



# Towards more accessible excited-state simulations with AI

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Virtual International Seminar on Theory Advancement" (VISTA)  
20 March 2024

*dr-dral.com*

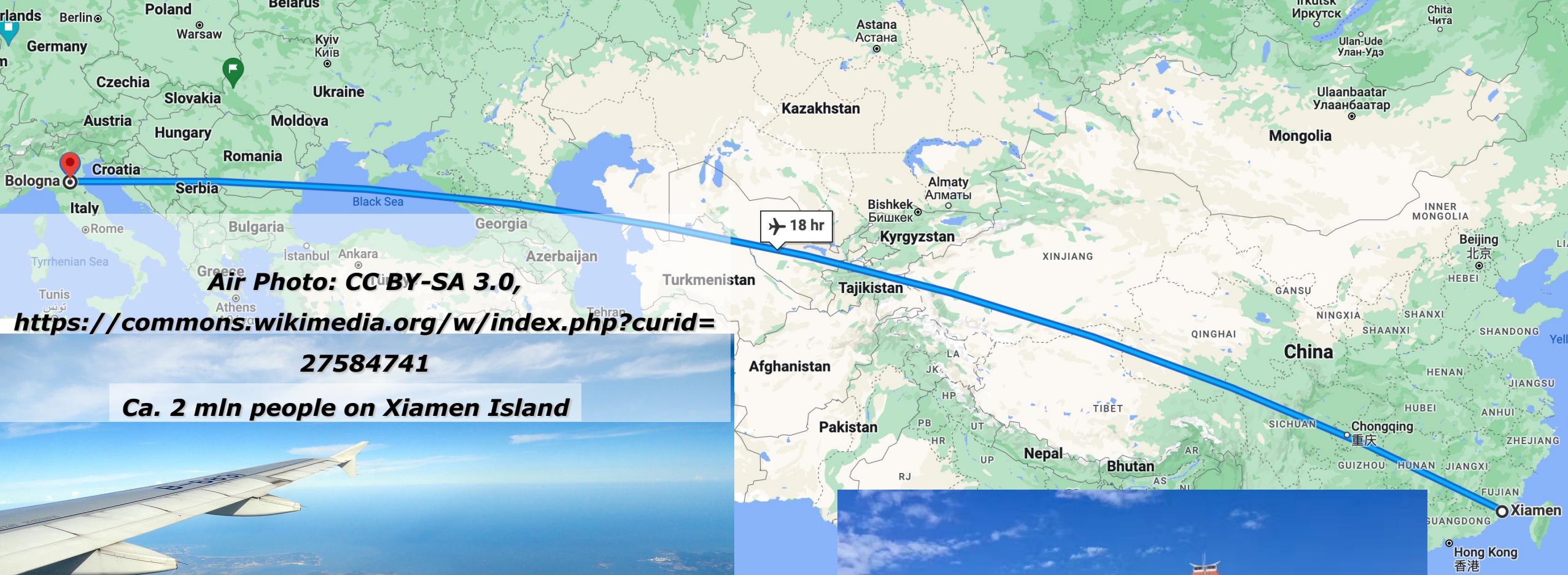
# **Group & Acknowledgements**

Hiring post-docs, PhD & MSc students!



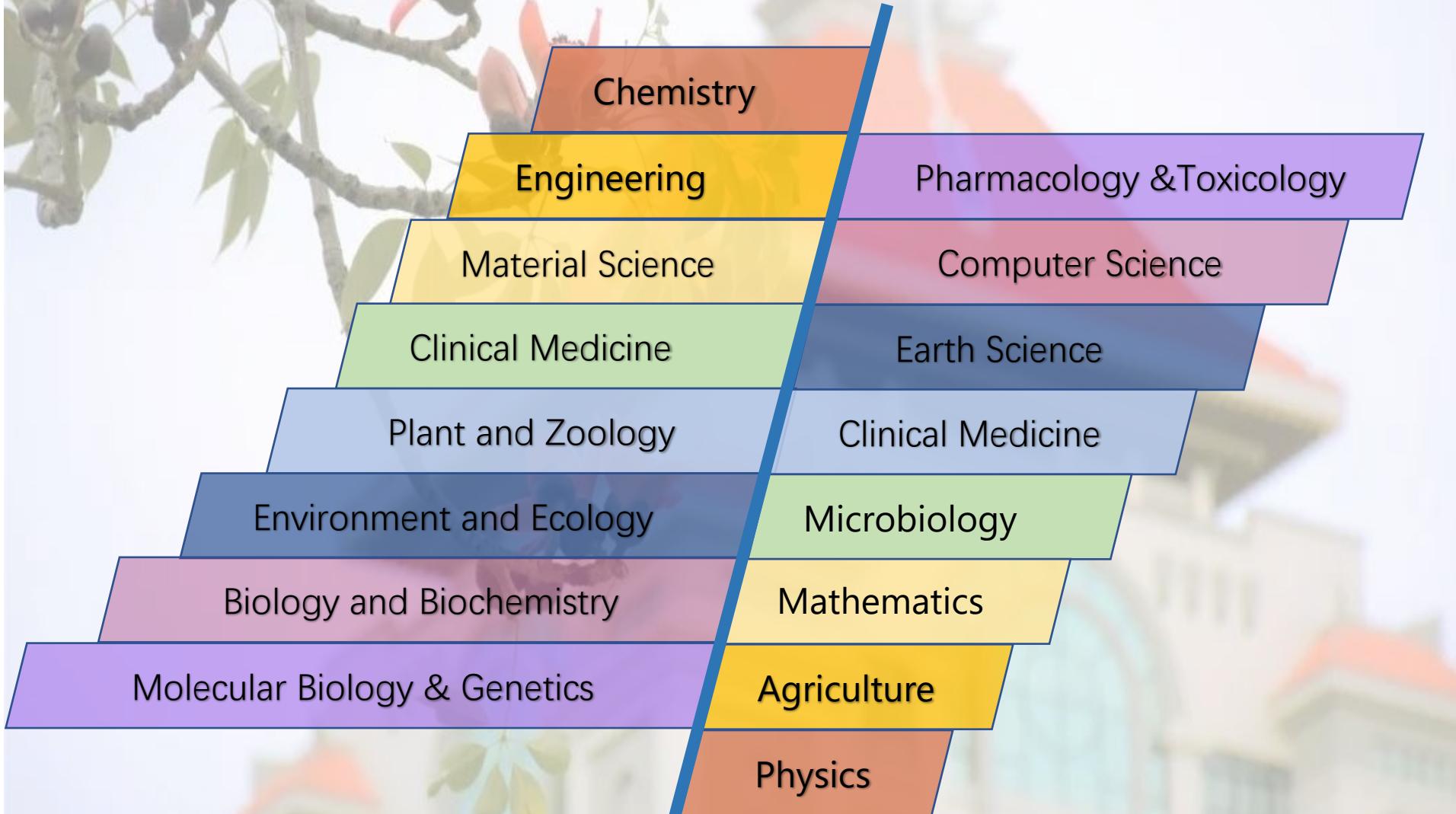
## **Funding**





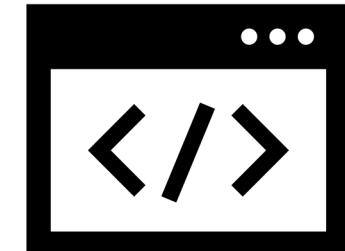
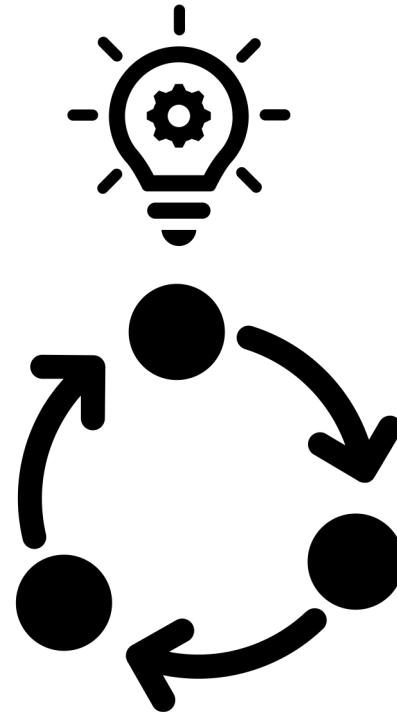
16 subjects rank top 1% globally. 11th in Mainland China.

Chemistry ranks top 1% globally (*ESI as of March 2019*).



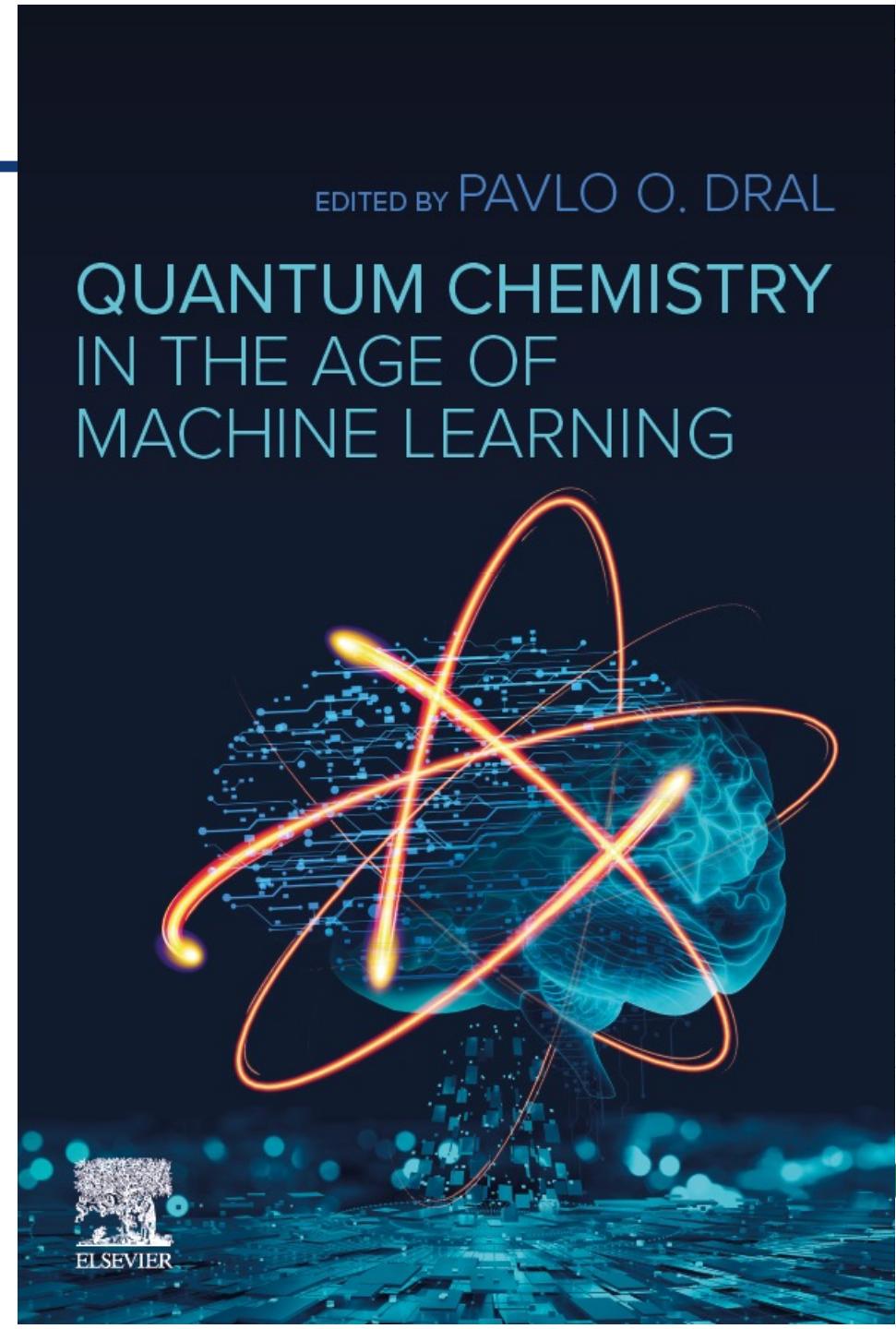
Develop AI methods and concepts to break the limitations of traditional quantum chemistry

Educate and promote



Provide tools

Published in  
September  
2022



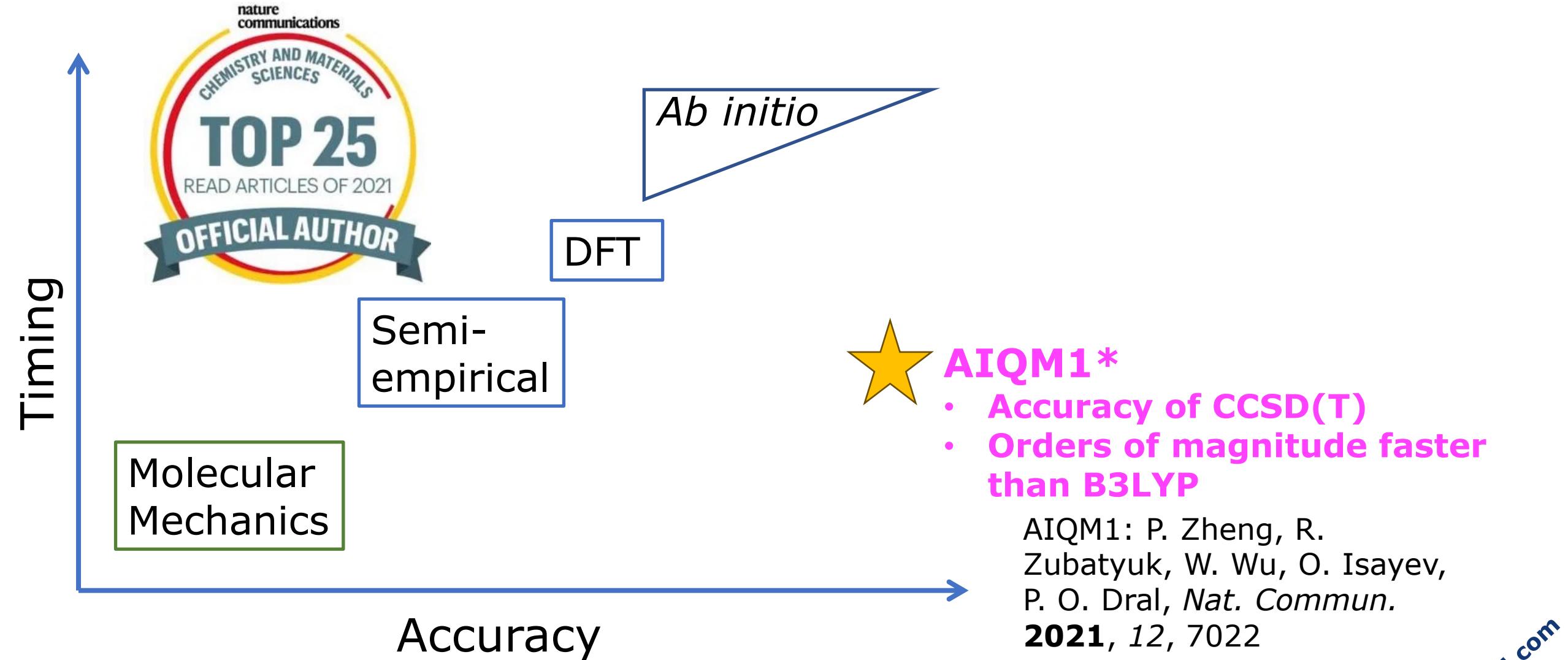
EDITED BY PAVLO O. DRAL

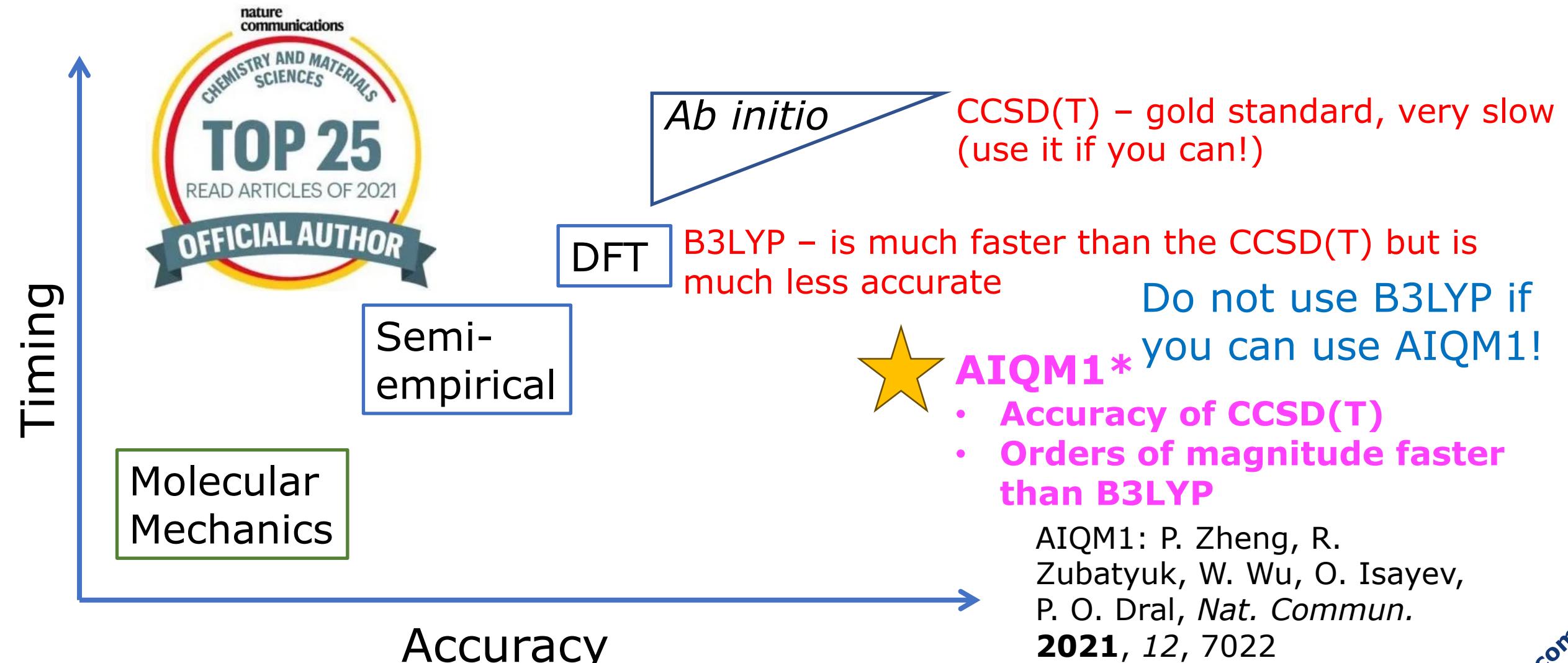
# QUANTUM CHEMISTRY IN THE AGE OF MACHINE LEARNING

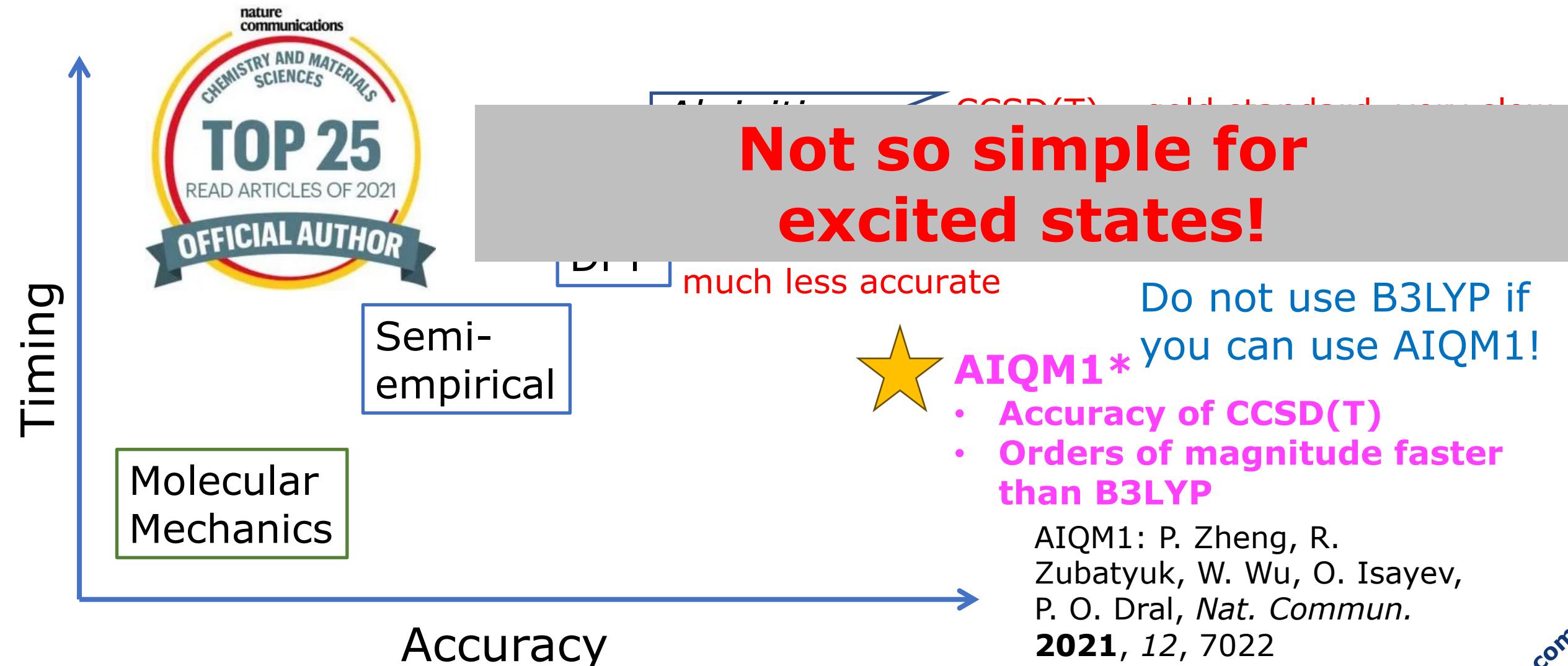
Chapter	Title
	Preface
<b>Part 1</b>	<b>Introduction</b>
1	Very brief introduction to quantum chemistry
2	Density functional theory
3	Semiempirical quantum mechanical methods
4	From small molecules to solid-state materials: A brief discourse on an example of carbon compounds
5	Basics of dynamics
6	Machine learning: An overview
7	Unsupervised learning
8	Neural networks
9	Kernel methods
10	Bayesian inference
<b>Part 2</b>	<b>Machine learning potentials</b>
11	Potentials based on linear models
12	Neural network potentials
13	Kernel method potentials
14	Constructing machine learning potentials with active learning
15	Excited-state dynamics with machine learning
16	Machine learning for vibrational spectroscopy
17	Molecular structure optimizations with Gaussian process regression
<b>Part 3</b>	<b>Machine learning of quantum chemical properties</b>
18	Learning electron densities
19	Learning dipole moments and polarizabilities
20	Learning excited-state properties
<b>Part 4</b>	<b>Machine learning-improved quantum chemical methods</b>
21	Learning from multiple quantum chemical methods: $\Delta$ -learning, transfer learning, co-kriging, and beyond
22	Data-driven acceleration of coupled-cluster and perturbation theory methods
23	Redesigning density functional theory with machine learning
24	Improving semiempirical quantum mechanical methods with machine learning
25	Machine learning wavefunction
<b>Part 5</b>	<b>Analysis of Big Data</b>
26	Analysis of nonadiabatic molecular dynamics trajectories
27	Design of organic materials with tailored optical properties: Predicting quantum-chemical polarizabilities and derived quantities

65  
authors!

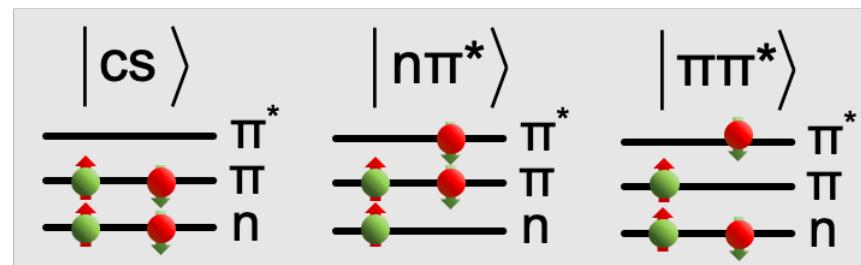
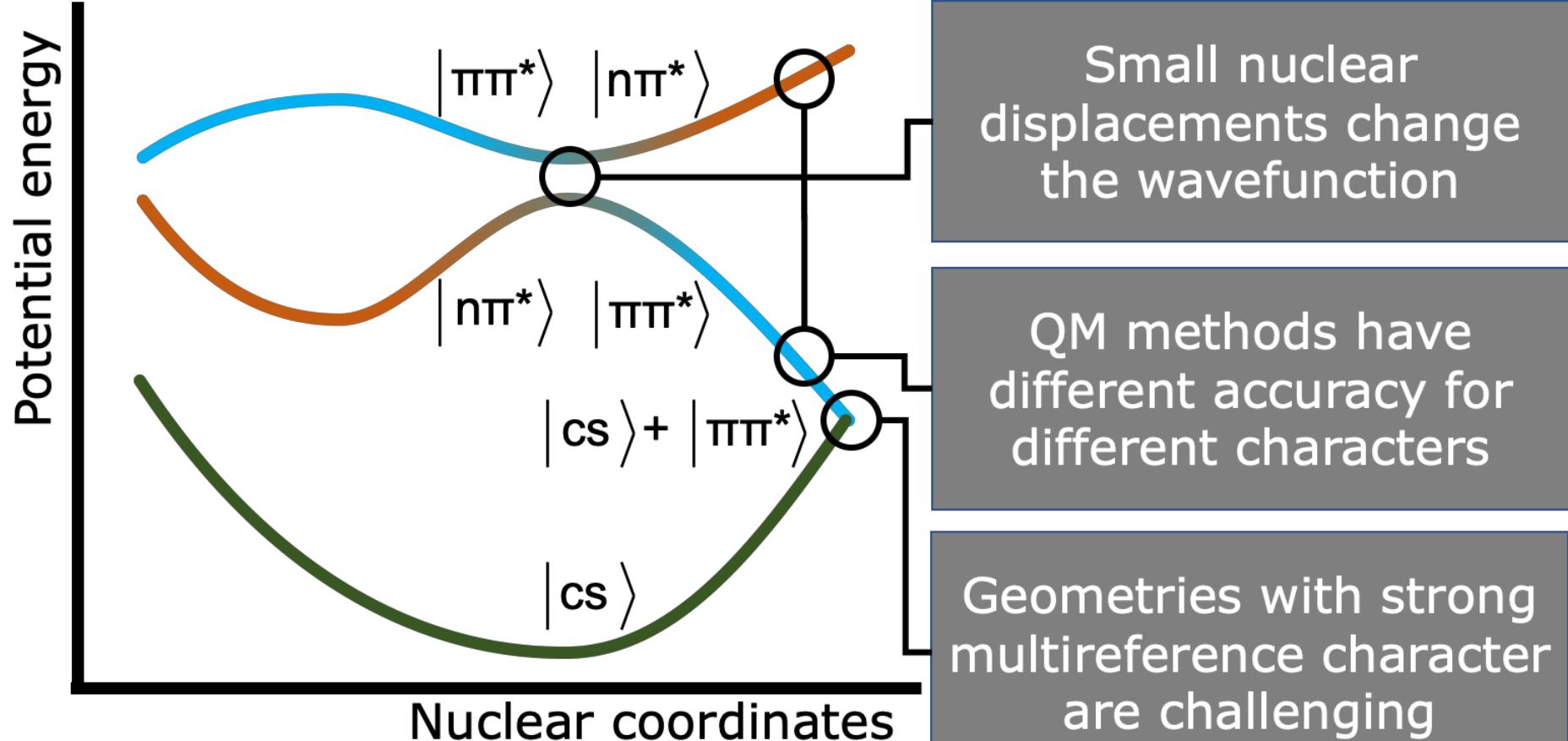
Exercises  
on GitHub



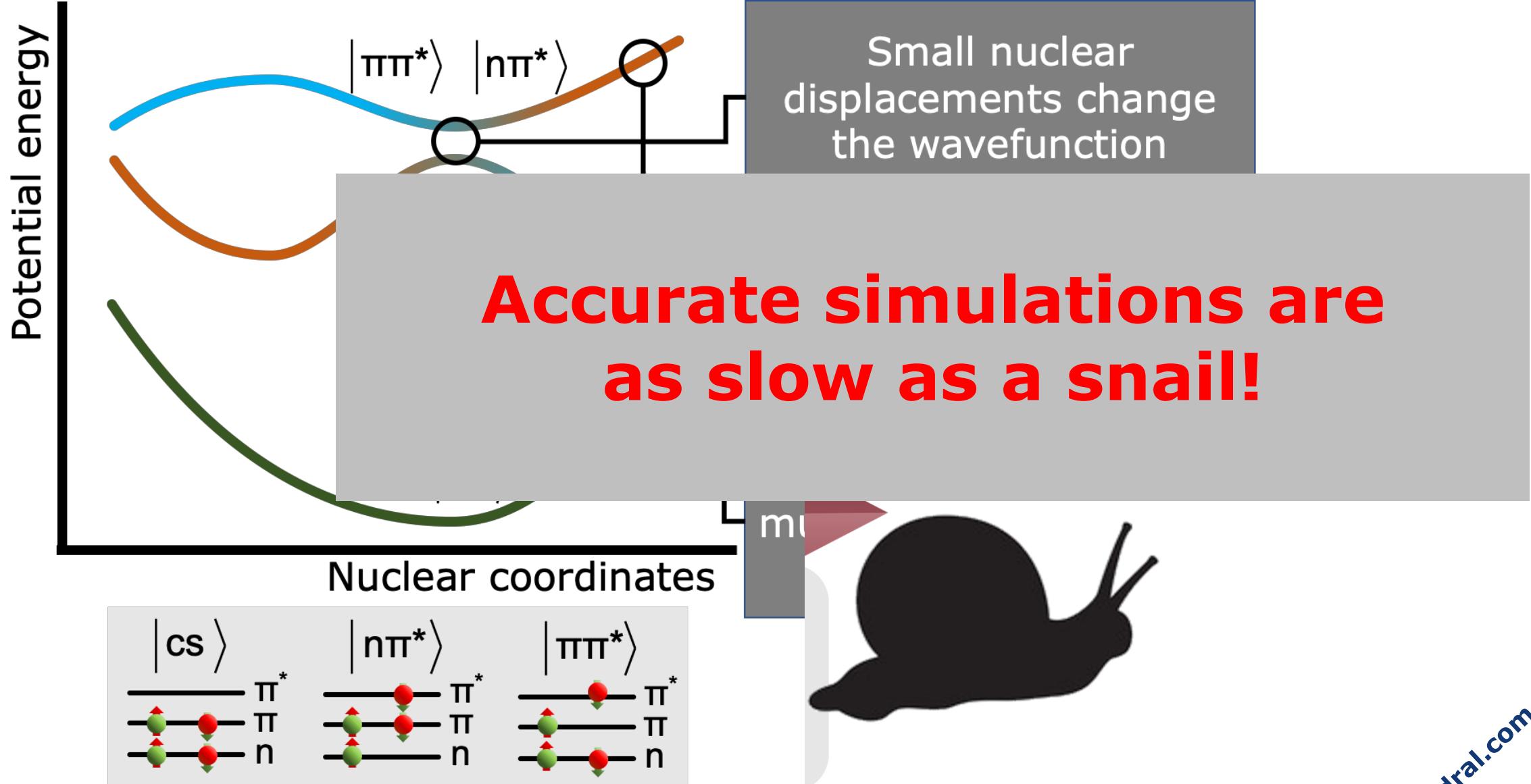




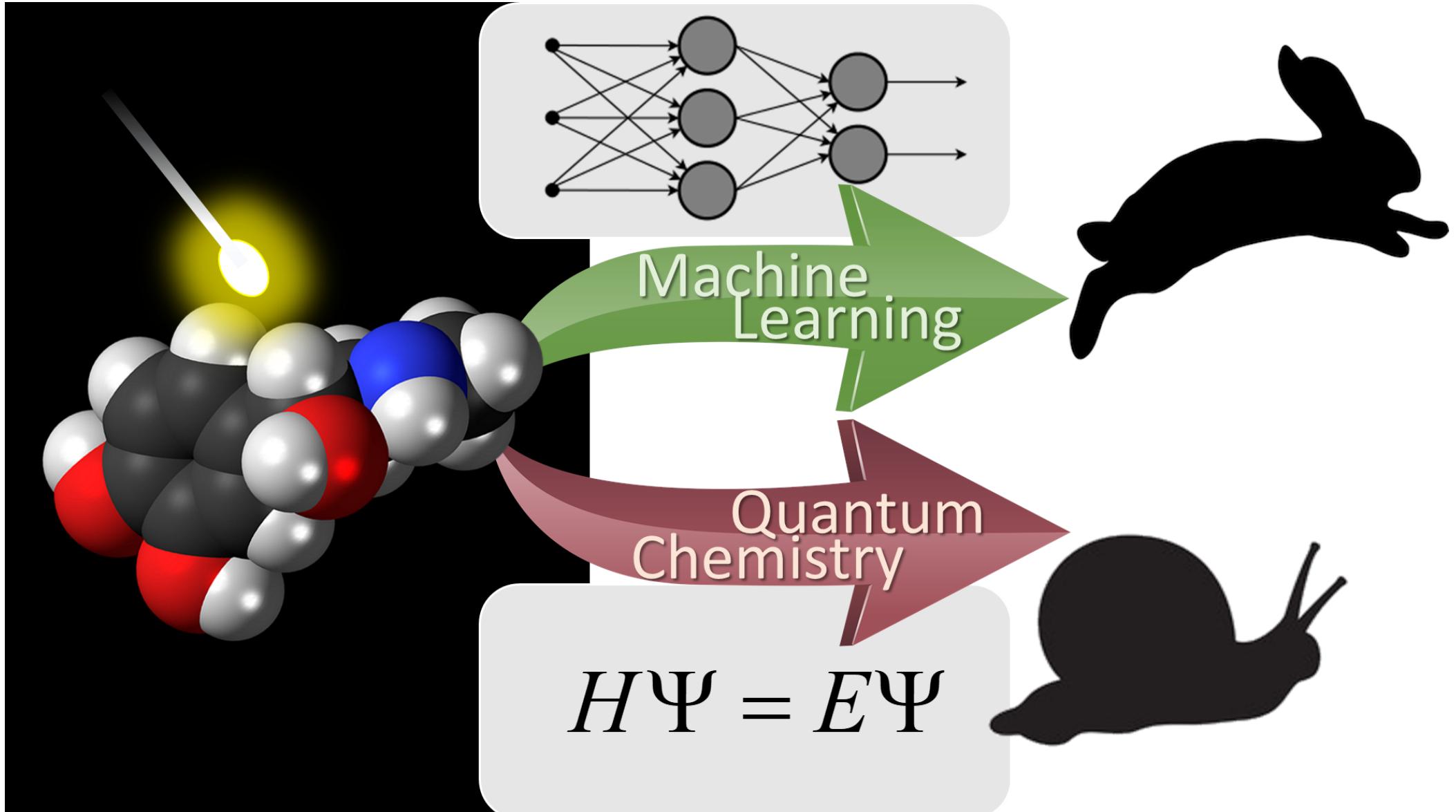
# Why excited states are challenging



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# Why excited states are challenging



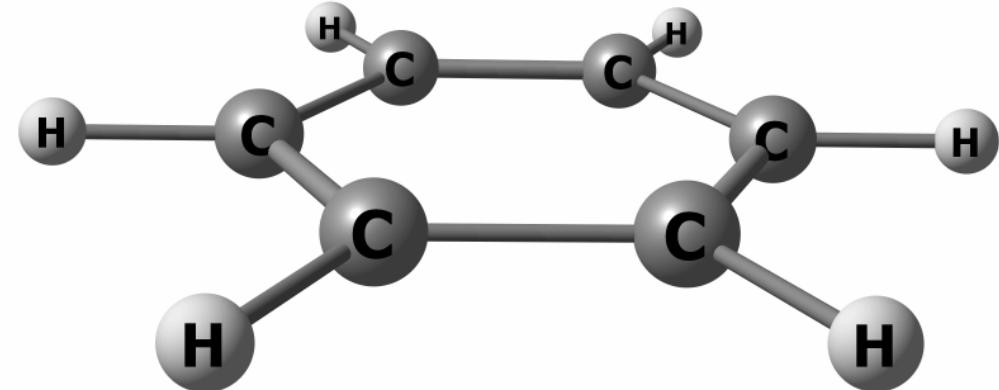
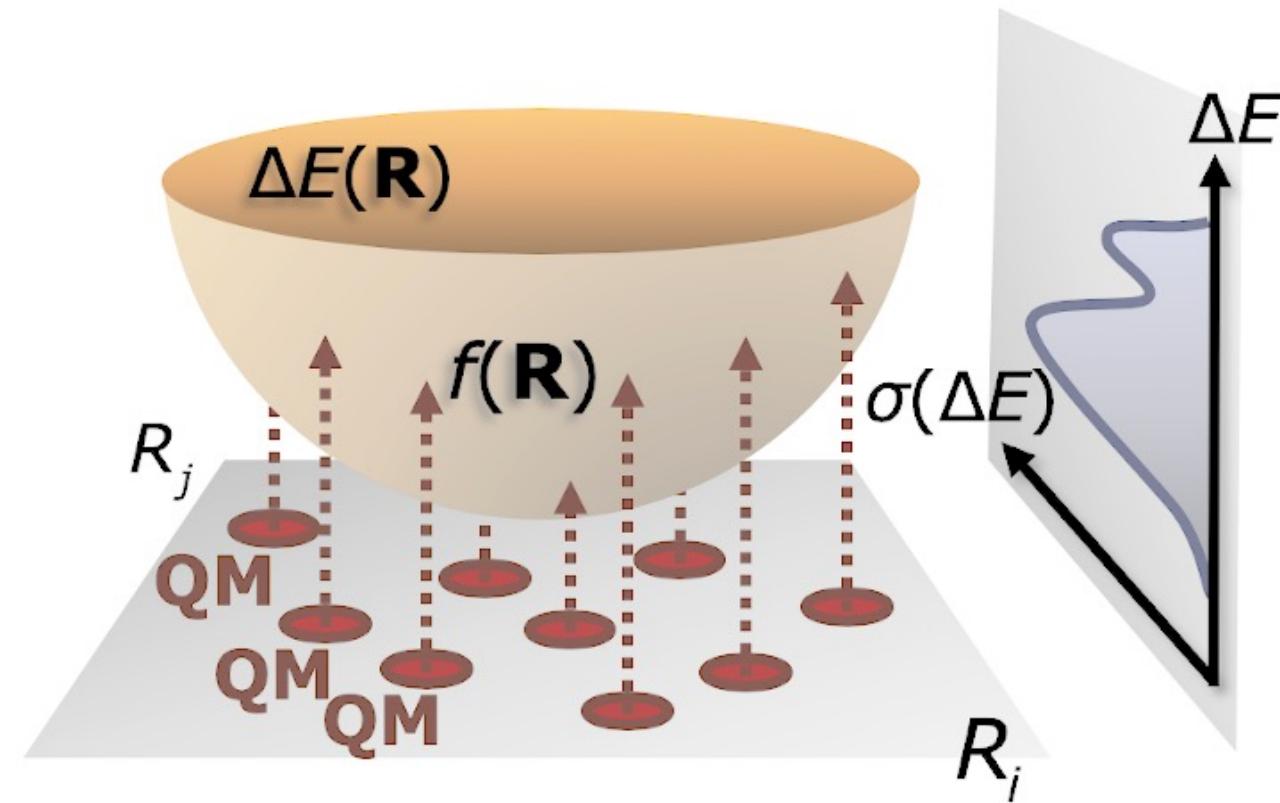
Conventional programming in quantum chemistry:

- Code for molecular orbitals
- Code for excitation energies
- Code for oscillator strengths
- ...

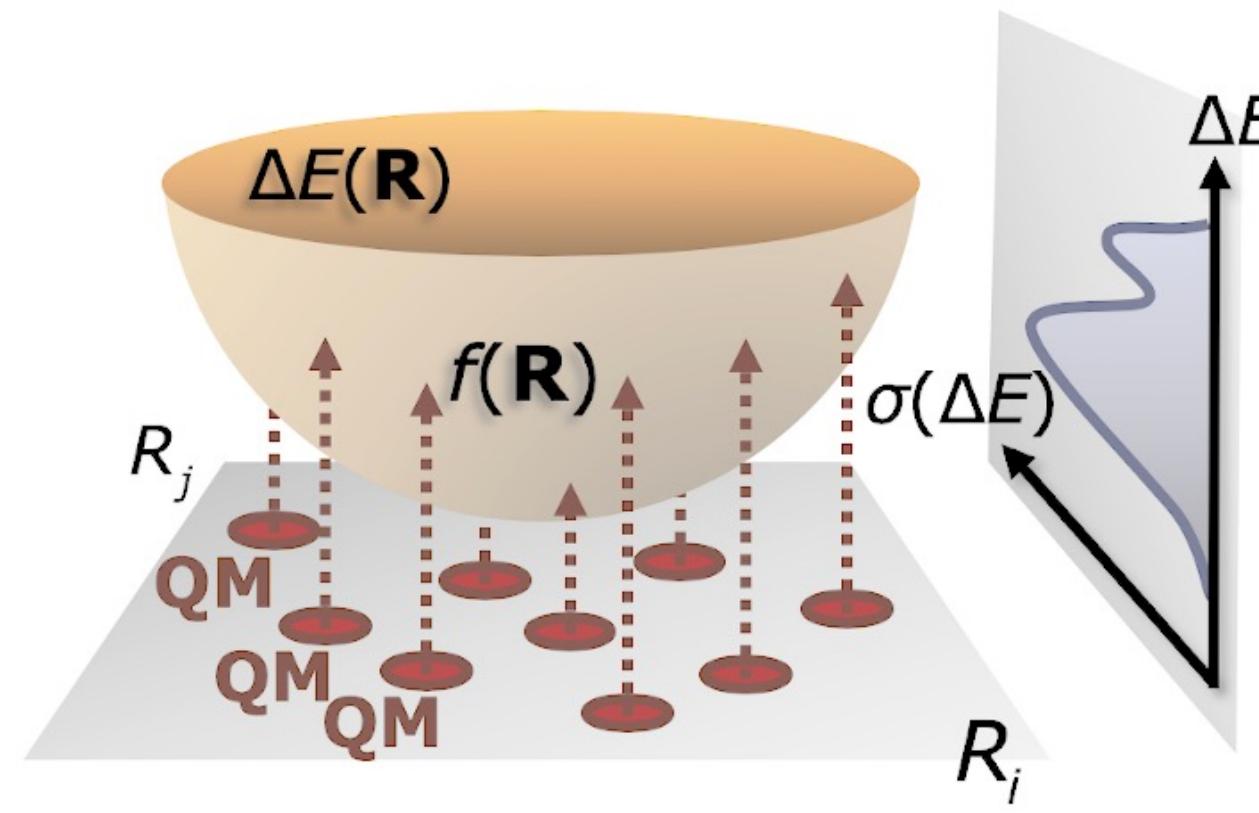
Machine learning (in principle – adaptations required!):

- The same code for all above
- ↑                   ↑                   ↑  
MOs           excitation energies      Oscillator strength  
Training data

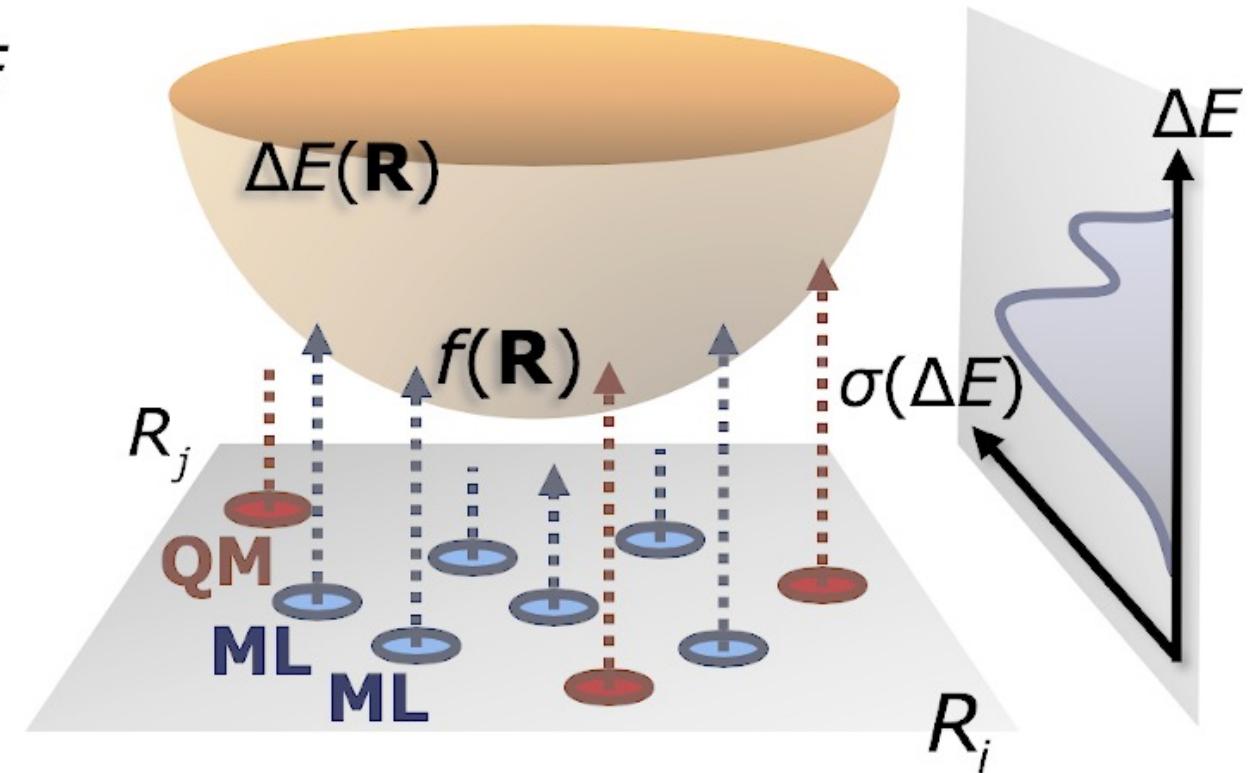
$N$  QM calculations are needed to simulate spectrum



$N$  QM calculations are needed to simulate spectrum



With ML, only  $M \ll N$  QM calculations are needed



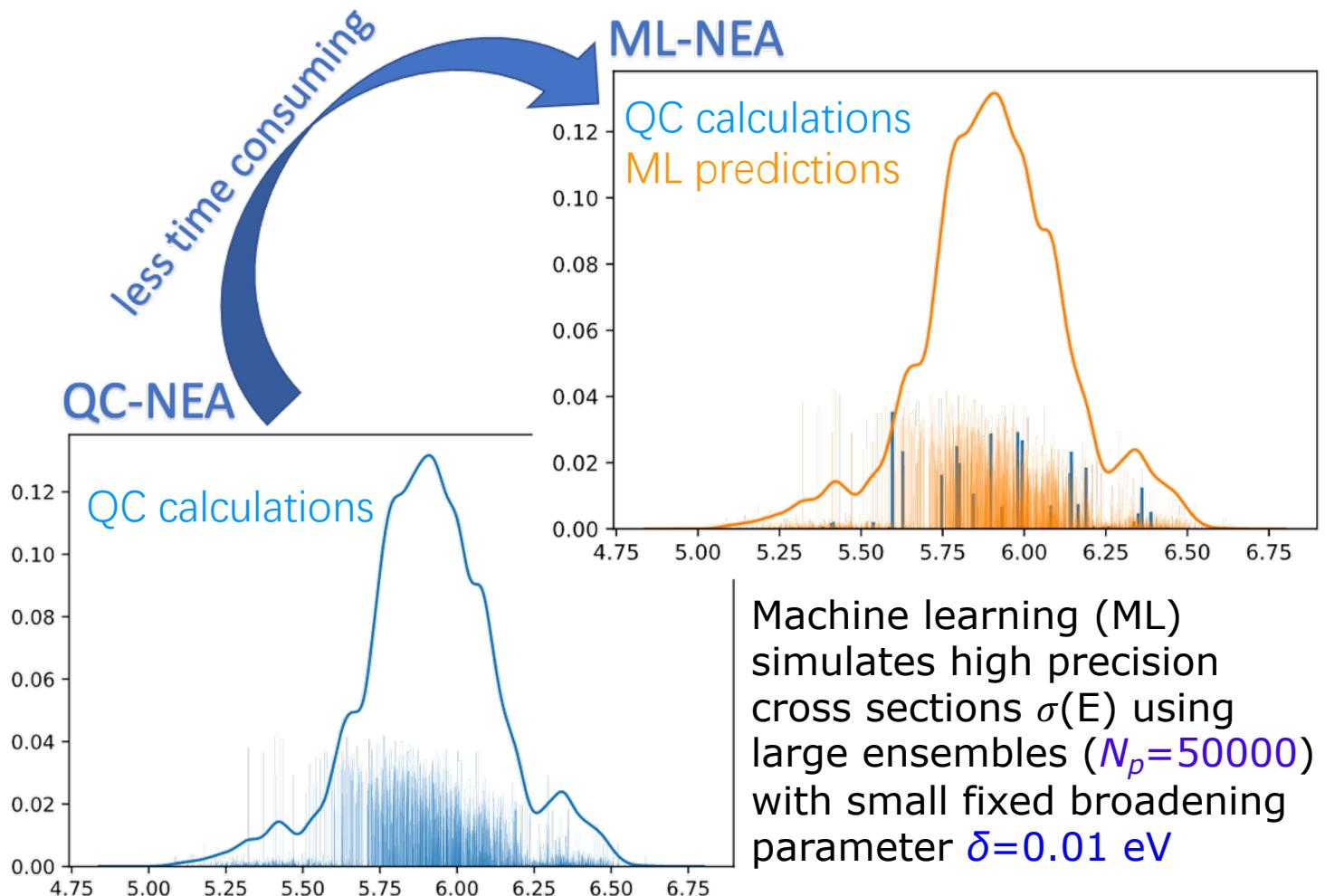
Learned properties:

- excitation energies

$$\Delta E_{0n}(\mathbf{x}_i)$$

- Oscillator strengths

$$f_{0n}(\mathbf{x}_i)$$



$$\sigma(E) = \frac{\pi e^2 h}{2mc\varepsilon_0 E} \sum_n^{N_{fs}} \frac{1}{N_p} \sum_i^{N_p} \Delta E_{0n}(\mathbf{x}_i) f_{0n}(\mathbf{x}_i) \frac{1}{\sqrt{2\pi(\delta/2)^2}} \exp\left(-\frac{(E - \Delta E_{0n})^2}{2(\delta/2)^2}\right)$$

# The KREG model

$$f(\mathbf{x}_i) = \sum_{j=1}^{N_{\text{tr}}} \alpha_j k(\mathbf{x}_i, \mathbf{x}_j)$$

$$k(\mathbf{x}_i, \mathbf{x}_j) = \exp\left(-\frac{1}{2\sigma^2} \sum_s (x_{i,s} - x_{j,s})^2\right)$$

the Gaussian kernel function  
( $\sigma$  is the kernel width)

$$\mathbf{x} = \left( \dots \quad \frac{R^{eq}}{R} \quad \dots \right)^T$$

RE descriptor

Analytical solution for the regression coefficients  $\alpha$  given  $N_{\text{tr}}$  training points

$$\begin{pmatrix} k(\mathbf{x}_1, \mathbf{x}_1) + \lambda & \cdots & k(\mathbf{x}_1, \mathbf{x}_{N_{\text{tr}}}) \\ \vdots & \ddots & \vdots \\ k(\mathbf{x}_{N_{\text{tr}}}, \mathbf{x}_1) & \cdots & k(\mathbf{x}_{N_{\text{tr}}}, \mathbf{x}_{N_{\text{tr}}}) + \lambda \end{pmatrix} \begin{pmatrix} \alpha_1 \\ \vdots \\ \alpha_{N_{\text{tr}}} \end{pmatrix} = \begin{pmatrix} y_1 \\ \vdots \\ y_{N_{\text{tr}}} \end{pmatrix}$$

$(\mathbf{K} + \lambda \mathbf{I})\alpha = \mathbf{y}$

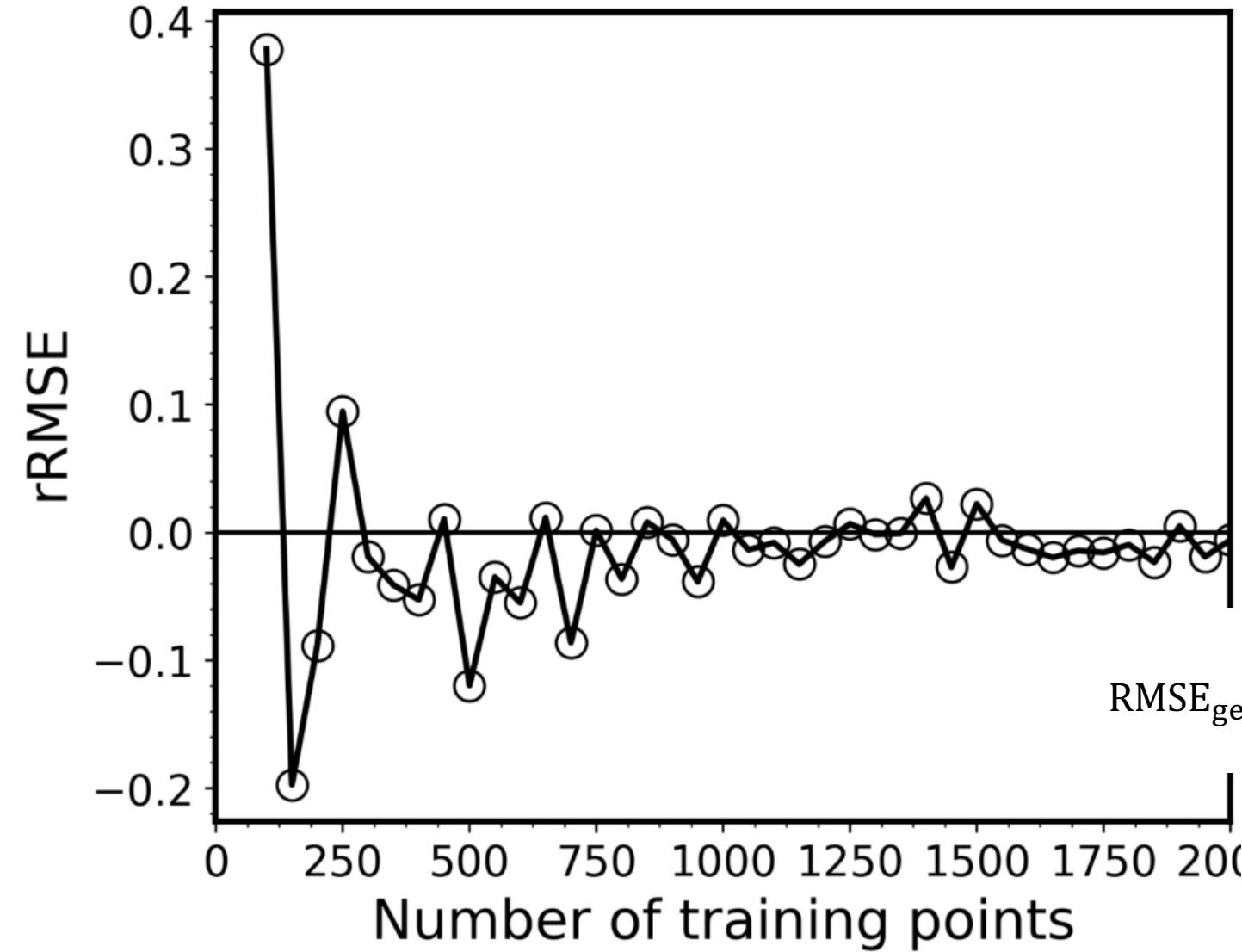
$\lambda$  is the regularization parameter  
ensuring transferability

Sub-training set Validate

for tuning  
hyperparameters

The **KREG** model (Kernel ridge regression [KRR] with **RE** descriptor and the **Gaussian** kernel function; RE descriptor stands for Internuclear distances Relative to Equilibrium) to complete all the ML tasks.

Train

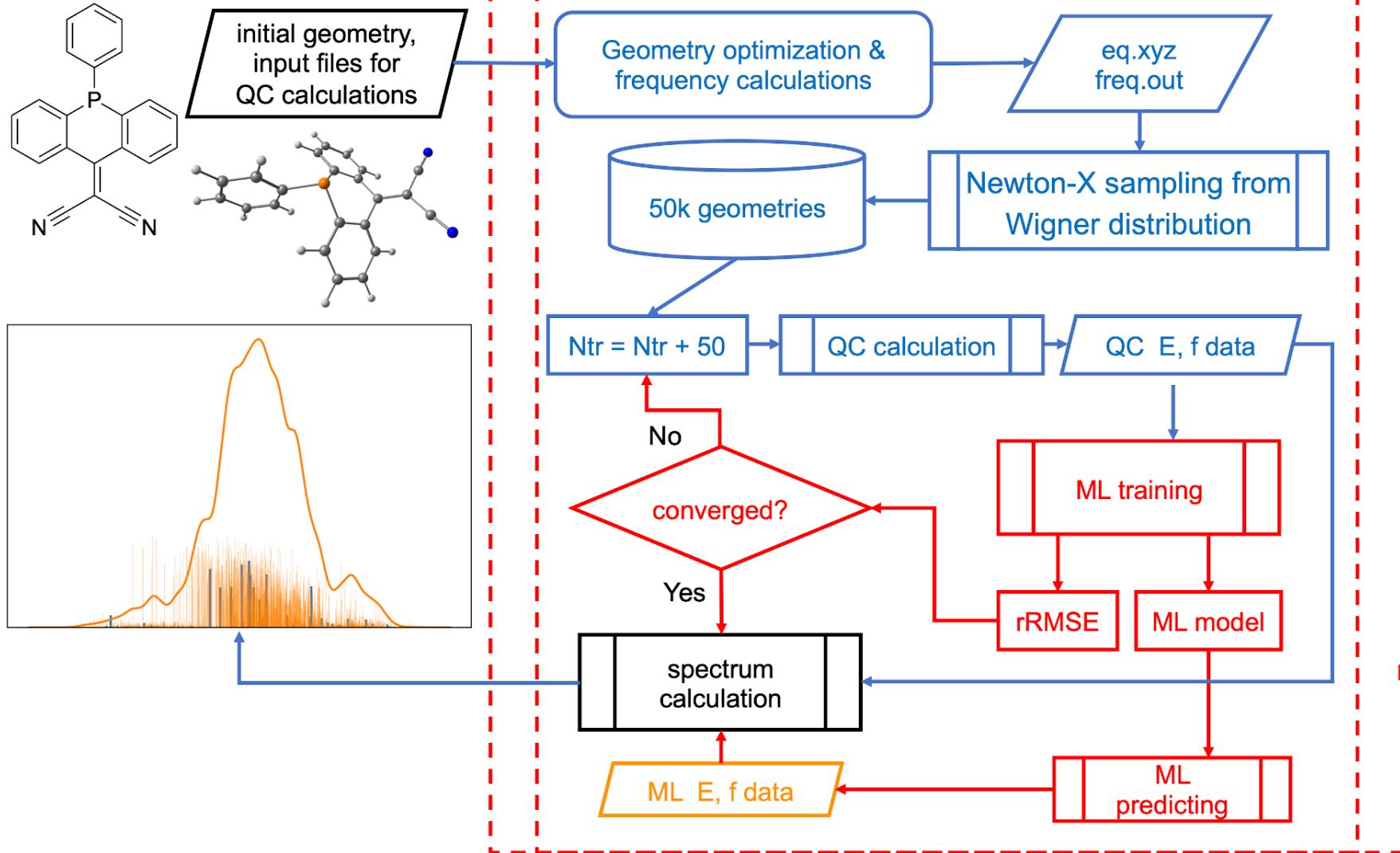


Optimal number of training points can be determined automatically using iterative procedure that stops after the relative change in ML validation errors drops below the threshold (typically  $r\text{RMSE} < 0.1$ ).

$$r\text{RMSE} = \frac{RMSE_{geom}(N_{tr}) - RMSE_{geom}(N_{tr} - N_{step})}{RMSE_{geom}(N_{tr})}$$

$$RMSE_{geom}(N_{tr}) = \sqrt[2N_S]{\prod_{i=1}^{N_S} RMSE_{\Delta E_{0n}}(N_{tr}) \cdot RMSE_{f_{0n}}(N_{tr})}$$

# Machine learning single-photon absorption spectra



Mario  
Barbatti

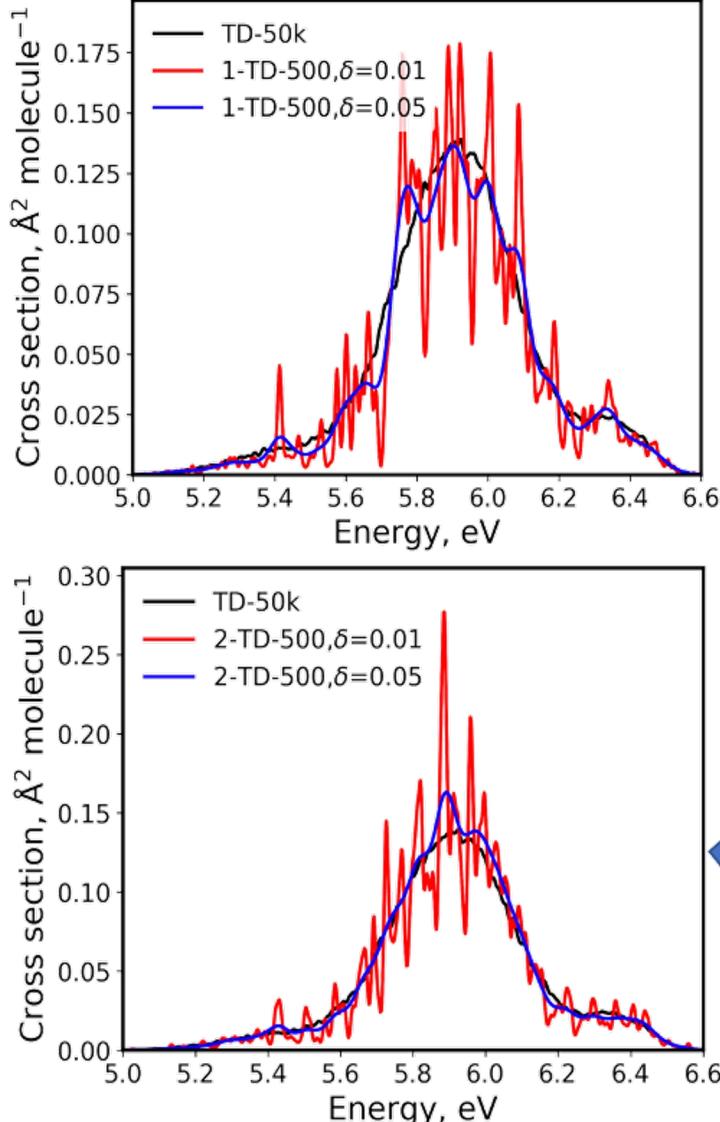


Bao-Xin  
Xue

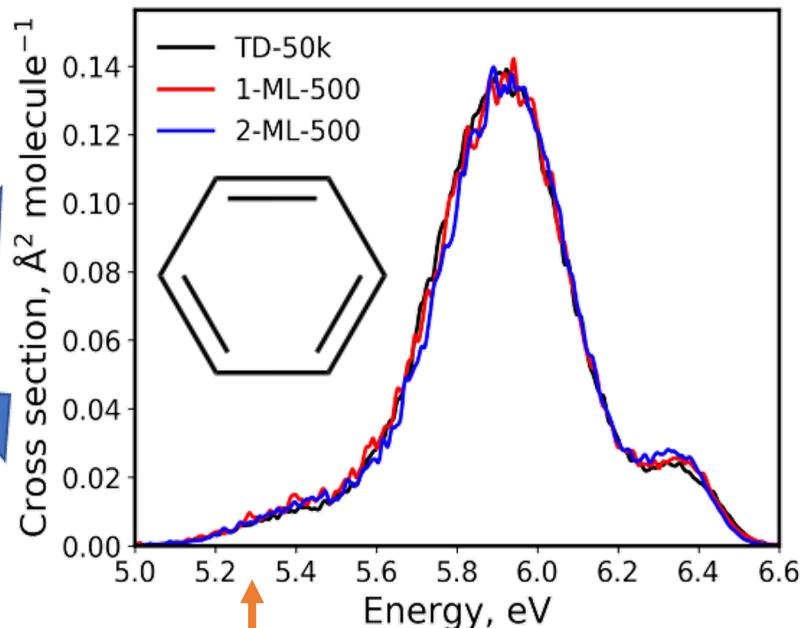
ML-NEA method: B.-X. Xue, P. O. Dral, M. Barbatti, *J. Phys. Chem. A* **2020**, 124, 7199–7210

Implementation in MLatom: P. O. Dral, F. Ge, B.-X. Xue, Y.-F. Hou, M. Pinheiro Jr, J. Huang, M. Barbatti, *Top. Curr. Chem.*, **2021**, 379, 27

# High-precision spectra of benzene

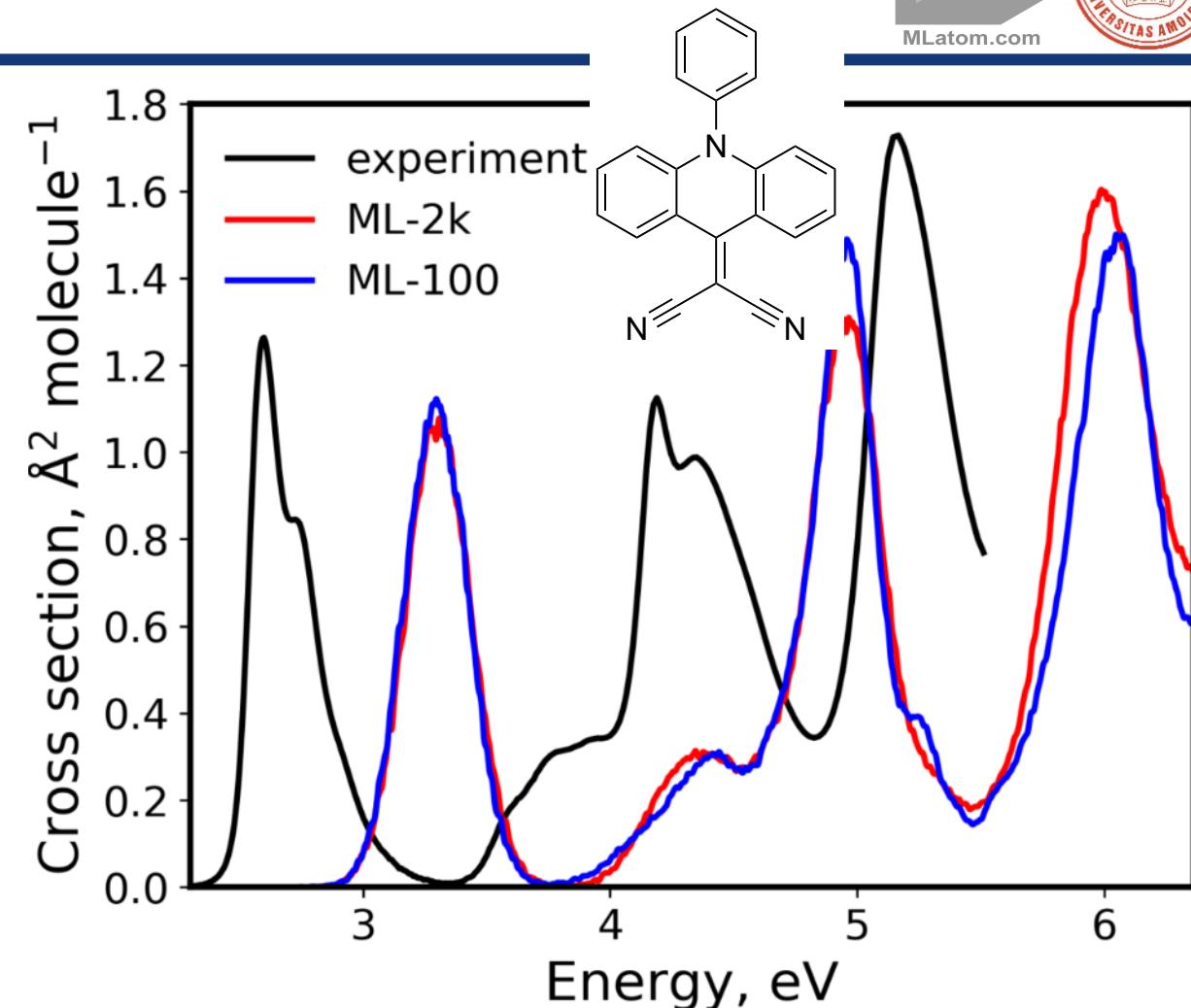
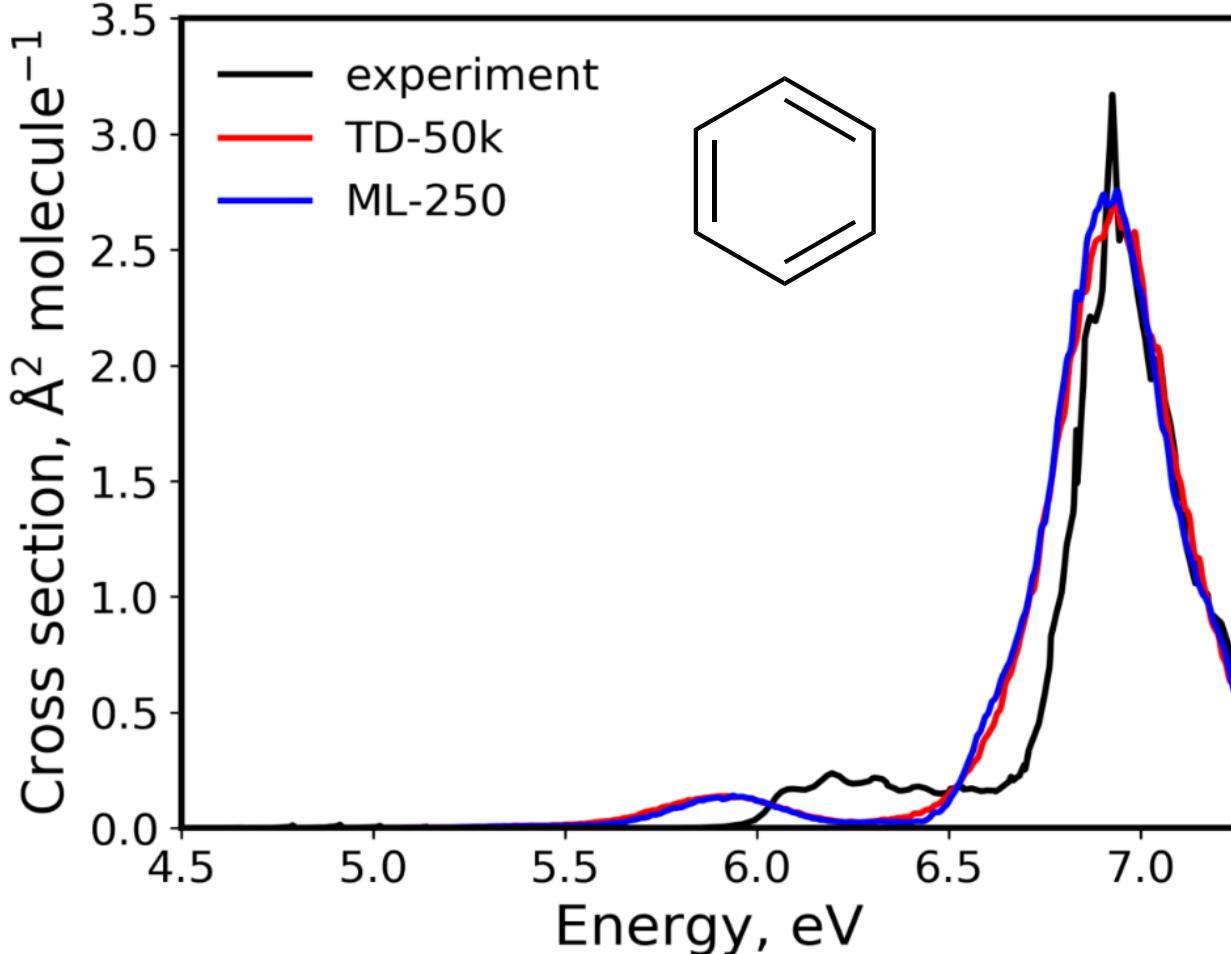


Two different medium-sized ensembles of the same size (500 points) sampled from a Wigner distribution give very different spectra at QC level

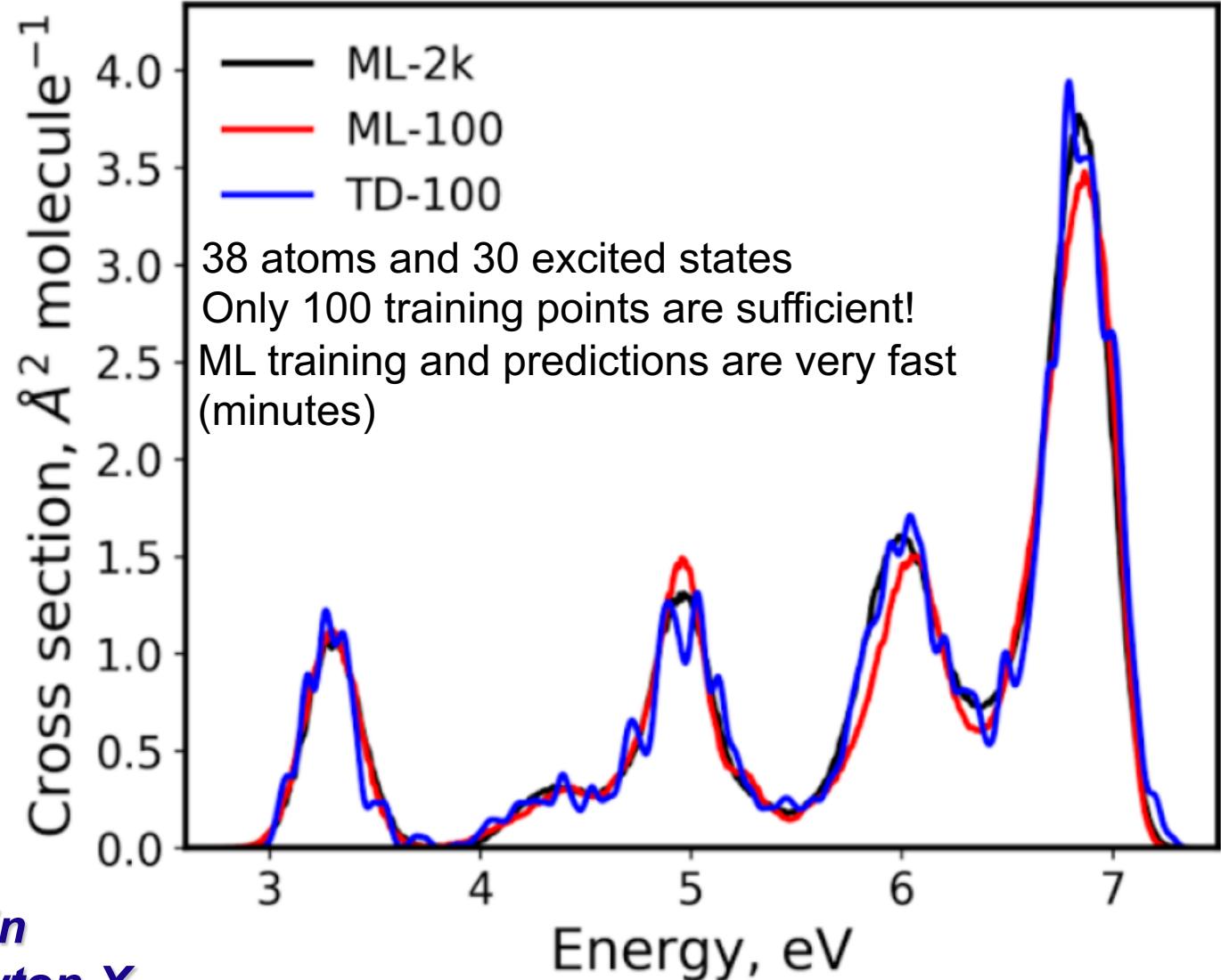
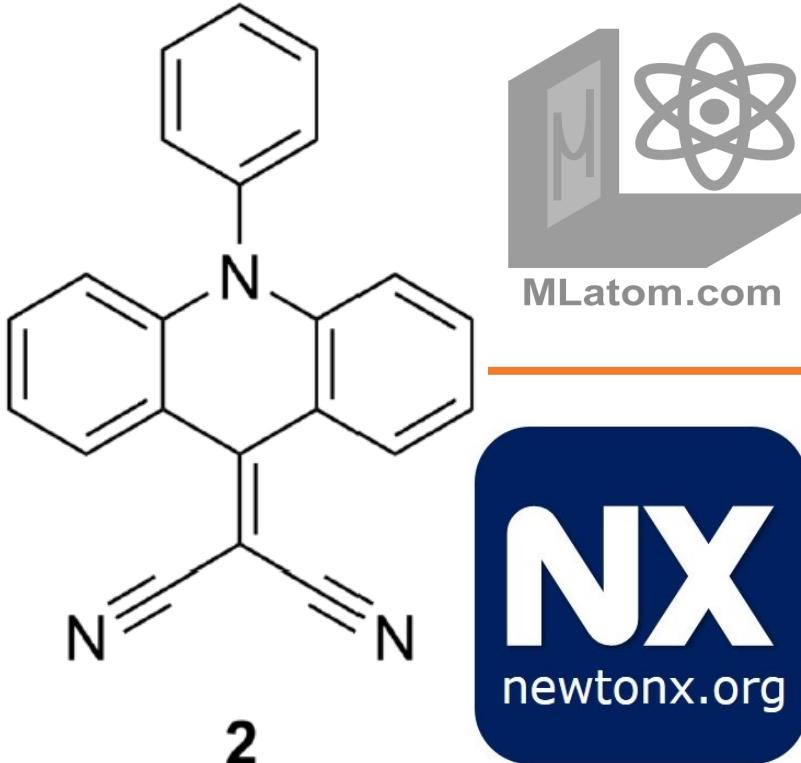


ML trained on both QC ensembles considerably improves precision of spectra that are very similar to each other

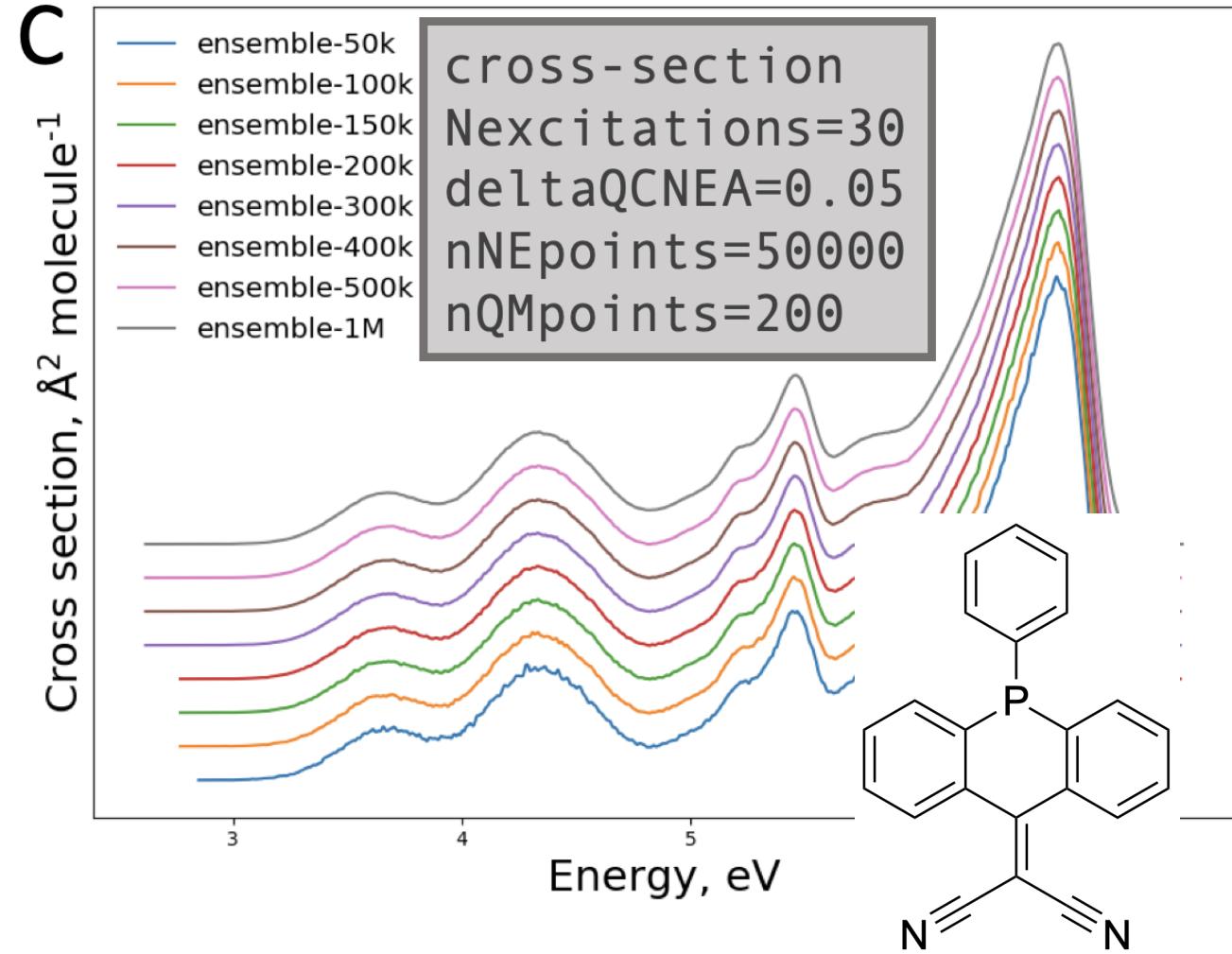
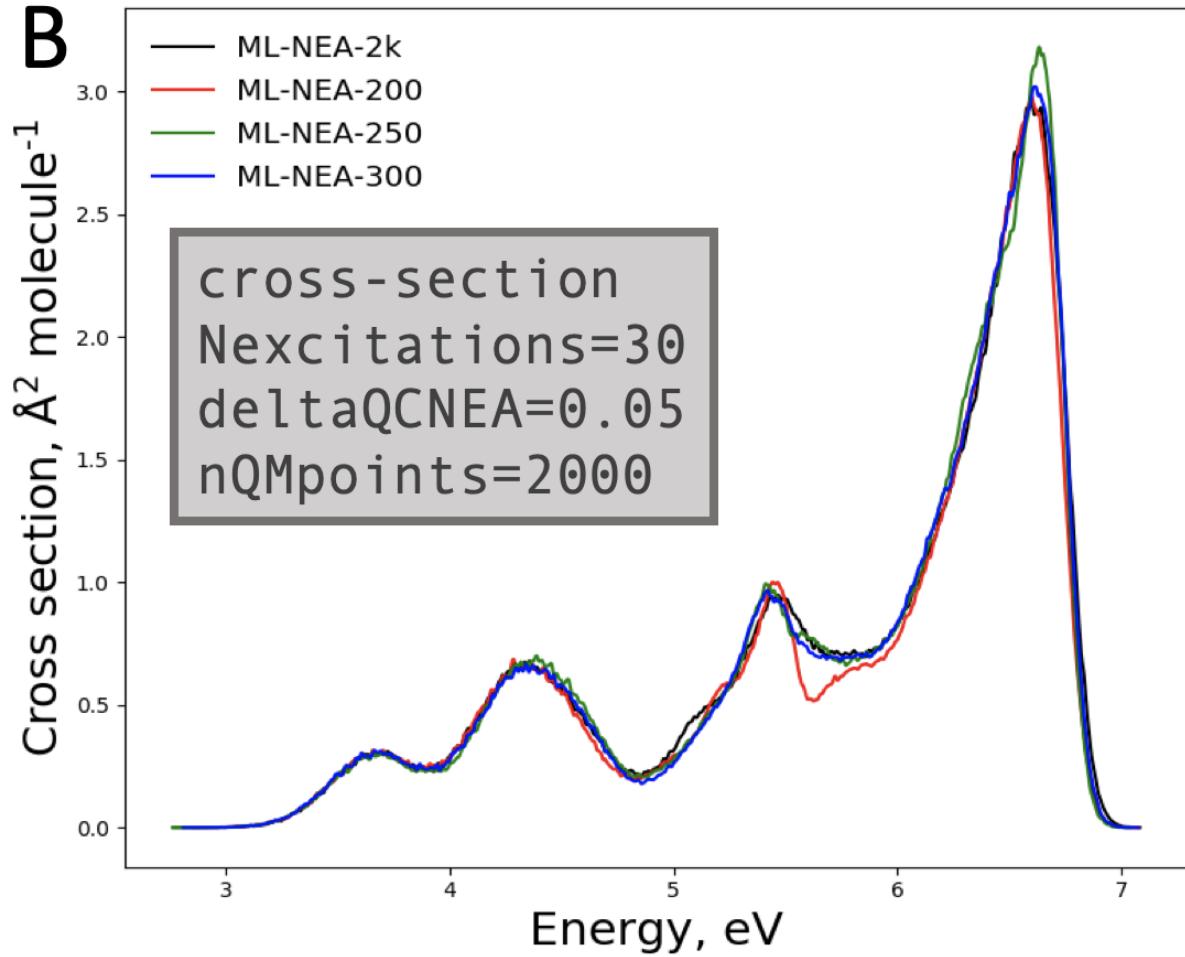
# The error of ML vs reference QM is smaller than the error of QM vs experiment



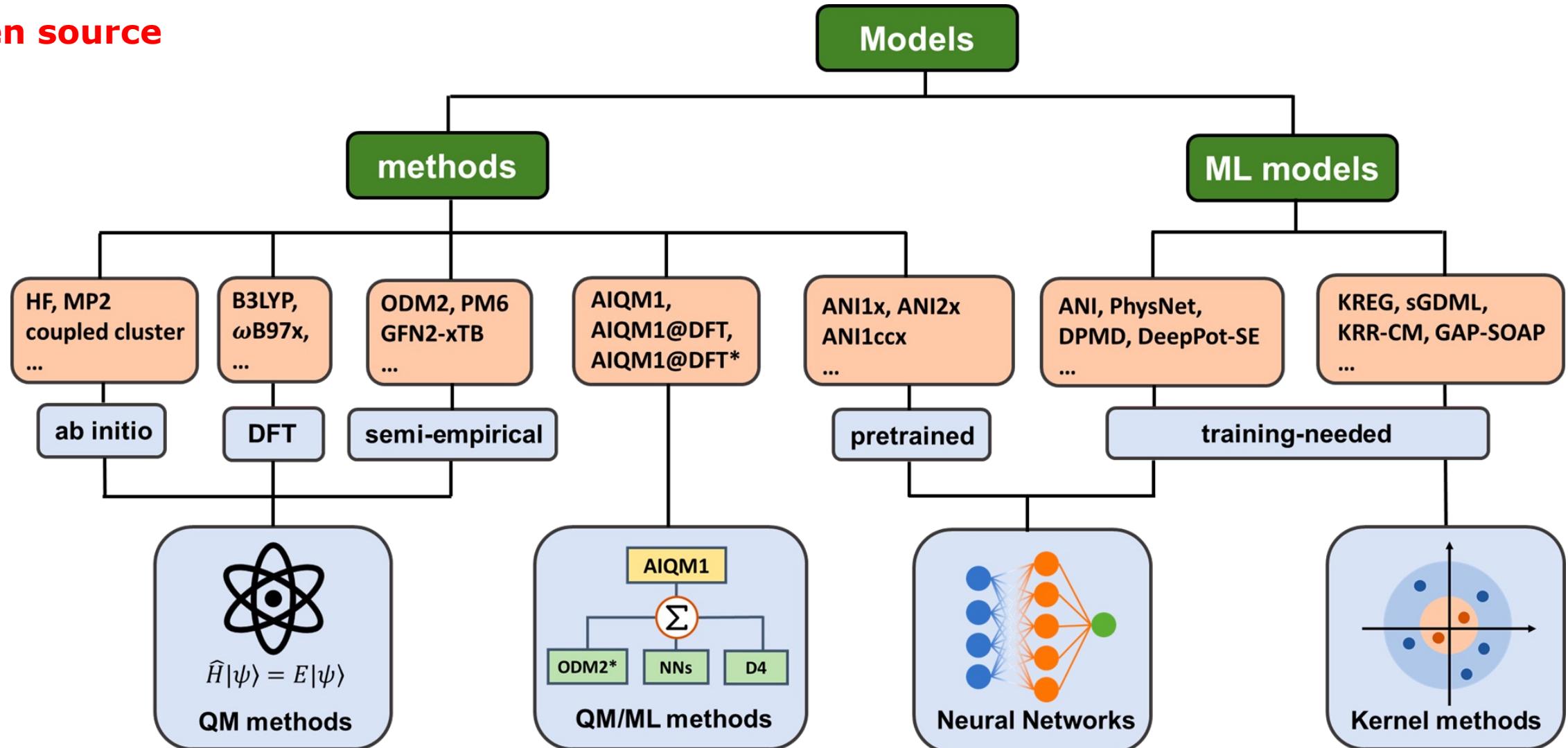
# *Black-box implementation into MLatom*



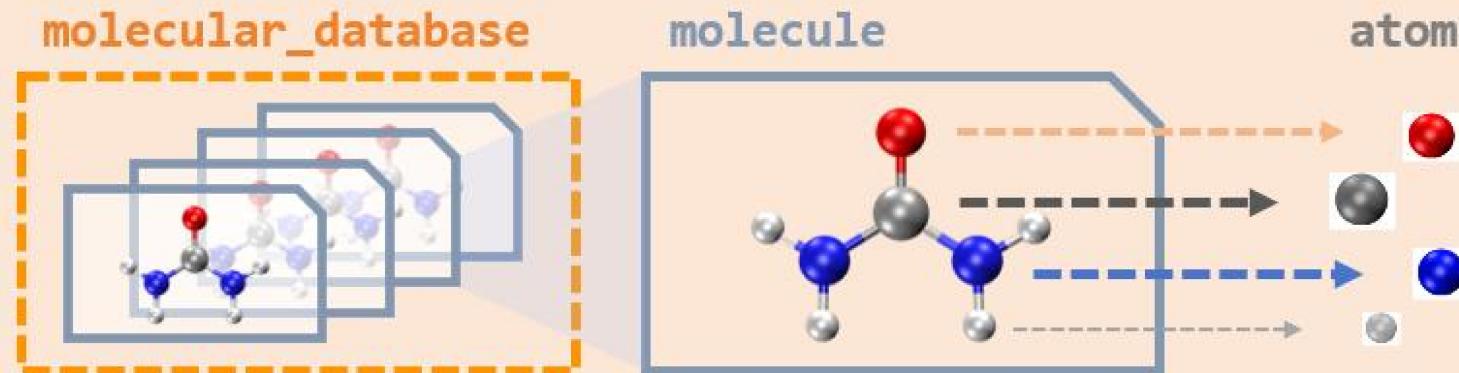
*ML-NEA is available in  
MLatom interfaced to Newton-X*



## Open source

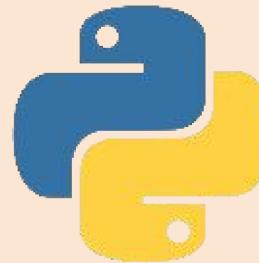


- Data in different formats and types **V3**



- Python API **V3**

```
import mlatom as ml
```



- Input file

```
ANI-1ccx
geomopt
xyzfile=init.xyz
optxyz=opt.xyz
```

- Command line

```
> $mlatom ANI-1ccx geomopt xyzfile=init.xyz optxyz=opt.xyz
```

\* 'V3' marks implementations released in MLatom 3

## Extras!

### MLQD

A Package for Quantum  
Dissipative Dynamics with  
Machine Learning  
by Arif Ullah, Anhui University

[MLQD: A. Ullah, P. O. Dral.  
*Comput. Phys. Commun.* **2024**,  
294, 108940]

Semi-empirical quantum chemical programs:

Machine learning programs:

PhysNet

GAP

TORCHANI



SEED

hyperopt

Dynamics and other atomistic simulation:

ASE

NX  
[newtonx.org](http://newtonx.org)



Quantum chemical programs:



Gaussian  
PySCF

GÅMESS



## Interfaces



MNDO



**XACS**  
Xiamen Atomistic  
Computing Suite

**XMVB**

**XEDA**

**MLatom**

### Cloud computing (free!)



[XACScloud.com](http://XACScloud.com)

- *Ab initio* valence bond calculations (**VBSCF**, **VBCI**, **BOVB**, ...)
- Generalized Kohn–Sham energy decomposition analysis (**GKS-EDA**)
- Artificial intelligence-enhanced quantum mechanical method 1 (**AIQM1**, faster and more accurate than B3LYP)
- Fast geometry optimization, MD, thermochemistry
- ... and much more

### Principal investigators (Xiamen University)

- Wei Wu
- Peifeng Su
- Pavlo O. Dral

### Partners

- Mario Barbatti, Aix Marseille University
- Benoît Braïda, Sorbonne Université
- Philippe Hiberty, University of Paris-Saclay
- Olexandr Isayev, Carnegie Mellon University
- Yirong Mo, UNC Greensboro
- Sason Shaik, Hebrew University
- Avital Shurki, Hebrew University
- Cheng Wang, Xiamen University

### Interfaces

TORCHANI

SPARROW

ASE    hyperopt

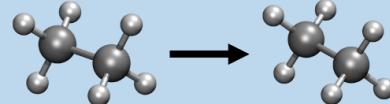


## Open source

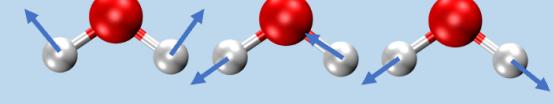
Single point calculations

Energies, forces, Hessian matrix...

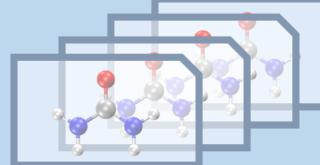
Geometry optimizations



Frequency calculations



Molecular dynamics

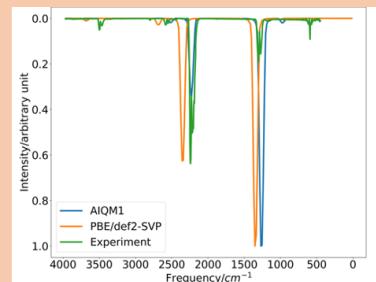


Thermochemistry  
calculations

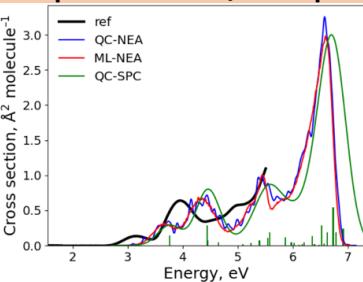
Heat of formation:

$$\Delta H_{\text{at},T} = \left[ \sum_A H_T(A) \right] - H_T$$

(Ro)vibrational spectra



One-photon UV-vis spectra



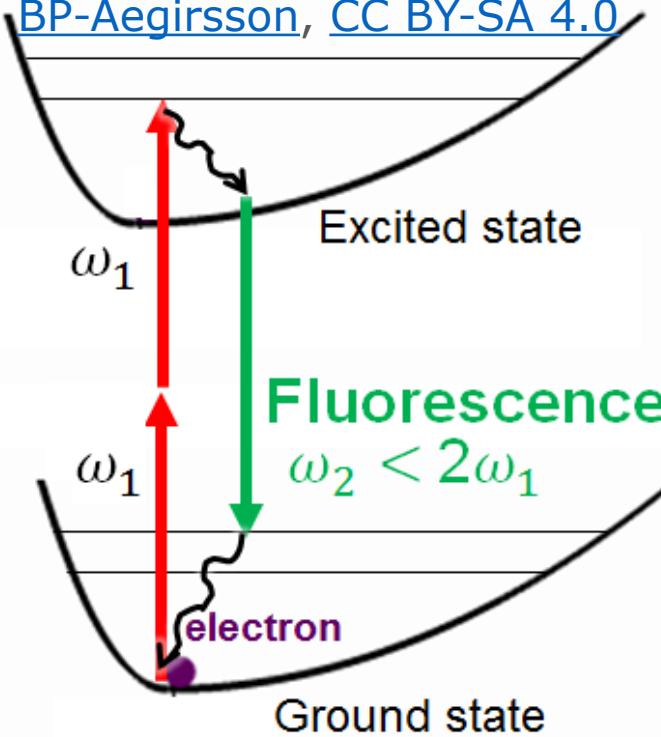
Properties &  
spectra

Simulations

Quantum dissipative  
dynamics

Two-photon  
absorption spectra

[BP-Aegirsson, CC BY-SA 4.0](#)

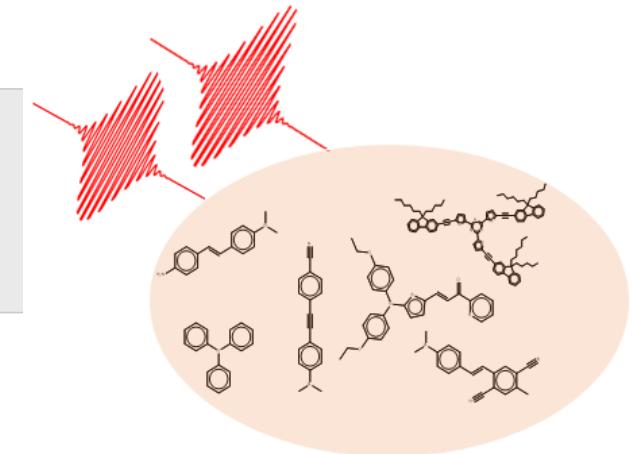


## Two-photon absorption applications:

- two-photon lithography
- Photodynamic therapy
- Bioimaging
- 3D printing
- Upconverted laser

Here we show how to calculate TPA cross section for RHODAMINE 6G and RHODAMINE 123 molecules with MLatom input file `mltpa.inp`:

MLTPA  
`SMILESfile=Smiles.csv`  
`auxfile=_aux.txt`



This input requires `Smiles.csv` file with SMILES of molecules:

```
CCNC1=CC2=C(C=C1C)C(=C3C=C(C(=[NH+]CC)C=C3O2)C)C4=CC=CC=C4C(=O)OCC.[Cl-]
COC(=O)C1=CC=CC=C1C2=C3C=CC(=N)C=C3O4=C2C=CC(=C4)N.Cl
```



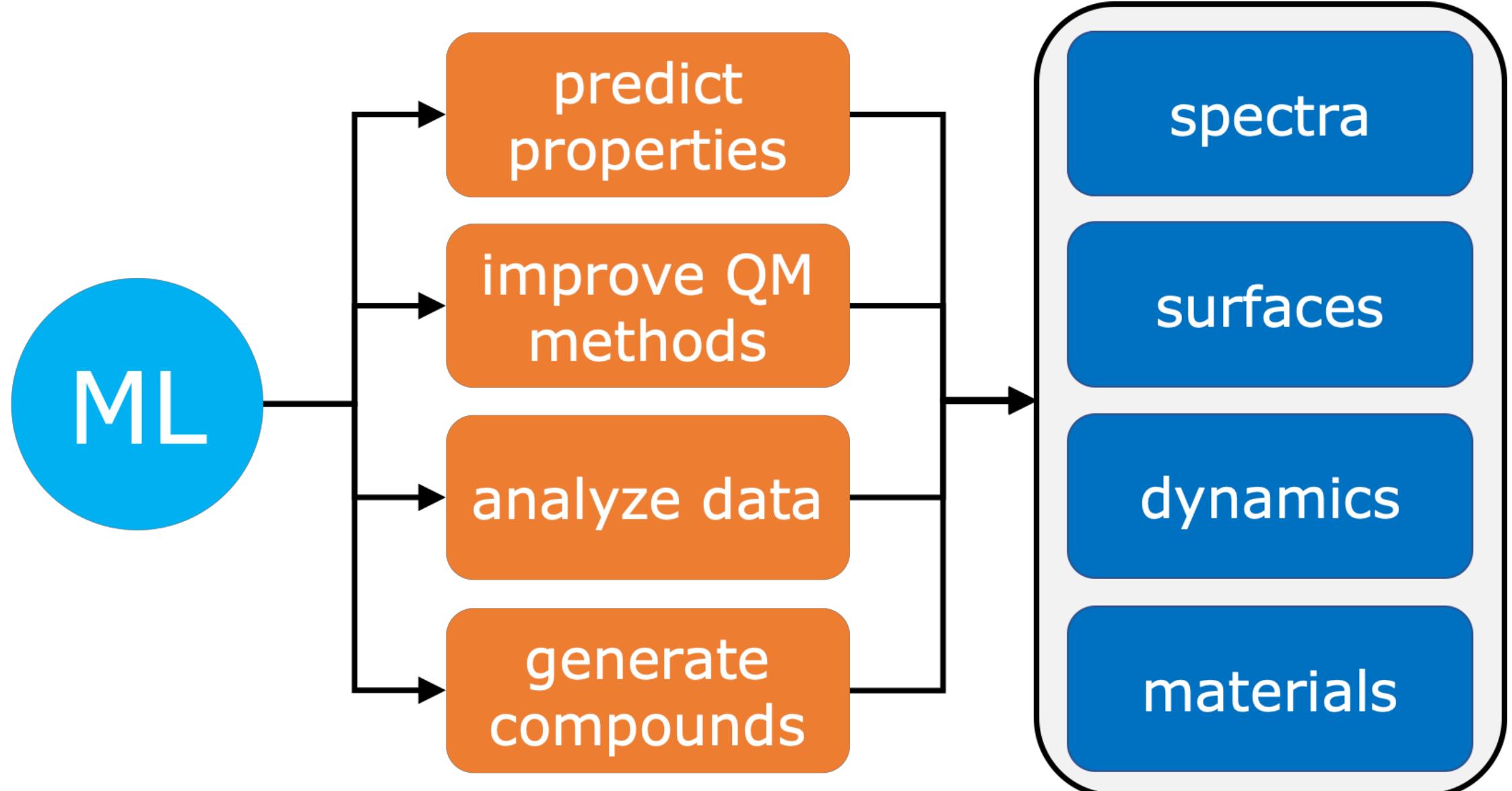
Yuming Su



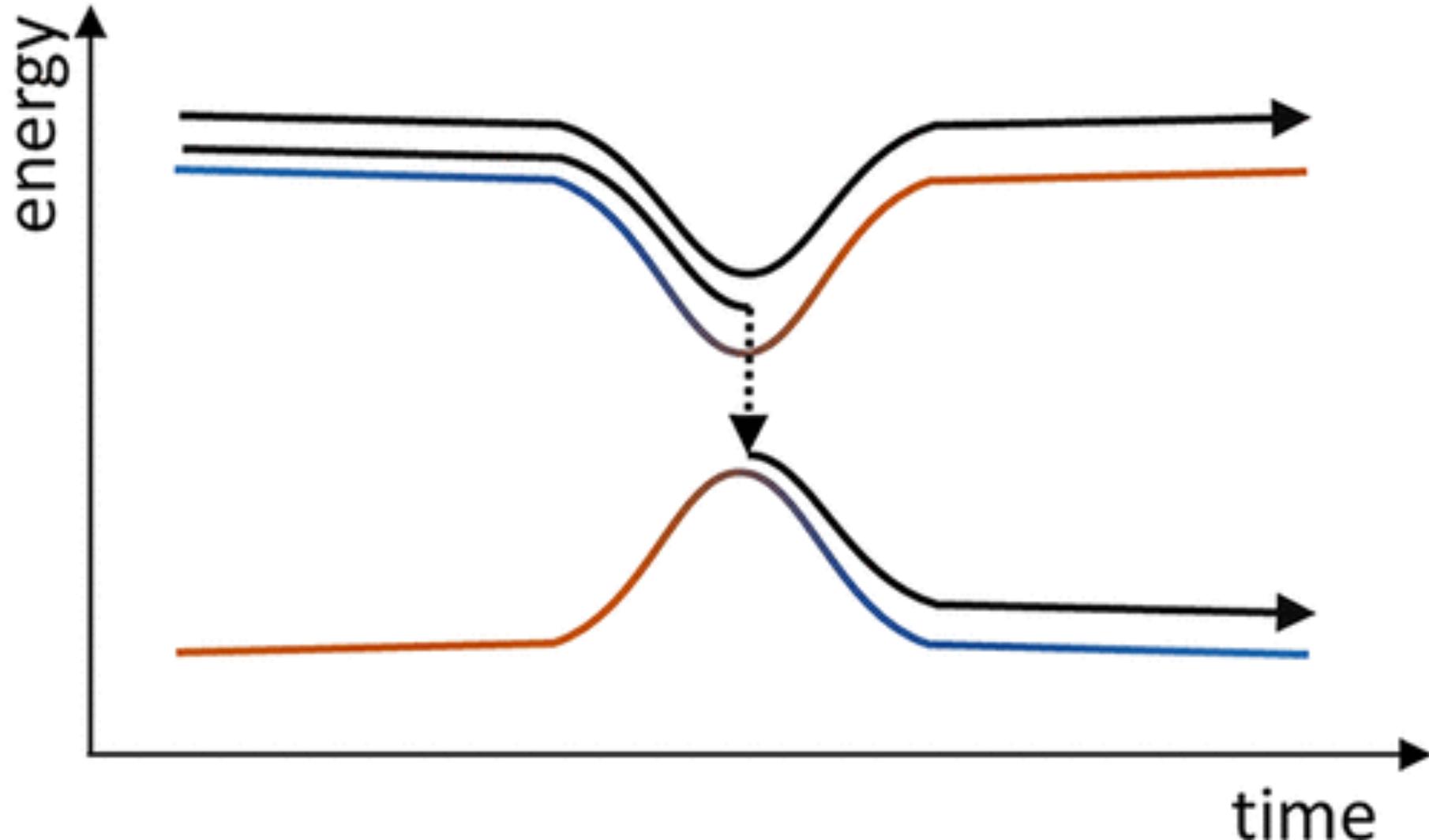
Zhou Da



Cheng Wang



# Surface Hopping



J. C. Tully, *J. Chem. Phys.* **1990**, 93, 1061

R. Crespo-Otero and M. Barbatti, *Chem. Rev.* **2018**, 118, 7026

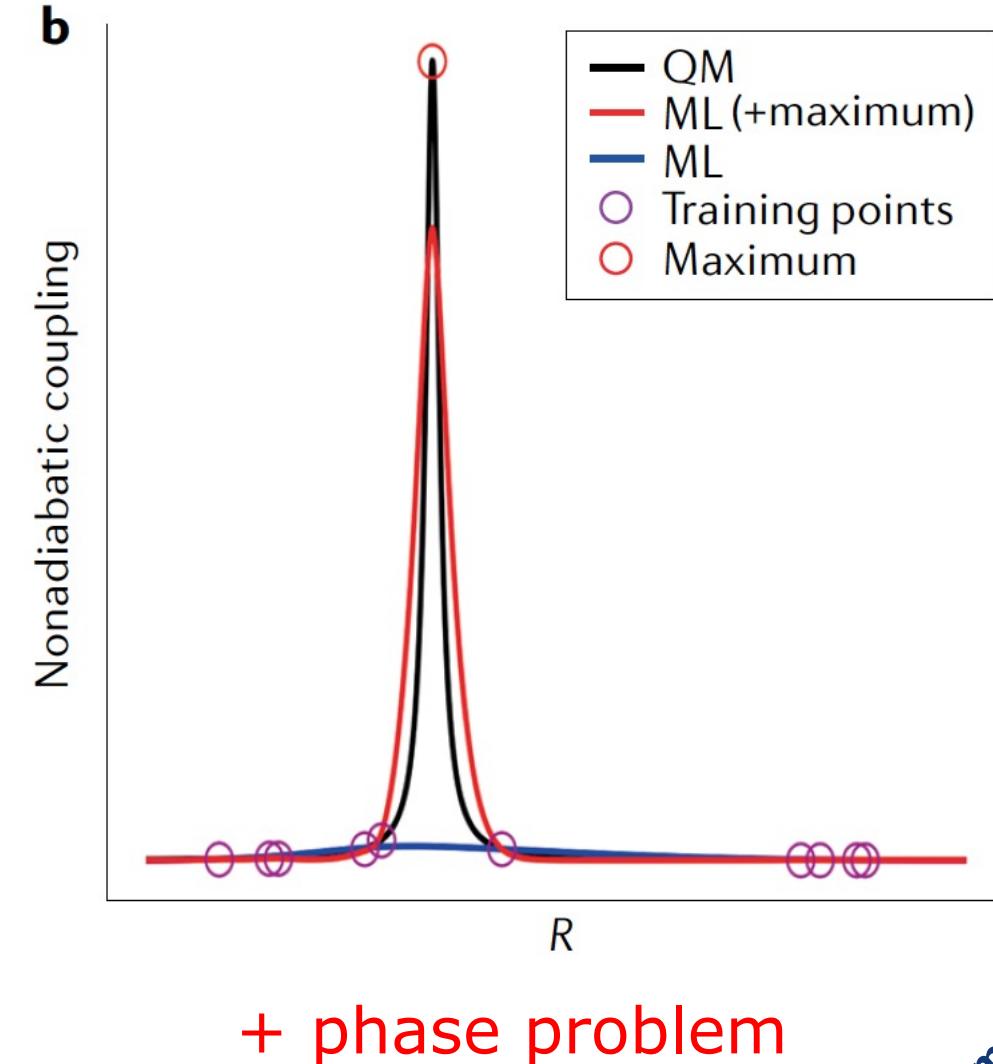
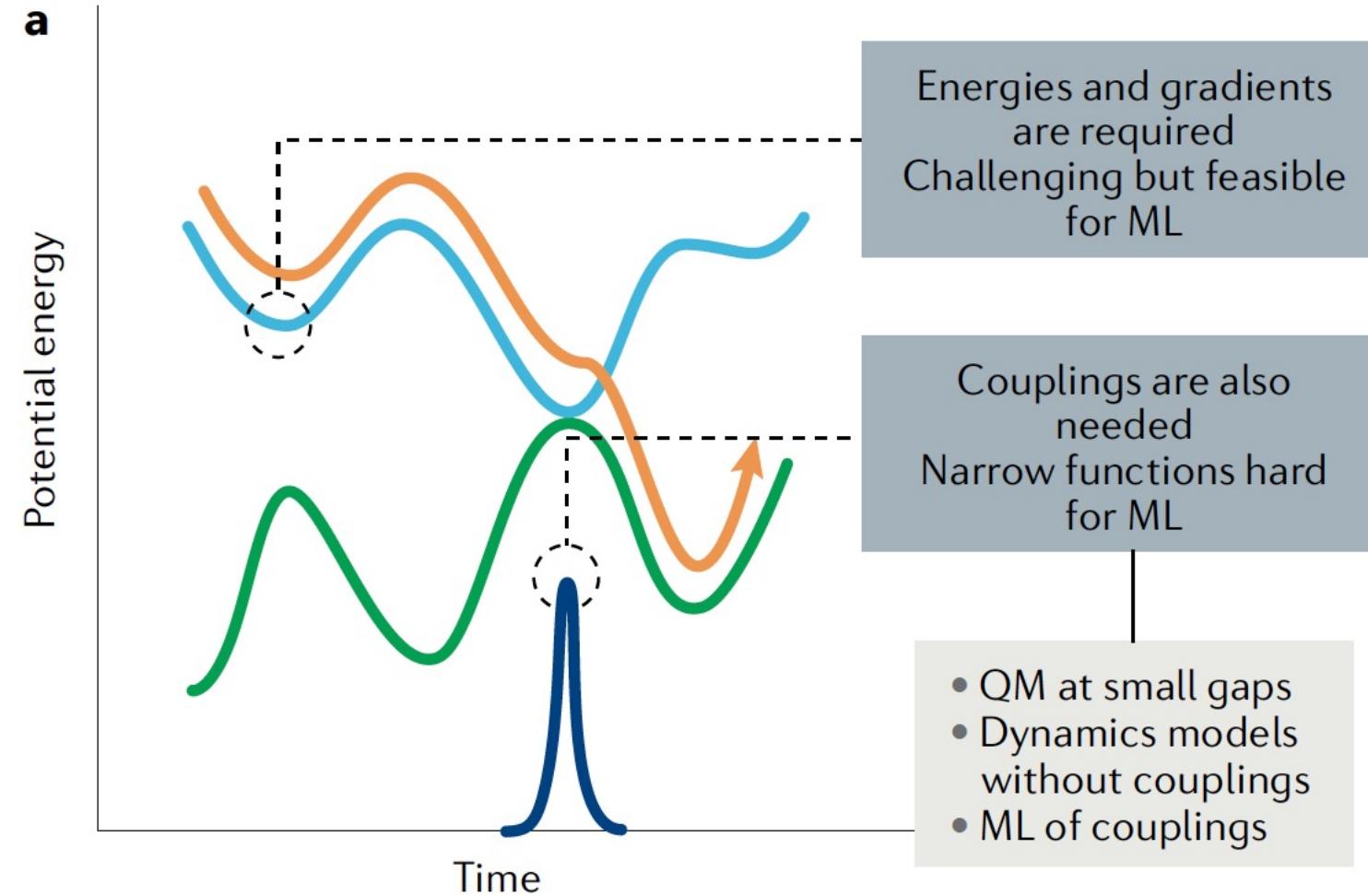
Typical nonadiabatic excited-state simulations:

- 100 trajectories
- for 1 ps = 1000 fs
- 0.5 fs time step

Number of QM calculations:

- 2000 per trajectory
- 200 000 in total

# Why ML-TSH is challenging



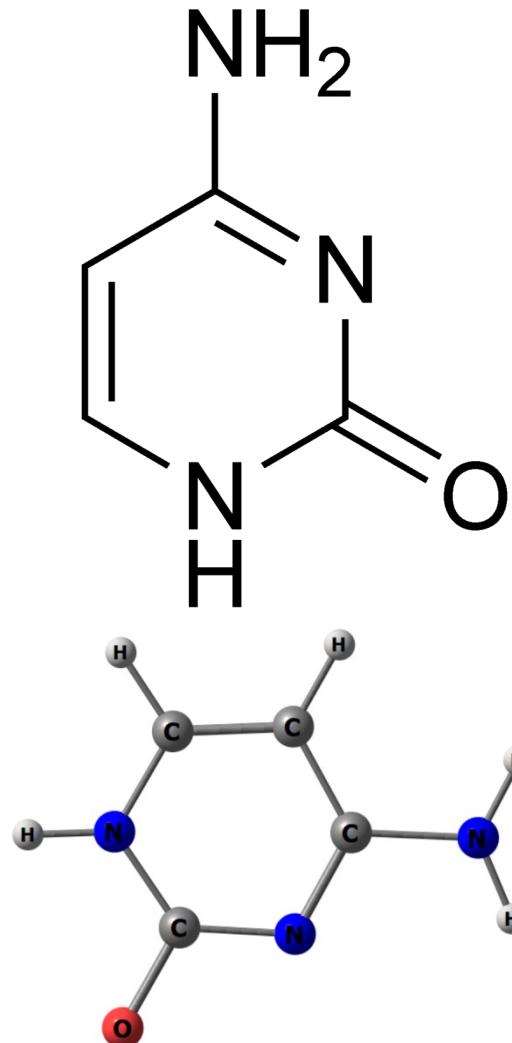
33-D A-SBH inspired by cytosine

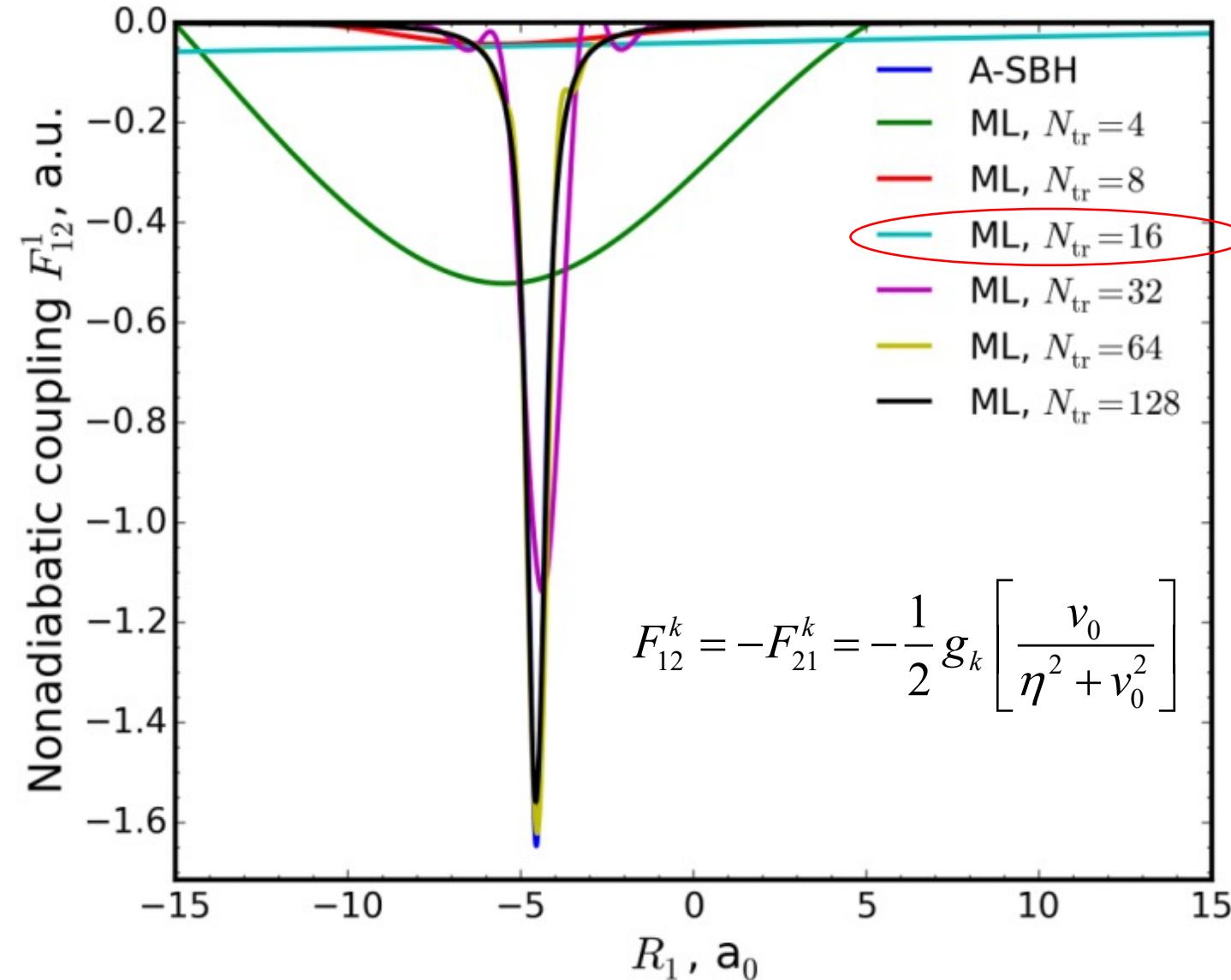
$$H = H_s + H_b + H_{sb}$$

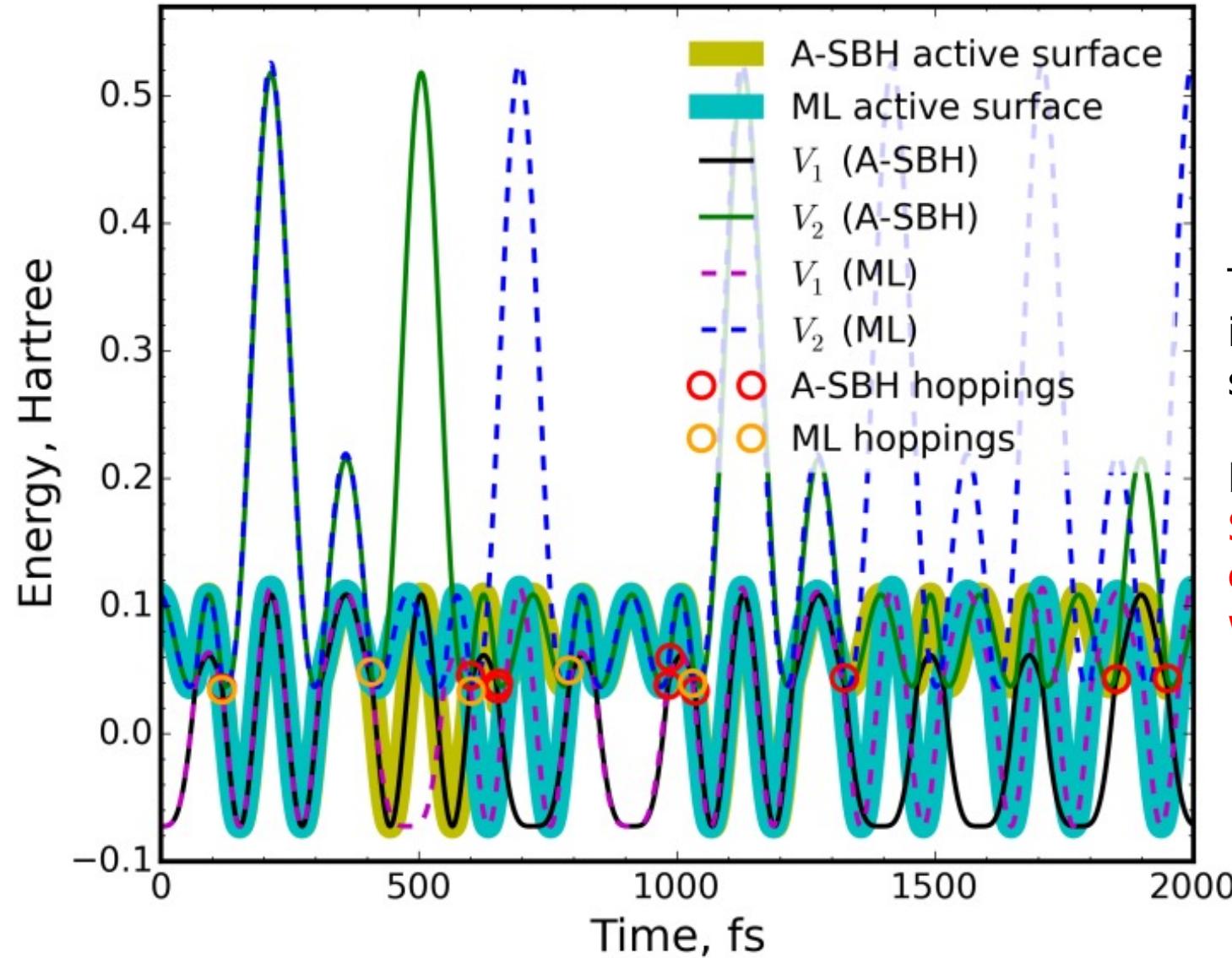
$$V_J = \frac{1}{2} \sum_{k=1}^N M_k \omega_k^2 R_k^2 + (-1)^J [\eta^2 + v_0^2]^{1/2}, \quad (J=1,2)$$

$$\frac{\partial V_J}{\partial R_k} = M_k \omega_k^2 R_k + (-1)^J g_k \left[ \frac{\eta}{[\eta^2 + v_0^2]^{1/2}} \right]$$

$$\eta = \left( \sum_{k=1}^N g_k R_k + \epsilon_0 \right)$$

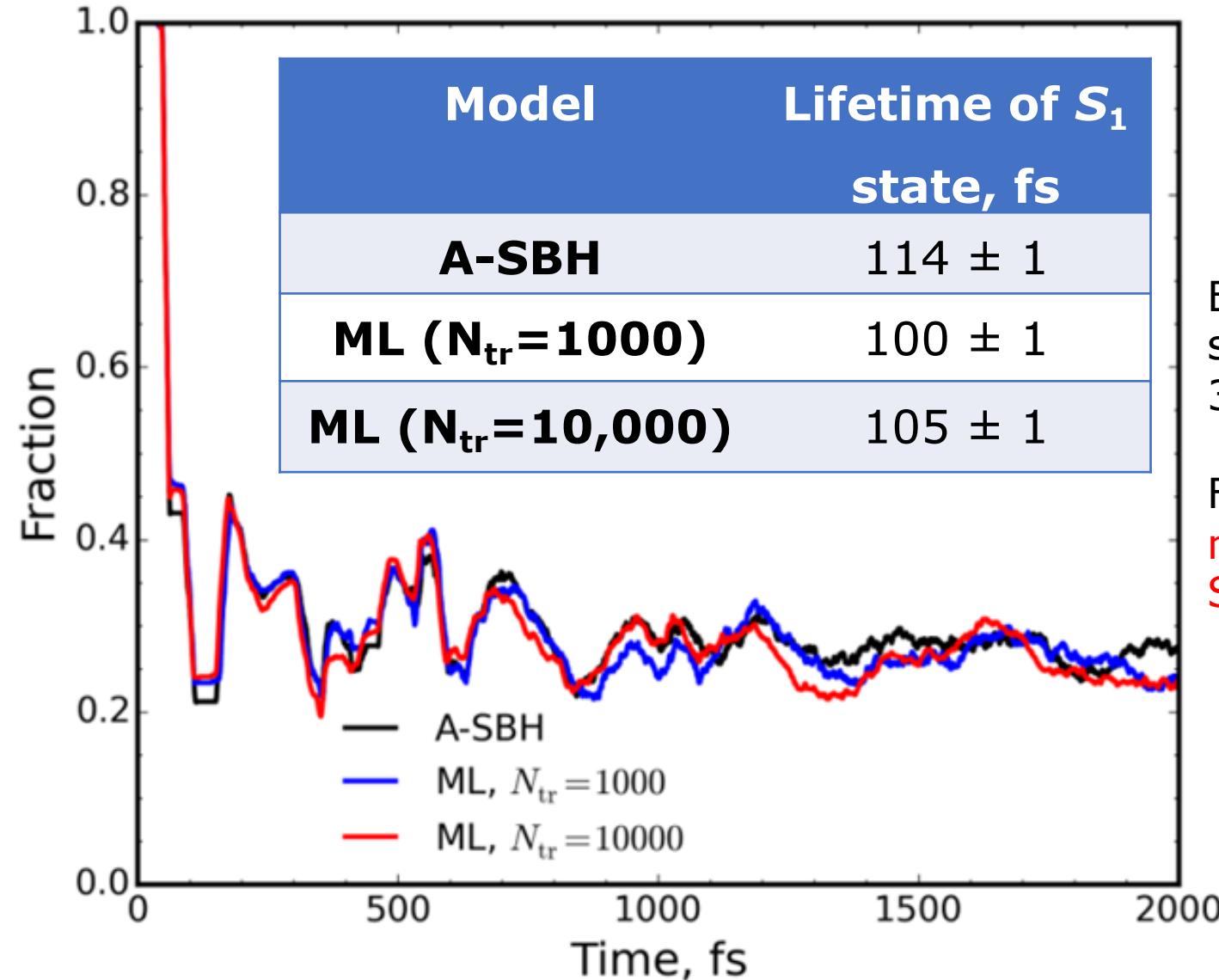






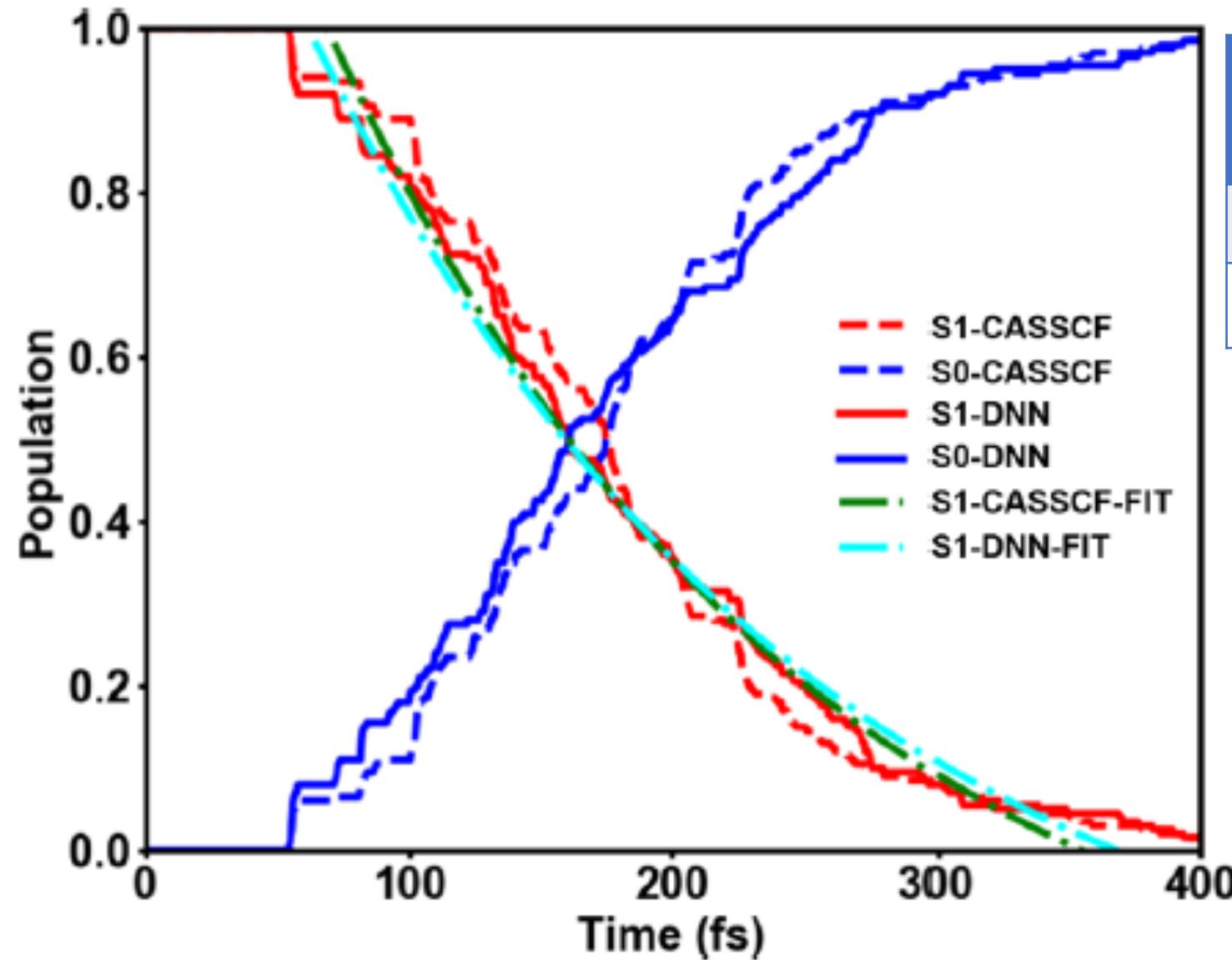
The simulations started from the same initial conditions and were run with the same random seed

During the ML trajectory propagation, A-SBH calculations were performed when the estimated energy gap between  $S_1$  and  $S_0$  was below 0.03 Hartree



Evolution of the fraction of trajectories on state  $S_1$  for the 33-D model averaged for 1,000 trajectories

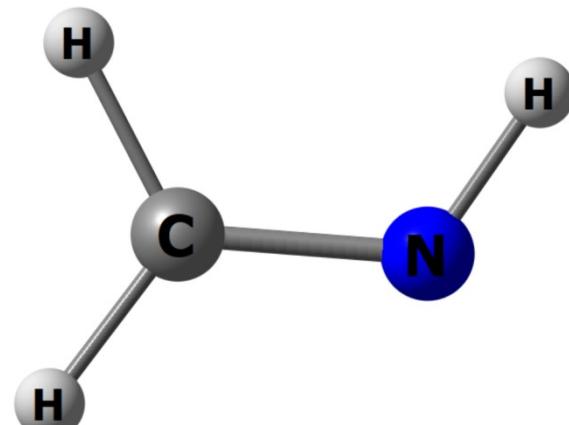
For small band gaps (<0.03 Hartree)  
nonadiabatic couplings were calculated with A-SBH



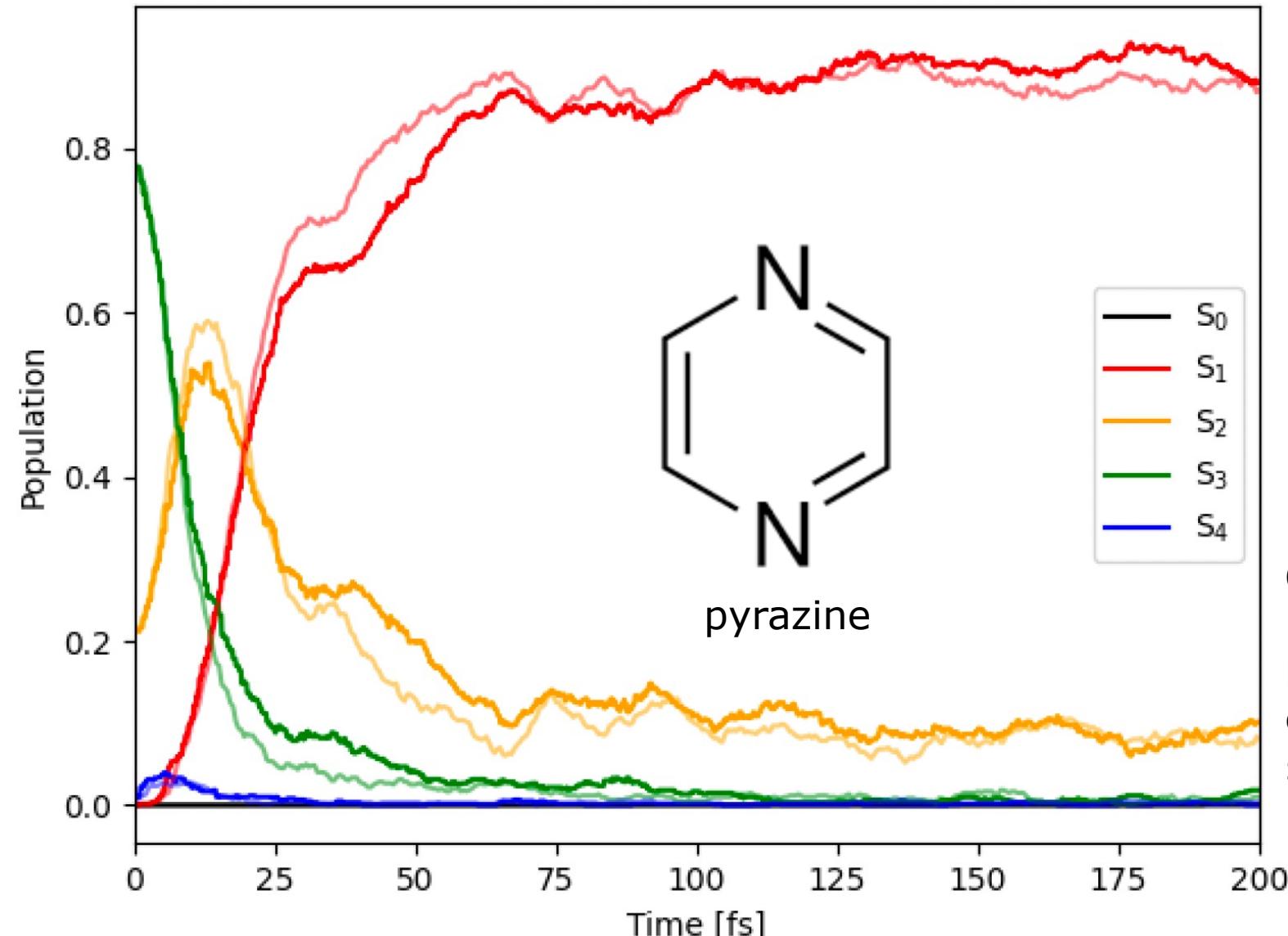
Model                      Lifetime of  $S_1$   
state, fs

CASSCF                      182

Deep NNs                      191



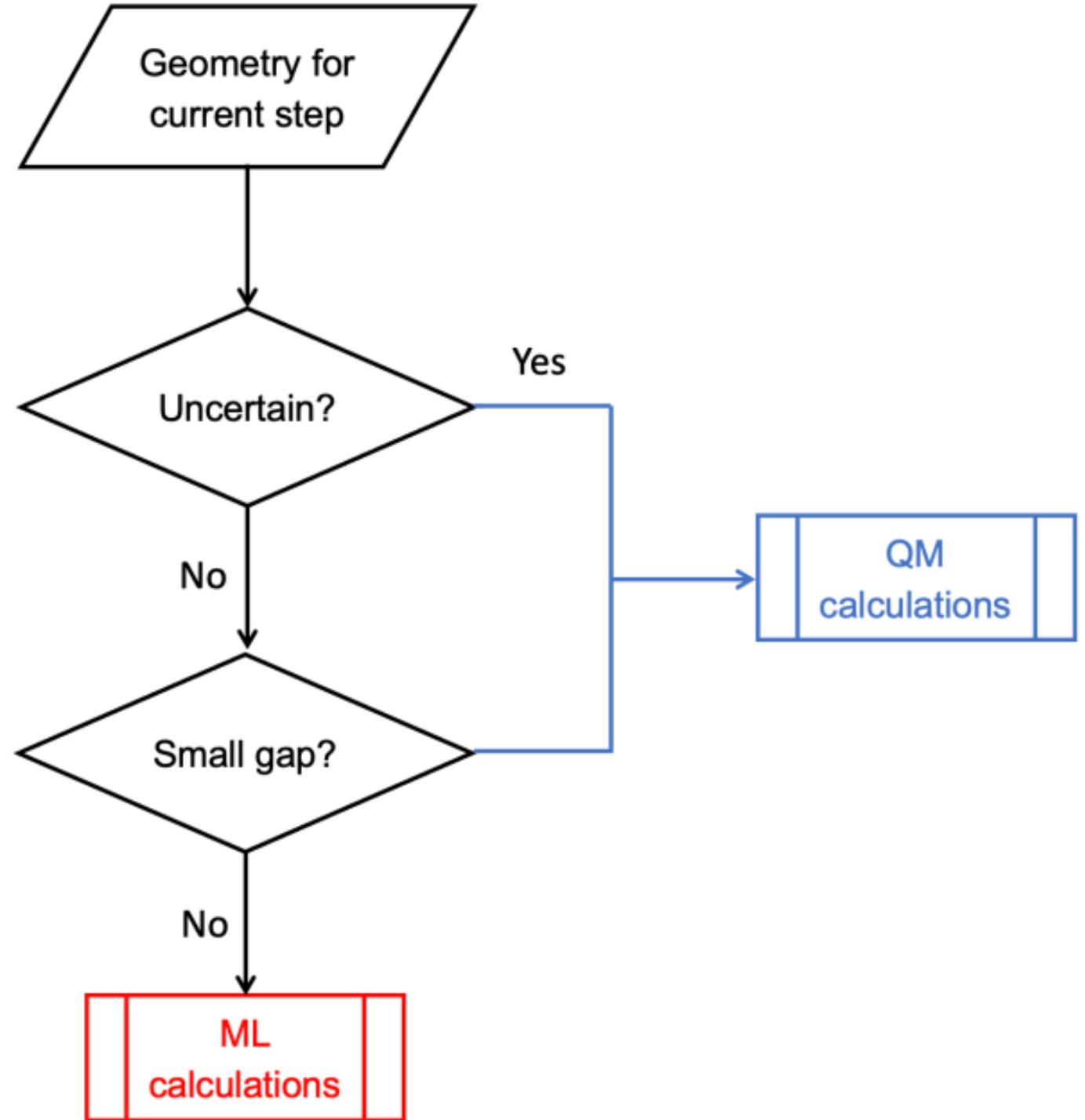
Zhu–Nakamura  
method for dynamics

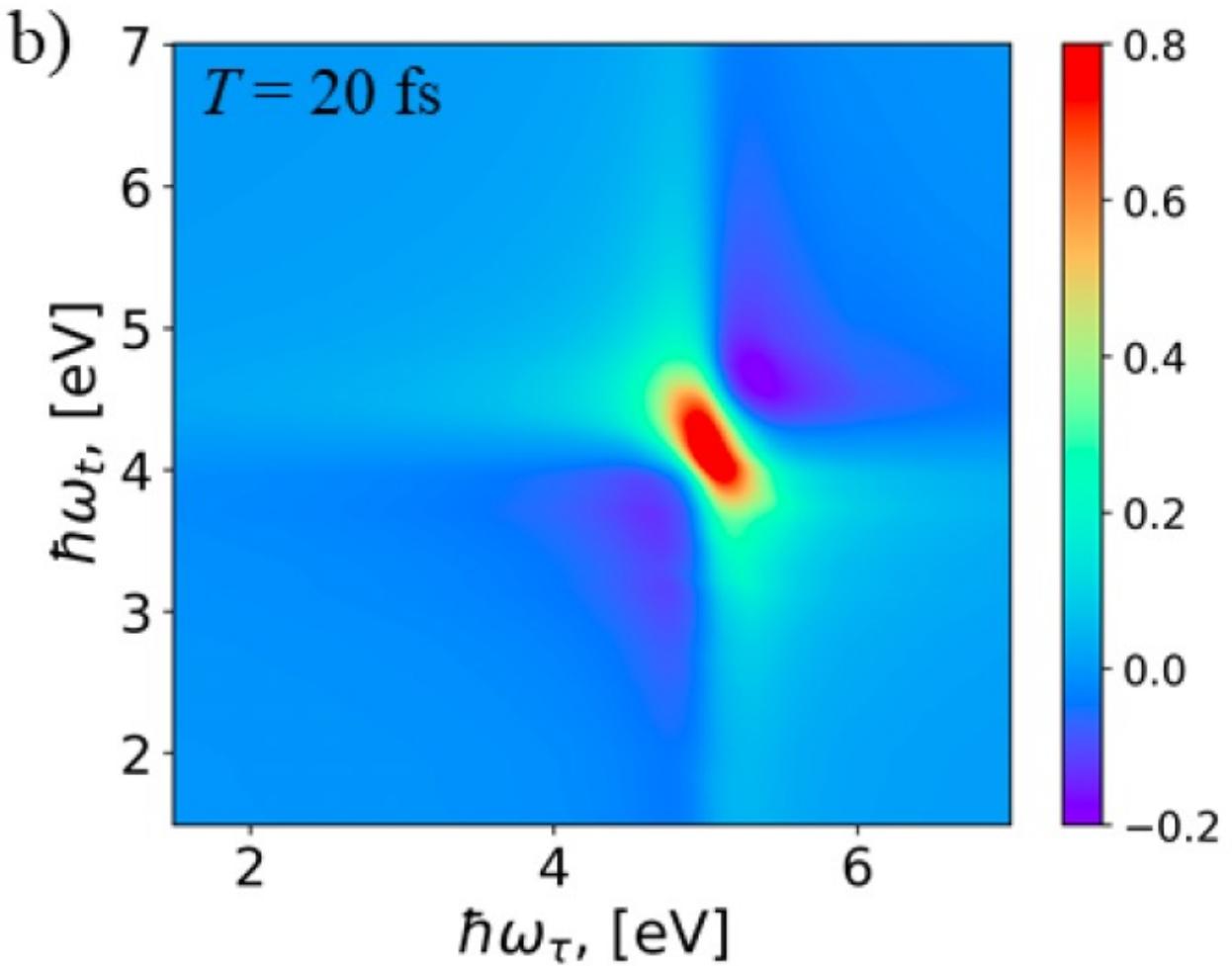
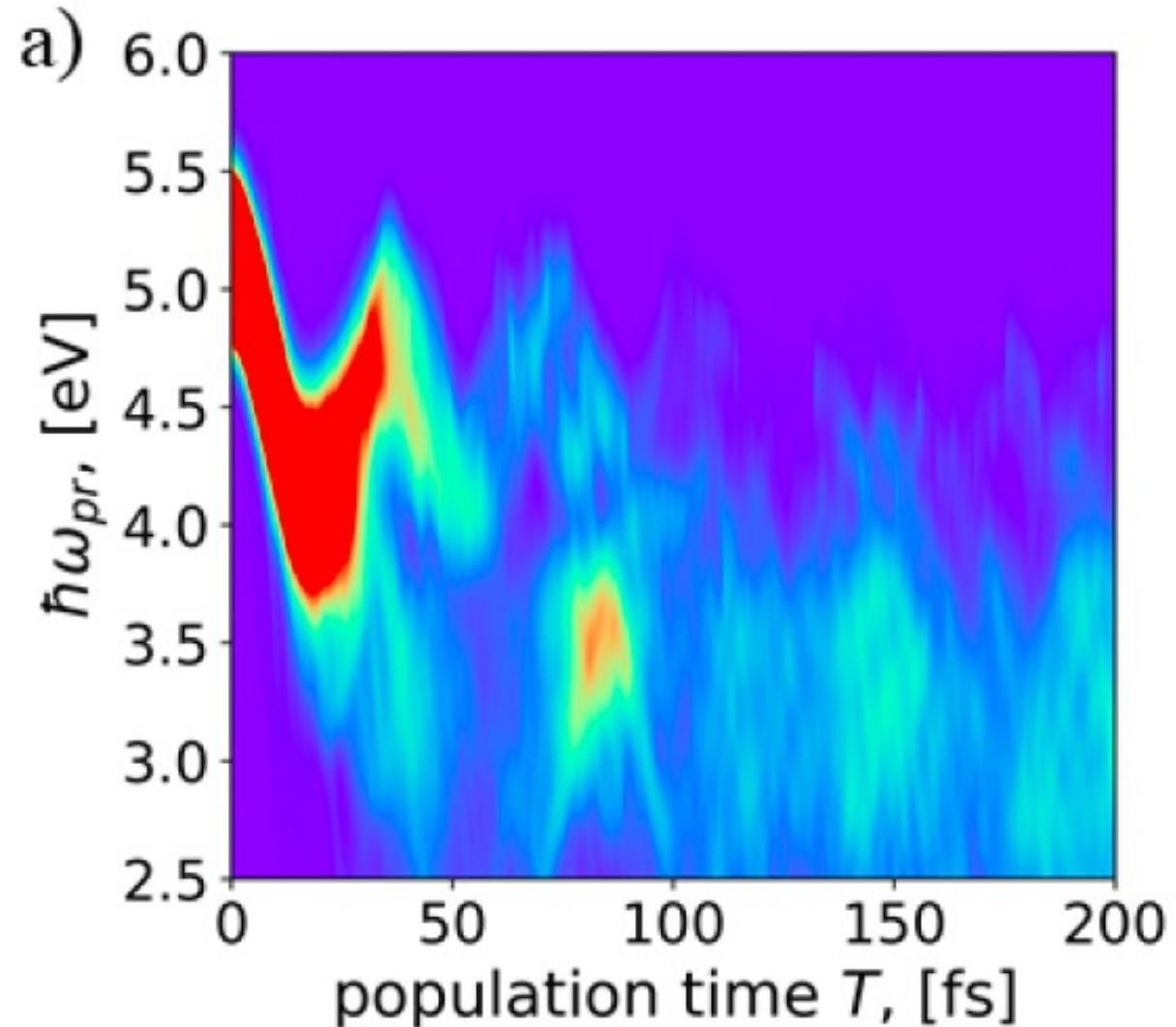


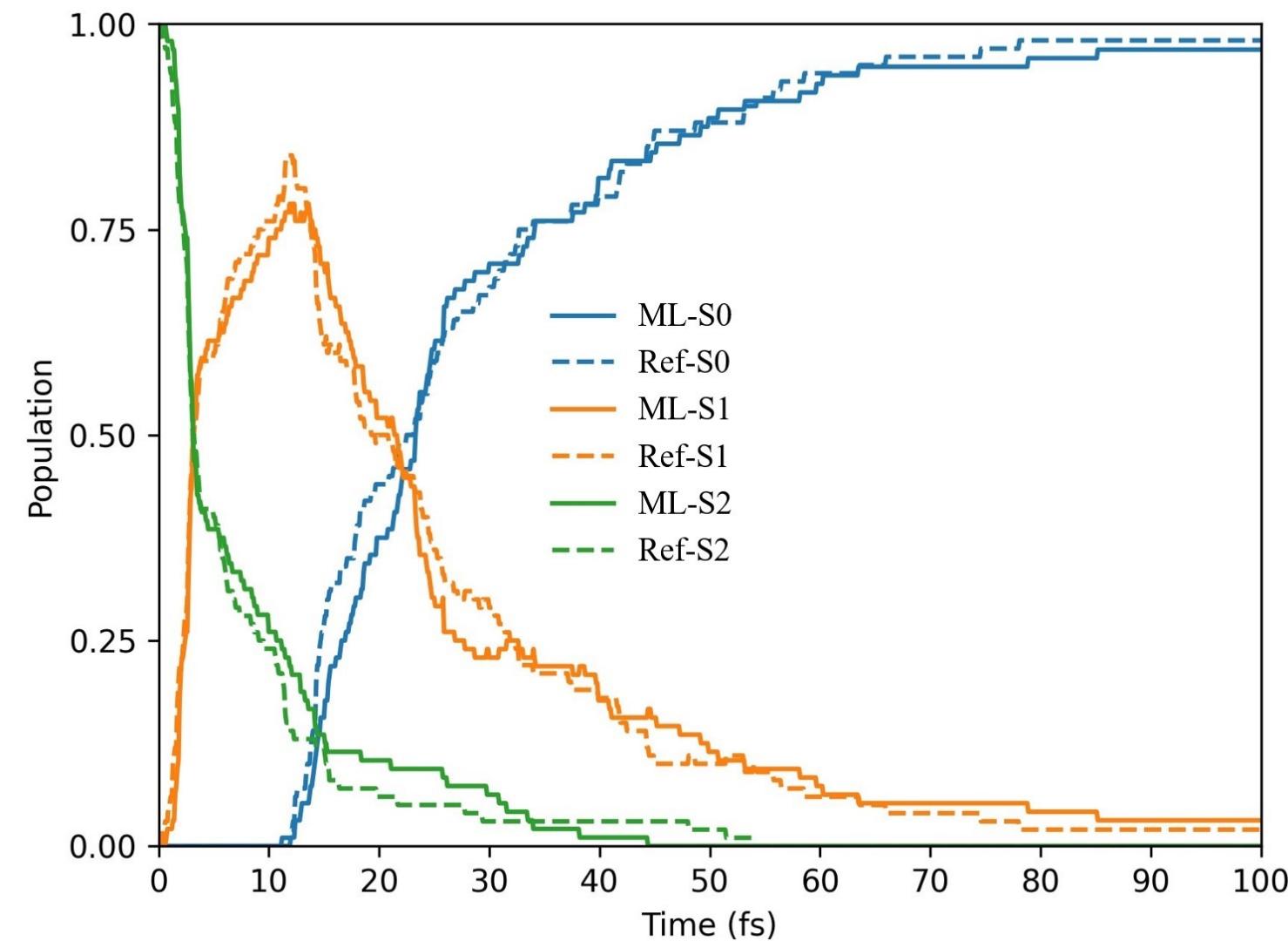
ML (ANI-type MLPs) – full colors  
QM reference – pale

ML cut the cost by at least 95%  
compared to pure first-principles  
simulations

S. V. Pios, M. F. Gelin, A. Ullah,  
P. O. Dral\*, L. Chen\*, *J. Phys.  
Chem. Lett.* **2024**, 15, 2325







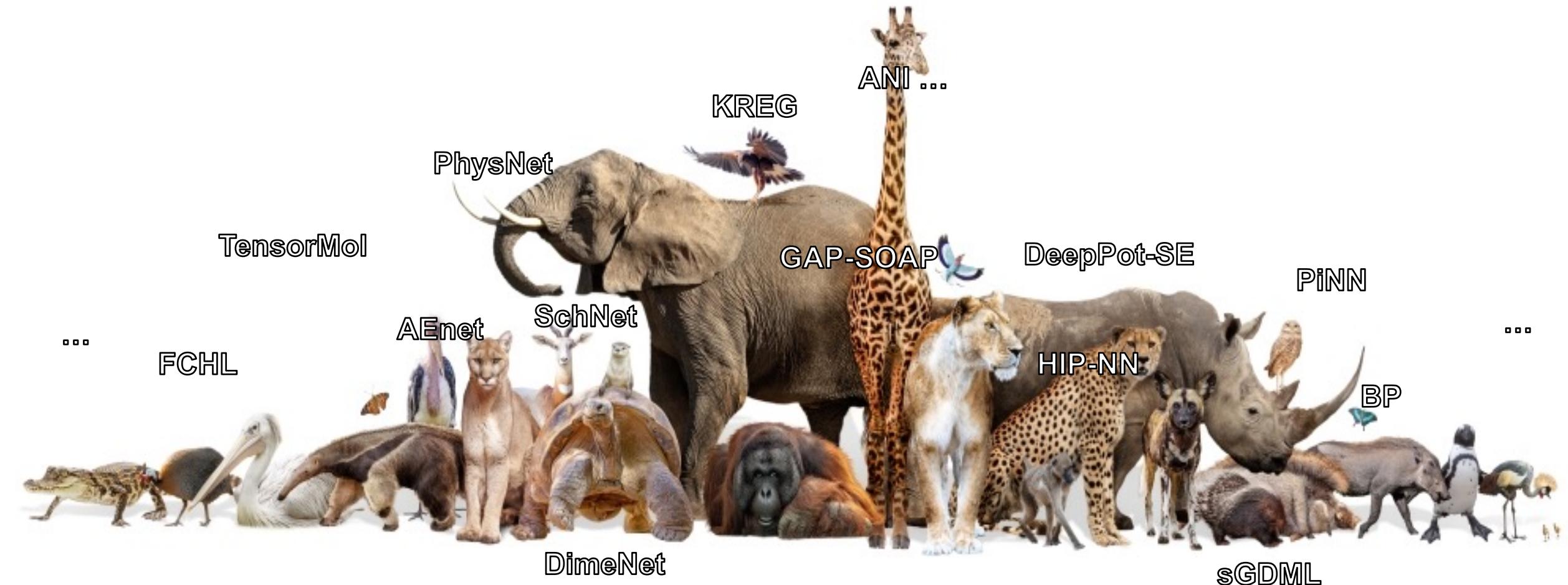
Molecule:  $\text{CNH}_4^+$

Reference:  
SA-3-CASSCF(12,8)/  
6-31G(d)

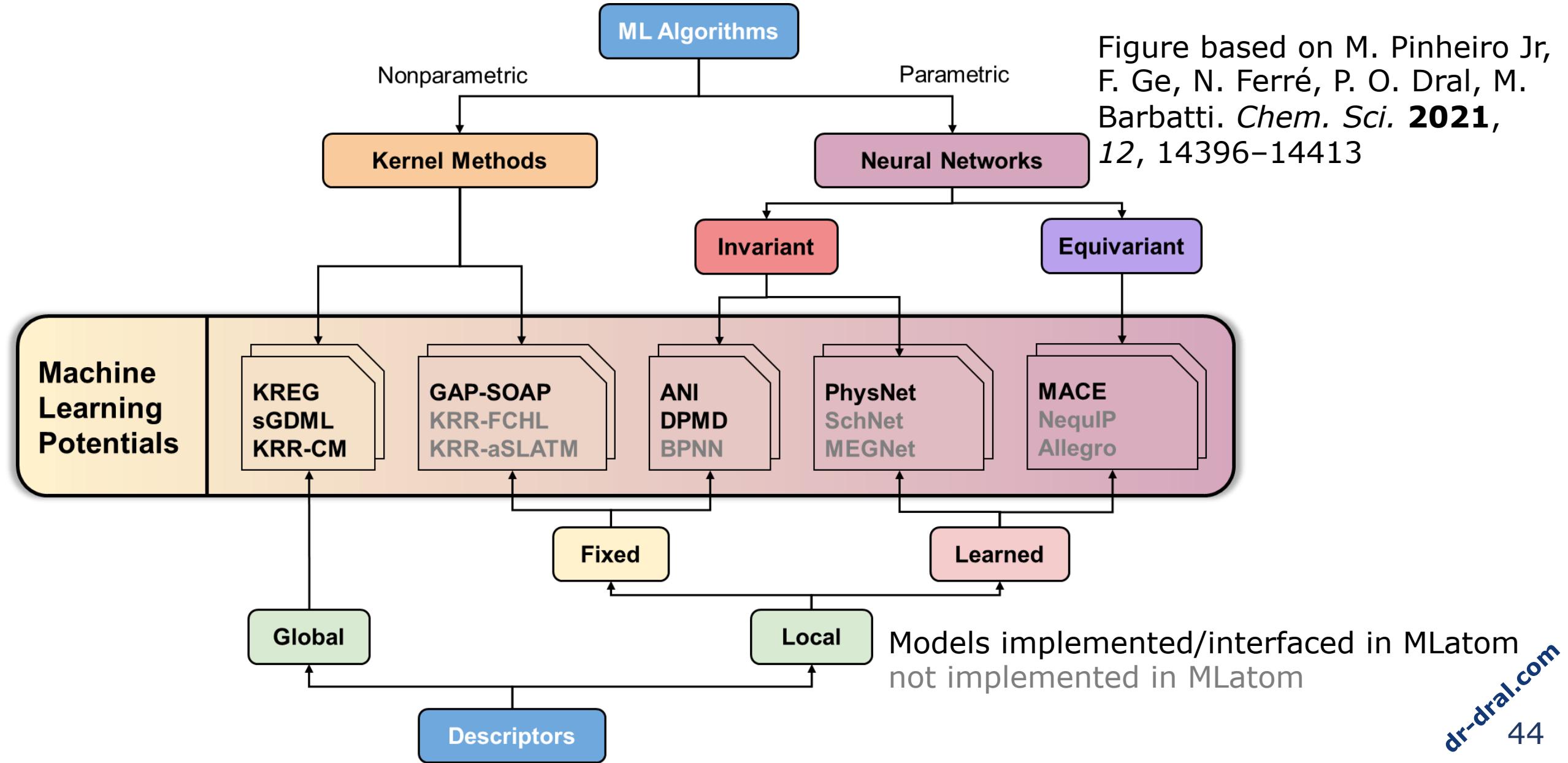
ML: ANI-type, trained on  
ca. 2500 points.

(back-hoppings  
prevented)

# Zoo of machine learning potentials



# Categories of machine learning potentials



# Current Work – AIQM1 Landau-Zener Surface Hopping

**Research System:**  $\text{CH}_2\text{NH}_2^+$

**Number of Electrons:** 16

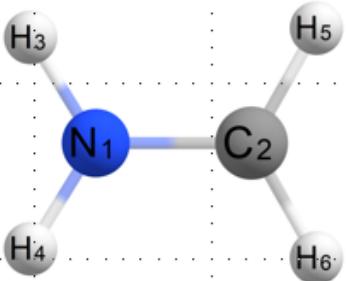
**TSH Package:** MLatom

**QC Calculation Package:** Columbus

**Reference Method:** SA-3-CASSCF(12,8)/6-31G(d)+LZ

**Prediction Method:** AIQM1(GUGA-CI)+LZ

**AIQM1 GUGA-CI Active Space:** Orb7-Orb9 (4,3)

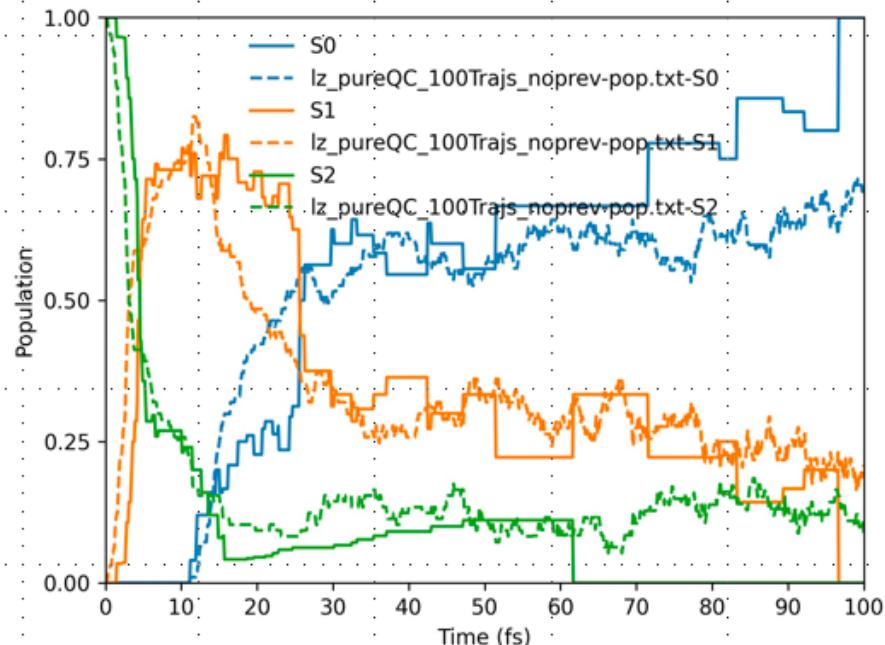
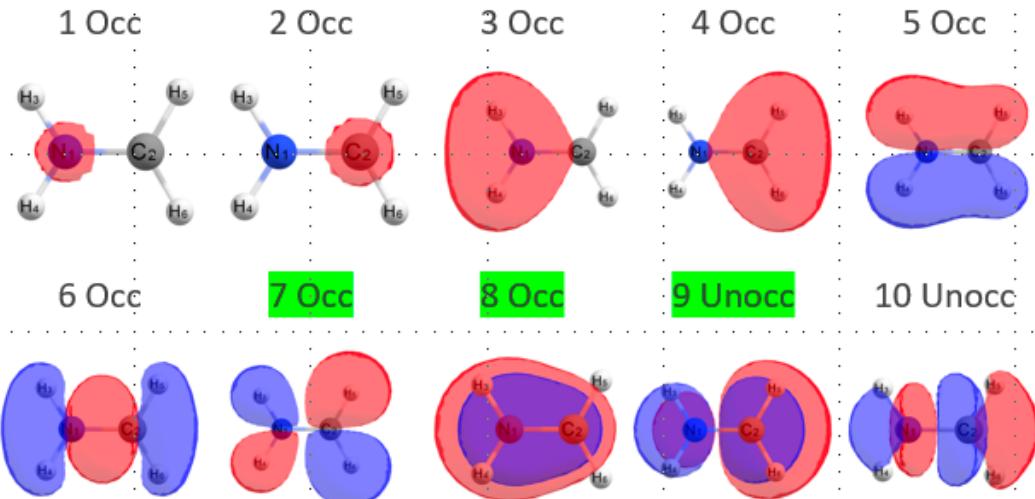


(small, ultrafast dynamics, classical photochemistry model system)



Lina Zhang

Lina Zhang, Pavlo O. Dral, et al., *unpublished*



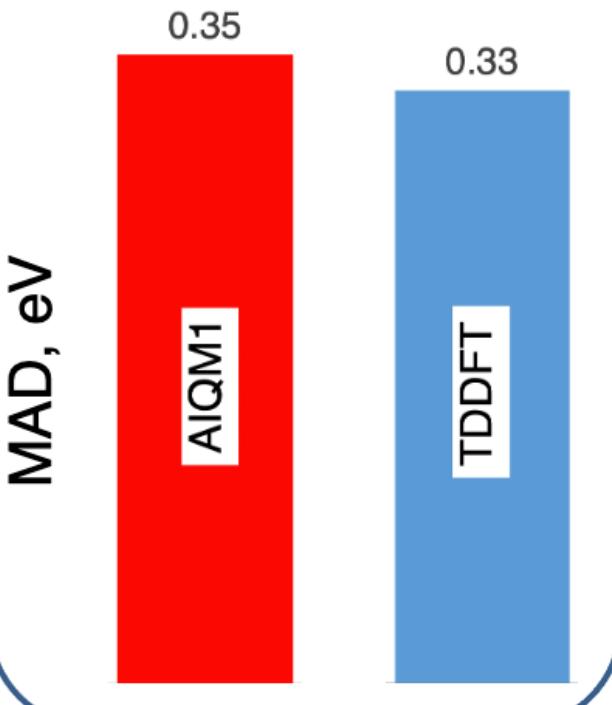
data set	ODM2	B3LYP/ 6-31G*	$\omega$ B97X/ 6-31G*	$\omega$ B97X-D/ 6-31G*	$\omega$ B97X/ def2-TZVPP	$\omega$ B97X-D4/ def2-TZVPP	ANI- 1ccx	AIQM1 @DFT*	AIQM1 @DFT	AIQM1	CCSD(T)* /CBS
energies, kcal/mol											
CHNO	2.64	6.71	4.10	3.84	3.21	2.76	—	2.49	2.12	0.87	—
G3/99	3.04	8.53	3.46	3.22	4.18	3.20	—	2.83	2.06	0.88	—
ISOMERS44 ( $\Delta H_f$ )	1.16	8.08	3.57	3.53	4.52	3.78	—	3.00	2.27	0.42	—
ISOMERS44 ( $\Delta H_r$ )	0.70	2.29	1.45	1.31	1.19	1.10	1.68	0.95	0.89	0.50	—
IsoL6/11	1.48	5.26	3.83	3.36	1.75	1.64	1.46	1.65	1.55	0.62	0.47
HC7/11	5.37	6.44	16.90	13.98	6.83	7.10	2.53	8.89	9.16	1.43	1.57

## Ground-state properties of neutral, closed-shell compounds (heats of formation, reaction enthalpies, and ZPVE-exclusive reaction energies)

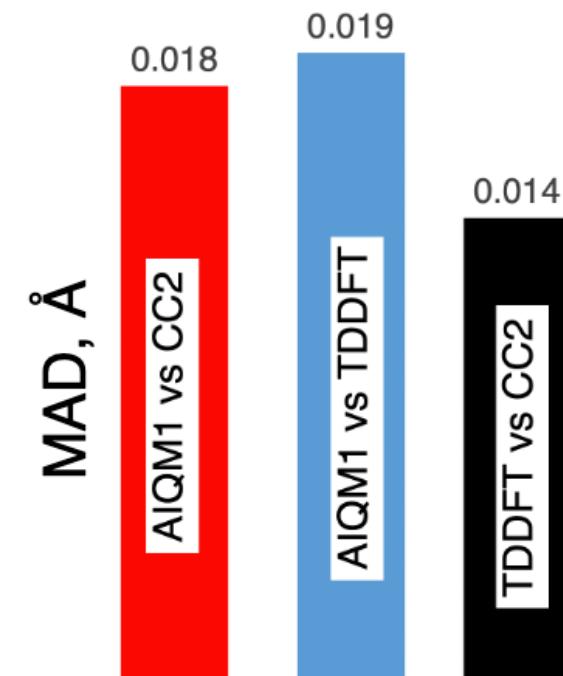
Torsion	0.74	0.55	0.30	0.29	0.20	0.19	0.23	0.23	0.23	0.19	0.05
bond lengths, Å											
CHNO	0.015	0.006	0.008	0.007	0.010	0.010	0.011	0.010	0.010	0.007	—
MGHBL9	0.023	0.007	0.006	0.005	0.002	0.002	0.047	0.011	0.011	0.004	—
MGNHBL11	0.026	0.006	0.003	0.002	0.008	0.008	0.004	0.008	0.008	0.002	—
bond angles, °											
CHNO	2.04	0.70	0.68	0.64	0.68	0.68	1.00	0.77	0.77	0.70	—
dihedral angles, °											
CHNO	4.07	5.20	4.68	6.10	7.12	7.11	5.86	2.14	2.14	2.31	—

data set	ODM2	B3LYP/ 6-31G*	$\omega$ B97X/ 6-31G*	$\omega$ B97X-D/ 6-31G*	$\omega$ B97X/ def2-TZVPP	$\omega$ B97X-D4/ def2-TZVPP	ANI- 1ccx	AIQM1 @DFT*	AIQM1 @DFT	AIQM1	CCSD(T)* /CBS
excitation energies, eV											
Thiel's set	0.35	0.32	0.45	0.36	0.36	0.36	—	0.35	0.35	0.35	—

## a Thiel's set benchmark



## b ExGeom benchmark



TDDFT:  
Linear-response TD B3LYP/TZVP

## c bond length

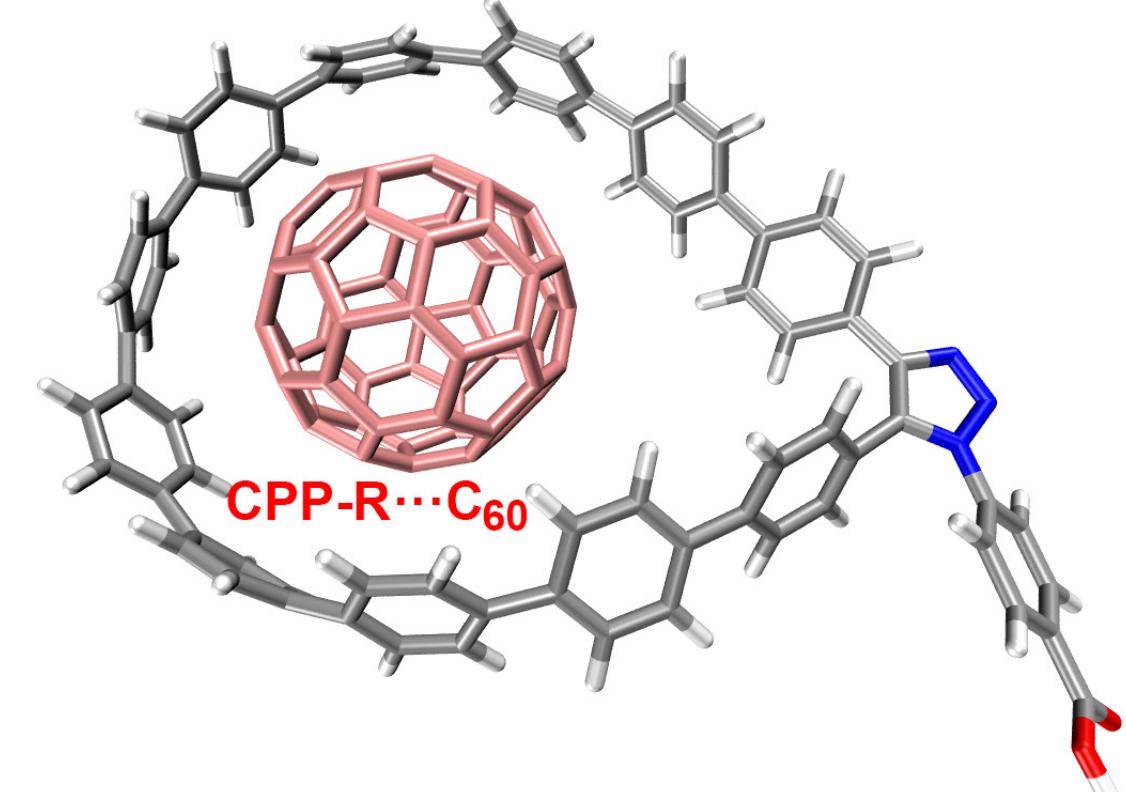
	1nπ*	3nπ*	3ππ*	
exp.	1.323	1.307	1.423	1.320
AIQM1	1.339	1.304	1.608	1.342
TDDFT	1.296	1.298	—	1.304
CC2	1.361	1.343	1.469	1.387

dr-dral.c

47

# AIQM1 investigation of cycloparaphenylenes

AIQM1 also predicts fluorescence quenching



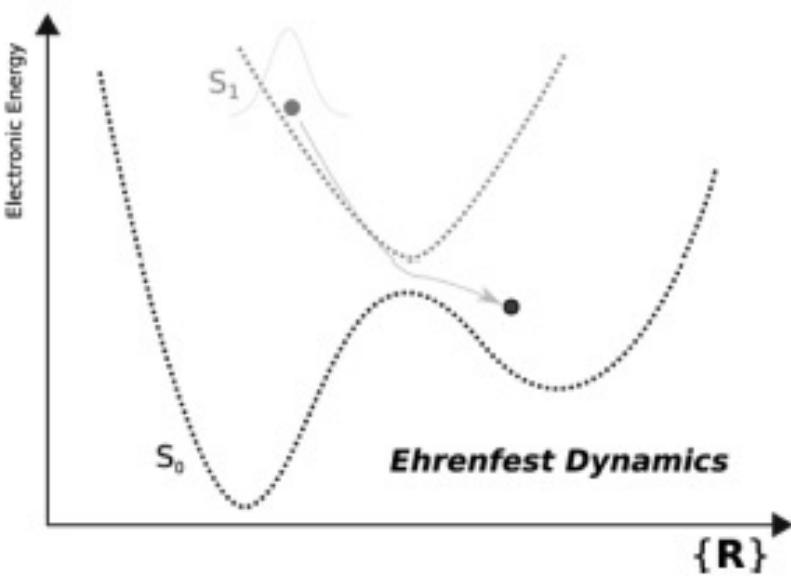
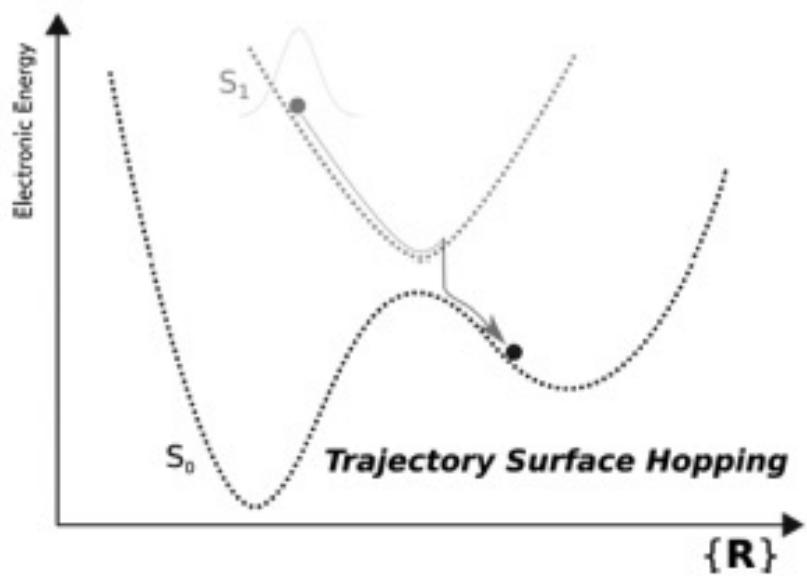
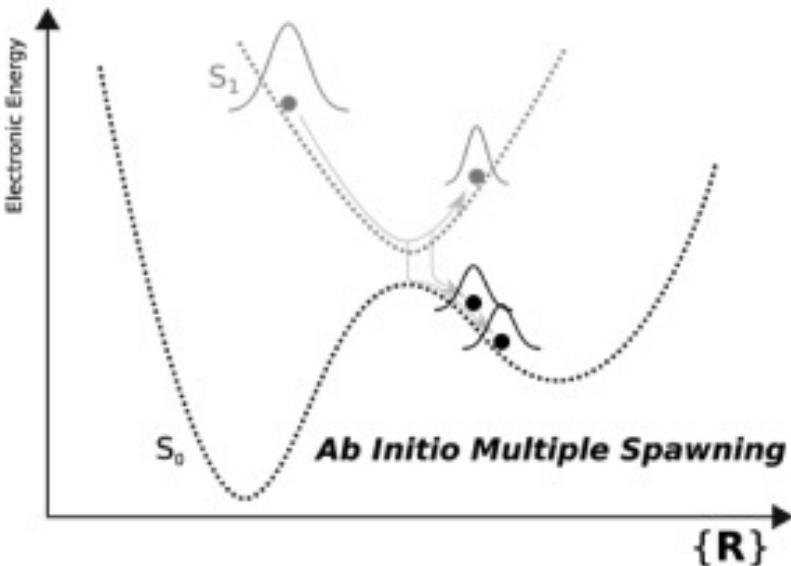
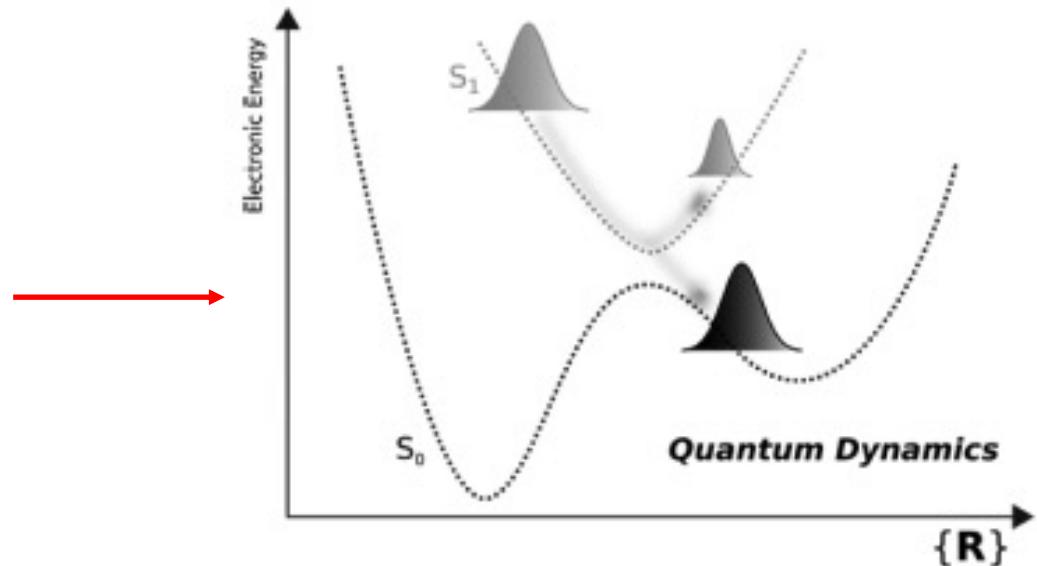
**Table S9.** Emission energy and oscillator strengths *f* of free molecules and their complexes with C<sub>60</sub> and C<sub>70</sub> at AIQM1/CIS in vacuum (S<sub>1</sub> to S<sub>0</sub> transition).

Species	<i>f</i>	Energy (eV)
3	0.750	3.11
4	0.751	3.12
5	0.750	3.12
6	0.750	3.12
7	0.748	3.12
3 ⊰ C <sub>60</sub>	0.000	2.58
4 ⊰ C <sub>60</sub>	0.000	2.58
5 ⊰ C <sub>60</sub>	0.000	2.58
6 ⊰ C <sub>60</sub>	0.000	2.58
7 ⊰ C <sub>60</sub>	0.000	2.59
M-3 ⊰ C <sub>70</sub>	0.000	2.10
M-4 ⊰ C <sub>70</sub>	0.000	2.09
M-5 ⊰ C <sub>70</sub>	0.000	2.10
M-6 ⊰ C <sub>70</sub>	0.000	2.10
M-7 ⊰ C <sub>70</sub>	0.000	2.10

AIQM1 can be useful for aggregation-induced emission,  
photocatalysis

T. A. Schaub, A. Zieleniewska, R. Kaur, M. Minameyer, W. Yang, C. M. Schüßlbauer, L. Zhang, M. Freiberger, L. N. Zakharov, T. Drewello, P. O. Dral, D. Guldi, R. Jasti. Tunable Macroyclic Poly paraphylene Nanolassos via Copper-Free Click Chemistry. *Chem. Eur. J.* **2023**, 29, e202300668

# Many flavors for quantum dynamics (QD)



# *Wish list for quantum dynamics (QD)*

- Treat both nuclei and electrons quantum mechanically
- Treat the system and environment
- Computationally fast enough for real systems

# Quantum dynamics of open systems

$$\hat{H} = \hat{H}_S + \hat{H}_{\text{env}} + \hat{H}_{\text{s-env}} [+ \hat{H}_{\text{reorg}}]$$

- $\hat{H}_S$  Hamiltonian of the system
- $\hat{H}_{\text{env}}$  Hamiltonian of environment (bath)
- $\hat{H}_{\text{s-env}}$  Hamiltonian of system-environment (system-bath) interaction
- $\hat{H}_{\text{reorg}}$  the reorganization terms

# Different ways to propagate QD

$$\frac{d}{dt} \rho(t) = \frac{i}{\hbar} [\hat{H}, \rho(t)]$$

Different integrators of Liouville–von Neumann equation,  $\rho$  – the density matrix

- hierarchical equations of motion (HEOM)
- the local thermalising Linblad master equation (LTLME)
- ...

# ***Machine learning to speed up dynamics***

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics

dynamics propagation is

- computationally expensive

# **Machine learning to speed up dynamics**

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

- computationally expensive

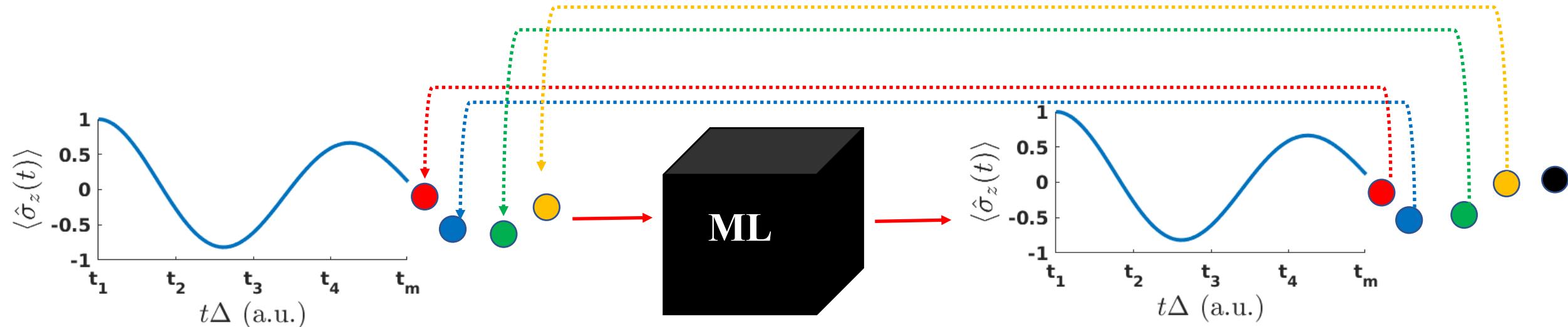
dynamics



ML dynamics

$$\rho(t) = f^{\text{ML}}[\rho(t - \Delta t)]$$

# Machine learning to speed up dynamics



$$\rho(t) = f^{\text{ML}}[\rho(t - \Delta t)]$$



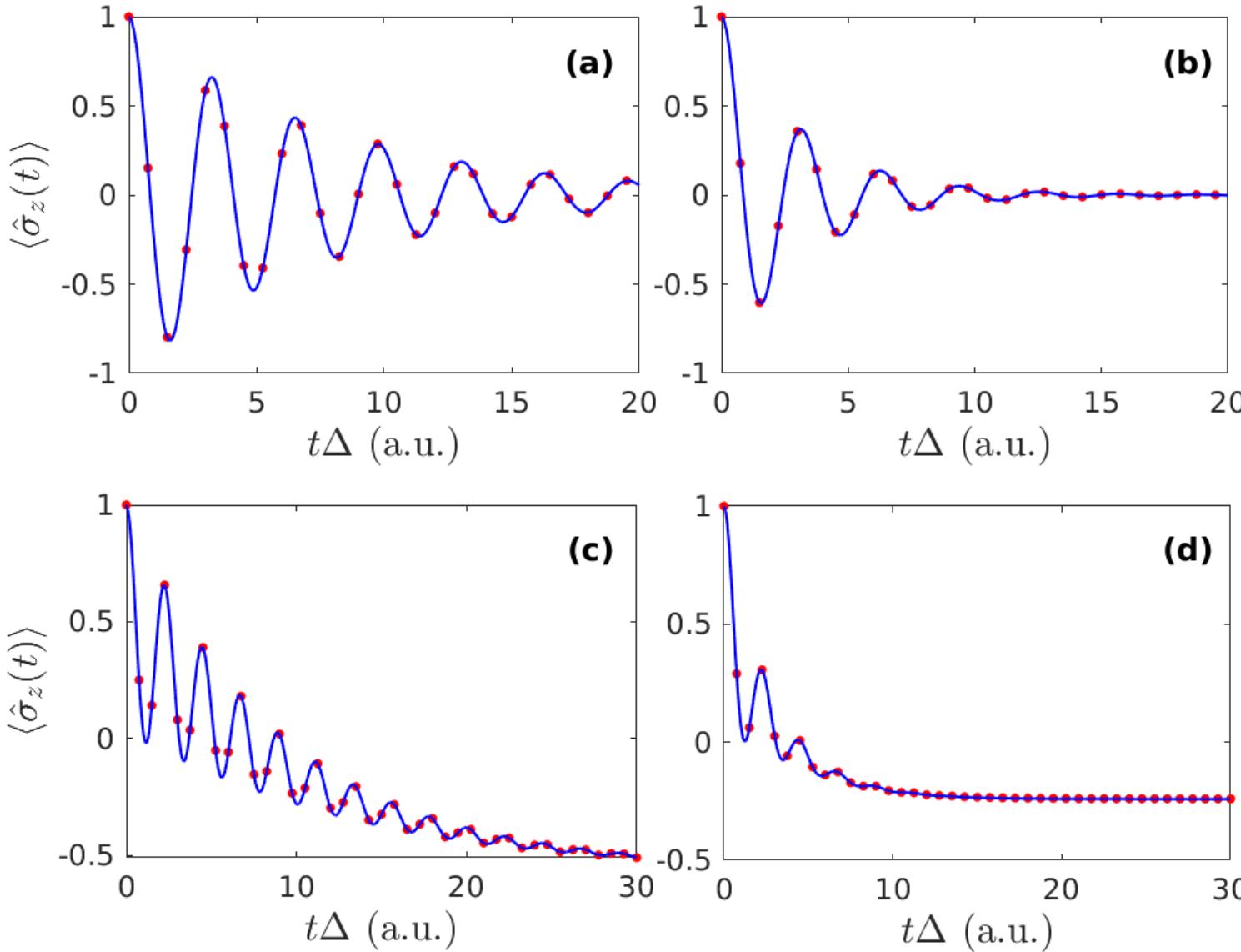
Spin-boson Hamiltonian:

$$\hat{H} = \frac{1}{2}\varepsilon\hat{\sigma}_z + \frac{1}{2}\Delta\hat{\sigma}_x + \sum_k \omega_k \hat{b}_k^\dagger \hat{b}_k + \hat{\sigma}_z \sum_k c_k (\hat{b}_k^\dagger + \hat{b}_k)$$

Arif Ullah

A. Ullah, P. O. Dral. Speeding up quantum dissipative dynamics of open systems with kernel methods. *New J. Phys.* **2021**, 23, 113019

# Machine learning to speed up dynamics



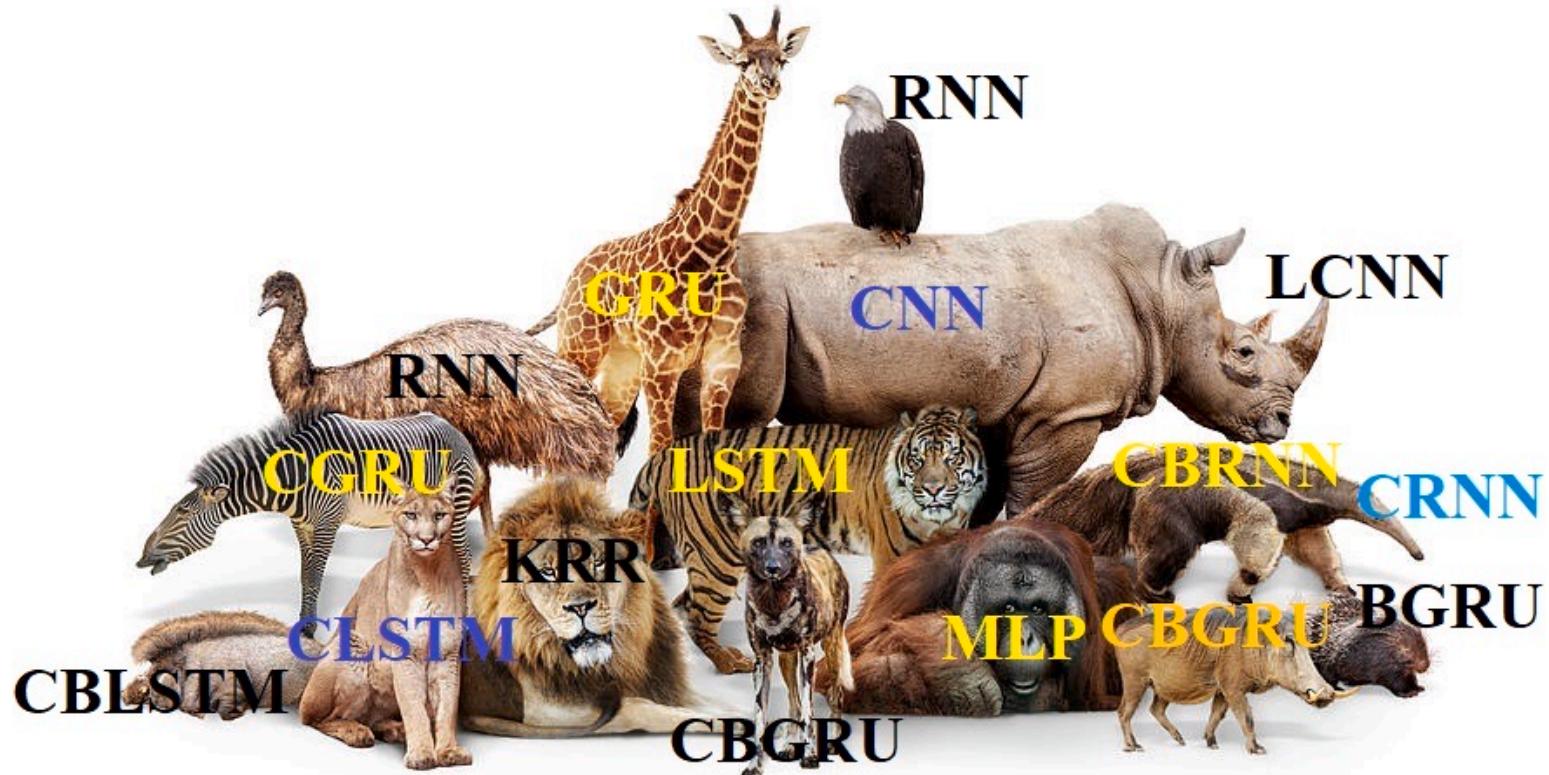
Test (unseen) trajectories for parameters not used in training trajectories

# Machine learning to speed up dynamics

$$\rho(t) = f^{\text{ML}}[\rho(t - \Delta t)]$$

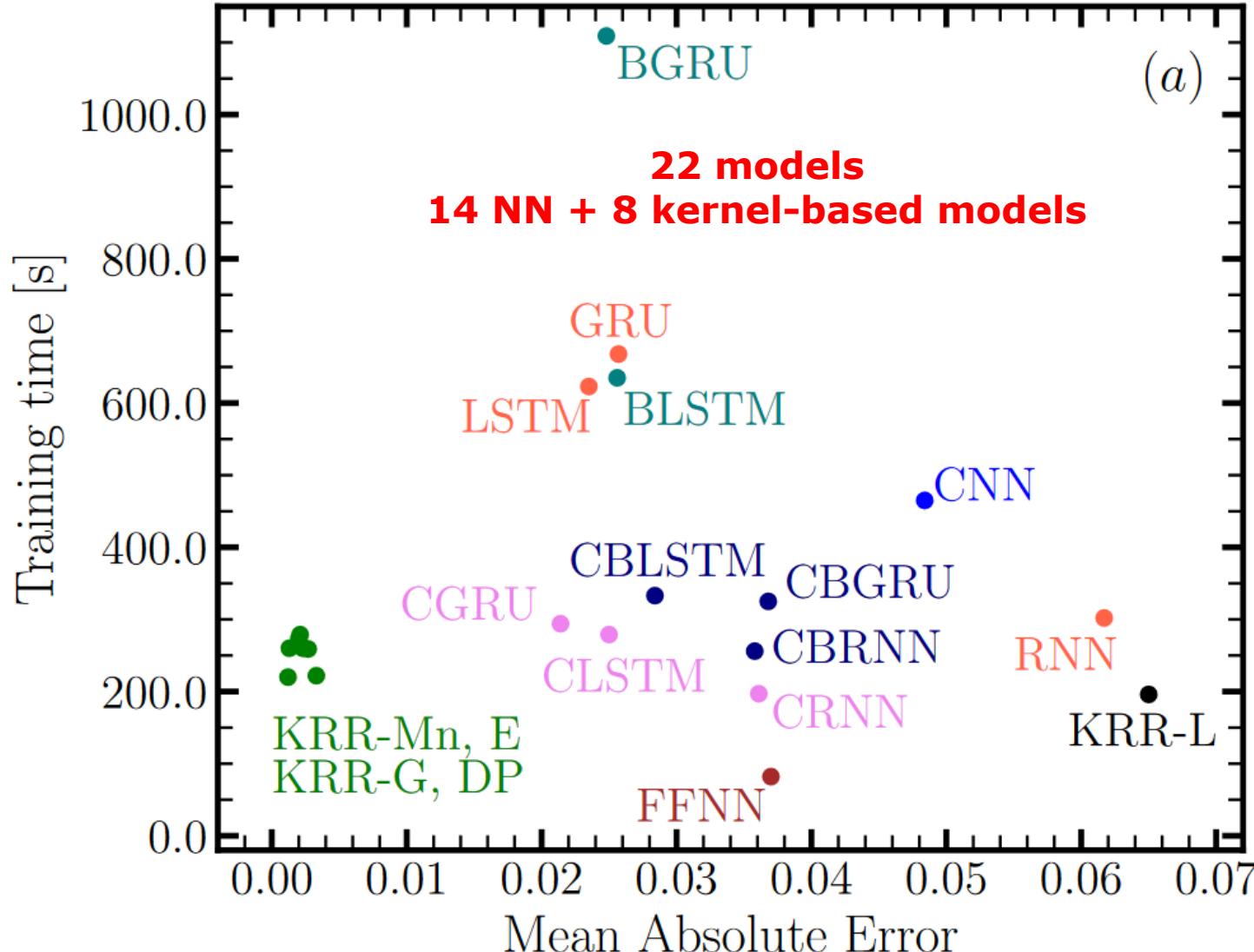
Many ways to do it:

- different algorithms
- different properties to learn ( $\rho$  or population)
- different systems, data sets...



- L. E. Herrera Rodriguez, A. A. Kananenka. **Convolutional Neural Networks** for Long Time Dissipative Quantum Dynamics. *J. Phys. Chem. Lett.* **2021**, 12, 2476–2483
- K. Lin, J. Peng, F. L. Gu, Z. Lan. Simulation of Open Quantum Dynamics with Bootstrap-Based **Long Short-Term Memory Recurrent Neural Network**. *J. Phys. Chem. Lett.* **2021**, 12, 10225–10234
- A. Ullah, P. O. Dral. Speeding up quantum dissipative dynamics of open systems with **kernel methods**. *New J. Phys.* **2021**, 23, 113019

# Good ML method for quantum dynamics?



Alexei  
Kananenka



Arif Ullah

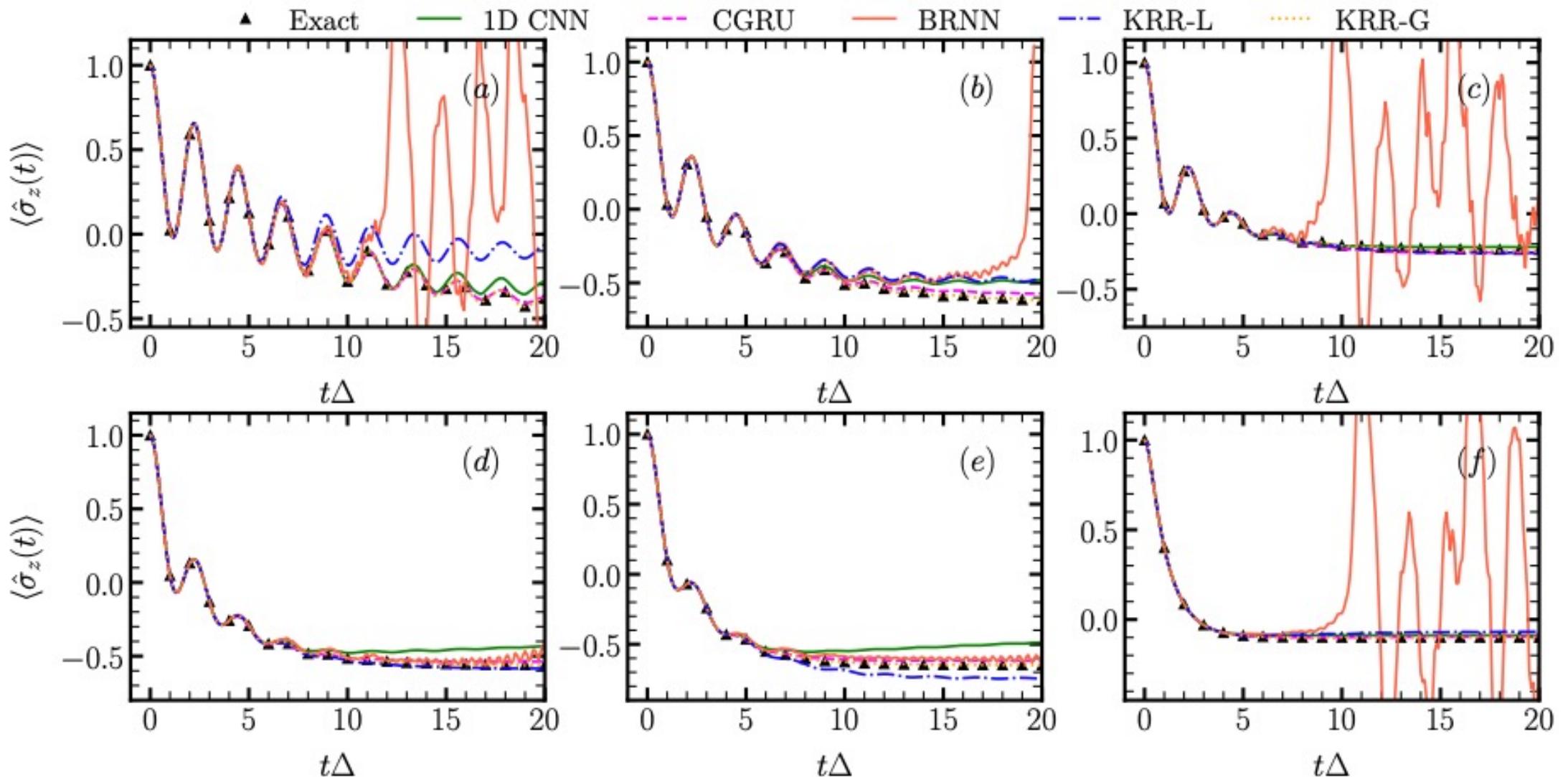


Luis Eduardo  
Herrera  
Rodríguez



Kennet  
Julian R.  
Espinosa

# Good ML method for quantum dynamics?



# ***Machine learning to speed up dynamics***

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

- computationally expensive

dynamics



ML dynamics

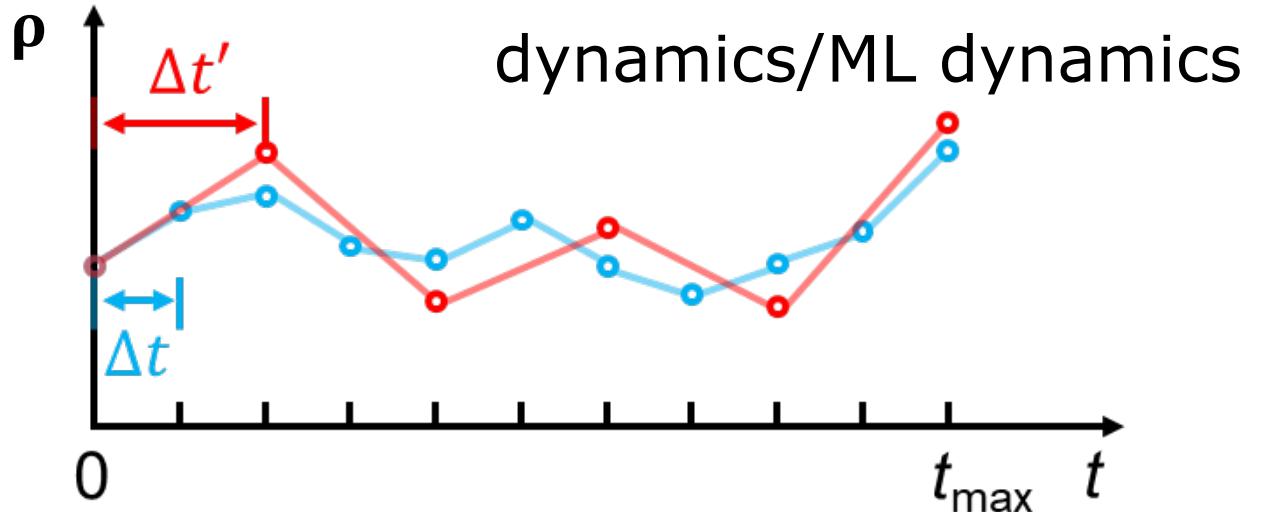
$$\rho(t) = f^{\text{ML}}[\rho(t - \Delta t)]$$

# Can we do better?

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

- computationally expensive
- recursive (iterative)



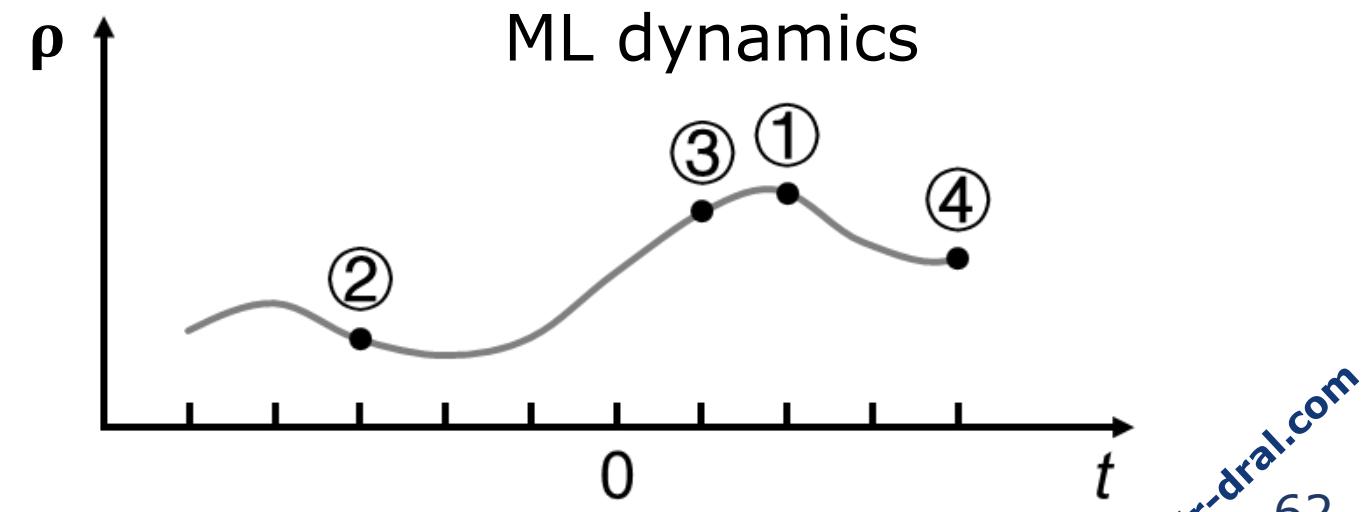
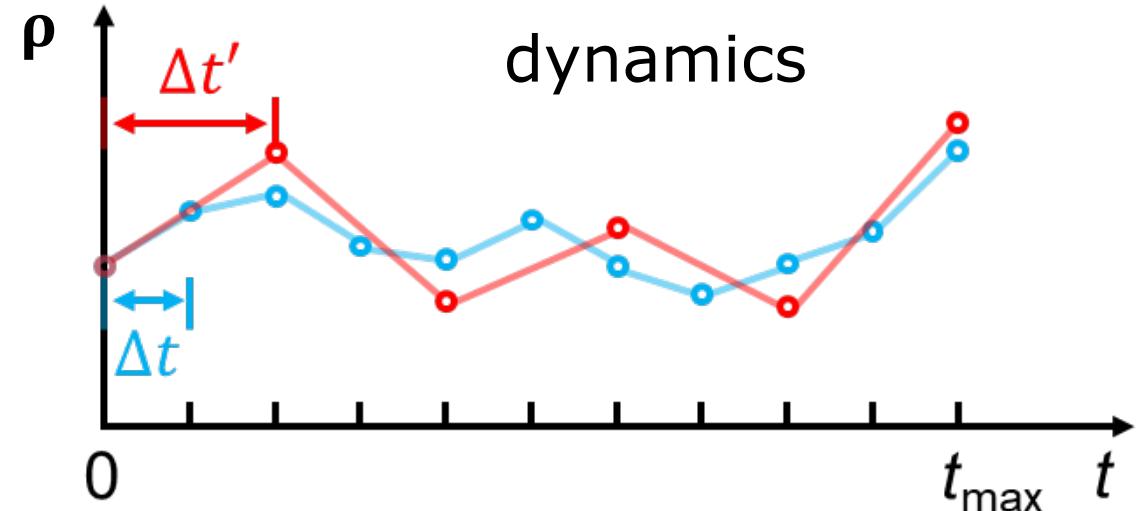
# Can we do better?

$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

- computationally expensive
- recursive (iterative)

$$\rho(t) = f[t; \text{other parameters}]$$



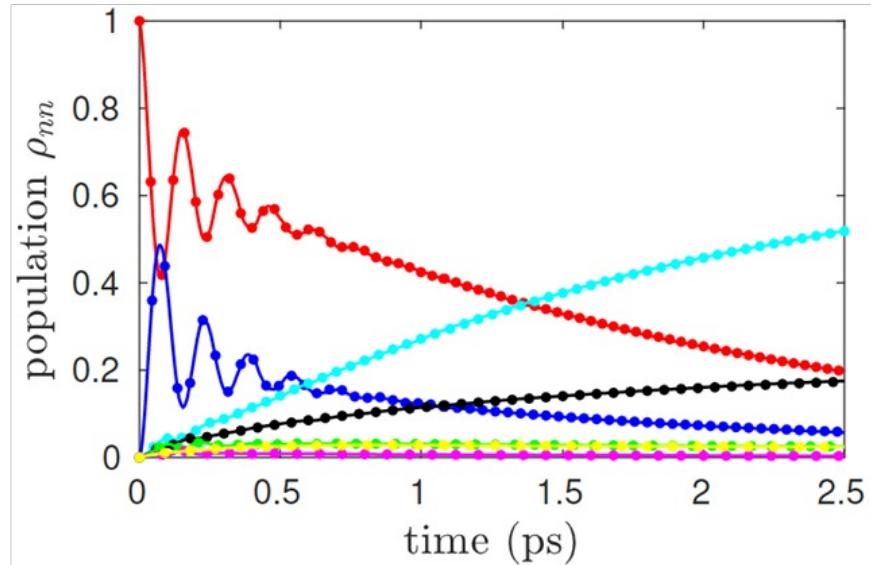
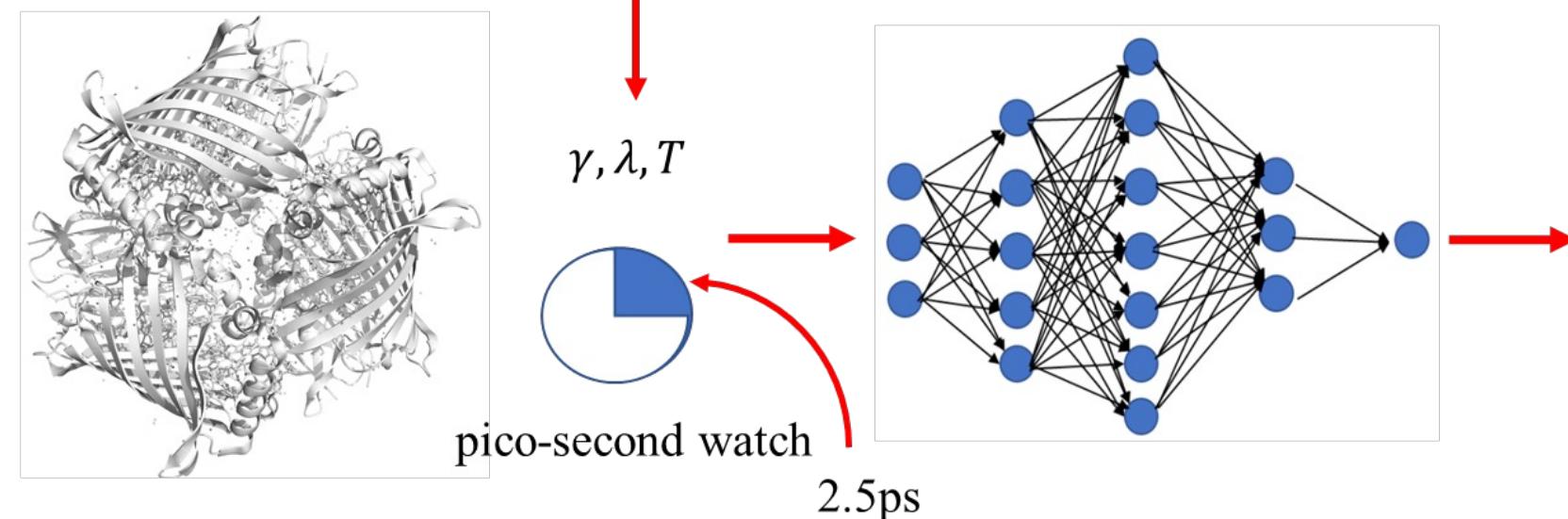
$\gamma$  = characteristic frequency

$\lambda$  = reorganization energy

$T$  = temperature

$$\rho(\text{time}) = f[\text{time}; \text{simulation parameters}]$$

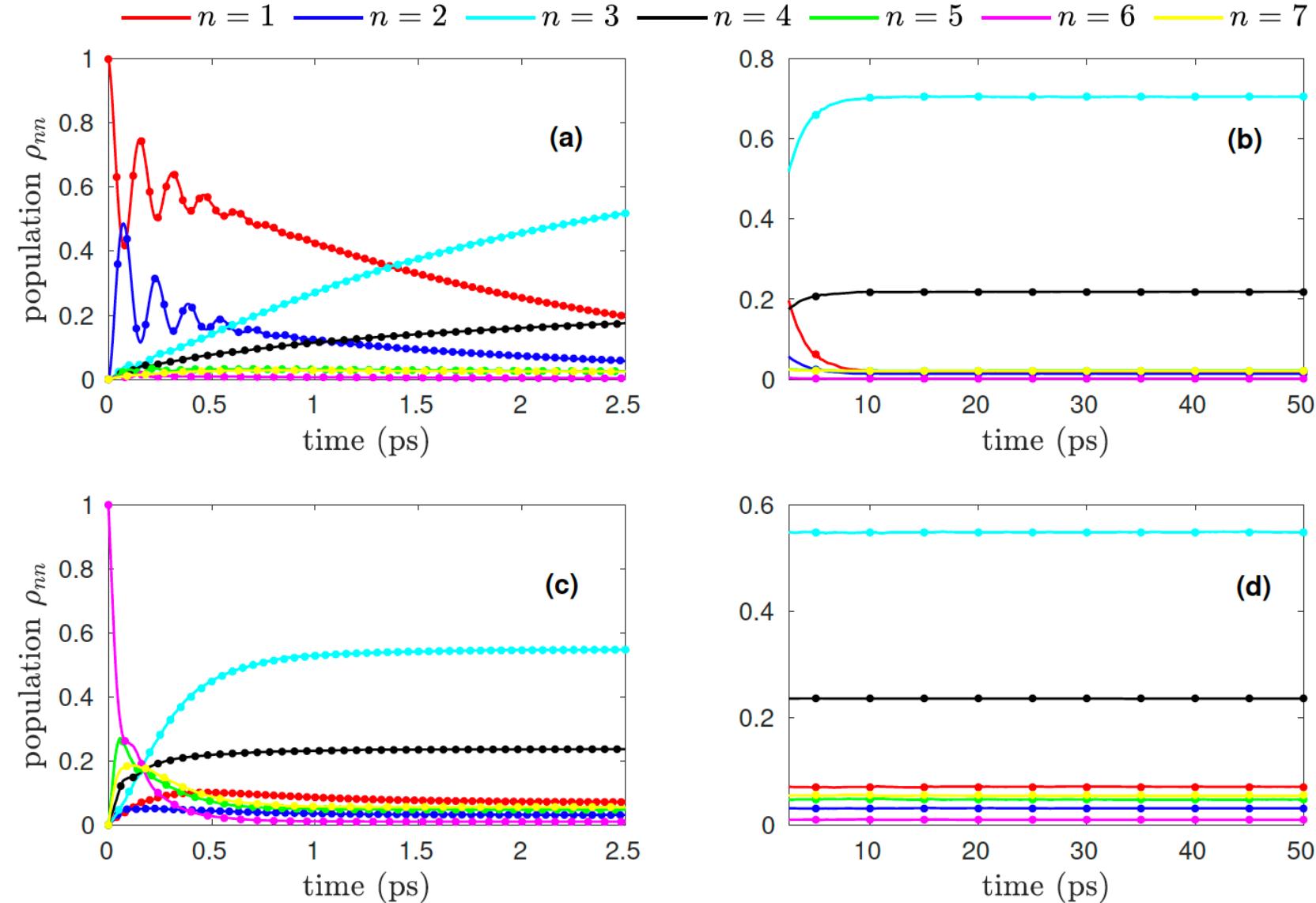
PDB code: 3ENI



7-sites Fenna–Matthews–Olson (FMO) complex

A. Ullah, P. O. Dral. Predicting the future of excitation energy transfer in light-harvesting complex with artificial intelligence-based quantum dynamics. *Nat. Commun.* **2022**, *13*, 1930

# AI-QD vs reference trajectories



Test (unseen) trajectories for parameters not used in training trajectories

Predictions of 0.57M trajectories up to 1 ns

# Can we do even better?

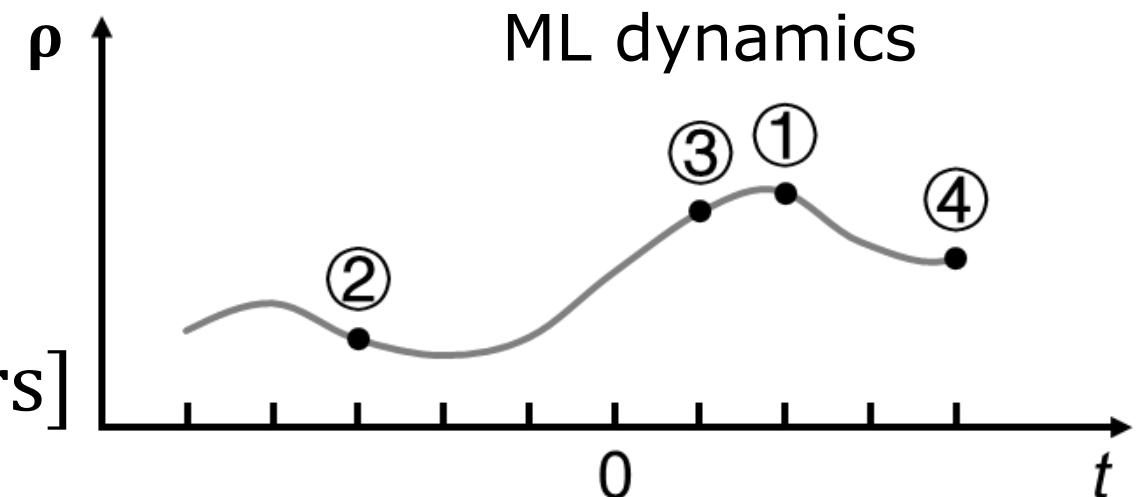
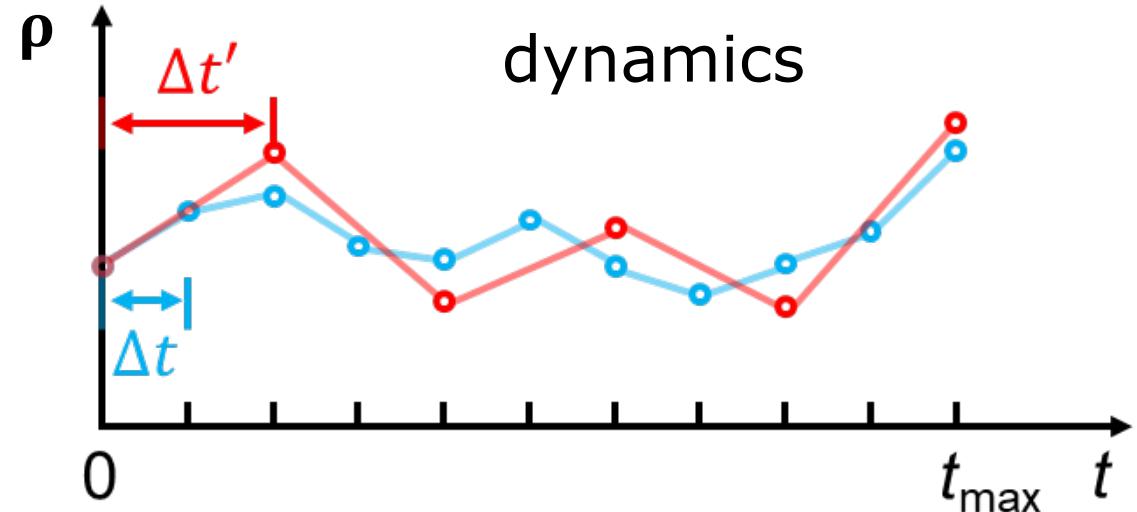
$$\rho(t) = f[\rho(t - \Delta t)]$$

dynamics propagation is

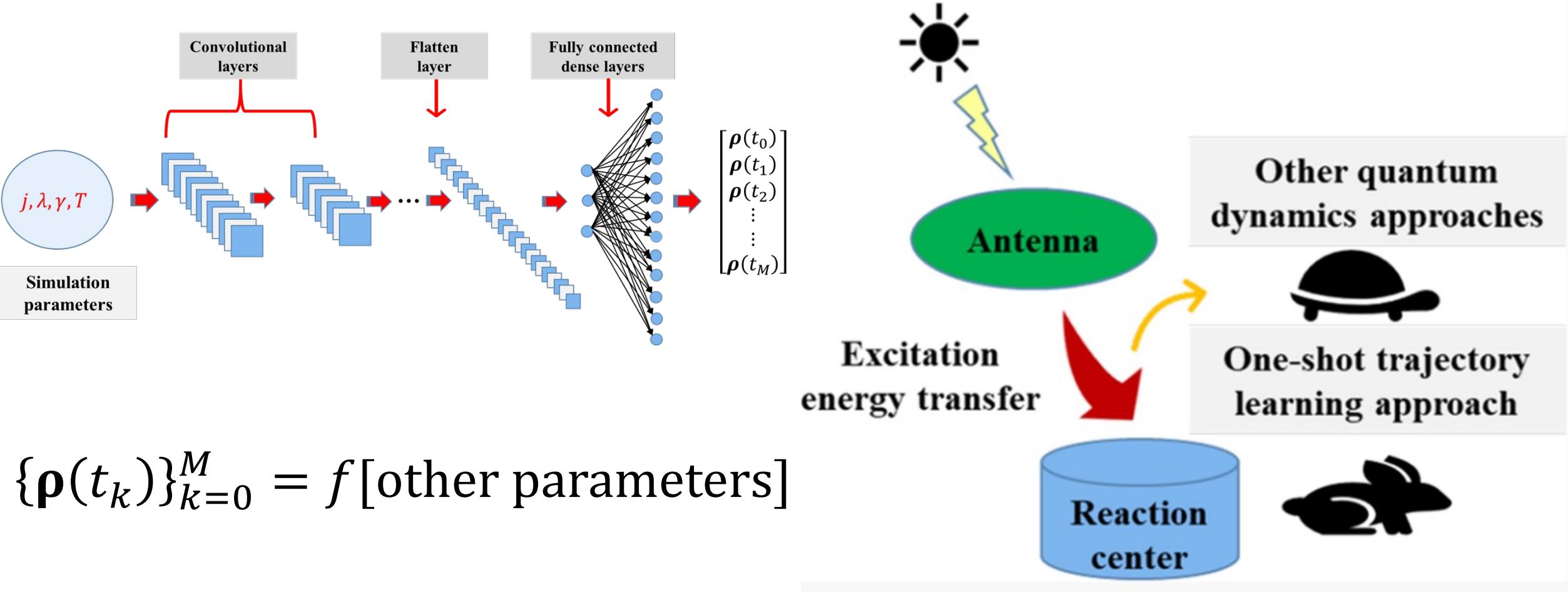
- computationally expensive
- recursive (iterative)

$$\rho(t) = f[t; \text{other parameters}]$$

$$\{\rho(t_k)\}_{k=0}^M = f[\text{other parameters}]$$



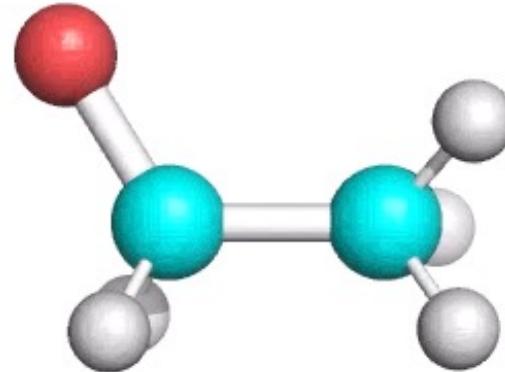
# One-Shot Trajectory Learning (OSTL)



$$\{\rho(t_k)\}_{k=0}^M = f[\text{other parameters}]$$

- **10 ps long dynamics in just 70 ms**
- good for massive simulation in parameter space

3D MD

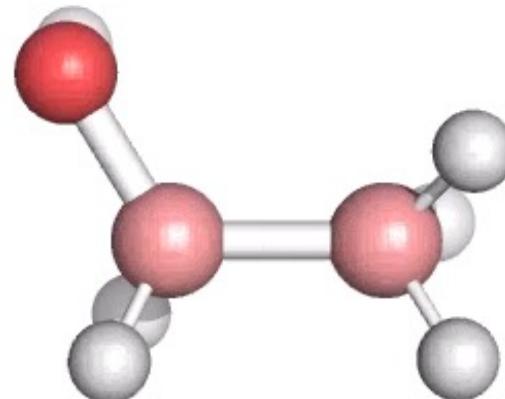


Very slow

## The direct learning of molecular dynamics with 4D-spacetime GICnet models



4D- $A^2I$



0.05 fs

Very fast, e.g., 1 ps trajectory (time step 0.05 fs) within 1 minute

Fuchun Ge

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University of Tennessee, US

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*Dates TBD*