

Maximal AND Subsequences



Alice has an array of n long integers, $A = [a_0, a_1, \dots, a_{n-1}]$. She wants to find all the k -element subsequences of A where the bitwise AND of the subsequence's elements is maximal.

For example, let $A = [6, 3, 7, 4]$ and $k = 3$. Now, let's apply the AND operation on all possible subsequences of size k :

Subsequences	Decimal	Binary
{6, 3, 7}	$6 \& 3 \& 7 = 2$	$110 \& 011 \& 111 = 010$
{6, 7, 4}	$6 \& 7 \& 4 = 4$	$110 \& 111 \& 100 = 100$
{6, 3, 4}	$6 \& 3 \& 4 = 0$	$110 \& 011 \& 100 = 000$
{3, 7, 4}	$3 \& 7 \& 4 = 0$	$011 \& 111 \& 100 = 000$

The maximal AND value of these subsequences is 4, and only 1 subsequence has that value: {6, 7, 4}.

Given A and k , find the maximal bitwise AND value of any subsequence of A , as well as the total number of subsequences having that maximal value modulo $10^9 + 7$.

Input Format

The first line contains two space-separated integers describing the respective values of n (the number of elements in the array) and k (the size of the subsequence).

Each of the n subsequent line contains a long integer describing the respective values of a_0, a_1, \dots, a_{n-1} .

Constraints

- $2 \leq k \leq n \leq 10^5$
- $0 \leq a_i \leq 10^{18}$

Output Format

Print two lines of output:

- The first line contains the maximal bitwise AND value of any k -element subsequence of A .
- The second line contains the number of subsequences of A having that maximal AND value, modulo $(10^9 + 7)$.

Sample Input 0

```
3 2
3
5
6
```

Sample Output 0

```
4
1
```

Explanation 0

For $A = [3, 5, 6]$ and $k = 2$, there are three possible subsequences of size k . Let's apply the AND

operation to each subsequence:

3 & 5 = 1
3 & 6 = 2
5 & 6 = 4

The maximum *bitwise AND* of any subsequence is **4**, and only **1** subsequence (**{5, 6}**) gives us that value. We then print **4** as our first line of output and the result of $1 \bmod (10^9 + 7) = 1$ as our second line of output.

Sample Input 1

```
4 2
21
19
22
20
```

Sample Output 1

```
20
3
```

Explanation 1

For $A = [21, 19, 22, 20]$ and $k = 2$, we perform the following *AND* operations on each subsequence:

21 & 19 = 17
21 & 22 = 20
21 & 20 = 20
19 & 22 = 18
19 & 20 = 16
22 & 20 = 20

The maximum *bitwise AND* of any subsequence is **20**, and there are **3** such subsequences (**{21, 22}**, **{21, 20}**, and **{22, 20}**) giving us that value. We then print **20** as our first line of output and the result of $3 \bmod (10^9 + 7) = 3$ as our second line of output.

Sample Input 2

```
4 3
9
15
27
14
```

Sample Output 2

```
10
1
```

Explanation 2

For $A = [9, 15, 27, 14]$ and $k = 3$, there are four k -element subsequences: **{9, 15, 27}**, **{9, 15, 14}**, **{9, 27, 14}**, and **{15, 27, 14}**. The maximum *bitwise AND* of any subsequence is **10**, and there is **1** such

subsequence ($\{15, 27, 14\}$) giving us that value. We then print **10** as our first line of output and the result of $1 \bmod (10^9 + 7) = 1$ as our second line of output.