

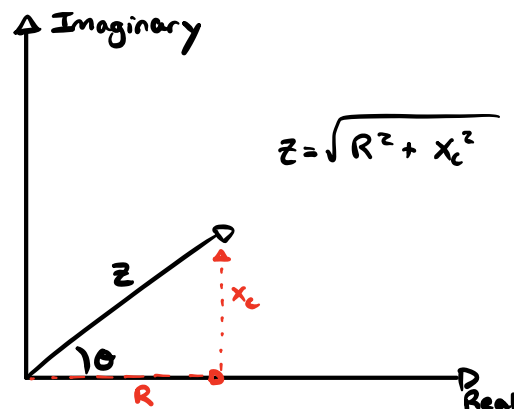
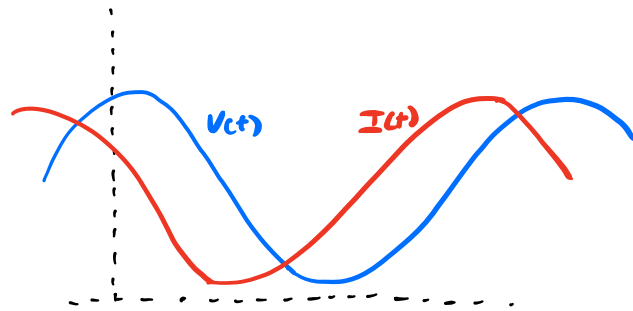
$$I = C \frac{dV}{dt}$$

$$I = C \omega V_0 \cos(\omega t)$$

$$I = \frac{V}{\frac{1}{\omega C}} \Leftrightarrow \frac{V}{R}$$

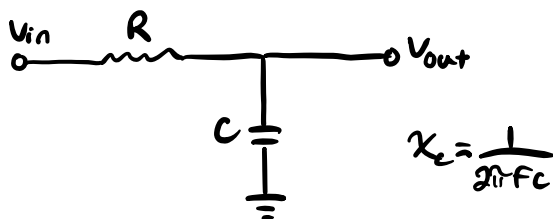
$$X_{\text{capacitor}} = \frac{1}{\omega C} = \frac{1}{2\pi f C}$$

↑  
Reactance (frequency-dependent resistor)



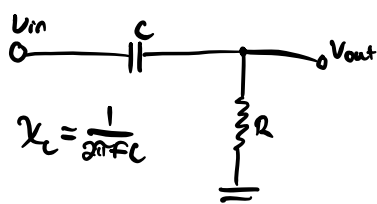
Impedance : general resistance of a circuit  
↑  
frequency-dependent

$$Z = R + iX_c$$



At  $f=0$ ,  $V_0 = V_{in}$  Lowpass filter

At  $f=\infty$ ,  $V_0 = 0$



At  $f=0$ ,  $V_0 = 0$  High pass Filter

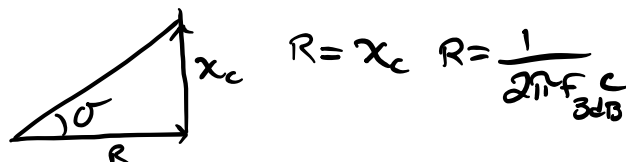
At  $f=\infty$ ,  $V_0 = V_{in}$

$$\frac{V_{out}}{V_{in}} = \frac{X_c}{R + X_c} = \frac{\frac{1}{\omega C}}{R + \frac{1}{\omega C}}$$

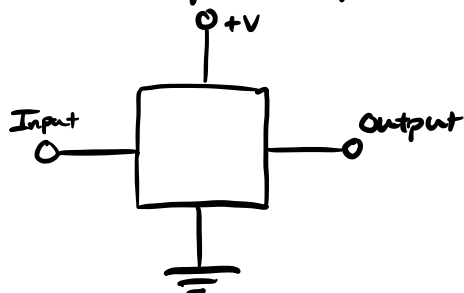
$$\frac{V_{out}}{V_{in}} \approx \frac{1}{\omega R C + 1}$$

$$\frac{V_{out}}{V_{in}} \approx \frac{R}{R + X_c} = \frac{R}{R + \frac{1}{\omega C}} = \frac{\omega R C}{\omega R C + 1}$$

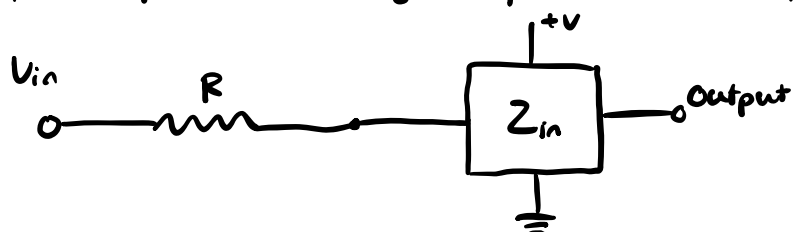
$$\frac{V_{out}}{V_{in}} \approx \frac{\omega R C}{\omega R C + 1}$$



Input/output Impedance

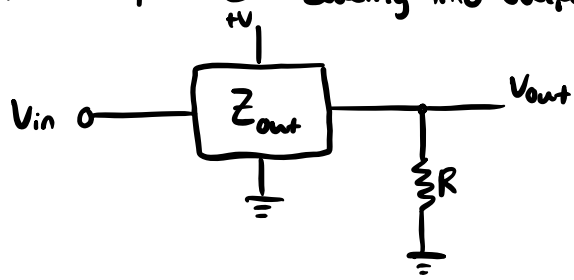


Input Impedance "Loading into input" - effective impedance



$$V_{out} = \frac{Z_{in} \cdot V_{in}}{R + Z_{in}}$$

Output Impedance "Loading into output"



"Loading into output"

$$V_{out} = \frac{R}{R + Z_{out}} V_{in}$$