### **Announcements**

□ Homework for tomorrow...

Ch. 30: CQ 10, Probs. 18, 20, & 22

CQ3: The answer lies in your (recently used) garden hose (look inside while turning it on).

30.4: 9.3 x 10<sup>-4</sup> m

30.6: a) 4.6 x 10<sup>21</sup> b) 4.3 x 10<sup>-12</sup> m

30.8: a)  $v_d = 7.5 \times 10^{-6} \text{ m/s}$ 

b)  $\tau = 2.1 \times 10^{-14} \text{ s}$ 

□ Office hours...

MW 10-11 am

TR 9-10 am

F 12-1 pm

■ Tutorial Learning Center (TLC) hours:

MTWR 8-6 pm

F 8-11 am, 2-5 pm

Su 1-5 pm

# Chapter 30

#### **Current & Resistance**

(Conductivity and Resistivity & Resistance and Ohm's Law)

#### Review...

□ Drift velocity...

$$v_d = \frac{e\tau}{m}E$$

□ Electron current...

$$i_e = \frac{n_e e \tau A}{m} E$$

□ Current...

$$I \equiv \frac{dQ}{dt} = i_e e$$

#### Review...

□ Current Density...

$$\boxed{J \equiv \frac{I}{A} = n_e e v_d}$$

□ Kirchoff's Junction Rule...

$$\Sigma I_{in} = \Sigma I_{out}$$

The current density in this wire is



- 1.  $4 \times 10^6 \,\text{A/m}^2$ .
- 2.  $2 \times 10^6 \,\text{A/m}^2$ .
- 3.  $4 \times 10^3 \,\text{A/m}^2$ .
- 4.  $2 \times 10^3 \,\text{A/m}^2$ .
- 5. Can't tell without knowing the length.

### 30.4: Conductivity and Resistivity

How is the current density, *J*, related to the *E*-field driving the current?

### Conductivity and Resistivity

How the current density, *J*, is related to the *E*-field driving the current:

$$J = \sigma E$$

where 
$$\sigma = \frac{n_e e^2 \tau}{m} = \text{conductivity}$$

### Conductivity and Resistivity

How the current density, J, is related to the E-field driving the current:

$$J = \sigma E$$

Where 
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$$[\sigma] = \Omega^{-1} m^{-1}$$

### Conductivity and Resistivity

How the current density, *J*, is related to the *E*-field driving the current:

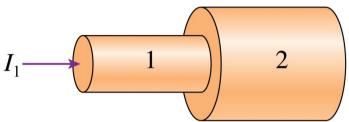
$$J = \sigma E$$

#### Notice:

- 1. *Current* is caused by the *E*-field exerting forces on the charge carriers.
- 2. The *current density* (& *current*) depend *linearly* on the *strength* of the *E*-field.
- 3. The *current density* also depends on the *conductivity* of the material.

Both segments of the wire are made of the same metal. Current  $I_1$  flows into segment 1 from the left.

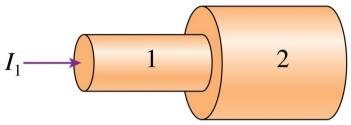
How does current  $I_1$  in segment 1 compare to current  $I_2$  in segment 2?



- 1.  $I_1 > I_2$ .
- 2.  $I_1 = I_2$ .
- 3.  $I_1 < I_2$ .
- 4. There's not enough information to compare them.

Both segments of the wire are made of the same metal. Current  $I_1$  flows into segment 1 from the left.

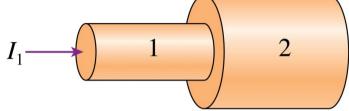
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- 1.  $J_1 > J_2$ .
- 2.  $J_1 = J_2$ .
- 3.  $J_1 < J_2$ .
- 4. There's not enough information to compare them.

Both segments of the wire are made of the same metal. Current  $I_1$  flows into segment 1 from the left.

How does the electric field  $E_1$  in segment 1 compare to the electric field  $E_2$  in segment 2?



- 1.  $E_1 > E_2$ .
- $E_1 = E_2$  but not zero.
- 3.  $E_1 < E_2$ .
- 4. Both are zero because metal is a conductor.
- 5. There's not enough information to compare them.

### 30.4: Conductivity and Resistivity

Define the *resistivity*...

$$\rho = \frac{1}{\sigma} = \frac{m}{n_e e^2 \tau}$$

# Conductivity and Resistivity

Define the resistivity...

$$\rho = \frac{1}{\sigma} = \frac{m}{n_e e^2 \tau}$$

$$[\rho] = \Omega \cdot m$$

### Conductivity and Resistivity

Define the resistivity...

$$\rho = \frac{1}{\sigma} = \frac{m}{n_e e^2 \tau}$$

**TABLE 30.2** Resistivity and conductivity of conducting materials

$$[\rho] = \Omega \cdot m$$

Material	Resistivity $(\Omega m)$	Conductivity $(\Omega^{-1} \mathbf{m}^{-1})$
Aluminum	$2.8 \times 10^{-8}$	$3.5 \times 10^{7}$
Copper	$1.7 \times 10^{-8}$	$6.0 \times 10^{7}$
Gold	$2.4 \times 10^{-8}$	$4.1 \times 10^{7}$
Iron	$9.7 \times 10^{-8}$	$1.0 \times 10^{7}$
Silver	$1.6 \times 10^{-8}$	$6.2 \times 10^{7}$
Tungsten	$5.6 \times 10^{-8}$	$1.8 \times 10^{7}$
Nichrome*	$1.5 \times 10^{-6}$	$6.7 \times 10^{5}$
Carbon	$3.5 \times 10^{-5}$	$2.9 \times 10^{4}$

<sup>\*</sup>Nickel-chromium alloy used for heating wires.

### i.e. 30.6: The *E*-field in a wire

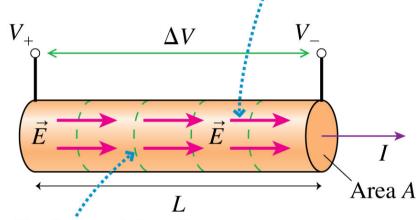
A 2.0 mm diameter aluminum wire carries a current of 800 mA. What is the E-field strength inside the wire?

### 30.5: Resistance and Ohm's Law

How is the *current*, *I*, related to the *potential difference*,

 $\Delta V$  in a wire?

The potential difference creates an electric field inside the conductor and causes charges to flow through it.



Equipotential surfaces are perpendicular to the electric field.

#### 30.5:

#### Resistance and Ohm's Law

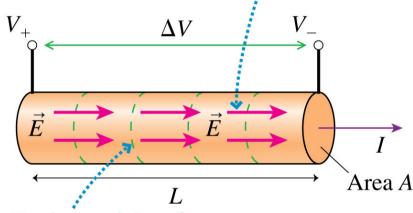
How is the *current*, I, related to the *potential difference*,  $\Delta V$  in a wire?

 $I = \frac{\Delta V}{R}$ 

- Ohm's Law

The potential difference creates an electric field inside the conductor and causes charges to flow through it.

SI Units of *R*?



Equipotential surfaces are perpendicular to the electric field.

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#### Resistance and Ohm's Law

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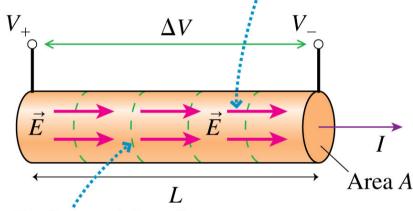
 $I = \frac{\Delta V}{R}$ 

- Ohm's Law

The potential difference creates an electric field inside the conductor and causes charges to flow through it.

SI Units of *R*?

$$[R] = \Omega$$



Equipotential surfaces are perpendicular to the electric field.

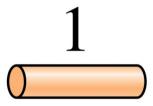
#### 30.5:

#### Resistance and Ohm's Law

#### Notice:

- $\blacksquare$  *Resistivity*,  $\rho$ , describes *just* the material.
- $lue{}$  Resistance, R, characterizes a specific piece of the conductor with a specific geometry.

Wire 2 has *twice* the length and *twice* the diameter of wire 1. What is the ratio  $R_2/R_1$  of their resistances?



- **1**. 1/4.
- **2**. 1/2.
- **3. 1.**
- 4. 2.
- 5. 4.

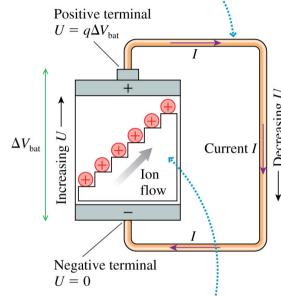


### Resistance and Ohm's Law

- A battery is a *source* of potential difference  $\Delta V_{\rm bat}$ .
- The battery *creates* a potential difference  $\Delta V_{\text{wire}} = \Delta V_{\text{bat}}$  between the ends of the wire.
- The potential difference in the wire  $\Delta V_{\rm wire}$  generates an E-field in the wire.
- The *E*-field establishes a current  $I = JA = \sigma AE$  in the wire.
- The current in the wire is determined *jointly* by the battery and the wire's resistance, *R* to be:

 $\Box I = \Delta V_{\text{wire}}/R$ 

The charge "falls downhill" through the wire, but a current can be sustained because of the charge escalator.



The charge escalator "lifts" charge from the negative side to the positive side. Charge q gains energy  $\Delta U = q \Delta V_{\rm hat}$ .