



Memory Hierarchy

CS:APP 6.2-6.3

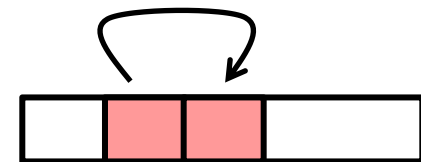
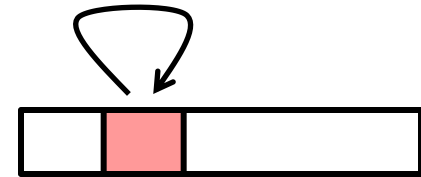
These slides adapted from materials provided by the textbook authors.

Memory Hierarchy

- Storage technologies and trends
- **Locality of reference**
- Caching in the memory hierarchy

Locality

- **Principle of Locality:** Programs tend to use data and instructions with addresses near or equal to those they have used recently
- **Temporal locality:**
 - Recently referenced items are likely to be referenced again in the near future
- **Spatial locality:**
 - Items with nearby addresses tend to be referenced close together in time



Locality Example

```
sum = 0;  
for (i = 0; i < n; i++)  
    sum += a[i];  
return sum;
```

■ Data references

- Reference array elements in succession (stride-1 reference pattern).
- Reference variable `sum` each iteration.

Spatial locality

Temporal locality

■ Instruction references

- Reference instructions in sequence.
- Cycle through loop repeatedly.

Spatial locality

Temporal locality

Qualitative Estimates of Locality

- **Claim:** Being able to look at code and get a qualitative sense of its locality is a key skill for a professional programmer.
- **Question:** Does this function have good locality with respect to array *a*?

```
int sum_array_rows(int a[M][N])
{
    int i, j, sum = 0;

    for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            sum += a[i][j];
    return sum;
}
```

Locality Example

- **Question:** Does this function have good locality with respect to array *a*?

```
int sum_array_cols(int a[M][N])
{
    int i, j, sum = 0;

    for (j = 0; j < N; j++)
        for (i = 0; i < M; i++)
            sum += a[i][j];
    return sum;
}
```

Locality Example

- **Question:** Can you permute the loops so that the function scans the 3-d array `a` with a stride-1 reference pattern (and thus has good spatial locality)?

```
int sum_array_3d(int a[M][N][N])
{
    int i, j, k, sum = 0;

    for (j = 0; j < N; j++)
        for (k = 0; k < N; k++)
            for (i = 0; i < M; i++)
                sum += a[i][j][k];

    return sum;
}
```

Memory Hierarchies

- **Some fundamental and enduring properties of hardware and software:**
 - Fast storage technologies cost more per byte, have less capacity, and require more power (heat!).
 - The gap between CPU and main memory speed is widening.
 - Well-written programs tend to exhibit good locality.
- **These fundamental properties complement each other beautifully.**
- **They suggest an approach for organizing memory and storage systems known as a **memory hierarchy**.**