

# Announcements

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❑ EXAM 2 on Tuesday, March 14!

❑ Homework for tomorrow...

Ch. 31: CQ 11, Probs. 24, 59, & 60

CQ6:  $P_c, P_d, P_a, P_b$

31.10:  $2.4 \times 10^{-5} \text{ m}$

31.16:  $1.2 \Omega$

31.42:  $3/8 \text{ W}$

❑ Office hours...

MW 10-11 am

TR 9-10 am

F 12-1 pm

❑ Tutorial Learning Center (TLC) hours:

MTWR 8-6 pm

F 8-11 am, 2-5 pm

Su 1-5 pm

# Chapter 31

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## Fundamentals of Circuits *(Parallel Resistors & Resistor Circuits)*

# Review...

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*Equivalent resistor* for resistors in *parallel*...

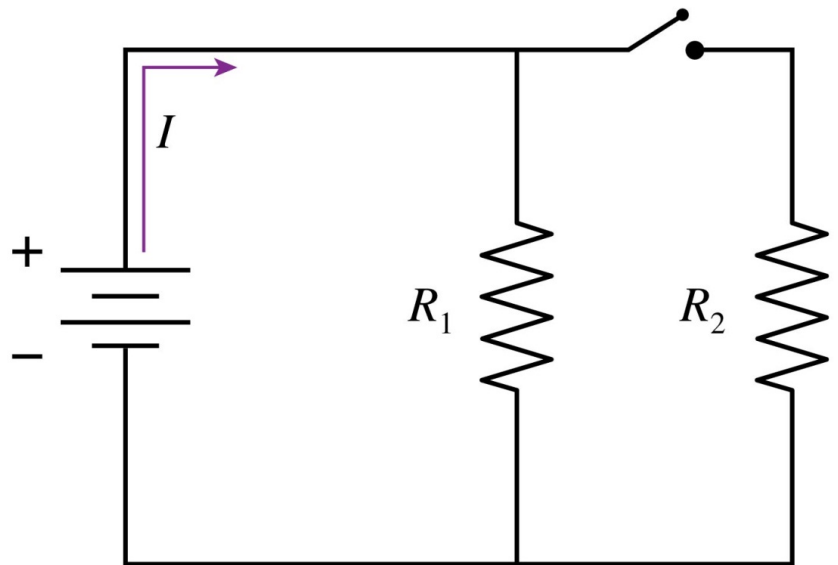
$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

## Quiz Question 1

When the switch closes, the battery current

Resistance in parallel  
goes down compared to 1

1. increases.
2. stays the same.
3. decreases.

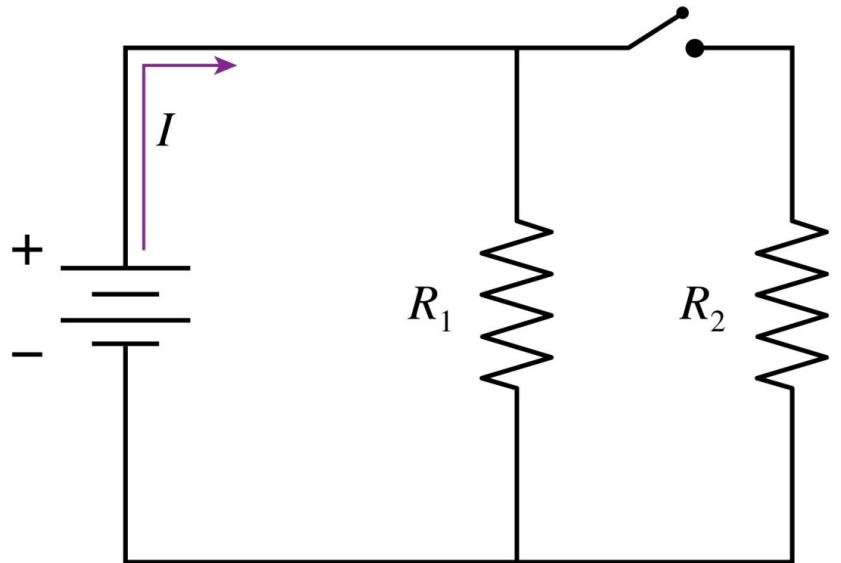


## Quiz Question 1

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When the switch closes, the battery current

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Notice:

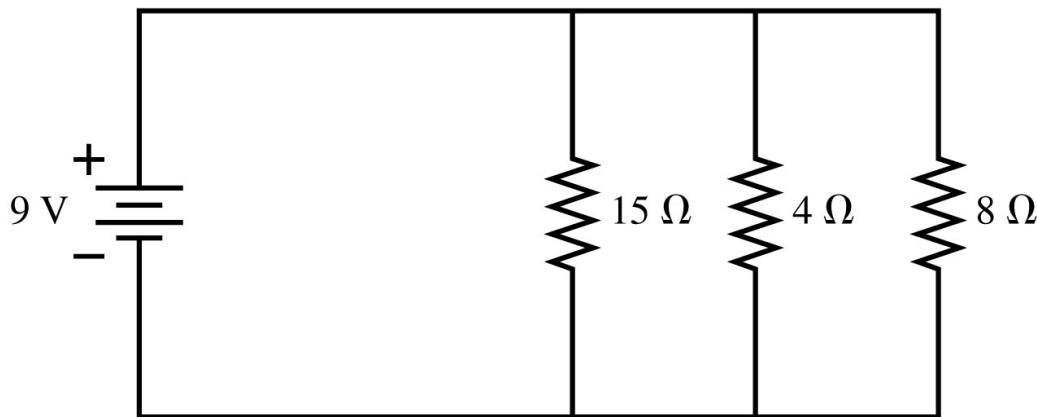
The equivalent of several resistors in parallel is *always less than* any single resistor in the group.

i.e. 31.8:

## A parallel resistor circuit

The three resistors of the figure below are connected to a 9V battery.

Find the battery *current* and the *potential difference* across and the *current* through each resistor.

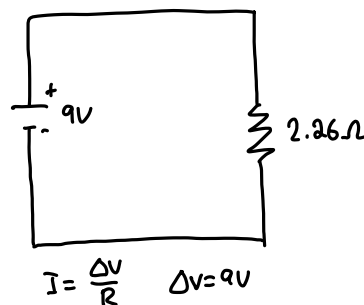


$$\frac{1}{R_{eq}} = \left( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right)$$

$$\frac{1}{R_{eq}} = \left( \frac{1}{15\Omega} + \frac{1}{4\Omega} + \frac{1}{8\Omega} \right)$$

$$\frac{1}{R_{eq}} = \left( \frac{53}{120\Omega} \right)$$

$$R_{eq} = 2.26\Omega$$



$$I = \frac{\Delta V}{R} \quad \Delta V = 9V \quad R = 2.26\Omega$$

$$I = 3.98 A$$

$$I \approx 4 A$$

$$I_1 = \frac{\Delta V}{R_1} \quad R_1 = 15\Omega \quad I_2 = \frac{\Delta V}{R_2} \quad R_2 = 4\Omega \quad I_3 = \frac{\Delta V}{R_3} \quad R_3 = 8\Omega$$

$$I_1 = 0.6 A$$

$$I_2 = 2.25 A$$

$$I_3 = 1.125 A$$

$$\Delta V_1 = 9V, I_1 = 0.6A$$

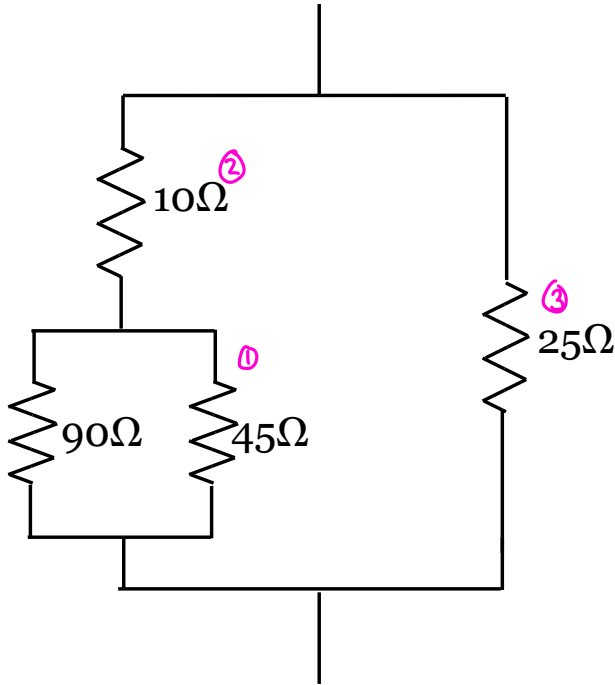
$$\Delta V_2 = 9V, I_2 = 2.25A$$

$$\Delta V_3 = 9V, I_3 = 1.125A$$

i.e. 31.9:

## A combination of resistors

What is the equivalent resistance of the group of resistors shown in the figure below?



$$1: \frac{1}{R_{eq}} = \left( \frac{1}{90\Omega} + \frac{1}{45\Omega} \right)$$

$$\frac{1}{R} = \left( \frac{1}{30\Omega} \right)$$

$$R = 30\Omega$$

$$(1+2) + (3)$$

$$\frac{1}{R} = \left( \frac{1}{40\Omega} + \frac{1}{25\Omega} \right)$$

$$R = 15.38\Omega$$

$$2: \begin{matrix} 1+2 \\ 30\Omega + 10\Omega \end{matrix}$$

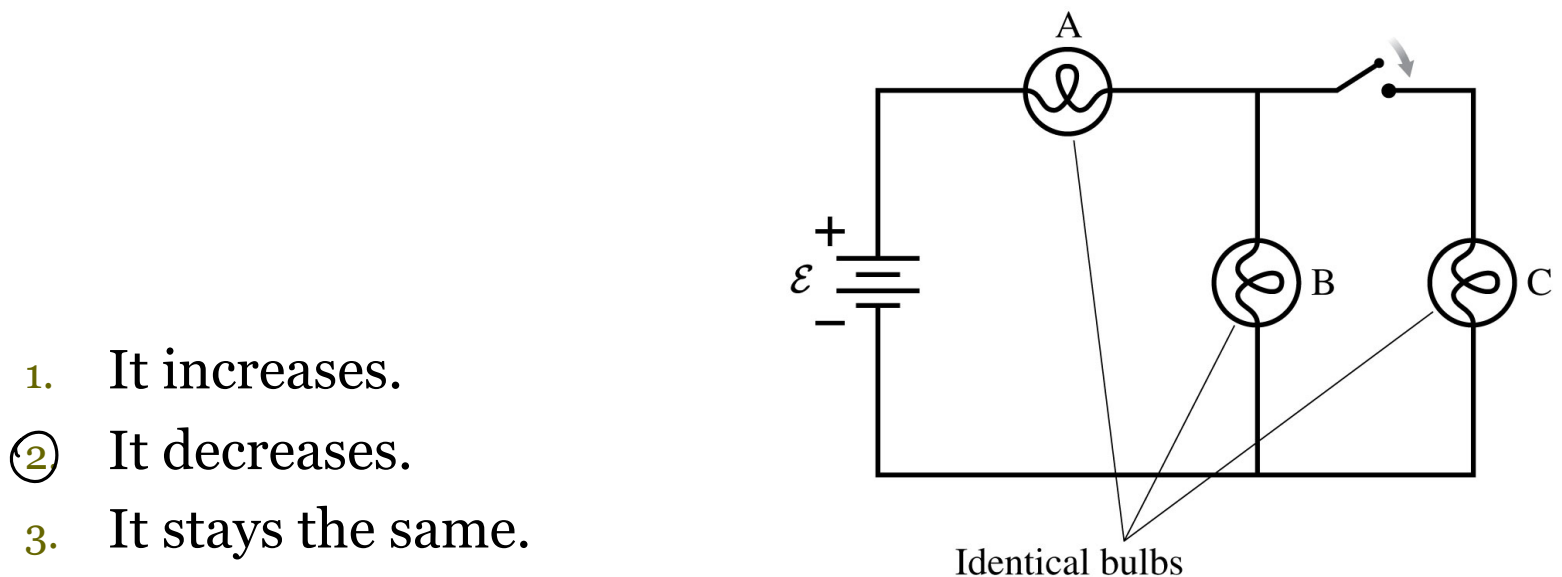
$$R = 40\Omega = 1+2$$

$$R = 15.4\Omega$$

## Quiz Question 2

Consider the circuit below, where the switch is open. The current is the same through bulbs A and B, and they are equally bright. Bulb C is not glowing.

The switch is now closed, what happens to the brightness of B?

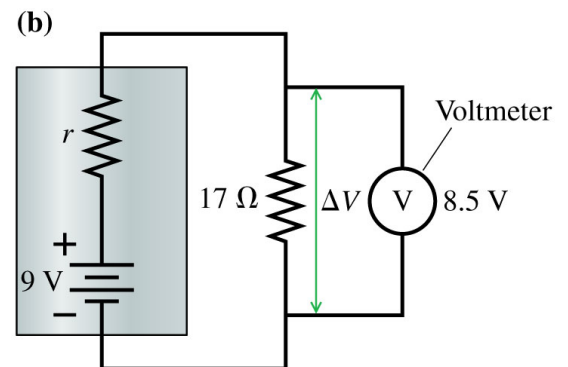
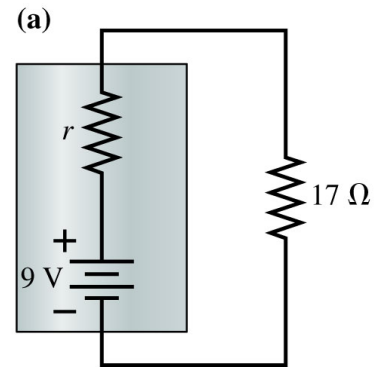


1. It increases.
- ② It decreases.
3. It stays the same.



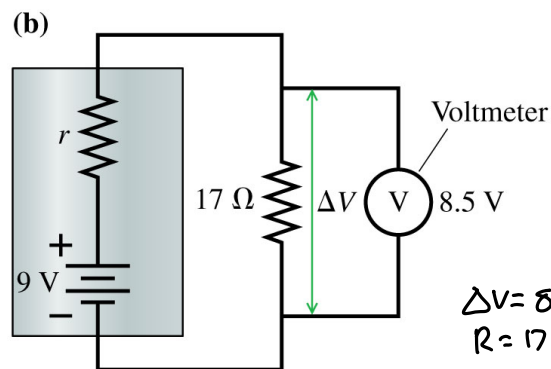
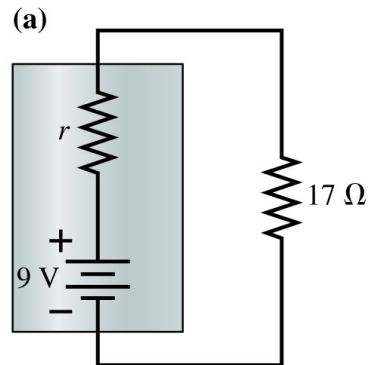
# Voltmeters...

- are used to measure *potential differences*.
- Must be wired in *parallel* with the circuit element whose voltage is to be measured.
- $R_{\text{voltmeter}} \sim \infty \Omega$



i.e.

What is the *internal resistance* of the battery in the figure below?



$$\Delta V = 8.5\text{ V}$$
$$R = 17\ \Omega$$

$$I = \frac{8.5\text{ V}}{17\ \Omega} = 0.5\text{ A}$$

$$9\text{ V} - I(r) - 8.5\text{ V} = 0$$

$$-Ir = -0.5\text{ V}$$

$$r = \frac{0.5\text{ V}}{0.5\text{ A}}$$

$$r = 1\ \Omega$$

# *Resistor Circuits*

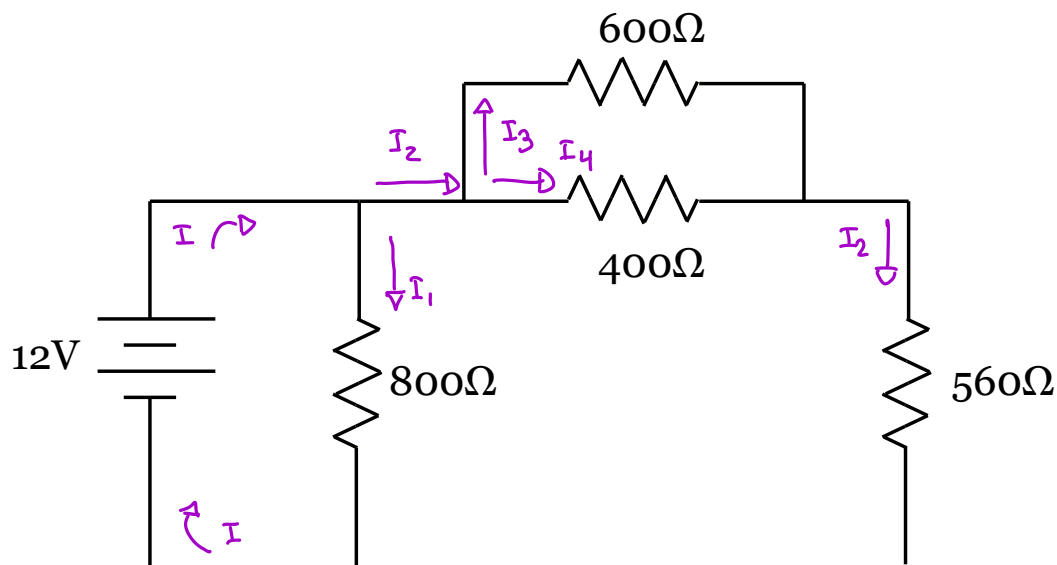
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1. Draw a circuit diagram, labeling all known quantities.
2. Reduce circuit to the smallest possible number of equivalent resistors.
3. Write Kirchhoff's loop rule for each loop and Kirchhoff's junction rule for each junction.
4. Solve the equations and check your results.

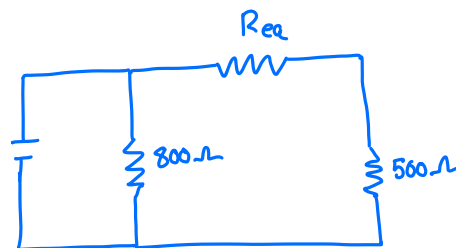
i.e. 31.10:

## Analyzing a complex circuit

Find the *current through* and the *potential difference across* each of the four resistors in the circuit shown below.

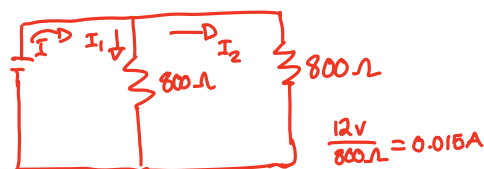


$$R_{eq} = \left( \frac{1}{600\Omega} + \frac{1}{400\Omega} \right)^{-1} = 240\Omega$$



$$R_{eq} + 240\Omega = 800\Omega$$

$$R_{eq}' = 400\Omega$$



$$\frac{12V}{800\Omega} = 0.015A$$

$$I = I_1 + I_2$$

$$I_1 = I_2$$

$$I = 0.03A$$

$$I = \frac{\Delta V}{R}$$

$$\Delta V = 12V$$

$$R = 400\Omega$$

$$I = 0.03A$$

