#### CS 471 Graph Theory

3-3-0

An introduction to the combinatorial, algorithmic and algebraic aspects of graph theory.

Prerequisite: CS 304, MAT 200

Note: See MAT 421. Students may not take this course for credit if they have received credit for MAT 421.

#### CS 499F Honours Dissertation

6-0-0

The student is required to complete a theoretical or applied project. The subject is arranged with the student's supervisor during the first four weeks of term. A written dissertation is required as well as two seminar presentation.

Note: This course is open only to final year Computer Science Honour Students in the dissertation stream, and only by permission of the department

# **Mathematics**

### **Faculty**

#### Madjid Allili,

B.Sc.(Algiers), M.Sc., Ph.D.(Sherbrooke); Professor

#### Thomas Brüstle,

B.Sc., (Ludwig-Maximilians), M.Sc., Ph.D. (Zurich), Professor, Maurice-Auslander Research Chair

#### François Huard,

B.Sc., M.Sc., Ph.D. (Sherbrooke); Professor

#### Trevor H. Jones,

B.Sc.H. (Acadia), M.Sc. (Dalhousie), Ph.D. (University of New Brunswick); Senior Instructor

#### Scosha Merovitz,

B.Sc.(Bishop's), M.Sc.(Dalhousie); Coordinator, Math/Stats Help Centre

#### David Smith,

B.Sc., M.Sc., Ph.D. (Sherbrooke); Adjunct Professor

#### N. Brad Willms,

B.Math. M.M., Ph.D. (Waterloo); Associate Professor Chair of the Department

# **Program Overview**

Mathematics is the language of the sciences, a language which allows scientists to quantify, model, understand and predict behaviour in an enormously diverse range of phenomena of interest. Simultaneously, Mathematics is often regarded as an art, as it is the creative study of patterns and of problem solving. Mathematics covers a wide range of disciplines including algebra, analysis, combinatorics and discrete mathematics, and differential equations. In first-year courses, mathematics students are joined by other science students, particularly from Physics and Computer Science. In the advanced courses, classes are very small, and some are given on an individual or tutorial basis.

The highest level of specialization is Honours, and Honours programs prepare students for direct entry into graduate work leading to a Master's or Ph.D. degree. All honours mathematics students have an opportunity to study independently and thus develop their reading and problem solving skills, and there is some chance to pursue special interests. The Majors programs provide students with an excellent general preparation for the career world, while not preventing entrance into graduate school (sometimes

after a qualifying year). The Majors programs have sufficient electives to allow students to combine their major with a second major or at least a minor (the least specialized type of program) in another discipline. Students are encouraged to add a minor or major and many do so. Popular choices include computer science, physics, music, English, French, Spanish, drama, and philosophy. The Department of Mathematics offers several specialized, interdisciplinary programs, jointly with other departments, including Hispanic Studies and the School of Education.

# First-year Calculus requirement

All Mathematics students require six course credits of Calculus studies, normally in their first year. Students with a Québec collegial diploma (DEC) shall be granted advance credit for these courses if they have completed a course in Differential Calculus and a course in Integral Calculus at CEGEP. If one or both of these courses were not completed at CEGEP, they must be completed at Bishop's and advanced credits shall be reduced accordingly. Students entering four-year programs in Mathematics with a grade 12 diploma (or equivalent) must register in MAT 191 and MAT 192 in their first year. These courses are included in the 120 total credit requirement. Students transferring into Mathematics programs may use credit for MAT 198 to replace MAT 191, and MAT 199 to replace MAT 192. Credit for MAT 197 with a grade of 80% or higher will also be accepted to replace MAT 191. Mathematical Contexts Minor program students normally complete MAT 198 and MAT 199 (instead of MAT 191 and MAT 192, although these are also acceptable), and do not need to do so in their first year.

# First-year Physics requirement

Mathematics students pursuing the Bachelor of Science (B.Sc.) degree require six course credits of introductory physics studies in their first year. Students in the Bachelor of Arts (B.A.) degree program are exempt from this requirement. Students with any DEC are exempt from this requirement if they have completed two introductory Physics courses, Mechanics, and Electricity and Magnetism, at CEGEP. If one or both of these courses were not completed, they must be completed at Bishop's and advanced credits shall be reduced accordingly. Students entering four-year B.Sc. programs in Mathematics with a grade 12 diploma (or equivalent) must register in PHY 191 and PHY 192 in their first year.

# **Humanities requirement**

Students must complete six course credits of humanities studies, normally in their first year at Bishop's. Students who have a Québec Collegial Diploma (DEC), students admitted as "Mature Students", and 2nd Bachelor's degree students are all exempt from this requirement. The Humanities requirement must include ENG 116 Effective Writing, or another English course (coded 'ENG'), and one additional course selected from Humanities courses in Classical Studies, English, History, Liberal Arts, Philosophy or Religion (courses coded CLA, ENG, HIS, LIB, PHI, or REL).

The Programs					
The Department of Mathematics offers the following degree programs:					
Name of Program	Code	Levels of Specialization Available	Degree Types Available		
Mathematics	MAT	Honours, Major or Minor	B.Sc. or B.A.		
Mathematics Education	EDM	double Major with Education	B.Sc. or B.A.		
Matemáticas en Español	n/a	Major in Mathematics combined with a Minor in Hispanic Studies	B.Sc. or B.A.		
Mathematical Contexts	MAC	Minor	B.A.		

### **Arts and Science requirement**

In addition to the Humanities requirement above, all students are required to complete at least three credits in either the Division of Humanities or the Division of Social Sciences. Students with program combinations which require more than 72 credits are exempt from this requirement.

Please refer to the Natural Sciences Division page for information on *Divisional Requirements*.

# **Computer Science requirement**

All Mathematics majors and honours students (except those in the Mathematics Education double major program) are required to complete the course CS 211 Programming Methodology.

# **Science Elective requirement**

Mathematics students pursuing a Bachelor of Science degree must complete three courses (at least nine course credits) of science electives in their degree program. Students in any B.A. degree program are exempt from this requirement.

# **Mathematics Electives**

Mathematics students (in any program) may not include courses from the list: MAT 190, MAT 191, MAT 192, MAT 196, MAT 197, MAT 198, MAT 199, as mathematics elective credits. Courses at the 460 level are only open to Honours students.

The courses MAT 190, MAT 196, MAT 197 are not accepted as credits for any Science or Mathematics degree. Mathematics courses MAT 190, MAT 191, MAT 192, MAT 196, MAT 197, MAT 198, MAT 199 may not be taken for credit by students who have already passed equivalent course(s) elsewhere. The course MAT 190 may not be taken for credit by any student without permission from their department chair. Students in Science programs, including Mathematics B.A., may receive a maximum of three credits in elementary statistics courses.

# Matemáticas en Español

This is a unique program combining a Major in Mathematics, a Minor in Hispanic Studies as well as one year of Spanish immersion at the Universidad San Francisco de Quito in Ecuador. Contact the Chair of the department for more details.

# Mathematics Education Double Major (108 credits for B.Sc., 93 credits for B.A.) MAJEDM

These students will find their program course list and additional program requirements listed in the School of Education's section of this Calendar.

# Mathematics Honours (99 credits for B.Sc., 84 credits for B.A.) HONMAT

Normally a student is admitted to an Honours program after completing a minimum of 12 credits in Mathematics courses with an average of at least 70% and having achieved an average of 65% in all courses taken at Bishop's.

To continue in an Honours program the student must obtain an average of at least 70% in Mathematics courses in each academic year.

In order to graduate with a Mathematics Honours degree, the student must have an overall average of 70% in all Mathematics courses.

### Requirements:

U1 (normally): MAT 191, MAT 192, ENG 116\*, Humanities 1xx option\*, PHY 191 & PHY 192 (for B.Sc. only).

MAT 108, MAT 200, MAT 206, MAT 207, MAT 209, MAT 220, CS 211, MAT 310, MAT 313, MAT 314, MAT 315, MAT 317, MAT 322, MAT 323

- 6 optional credits of Mathematics courses at the 100 level or higher,
- 9 optional credits of Mathematics courses at the 300 level or higher,
- 6 optional credits of Mathematics courses at the 400 level or higher,
- 6 optional credits of Mathematics courses at the 460 level,
- 3 credits to satisfy the Arts and Science requirement.
- B.Sc. students must include at least 9 additional Science credits among their options.
- \*Students with a CEGEP DEC or mature students will be granted exemption credits for these courses.

#### **Total credits:**

B.Sc.: 72 Mathematics, 6 Physics, 3 Computer Science,

9 Science options, 6 Humanities, 3 Arts and Science options, 21 credits of free electives

B.A.: 72 Mathematics, 3 Computer Science, 6 Human-

ities, 3 Arts and Science options, 36 credits of free electives

#### Recommended schedule:

Fall Winter

#### Year 1

(for students in a four-year program or lacking some CEGEP requirements)

requiren	nents)		
	MAT 191		MAT 192
	PHY 191 (B.Sc. students)		PHY 192 (B.Sc. students)
	ENG 116		Humanities electives
	elective (B.A. students)		elective (B.A. students)
	elective		elective
	elective		elective
Year 2	MAT 200		MAT 220
	MAT 206		MAT 207
	MAT 108		MAT 209
	CS 211		elective
	elective		elective
Year 3	MAT 1xx		MAT 1xx
	MAT 313	MAT 314	
	MAT 322	MAT 323	
	MAT 3xx	MAT 3xx	
	elective elective		
Year 4	MAT 315		MAT 317

MAT 310 MAT 3xx
MAT 4xx MAT 4xx
MAT 46x MAT 46x
Elective Elective

This schedule is provided as a recommendation only. The order in which the courses are taken is subject to change. Students are encouraged to consult the Chair of the department before registering for their courses. The code MAT nxx refers to any 3-credit MAT course at the n-hundred level or higher.

# Mathematics Major (81 credits for B.Sc., 66 credits for B.A.)

**MAJMAT** 

#### **Requirements:**

U1 (normally): MAT 191, MAT 192, ENG 116\*, Humanities 1xx option\*, PHY 191 & PHY 192 (for B.Sc. only)

MAT 108, MAT 200, MAT 206, MAT 207, MAT 209, CS 211, MAT 310, MAT 313, MAT 314, MAT 315, MAT 322

3 credits from the list {MAT 202, MAT 203 OR MAT 220}

6 optional credits of Mathematics courses at the 100 level or higher,

9 optional credits of Mathematics courses at the 300 level or higher.

3 credits to satisfy the Arts and Science requirement.

B.Sc. students must include at least 9 additional Science credits among their options.

\*Students with a CEGEP DEC and mature students will be granted exemption for these courses.

#### **Total credits:**

B.Sc.: 54 Mathematics, 3 Computer Science, 6 Physics,

6 Humanities,

9 Science options, 3 Arts and Science options,

Winter

39 credits of free electives.

B.A.: 54 Mathematics, 3 Computer Science,

6 Humanities, 3 Arts and Science options,

54 credits of free electives.

# Recommended schedule: Fall

**Year 1**(for students in a four-year program or lacking some CEGEP

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requirem	ents)	
	MAT 191	MAT 192
	PHY 191 (B.Sc. students)	PHY 192 (B.Sc. students)
	ENG 116	Humanities elective
	elective (B.A. students)	elective (B.A. students)
	elective	elective
	elective	elecive
Year 2	MAT 200	MAT {202 or 203 or 220}
	MAT 206	MAT 207
	MAT 108	MAT 209
	CS 211	elective
	elective	elective
Year 3	MAT 1xx	MAT 1xx
	MAT 313	MAT 314
	MAT 322	MAT 3xx
	elective	elective
	elective	elective
Year 4	MAT 315	MAT 3xx
	MAT 310	MAT 3xx
	elective	elective
	elective	elective
	elective	elective

This schedule is provided as a recommendation only. The order in which the courses are taken is subject to change. Students are encouraged to consult the Chair of the department before registering for their course. The code MAT nxx refers to any 3-credit MAT course at the n-hundred level or higher.

# Mathematics Minor; B.Sc., B.A. (30 credits) MINMAT

U1 (normally): MAT 191, MAT 192.

MAT 206, MAT 207, MAT 108, MAT 209 or MAT 200 plus 12 additional mathematics credits, including at least 6 credits at the 300 level or higher.

# Minor in Mathematical Contexts; B.A. (30 credits) MINMAC

The ancient, rich, and universal endeavor which is mathematics underlies all of science and engineering. Increasingly however, mathematical contexts are entwined in the fabric of modern humanistic studies.

The mathematics of social choice is enlightening the study of politics, sociology, and anthropology. The modern mathematics of management science is essential not only in the world of Business and Economics, but also to the work of human geographers who rely on mathematical modeling. Mathematical contexts reach even to the creative arts. Here new geometries, elliptic, hyperbolic, and most recently, fractal, are providing fresh and exciting sources of pattern and inspiration, the raw materials of the visual artist.

Statistics are encountered daily in every media, while statistical analyses have invaded every facet of modern life. Indeed, if for no other reason, educated persons today must understand mathematical concepts for the critical evaluation of data. Such is required in order to avoid deception and bogus claims based on false or misleading representations of statistics. Finally, the information age has given new context to an ancient mathematics: coding theory. From data encryption to internet security, mathematics is the context of modern human communication.

Many students of the Liberal Arts and Humanities, Education, and the Social Sciences, come to the discipline of Mathematics relatively late. Recently convinced of the necessity of broadening the mathematical context of their education, they nevertheless now face a language barrier. Not having pursued mastery of the high-school "advanced math" curriculum, or having gone "rusty" from lack of recent use, they now find the language of mathematics, that of quantitative reasoning, unfamiliar, foreign, and even intimidating.

It is for such students that the Minor in Mathematical Contexts is intended. Here mathematical concepts are developed and analytical thinking is employed to systematically study patterns (the raw materials of mathematics) discovered in diverse fields of study. The emphasis will be on mathematical context and thinking; not on techniques, computations, and prerequisite skills. An adult willingness to think deeply, and academic admission to Bishop's University, are the only prerequisites. In no way should these courses be confused with the "remediation" courses of other institutions: rectifying shortcomings in algebraic skills is not the goal. Rather, developing analytical problem solving skills in mathematical contexts is the objective. Successful students will find, incidentally, that their Bishop's B.A. degree has been significantly enhanced by this innovative program of study for citizens of the 21st century.

The minor in Mathematical Contexts can be added to any degree program and consists of the following courses:

MAT 200	Discrete Mathematics
MAT 108	Matrix Algebra
PHY 101	Statistical Methods
MAT 198*	Calculus I (for Life Sciences),

prerequisite: MAT 190 recommended

MAT 199\* Calculus II (for Life Sciences), prerequisite: MAT 198

\* (Remedial Precalculus and Algebra courses are available)
An additional 15 course lecture credits in Mathematics must be chosen from among:

Excursions in Modern Mathematics*
Further Excursions in Modern Mathematics**
History of Mathematics
Linear Algebra, prerequisite: MAT 108
Modern Geometry: Euclidean to Fractal,
prerequisite: MAT 200
Further Discrete Mathematics,
prerequisite: MAT 200
Number Theory
Introduction to Modern Algebra I,
prerequisite: MAT 200, MAT 209

prerequisite: MAT 322

Notes: The two courses, PMA 160 and PMA 260 may replace PHY 101 in the required list of courses. A student may not graduate

Introduction to Modern Algebra II,

with a double minor in mathematics.

\* The science version of this course, MAT 110 is also accepted.

# **Mathematics Electives**

**MAT 323** 

Mathematics students (in any program) may not include courses from the list: MAT 190, MAT 191, MAT 192, MAT 196, MAT 197, MAT 198, MAT 199, as mathematics elective credits. Courses at the 460 level are only open to Honours students.

The courses MAT 190, MAT 196, MAT 197 are not accepted as credits for any Science or Mathematics degree. Mathematics courses MAT 190, MAT 191, MAT 192, MAT 196, MAT 197, MAT 198, MAT 199 may not be taken for credit by students who have already passed equivalent course(s) elsewhere. The course MAT 190 may not be taken for credit by any student without permission from their department chair. Students in Science programs, including Mathematics B.A., may receive a maximum of three credits in elementary statistics courses.

<sup>\*\*</sup> The science version of this course, MAT 111 is also accepted.