

Fundamental Mechanics: Quiz 11

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Name: Taylor Lourenco

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Formulae:

$$\Delta s = r\Delta\theta \quad \omega = \frac{d\theta}{dt} \quad \alpha = \frac{d\omega}{dt} \quad a_t = \alpha r \quad v_t = \omega r$$

$$\Delta\theta = \omega_i \Delta t + \frac{1}{2} \alpha (\Delta t)^2 \quad \omega_f = \omega_i + \alpha \Delta t \quad \omega_f^2 = \omega_i^2 + 2\alpha \Delta\theta$$

$$\tau = rF \sin \phi \quad \tau_{\text{net}} = I\alpha \quad K_{\text{trans}} = \frac{1}{2} mv^2 \quad K_{\text{rot}} = \frac{1}{2} I\omega^2$$

$$I = \sum_i m_i r_i^2 \quad (\text{point masses}) \quad I = MR^2 \quad (\text{hoop}) \quad I = \frac{1}{2} MR^2 \quad (\text{disk})$$

A 4.0 kg solid disk with radius 0.40 m rotates counterclockwise about an axle through its center with angular velocity 50 rad/s. Subsequently a friction force acts at the edge of the disk and brings the disk to a stop in 5.0 s. Determine the magnitude of the friction force.

$$I = \frac{1}{2} m r^2 \quad R = 0.40 \text{ m} \quad M = 4.0 \text{ kg}$$

$$\tau = I\alpha$$

$$FR = I\alpha$$

$$\omega_i = 50 \text{ rad/s}$$

$$\omega_f = \omega_i + \alpha \Delta t$$

$$\omega_f = 0 \text{ rad/s}$$

$$0 = 50 \text{ rad/s} + \alpha (5.0 \text{ s})$$

$$\alpha = -10 \text{ rad/s}^2$$

$$-50 \text{ rad/s} = \alpha (5.0 \text{ s})$$

$$\alpha = -10 \text{ rad/s}^2$$

$$\tau = I\alpha$$

$$FR = \left(\frac{1}{2} m r^2\right) \alpha$$

$$F = \frac{1}{R} \left(\frac{1}{2} m r^2\right) \alpha$$

$$F = \frac{1}{(0.40 \text{ m})} \left(\frac{1}{2} (4.0 \text{ kg}) (0.40 \text{ m})^2\right) (-10 \text{ rad/s}^2)$$

$$F = 2.5 \text{ m} (0.32 \text{ kg} \cdot \text{m}^2) (-10 \text{ rad/s}^2)$$

$$F = -8 \text{ N}$$

Magnitude of
force ; $F = 8 \text{ N}$