

## Search



# Informed Search- Heuristics

# Review- A\*

- A\* uses both backward costs and (estimates of) forward costs

$$f(n) = g(n) + h(n)$$

- A\* is optimal with **admissible** / **consistent** heuristics

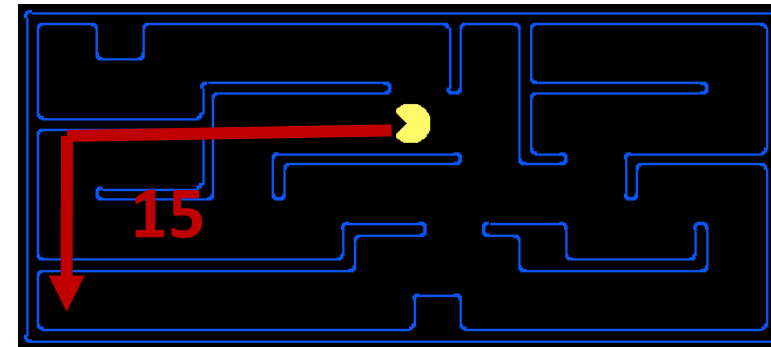
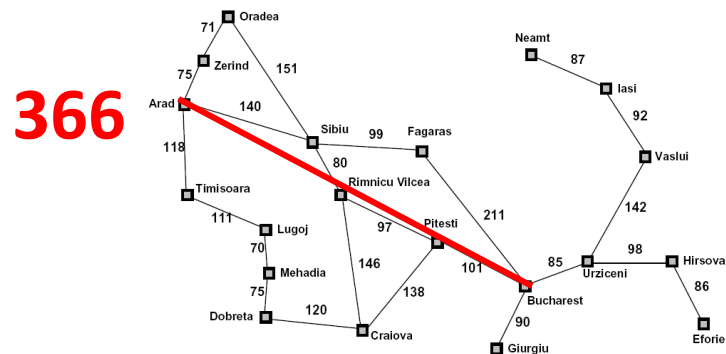
$$0 \leq h(n) \leq h^*(n)$$

$$h(n_1) - h(n_2) \leq C(n_1, n_2)$$

- Heuristic design is key: often use relaxed problems

# Creating Admissible Heuristics

- Most of the work in solving hard search problems optimally is in coming up with admissible heuristics
- Often, admissible heuristics are solutions to *relaxed problems*, where new actions are available

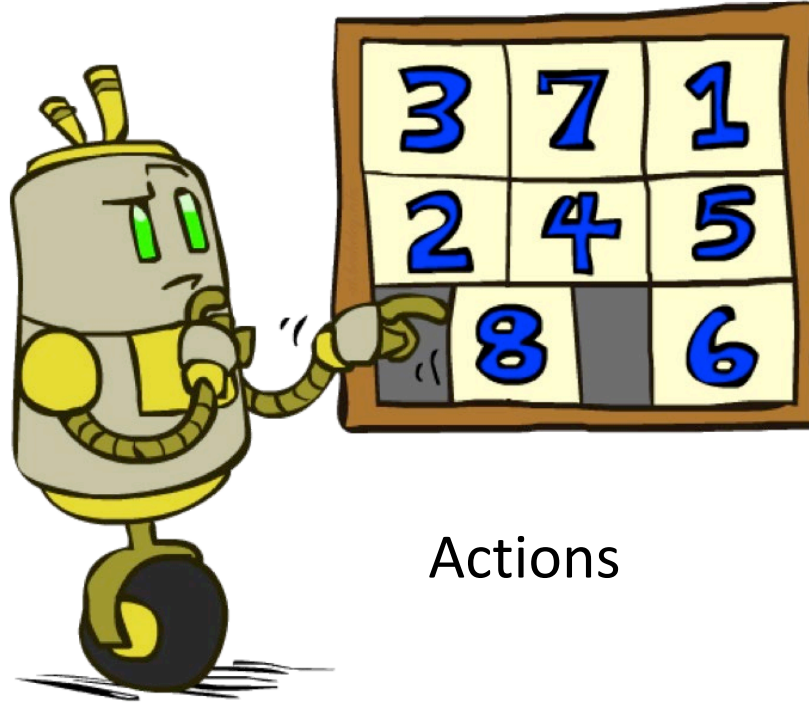


- Inadmissible heuristics are often useful too

# Example: 8 Puzzle

7	2	4
5		6
8	3	1

Start State



Actions

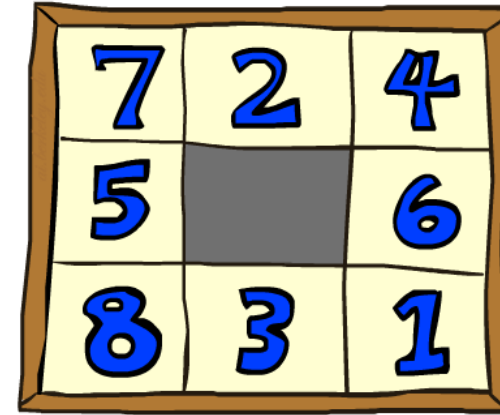
	1	2
3	4	5
6	7	8

Goal State

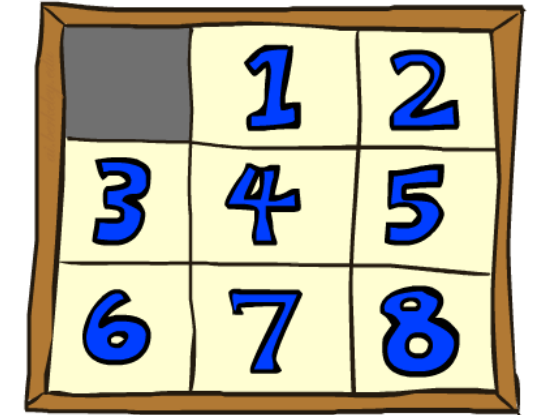
- What are the states?
- How many states?
- What are the actions?
- How many successors from the start state?
- What should the costs be?

# 8 Puzzle Heuristic I

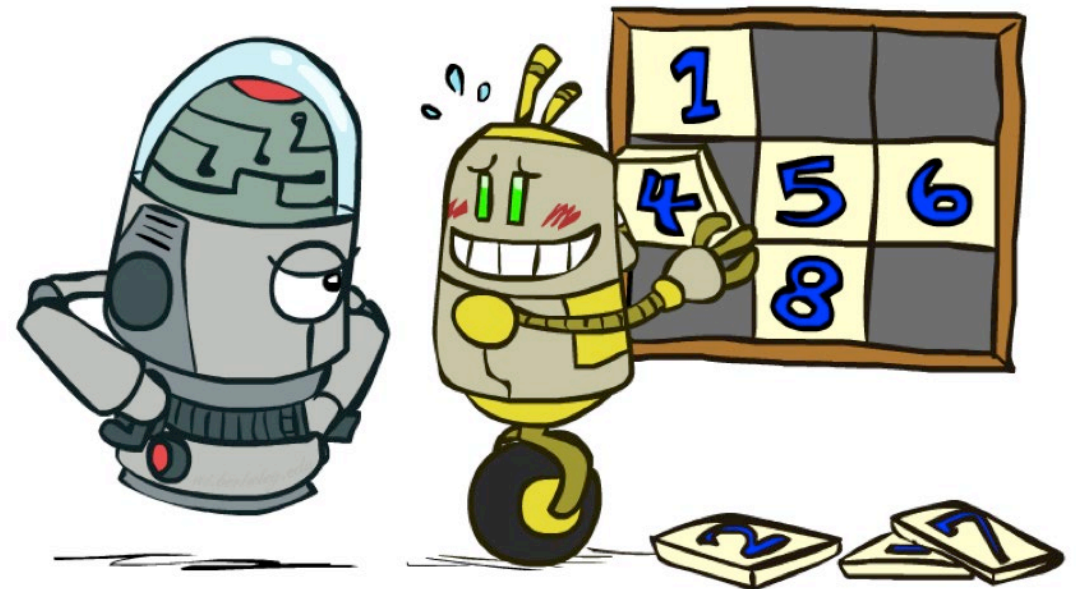
- Heuristic: Number of tiles misplaced
- Why is it admissible?
- $h(\text{start}) = 8$
- This is a *relaxed-problem* heuristic



Start State

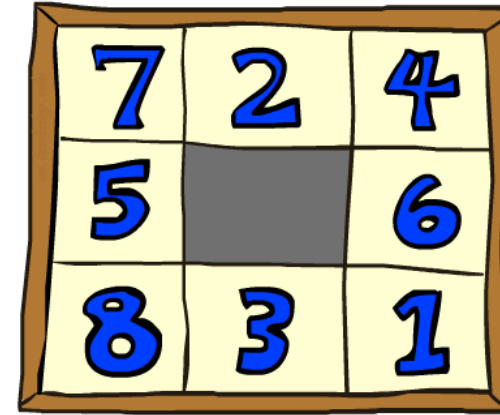


Goal State

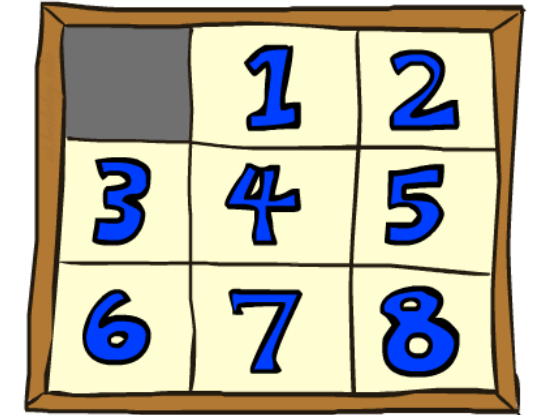


# 8 Puzzle Heuristic II

- What if we had an easier 8-puzzle where any tile could slide any direction at any time, ignoring other tiles?
- Total *Manhattan* distance
- Why is it admissible?
- $h(\text{start}) = 3 + 1 + 2 + \dots = 18$



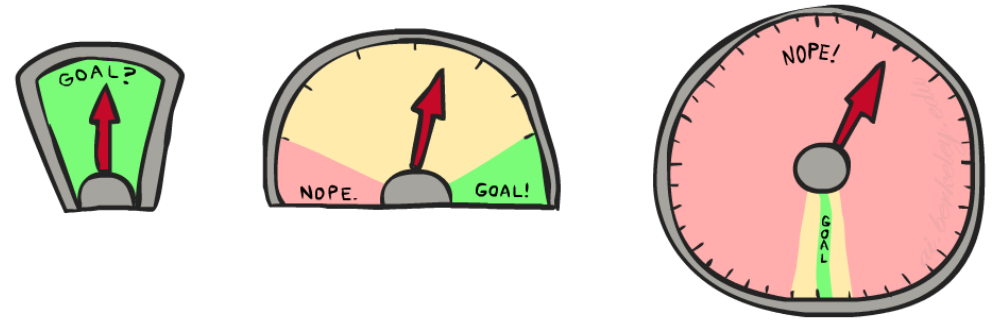
Start State



Goal State

# Accuracy of a heuristic

- How about using the *actual cost* as a heuristic?
  - Would it be admissible?
  - Would we save on nodes expanded?
  - What's wrong with it?



- With A\*: a trade-off between quality of estimate and work per node
  - As heuristics get closer to the true cost, you will expand fewer nodes but usually do more work per node to compute the heuristic itself



# Quality of Heuristics

## Analytic Method

$N$  Total number of nodes expanded

$d$  The solution depth (optimal)

$b^*$  Effective branching factor

## Empirical Method

	Average nodes expanded (Search cost)			Effective Branching Factor		
Optimal Soln'	4 steps	8 steps	12 steps	4 steps	8 steps	12 steps
No $h$ (IDS)	112	6,300	$3.6 \times 10^6$	2.87	2.80	2.78
A* TILES	13	39	227	1.48	1.33	1.42
A* MANHATTAN	12	25	73	1.45	1.24	1.24