

BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI
(MID SEMESTER EXAMINATION SP/2023)

CLASS: BTECH
BRANCH: ALL

SUBJECT: MA107: MATHEMATICS-II

SEMESTER : II
SESSION : SP/2023

TIME: 02 Hours

FULL MARKS: 25

INSTRUCTIONS:

1. The question paper contains 5 questions each of 5 marks and total 25 marks.
2. Attempt all questions.
3. The missing data, if any, may be assumed suitably.
4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

- Q.1(a) Find only the complementary function of the differential equation [2] CO 1 BL-1 &2
- $$3\frac{d^2y}{dx^2} + 8\frac{dy}{dx} + 4y = 0$$
- Q.1(b) Find only the particular integral of the differential equation [3] BL-1 &2
- $$\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = 2\sin x + 3\cos x$$
- Q.2 Solve the Cauchy Euler's linear differential equation- [5] BL-1,2,3
- $$x^3 \frac{d^3y}{dx^3} + 3x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} = 24x^2$$
- Q.3 Find the power series solution of the differential equation [5] BL-1,2,3
- $$\frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 2y = 0$$
- about an ordinary point $x = 0$ only.
- Q.4(a) Find the values of m and n if $3x^2 = mP_2(x) + nP_0(x)$ where $P_0(x)$ and $P_2(x)$ are Legendre's polynomials. [2] BL-2,3
- Q.4(b) Show that $J_{1/2}(x) = \sqrt{\frac{2}{\pi x}} \sin x$ [3] BL-1,2
- Q.5 Find the Fourier series to represent the function defined as [5] BL-1,2,3
- $$f(x) = \begin{cases} \pi + x, & -\pi < x < 0 \\ 0, & 0 \leq x < \pi \end{cases}$$