

$$Z = f(x,y) = 2(x-1)^2 + 4(y-3)^2 + 6$$

$$P(2,-2,12)$$

$$Z - Z_0 = f_x(x_0, y_0)(x - x_0) + f_y(x_0, y_0)(y - y_0)$$

$$\frac{\partial Z}{\partial x} = 2(x^2 - 2x + 1) \quad \frac{\partial Z}{\partial y} = 4(y-3)^2$$

$$\frac{\partial Z}{\partial x} = 4x - 4$$

$$4y^2 - 24y + 36$$

$$\frac{\partial Z}{\partial y} = 8y - 24$$

$$\frac{\partial Z}{\partial x}(2, -2) = 4(2) - 4 = 8 - 4 = 4$$

$$\frac{\partial Z}{\partial y}(2, -2) = 8(-2) - 24 = -16 - 24 = -40$$

$$Z - 12 = 4(x-2) + (-40)(y+2)$$

$$Z = 4x - 8 - 40y - 80 + 12$$

$$Z = 4x - 40y - 76$$

$$f(x,y) = \sqrt{y + \cos^2 x}$$

Find lin approx at  $(\pi, 0)$

$$\frac{\partial Z}{\partial x} = (y + \cos^2 x)^{\frac{1}{2}}$$

$$u = \cos x$$

$$u^2 = \cos^2 x$$

$$2u \cdot u' = 2\cos x \cdot -\sin x$$

$$\frac{1}{2}(y + \cos^2 x)^{-\frac{1}{2}} \cdot -2\cos x \sin x$$

$$\frac{-2\cos x \sin x}{2\sqrt{y + \cos^2 x}}$$

$$\frac{\partial Z}{\partial y} = \frac{1}{2}(1 + \cos^2 x)^{-\frac{1}{2}} \cdot 1$$

$$\frac{\partial Z}{\partial x} = \frac{-\cos x \sin x}{\sqrt{y + \cos^2 x}}$$

$$\frac{\partial Z}{\partial y} = \frac{1}{2\sqrt{y + \cos^2 x}}$$

$$\frac{\partial Z}{\partial x}(\pi, 0) = \frac{0}{0}$$

$$\frac{\partial Z}{\partial y}(\pi, 0) = \frac{1}{2}$$

$$Z - 1 = 0(x - \pi) + \frac{1}{2}(y - 0)$$

$$Z - 1 = \frac{1}{2}y$$

$$Z = \frac{1}{2}y + 1$$

$$L(x,y) = Z = \frac{1}{2}y + 1$$

Defn: If  $\frac{\partial f}{\partial x}$  and  $\frac{\partial f}{\partial y}$  are

continuous in a neighborhood of  $(x_0, y_0)$

we say  $f$  is differentiable at  $(x_0, y_0)$

$$\lim_{h \rightarrow 0} \frac{f(a+h, b) - f(a, b)}{h}$$

$$\lim_{h \rightarrow 0} \frac{f(a, b+h) - f(a, b)}{h}$$

$$h = 10$$

$$h = -10$$

$$f(v, t)$$

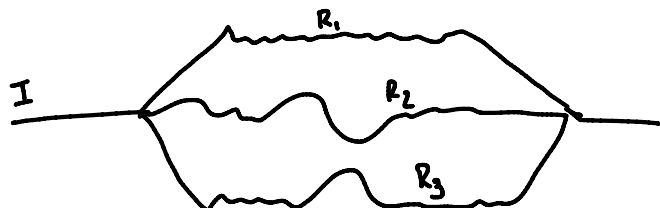
$$f(40, 20) = 28$$

$$\frac{\partial f}{\partial v}(40, 20) \approx \frac{f(50, 20) - f(30, 20)}{50 - 30} = \frac{40 - 17}{20} = \frac{23}{20}$$

$$\frac{\partial f}{\partial t}(40, 20) \approx \frac{f(40, 30) - f(40, 10)}{30 - 10} = \frac{31 - 25}{20} = \frac{6}{20} = \frac{3}{10}$$

$$h - 28 = \frac{23}{20}(v - 40) + \frac{3}{10}(t - 20)$$

$$h = 28 + \frac{23}{20}(v - 40) + \frac{3}{10}(t - 20)$$



Equivalent to a single resistance  $R$

$$R_1 = 32 \Omega$$

$$R_2 = 25 \Omega \pm 0.5\%$$

$$R_3 = 4 \Omega$$

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$R = R(R_1, R_2, R_3) \quad R(32, 25, 4) = 3.1128$$

$$L(R_1, R_2, R_3) = \frac{\partial R}{\partial R_1}(32, 25, 4) + \frac{\partial R}{\partial R_2}(32, 25, 4) + \frac{\partial R}{\partial R_3}(32, 25, 4)$$

$$\frac{\partial R}{\partial R_1} = -\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}\right)^2 \left(\frac{1}{R_1^2}\right) \approx 0.00446 \quad L(R_1, R_2, R_3) = 0.00446(0.005 \cdot 32) + 0.005(0.005 \cdot 25) + 0.0056(0.005 \cdot 4) + 3.1128$$

$$\frac{\partial R}{\partial R_2} = -\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}\right)^2 \left(\frac{1}{R_2^2}\right) \approx 0.0155$$

$$3.1281 - 3.1128$$

$$\frac{\partial R}{\partial R_3} = -\left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}\right)^2 \left(\frac{1}{R_3^2}\right) \approx 0.0056$$