

2.2

Variable	Best Estimate	Probable Range	
Position, $x$	53.3	53.1 to 53.5 (cm)	$\int = 0.2 \text{ cm}$
Velocity, $v$	-13.5	-14.0 to -13.0 (cm/s)	$\int = -0.5 \text{ cm/s}$
Acceleration, $a$	93	90 to 96 (cm/s <sup>2</sup> )	$\int = 3 \text{ cm/s}^2$

$$x_{\text{best}} \pm \int x$$

$$\begin{array}{l} 53.3 \pm 0.2 \text{ cm} \\ -13.5 \pm 0.5 \text{ cm/s} \\ 93 \pm 3 \text{ cm/s}^2 \end{array}$$

2.4

a.)  $x = 3.323 \pm 1.4 \text{ mm}$

$$x = 3.3 \pm 1.4 \text{ mm}$$

b.)  $t = 1,234,567 \pm 54321 \text{ s}$

$$t = 1.2345 \times 10^4 \pm 5.4321 \times 10^4 \text{ s}$$

c.)  $\lambda = 5.33 \times 10^{-7} \pm 3.21 \times 10^{-9} \text{ m}$

$$\lambda = (533 \pm 3.00) \times 10^{-9} \text{ m}$$

d.)  $r = 0.000,000,538 \pm 0.000,000,03 \text{ mm}$

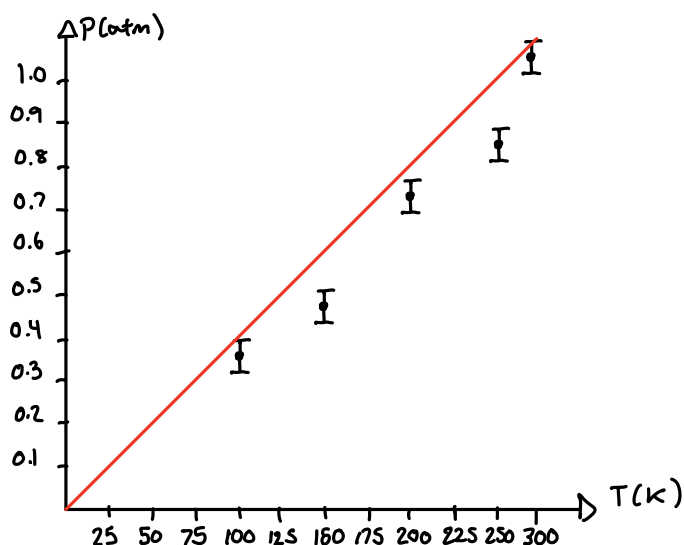
$$r = (53 \pm 3.0) \times 10^{-8} \text{ mm}$$

2.12

Trial no.	Acceleration $a \text{ (m/s}^2\text{)}$	Expected Acceleration $g \sin \theta \text{ (m/s}^2\text{)}$	Discrepancies	Uncertainty
1	$2.04 \pm 0.04$	$2.36 \pm 0.1$	-0.32	$\pm 0.14$
2	$3.58 \pm 0.06$	$3.88 \pm 0.08$	-0.30	$\pm 0.14$
3	$4.32 \pm 0.08$	$4.57 \pm 0.05$	-0.25	$\pm 0.13$
4	$4.85 \pm 0.09$	$5.05 \pm 0.04$	-0.20	$\pm 0.13$
5	$5.53 \pm 0.01$	$5.72 \pm 0.03$	-0.19	$\pm 0.13$

The discrepancies do not lie in the range of the uncertainty so we cannot say  $a$  is given by  $g \sin \theta$

2.15



Since the data is close to or going through the error bars, this is consistent with the claim.

2.23

Meter Stick:  $\delta l: \frac{1 \text{ mm}}{2} = 0.5 \text{ mm}$

$l = 2 \text{ cm}$

Error:  $\frac{0.5 \text{ mm}}{20 \text{ mm}} = 0.025 = 2.5\%$

$E = \frac{\delta l}{l}$

The meterstick cannot make this measurement.  
2.5%

Microscope:  $\delta l: \frac{0.1 \text{ mm}}{2} = 0.05 \text{ mm}$

$l = 2 \text{ cm}$

Error:  $\frac{0.05 \text{ mm}}{20 \text{ mm}} = 0.0025 = 0.25\%$

The microscope can make this measurement.  
0.25%

2.27

a.)  $x = 6.1234$  F.u. = 2%

$6.1234 \cdot (0.02) = 0.122468$

1 sig Fig 0.1

$6.1 \pm 0.1$ , 2 sig Figs

b.)  $y = 1.1234$  F.u. = 2%

$1.1234 \cdot 0.02 = 0.022468$

$1.12 \pm 0.02$ , 3 sig Figs

## 2.28

a.)  $a = 11.5 \pm 0.2 \text{ cm}$   $b = 25.4 \pm 0.2 \text{ s}$   $q = ab$

$$a_{\text{best}} \cdot b_{\text{best}} = 11.5 \cdot 25.4 = 292.1 \text{ cm} \cdot \text{s}$$

$$\text{uncertainty in } a: \frac{\Delta a}{a_{\text{best}}} = \frac{0.2}{11.5} = 0.017391 = 1.739\%$$

$$\text{uncertainty in } b: \frac{\Delta b}{b_{\text{best}}} = \frac{0.2}{25.4} = 0.007874 = 0.7874\%$$

$$\text{absolute uncertainty: } 1.739\% + 0.7874\% = 2.526\%$$

$$292.1 \times 0.025 = 7.3 \equiv \text{uncertainty}$$

$$q = 292 \pm 7 \text{ cm} \cdot \text{s}$$

b.)  $a = 5.0 \text{ m} \pm 7\%$   $b = 3.0 \text{ N} \pm 1\%$

$$a_{\text{best}} \cdot b_{\text{best}} = 15 \text{ N} \cdot \text{m}$$

$$\text{uncertainty in } a: \frac{\Delta a}{a_{\text{best}}} = \frac{0.35}{5.0} = 0.07 = 7\%$$

$$7\% \text{ of } 5.0 = 0.35$$

$$\text{uncertainty in } b: \frac{\Delta b}{b_{\text{best}}} = \frac{0.03}{3.0} = 0.01 = 1\%$$

$$1\% \text{ of } 3.0 = 0.03$$

$$\text{absolute uncertainty: } 0.07 + 0.01 = 0.08 = 8\%$$

$$15 \text{ N} \cdot 0.08 = 1.2 \equiv \text{uncertainty}$$

$$q = 15 \pm 1.2 \text{ N} \cdot \text{m}$$