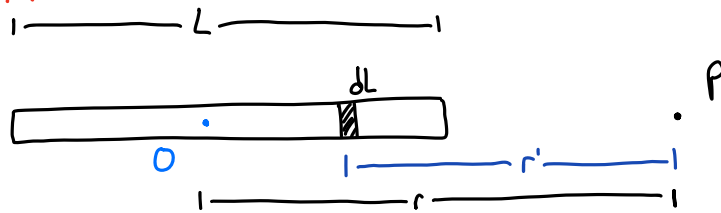


Ch. 26 P. 40

26.P.40



$$\lambda = \frac{Q}{L}$$

$$L\lambda = Q$$

$$E = \frac{K\Delta Q}{\Delta r}$$

a.)

$$\int_{-L/2}^{L/2} \frac{K\Delta Q}{(r-r')^2} = \int_{-L/2}^{L/2} \frac{K\lambda}{(r-r')^2} dr = \int_{-L/2}^{L/2} \frac{KQ}{L(r-r')^2} dr \quad \begin{matrix} u = r - r' \\ du = -dr \end{matrix}$$

$$\int_{-L/2}^{L/2} \frac{KQ}{L(r-r')^2} dr = \frac{KQ}{L} \int_{-L/2}^{L/2} \frac{1}{(r-r')^2} dr = \frac{KQ}{L} \int_{-L/2}^{L/2} (r-r')^{-2} dr$$

$$\frac{KQ}{L} \int_{-L/2}^{L/2} (u)^{-2} r' du = \frac{KQ}{L} \left[\frac{-r'}{(r-r')} \right]_{-L/2}^{L/2} = KQ \left(\frac{1}{r^2 - L^2/4} \right) \quad \text{a.) } \frac{KQ}{r^2 - L^2/4}$$

b.)

$$\frac{L/2 - (-L/2)}{L} = \frac{L}{L} = 1 \quad \text{L's cancel out} \quad \frac{KQ}{r^2 - L^2/4}$$

If \$r\$ is growing much bigger in comparison to \$L\$, we can treat \$L\$ as if it were approaching 0.

$$\text{b.) } \frac{KQ}{r^2}$$

$$\lim_{L \rightarrow 0} \frac{KQ}{r^2 - L^2/4} = \frac{KQ}{r^2 - 0/4} = \frac{KQ}{r^2}$$

c.)

$$\frac{KQ}{r^2 - L^2/4} \quad \begin{matrix} r = 0.03 \text{ m} \\ L = 0.05 \text{ m} \\ Q = 3.0 \times 10^{-9} \text{ C} \end{matrix}$$

$$\frac{9.0 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2} (3.0 \times 10^{-9} \text{ C})}{(0.03 \text{ m})^2 - (0.05 \text{ m})^2/4} = 9.8 \times 10^4 \text{ N/C} \quad \text{c.) } 9.8 \times 10^4 \text{ N/C}$$

$$\text{a.) } \frac{KQ}{r^2 - L^2/4} \quad \text{b.) } \frac{KQ}{r^2} \quad \text{c.) } 9.8 \times 10^4 \text{ N/C}$$

Ch. 28 CQ: 4 Probs 2 & 4

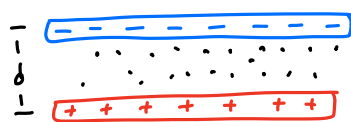
Conceptual
28.C.4

a.) The change in potential energy of path (1-D3) and path (1-D2) are equal because it is a conservative force. It is also the same height for both paths.

b.) Same speeds since change in potential energy is equal.

Problems

28.P.2



$$\vec{E} = 20,000 \text{ N/C}$$

$$d = 0.001 \text{ m}$$

$$W = KE$$

$$\Delta u = -w$$

$$\Delta u = qE\Delta s$$

$$W = \frac{1}{2}mv^2$$

$$\vec{E} = \frac{\eta}{\epsilon_0}$$

$$\epsilon_0 \vec{E} = \eta$$

$$\eta = 1.77 \times 10^{-7} \text{ C/m}^2$$

$$q = -1.602 \times 10^{-19} \text{ C}$$

$$q = -1.60 \times 10^{-19} \text{ C}$$

$$-QE\Delta s = -\frac{1}{2}mv^2$$

$$E = 20,000 \text{ N/C}$$

$$E = 20,000 \text{ N/C}$$

$$2QE\Delta s = mv^2$$

$$\Delta s = 0.001 \text{ m}$$

$$\Delta s = 0.001 \text{ m}$$

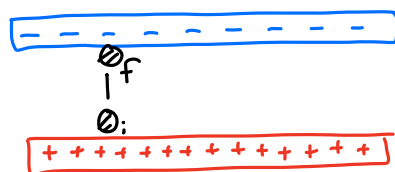
$$\frac{2QE\Delta s}{m_e} = v^2$$

$$m_e = 9.11 \times 10^{-31} \text{ kg}$$

$$v = \sqrt{\frac{2QE\Delta s}{m_e}}$$

$$v = 2.65 \times 10^6 \text{ m/s}$$

28.P.4



$$v_i = 0 \text{ m/s}$$

$$v_f = 50,000 \text{ m/s}$$

$$KE = \frac{1}{2}mv^2$$

$$m = 4m$$

$$\text{Proton: } \frac{1}{2}m_p v_p^2$$

$$\text{Helium: } \frac{1}{2}m_H v_H^2$$

$$\text{uniform } \vec{E} \therefore$$

$$KE_p = KE_H$$

$$\frac{1}{2}m_p v_p^2 = \frac{1}{2}m_H v_H^2$$

$$m_p v_p^2 = m_H v_H^2$$

$$v_H^2 = \frac{m_p v_p^2}{m_H}$$

$$v_H = \sqrt{\frac{m_p v_p^2}{m_H}}$$

$$v_H = \sqrt{\frac{m_p v_p^2}{4m_H}}$$

$$v_p = 50,000 \text{ m/s}$$

$$m_p = 1.67 \times 10^{-27} \text{ kg}$$

$$m_H = 4(1.67 \times 10^{-27} \text{ kg})$$

$$v_H = 25,000 \text{ m/s}$$