Heeger model

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²State Key Laboratory for Structural Chemistry of Unstable and Stable Species, Beijing National Laboratory for Molecular Sciences (BNLMS), Institute of Chemistry, Chinese Academy of Sciences, Zhongguancun, 100190 Beijing, People's Republic of China

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This disorder is dynamic, i.e., time-dependent

PRL 96, 086601 (2006)

PHYSICAL REVIEW LETTERS

week ending
3 MARCH 2006

Charge-Transport Regime of Crystalline Organic Semiconductors: Diffusion Limited by Thermal Off-Diagonal Electronic Disorder

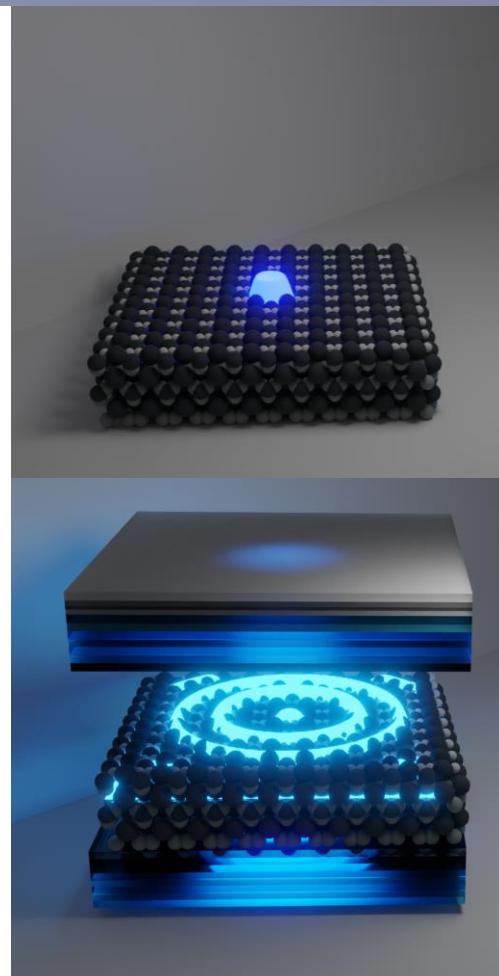
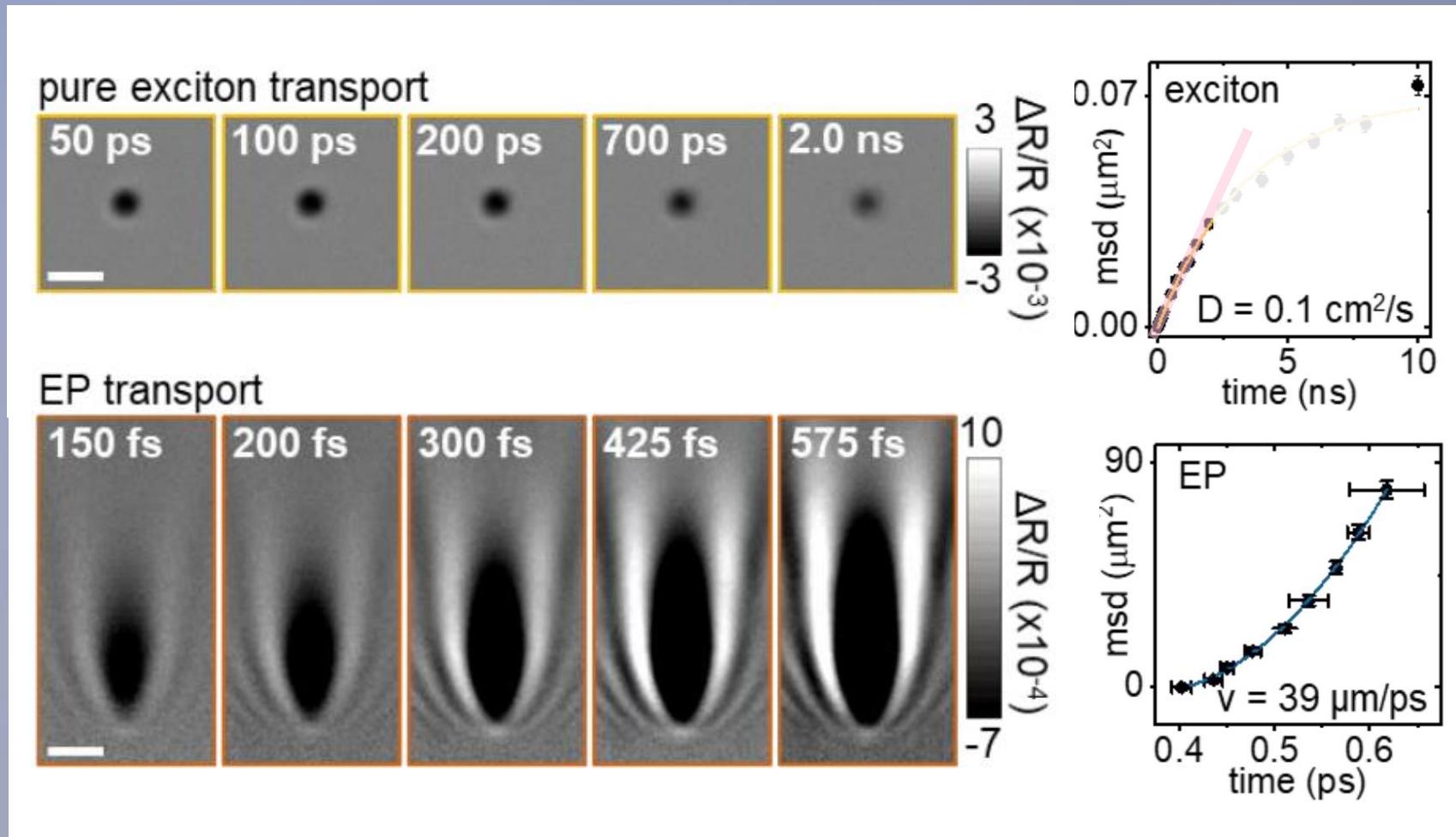
Alessandro Troisi¹ and Giorgio Orlandi²

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(Received 23 November 2005; published 3 March 2006)

Exciton-Polariton Transport



Also see:

Pandya et. Al. Adv. Sci. 9, 2105569 (2022)

Balasubrahmanyam et. al. Nat. Matter (2023)

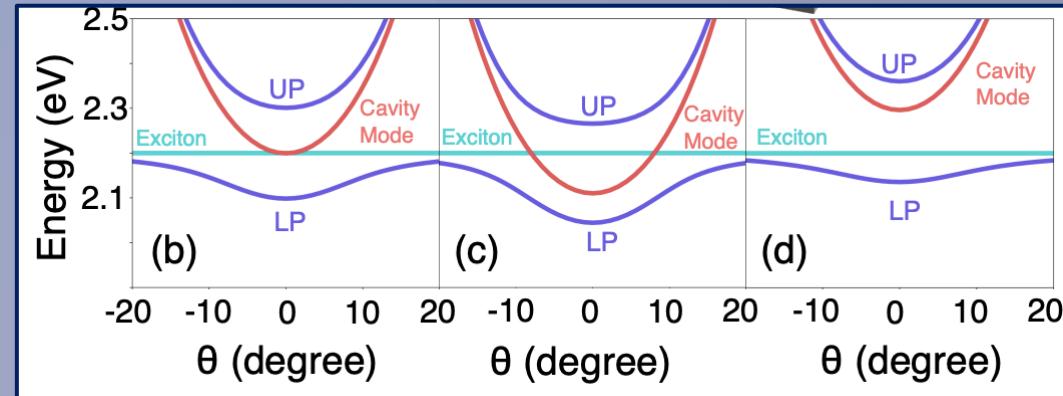
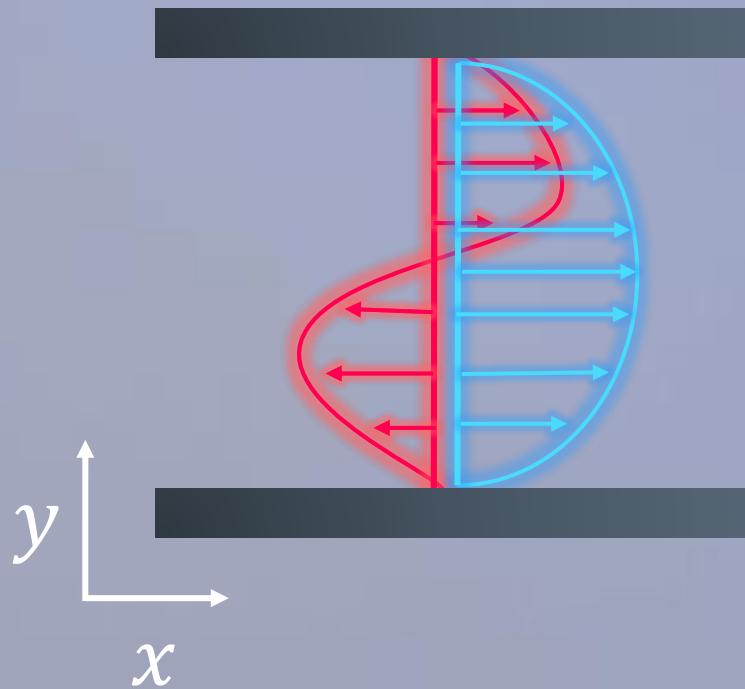
Xu[†], Mandal[†], ..., Milan, Reichman (arXiv: 2205.01176) 2022

Light-Matter Hamiltonian

$$\hat{H}_{\text{LM}} = \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1}) + \gamma \sum_n Q_n \hat{c}_n^\dagger \hat{c}_n + \frac{1}{2} \sum_n (P_n^2 + \omega_p^2 Q_n^2)$$

$$+ \sum_{\mathbf{k}} \hat{a}_{\mathbf{k}}^\dagger \hat{a}_{\mathbf{k}} \omega_{\mathbf{k}} + g_c \sum_{n,\mathbf{k}} (\hat{c}_n^\dagger \hat{a}_{\mathbf{k}} e^{ik_x \cdot \mathbf{R}_n} + \hat{a}_{\mathbf{k}}^\dagger \hat{c}_n e^{-ik_x \cdot \mathbf{R}_n}) \sin(k_y \cdot \mathbf{R}_n)$$

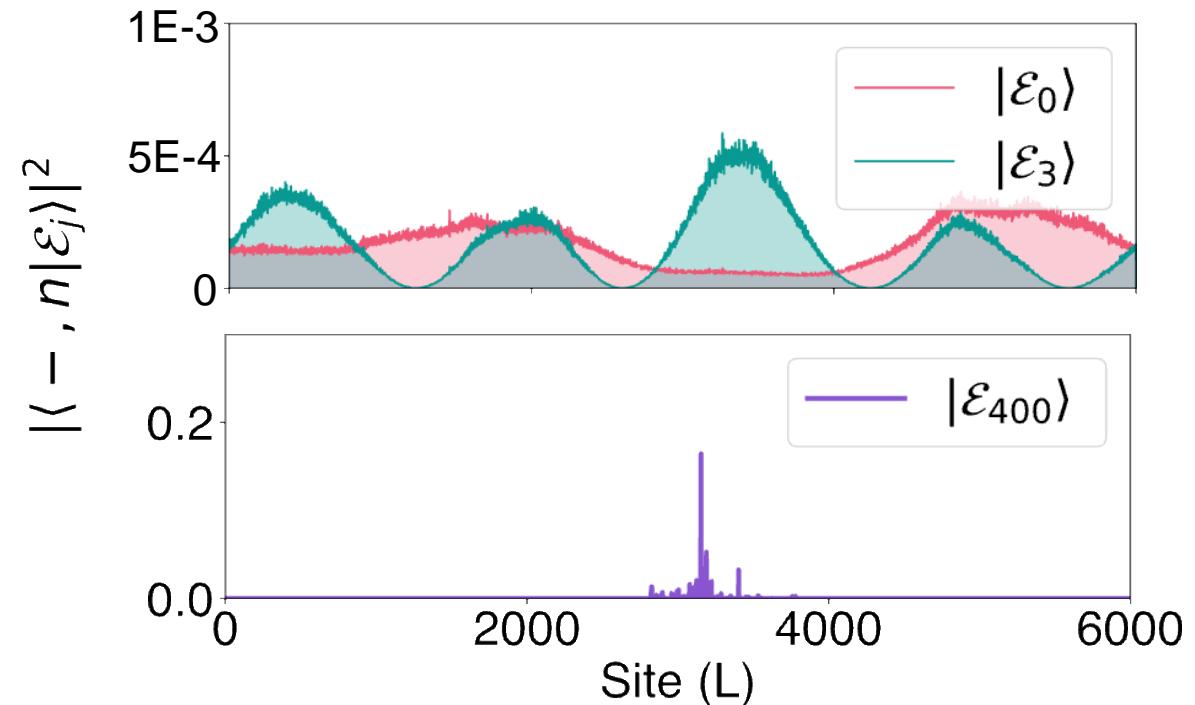
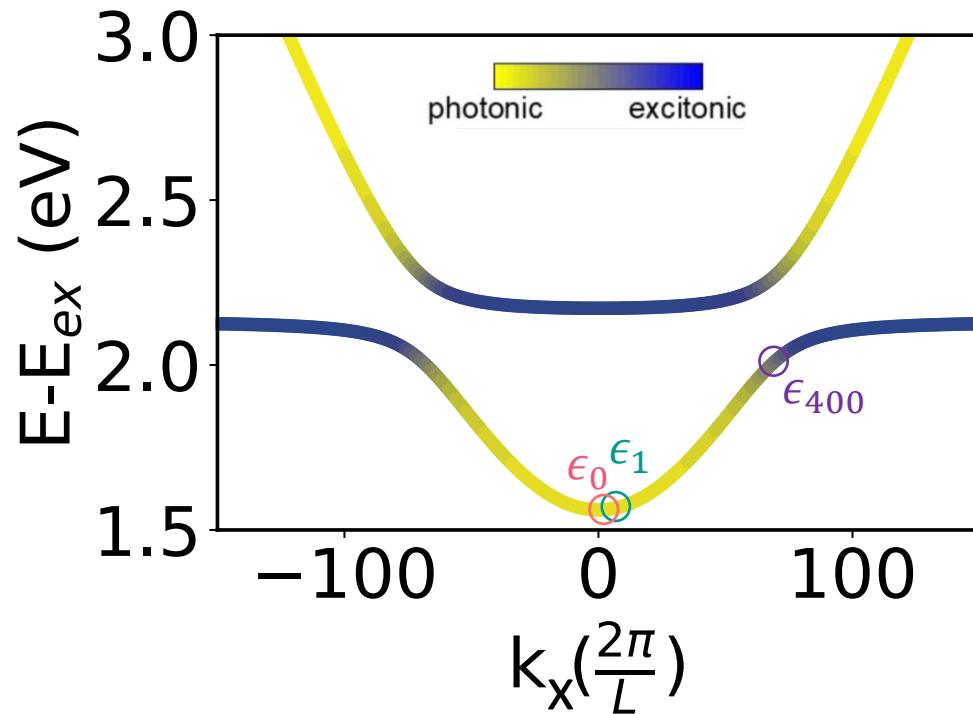
Photon Modes



Cavity operators do not couple to phonons. Photon frequency is off-resonant to phonon frequency.

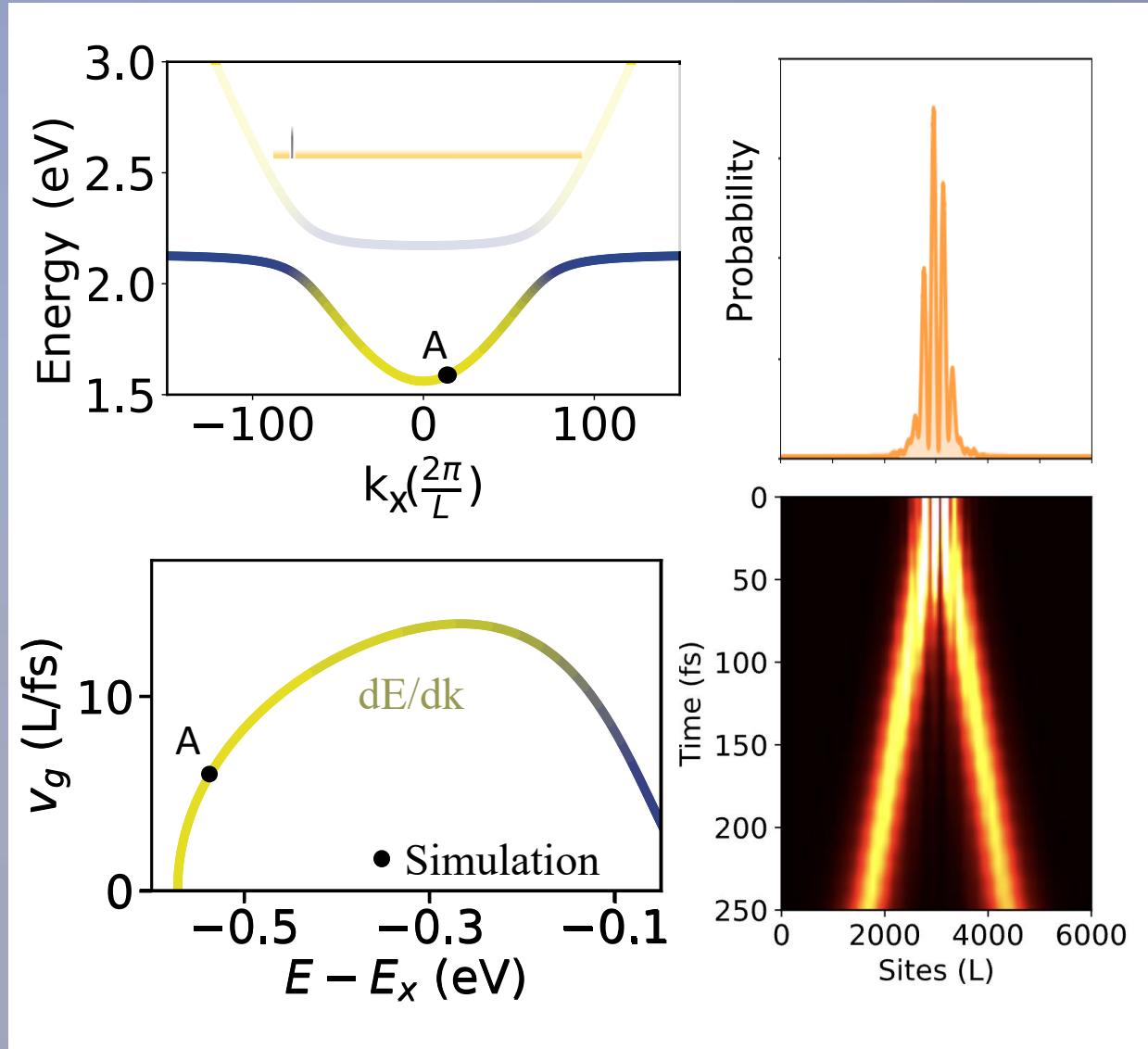
Polaritons, which are partially excitonic, have effectively smaller coupling to phonons.

Polariton States at various Detuning



Higher Exciton character \rightarrow Higher Phonon Coupling \rightarrow Higher Localization

Group Velocity



At low exciton character (at large detuning) the exciton-polariton wavepacket **propagates ballistically**.

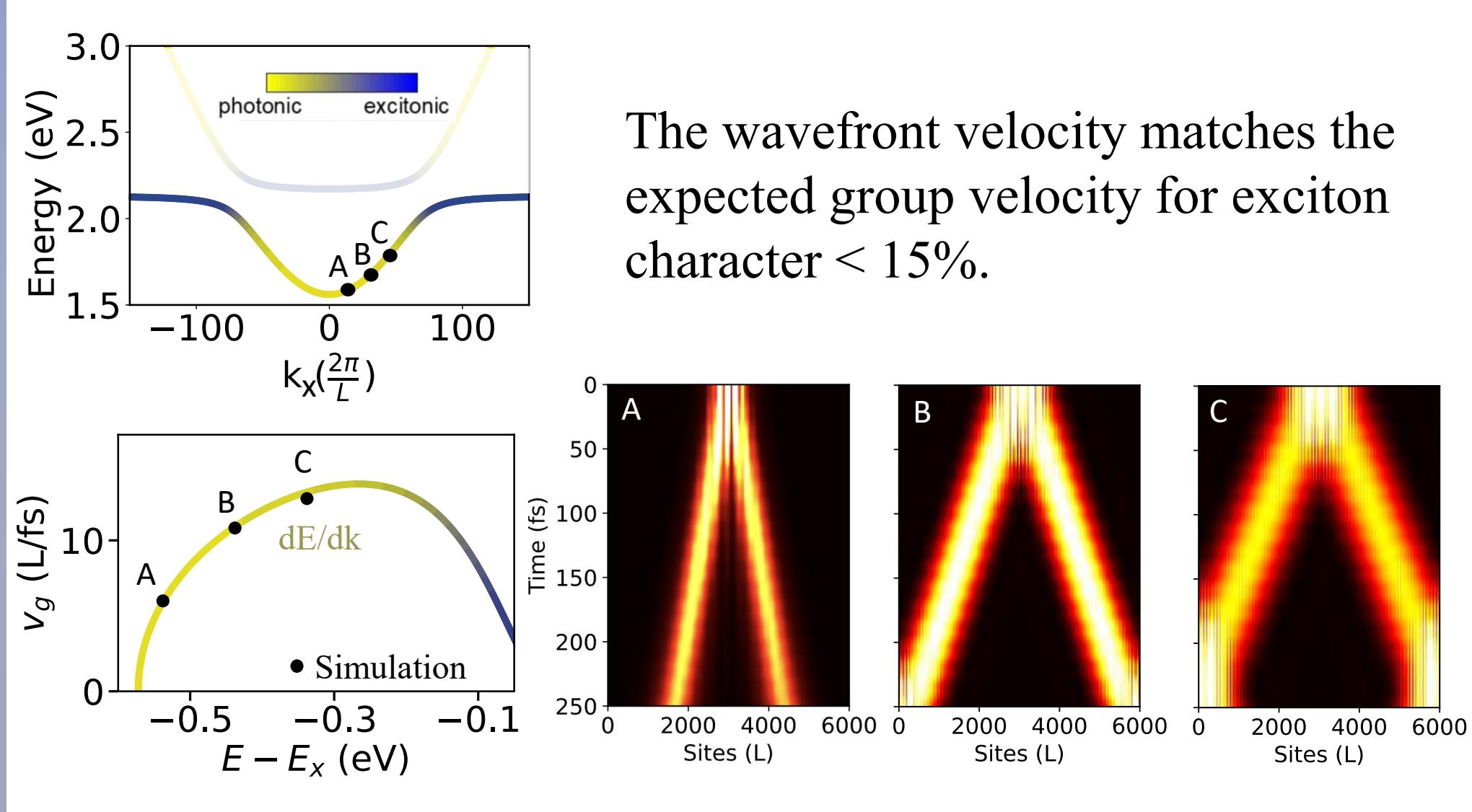
The wavefront velocity matches the expected group velocity.

Also see: Berghuis et. Al. ACS photonics 9 (7), 2263-2272

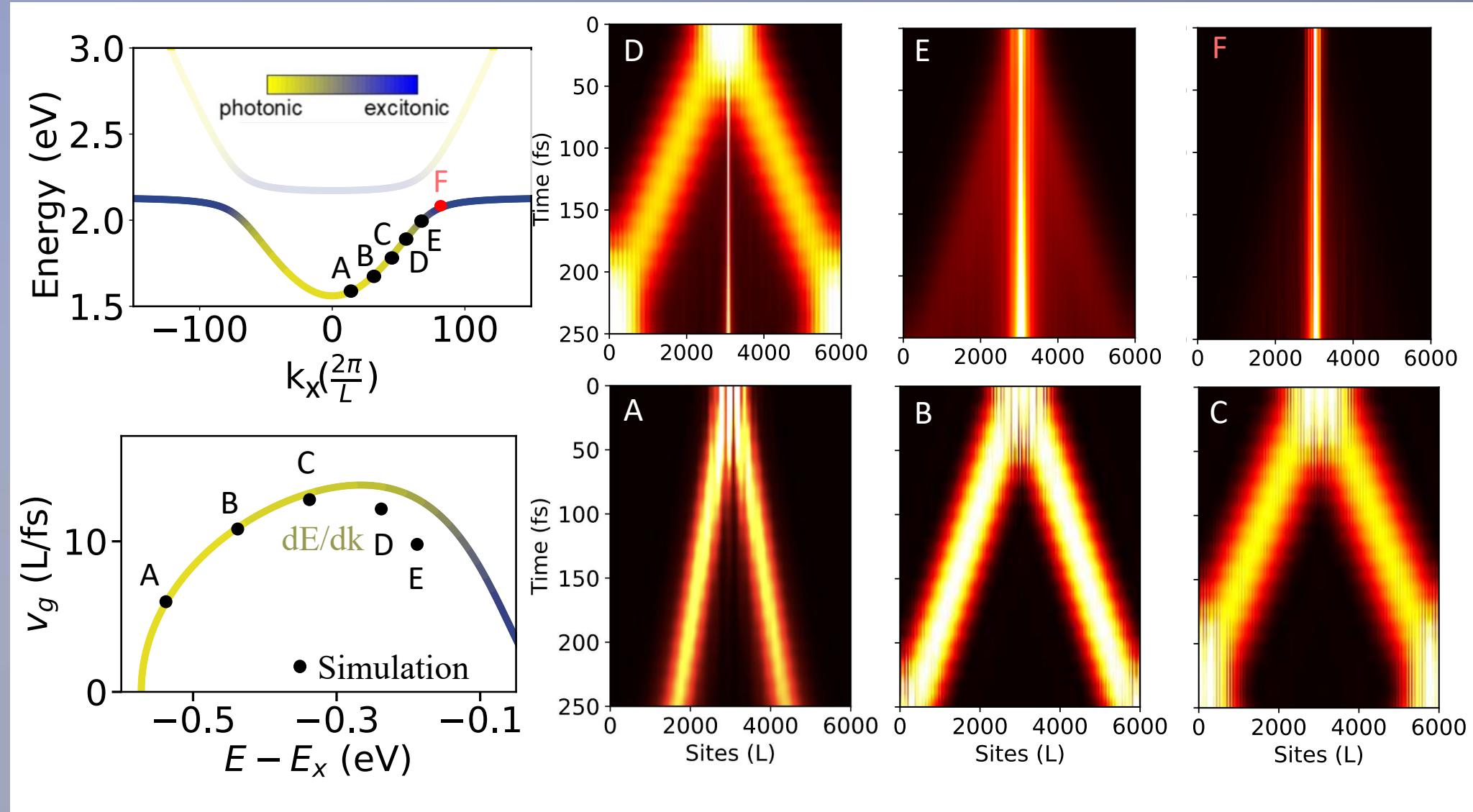
Sokolovskii et. Al. arXiv:2209.07309

Xu[†], Mandal[†], Milan, Reichman (arXiv: 2205.01176) 2022

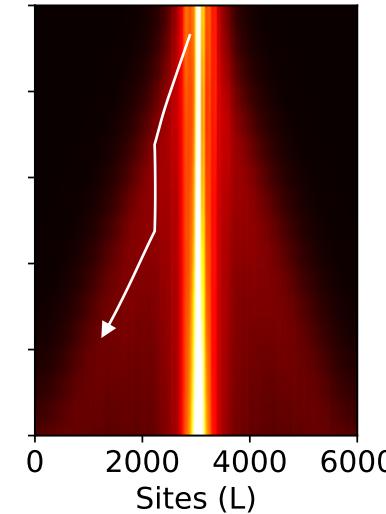
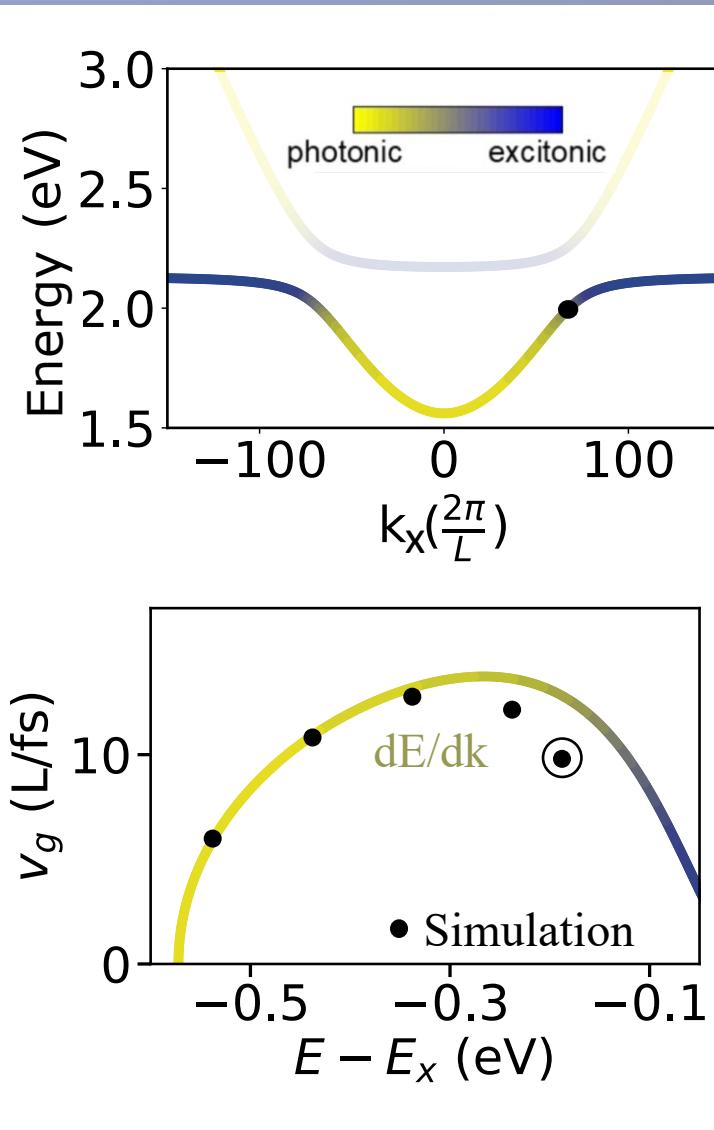
Group Velocity vs Exciton Character



Group Velocity



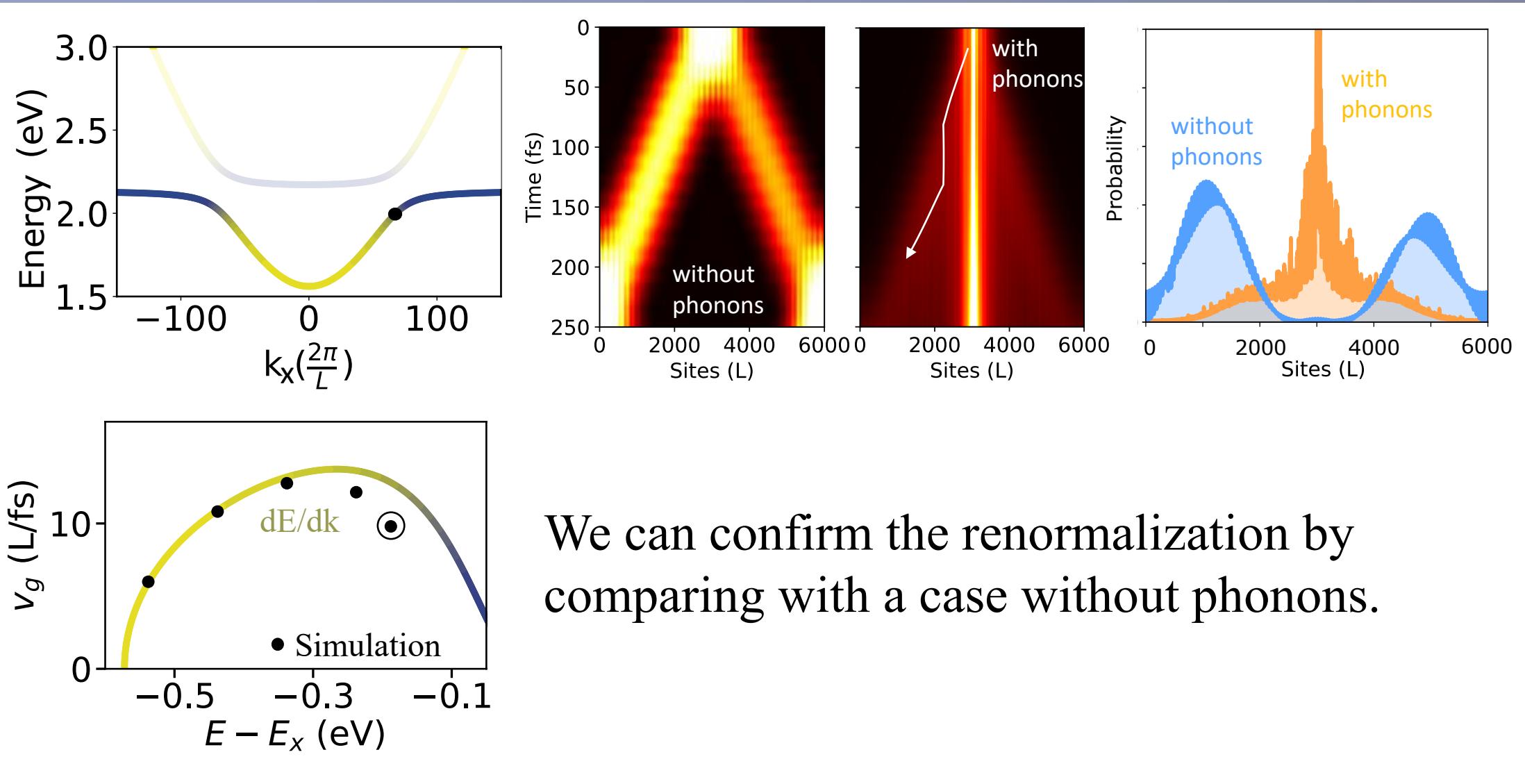
Velocity Renormalization



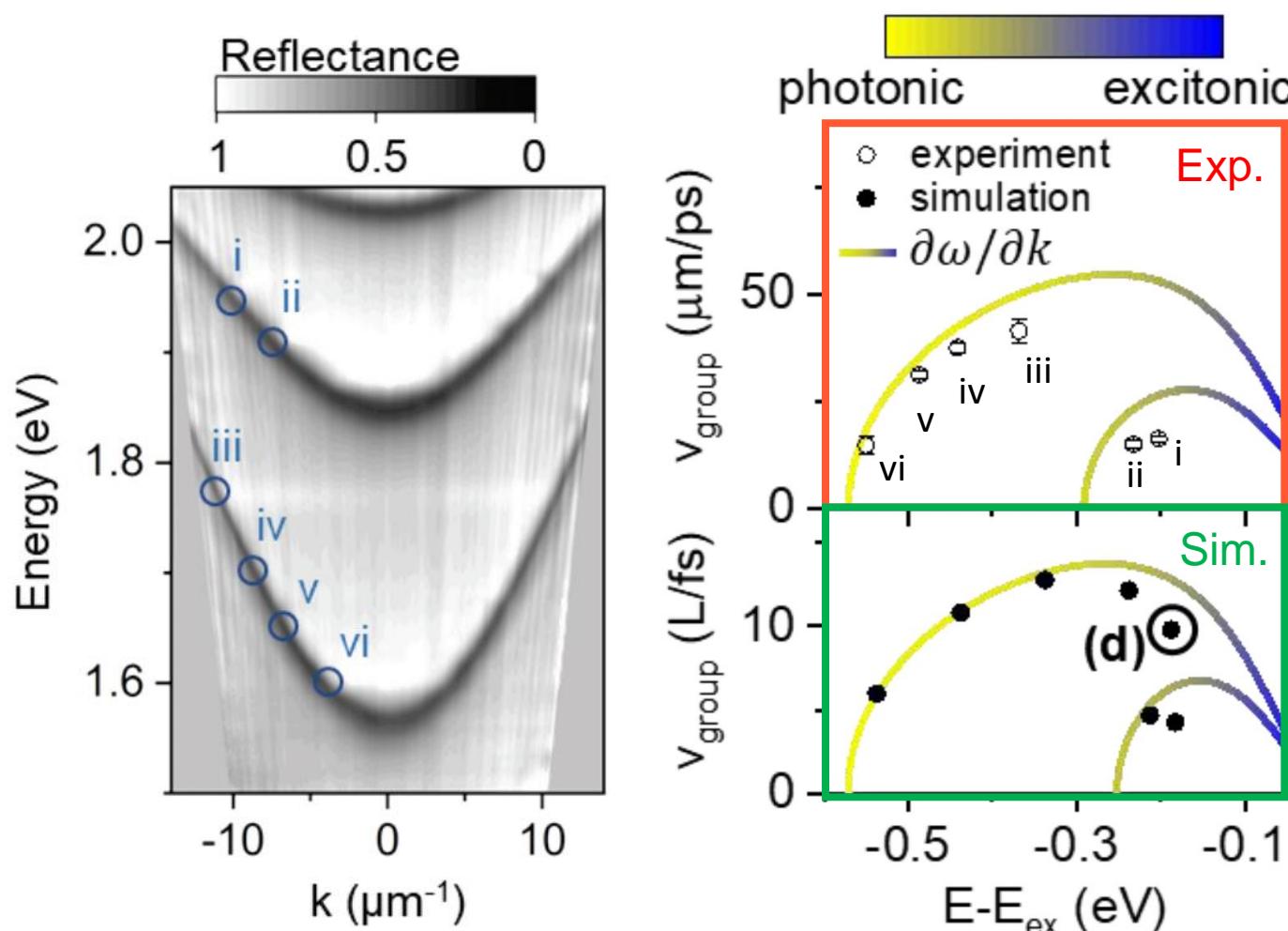
At exciton character 25-40% → Phonons
renormalizes polariton group velocity

Phonon induced transient localization
leads to reduced velocity

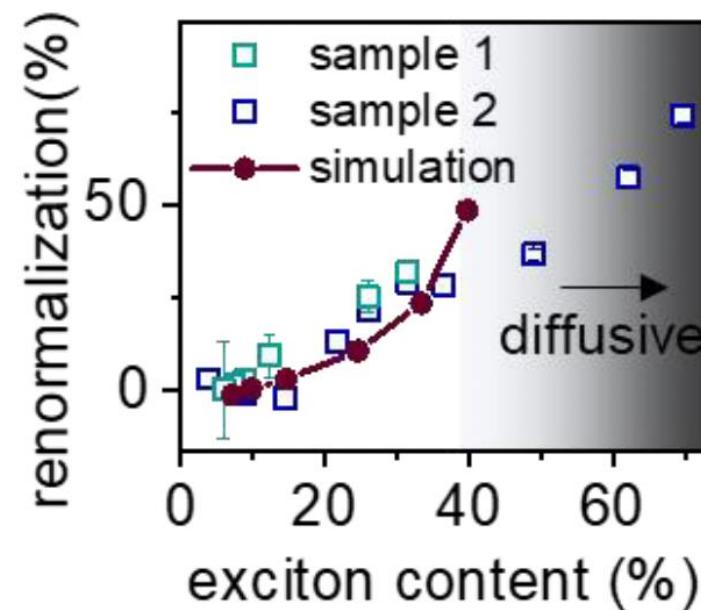
Group Velocity



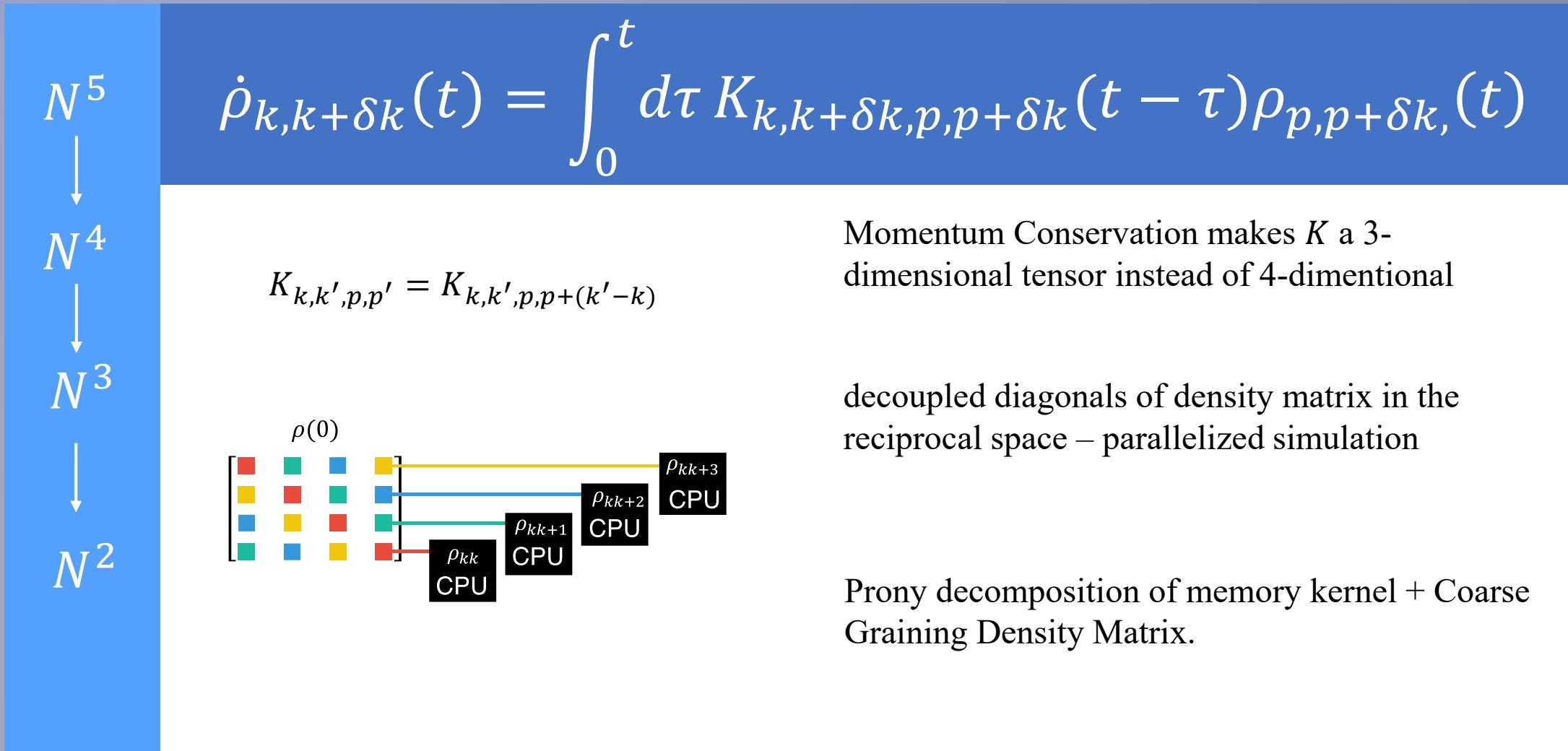
Experiment & Theory: Group Velocity



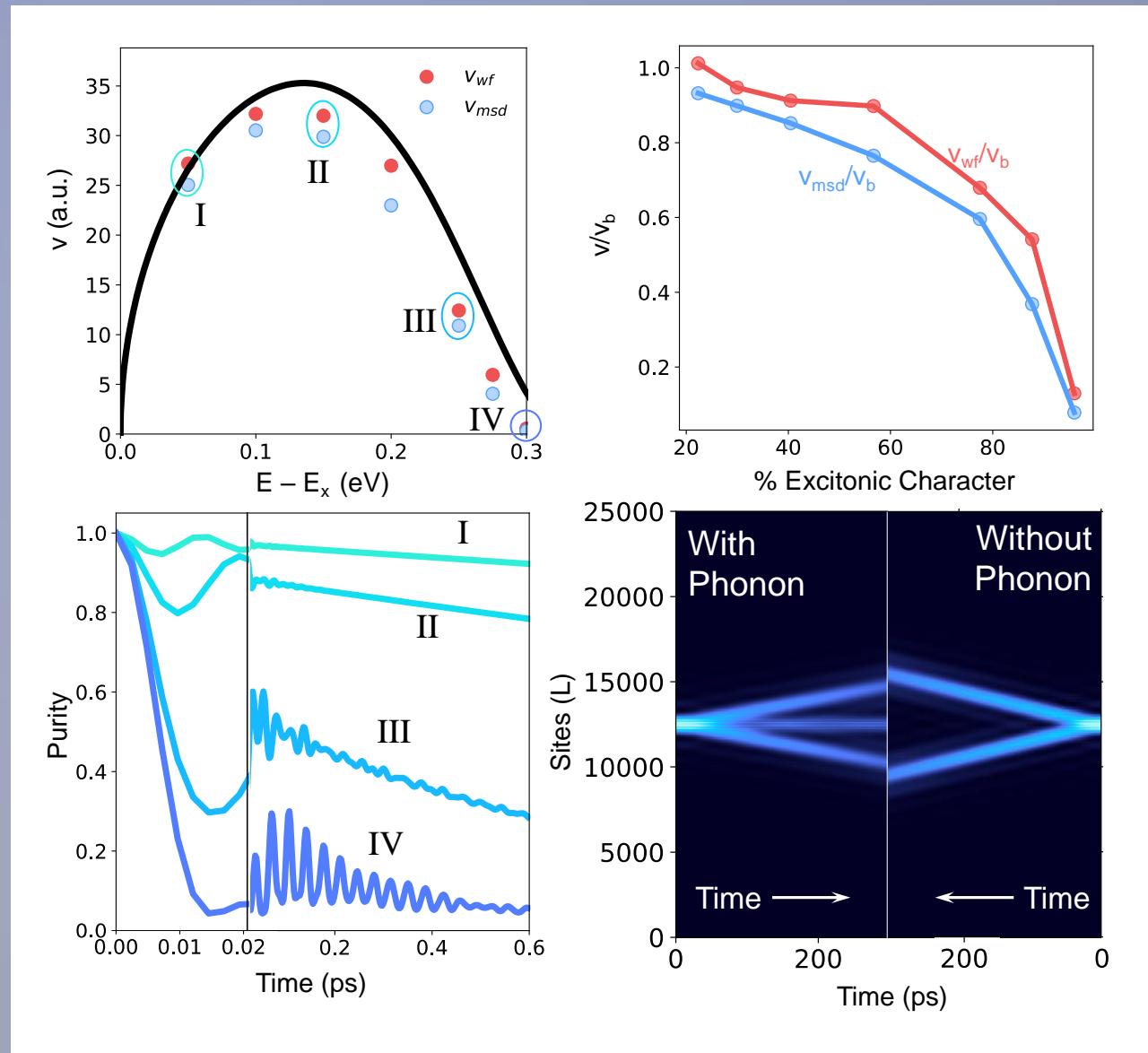
We experimentally observe the same phenomena.



Aim: Simulate a matter system with $\sim 10^4$ sites and 10^2 cavity modes (~ 10000 states)



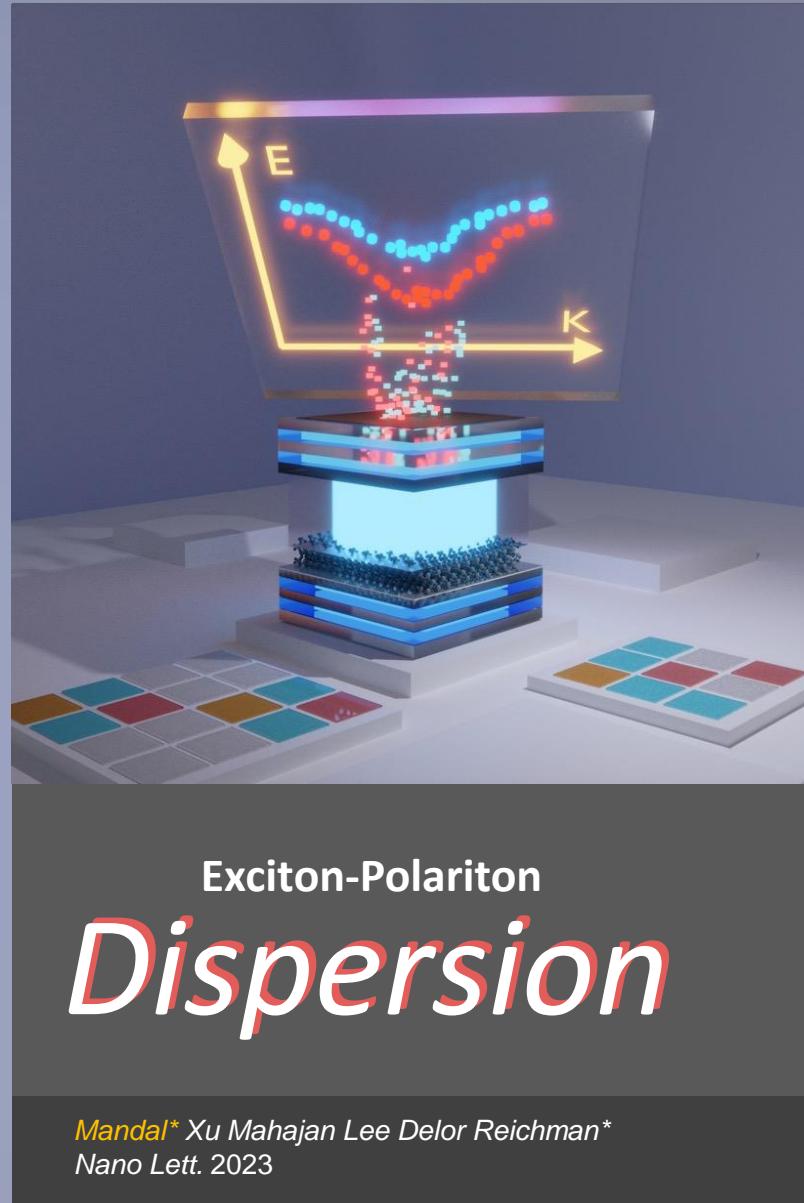
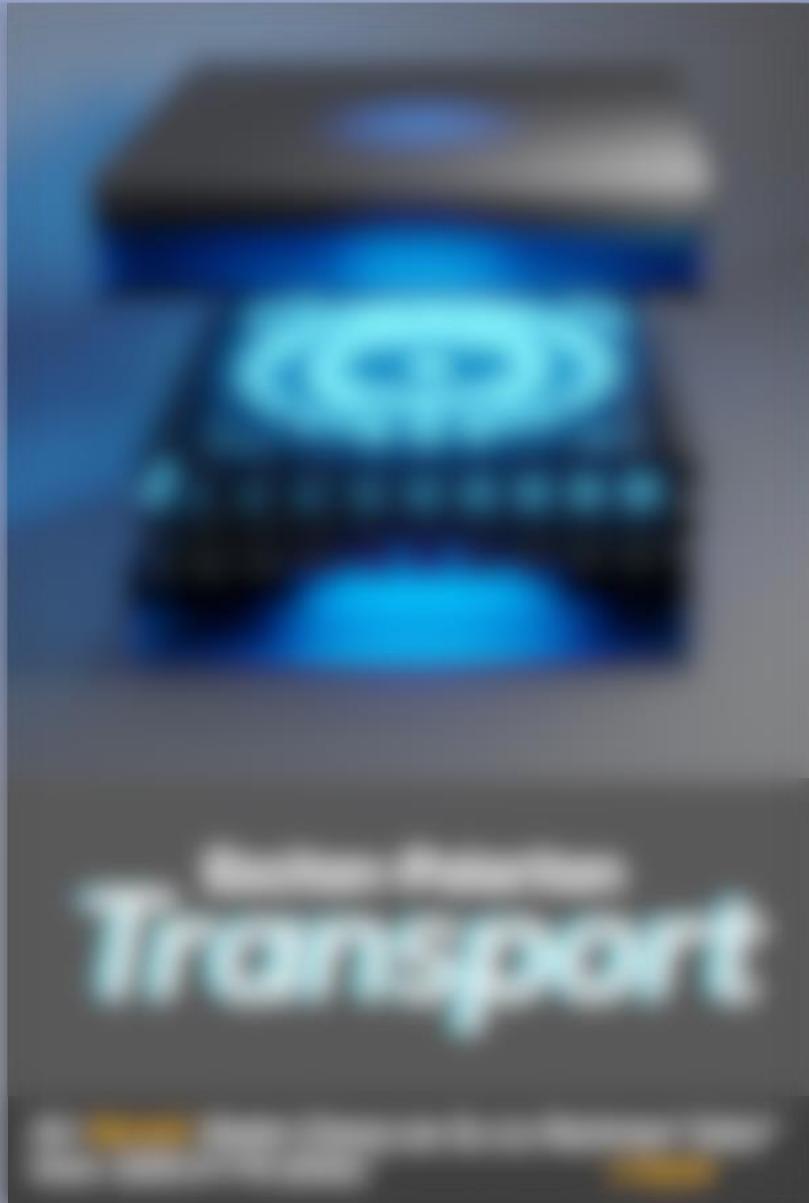
Polariton Transport



Higher purity ==
Coherent.

We perform
Non-Markovian
Master Equation
simulation with
25000 states!

Topics



Exciton-Polariton
Dispersion

*Mandal** Xu Mahajan Lee Delor Reichman*
Nano Lett. 2023

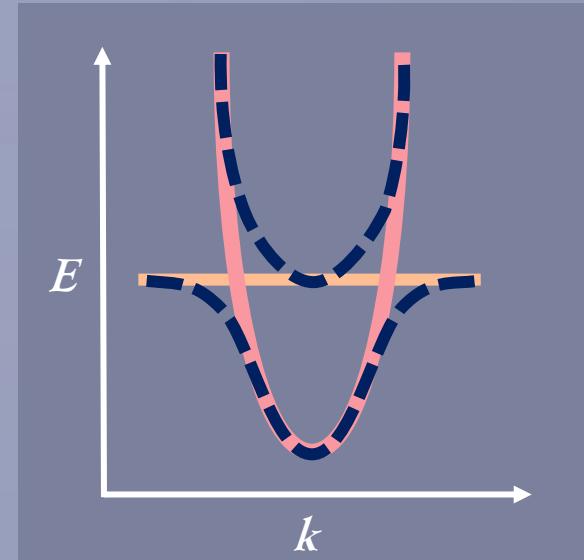
Light-Matter Hamiltonian

$$\begin{aligned}\hat{H}_{\text{LM}} = & \epsilon_0 \sum_n \hat{c}_n^\dagger \hat{c}_n - \tau \sum_n (\hat{c}_{n+1}^\dagger \hat{c}_n + \hat{c}_n^\dagger \hat{c}_{n+1}) \\ & + \sum_{\mathbf{k}} \hat{a}_{\mathbf{k}}^\dagger \hat{a}_{\mathbf{k}} \omega_{\mathbf{k}} + g_c \sum_{n,\mathbf{k}} (\hat{c}_n^\dagger \hat{a}_{\mathbf{k}} e^{ik_{\parallel} \cdot \mathbf{R}_n} + \hat{a}_{\mathbf{k}}^\dagger \hat{c}_n e^{-ik_{\parallel} \cdot \mathbf{R}_n}) \sin(k_{\perp} \cdot \mathbf{R}_n)\end{aligned}$$

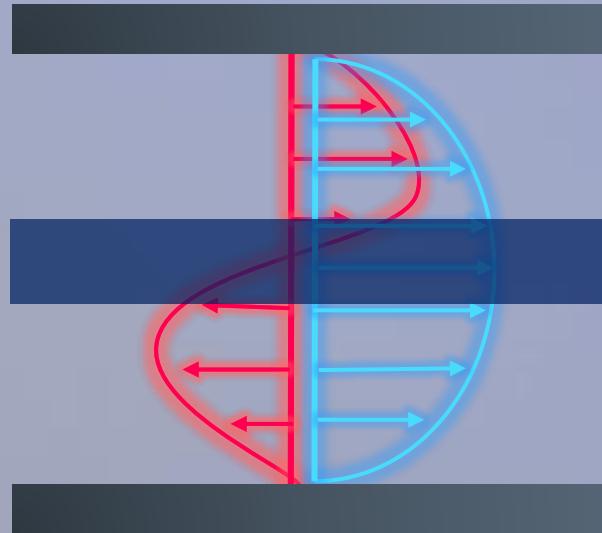


$$\hat{H}_{\text{LM}} = \sum_k \hat{c}_k^\dagger \hat{c}_k \epsilon_k + \hat{a}_k^\dagger \hat{a}_k \omega_k - g(\hat{a}_k^\dagger \hat{c}_k + \hat{c}_k^\dagger \hat{a}_k) = \sum H_k$$

ϵ	Ω_1
Ω_1	ω_{C_1}



Expectation: Exciton-Polariton Band Structure is obtained by a $(N+1) \times (N+1)$ Matrix.
 N = number of cavity mode branches.



$$\hat{H}_{LM} = \sum_k \hat{c}_k^\dagger \hat{c}_k \epsilon_k + \hat{a}_k^\dagger \hat{a}_k \omega_k - g(\hat{a}_k^\dagger \hat{c}_k + \hat{c}_k^\dagger \hat{a}_k) = \sum H_k$$

	Ω_1	Ω_2	Ω_3
Ω_1	c_1	0	0
Ω_2	0	c_2	0
Ω_3	0	0	c_3

Problem with N+1 Hamiltonian

(N+1)x(N+1) model do not reproduce exciton polariton dispersion

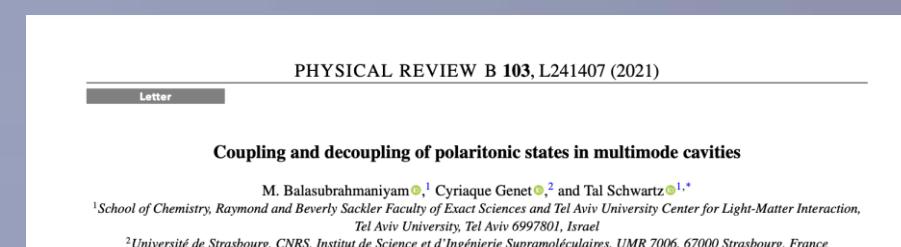
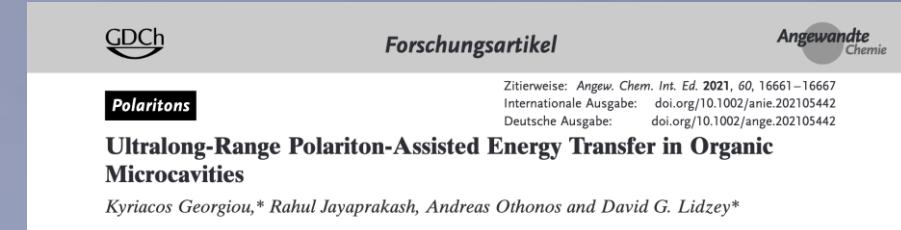
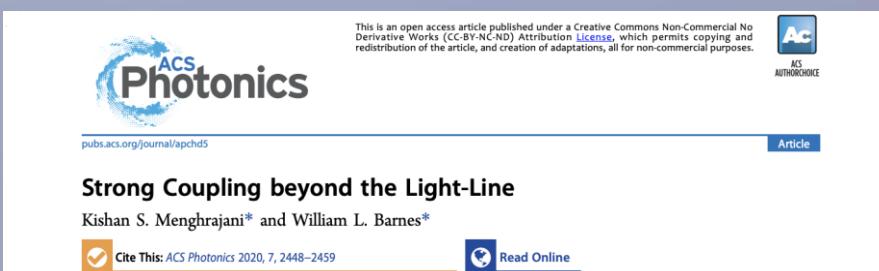
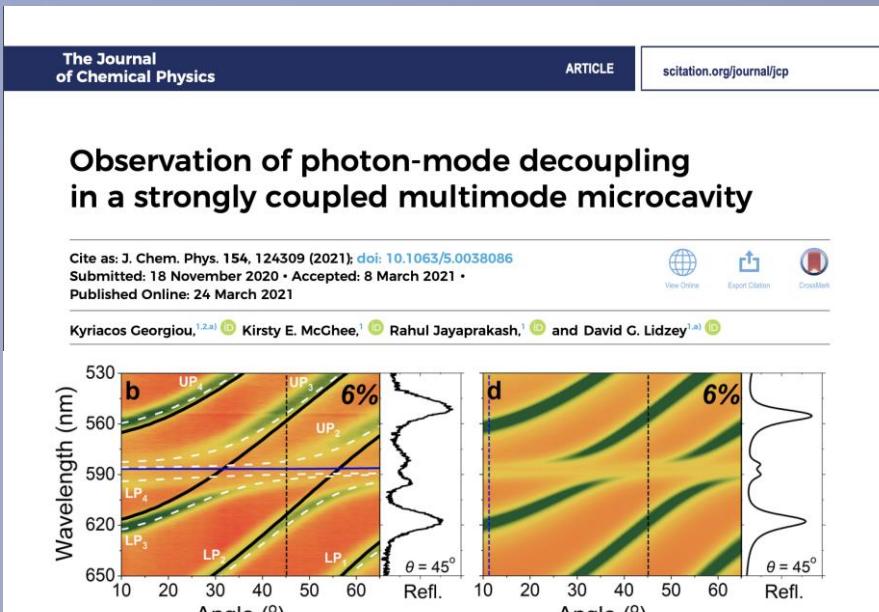
2N x 2N model reproduce exciton polariton dispersion

N+1 Hamiltonian
(cannot be used)

	Ω_1	Ω_2	Ω_3
Ω_1	c ₁	0	0
Ω_2	0	c ₂	0
Ω_3	0	0	c ₃

2N Hamiltonian

	Ω_1	0	0	0	0
Ω_1	c ₁	0	0	0	0
0	0	Ω_2	0	0	0
0	0	Ω_2	c ₂	0	0
0	0	0	0	Ω_3	0
0	0	0	0	Ω_3	c ₃



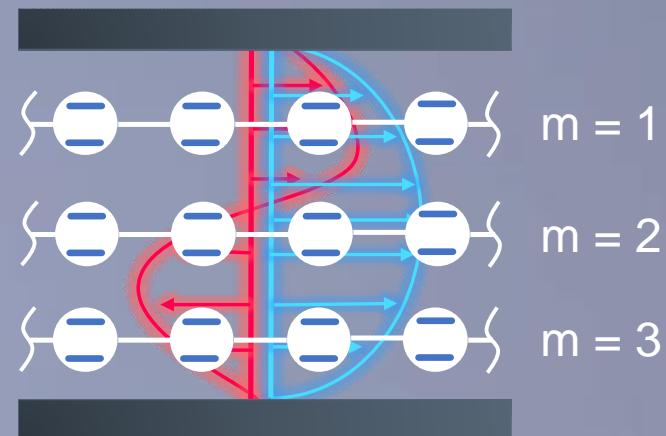
We have a simple microscopic understanding of this phenomena

Multilayer GTC Hamiltonian

$$\hat{H}_{\text{LM}} = \sum_k \hat{c}_{k_x,m}^\dagger \hat{c}_{k_x,m} \epsilon_k + \hat{a}_{k_x k_y}^\dagger \hat{a}_{k_x k_y} \omega_k + g \left(\hat{a}_{k_x k_y}^\dagger \hat{c}_{k_x,m} + \hat{c}_{k_x,m}^\dagger \hat{a}_{k_x k_y} \right) \sin k_y Y_m$$

$$= \sum_k \hat{H}_{k_x}$$

$$\begin{bmatrix} \hat{c}_{k_x,1}^\dagger & \dots & \hat{c}_{k_x,m}^\dagger \end{bmatrix} Q \times R \begin{bmatrix} \hat{a}_{k_x,1} \\ \vdots \\ \hat{a}_{k_x,m} \end{bmatrix}$$



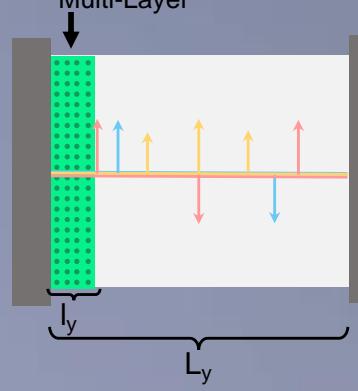
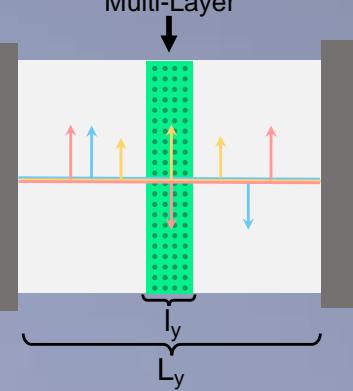
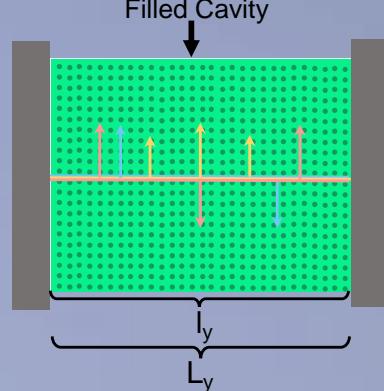
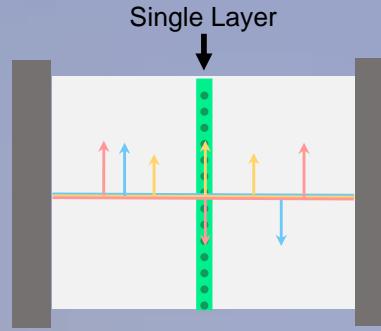
New Excitonic Operators

$$\begin{aligned}\hat{H}_{\text{LM}} &= \sum_k \hat{c}_{k_x,m}^\dagger \hat{c}_{k_x,m} \epsilon_k + \hat{a}_{k_x k_y}^\dagger \hat{a}_{k_x k_y} \omega_k + g \left(\hat{a}_{k_x k_y}^\dagger \hat{c}_{k_x,m} + \hat{c}_{k_x,m}^\dagger \hat{a}_{k_x k_y} \right) \sin k_y Y_m \\ &= \sum_k \hat{H}_{k_x}\end{aligned}$$

$$\begin{bmatrix} \hat{c}_{k_x,1}^\dagger & \dots & \hat{c}_{k_x,m}^\dagger \end{bmatrix} Q \times R \begin{bmatrix} \hat{a}_{k_x,1} \\ \vdots \\ \hat{a}_{k_x,m} \end{bmatrix}$$


For filled cavities $\hat{c}_{k_x,k_y}^\dagger$ operator only couple to $\hat{a}_{k_x k_y}$

Simple Matrix Models



ϵ	Ω_1	Ω_2	Ω_3	Ω_4	Ω_5
Ω_1	ω_{c_1}	0	0	0	0
Ω_2	0	ω_{c_2}	0	0	0
Ω_3	0	0	ω_{c_3}	0	0
Ω_4	0	0	0	ω_{c_4}	0
Ω_5	0	0	0	0	ω_{c_5}

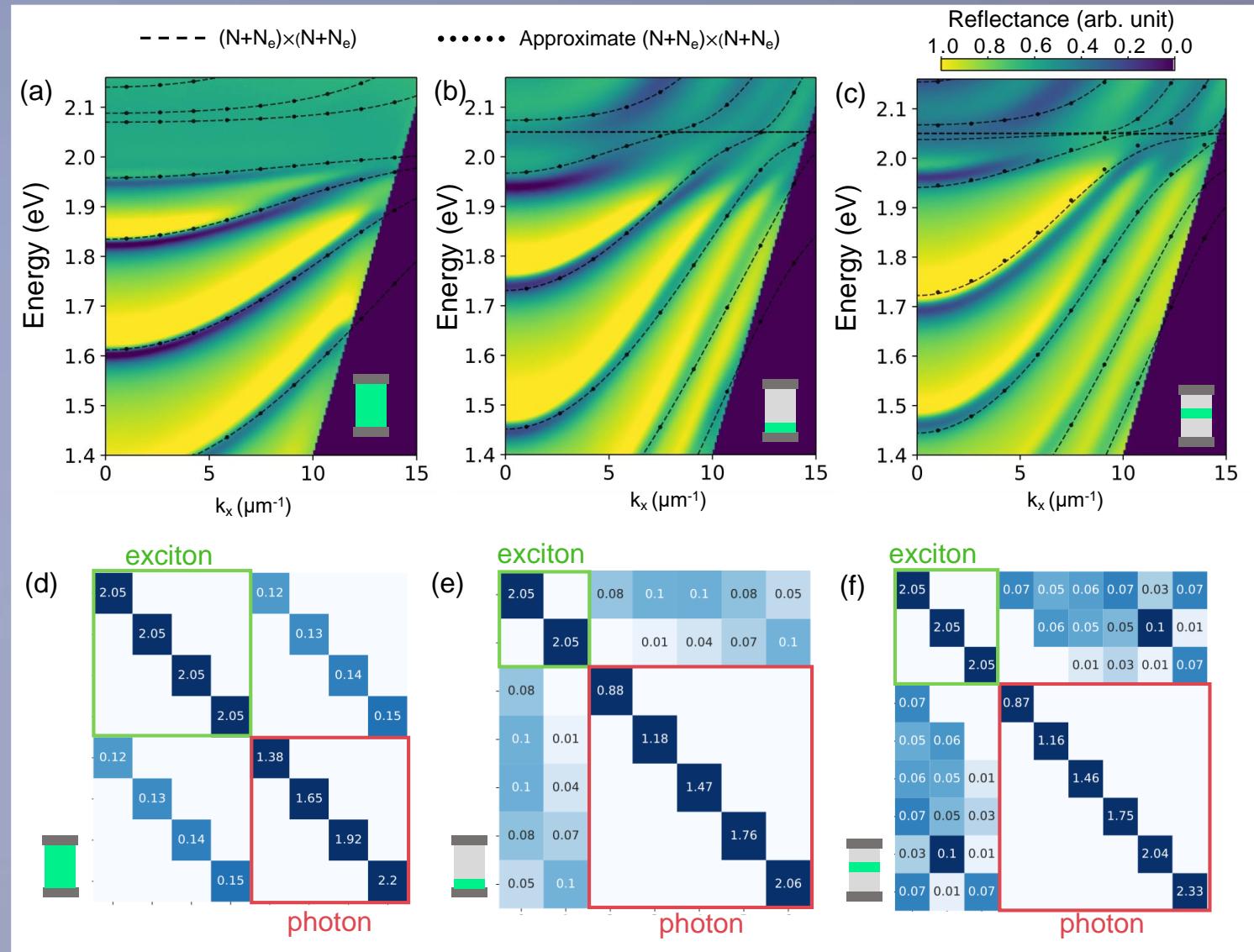
ϵ	Ω_1	0	0	0	0
Ω_1	ω_{c_1}	0	0	0	0
0	0	ϵ	Ω_2	0	0
0	0	Ω_2	ω_{c_2}	0	0
0	0	0	0	ϵ	Ω_3
0	0	0	0	Ω_3	ω_{c_3}

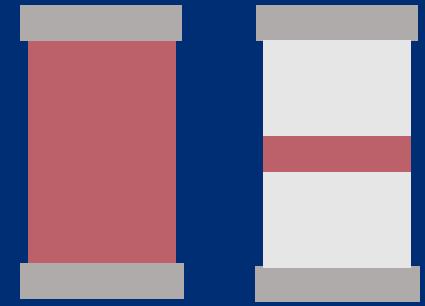
ϵ	Ω_1	Ω_3	0	0	0
Ω_1	ω_{c_1}	0	0	0	0
Ω_3	0	ω_{c_3}	0	0	0
0	0	0	ϵ	Ω_2	Ω_4
0	0	0	Ω_2	ω_{c_2}	0
0	0	0	Ω_4	0	ω_{c_4}

ϵ	Ω_1	Ω_2	Ω_3	Ω_4	Ω_5
Ω_1	ω_{c_1}	0	0	0	0
Ω_2	0	ω_{c_2}	0	0	0
Ω_3	0	0	ω_{c_3}	0	0
Ω_4	0	0	0	ω_{c_4}	0
Ω_5	0	0	0	0	ω_{c_5}

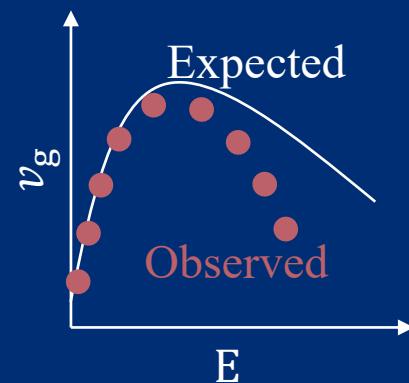
Comparing to Experiment

The theoretical models
predicts the experiment



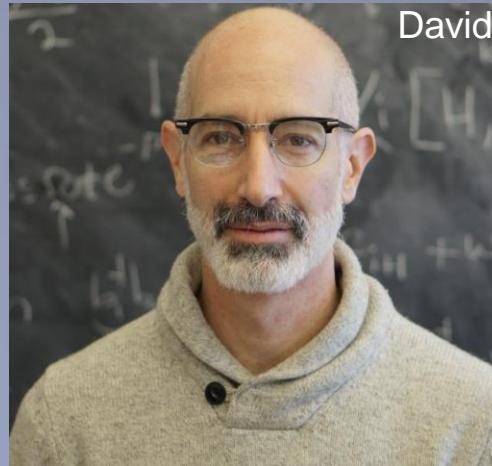
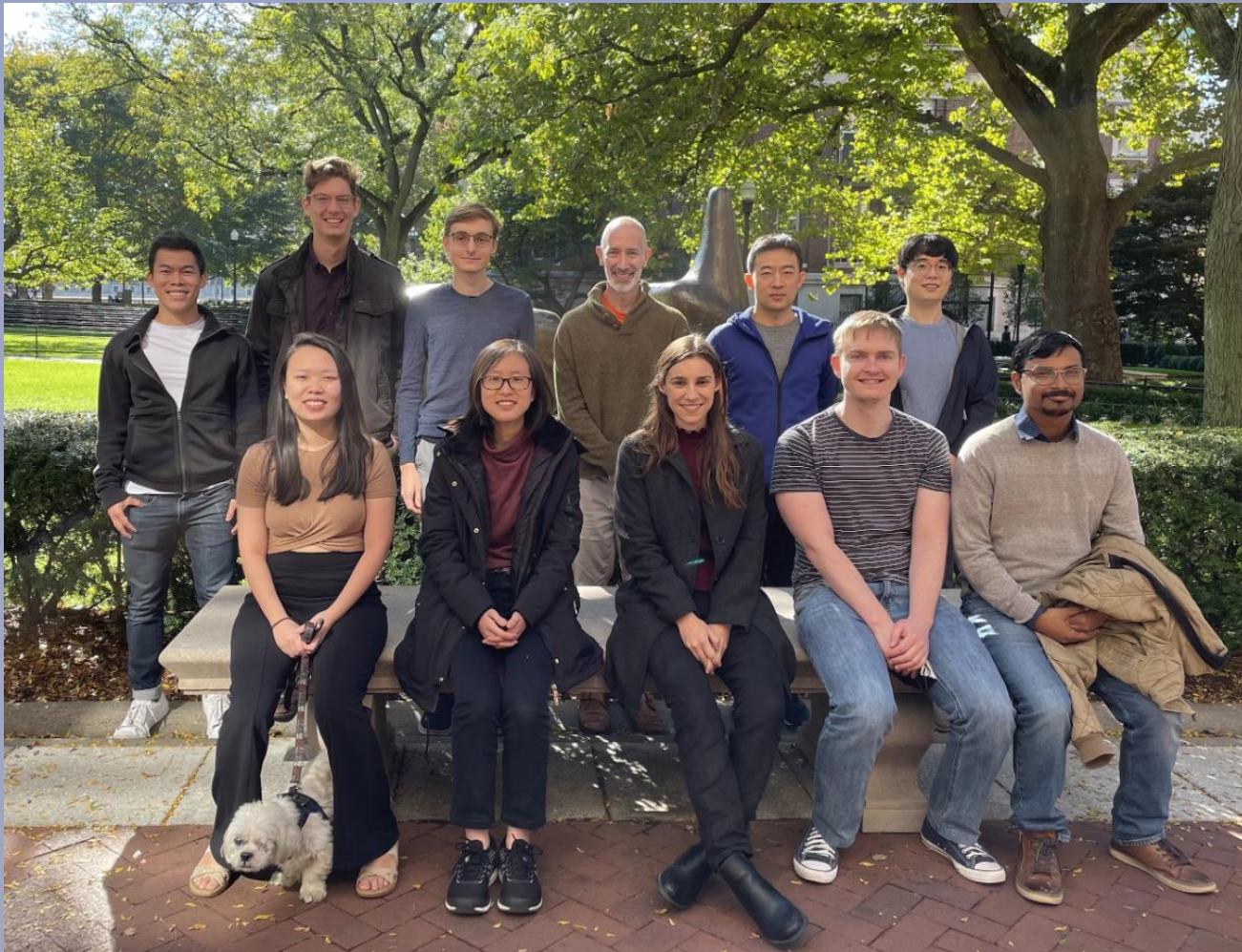


- For extended materials: $2N$ Hamiltonian (N = number of cavity mode branch) should be used.
- For arbitrary setup : $N+N_e$ Hamiltonian (N = number of cavity mode branch, $N_e < N$) should be used.



- We simulated exciton-polariton transport with Semi-classical approach.
- We find ballistic (Coherent) motion when exciton character is low. (< 40%)
- We find phonons can **rescale** group velocity through a transient localization mechanism.
- Coherence is long-lived (\sim ps) for low exciton character.

Acknowledgements



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