

Sections			
Data Science Lifecycle, Python And Pandas .	2	Covariance And Correlation, Independence	
1.0.1 Piazza	$\frac{-}{2}$	- Sampling	17
1.0.2 Lectures	2	8.0.1 Piazza	17
1.0.3 Assignments	3	8.0.2 Lectures	17
1.0.4 Quiz	3	8.0.3 Assignments	17
1.0.5 Concept Summary	3	8.0.4 Quiz	17
Pandas, Exploring And Cleaning Tabular		8.0.5 Concept Summary	17
Data	5	CLT And Hypothesis Testing	19
2.0.1 Piazza	5	9.0.1 Piazza	19
2.0.2 Lectures	5	9.0.2 Lectures $\dots$	19
2.0.3 Assignments	5	9.0.3 Assignments	19
2.0.4 Quiz	5	9.0.4 Concept Summary	19
2.0.5 Concept Summary	5	Exam 2	22
Exploratory Data Analysis And Visualization		10.0.1 Piazza	22
7		10.0.2 Lectures	22
3.0.1 Piazza	7	10.0.3 Quiz	22
3.0.2 Lectures	7	10.0.4 Exam	22
3.0.3 Assignments	7	Confidence Intervals	23
3.0.4 Quiz	7	11.0.1 Piazza	23
3.0.5 Concept Summary	7	11.0.2 Lectures	23
Visualization And Introduction To Probability		11.0.3 Assignments	23
9	0	11.0.4 Confidence Intervals	23
4.0.1 Piazza	9 9	Intro To Modeling And Loss Models: Sim-	
4.0.2 Lectures	9	ple Linear Regression	25
4.0.3 Assignments	9	12.0.1 Piazza	25
4.0.4 Quiz 4.0.5 Concept Summary	9	12.0.2 Lectures	25
Probability: Independence, Simulation,	Э	12.0.3 Assignments	25
Random Variables	11	12.0.4 Concept Summary	25
5.0.1 Piazza	11	Multiple Linear Regression And Feature	
5.0.2 Lectures	11	Engineering	<b>27</b>
5.0.3 Assignments	11	13.0.1 Piazza	27
5.0.4 Quiz	11	13.0.2 Lectures	27
5.0.5 Concept Summary	11	13.0.3 Assignments	27
Exam 1	14	13.0.4 Quiz	27
6.0.1 Piazza	14	13.0.5 Concept Summary	27
6.0.2 Lectures	14	Influence In Multiple Linear Regression	<b>30</b>
6.0.3 Quiz	14	14.0.1 Piazza	30
Expected Value, Variance - Discrete And		14.0.2 Lectures	30
Continuous RV	<b>15</b>	14.0.3 Assignments	30
7.0.1 Piazza	15	14.0.4 Concept Summary	30
7.0.2 Lectures	15	Final Project	32
7.0.3 Assignments	15	15.0.1 Piazza	32
7.0.4 Concept Summary	15	15.0.2 Assignments	32

Week 1: (1/15 - 1/21)

# Data Science Lifecycle, Python And Pandas

### 1.0.1 Piazza

Must post / respond to two Piazza posts. (1/23/24)

### 1.0.2 Lectures

The lecture videos for this week are:

• Course Overview  $\approx 54$  min.

- Pandas Part  $1 \approx 54$  min.
- Pandas Part  $2 \approx 54$  min.
- Python Walkthrough  $\approx 47$  min.
- Learning to Use Jupyter Notebooks  $\approx 9$  min.
- Using Markdown In Jupyter Notebooks  $\approx 11$  min.
- Writing Mathematics In Jupyter Notebooks  $\approx 16$  min.
- Beginning Python  $\approx 44$  min.
- Python Basic NumPy  $\approx 18$  min.
- Quick Calculus Refresher  $\approx 21$  min.

The lecture notes for this week are:

- Course Overview Data Science Lifecycle
- Pandas Part 1
- Pandas Part 2
- LATEX

### 1.0.3 Assignments

The assignment for this week is:

• The assignment for this week is **Data Science Lifecycle**, **Python And Pandas**. (1/23/24)

### 1.0.4 Quiz

The quizzes for this week are:

• Math Concept Quiz • Finalized Math Concept Quiz (1/30/24)

### 1.0.5 Concept Summary

The concept that is being explored this week is The Data Science Lifecycle.

### The Data Science Lifecycle

### Overview

The Data Science Lifecycle provides a systematic approach to managing data science projects. This structured methodology ensures that projects progress efficiently from conception through to deployment, facilitating the transformation of raw data into actionable insights. It is designed to align data science projects with business objectives, ensuring relevance and value in the outcomes.

### Detailed Phases of the Data Science Lifecycle

Business Understanding is the cornerstone of any data science project. It involves defining the objectives and scope of the project in alignment with business goals. This phase requires intensive discussions with stakeholders to pinpoint the critical questions that the project should address and to

establish clear success metrics.

### Data Acquisition and Understanding

- Data Collection: Gathering data from a variety of sources including databases, files, and external APIs, ensuring that the data aligns with the needs identified in the business understanding phase.
- Data Exploration: Applying statistical methods to gain insights into the data, understand its structure, and uncover any underlying patterns or anomalies.
- Data Quality Assessment: Identifying and addressing issues related to data quality such as missing values or inconsistent formats, which are critical for the next stages of the lifecycle.

Data Preparation involves cleaning and transforming the data. This stage is pivotal as it prepares the data for effective analysis by addressing any quality issues identified previously, normalizing data formats, and engineering features that will be used in modeling.

Modeling is at the heart of the data science lifecycle where theoretical models are turned into practical tools:

- **Model Selection**: Choosing appropriate algorithms that best fit the business problem, data characteristics, and expected outcomes.
- Model Training: Fitting models to the data, adjusting parameters to improve their accuracy and effectiveness.
- Model Validation: Rigorously testing models to ensure they perform well against predefined metrics and real-world scenarios.

### **Evaluation**

Evaluation involves assessing whether the models meet the business objectives set in the initial phase. This includes reviewing the model outputs in detail and ensuring that they provide the insights needed to make informed business decisions.

### Deployment

Deployment marks the integration of the model into the business environment where it can start providing value by generating actionable insights. This stage also includes setting up mechanisms for monitoring the model's performance and establishing processes for ongoing maintenance.

The lifecycle is characterized by a Feedback Loop, which involves continual monitoring and refining of the models based on feedback and new data. This ensures that the models remain relevant and perform optimally over time.

### Summary

The Data Science Lifecycle is critical for ensuring that data science projects deliver maximum value by aligning closely with business objectives and adapting to new data and insights. This structured approach aids organizations in navigating the complexities of data-driven decision-making, fostering a culture of continuous improvement and innovation.

### Week 2: (1/22 - 1/28)



### Pandas, Exploring And Cleaning Tabular Data

### 2.0.1 Piazza

Must post / respond to two Piazza posts. (1/30/24)

#### 2.0.2 Lectures

The lecture videos for this week are:

- Pandas Part  $3 \approx 54$  min.
- Pandas Part  $4 \approx 54$  min.
- Discussion 2 Video Walkthrough: Basics with Pandas and In-Depth with NumPy  $\approx 73$  min.

The lecture notes for this week are:

- Pandas Part 3
- Pandas Part 4
- Permutations And Combinations
- Section 7.1 Intro To Discrete Probability
- Section 7.2 Probability Theory And Applications

### 2.0.3 Assignments

The assignment for this week is:

• The assignment for this week is Pandas, Exploring And Cleaning Tabular Data. (1/30/24)

### 2.0.4 Quiz

The quizzes for this week are:

• Python And Pandas Quiz • Finalized Python And Pandas Quiz (1/30/24)

### 2.0.5 Concept Summary

The concept that is being summarized this week is **Pandas**, **Exploring And Cleaning Tabular Data**.

### Pandas, Exploring And Cleaning Tabular Data

### Overview

Pandas is a powerful Python library used for data manipulation and analysis, particularly suited for working with tabular data. It provides robust tools for cleaning, transforming, and analyzing data

efficiently, making it indispensable in the data science toolkit. The ability to handle large datasets with ease and integrate smoothly with other data analysis libraries makes pandas a cornerstone for data exploration and preprocessing tasks.

### Detailed Phases of Exploring and Cleaning Data with Pandas

Data Exploration is an essential first step in understanding the structure and quality of the dataset. Pandas provides numerous functions to facilitate this process:

- Reading Data: Pandas can read data from various formats like CSV, Excel, JSON, SQL databases, and more, allowing for easy ingestion of data into Python environments.
- Viewing Data: Functions like head(), tail(), and describe() give a quick overview of the data, displaying the first and last rows and summarizing the statistical attributes of numerical columns.
- Data Profiling: This involves more comprehensive analysis using methods such as info() and describe() to assess data types, non-null values, and other attributes that indicate data quality and completeness.

Data Cleaning with pandas is critical for preparing data for analysis:

- Handling Missing Values: Pandas provides several methods to detect, remove, or fill missing values, such as isnull(), dropna(), and fillna().
- Data Transformation: This includes operations like merging, joining, or reshaping data. Functions like merge(), concat(), and pivot() are extensively used to modify data structures and prepare datasets for analysis.
- Filtering and Sorting Data: Pandas enables filtering and sorting of data based on conditions, which is crucial for narrowing down data to relevant subsets for specific analyses, using loc(), iloc(), and sort\_values().

#### Advanced Features

Beyond basic cleaning and exploration, pandas also offers advanced features that enhance its functionality:

- **Time Series Analysis**: Pandas has built-in support for date and time data types and time series functionalities, which are essential for analyzing chronological data.
- **High-Performance Operations**: With tools like **groupby()** for grouping large data sets and **apply()** for applying functions to data frames, pandas supports complex operations that are highly performant on large datasets.

### Summary

The use of pandas for exploring and cleaning tabular data is pivotal in data science. It streamlines the process of data preparation, allowing for more efficient and accurate analysis. By providing a rich set of tools for dealing with diverse data types and structures, pandas not only simplifies data manipulation but also enhances the overall data analysis workflow, promoting a culture of data-driven decision-making.

### Week 3: (1/29 - 2/4)



### Exploratory Data Analysis And Visualization

### 3.0.1 Piazza

Must post / respond to two Piazza posts. (2/6/24)

#### 3.0.2 Lectures

The lecture videos for this week are:

- Lecture 6: Data Wrangling And EDA  $\approx 54$  min.
- Lecture 7: EDA And Visualization  $\approx 54$  min.
- Lecture 8: Quiz Walkthrough And Visualization  $\approx 54$  min.
- Discussion 3: More With Pandas  $\approx 50$  min.

The lecture notes for this week are:

- Pandas Part 4
- Exploratory Data Analysis
- Visualization

#### 3.0.3 Assignments

The assignment for this week is:

• The assignment for this week is Exploratory Data Analysis And Visualization. (2/6/24)

### 3.0.4 Quiz

The quizzes for this week are:

• Math And Pandas Quiz • Finalized Math And Pandas Quiz (2/6/24)

### 3.0.5 Concept Summary

The concept that is being covered this week is Exploratory Data Analysis And Visualization.

### Exploratory Data Analysis And Visualization

#### Overview

Exploratory Data Analysis (EDA) and Visualization are critical components of the data science process, providing a means to 'look under the hood' of the dataset. EDA is a philosophy of understanding and breaking down data using simple summary statistics and graphical representations. Visualization complements this by offering a visual context that can reveal hidden patterns, trends, and anomalies that might not be apparent from raw data alone. Together, these practices help in

making informed hypotheses and decisions about the dataset before moving on to more complex analyses.

### Detailed Phases of Exploratory Data Analysis and Visualization

Understanding the Data forms the foundation of EDA. It involves:

- Summary Statistics: Utilizing measures like mean, median, mode, variance, and standard deviation to gain insights into the data distribution.
- Correlation Analysis: Assessing relationships between variables using correlation coefficients to understand how variables interact with each other.

Data visualization then takes these insights and translates them into a graphical context:

- Graphical Techniques: Using plots and charts, such as histograms, box plots, scatter plots, and bar charts to visually summarize the distribution and relationships of the data.
- Interactive Visualizations: Leveraging advanced visualization tools to create dynamic plots that allow users to manipulate and explore data in real-time, enhancing the interactive analysis experience.

Identifying Patterns and Anomalies is a key outcome of EDA and visualization. This involves detecting outliers, gaps, and clusters within the data, which can be crucial for predictive modeling and decision-making.

#### **Data Visualization Tools**

A variety of tools facilitate EDA and visualization:

- **Programming Tools**: Libraries such as Matplotlib, Seaborn, and Plotly in Python offer robust capabilities for creating a wide range of static and interactive visualizations.
- Business Intelligence Tools: Platforms like Tableau, Power BI, and Qlik provide user-friendly interfaces for creating dashboards and reports that are accessible to users without a programming background.

### Summary

Exploratory Data Analysis and Visualization are indispensable for a deep understanding of the underlying data, enabling data scientists to extract meaningful patterns and insights that guide further analysis and modeling. By integrating statistical analysis with visual storytelling, these practices foster a comprehensive approach to data interpretation, ensuring that subsequent analyses are well-informed and grounded in the actual data characteristics.

### Week 4: (2/5 - 2/11)



### Visualization And Introduction To Probability

### 4.0.1 Piazza

Must post / respond to two Piazza posts. (2/13/24)

### 4.0.2 Lectures

The lecture videos for this week are:

- Visualization and Introduction to Probability  $\approx 54$  min.
- Probability Part  $1 \approx 54$  min.
- Quiz Walkthrough; Probability  $\approx 54$  min.
- Bike Sharing EDA and Visualization  $\approx 49$  min.

The lecture notes for this week are:

- Intro To Probability Lecture Notes
- Probability II Total Probability, Bayes Rule And Independence Lecture Notes

### 4.0.3 Assignments

The assignment for this week is:

• The assignment for this week is Visualization And Introduction To Probability. (2/13/24)

### 4.0.4 Quiz

The quizzes for this week are:

• Quiz 4 • Finalized Quiz 4 (2/13/24)

### 4.0.5 Concept Summary

The concept that is being covered this week is Visualization And Introduction To Probability.

### Visualization And Introduction To Probability

#### Overview

Visualization and an Introduction to Probability are fundamental concepts in data science, essential for both understanding data distributions and predicting future events. Visualization serves as a powerful tool for representing data graphically, aiding in the intuitive comprehension of complex relationships and trends. Concurrently, probability theory provides the mathematical framework necessary for quantifying the likelihood of various outcomes, enabling more informed decision-making

based on data analysis.

### **Key Concepts in Visualization**

Visualization is pivotal in data exploration, as it transforms abstract numbers into visual objects that the human brain can easily interpret. Effective visualization techniques include:

- Choosing the Right Type of Visualization: Depending on the nature of the data and the questions being addressed, different charts such as line graphs, bar charts, and pie charts are used.
- **Design Principles**: Good visualizations adhere to design principles that enhance readability and comprehension, such as appropriate color schemes, minimalistic designs, and clear labeling.

Visual tools not only help in identifying patterns, trends, and outliers but also facilitate the presentation of findings to non-technical stakeholders, making the data actionable.

### Introduction to Probability

Probability theory is a branch of mathematics concerned with the analysis of random phenomena. The core elements include:

- **Probability Basics**: Concepts such as random experiments, outcomes, sample spaces, and events, along with the rules for computing probabilities.
- Conditional Probability and Independence: Understanding how the probability of events changes in relation to the occurrence of other events.

Probability plays a crucial role in modeling and predicting outcomes, which is fundamental in fields ranging from business analytics to artificial intelligence.

### Combining Visualization with Probability

Integrating visualization with probability theory enhances analytical capabilities:

- Visualizing Probabilities: Graphical representations such as probability trees and Venn diagrams help in visualizing complex probabilistic relationships.
- Statistical Plots: Histograms and scatter plots are used to depict and analyze the distribution of data, facilitating the understanding of probability densities and relationships among variables.

### Summary

Visualization and probability are intertwined disciplines that significantly empower data scientists to extract, analyze, and communicate insights from data. Visualization aids in making the abstract tangible, while probability provides the means to anticipate and quantify the uncertainty inherent in real-world data. Together, they form a robust toolkit for tackling the challenges of data-driven decision-making in a probabilistic world.

### Week 5: (2/12 - 2/18)



# angleProbability: Independence, Simulation, Random Variables

### 5.0.1 Piazza

Must post / respond to two Piazza posts. (2/20/24)

### 5.0.2 Lectures

The lecture videos for this week are:

- Probability Cont. Independence And Simulation  $\approx 54$  min.
- Probability Cont. Independence And Simulation Jupyter Notebook Examples  $\approx 27$  min.
- Random Simulation Example  $\approx 45$  min.
- Independence Cont. Discrete Random Variables  $\approx 54$  min.
- Quiz Walkthrough, Common Discrete RVs, Expectation ≈ 54 min.

The lecture notes for this week are:

- Independence Lecture Notes
- Discrete Random Variables Lecture Notes
- Expected Value And Variance Lecture Notes

### 5.0.3 Assignments

The assignment for this week is:

• The assignment for this week is **Probability: Independence, Simulation, Random Variables**. (2/20/24)

### 5.0.4 Quiz

The quizzes for this week are:

Quiz 5 • Finalized Quiz 5 (2/20/24)

### 5.0.5 Concept Summary

The concept that is being covered this week is **Probability: Independence**, **Simulation**, **Random Variables**.

Probability: Independence, Simulation, Random Variables

### Overview

Probability is a fundamental concept in statistics that helps in quantifying the likelihood of events and understanding random phenomena. Key areas within probability that significantly enhance the understanding and application of statistical methods include Independence, Simulation, and Random Variables. These concepts allow for robust modeling of complex systems, predictive analytics, and decision-making under uncertainty.

### Independence in Probability

Independence is a critical concept in probability that occurs when the occurrence of one event does not affect the occurrence of another. This principle is foundational in:

- Simplifying Probability Calculations: Independent events allow the probability of joint occurrences to be calculated as the product of their individual probabilities.
- Statistical Inference: Independence is assumed in many statistical tests and models to ensure valid results.

Understanding and identifying independence among events or variables are essential for accurate model building and analysis.

### Simulation Techniques

Simulation involves using random sampling techniques to model and study complex systems when analytic solutions are infeasible:

- Monte Carlo Simulations: These are used to approximate the probability of complex events by simulating random samples and observing the proportion of outcomes that satisfy the event condition.
- **Bootstrapping**: A method for estimating statistical measures by sampling with replacement from data, allowing assessment of variability in statistical estimates.

Simulation provides a powerful tool for prediction and estimation in scenarios where traditional methods are limited or impractical.

### Random Variables

A random variable is a variable whose possible values are numerical outcomes of a random phenomenon. There are two main types of random variables:

- **Discrete Random Variables**: These take on a countable number of distinct values. Examples include binomial and Poisson distributions.
- Continuous Random Variables: These take on an infinite number of possible values, typically measurements, and are described by probability density functions. Examples include normal and exponential distributions.

Random variables are central to probability theory as they formalize the way to represent and analyze randomness and uncertainty in a quantitative manner.

### Summary

The concepts of Independence, Simulation, and Random Variables are integral to understanding and applying probability in various fields such as finance, engineering, and science. They provide the tools to model uncertainty, make predictions, and infer properties about larger populations based on sample data. Mastery of these topics is crucial for anyone looking to deepen their understanding of probability and statistics.



### Week 6: (2/19 - 2/25)



### Exam 1

### 6.0.1 Piazza

Must post / respond to two Piazza posts. (2/27/24)

### 6.0.2 Lectures

The lecture videos for this week are:

• Expected Value, Variance, Discrete And Continuous RV  $\approx 54$  min.

The lecture notes for this week are:

• Expected Value, Variance Discrete And Continuous RV Lecture Notes

### 6.0.3 Quiz

The quizzes for this week are:

Quiz 6 • Finalized Quiz 6 (2/27/24)

### Exam

The exam for this week is:

• Exam 1 • Exam 1 (2/23/24)

### Week 7: (2/26 - 3/3)



# Expected Value, Variance - Discrete And Continuous RV

### 7.0.1 Piazza

Must post / respond to two Piazza posts. (3/5/24)

#### 7.0.2 Lectures

The lecture videos for this week are:

- Random Variables And Distributions Notebook Walkthrough  $\approx 83$  min.
- RV And Distributions, Expectation And Variance  $\approx 54$  min.
- Joint Distributions, Covariance, Independence  $\approx 54$  min.
- Covariance And Correlation, Independence  $\approx 54$  min.

The lecture notes for this week are:

- Expected Value, Variance Discrete And Continuous RV Lecture Notes
- More With RV Discrete Vs. Continuous Expected Value And Variance Lecture Notes
- Joint Distributions Covariance And Correlation Lecture Notes
- Sampling Lecture Notes

### 7.0.3 Assignments

The assignment for this week is:

• The assignment for this week is **Expected Value**, **Variance - Discrete And Continuous RV**. (3/5/24)

### 7.0.4 Concept Summary

### Expected Value, Variance - Discrete And Continuous RV

#### Overview

Expected Value and Variance are fundamental statistical measures that describe the distribution of random variables (RVs). They play crucial roles in the fields of probability, statistics, and many practical applications like finance and risk management. Expected value provides a measure of the central tendency of a random variable, while variance measures the spread or dispersion around this central value. Understanding these concepts for both discrete and continuous random variables allows

for deeper insights into the behavior of random processes and decision-making under uncertainty.

### **Expected Value**

The Expected Value (EV) of a random variable gives a sense of the 'average' outcome one might expect if an experiment were repeated many times:

- Discrete Random Variables: The expected value is calculated by summing the products of each possible value of the random variable and its corresponding probability. It is denoted as  $E(X) = \sum_{i=1}^{n} x_i p_i$ , where  $x_i$  are the possible values and  $p_i$  their probabilities.
- Continuous Random Variables: For continuous variables, the expected value is determined by integrating the product of the variable's values and their probability density function (PDF) over the possible range of values. It is expressed as  $E(X) = \int_{-\infty}^{\infty} x f(x) dx$ , where f(x) is the PDF.

#### Variance

Variance quantifies the variability or spread of a random variable's possible outcomes around its expected value:

- Discrete Random Variables: Variance is calculated by summing the squared differences between each possible value and the expected value, each weighted by its probability:  $Var(X) = \sum_{i=1}^{n} (x_i E(X))^2 p_i$ .
- Continuous Random Variables: Similar to the discrete case, but involving integration:  $Var(X) = \int_{-\infty}^{\infty} (x E(X))^2 f(x) dx$ .

Both expected value and variance are essential for understanding the distribution characteristics of random variables, influencing everything from risk assessment to optimization in various applications.

### Summary

Expected Value and Variance are critical in both theoretical and applied statistics, providing key insights into the likelihood and variability of outcomes for discrete and continuous random variables. These measures help statisticians and data scientists to predict outcomes and make informed decisions based on the underlying probabilities. Understanding these concepts is fundamental for analyzing risk, optimizing strategies, and modeling in uncertain environments.

### Week 8: (3/4 - 3/10)



# Covariance And Correlation, Independence - Sampling

### 8.0.1 Piazza

Must post / respond to two Piazza posts. (3/12/24)

### 8.0.2 Lectures

The lecture videos for this week are:

- Sampling  $\approx 54$  min.
- Central Limit Theorem  $\approx 54$  min.
- Hypothesis Testing  $\approx 54$  min.

The lecture notes for this week are:

- Sampling Lecture Notes
- Sample Statistics and The Central Limit Theorem Lecture Notes
- Hypothesis Testing Lecture Notes

### 8.0.3 Assignments

The assignment for this week is:

• The assignment for this week is Covariance And Correlation, Independence - Sampling. (3/12/24)

### 8.0.4 Quiz

The quizzes for this week are:

Quiz 7 • Finalized Quiz 7 (3/12/24)

### 8.0.5 Concept Summary

The concept that is being covered this week is Covariance And Correlation, Independence - Sampling.

### Covariance And Correlation, Independence - Sampling

### Overview

Covariance and correlation are essential statistical tools used to measure how much two random variables change together, thus providing insights into their relationship. On the other hand, independence in sampling is crucial in ensuring that statistical inferences made from data are valid and

reliable. Understanding these concepts allows analysts to explore relationships within data accurately and to make predictions based on these relationships.

### **Understanding Covariance and Correlation**

Covariance is a measure used to determine the extent to which two variables change in tandem:

- Positive Covariance: Indicates that two variables tend to increase or decrease together.
- Negative Covariance: Suggests that one variable increases when the other decreases.
- Zero Covariance: Implies no detectable linear relationship between the variables.

Covariance provides a preliminary insight into the relationship between variables, but it does not normalize these relationships, which can make comparisons across different datasets difficult.

Correlation, on the other hand, takes covariance and scales it by the standard deviations of the respective variables, thus producing a dimensionless quantity that makes comparison between variables straightforward:

- Correlation Coefficient (Pearson's r): Values range from -1 to 1. A correlation of 1 means a perfect positive linear relationship, -1 means a perfect negative linear relationship, and 0 means no linear relationship exists.
- Spearman's Rank Correlation: Used for measuring the relationship between ranked variables. It can be more appropriate than Pearson's correlation when dealing with non-linear data.

Correlation coefficients are widely utilized in the fields of finance, meteorology, psychology, and other sciences to validate theories, test hypotheses, and build models that depend on the interrelationships between variables.

### Independence in Sampling

Independence in sampling is pivotal for the integrity of statistical analysis:

- Principle of Independence: States that the outcome of one sample should not affect the outcome of another. This principle is vital for methods such as hypothesis testing and regression modeling, where the validity of results depends on the assumption that all observations are obtained independently.
- Achieving Independence: Methods such as simple random sampling and stratified sampling help achieve independence. These methods ensure that each individual observation is selected without bias and does not influence the selection of other observations.

Dependence, the opposite of independence, can lead to skewed results and biased conclusions if not properly managed, especially in complex models such as time series analysis where past values might influence future values.

### Summary

The study of covariance and correlation alongside the practice of ensuring independence in sampling are crucial in the accurate analysis of data. Covariance and correlation offer insights into the degree and nature of relationships between two variables, while independence in sampling underpins the reliability of statistical inferences made from data sets. Together, these concepts form the bedrock of statistical analysis, supporting rigorous data exploration, hypothesis testing, and predictive modeling.

### Week 9: (3/11 - 3/17)



## CLT And Hypothesis Testing

### 9.0.1 Piazza

Must post / respond to two Piazza posts. (3/19/24)

### 9.0.2 Lectures

The lecture videos for this week are:

- Hypothesis Testing  $\approx 54$  min.
- Testing Hypothesis And The Central Limit Theorem Walkthrough  $\approx 63$  min.
- A/B Testing  $\approx 54$  min.
- A/B Testing Walkthrough  $\approx 33$  min.
- Errors In Hypothesis Testing  $\approx 54$  min.

The lecture notes for this week are:

- Hypothesis Testing Lecture Notes
- AB Testing, Randomized Control Tests And Causality Lecture Notes
- Errors in Hypothesis Testing, PHacking Lecture Notes

### 9.0.3 Assignments

The assignment for this week is:

• The assignment for this week is CLT And Hypothesis Testing. (3/19/24)

### 9.0.4 Concept Summary

The concept that is being covered this week is CLT And Hypothesis Testing.

### **CLT And Hypothesis Testing**

#### Overview

The Central Limit Theorem (CLT) and Hypothesis Testing are foundational concepts in statistics, crucial for making inferences about populations from sample data. The CLT provides the theoretical backbone for understanding how sample means behave, especially with large sample sizes, while hypothesis testing is a methodological framework used to make decisions and test claims about population parameters based on sample statistics. Understanding both concepts allows statisticians

to perform reliable and robust statistical analyses.

#### Central Limit Theorem

The Central Limit Theorem is a fundamental principle in probability theory that explains why the normal distribution arises so commonly and why it is generally applicable in statistical methodologies:

- Statement of CLT: It states that the distribution of the sample means will approximate a normal distribution, regardless of the shape of the population distribution, as long as the sample size is sufficiently large (usually n > 30).
- Implications: This theorem allows for the simplification of analysis in many statistical applications because it justifies the use of the normal probability model in the sampling distribution of the mean. This is particularly useful for inferential statistics where exact distributions are unknown.

### Hypothesis Testing

Hypothesis Testing is a systematic method used to evaluate assumptions (hypotheses) about a parameter in a given population:

### • Steps in Hypothesis Testing:

- 1. Formulation of Null (H0) and Alternative (H1) Hypotheses: The null hypothesis typically represents a theory that there is no effect or no difference, and the alternative is what the researcher aims to prove.
- 2. Selection of a Significance Level ( $\alpha$ ): Commonly set at 0.05, this is the threshold for deciding whether to reject the null hypothesis.
- 3. Calculation of Test Statistic: Based on the sample data, calculate a statistic that is appropriate for the test (e.g., t-statistic for a t-test).
- 4. Determination of the P-value or Critical Value: Compare the calculated statistic to a critical value derived from an appropriate distribution.
- 5. Decision: Reject or fail to reject the null hypothesis based on the comparison between the P-value and the significance level.
- Types of Errors: Understanding Type I (false positive) and Type II (false negative) errors is critical in hypothesis testing. These errors reflect the probabilities of incorrectly rejecting a true null hypothesis or failing to reject a false null hypothesis, respectively.

### Combining CLT and Hypothesis Testing

Integrating the Central Limit Theorem with Hypothesis Testing provides a powerful approach to statistical inference:

- By assuming the normal distribution of the sample mean, as justified by the CLT, statisticians can apply hypothesis testing even when the population standard deviation is unknown, using the sample standard deviation as an estimate.
- This integration simplifies the calculation of test statistics under the normality assumption, enhancing the accuracy and reliability of hypothesis tests.

### Summary

The Central Limit Theorem and Hypothesis Testing are indispensable tools in the field of statistics, enabling practitioners to make precise inferences about population parameters from sample data. These concepts are not only theoretical but also immensely practical, forming the basis for data analysis across scientific research, business analytics, and many other domains.



### Week 10: (3/18 - 3/24)



### Exam 2

### 10.0.1 Piazza

Must post / respond to two Piazza posts. (3/26/24)

### 10.0.2 Lectures

The lecture videos for this week are:

- Confidence Intervals And The Bootstrap  $\approx 54$  min.
- Quiz 9 Walktrhough  $\approx 16$  min.

The lecture notes for this week are:

• Confidence Intervals And The Bootstrap Lecture Notes

### 10.0.3 Quiz

The quizzes for this week are:

• Quiz 8 • Finalized Quiz 8 (4/9/24)

### 10.0.4 Exam

The exam for this week is:

- Practice Exam 2 (3/22/24)
- Exam 2 Exam 2 (3/22/24)

### Week 11: (4/1 - 4/7)



### Confidence Intervals

### 11.0.1 Piazza

Must post / respond to two Piazza posts. (4/9/24)

### 11.0.2 Lectures

The lecture videos for this week are:

- Interpretting Confidence Intervals  $\approx 54$  min.
- Confidence Intervals And Designing Experiments  $\approx 54$  min.
- Modeling  $\approx 54$  min.
- Climate Change Notebook  $\approx 44$  min.

The lecture notes for this week are:

- Confidence Interval Guide Lecture Notes
- Interpreting Confidence Intervals Lecture Notes
- Confidence Intervals And Designing Experiments Lecture Notes
- Introduction To Modeling Lecture Notes

### 11.0.3 Assignments

The assignment for this week is:

• The assignment for this week is Confidence Intervals. (4/9/24)

### 11.0.4 Confidence Intervals

The concept that is being covered this week is **Confidence Intervals**.

### Confidence Intervals

#### Overview

Confidence intervals (CIs) are a fundamental statistical tool used to estimate the range within which a population parameter is likely to lie based on sample data. These intervals provide a measure of the uncertainty associated with sampling variability and offer a range of values that are believed to cover the true parameter with a certain level of confidence, typically expressed as 90%, 95%, or 99%. Understanding and using confidence intervals correctly is essential for making informed decisions in

scientific research, business analytics, and policy making.

### Construction of Confidence Intervals

The process of constructing a confidence interval typically involves several key steps:

- **Determine the Sample Statistic**: Calculate a point estimate of the parameter (e.g., the sample mean or proportion) from the observed data.
- Select the Confidence Level: Choose the confidence level (e.g., 95%) which reflects the degree of certainty desired in the estimate.
- Calculate the Margin of Error: Determine the margin of error for the interval using the appropriate standard error and the critical value from the corresponding distribution (usually z or t-distribution).

### Significance and Interpretation

### Interpretation of Confidence Intervals:

- A 95% confidence interval means that if we were to take 100 different samples and compute a confidence interval for each, approximately 95 of these intervals would be expected to contain the true population parameter.
- Confidence intervals are particularly valuable in research for assessing the reliability of estimates and for comparing different studies or datasets.

### Importance of Confidence Intervals in Statistical Analysis:

- Assessing Estimate Precision: Confidence intervals provide more information than a simple point estimate, indicating the range within which the true value lies and the precision of the estimate.
- Testing Hypotheses: Confidence intervals can be used for hypothesis testing. If a confidence interval does not contain a value of interest (e.g., zero in the case of estimating differences), this can be seen as evidence against the null hypothesis that this value is true.

#### Limitations

While confidence intervals are a powerful statistical tool, they do have limitations:

- Dependence on Correct Model Assumptions: The accuracy of confidence intervals depends heavily on the correctness of the model and assumptions used in their construction, such as the assumption of normality or independence.
- Misinterpretation: Confidence intervals can be misunderstood. They do not say that the true parameter has a 95% chance of being within the interval—rather, they provide a range that is likely to capture the true parameter in 95% of samples.

### Summary

Confidence intervals are an essential part of inferential statistics, aiding in decision making by providing a range of plausible values for an unknown parameter. They enhance the understanding of data variability and help quantify the certainty of statistical estimates, thereby playing a crucial role in scientific research and quantitative analysis.

### Week 12: (4/8 - 4/14)



# $\sum$ Intro To Modeling And Loss Models: Simple Linear Regression

### 12.0.1 Piazza

Must post / respond to two Piazza posts. (4/16/24)

### 12.0.2 Lectures

The lecture videos for this week are:

- Intro To Modeling And Loss Models  $\approx 54$  min.
- Simple Linear Regression  $\approx 23$  min.
- SLR Inference  $\approx 54$  min.
- sklearn And Linear Regression  $\approx 21$  min.
- Simple And Multiple Linear Regression Walkthrough  $\approx 40$  min.

The lecture notes for this week are:

- Introduction To Modeling Lecture Notes
- Simple Linear Regression Lecture Notes
- Inference With Simple Linear Regression Lecture Notes
- Sklearn And Multiple Linear Regression Lecture Notes

### 12.0.3 Assignments

The assignment for this week is:

• The assignment for this week is Intro To Modeling And Loss Models: Simple Linear Regression. (4/16/24)

### 12.0.4 Concept Summary

The concept that is being covered this week is **Intro To Modeling And Loss Models: Simple Linear Regression**.

### Intro To Modeling And Loss Models: Simple Linear Regression

### Overview

Modeling is a fundamental aspect of statistical analysis and predictive analytics, allowing researchers and analysts to understand and predict behaviors based on observed data. Simple Linear Regression is one of the most basic forms of statistical modeling techniques used to predict an outcome variable

(dependent variable) based on one predictor variable (independent variable). It provides a clear and straightforward way to quantify the relationship between two variables and is extensively used in economics, finance, natural sciences, and social sciences.

### Principles of Simple Linear Regression

Simple Linear Regression aims to model the relationship between two variables by fitting a linear equation to observed data. The steps in building a regression model include:

- Model Formulation: Determine the dependent variable and the independent variable. The model takes the form  $Y = \beta_0 + \beta_1 X + \epsilon$ , where Y is the dependent variable, X is the independent variable,  $\beta_0$  is the y-intercept,  $\beta_1$  is the slope of the line, and  $\epsilon$  is the error term.
- Parameter Estimation: Use statistical methods, typically the method of least squares, to estimate the parameters  $\beta_0$  and  $\beta_1$  that minimize the sum of the squared difference between the observed values and the values predicted by the model.

### Assumptions of Simple Linear Regression

For the model to provide reliable predictions, several key assumptions must be satisfied:

- Linearity: The relationship between the independent and dependent variable must be linear.
- Independence: Observations must be independent of each other.
- Homoscedasticity: The variance of residual terms (differences between observed and predicted values) should be constant.
- Normality: The residuals of the model should be normally distributed.

### Loss Models in Simple Linear Regression

In the context of regression, the concept of 'loss' refers to the penalty for a bad prediction, which in this case is quantified as the error between the observed values and the values predicted by the model:

• Squared Loss Function: Simple Linear Regression typically uses the squared loss function (also known as least squares), where the loss is calculated as the square of the difference between the predicted and actual values. This method emphasizes larger errors more significantly than smaller ones, which can be particularly useful in finding a line of best fit that minimizes these errors.

#### **Evaluating Model Performance**

The performance of a simple linear regression model can be evaluated using several metrics:

- Coefficient of Determination ( $R^2$ ): Measures the proportion of the variance in the dependent variable that is predictable from the independent variable.
- **Residual Standard Error**: Measures the average amount that the response will deviate from the true regression line.

### Summary

Simple Linear Regression is a powerful tool for predictive modeling, providing valuable insights into linear relationships between variables. Understanding its principles, assumptions, and methods for evaluating its performance is crucial for effectively applying this technique in practical scenarios, ensuring that predictions are both accurate and reliable.

### Week 13: (4/15 - 4/21)



# Multiple Linear Regression And Feature Engineering

### 13.0.1 Piazza

Must post / respond to two Piazza posts. (4/23/24)

### 13.0.2 Lectures

The lecture videos for this week are:

- Multiple Linear Regression  $\approx 33$  min.
- Feature Engineering  $\approx 54$  min.
- Cross Validation  $\approx 54$  min.

The lecture notes for this week are:

- Sklearn And Multiple Linear Regression Lecture Notes
- Feature Engineering Lecture Notes
- Cross Validation Lecture Notes

### 13.0.3 Assignments

The assignment for this week is:

• The assignment for this week is **Final Project Part 1**. (4/26/24)

### 13.0.4 Quiz

The quizzes for this week are:

• Quiz 9 • Finalized Quiz 9 (4/23/24)

### 13.0.5 Concept Summary

The concept that is being covered this week is Multiple Linear Regression And Feature Engineering.

### Multiple Linear Regression And Feature Engineering

### Overview

Multiple Linear Regression (MLR) extends the concepts of simple linear regression to include more than one independent variable. This technique is used to model the relationship between a dependent variable and multiple predictors, providing a more comprehensive understanding of factors affecting the outcome. Feature Engineering is a critical process in machine learning that involves creating new input features from existing variables to improve model accuracy. MLR and feature engineering together form a powerful toolkit for predictive modeling across various fields such as economics, health sciences, and machine learning.

### Multiple Linear Regression

Formulation of Multiple Linear Regression:

- Model Equation: MLR models the relationship between several independent variables and a dependent variable by fitting a linear equation to observed data. The equation is  $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \cdots + \beta_n X_n + \epsilon$ , where:
  - -Y is the dependent variable.
  - $-X_1, X_2, \ldots, X_n$  are the independent variables.
  - $-\beta_0, \beta_1, \ldots, \beta_n$  are the coefficients that represent the weights of the respective independent variables.
  - $-\epsilon$  is the error term, capturing all other factors that influence Y but are not included in the model.
- Parameter Estimation: Typically, the coefficients are estimated using the least squares criterion, which aims to minimize the sum of the squared residuals (the differences between observed and predicted values).

### Assumptions of Multiple Linear Regression

Multiple Linear Regression relies on several key assumptions to ensure reliable predictions:

- Multicollinearity: The model assumes little or no multicollinearity among the independent variables. High multicollinearity can undermine the statistical significance of the independent variables.
- **Linearity and Additivity**: The relationship between the dependent and independent variables should be linear. The effect of changes in an independent variable X on the dependent variable Y is constant.
- Independence of Residuals: Residuals should be independent of each other, which implies that the residuals are spread randomly and do not follow any pattern.
- Homoscedasticity: The residuals should have constant variance at every level of the independent variable.
- **Normal Distribution of Residuals**: For inference purposes, the residuals should be normally distributed.

### Feature Engineering in Multiple Linear Regression

Enhancing Model Performance with Feature Engineering:

- Creating Interaction Terms: To capture the effect of interactions between variables that may affect the dependent variable.
- Polynomial Features: Including non-linear relationships by adding squared or higher-order terms of the predictors.
- Transformation of Variables: Applying transformations such as logarithmic, square root, or inverse to achieve linearity or reduce skewness in the data.
- Handling Categorical Variables: Using techniques like one-hot encoding to convert categorical variables into a format that can be provided to ML models.

### Summary

Multiple Linear Regression, complemented by strategic feature engineering, significantly enhances the ability to understand complex relationships within data. These methodologies are indispensable in scenarios where the impact of multiple variables on an outcome needs to be assessed simultaneously, providing clarity and precision in predictive analytics. Through careful consideration of model assumptions and judicious feature selection and transformation, practitioners can build robust models that effectively capture the dynamics of real-world phenomena.



### Week 14: (4/22 - 4/28)



### Influence In Multiple Linear Regression

#### 14.0.1 Piazza

Must post / respond to two Piazza posts. (4/30/24)

#### 14.0.2 Lectures

The lecture videos for this week are:

- Influence In Multiple Linear Regression Models  $\approx 54$  min.
- Quiz Walkthroug, Project, Fairness In Housing Appraisal  $\approx 25$  min.
- Modeling And Analyzing COVID-19 Cases Walkthrough  $\approx 55$  min.
- Intro To Classification Logistic Regression  $\approx 54$  min.

The lecture notes for this week are:

- Inference In Multiple Linear Regression Lecture Notes
- Logistic Regression Lecture Notes

### 14.0.3 Assignments

The assignment for this week is:

• The assignment for this week is **Final Project Part 2**. (5/3/24)

### 14.0.4 Concept Summary

The concept that is being covered this week is Influence In Multiple Linear Regression.

### Influence In Multiple Linear Regression

### Overview

Influence in multiple linear regression refers to the effect that specific observations or groups of observations have on the fitted regression model. Highly influential points can disproportionately affect the slope of the regression line and other inferential statistics, potentially leading to misleading results. Understanding and identifying influential observations are crucial for ensuring the reliability and accuracy of regression analysis.

### Assessing Influence in Multiple Linear Regression

The assessment of influence in multiple linear regression involves several statistical measures and diagnostics that help in identifying observations that have a significant impact on the coefficients and predictions of the model:

• Leverage: Leverage measures the influence an observation has on its own fitted value, relative

to its position with respect to the mean of the independent variables. High leverage points are those that have extreme values on one or more predictors.

- Residuals: While residuals (the differences between observed and predicted values) themselves do not measure influence, large residuals, when combined with high leverage, can indicate potential influence.
- Cook's Distance: A commonly used measure that combines the leverage of an observation with the size of its residual to determine its influence on the fitted values across all observations in the dataset. Observations with large Cook's Distance values may be unduly influencing the regression model.

### Mitigating the Effects of Influential Observations

Once influential observations are identified, there are several strategies for dealing with them to ensure the robustness of the model:

- Robust Regression: Using regression techniques that are less sensitive to outliers and influential points, such as weighted least squares or ridge regression, can help mitigate the effects of these observations.
- Removing Influential Points: In cases where the influence is due to data errors or anomalies that do not represent the population, removing these points might be justified. However, care must be taken to ensure that the removal of data does not bias the results.
- Transforming Variables: Applying transformations to the variables (e.g., logarithmic, square root) can reduce the influence of outliers by making the data more homoscedastic (having uniform variance) and normally distributed.

### Importance of Understanding Influence

Understanding the influence of observations in multiple linear regression is vital for:

- Model Accuracy: Ensuring that the model accurately reflects the underlying data without being overly affected by anomalies.
- **Decision Making**: Providing reliable information for decision-making processes in business, economics, health sciences, and other fields.
- Statistical Inference: Maintaining the integrity of statistical inferences made from the model.

### Summary

Influence in multiple linear regression is a critical aspect of model diagnostics. It involves identifying and addressing observations that unduly affect the model's results, ensuring that the conclusions drawn from the model are valid and representative of the broader data set. By effectively managing influential data points, analysts can enhance the robustness and reliability of their regression models, leading to more accurate predictions and insights.

## Week 15: (4/29 - 5/5)



# Final Project

### 15.0.1 Piazza

Must post / respond to two Piazza posts. (5/7/24)

### 15.0.2 Assignments

The assignment for this week is:

• The assignment for this week is **Final Project**. (5/3/24)

