

Mon: HW due by 5pm

Tues: Discussion / quiz

Supp Ex 9, 11

Ch 2 Con Q 11

Ch 2 Probs 9, 12, 38

Extra challenge optional

40, 82, 41

Weds: Lecture.

Survey: Q1 Hope to learn?

Q2 Do with knowledge?

TYPICAL: physics content, motion, everyday world
application to major/career; get degree

ALSO: * solve problems, arguments using technical concepts/math,
* doing word problems
* decide what is relevant

Recap : Velocity

Velocity describes the rate at which position changes. Schematically:

Velocity = rate of change
of position

Conceptual Idea

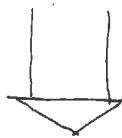


Mathematical
Definition

Observe position, x , as time, t passes.
Then

$$v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$$

speed = absolute
value of
velocity



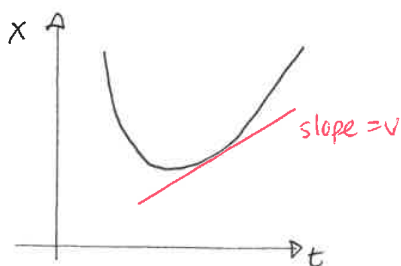
Computing / calculating

Given position information,
how to get velocity

1) Use calculus to get
derivatives

2) graphically

$v =$ slope of tangent to x vs t

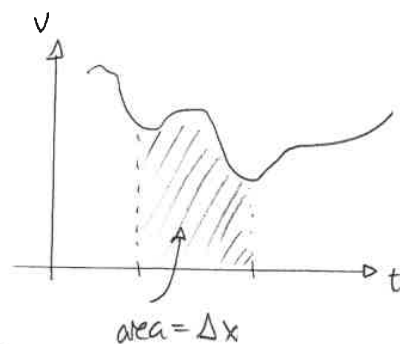


Given velocity information,
how to get position

1) use calculus (integration)

2) graphically:

$\Delta x =$ area between graph
of v vs t at time axis



Acceleration

Although velocity contains useful information about motion, it is not the quantity that appears most readily in the physics of motion. That role belongs to quantity that describes how velocity changes. Specifically we need to consider the rate at which velocity changes - this is acceleration. Before defining this we consider ways in which velocity can change as time passes.

Demo PHET Moving Man \rightarrow Charts Tab

$$\text{set } \begin{cases} x_0 = 0 \\ v_0 = -4 \\ a = 2 \end{cases}$$

observe - graph of x, v

- look at
- a) initial \rightarrow left most turn
- b) moving left \rightarrow moving right
- c) after turn.



We see that velocity can change by either or both of:

- a) speed changing
- b) direction changing

To describe changes in velocity we will use:

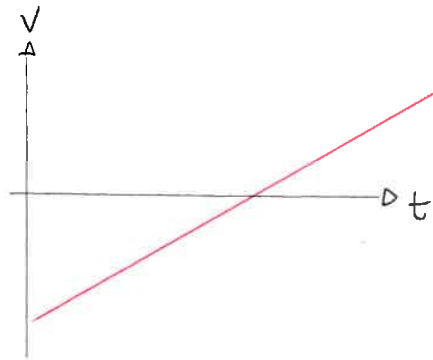
Acceleration = rate of change of velocity with respect to time

with formal definition

| | | |
|---|---|--|
| time t_i | time t_f | The average acceleration over an interval from t_i to t_f is: |
|  |  | |
| velocity v_i "initial" | velocity v_f "final" | $a_{\text{avg}} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i}$ |

units:
 m/s^2

Consider the moving man demo.



graph \Rightarrow velocity increases at a constant rate.

| time t | velocity v |
|-------------|-----------------|
| 0.0s | -4.0m/s |
| 1.0s | -2.0m/s |
| 2.0s | 0.0m/s |
| 3.0s | 2.0m/s |
| 4.0s | 4.0m/s |

data \Rightarrow velocity increases by 2.0m/s every 1.0s.

$$\Rightarrow \text{acceleration} = \frac{2.0\text{m/s}}{1.0\text{s}} = 2.0\text{m/s}^2$$

Warm Up 1

Note: 1) acceleration describes how velocity changes with time and does not give complete information about velocity at any single instant.

Quiz 1

There is no direct correlation between larger velocity and larger acceleration. The moving man demo illustrates this. The acceleration is the same but the velocity is constantly changing.

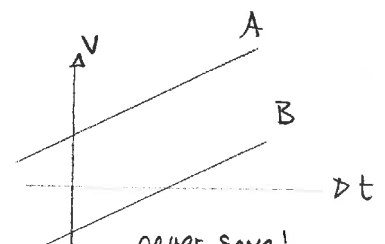
2) Acceleration is not immediately related to speed. We can see that at 1.0s and 3.0s the speeds of the man are the same. But his acceleration is non-zero.

Warm Up 2

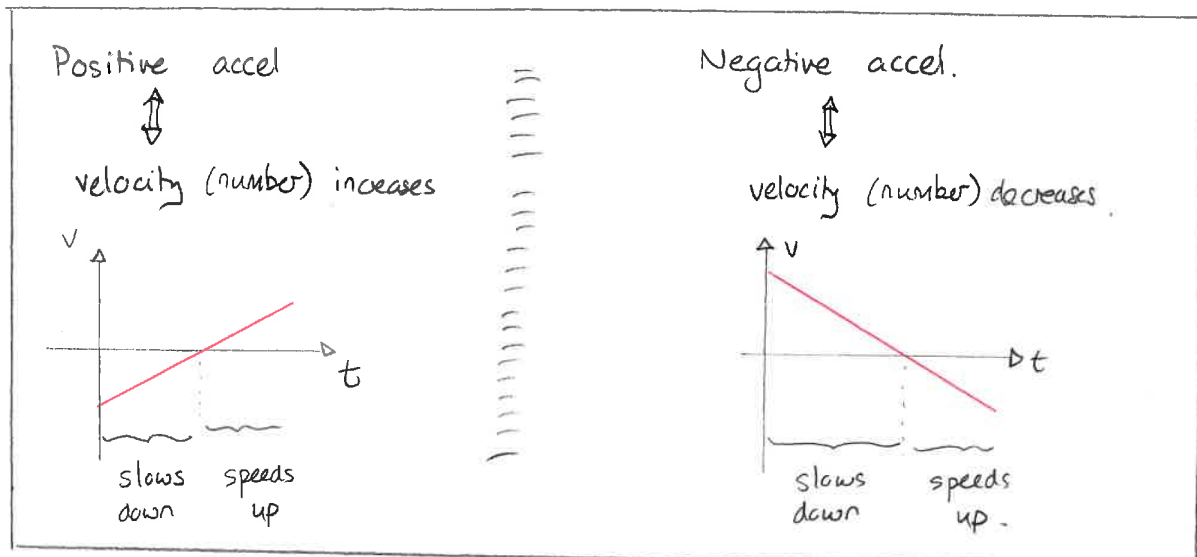
Demo: Moving Man:

A) $v = 4\text{m/s}$
 $a = 2\text{m/s}^2$

vs B) $v = -4\text{m/s}$
 $a = 2\text{m/s}^2$



Additionally acceleration can be positive or negative. The sign of acceleration only describes how velocity changes.



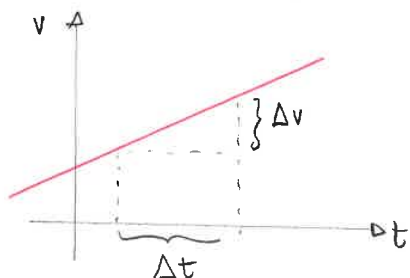
Quiz 2

Quiz 3

Demo. Moving Man demo

Motion with constant acceleration

Most of these examples have illustrated motion with constant acceleration. In these cases a graph of velocity vs time gives a straight line and



Acceleration = slope of velocity vs time graph

Additionally, it is exactly true that $a = \frac{\Delta v}{\Delta t}$

Thus

$$\Delta v = a \Delta t$$

$$\Rightarrow \boxed{v_f = v_i + a \Delta t}$$

Constant acceleration
only