

Announcements

□ Homework for tomorrow...

Ch. 29: CQ 10, Probs. 20, 22, & 54

CQ4a) $E_1 = E_2 = -(10 \text{ V/m}) \hat{i}$

b) $E_1 = -(5 \text{ V/m}) \hat{i}$, $E_2 = -(20 \text{ V/m}) \hat{i}$

CQ5: accelerates right

29.6: $W = 1.6 \times 10^{-13} \text{ J}$

29.12: $E_x(0\text{cm} < x < 2\text{cm}) = +2,500 \text{ V/m}$ $E_x(2\text{cm} < x < 3\text{cm}) = -10,000 \text{ V/m}$

29.44: $E = 40 \text{ V/m}$, $\theta = 27^\circ$ ccw from $+x$ -axis

□ Office hours...

MW 10-11 am

TR 9-10 am

F 12-1 pm

□ Tutorial Learning Center (TLC) hours:

MTWR 8-6 pm

F 8-11 am, 2-5 pm

Su 1-5 pm

Chapter 29

Potential & Field (*Combinations of Capacitors*)

Review...

□ *Kirchoff's Loop Rule...*

$$\Delta V_{loop} = \sum_i (\Delta V)_i = 0$$

□ *Conductors in Electrostatic Equilibrium...*

□ *Capacitance...*

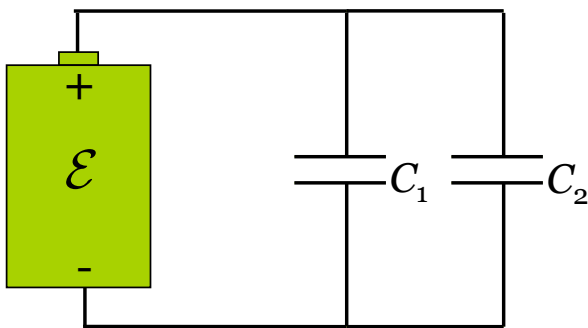
$$C \equiv \frac{Q}{\Delta V_C}$$

$$C = \frac{\epsilon_0 A}{d} \quad (\text{parallel-plate capacitor})$$

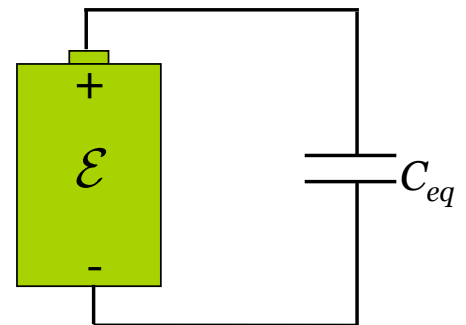
Combinations of Capacitors

Consider two capacitors in *parallel*...

- Can we find an *equivalent capacitor*, C_{eq} , to the two capacitors, C_1 & C_2 ?



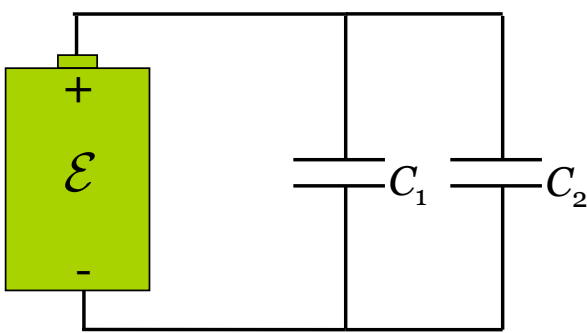
$\stackrel{?}{=}$



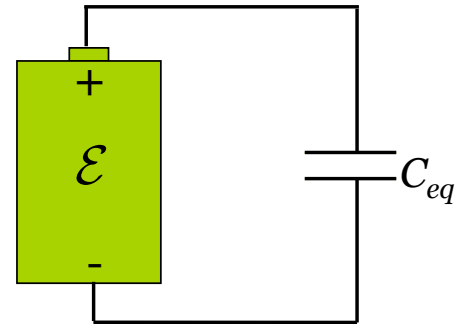
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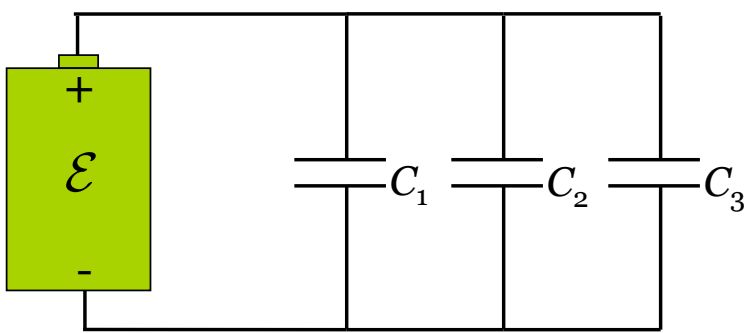
- YES!

$$C_{eq} = C_1 + C_2$$

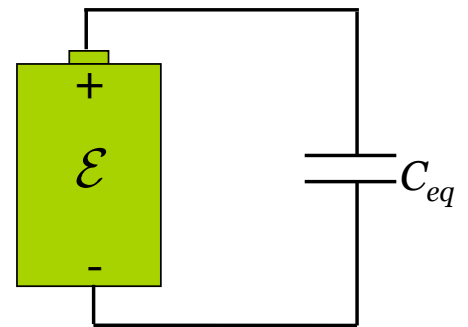
Combinations of Capacitors

What about for *several* capacitors in *parallel*?

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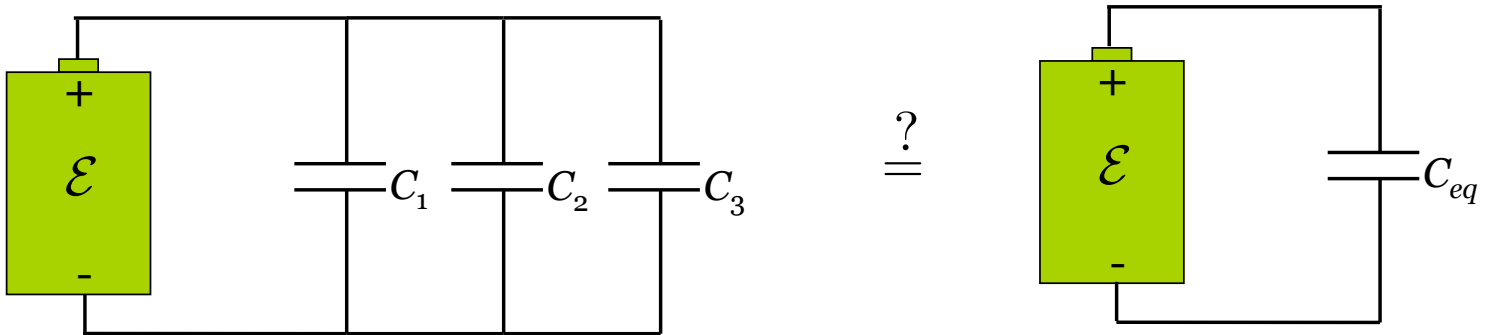
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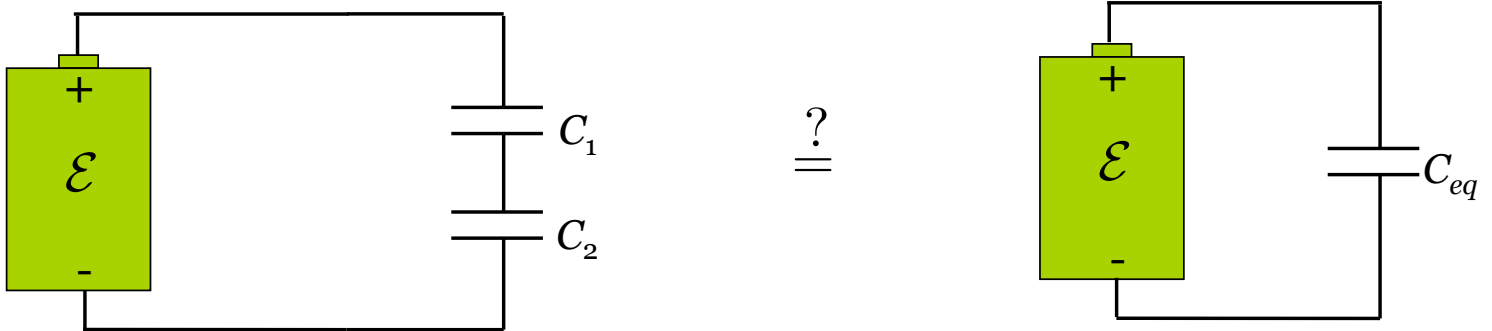


$$C_{eq} = C_1 + C_2 + \dots$$

Combinations of Capacitors

Consider two capacitors in *series*...

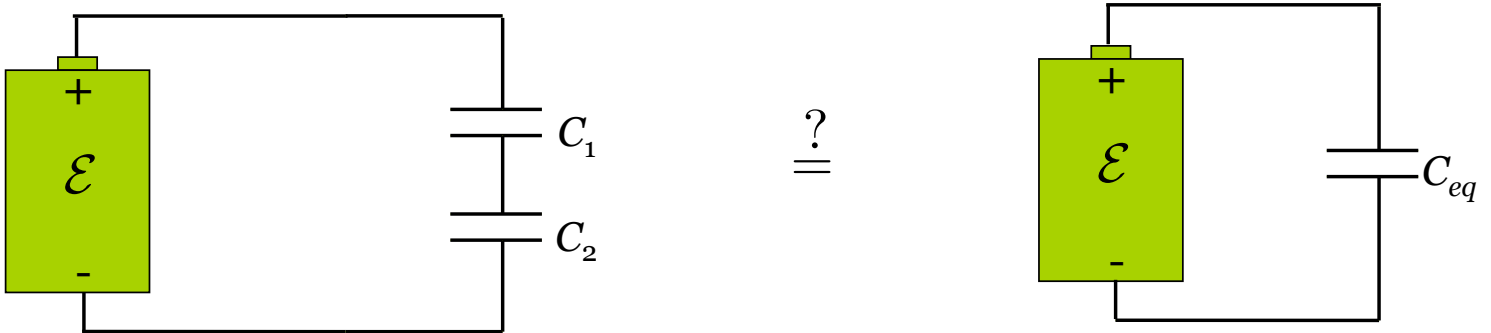
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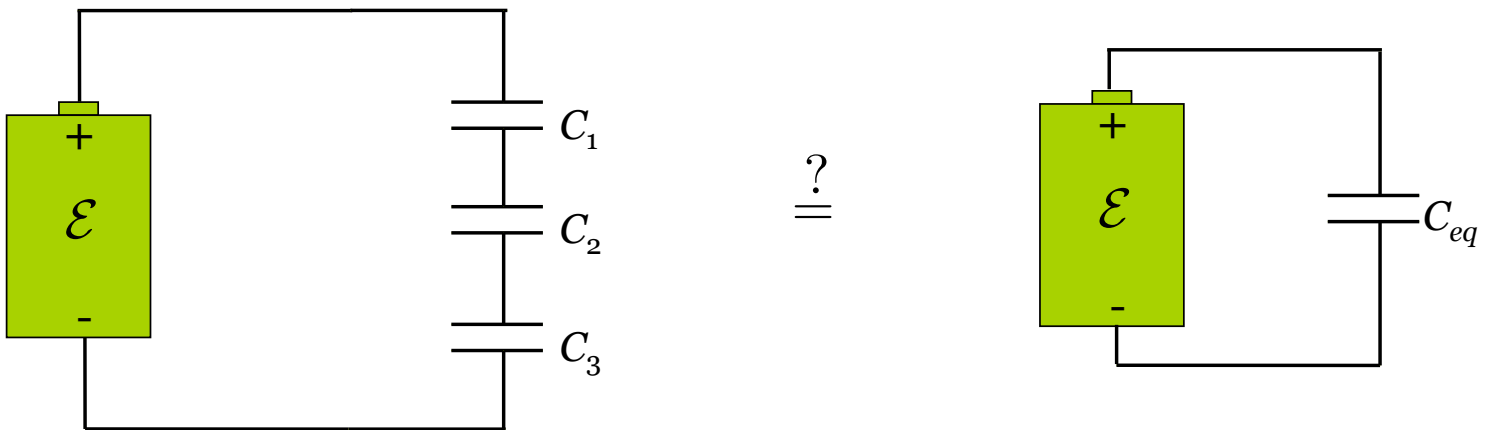
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$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

Combinations of Capacitors

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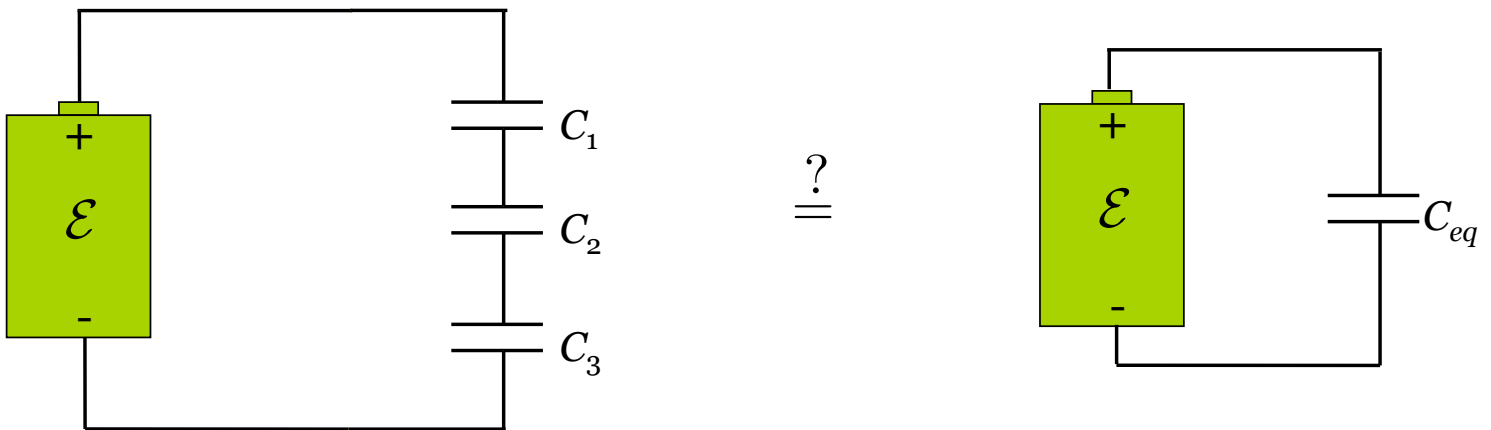
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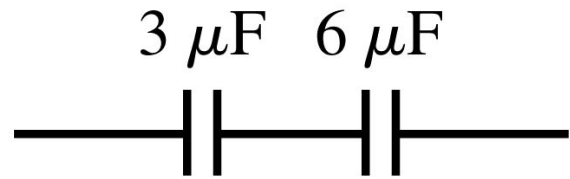
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Quiz Question 1

The equivalent capacitance is



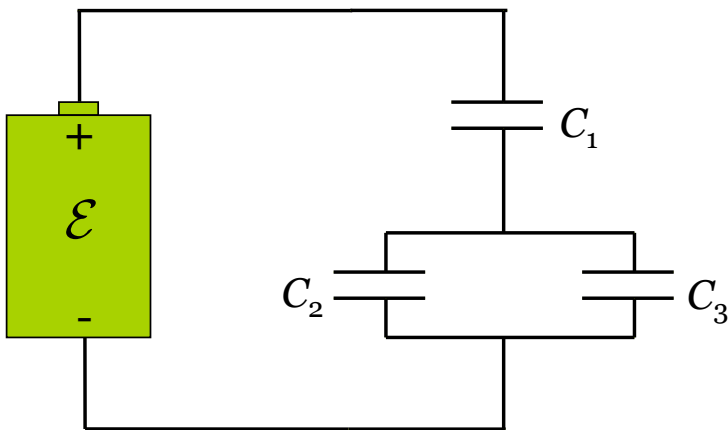
1. $9\ \mu\text{F}$.
2. $6\ \mu\text{F}$.
3. $3\ \mu\text{F}$.
4. $2\ \mu\text{F}$.
5. $1/2\ \mu\text{F}$.

i.e. 29.7:

A Capacitor Circuit

Find the charge on and the potential difference across each of the three capacitors in the figure below.

Given: $\mathcal{E} = 12 \text{ V}$, $C_1 = 3 \mu\text{F}$, $C_2 = 5 \mu\text{F}$, $C_3 = 1 \mu\text{F}$

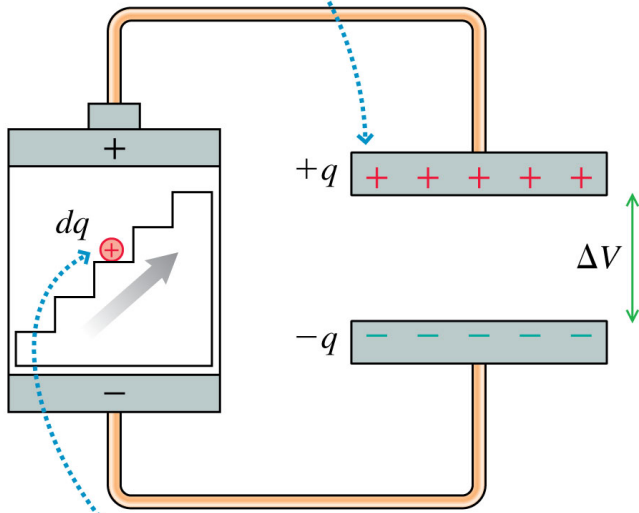


29.6:

The Energy Stored in a Capacitor

How much *energy* is transferred from the battery to the capacitor?

The instantaneous charge on the plates is $\pm q$.



Initially : $q = 0, U = 0$

Finally : $q = Q, U = U_C$

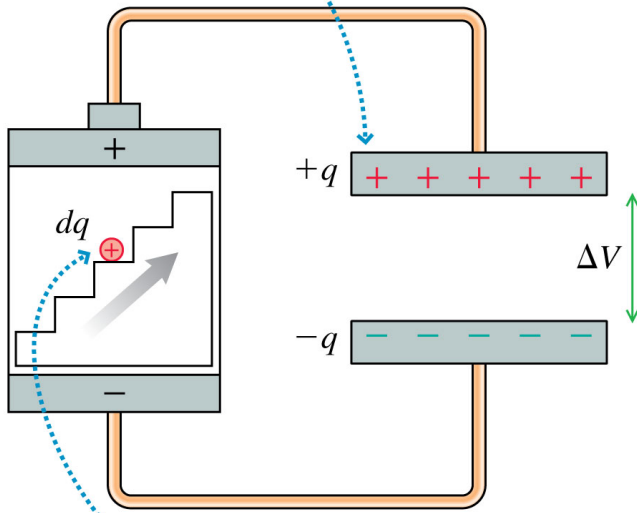
The charge escalator does work $dq \Delta V$ to move charge dq from the negative plate to the positive plate.

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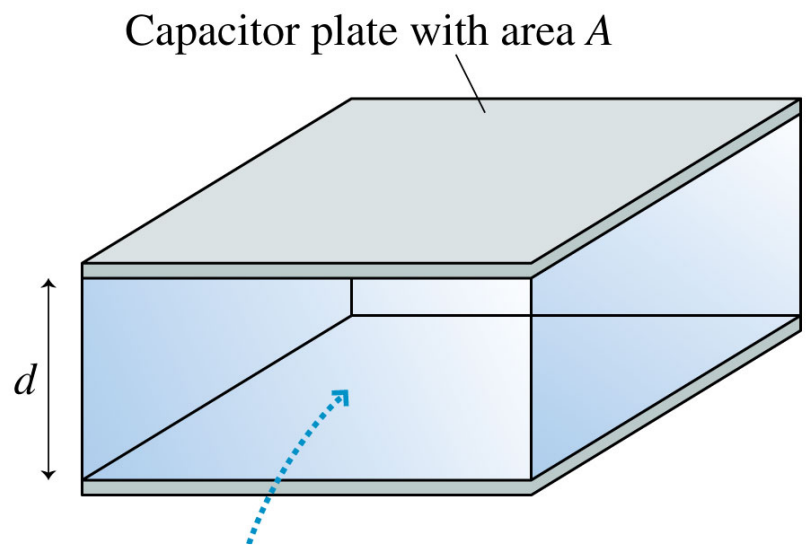
$$U_C = \frac{Q^2}{2C}$$

or

$$U_C = \frac{1}{2} C (\Delta V_C)^2$$

The Energy in the Electric Field

Q: If a capacitor is analogous to a stretched spring, *where* is the stored energy?



The Energy in the Electric Field

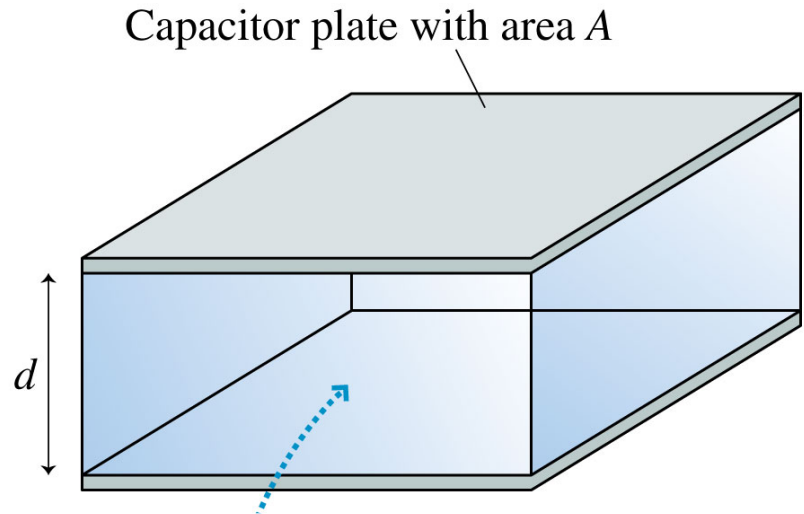
Q: If a capacitor is analogous to a stretched spring, *where* is the stored energy?

□ A: In the E -field!

$$u_E = \frac{1}{2} \epsilon_0 E^2$$

energy stored

volume in which it is stored



When the capacitor is discharged, the energy is released as the E -field *collapses*.