5393 Quantum Mechanics Homework 1

Reading Assignment Sakurai Sections 1.1 through 1.4

Problems Sakurai Chapter 1

prob. 1.1, 1.3, 1.7, 1.8

Date Due Sept. 31, 2021 by 5:00 pm

Additional Problems:

Q-1 Let $\tilde{\mathbf{K}}$ be the operator defined by $\tilde{\mathbf{K}} = |\phi\rangle\langle\psi|$, where $|\phi\rangle$ and $|\psi\rangle$ are two vectors of the state space.

- (a) Under what condition is $\tilde{\mathbf{K}}$ Hermitian?
- (b) Calculate $\tilde{\mathbf{K}}^2$. Under what condition is $\tilde{\mathbf{K}}$ a projection operator?
- (c) Show that $\tilde{\mathbf{K}}$ can always be written in the form $\tilde{\mathbf{K}} = \lambda \tilde{\mathbf{P}}_1 \tilde{\mathbf{P}}_2$ where λ is a constant to be calculated and $\tilde{\mathbf{P}}_1$ and $\tilde{\mathbf{P}}_2$ are projection operators.