

# Announcements

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- ❑ EXAM 2 will be returned at the END of class *today*!
- ❑ NO LAB *this* Friday!
- ❑ Homework for tomorrow...

Ch. 32: Probs. 4, 5, & 6

- ❑ Office hours...

MW 10-11 am

TR 9-10 am

F 12-1 pm

- ❑ Tutorial Learning Center (TLC) hours:

MTWR 8-6 pm

F 8-11 am, 2-5 pm

Su 1-5 pm

# Chapter 32

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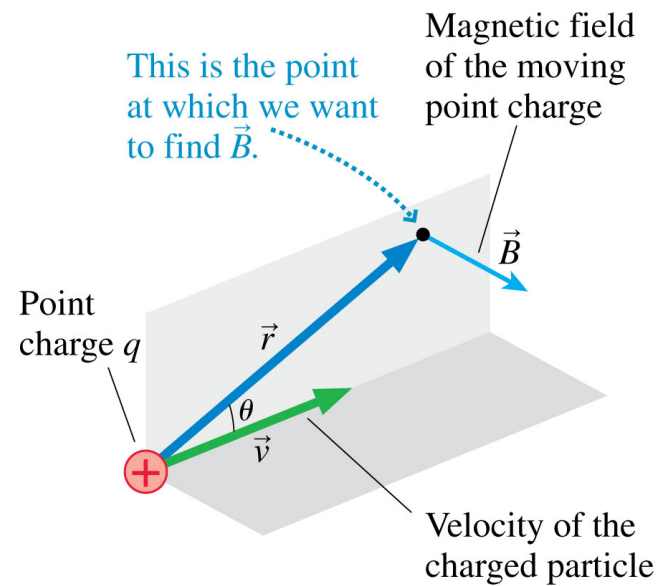
## The Magnetic Field

*(The Source of Magnetic Field: Moving  
Charges & The Magnetic Field of a Current)*

## Review...

The *magnetic field* of a charged particle  $q$  moving with velocity  $v$  is given by:

$$B_q = \frac{\mu_0}{4\pi} \frac{qv \sin \theta}{r^2}$$



*Notice:*

*All* charges create  $E$ -fields,  
but *only* moving charges create  $B$ -fields.

i.e. 32.1:

## The $B$ -field of a proton

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A proton moves with velocity  $\vec{v} = 1.0 \times 10^7 \hat{i}$  m/s . As it passes the origin, what is the  $B$ -field at the  $(x, y, z)$  positions

1. (1 mm, 0 mm, 0 mm),
2. (0 mm, 1 mm, 0 mm), and
3. (1 mm, 1 mm, 0 mm)?

# Superposition

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$B$ -fields have been found experimentally to obey the *principle of superposition*.

For  $n$  moving point charges, the *net*  $B$ -field is given by the vector sum...

$$\vec{B}_{total} = \vec{B}_1 + \vec{B}_2 + \dots + \vec{B}_n$$

# The Vector or Cross Product

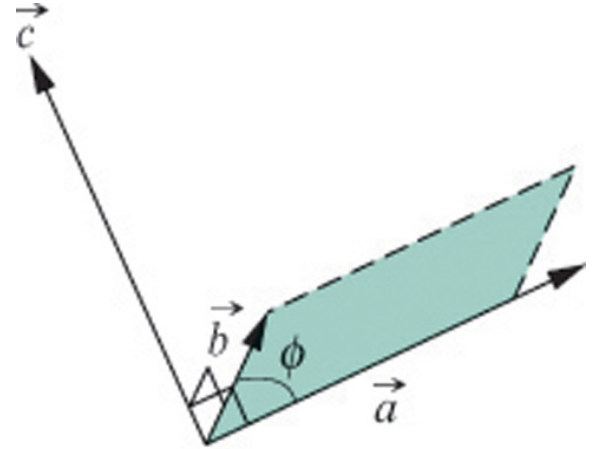
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The *vector or cross product* is defined as...

$$\vec{c} = \vec{a} \times \vec{b}$$

where the magnitude is:

$$c = ab \sin \phi$$



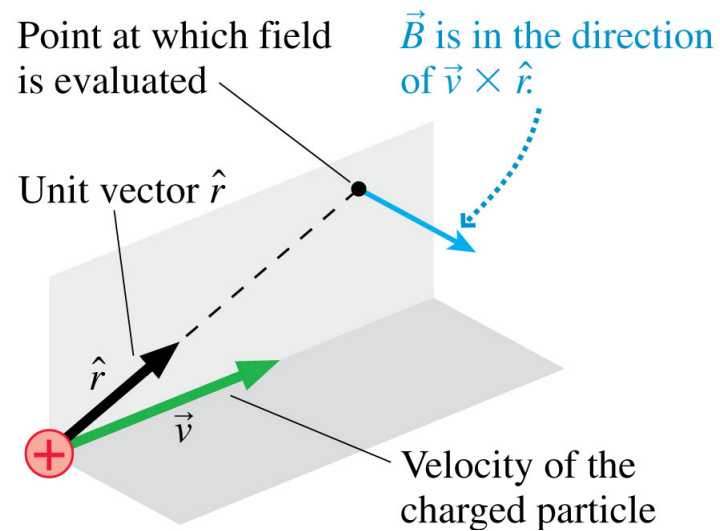
Note:

- vectors  $a$  &  $b$  form a plane, vector  $c$  is  $\perp$  to the plane
- Right hand rule gives the direction of vector  $c$
- $c = \text{area of the parallelogram formed by vectors } a \text{ \& } b$ .

# Biot-Savart Law

The Biot-Savart law can be written in terms of the cross product

$$\vec{B}_q = \frac{\mu_0}{4\pi} \frac{q \vec{v} \times \hat{r}}{r^2}$$



where unit vector  $\hat{r}$  points from charge  $q$  to the field point.

## Quiz Question 1

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What is the direction of the magnetic field at the position of the dot?

1. Into the screen.
2. Out of the screen.
3. Up.
4. Down.
5. Left.



$\vec{v}$  into screen



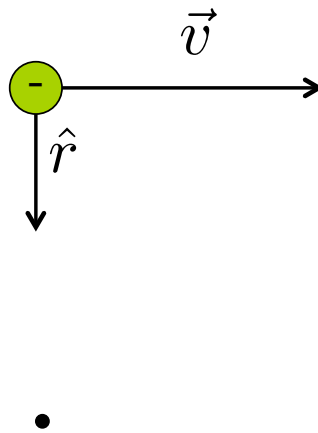
i.e. 32.2:

## The $B$ -field direction of a moving electron

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The electron in the figure below is moving to the right.

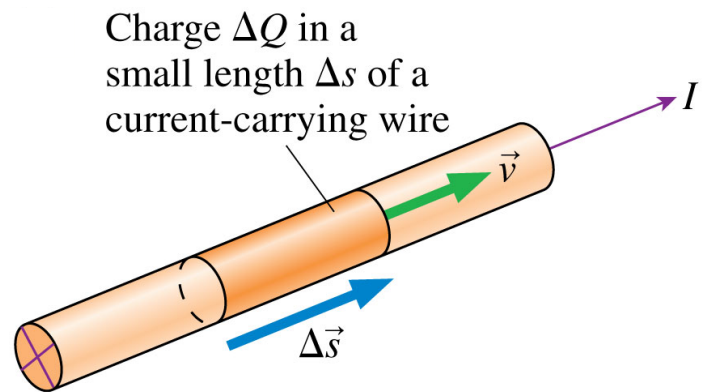
What is the direction of the electron's  $B$ -field at the position indicated with a dot?



## 32.4: The Magnetic Field of a Current

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The  $B$ -field of a very short segment of current is..

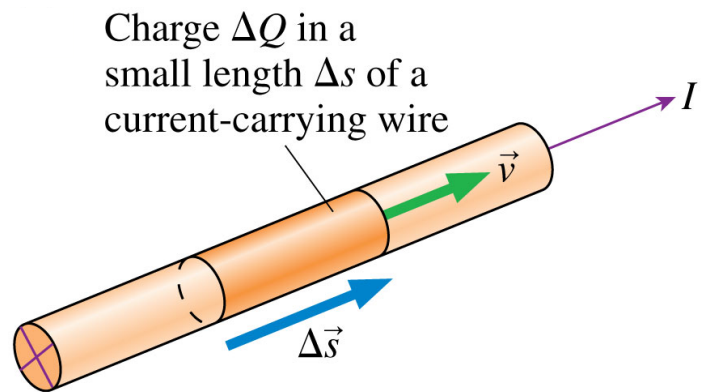


## 32.4:

# The Magnetic Field of a Current

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The  $B$ -field of a very short segment of current is..



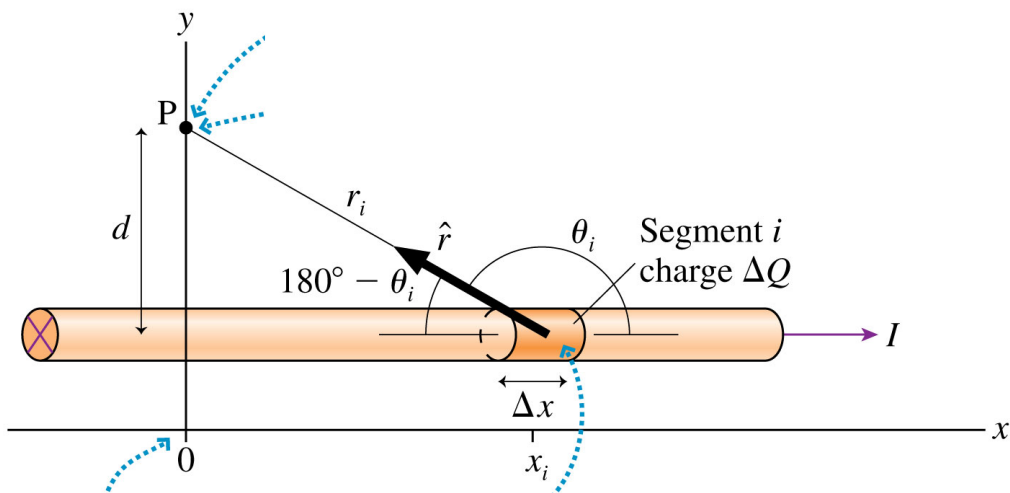
$$\vec{B}_{I \text{ seg}} = \frac{\mu_0}{4\pi} \frac{I \Delta\vec{s} \times \hat{r}}{r^2}$$

i.e. 32.3:

## The $B$ -field of a long, straight wire

A long, straight wire carries current  $I$  in the positive  $x$ -direction.

Find the  $B$ -field of a point that is distance  $d$  from the wire.

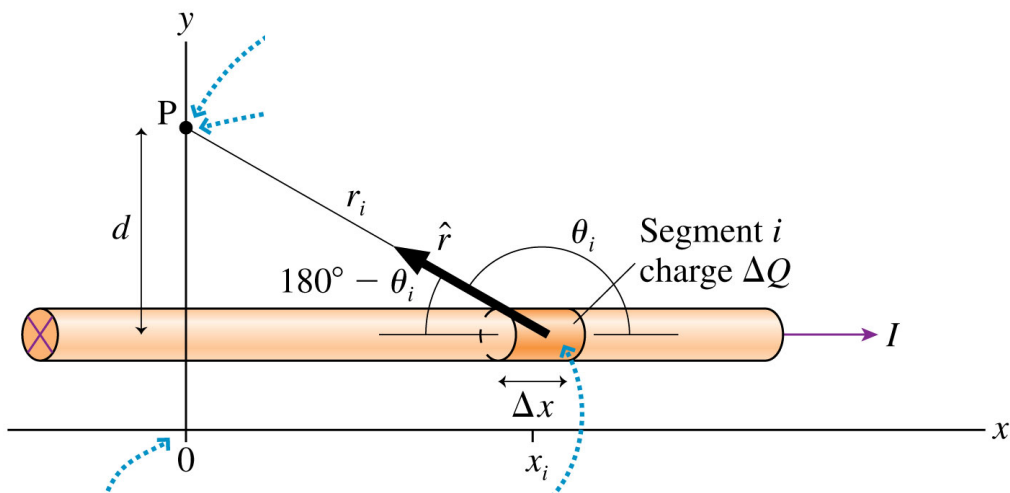


i.e. 32.3:

## The $B$ -field of a long, straight wire

A long, straight wire carries current  $I$  in the positive  $x$ -direction.

Find the  $B$ -field of a point that is distance  $d$  from the wire.



$$B_{wire} = \frac{\mu_0 I}{2\pi d}$$