

Announcements

□ Homework for tomorrow...

Ch. 31: CQ 10, Probs. 20, 22, & 46

CQ3: $\Delta V_{12} = 3V$

31.1: See whiteboard

31.6: 8V, 22V

31.8: (48/25)W, (72/25)W

□ Office hours...

MW 10-11 am

TR 9-10 am

F 12-1 pm

□ Tutorial Learning Center (TLC) hours:

MTWR 8-6 pm

F 8-11 am, 2-5 pm

Su 1-5 pm

Chapter 31

Fundamentals of Circuits (*Real Batteries & Parallel Resistors*)

Review...

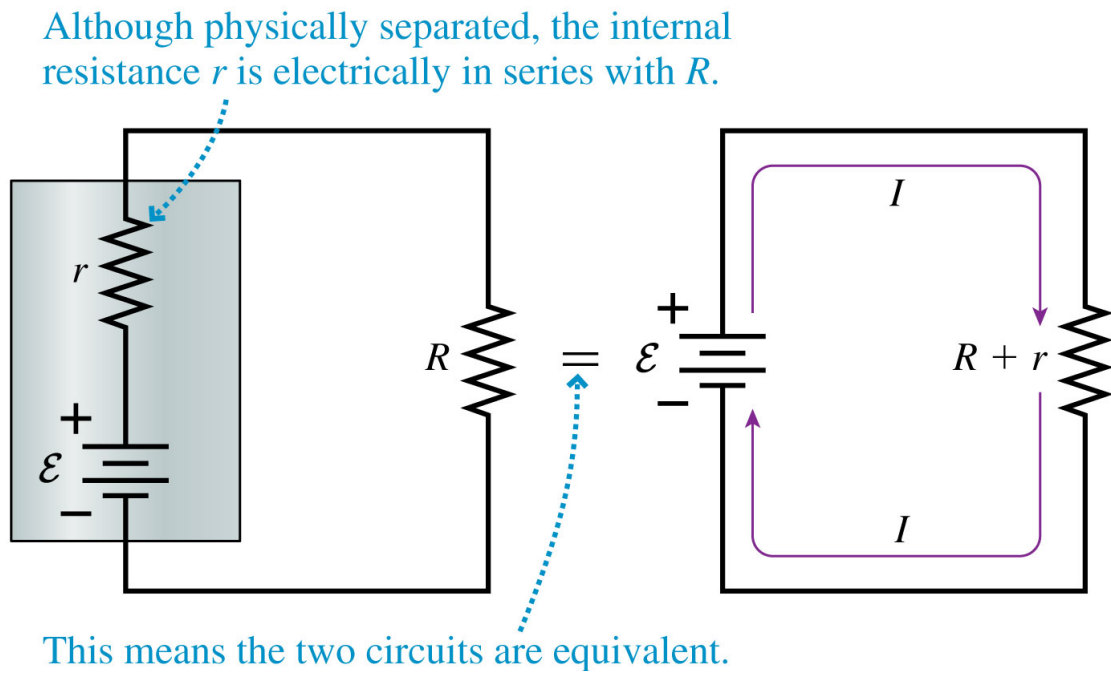
Resistors in *series*....

$$R_{eq} = R_1 + R_2 + \dots$$

Terminal voltage across a *real* battery...

$$\Delta V_{bat} = \mathcal{E} - Ir \leq \mathcal{E}$$

31.5: Real Batteries



Notice:

$$\Delta V_R = \Delta V_{bat} \text{ , } \Delta V_R \neq \mathcal{E}$$

i.e. 31.6:

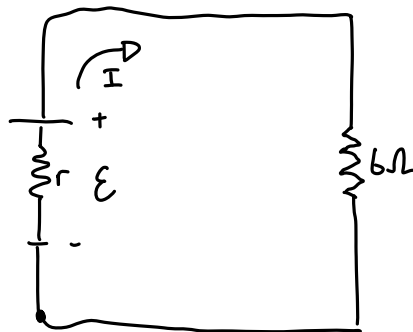
Lighting up a flashlight

A 6.0Ω flashlight bulb is powered by a 3.0V battery with an internal resistance of 1.0Ω .

What are the power dissipation of the bulb and the terminal voltage of the battery?

$$P_R = ?$$
$$\Delta V = ?$$

$$R = 6.0\Omega$$
$$\mathcal{E} = 3.0\text{V}$$
$$r = 1.0\Omega$$



$$3.0\text{V} - I(r) - I(R) = 0$$
$$I(r + R) = 3.0\text{V}$$
$$I = \frac{3.0\text{V}}{r + R}$$
$$I = 0.43\text{A}$$

$$P_R = I^2 R$$
$$= (0.43\text{A})^2 (6\Omega)$$

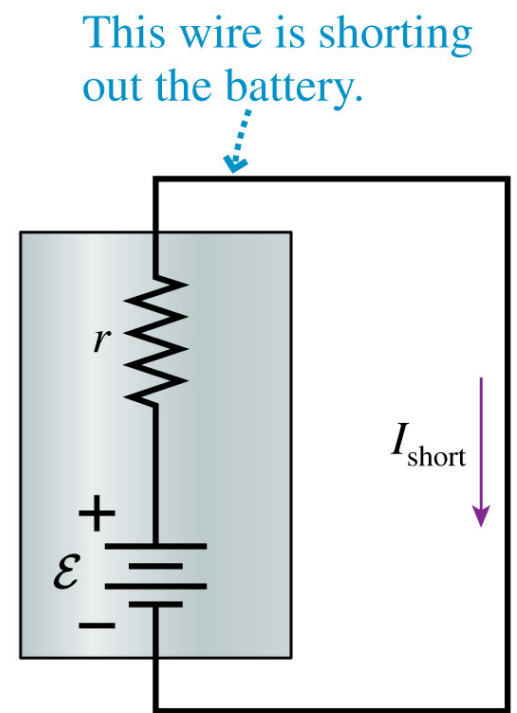
$$P_R = 1.1\text{W}$$
$$\Delta V = 2.6$$

$$\Delta V_B = \mathcal{E} - Ir$$
$$\Delta V = 3.0\text{V} - I(r)$$
$$= 3.0\text{V} - 0.43\text{A}(1\Omega)$$
$$\Delta V = 2.6\text{V}$$

A Short Circuit...

What is the current in this circuit?

$$\mathcal{E} - I_s r = 0$$
$$I_s = \frac{\mathcal{E}}{r}$$



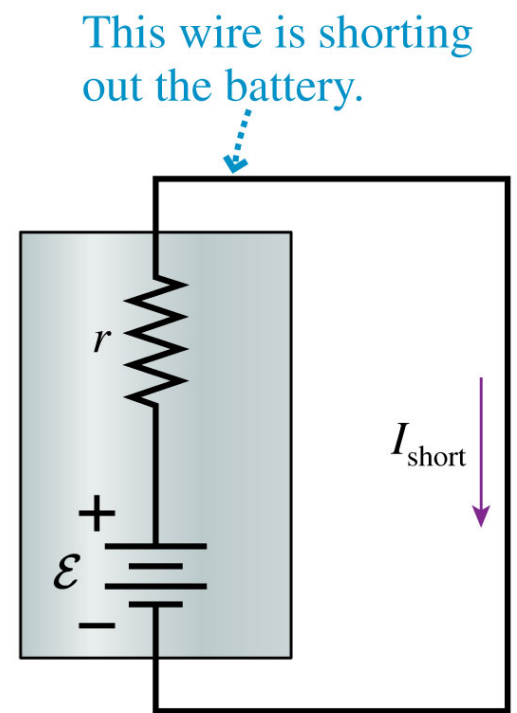
A Short Circuit...

What is the current in this circuit?

$$I_{short} = \frac{\mathcal{E}}{r}$$

Notice:

This is the *maximum possible current* that this battery can produce!

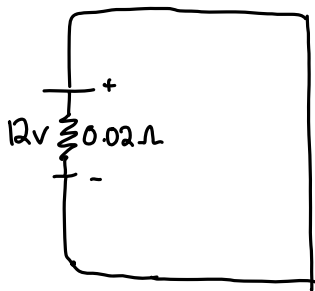


i.e. 31.7:

A short-circuited battery

What is the short-circuit current of a 12V car battery with an internal resistance of 0.020Ω ?

What happens to the power supplied by the battery?



7,200 W

$$12\text{V} - I(0.02\Omega) = 0$$

$$I = \frac{12\text{V}}{0.02\Omega}$$

$$I = 600\text{A}$$

$$P_r = I^2 r$$

$$= (600\text{A})^2 (0.02\Omega)$$

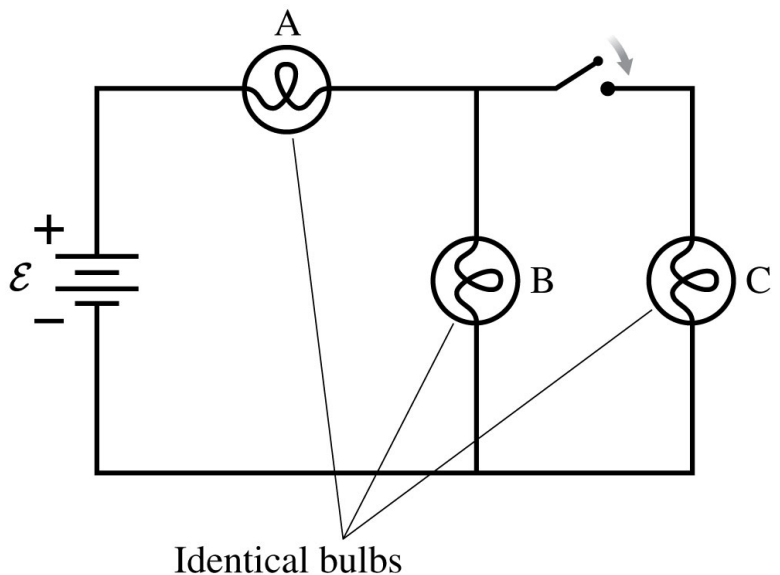
$$P_r = 7.2 \times 10^3 \text{W}$$

Quiz Question 1

Consider the circuit below, where the switch is open. The current is the same through bulbs A and B, and they are equally bright. Bulb C is not glowing.

The switch is now closed, what happens to the brightness of A?

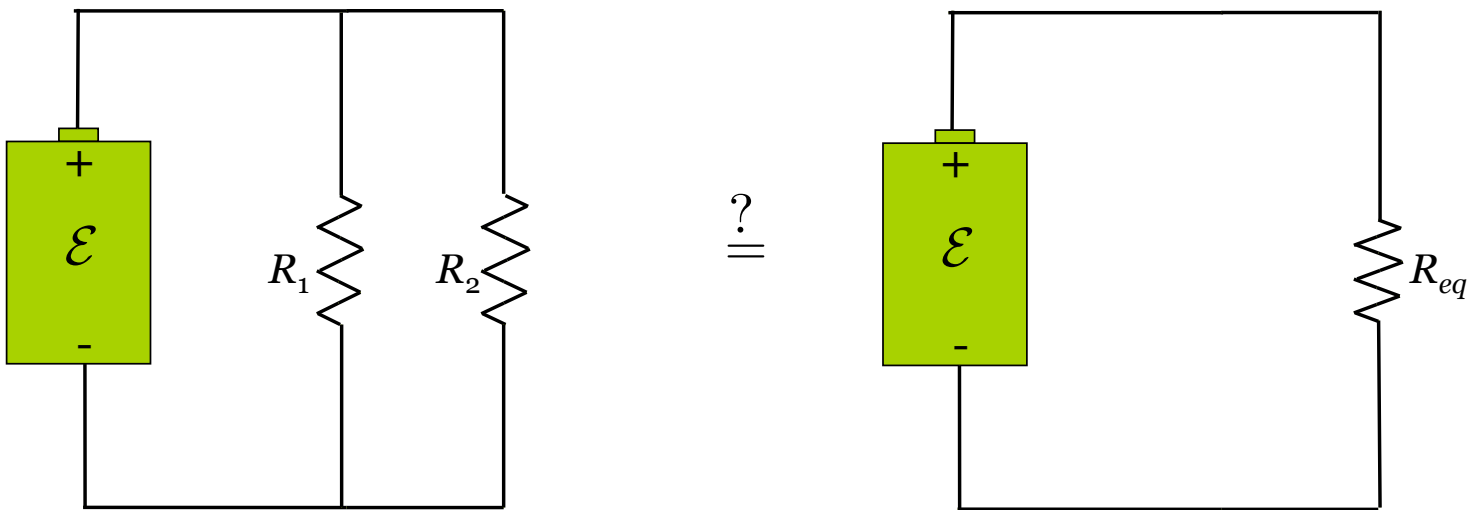
1. It increases.
2. It decreases.
3. It stays the same.



31.6: Parallel Resistors

Consider two resistors in *parallel*...

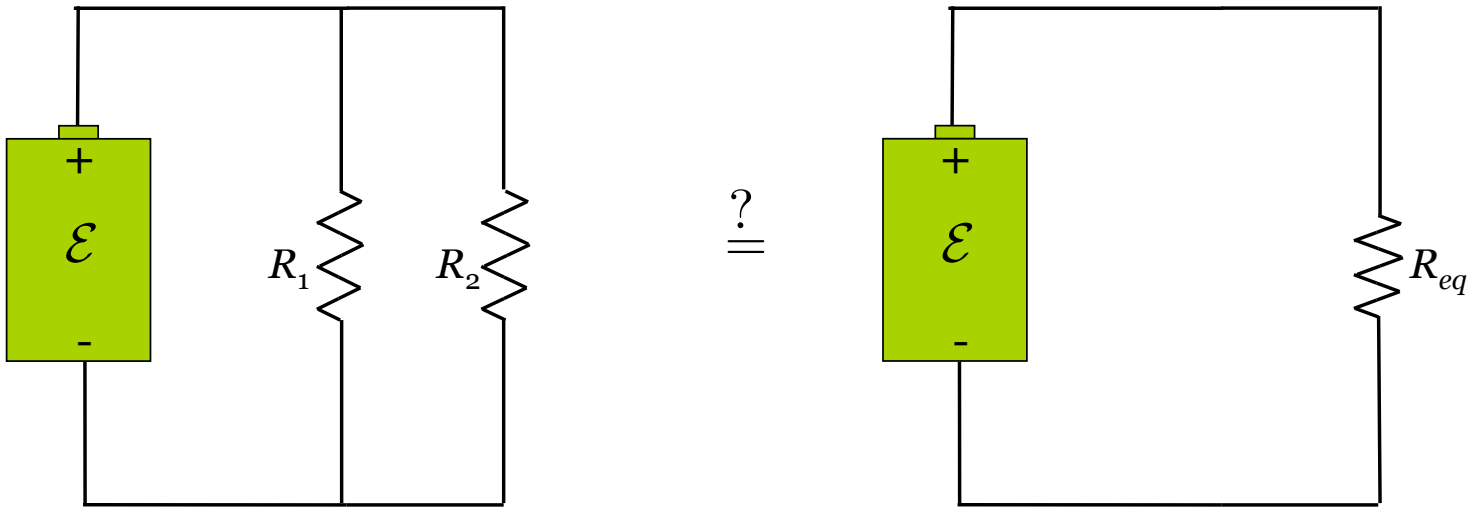
- Can we find an *equivalent resistor*, R_{eq} , to the two resistors, R_1 & R_2 ?



31.6: Parallel Resistors

Consider two resistors in *parallel*...

- Can we find an *equivalent resistor*, R_{eq} , to the two resistors, R_1 & R_2 ?



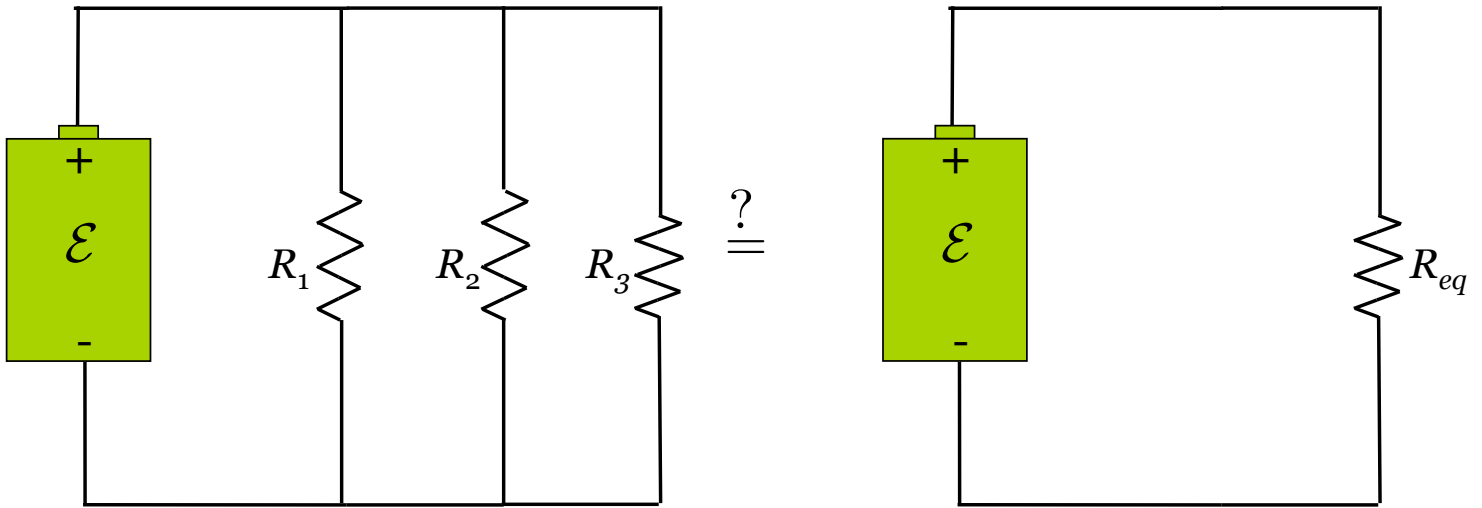
- YES!

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$$

31.6: Parallel Resistors

What about several resistors in *parallel*...

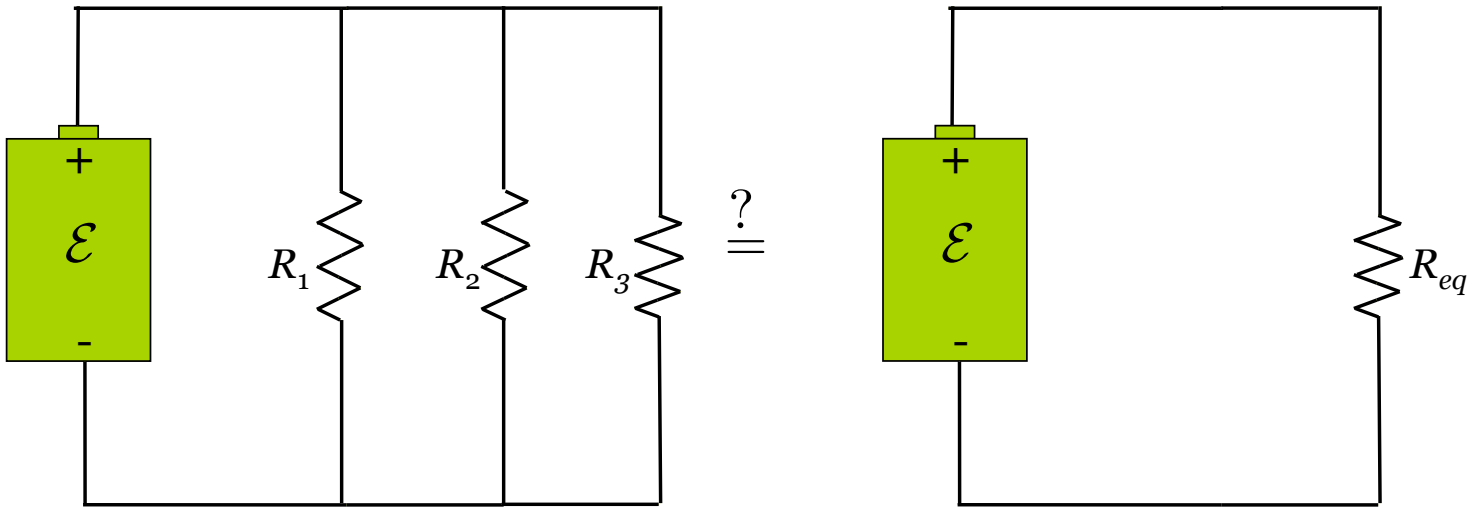
- Can we find an *equivalent resistor*, R_{eq} , to the the resistors, R_1, R_2, \dots (all in *parallel*)?



31.6: Parallel Resistors

What about several resistors in *parallel*...

- Can we find an *equivalent resistor*, R_{eq} , to the the resistors, R_1, R_2, \dots (all in *parallel*)?



- YES!

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

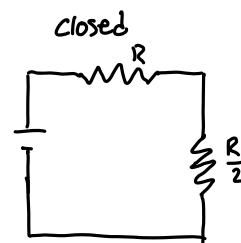
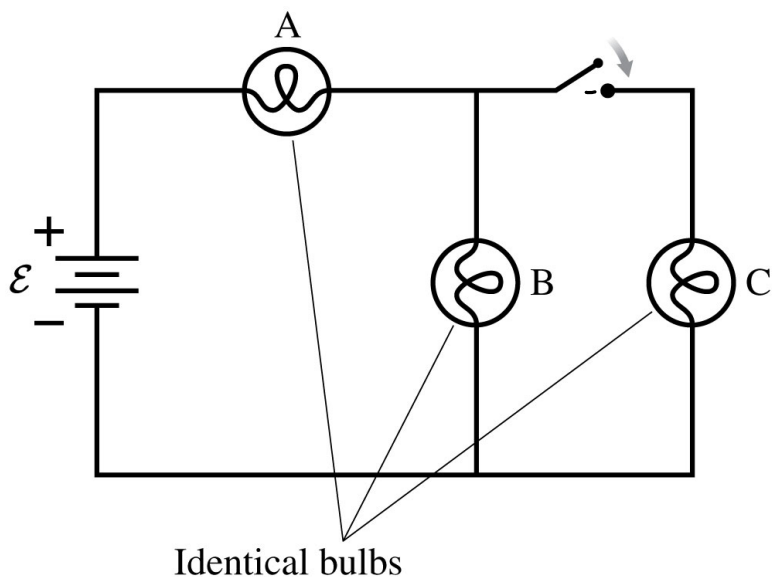
Quiz Question 1, continued..

Consider the circuit below, where the switch is open. The current is the same through bulbs A and B, and they are equally bright. Bulb C is not glowing.

The switch is now closed, what happens to the brightness of A?

$$\begin{aligned}\mathcal{E} - I(R+R) &= 0 \\ I &= \frac{\mathcal{E}}{2R} \Rightarrow \text{open}\end{aligned}$$

- ① It increases.
2. It decreases.
3. It stays the same.



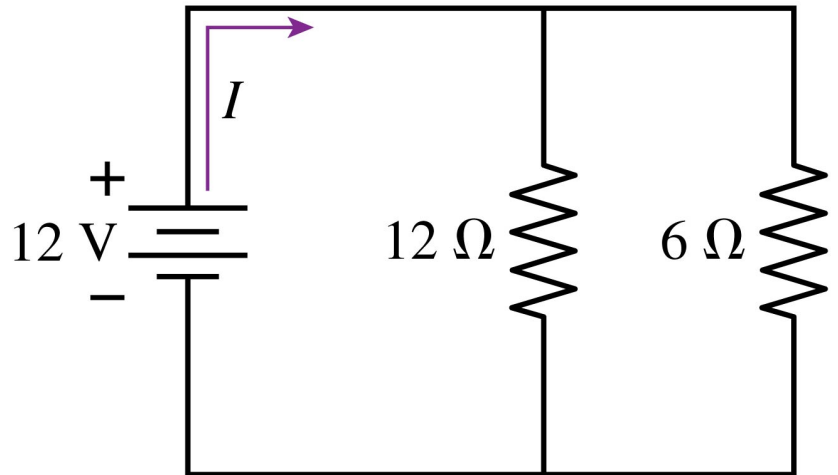
$$\begin{aligned}\frac{1}{R_{eq}} &= \frac{1}{R} + \frac{1}{R} = \frac{2}{R} \\ R_{eq} &= \frac{R}{2}\end{aligned}$$

$$\begin{aligned}\mathcal{E} - I\left(\frac{3}{2}R\right) &= 0 \\ I\left(\frac{3}{2}R\right) &= \mathcal{E} \\ I &= \frac{2}{3} \frac{\mathcal{E}}{R}\end{aligned}$$

Quiz Question 2

The battery current I is

- ① 3 A.
- 2. 2 A.
- 3. 1 A.
- 4. $2/3$ A.
- 5. $1/2$ A.



$$\frac{1}{R} = \frac{1}{12} + \frac{1}{6}$$

$$\frac{1}{R} = \frac{1}{12} + \frac{2}{12}$$

$$\frac{1}{R} = \frac{3}{12}$$

$$R = \left(\frac{12}{3}\right) = 4\ \Omega$$

$$I = \frac{\Delta V}{R}$$

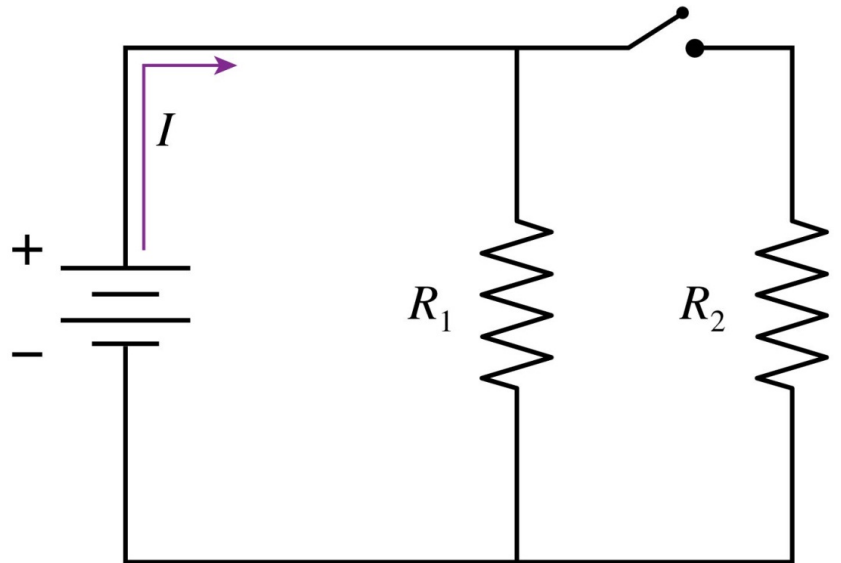
$$I = \frac{12\text{V}}{4\ \Omega}$$

$$I = 3\text{A}$$

Quiz Question 3

When the switch closes, the battery current

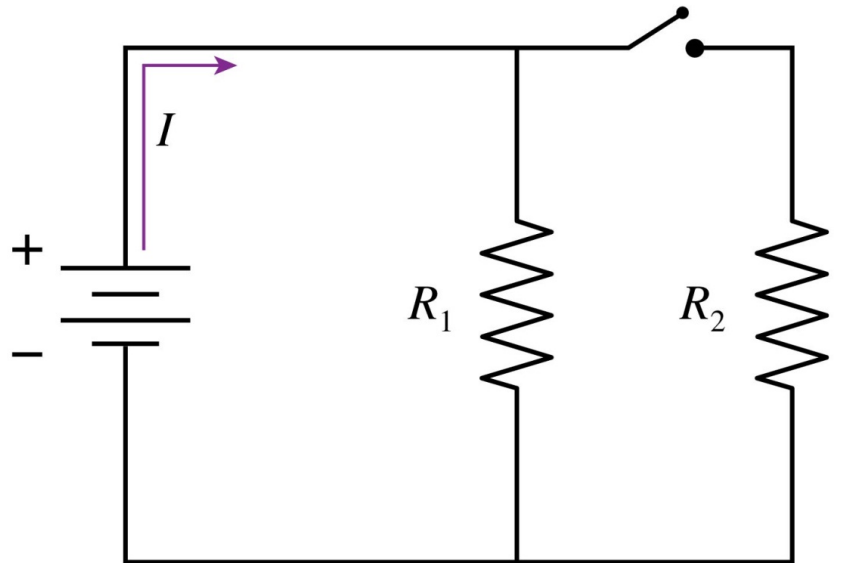
1. increases.
2. stays the same.
3. decreases.



Quiz Question 3

When the switch closes, the battery current

1. increases.
2. stays the same.
3. decreases.



Notice:

The equivalent of several resistors in parallel is *always less than* any single resistor in the group.