

## Key points of 01/19 lecture:

- Statistical mechanics: system in equilibrium (static, no statement on likelihood)
- Micro canonical ensemble: isolated system w/ macro variables  $E, V, N$
- Postulate of equal a priori probability: in thermodynamic equilibrium, all states consistent with macro variables are equally probable.

- Ensemble average:

$$\langle f \rangle = \frac{\int f(\vec{p}, \vec{q}) \rho(\vec{p}, \vec{q}) d^{3N} \vec{p} d^{3N} \vec{q}}{\int \rho(\vec{p}, \vec{q}) d^{3N} \vec{p} d^{3N} \vec{q}}$$

↑  
observed  
value

$$\rho(\vec{p}, \vec{q}) = \begin{cases} \text{const} & \text{for } E < \mathcal{H}(\vec{p}, \vec{q}) < E + \Delta E \\ 0 & \text{otherwise} \end{cases}$$

- Fluctuations  $\ll 1$ :  $\frac{\langle f^2 \rangle - \langle f \rangle^2}{\langle f \rangle^2} \ll 1$

Thermodynamics  $\leftrightarrow$  Statistical Mechanics

$$\bullet \left\{ S(E, V, N) = k \log T(E, V, N) \right\}; \left\{ \left( \frac{\partial S(E, V, N)}{\partial E} \right)_{V, N} = T^{-1} \right\}$$

absolute temperature