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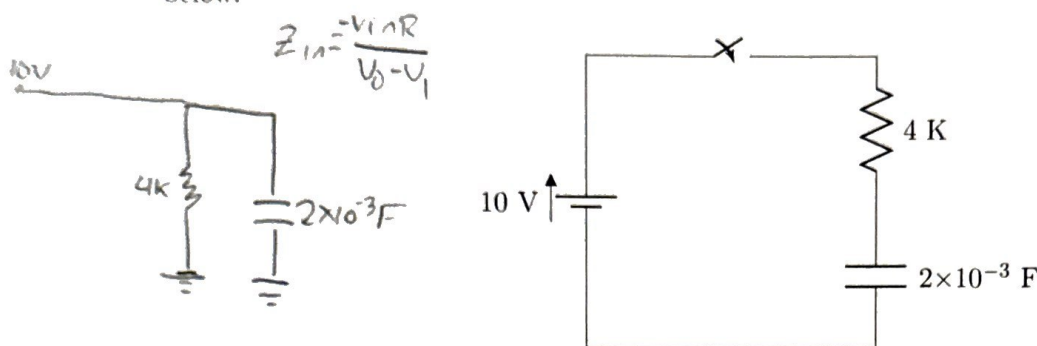
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Electronics for Scientists

RC Circuit

Instructions

Complete the following exercises to the best of your ability.

 A RC circuit has a 10 volt battery, a switch, a 4 K resistor and a 2×10^{-3} F capacitor, as shown below.


$$V_1 = V_0 e^{-t/\tau}$$

$$I = \frac{\Delta V}{R} \quad \Delta V = 12V$$

$$I = C \frac{dV}{dt}$$

 The capacitor is initially uncharged and the switch is closed at $t = 0$.

1. What is the time constant for this circuit?
2. At a time of 1 time constant after the switch is closed, find the current through the circuit, the voltage across and resistor, and the voltage across the capacitor.
3. At a time of 2 time constant after the switch is closed, find the current through the circuit, the voltage across and resistor, and the voltage across the capacitor.

$$1.) \tau = R \times C$$

$$= 4K(2 \times 10^{-3} F) = 8$$

$$\tau = 8 \text{ s}$$

$$t = 1RC$$

$$2.) t = 1.8$$

$$\tau = 8$$

$$V_1 = 10V e^{-t/\tau} = 8.8V \quad \Delta V = 1.2V \quad Z_1 = 33,333.3 \Omega$$

$$I = 0.26 \text{ mA}$$

$$V_R = 1.07V \quad V_C = 0.134V$$

$$3.) t = 2$$

$$\tau = 16$$

$$V_1 = 10V e^{-t/\tau} = 8.8V$$

$$I = 0.26 \text{ mA}$$

$$V_R = 1.07V \quad V_C = 0.134V$$

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Phys 251 HW 3



$R_1 = R_2 = 10k$
 $C = 0.1 \mu F$
 $R_3 = R_1 + R_2$

$R_3 = \frac{R_1 R_2}{R_1 + R_2} = \frac{10k(10k)}{10k + 10k} = 5k$

$I(5k) + I(0.1 \mu F) = V_0$

$I(R) + I(C) = V_0$

$R \frac{dV}{dt} + \frac{V}{C} = V_0$

$\frac{dV}{dt} (RC + \frac{1}{C}) = V_0$

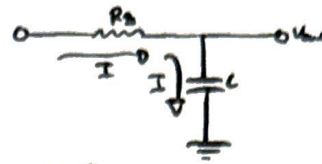
$\frac{dV}{dt} (\frac{R+1}{C}) = V_0$

$\frac{dV}{dt} = V_0 \left(\frac{C}{R+1} \right)$

$\int \frac{dV}{V_0} = \frac{C}{R+1} \int dt$

$\ln V = \frac{C}{R+1} t + K$

$\frac{RC + \frac{1}{C}}{C}$

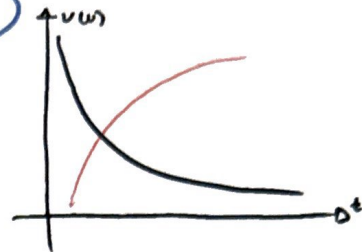


$I = C \frac{dV}{dt} \quad I = \frac{CV}{R}$

$\frac{dV}{dt} = \frac{CV}{R}$

$V = C \frac{1}{2} t^2$

$V = C \frac{1}{2} t^2$



1.18 | $C = 1 \mu F$
 $I = 1 mA$
 $V = 10 V$

$Q = CV$

$Q = I \cdot \Delta t$

$CV = I \Delta t$

$\Delta t = \frac{CV}{I} = \frac{1.0 \times 10^{-6} F (10 V)}{1.0 \times 10^{-3} A} = 0.01 s$

$\Delta t = 0.01 s$