

Recent advances in modelling plasmon-assisted hot-carrier dynamics

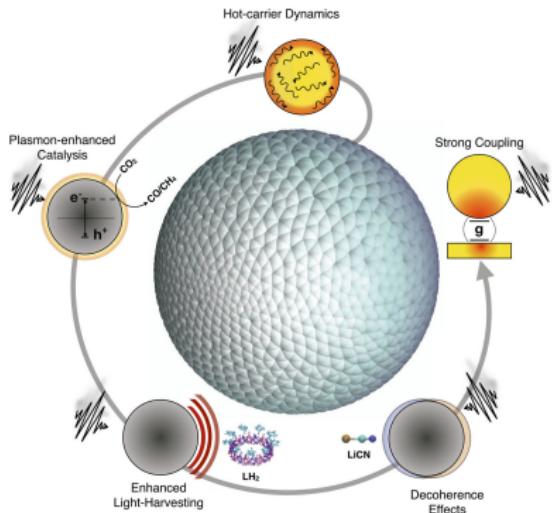
Emanuele Coccia

Dipartimento di Scienze Chimiche e Farmaceutiche, Università di Trieste, Via Giorgieri 1, 34127, Trieste

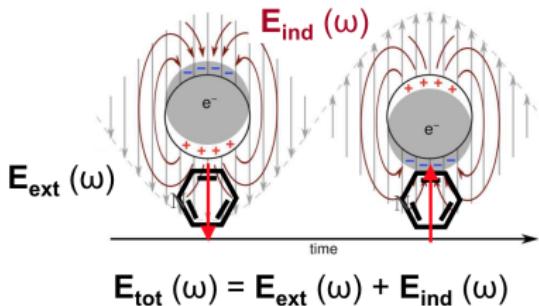


VISTA seminar

Molecular plasmonics



- Collective electron excitations in a nanoparticle (NP)
- Au, Ag, ...
- Exceptional tunable (size, shape, material) optical properties
- Sensitivity and selectivity
- Enhancement or quenching of molecular absorption, ...

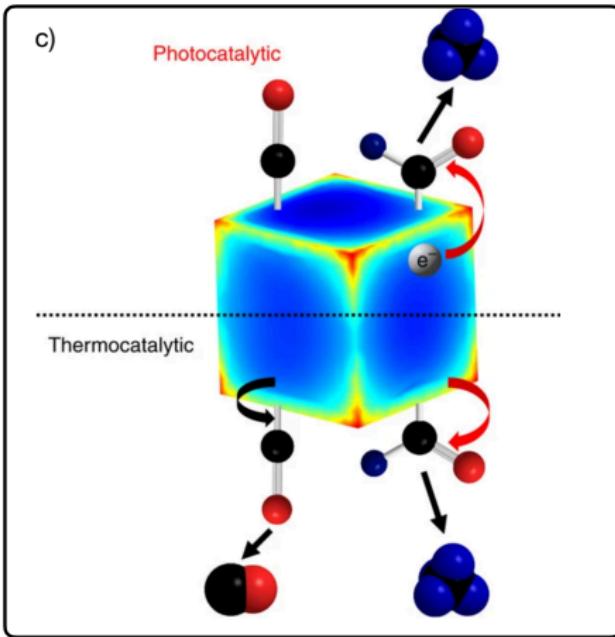
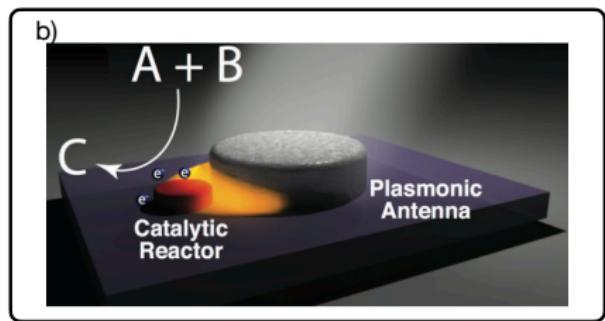
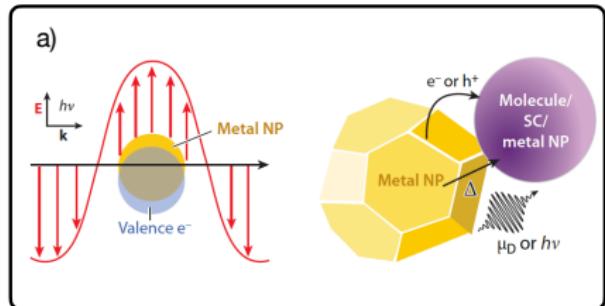


R. P. Van Duyne, *Science*, **306**, 985 (2004)
A. Lauchner *et al.*, *Nano Lett.*, **15**, 6208 (2015)
S. Ezendam *et al.*, *ACS Energy Lett.*, **7**, 778 (2022)

$$|E_{tot}| \gg |E_{ext}|$$

Plasmon-mediated photocatalysis

Plasmon-mediated photocatalysis



D. F. Swearer *et al.*, PNAS, **113**, 8916 (2016)

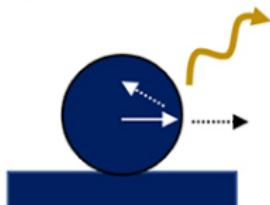
X. Zhang, X. Li, D. Zhang, N. Q. Su, W. Yang, H. O. Everitt and J. Liu, Nat. Commun., **8**, 14542 (2017)

J. M. P. Martinez, J. L. Bao and E. A. Carter, Annu. Rev. Phys. Chem., **72**, 99 (2021)

Hot-carrier generation



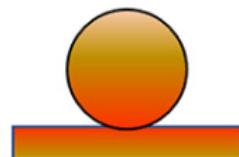
Plasmon excitation
 $t = 0 \text{ s}$



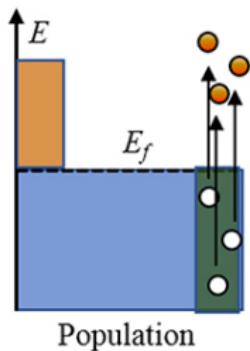
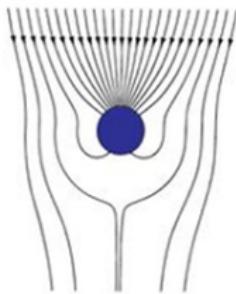
Landau damping
 $t = 1 - 100 \text{ fs}$



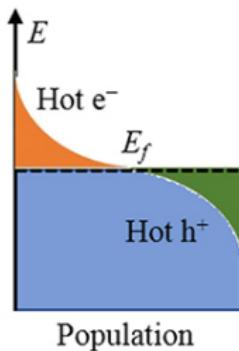
Carrier relaxation
 $t = 100 \text{ fs} - 1 \text{ ps}$



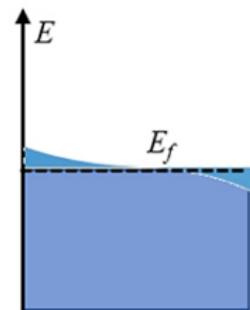
Thermal dissipation
 $t = 100 \text{ ps} - 10 \text{ ns}$



Population



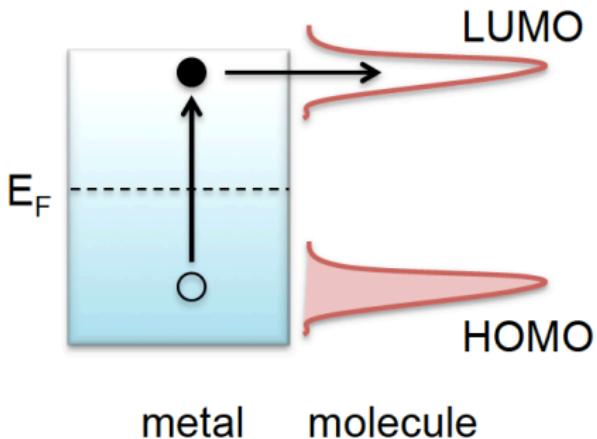
Population



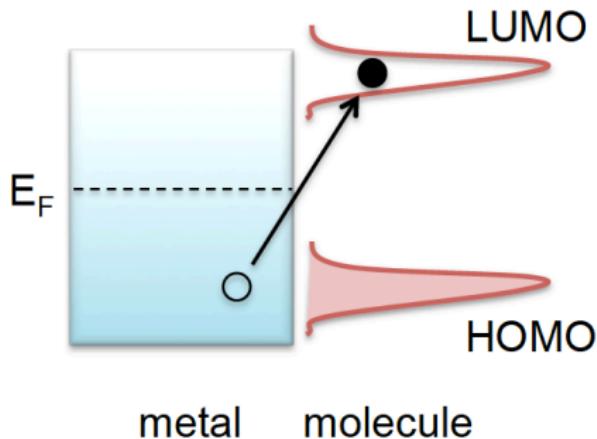
Population

Hot-carrier generation

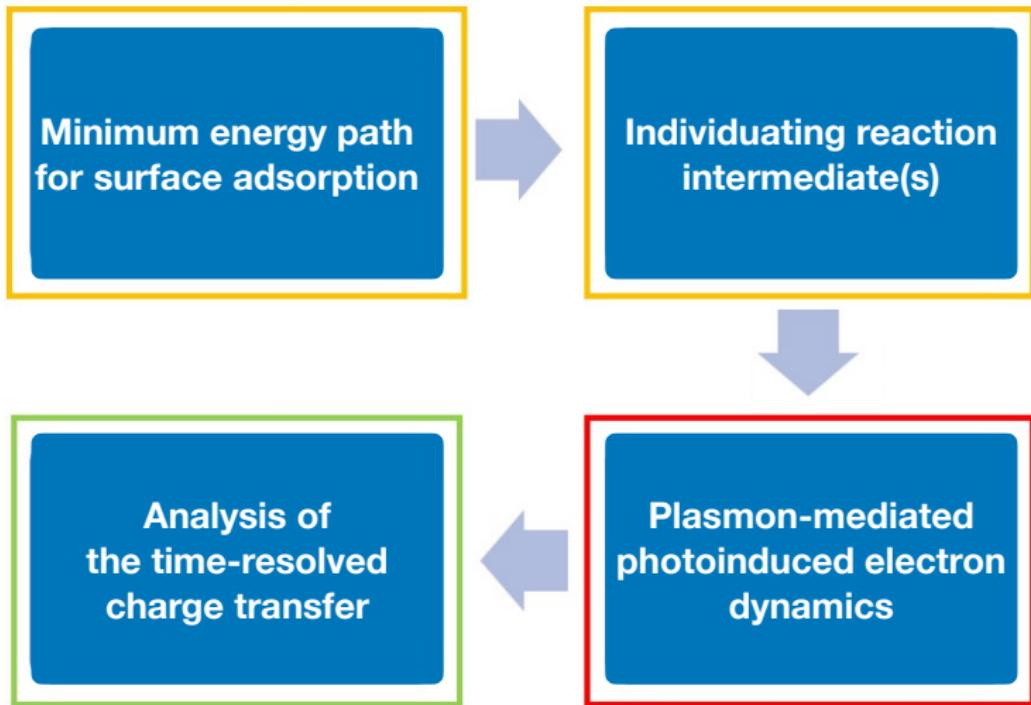
Indirect transfer



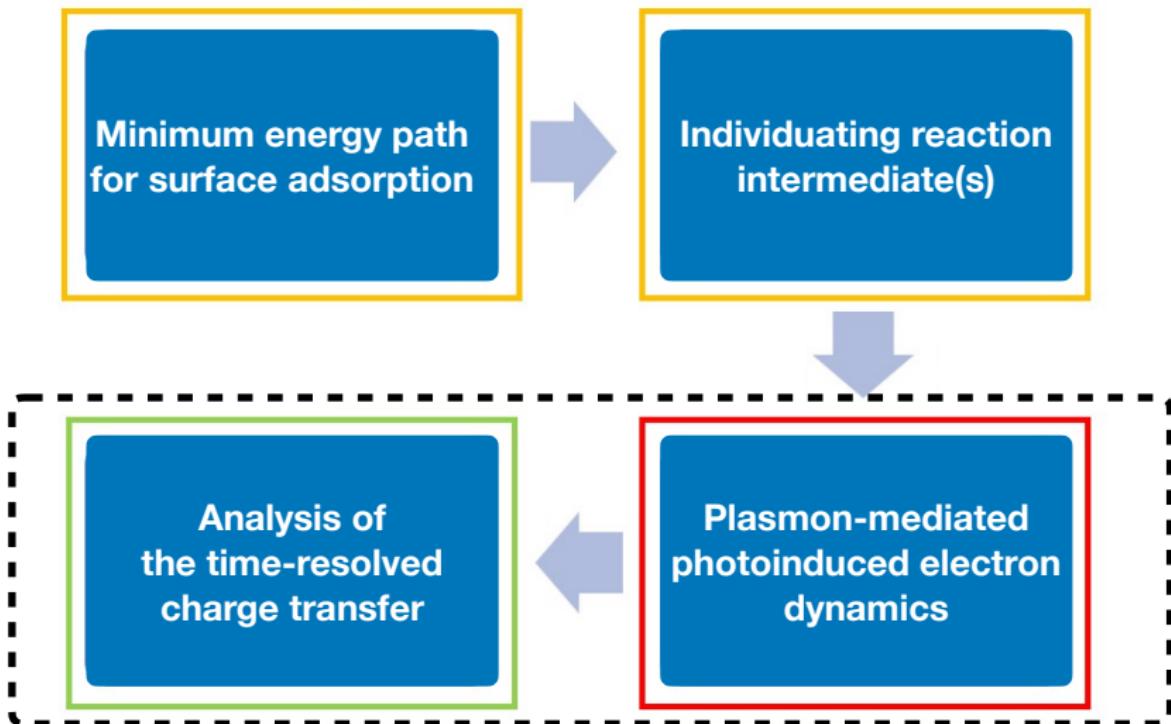
Direct transfer



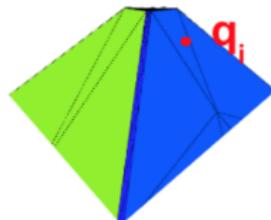
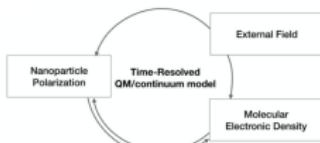
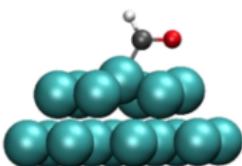
Plasmon-mediated photocatalysis: modelling



Plasmon-mediated photocatalysis: modelling



Time-domain QM/continuum approach



Time-dependent Schrödinger equation

$$i \frac{\partial |\Psi(t)\rangle}{\partial t} = \hat{H}(t) |\Psi(t)\rangle$$

$$\hat{H}(t) = \hat{H}_0 - \vec{\mu} \vec{E}_{ext}(t) + \mathbf{q}(t) \mathbf{V}$$

$$|\Psi(t)\rangle = \sum_{\lambda} C_{\lambda}(t) |\lambda\rangle$$

$$|\lambda\rangle = \sum_i \sum_a d_{i,\lambda}^a |\Phi_i^a\rangle$$

EOM for surface charges

$$\mathbf{q}(\omega) = \frac{1}{2\pi} f(\omega) \mathbf{F}(\omega)$$

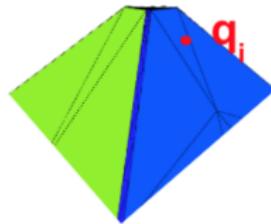
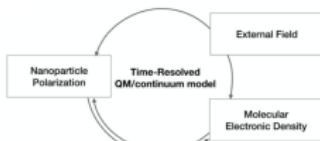
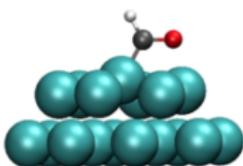
$$f(\omega) = \frac{\epsilon(\omega) - 1}{\epsilon(\omega) + 1}$$

$$\begin{aligned} \mathbf{F}(\omega) &= -[\mathbf{AD}^* \mathbf{q}(\omega) \\ &+ \mathbf{S}^{-1} (2\pi \mathbf{I} + \mathbf{DA}) \mathbf{V}(\omega)] \end{aligned}$$

$$\ddot{\mathbf{q}}(t) = -\gamma \dot{\mathbf{q}}(t) - \mathbf{Q}_{\omega} \mathbf{q}(t) + \mathbf{Q}_f \mathbf{q}(t)$$

Reaction field theory and time-resolved QM/continuum approach for nanoparticles

Time-domain QM/continuum approach



Time-dependent Schrödinger equation

$$i \frac{\partial |\Psi(t)\rangle}{\partial t} = \hat{H}(t) |\Psi(t)\rangle$$

$$\hat{H}(t) = \hat{H}_0 - \vec{\mu} \vec{E}_{ext}(t) + \mathbf{q}(t) \mathbf{V}$$

$$|\Psi(t)\rangle = \sum_{\lambda} C_{\lambda}(t) |\lambda\rangle$$

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$$\ddot{\mathbf{q}}(t) = -\gamma \dot{\mathbf{q}}(t) - \mathbf{Q}_{\omega} \mathbf{q}(t) + \mathbf{Q}_f \mathbf{q}(t)$$

Real-time simulations with polarizable continuum model (RT-PCM-NP)

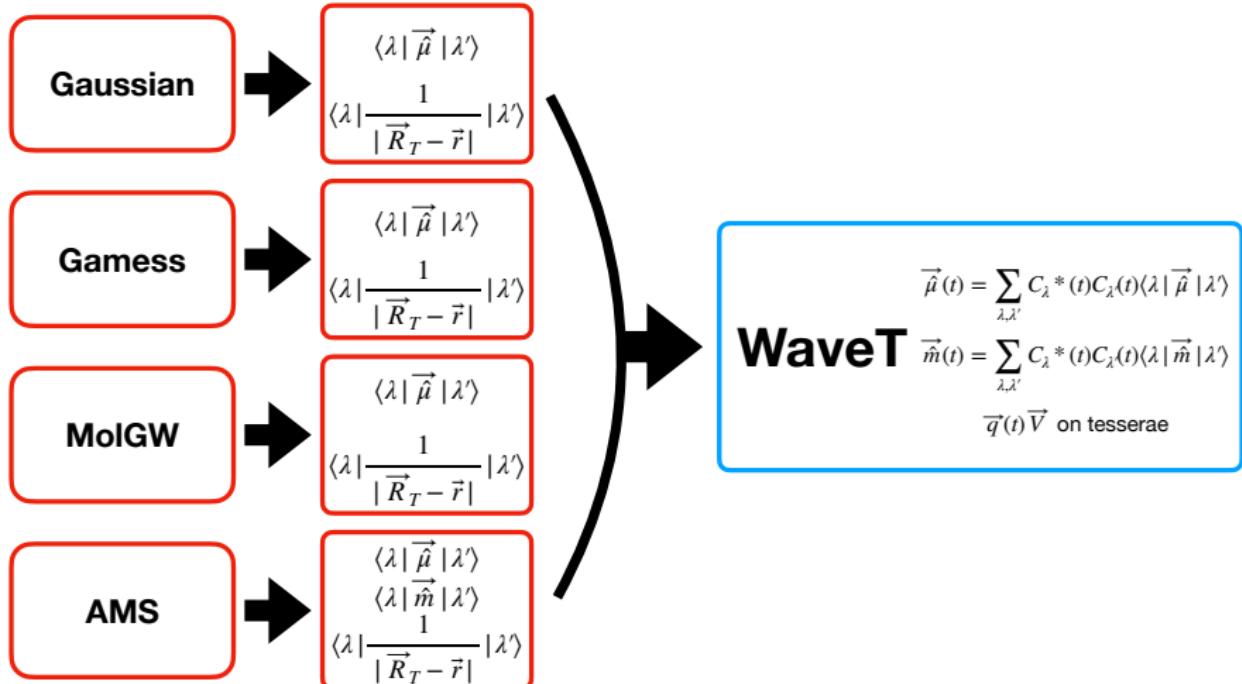
S. Pipolo and S. Corni, *J. Phys. Chem. C*, **120**, 28774 (2016)

EC and S. Corni, *J. Chem. Phys.*, **151**, 044703 (2019)

G. Dall'Osto, G. Gil, S. Pipolo and S. Corni, *J. Chem. Phys.*, **153**, 184114 (2020)

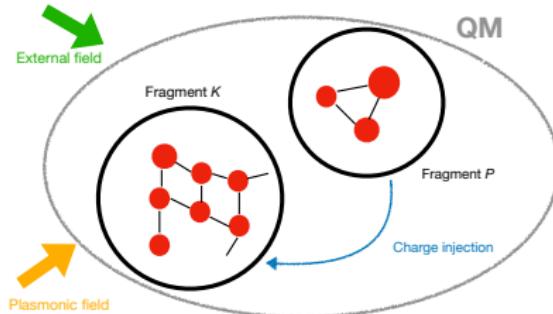
EC, J. Fregoni, C. A. Guido, M. Marsili, S. Pipolo and S. Corni, *J. Chem. Phys.*, **153**, 200901 (2020)

Time-domain QM/continuum model



WaveT: https://github.com/stefano-corni/WaveT_TDPlas

Time-domain QM/continuum model



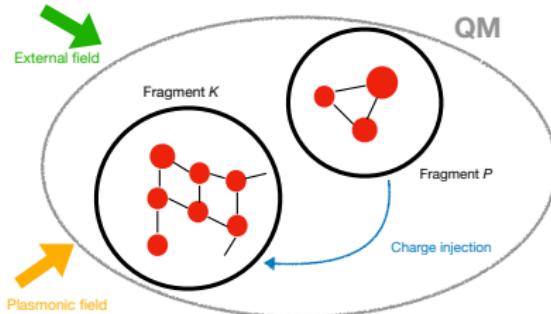
- $\Delta \text{PDOS}_K(t, \epsilon) \equiv \text{PDOS}_K(t, \epsilon) - \text{PDOS}(0, \epsilon)$

$$\begin{aligned}\Delta \text{PDOS}_K(t, \epsilon) &= - \sum_i^{occ} w_i^K \text{Re} \left[\sum_{\lambda, \lambda'} C_\lambda^*(t) C_{\lambda'}(t) \sum_a^{vir} (d_{i,\lambda}^a)^* d_{i,\lambda'}^a \right] L(\epsilon - \epsilon_i) \\ &+ \sum_a^{vir} w_a^K \text{Re} \left[\sum_{\lambda, \lambda'} C_\lambda^*(t) C_{\lambda'}(t) \sum_i^{occ} (d_{i,\lambda}^a)^* d_{i,\lambda'}^a \right] L_\eta(\epsilon - \epsilon_i)\end{aligned}$$

Charge population

Electron/hole (APDOS) Charge transfer

Time-domain QM/continuum model



- $\Delta \text{PDOS}_K(t, \epsilon) \equiv \text{PDOS}_K(t, \epsilon) - \text{PDOS}(0, \epsilon)$

$$\begin{aligned}\Delta \text{PDOS}_K(t, \epsilon) &= - \sum_i^{occ} w_i^K \text{Re} \left[\sum_{\lambda, \lambda'} C_\lambda^*(t) C_{\lambda'}(t) \sum_a^{vir} (d_{i,\lambda}^a)^* d_{i,\lambda'}^a \right] L(\epsilon - \epsilon_i) \\ &+ \sum_a^{vir} w_a^K \text{Re} \left[\sum_{\lambda, \lambda'} C_\lambda^*(t) C_{\lambda'}(t) \sum_i^{occ} (d_{i,\lambda}^a)^* d_{i,\lambda'}^a \right] L_\eta(\epsilon - \epsilon_i)\end{aligned}$$

- Charge population

$$\text{electron/hole: } \frac{1}{2} \int_{-\infty}^{\infty} [\Delta \text{PDOS}(t, \epsilon) \pm |\Delta \text{PDOS}(t, \epsilon)|] d\epsilon$$

Carbon dioxide hydrogenation

ARTICLE

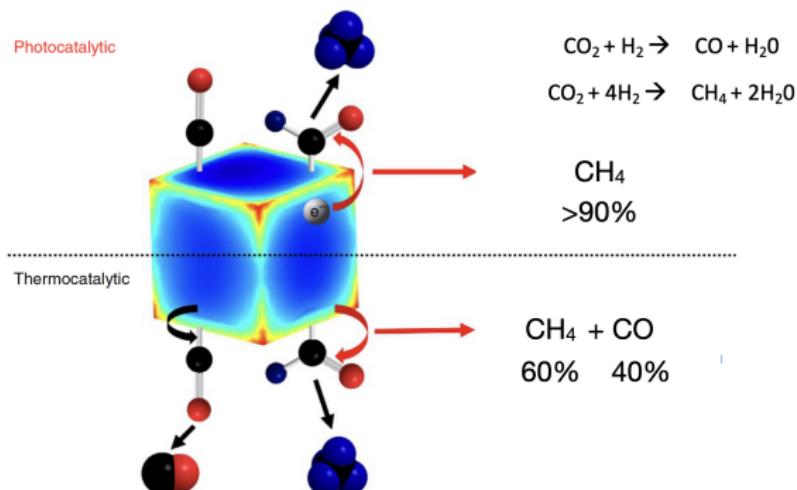
Received 28 Sep 2016 | Accepted 11 Jan 2017 | Published 23 Feb 2017

DOI: 10.1038/ncomms14542

OPEN

Product selectivity in plasmonic photocatalysis for carbon dioxide hydrogenation

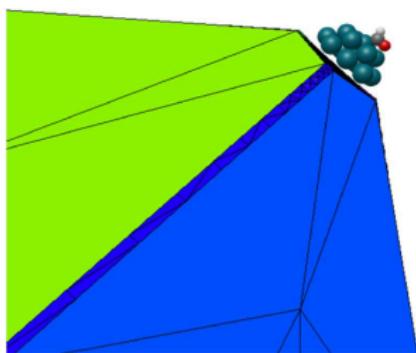
Xiao Zhang¹, Xueqian Li¹, Du Zhang¹, Neil Qiang Su¹, Weitao Yang¹, Henry O. Everitt^{2,3} & Jie Liu¹



Selectivity enhancement due to hot carriers?

X. Zhang, X. Li, D. Zhang, N. Q. Su, W. Yang, H. O. Everitt and J. Liu, *Nat. Commun.*, **8**, 14542 (2017)

Results: modelling the system



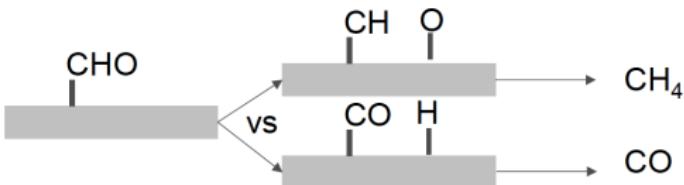
- QM portion

- Two Rh layers from Rh(111) slab
- CHO-Rh₁₉ optimized at DFT (PBE/DZ) level (AMS)

- Classical portion

- Rh nanocube 37 nm in side (as in exp.)
- $\epsilon(\omega)$ from exp.

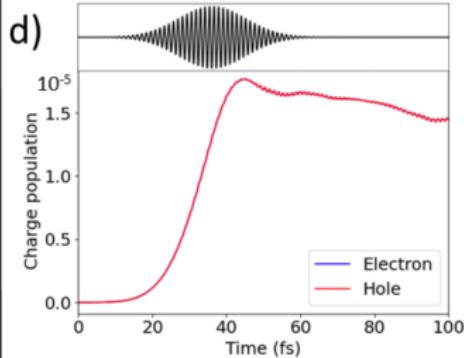
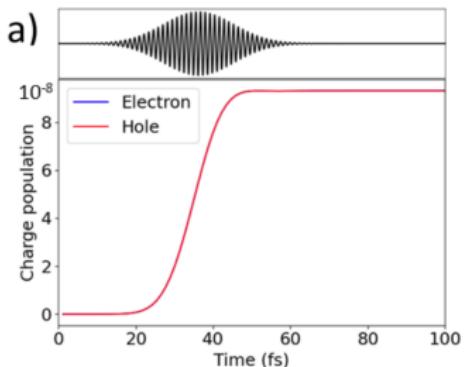
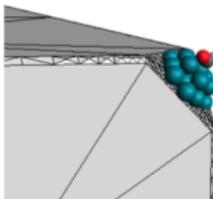
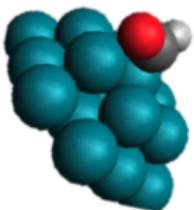
CHO dissociation is the rate-determining step



M. Vanzan, M. Marsili and S. Corni, *Catalysts*, **11**, 538 (2021)

G. Dall'Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

Results: nanocube effect on carrier injection



enhancement of 10^3 with NP
change of the time profile

WaveT code for 100-fs

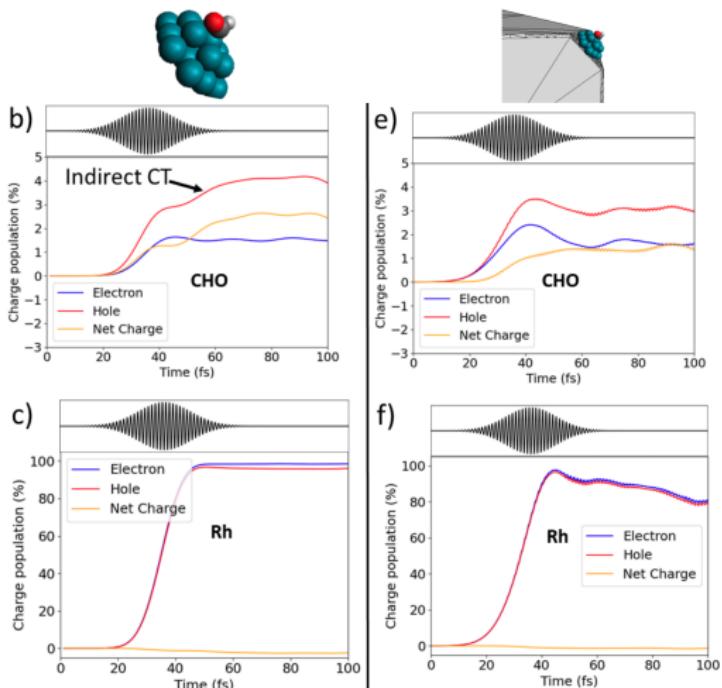
Pulse wavelength: 365 (FWHM 21 fs), weak field, linear polarization \perp to the vertex

DFT+GW/BSE: PBE0/def-TZVP, $G_n W_n$ (4 iter.), static BSE kernel (455 states)

1000 td charges, clamped nuclei

G. Dall'Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

Results: nanocube effect on carrier injection

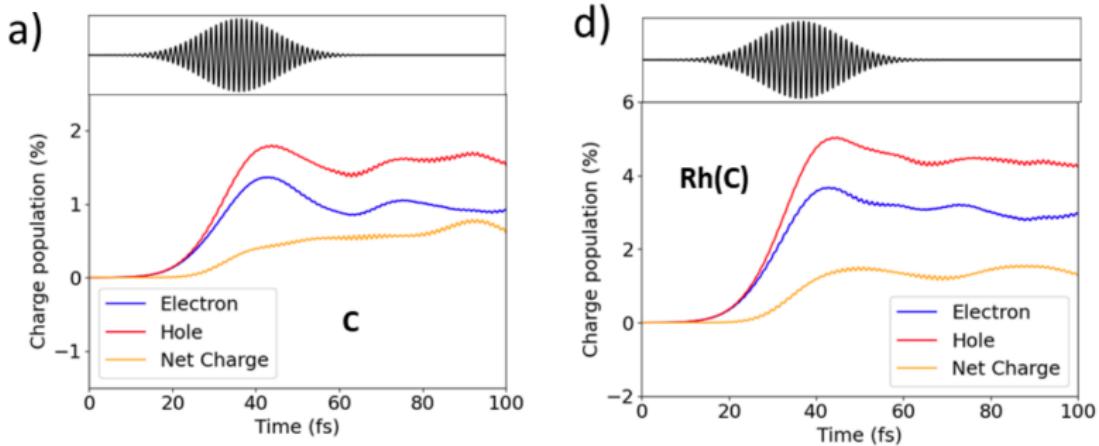
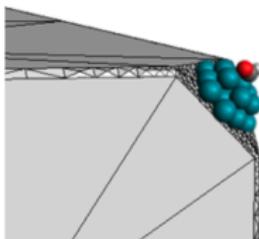


w/o NP: direct and delayed plasmon-assisted charge transfer

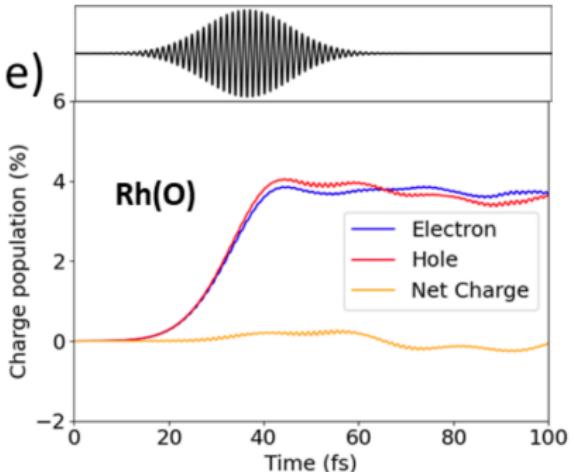
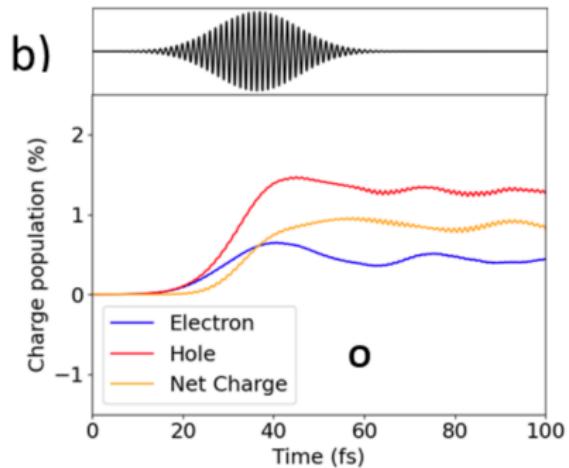
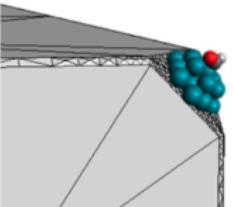
w NP: direct charge transfer (10^{10} s^{-1} hot-carrier generation)

G. Dall'Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

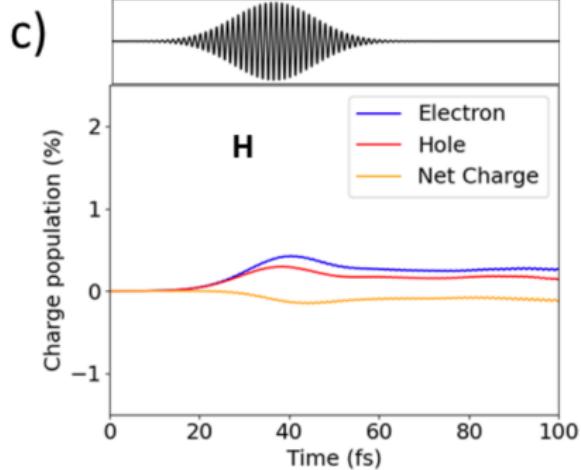
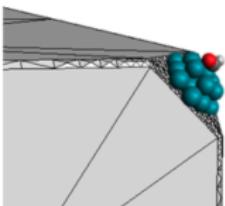
Results: charge population on CHO



Results: charge population on CHO



Results: charge population on CHO



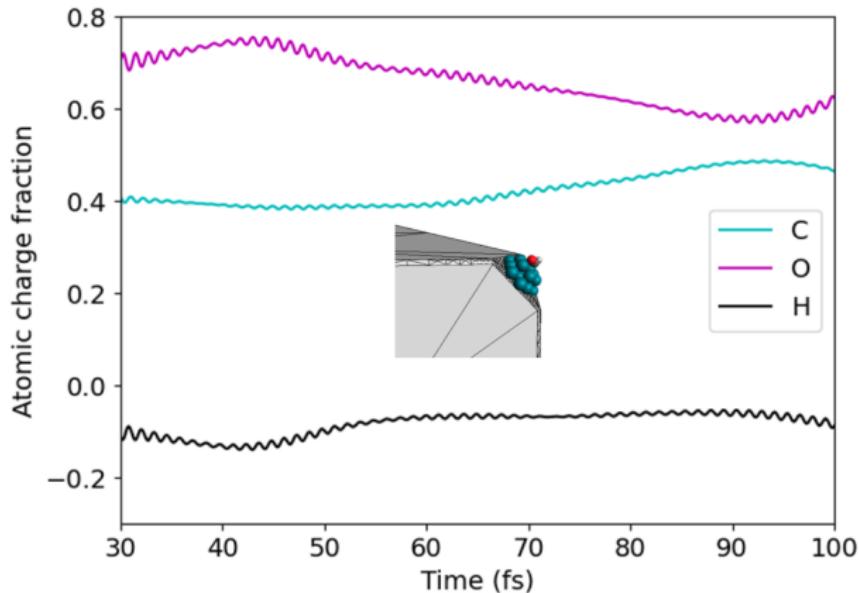
f)

Atom	Net Charge
C	↗
O	↗
H	↘
Rh(C)	↗
Rh(O)	=

Hole injection into C and O

G. Dall'Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

Results: CH_4 favoured over CO



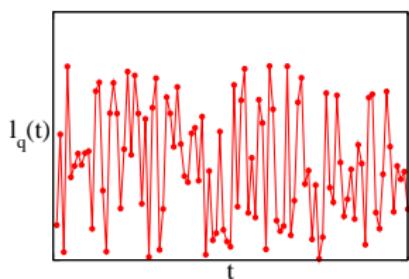
Electron-poor oxygen atom: $\text{CH} + \text{O}$

G. Dall’Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

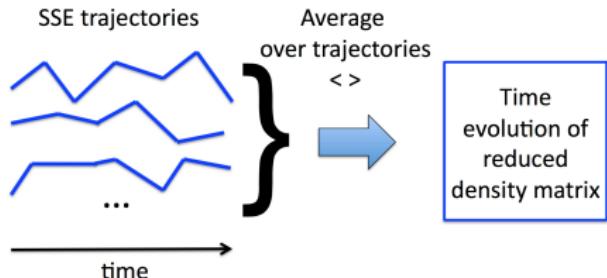
Stochastic Schrödinger equation (SSE)

$$i \frac{\partial}{\partial t} |\Psi(t)\rangle = \hat{H}(t) |\Psi(t)\rangle + \sum_q l_q(t) \hat{S}_q |\Psi(t)\rangle - \frac{i}{2} \sum_q \hat{S}_q^\dagger \hat{S}_q |\Psi(t)\rangle$$

$$|\Psi(t)\rangle = \sum_{\lambda} C_{\lambda}(t) |\lambda\rangle$$



● SSE in Markovian limit
R. Biele and R. D'Agosta, *J. Phys.: Condens. Matter*, **24** 273201(2012)



interaction channels S_q

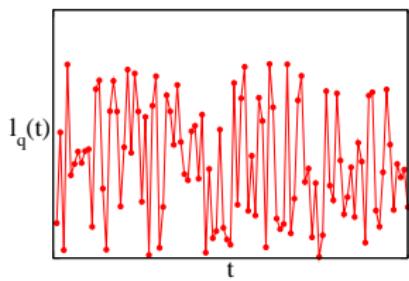
Dephasing (D)

R. Biele and R. D'Agosta, *J. Chem. Phys.*, **136**, 204102 (2012)
EPL (Europhysics Letters), **101**, 10001 (2013)

Stochastic Schrödinger equation (SSE)

$$i \frac{\partial}{\partial t} |\Psi(t)\rangle = \hat{H}(t) |\Psi(t)\rangle + \sum_q l_q(t) \hat{S}_q |\Psi(t)\rangle - \frac{i}{2} \sum_q \hat{S}_q^\dagger \hat{S}_q |\Psi(t)\rangle$$

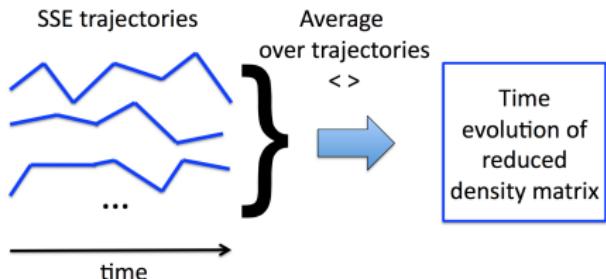
$$|\Psi(t)\rangle = \sum_{\lambda} C_{\lambda}(t) |\lambda\rangle$$



- Interaction channels \hat{S}_q :
- Dephasing (T_2)

EC, F. Troiani and S. Corni, *J. Chem. Phys.*, **148**, 204112 (2018)
EC and S. Corni, *J. Chem. Phys.*, **151**, 044703 (2019)

• SSE in Markovian limit
R. Biele and R. D'Agosta, *J. Phys.: Condens. Matter*, **24** 273201 (2012)



SSE for analysis

Pure dephasing operator

$$\begin{aligned}\hat{S}_q^{\text{dep}} &= \sqrt{\gamma_q/2} \sum_p P(\lambda, \lambda') |\lambda\rangle\langle\lambda'| \\ T_2 &= \frac{1}{\gamma_q} \\ P(\lambda, \lambda') &= -1 \quad \text{if } \lambda = \lambda' \\ &= 1 \quad \text{otherwise}\end{aligned}$$

APDOS applied to the SSE

$$\begin{aligned}\text{APDOS}_{\text{SSE}}^{(n)}(\epsilon, \alpha) &= - \sum_{\lambda, \lambda'} \text{Re} \left[\sum_{\mu} C(\lambda, \mu) \sum_{\nu} (d_{\mu})^* d_{\nu} \right] I_n(\epsilon - \alpha) \\ &\quad + \sum_{\lambda, \lambda'} \text{Re} \left[\sum_{\mu} C(\lambda, \mu) \sum_{\nu} (d_{\nu})^* d_{\mu} \right] I_n(\epsilon - \alpha)\end{aligned}$$

The pure dephasing contribution is defined by using APDOS_{SSE}⁽ⁿ⁾ with the pure dephasing operator.

SSE for analysis

Pure dephasing operator

$$\begin{aligned}\hat{S}_q^{\text{dep}} &= \sqrt{\gamma_q/2} \sum_p P(\lambda, \lambda') |\lambda\rangle\langle\lambda'| \\ T_2 &= \frac{1}{\gamma_q} \\ P(\lambda, \lambda') &= -1 \quad \text{if } \lambda = \lambda' \\ &= 1 \quad \text{otherwise}\end{aligned}$$

ΔPDOS applied to the SSE

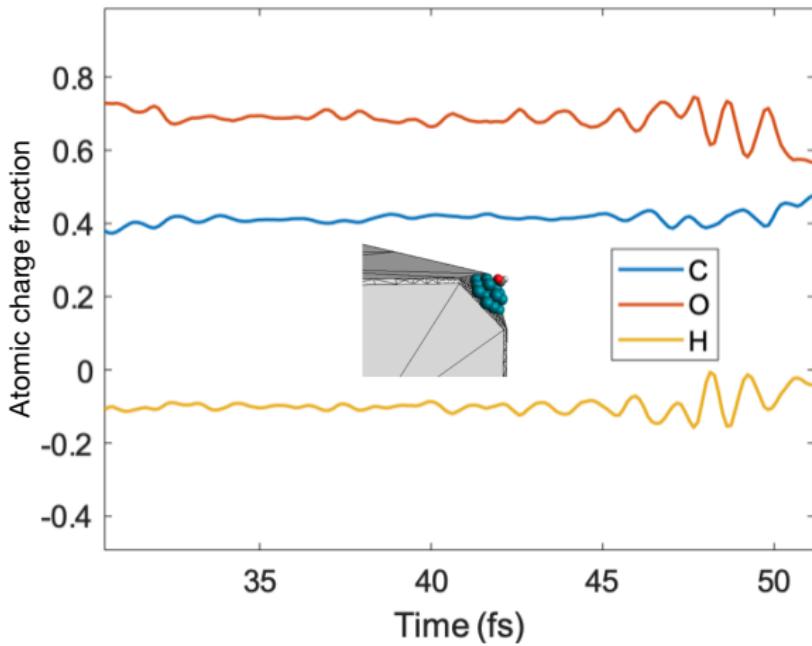
$$\begin{aligned}\Delta\text{PDOS}_K^{\text{SSE}}(t, \epsilon) &= - \sum_i^{occ} w_i^K \text{Re} \left[\sum_{\lambda, \lambda'} \overline{C_\lambda^*(t) C_{\lambda'}(t)} \sum_a^{vir} (d_{i,\lambda}^a)^* d_{i,\lambda'}^a \right] L_\eta(\epsilon - \epsilon_i) \\ &\quad + \sum_a^{vir} w_a^K \text{Re} \left[\sum_{\lambda, \lambda'} \overline{C_\lambda^*(t) C_{\lambda'}(t)} \sum_i^{occ} (d_{i,\lambda}^a)^* d_{i,\lambda'}^a \right] L_\eta(\epsilon - \epsilon_i).\end{aligned}$$

SSE version of charge population is defined by using $\Delta\text{PDOS}_K^{\text{SSE}}(t, \epsilon)$

EC, F. Troiani and S. Corni, *J. Chem. Phys.*, **148**, 204112 (2018)

G. Dall'Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

Results: $T_2 = 5$ fs



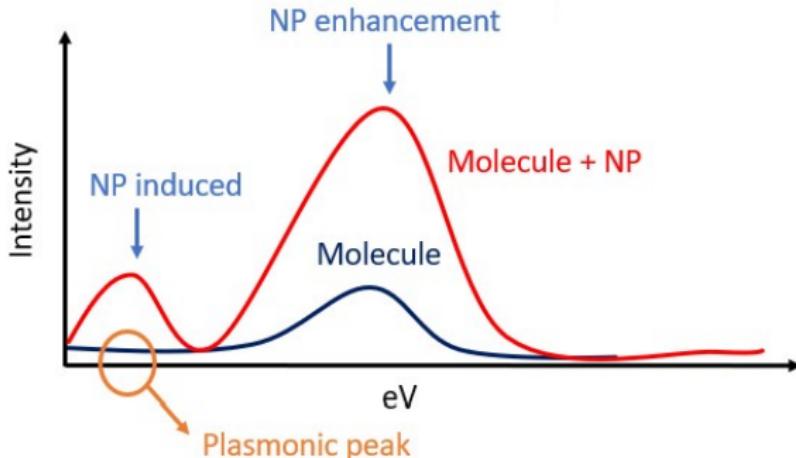
Same picture as in coherent dynamics

G. Dall'Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

Plasmon-enhanced circular dichroism

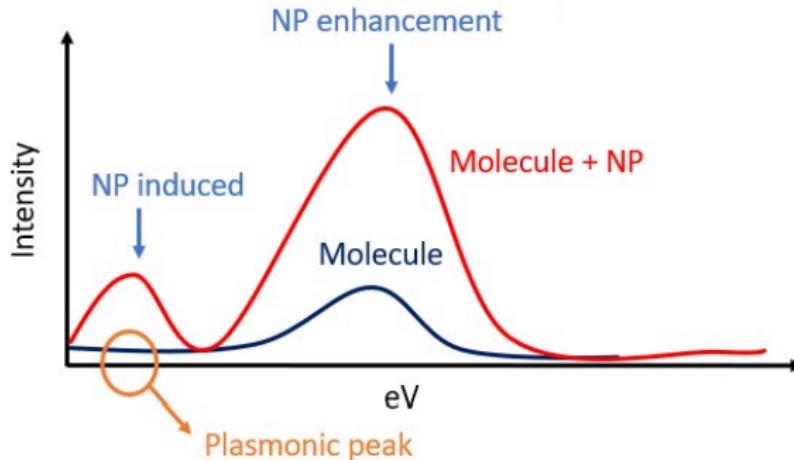
Plasmon-enhanced circular dichroism

- Plasmonic systems with intrinsic chirality
- **Achiral plasmonic NPs coupled to a chiral molecule**
- Chiral arrangement of achiral plasmonic NPs



Plasmon-enhanced circular dichroism

- Plasmonic systems with intrinsic chirality
- **Achiral plasmonic NPs coupled to a chiral molecule**
- Chiral arrangement of achiral plasmonic NPs



Only electronic circular dichroism (ECD) is considered here

A. O. Govorov, Z. Fan, P. Hernandez, J. M. Slocik and R. R. Naik, *Nano Lett.*, **10**, 1374 (2010)

M. Hentschel, M. Schaferling, X. Duan, H. Giessen and N. Liu, *Sci. Adv.*, **3**, e1602735 (2017)

N. S. Shahana Nizar, M. Sujith, K. Swathi, C. Sissa, A. Painelli and K. G. Thomas, *Chem. Soc. Rev.*, **50**, 11208 (2021)

RT-PCM-NP for ECD

- Same multiscale method as for photocatalysis ([RT-PCM-NP](#))

↳ same computational scheme, just different quantities

↳ time-dependent induced magnetic dipole moment

$$\Delta \vec{m}(t) = \vec{m}(t) - \vec{m}(0)$$

$$\vec{m}(t) = \sum_{\alpha} C_\alpha(t) C_\alpha(0) \vec{m}_\alpha$$

RT-PCM-NP for ECD

- Same multiscale method as for photocatalysis (RT-PCM-NP)
- Electric (external + induced) perturbation to the time-dependent induced magnetic dipole moment

$$\begin{aligned}\Delta \vec{m}(t) &= \vec{m}(t) - \vec{m}(0) \\ \vec{m}(t) &= \sum_{\lambda, \lambda'} C_{\lambda}^*(t) C_{\lambda'}(t) \langle \lambda | \hat{\vec{m}} | \lambda' \rangle\end{aligned}$$

• ECD spectrum as Fourier transform of $\Delta \vec{m}(t)$

$$P_{\text{ECD}}^{(R)}(\omega) = \frac{1}{2mcE_{\text{ext},\mu}^2(\omega)} \int_0^{+\infty} -\Delta m(t) e^{i(\omega t + \pi/2)} dt$$

RT-PCM-NP for ECD

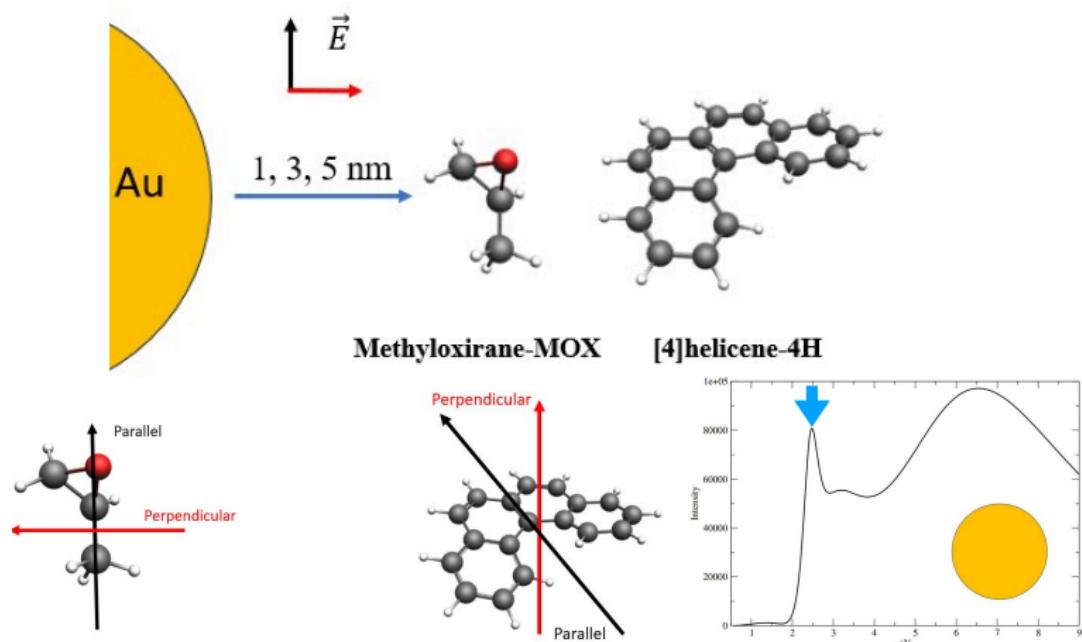
- Same multiscale method as for photocatalysis ([RT-PCM-NP](#))
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- ECD spectrum as Fourier transform of $\Delta \vec{m}(t)$

$$P_{nl}^{ECD}(\omega) = -\frac{i}{2\pi\omega E_{ext,n}^0(\omega)} \int_0^{+\infty} -\Delta m_l(t) e^{i(\omega+i\Gamma)t} dt$$

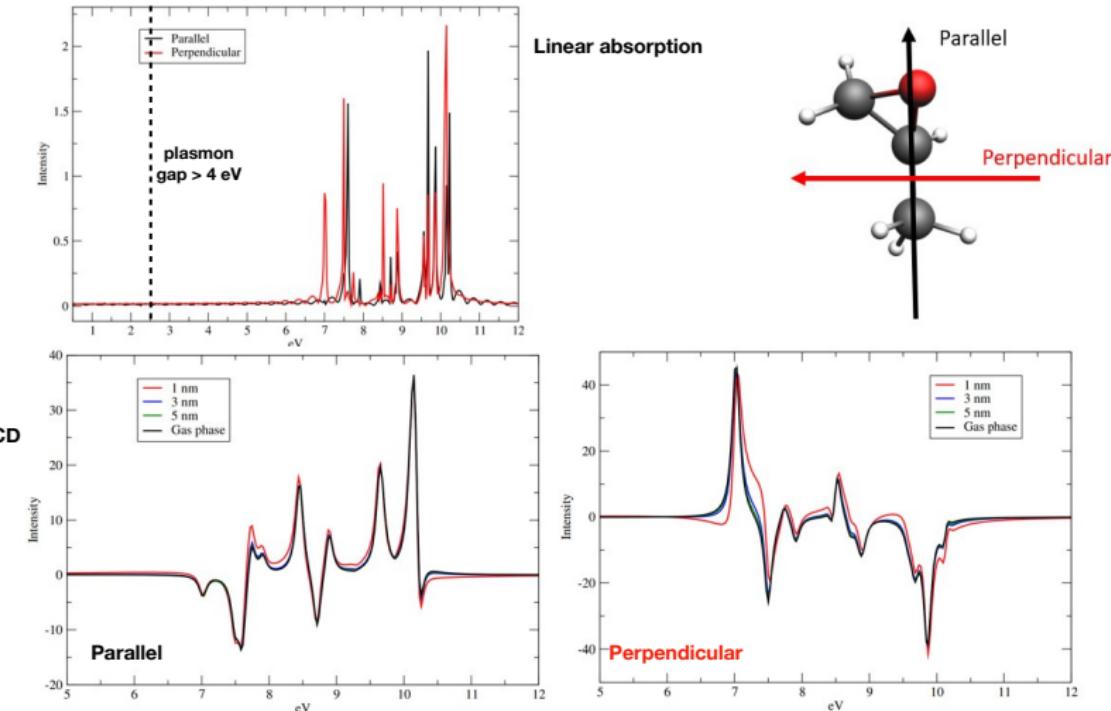
Modelling the systems



Ground-state geometry of MOX and 4H from literature. TDDFT/B3LYP/TZP: 20 electronic states for MOX, 40 for 4H. 150-fs dynamics, time step of 0.7 fs, δ pulse with FWHM of 94 fs. NP radius equal to 2.5 nm, 2700 tesserae, exp Au dielectric function

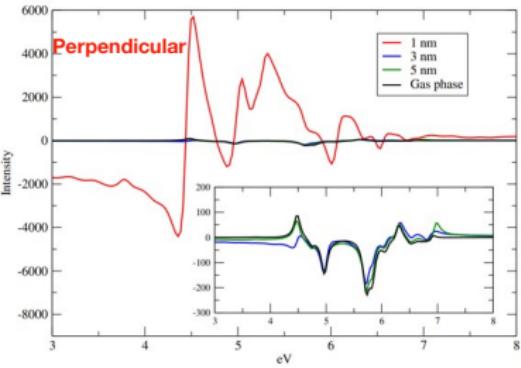
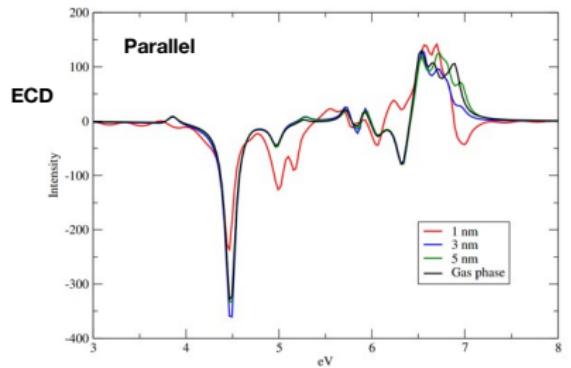
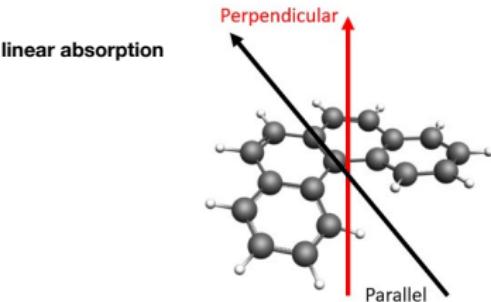
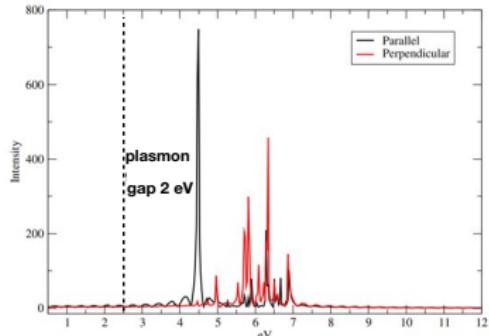
L. Biancorosso, P. D'Antoni, S. Corni, M. Stener and EC, submitted

MOX



No plasmonic effect for MOX

L. Biancorosso, P. D'Antoni, S. Corni, M. Stener and EC, submitted



Enhancement by a factor 60 for perpendicular configuration
 L. Biancorosso, P. D'Antoni, S. Corni, M. Stener and EC, submitted

Conclusions

- General model for hot-carrier dynamics
- Microscopic understanding of plasmon-assisted reaction selectivity in CO_2 hydrogenation
- Microscopically controlled computational scheme (GSE)
- (De)coherence as a further design element in nanoplasmronics and plasmon-mediated photocatalysis

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Conclusions

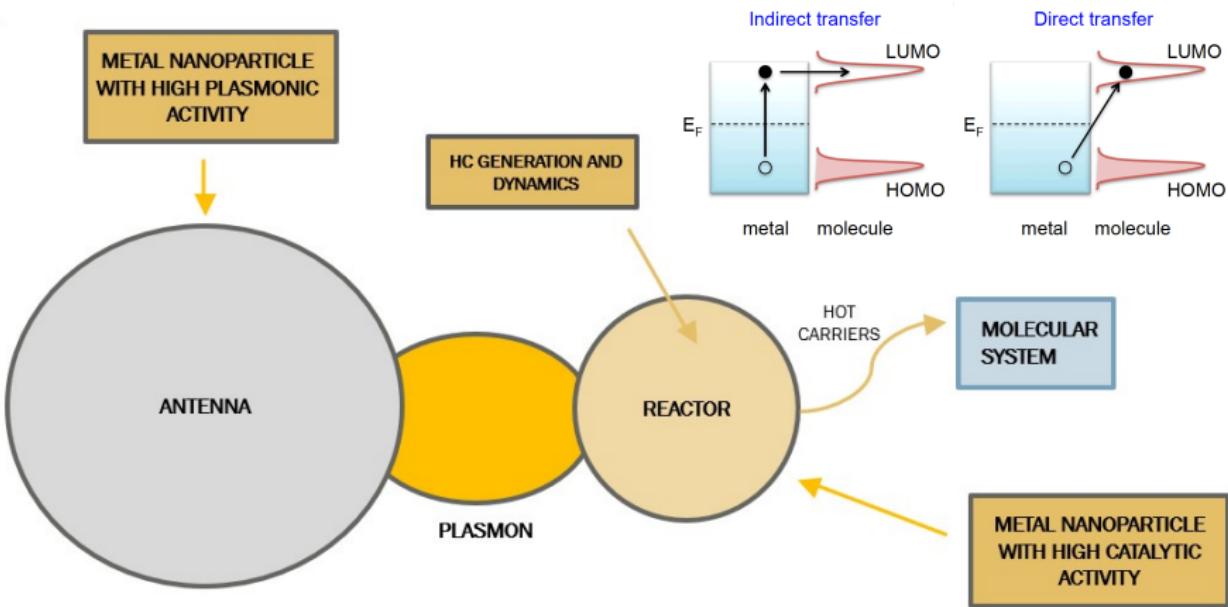
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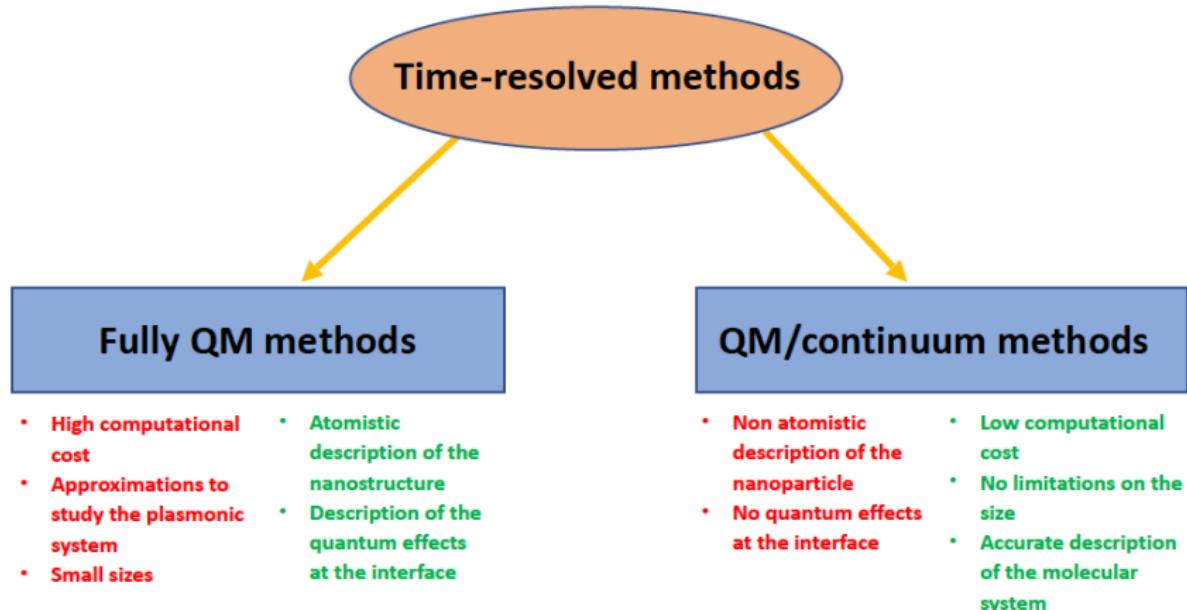
Acknowledgements

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- Margherita Marsili (Univ. Bologna)
- Leonardo Biancorosso (Univ. Trieste)
- Mauro Stener (Univ. Trieste)



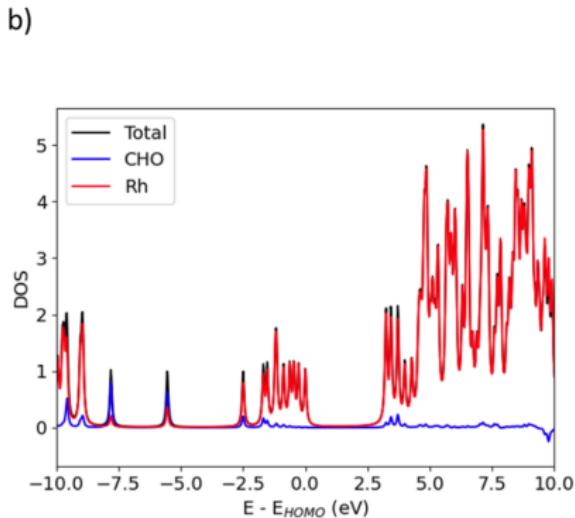
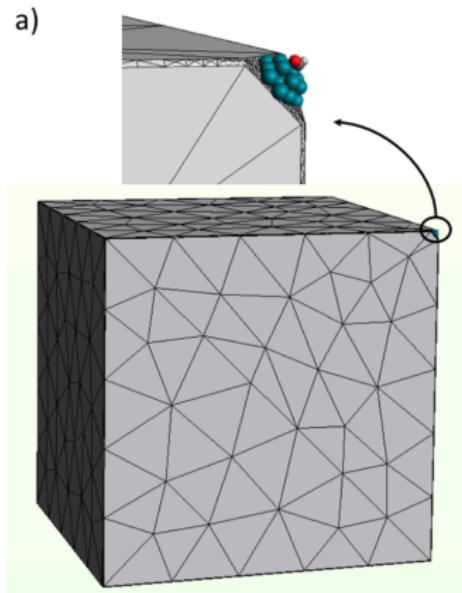
Plasmon-assisted photocatalysis





Results: before turning on the pulse

Ground-state PDOS (after equilibration)

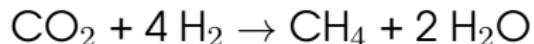


Anti-bonding orbitals populated

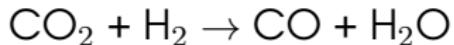
G. Dall'Osto, M. Marsili, M. Vanzan, D. Toffoli, M. Stener, S. Corni and EC, submitted

Competitive reactions

Methanation



Carbon monoxide formation

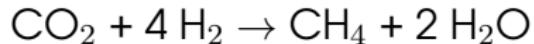


Rate-determining step (rds)

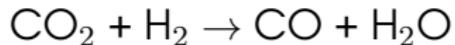


Competitive reactions

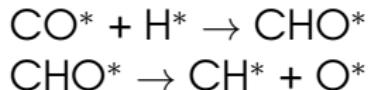
Methanation



Carbon monoxide formation



Rate-determining step (rds)



Competitive reactions

- Desorption of CO from Rh has the rds of CO production
- Dissociation of CH-O as the rds for CH_4 production
- Competition between CO desorption and C-O bond cleavage in CHO dictates the product selectivity

Carrier injection

Electron injection

$$\frac{1}{2} \int_{-\infty}^{\infty} [\Delta\text{PDOS}(t, \epsilon) + |\Delta\text{PDOS}(t, \epsilon)|] d\epsilon$$

Hole injection

$$\frac{1}{2} \int_{-\infty}^{\infty} [\Delta\text{PDOS}(t, \epsilon) - \Delta\text{PDOS}(t, \epsilon)] d\epsilon$$

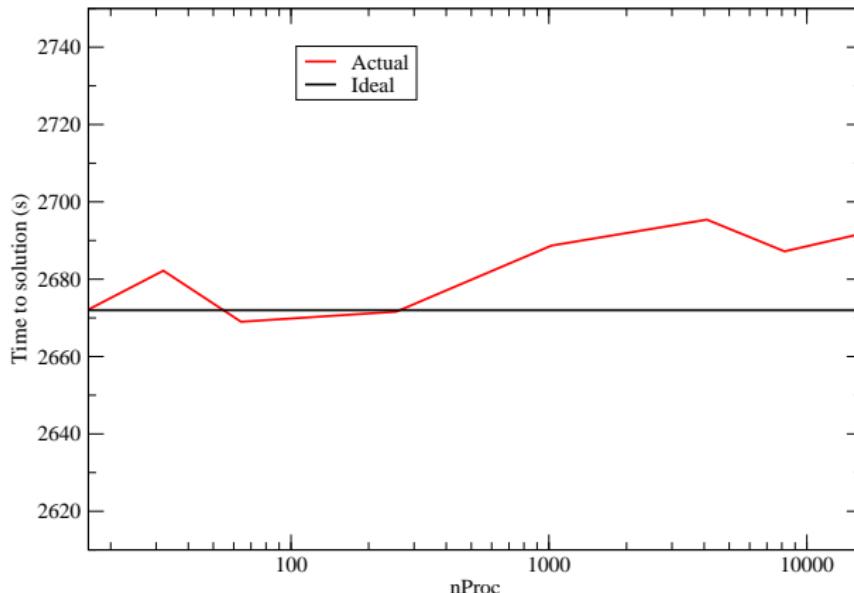
Equilibration step

- Starting from a GW-BSE calculation in vacuum
- A finite set of $|\lambda\rangle_{vac}$ states is chosen as the “active space”
- The total energy of the NP/molecule system is self-consistently minimized from the molecule in its vacuum ground-state $|0\rangle_{vac}$ close to NP
- NP is provided of a set of starting polarization charges
- The molecule is in a novel ground-state $|0\rangle_{eq} = \sum_\lambda a_\lambda^{GS} |\lambda\rangle_{vac}$
- The NP polarization, frozen at the ground-state, provides a modified molecular Hamiltonian that is diagonalized in the molecular active space, obtaining a new set of excited states $|\lambda\rangle_{eq} = \sum_{\lambda'} a_{\lambda'}^\lambda |\lambda'\rangle_{vac}$

OpenMP+MPI parallelization for SSE

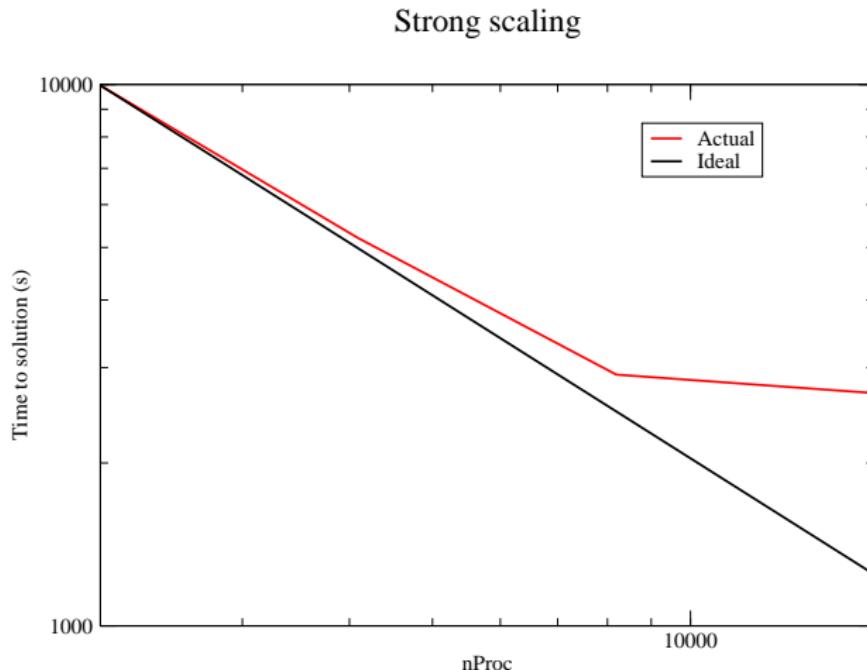
- PRACE Preparatory Project 2010PA4253 on Curie (2/2/2018 - 2/8/2018)
- Molecule+NS system

Weak scaling

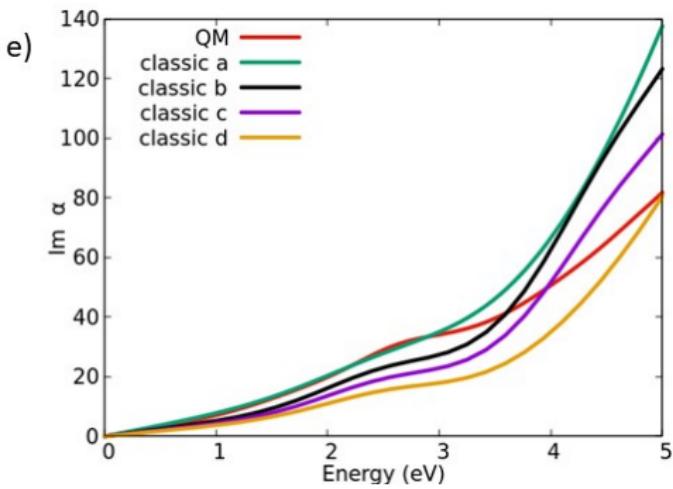
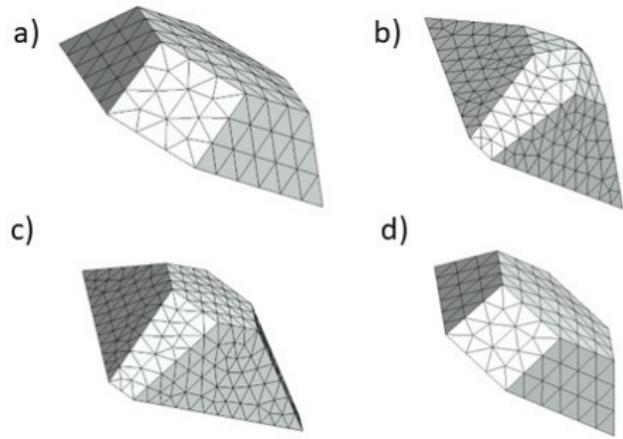


OpenMP+MPI parallelization for SSE

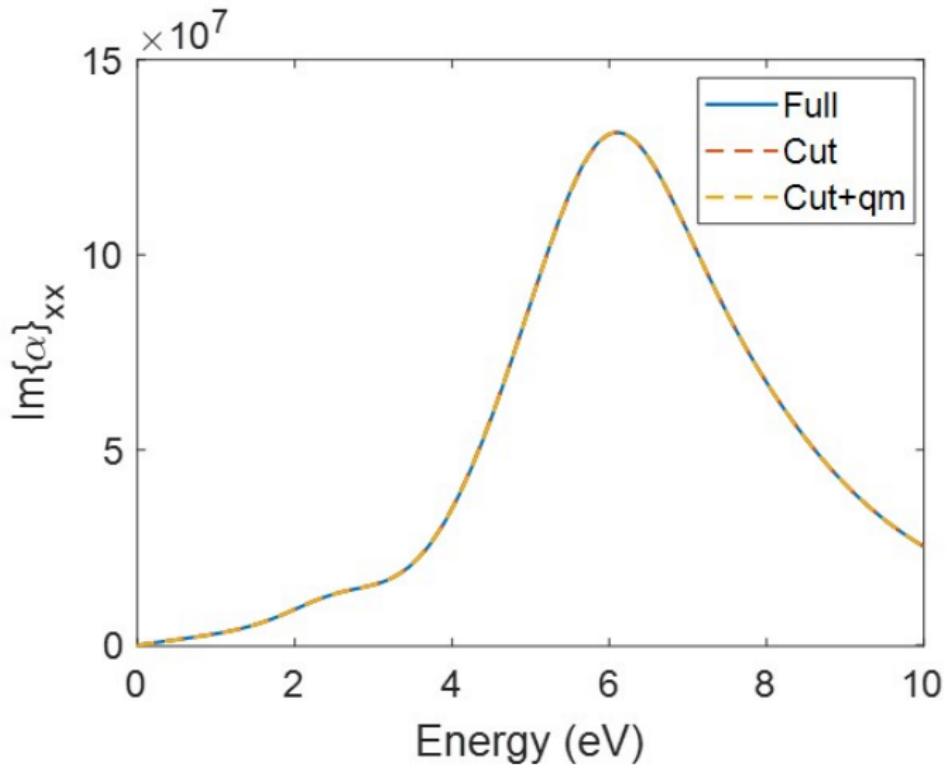
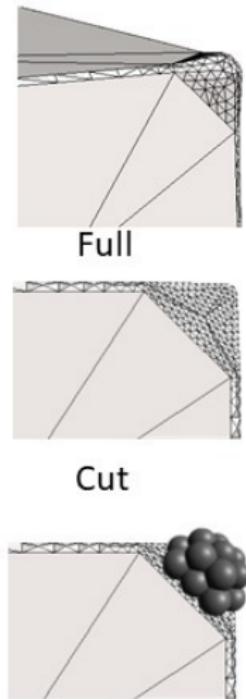
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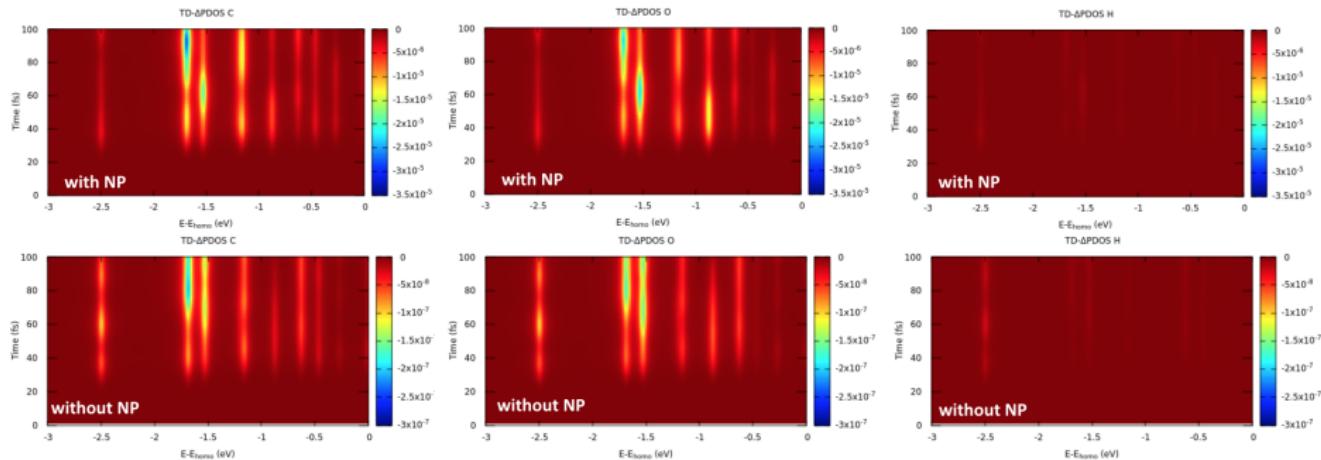
Modeling the Rh nanocube



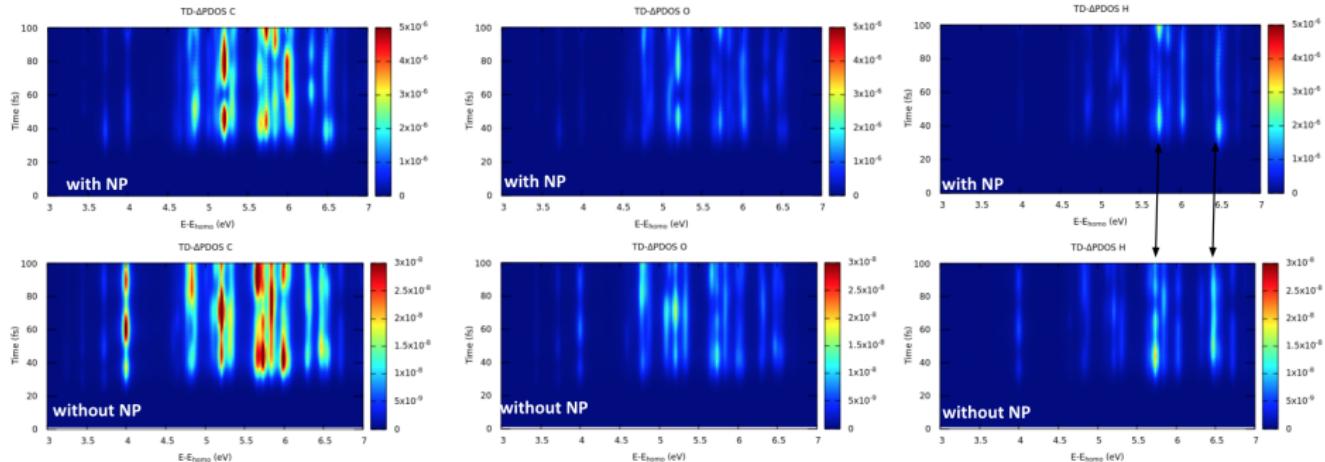
Modeling the Rh nanocube



Valence band

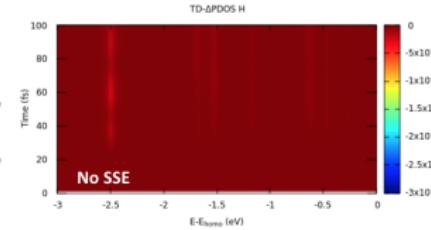
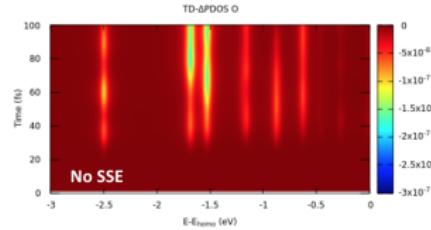
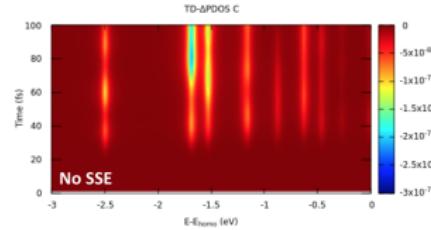
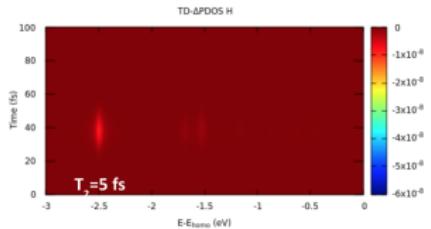
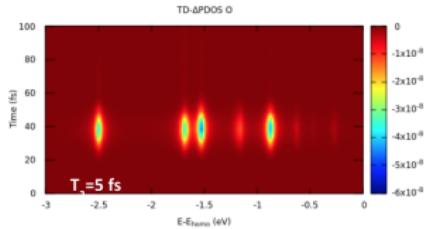
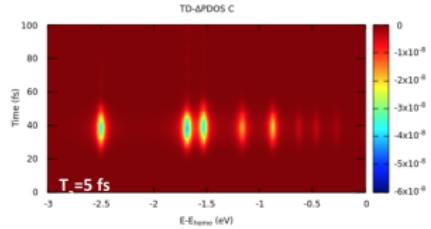


Conduction band



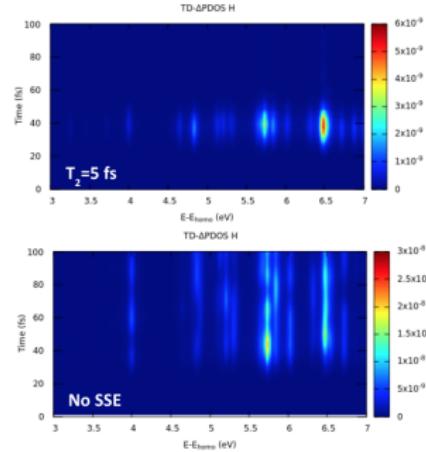
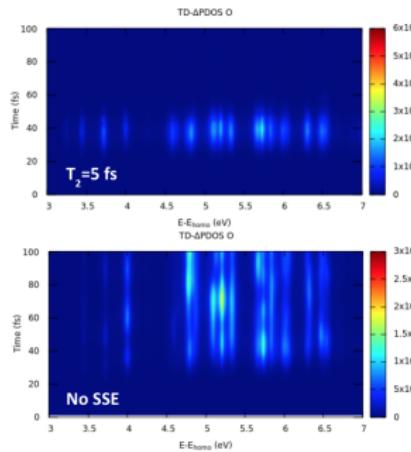
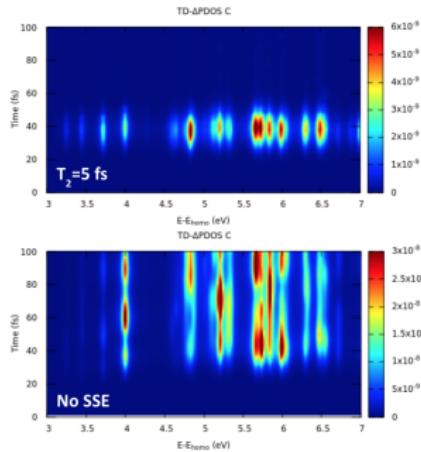
$T_2 = 5$ fs, valence band

Without NP



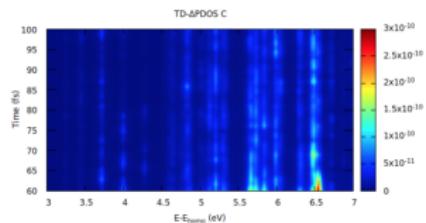
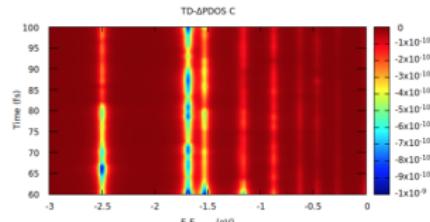
$T_2 = 5$ fs, conduction band

Without NP

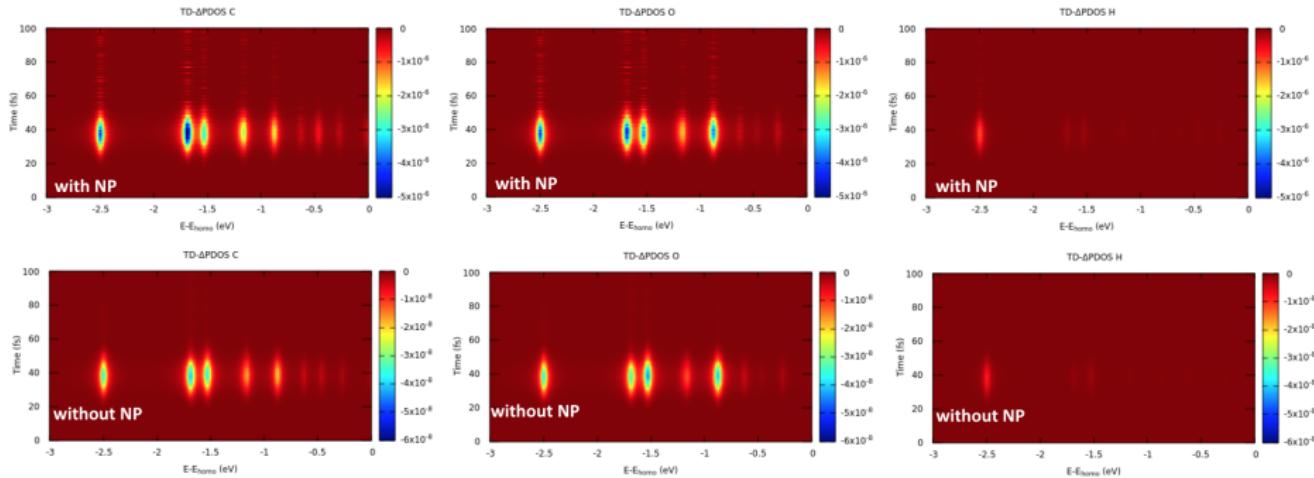


$T_2 = 5 \text{ fs}$

Dephasing = 5 fs, without NP



$T_2 = 5$ fs, valence band



$T_2 = 5$ fs, conduction band

Dephasing = 5 fs

