

$$PV = NkT, E = fNkT = fPV : N = 6.02 \times 10^{23}, k = 1.38 \times 10^{-23} \text{ J/K}$$

$$\left(P + \frac{a}{V^2}\right)(V - nb) = NkT, E = \frac{3}{2}NkT - \frac{aN^2}{V} : \gamma = \frac{C_P}{C_V}$$

$$PV^\gamma = \text{const.} : TP^{(1-\gamma)/\gamma} = \text{const.} : TV^{(\gamma-1)} = \text{const.}$$

$$K = -\frac{1}{V} \left(\frac{\partial V}{\partial P} \right)_T, \alpha = \frac{1}{V} \left(\frac{\partial V}{\partial T} \right)_P, dE = Tds - PdV + \mu dN$$

$$Q = mC\Delta T, \delta Q = TdS, \Delta E = C\Delta T, w = - \int P(V) dV$$

$$\delta Q = \left[P + \left(\frac{\partial E}{\partial V} \right) + \left(\frac{\partial P}{\partial V} \right) \left(\frac{\partial E}{\partial P} \right) \right] dV$$

$$H = E + PV, G = E - TS + PV, F = E - TS, w_{by} \leq -\Delta F$$

$$\eta = \left| \frac{W_{net}}{Q_+} \right| = 1 - \left(\frac{V_F}{V_i} \right)^{\gamma-1}, \eta \leq 1 - \frac{T_L}{T_H}$$

$$\text{No } W_{nm} \text{ on system : } \Delta G \leq W_{nm} : W_{nm} \text{ on system : } -\Delta G \leq W_{nm}$$

$$\bar{x} = \sum x_i \cdot P(x_i), \bar{x^2} = \sum x_i^2 \cdot P(x_i), \sigma = \sqrt{(\bar{x^2}) - (\bar{x})^2}, P(k) = \binom{N}{k} p^k q^{N-k}, \text{Prob (macrostate)} = \frac{\Omega(N, q)}{\# \text{ microstates}} : p=q=1/2$$

$$E = -8M, M = M(N_+ - N_-), \bar{N}_\pm = N P_\pm, \bar{N}_\pm^2 = \bar{N}_\pm^2 + N P_\pm^2, \Omega(N, q) = \binom{N+q-1}{q} = \frac{(N+q-1)!}{q!(N-1)!}, E = \hbar \omega (q + 1/2)$$

$$\Omega = \Omega_A \Omega_B, \ln(N!) \approx N \ln(N) - N + \frac{1}{2} \ln(2\pi N), N! \approx N^N e^{-N} \sqrt{2\pi N}, \left(1 + \frac{x}{n}\right)^n \approx e^x, s = k \ln[\Omega]$$

$$\Gamma(E) = \# \text{ of microstates}, E = \frac{\hbar^2}{8mL^2} (n_x^2 + n_y^2 + n_z^2), P = \frac{e^{-\beta E}}{Z}, Z = \sum e^{-E_i \beta}, \hat{E} = -\frac{\partial}{\partial \beta} \ln(Z), C = \frac{\partial \bar{E}}{\partial T}$$

$$S = k \ln[g(E) dE]$$

$$P_{\text{speed}}(v) = 4\pi \left(\frac{m}{2\pi kT} \right)^{3/2} v^2 e^{-v^2 m / 2kT} = \alpha v^2 e^{-v^2 \delta}, Z_{\text{single}} = \alpha \int e^{-(p_x^2 + p_y^2 + p_z^2) \beta / 2m} dp_x dp_y dp_z$$

$$\bar{n}_k = \frac{1}{e^{(\epsilon - \mu)\beta} - 1} \rightarrow \text{Bosons}, \bar{n}_k = \frac{1}{e^{(\epsilon - \mu)\beta} + 1} \rightarrow \text{Fermions}$$

$$\bar{V} = \alpha \int_0^\infty v P(v), \text{Avg. k.E. } \bar{V^2} = \alpha \int_0^\infty v^2 P(v)$$

$$\left(\frac{\partial E}{\partial y} \right)_x = - \left(\frac{\partial E}{\partial x} \right)_y \left(\frac{\partial x}{\partial y} \right)_z, \left(\frac{\partial x}{\partial y} \right)_z \left(\frac{\partial y}{\partial z} \right)_x \left(\frac{\partial z}{\partial x} \right)_y = -1$$

$$\frac{1}{T} = \left(\frac{\partial S}{\partial E} \right)_{V,N}, \frac{P}{T} = \left(\frac{\partial S}{\partial V} \right)_{E,N}, \left(\frac{\partial S}{\partial P} \right)_T = - \left(\frac{\partial V}{\partial T} \right)_P$$

$$C_P = \left(\frac{\partial H}{\partial T} \right)_P, C_P = \left(\frac{\partial E}{\partial T} \right)_P + P \left(\frac{\partial V}{\partial T} \right)_P, C_P = C_V + TV \frac{\alpha^2}{\kappa}$$

$$C_V = \left(\frac{\partial E}{\partial T} \right)_V, C_V = \left(\frac{\partial H}{\partial T} \right)_V - V \left(\frac{\partial P}{\partial T} \right)_V$$

$$\text{Gas} \rightarrow \Delta s = \int_{T_i}^{T_f} \frac{C_V}{T} dT, \Delta s = \int_{T_i}^{T_f} \frac{C_P}{T} dT, \Delta s = \frac{Q}{T} = \frac{mC\Delta T}{T}$$

$$S = f \mu k \ln(T_i) + \mu k \ln(V_i) + \tilde{h}(N) \quad \text{Boltz}$$