

Key points of 02/16 lecture

- Non-relativistic (non-interacting) ideal gas:

$$Q_N(T, V) = \frac{1}{N!} \left(\frac{V}{\lambda^3} \right)^N$$

three spatial
dimensions

$$\text{where } \lambda = \frac{h}{\sqrt{2\pi m kT}}$$

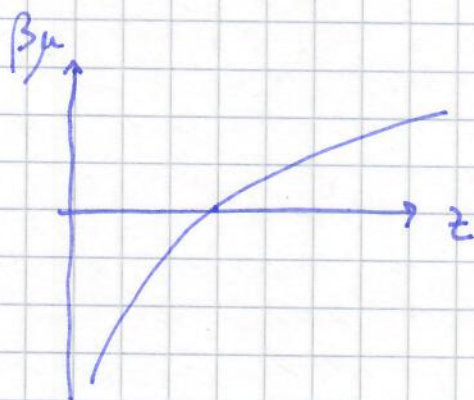
- $\mathcal{Q}(\mu, T, V) = \exp\left(\frac{zV}{\lambda^3}\right)$

- $PV = kT \log \mathcal{Q} = kT \langle N \rangle$

ideal gas law in grand-canonical ensemble

(or: thermal equation of state of non-relativistic ideal gas)

- $\mu = \left(\frac{\partial U}{\partial N} \right)_{S, V}$



←
classical
regime

→
quantum
regime

* negative μ : energy goes down as one adds a particle (system is "happy" to accept new particle)

$$dU = -P dV + T dS + \mu dN$$



goes
down as N goes up