

Wave Properties of Matter Q.M. 1

Main Concepts

Wave-Particle Duality)
Probabilistic Interpretation

Idea of Bohr Correspondance
works w/ size & temperature.

Uncertainty Principle

Wave Function, the "meaning" of matter waves, & Einstein Podolsky-Rosen proposal

5.2 De Broglie waves

5.1 } x-ray & electron diffraction
5.3 }

$$\vec{\nabla} \times \vec{E} = - \frac{\partial \vec{B}}{\partial t}$$

$$\vec{\nabla} \times \vec{B} = \mu \vec{J} + \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

- 1) Matter-energy & space-time "dualities"
- 2) Planck's Quantization hypothesis & P.E. effect
⇒ Wave-particle "Duality" of Radiation
- 3) Bohr Model & assumptions of Quantizing L

Photon Energy

$$E = h\nu \quad E = pc$$

$$c = \lambda\nu$$

⇓

$$h\nu = p(\lambda\nu)$$

$$\lambda = h/p$$

De Broglie suggests that matter has a wavelength. (Matter sometimes acts like a wave)

Ex 5.2

λ_0 for a "classical" tennis ball vs a Quantum Electron

Tennis Ball

$$m = 0.06 \text{ kg}$$

$$v = 10 \text{ m/s}$$

$$\lambda = \frac{h}{p} = \frac{6.63 \times 10^{-34} \text{ J}\cdot\text{s}}{(0.06 \text{ kg})(10 \text{ m/s})} = 1.105 \times 10^{-37} \text{ m}$$

Electrons

$$K = 50 \text{ eV}$$

$$\lambda = \frac{h}{p} = \frac{h}{\sqrt{2mK}} = \frac{hc}{\sqrt{2mc^2K}} = \frac{hc}{\sqrt{2(0.511 \text{ MeV})(50 \text{ eV})}} = 0.17 \text{ nm}$$

Ex 5.4

$$T = 300 \text{ K}$$

$$\langle K \rangle = \frac{3}{2} kT = \frac{p^2}{2m}$$

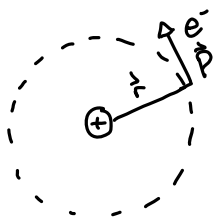
$$p = \sqrt{3mKT}$$

$$\lambda = \frac{h}{p} = 2.52 \text{ m} \cdot K^{-1/2} \frac{1}{T^{1/2}}$$

$$\lambda = 0.145 \text{ nm} \quad T = 300 \text{ K}$$

$$\lambda = 0.287 \text{ nm} \quad T = 77 \text{ K}$$

Bohr's Quantization Condition:



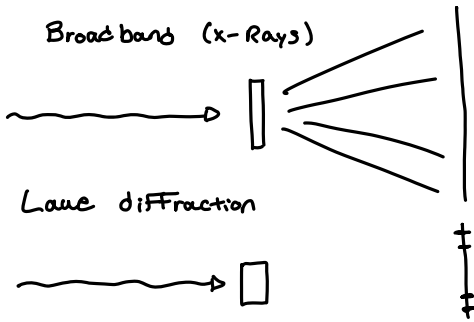
De Broglie Says "Stationary States are standing matter waves"

$$n\lambda = 2\pi r \quad \lambda = \frac{h}{p}$$

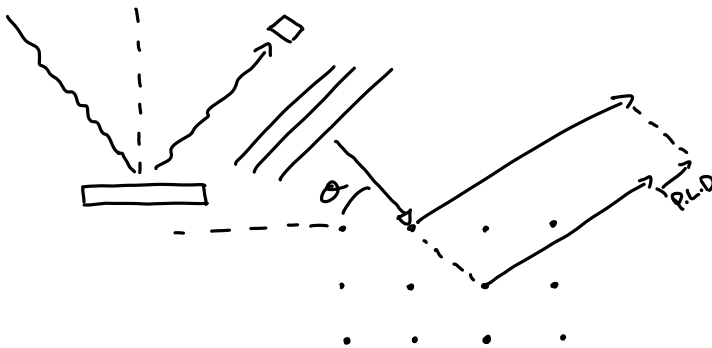
$$\frac{nh}{p} = 2\pi r \Rightarrow r = \frac{n\hbar}{p} \quad \hbar = \frac{h}{2\pi}$$

$$|L| = |r \times p| \Rightarrow L = rp = \left(\frac{n\hbar}{p}\right)p \Rightarrow L = n\hbar \quad \text{Bohr's Condition}$$

X-Ray Scattering



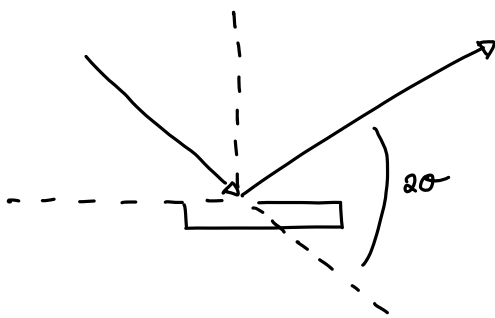
Pattern of Spots is regular and reflects underlying Crystal Structure.



- 1) Angle of Incidence = Angle of reflection
- 2) $n\lambda = \text{PLD}$ for constructive interference



$$n\lambda = 2d \sin \theta$$



Ex: x-Rays Bragg Scattered from NaCl ($n=1$)

$$\lambda = \frac{2d \sin \theta}{n}$$

$$2\theta = 20^\circ \Rightarrow \theta = 10^\circ$$

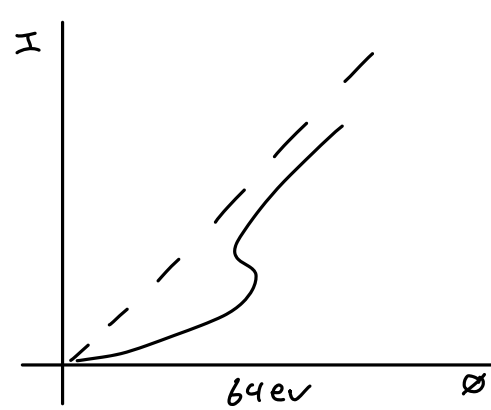
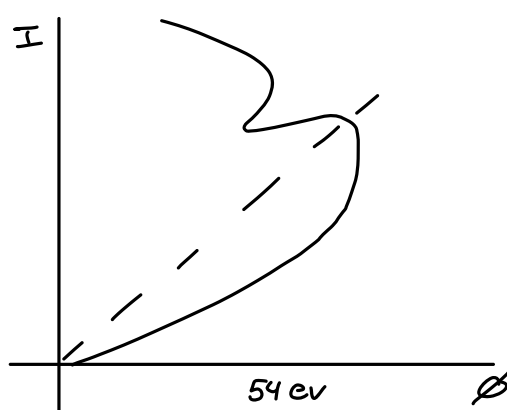
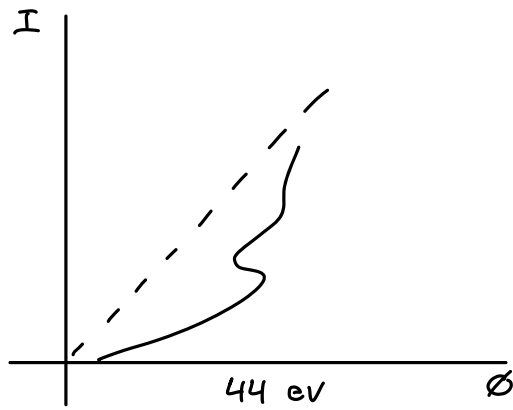
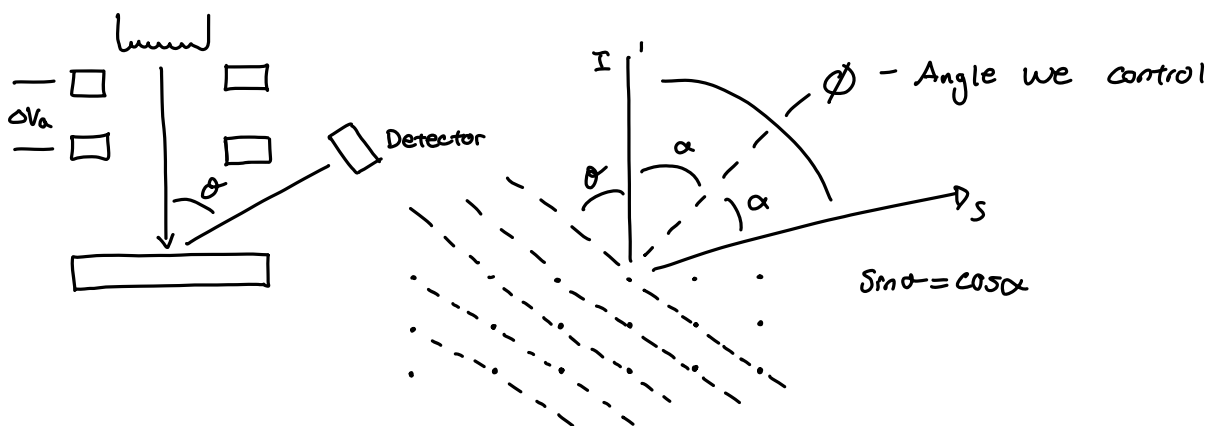
$$\frac{\# \text{ atoms}}{V} = \frac{N_A}{\mu_m} = 4.5 \times 10^{23} \#/\text{cm}^3$$

$$N_A = 6.02 \times 10^{23} \#/\text{mol}$$

$$\mu_m = 58.5 \text{ g/mol}$$

$$\rho = 2.16 \text{ g/cm}^3$$

$$d = \sqrt[3]{V/\#} = 2.8 \times 10^{-10} \text{ m} = 0.28 \text{ nm} \Rightarrow \lambda = \frac{2d \sin \theta}{n} = 0.097 \text{ nm}$$



$$\begin{aligned}
 n\lambda &= 2d \sin \theta \\
 &= 2d \cos \alpha = 2d \sin \alpha \cos \alpha = d \sin 2\alpha \quad (n=1) \\
 &= d \sin \phi
 \end{aligned}$$

$$\begin{aligned}
 D &= 0.015 \text{ nm} \quad \lambda = \frac{D \sin \phi}{n} = 0.163 \text{ nm} \\
 \phi &= 60^\circ
 \end{aligned}$$