

8/30/2019

Density

$$d = m/v$$

ex: "gold nugget" has a mass = 59.9g
volume = 5.25 mL

$$d = \frac{59.9g}{5.25mL} = 11.4 g/mL \quad \text{gold?} \quad \text{No!}$$

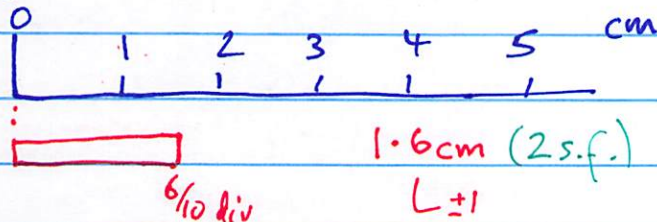
How certain are we?

When we measure, we generally assume last digit has some error, ± 1 .

ex: 8.2 mL
certain uncertain
 ± 1
8.1 - 8.3

vs. 8.25 mL
certain ± 1
8.24 - 8.26

When we read a scale, we always estimate our reading to $1/10$ division.



a measure of precision

Significant Figures (sig figs, s.f.) = #certain digits + 1

Rules for counting #s.f.

1. Non-zero digits (✓) ex: $\overset{\checkmark}{7}\overset{\checkmark}{3}s$ (2s.f.)
 2. Interior zeros (✓) ex: $\overset{\checkmark}{1}\overset{\checkmark}{0}\overset{\checkmark}{8}Kg$ (3s.f.)
 3. Leading zeros (✗) ex: $\overset{\times}{0}.\overset{\times}{0}\overset{\checkmark}{1}\overset{\checkmark}{3}\overset{\checkmark}{0}\overset{\checkmark}{7}m$ (4s.f.)
 4. Trailing zeros: (✓) if d.p. ex: $5.\overset{\checkmark}{0}\overset{\checkmark}{0}\overset{\checkmark}{0}\overset{\checkmark}{0}mol$ (5 s.f.)
(✗) if no d.p. ex: $\overset{\checkmark}{5}\overset{\times}{0},\overset{\times}{0}\overset{\times}{0}\overset{\times}{0}mol$ (1s.f.)
- $\overset{\checkmark}{7}\overset{\checkmark}{3}\overset{\checkmark}{0}\overset{\checkmark}{5}.0\mu m$ (5s.f.) $\overset{\checkmark}{6}\overset{\checkmark}{0}\overset{\checkmark}{0}.A$ (3s.f.) $\rightarrow 599-601$
 $\overset{\checkmark}{0}.\overset{\checkmark}{0}\overset{\checkmark}{0}\overset{\checkmark}{8}$ (4s.f.) $\overset{\checkmark}{6}\overset{\checkmark}{0}\overset{\checkmark}{0}A$ (1s.f.) $\rightarrow 500-700$

Sci. Notation

s.f. 7.1×10^{-8} 1.300×10^{1024}
(2s.f.) ignore (4s.f.) ignore

Defined / Exact / Counted #'s

(∞s.f.) (∞s.f.) ∞s.f. ∞s.f.
ex: $2.54cm = 1in$ $1min = 60s$ 4 fingers
(defined) (exact) counted
no error

Calculations w/ sig-figs

- least precise # affects the final answer!

(1) \times, \div ... fewest #s.f.

ex: $\overset{2s.f.}{3.8} \times \overset{3s.f.}{2.00} = 0.900676693 \quad (2s.f.)$
 $\underline{8.4381} \quad 5s.f. = 0.90 \quad (2s.f.)$

ex: $0.937 \xrightarrow{\text{2s.f.}} 0.94 \quad (2s.f.)$

(2) $+, -$... fewest #dp

↳ decimal places.

ex: $\begin{array}{r} 1.8470 \quad (4dp) \\ + 3.22 \quad (2dp) \\ \hline 5.0670 \quad (2dp) \end{array}$

↳ $5.07 \quad (2dp)$

what about: $\overset{\text{add}}{\underbrace{8.71 + 0.03}_{8.74}} = ? \quad (2) \quad \overset{2dp.}{\overset{(3s.f.)}{\downarrow}} \quad \begin{array}{r} 8.74 \\ \hline 0.001714 \quad (4s.f.) \end{array}$

$\check{\check{\check{\times}}} \quad 5099.183... \quad (3s.f.)$

$5100 \quad (2s.f.)$

$5100. \quad (4s.f.) \longrightarrow 5100 \quad (3s.f.)$
 $5.10 \times 10^3 \quad (3s.f.)$