BIRLA INSTITUTE OF TECHNOLOGY, MESRA, RANCHI (MID SEMESTER EXAMINATION SP2023)

CLASS: BTECH BRANCH: CSE/IT

SEMESTER: IV

SESSION: SP2023

SUBJECT: CS241 DESIGN AND ANALYSIS OF ALGORITHM

TIME:

02 Hours

FULL MARKS: 25

INSTRUCTIONS:

- 1. The question paper contains 5 questions each of 5 marks and total 25 marks.
- 2. Attempt all questions.
- 3. The missing data, if any, may be assumed suitably.
- 4. Tables/Data handbook/Graph paper etc., if applicable, will be supplied to the candidates

- CO BL Q.1 What is the significance of Asymptotic Notations in Design and Analysis of an [5] CO1, CO2 BL3 algorithm? Illustrate 0, Ω , Θ notations in term of Time Complexity with suitable examples.
- Q.2 Derive the Best Case and Worst-Case Time Complexity of Insertion Sort and prove [5] CO1, CO2 BL4. that Insertion Sort is stable. BL₅
- Q.3 State and explain the Master Theorem. Solve the following recurrence relations [5] CO1, CO2 BL2. using Master Theorem. BL3

$$T(n) = 2 T(n/2) + n/\log n$$

$$T(n) = 2 T(n/2) + n \log n^{-2}$$

$$T(n) = T\left(\frac{n}{4}\right) + n \log n$$

$$T(n) = T\left(\frac{n}{2}\right) + 1$$

$$T(n) = 2T\left(\frac{n}{2}\right) + n \log n$$

- Q.4 Write the Quick Sort algorithm and derive its Time Complexity for Best Case and [5] CO1, BL4 Worst-Case. CO2, CO3
- Explain the Binary Search algorithm and derive its Time Complexity using [2] Q.5(a)CO1, BL₃ mathematical induction method. CO2, CO3 BL₄
- Q.5(b) Solve the following using Recursion Tree method: [3] CO1, T(n) = 2T(n/2) + nCO2, CO3 $T(n) = 3 T(n/4) + cn^2$

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