

## HW4

1. Ans

(a) Since each node has a dedicated channel to every other node,  $H_{avg} = 1$

$$T_{rmin} = H_{avg}T_r = 15ns$$

$$T_s = \frac{L}{d} = 31.25ns$$

$$\text{As } T_w = 0$$

$$T_0 = H_{avg}T_{rmin} + T_s = 46.25ns$$

(b)  $T_{rmin} = H_{avg}T_r = 240ns$

$$T_s = \frac{L}{d} = 31.25ns$$

$$\text{As } T_w = 0$$

$$T_0 = H_{avg}T_{rmin} + T_s = 271.25ns$$

2. Ans

For a big n stages,  $N=2^n$  nodes

The geometric calculation denotes that

$$avg = 10(n-1 + \sqrt{1+2^{2n-6}} + \sqrt{1+2^{2n-8}} + \dots)$$

for that in fig4.3,  $avg = 10(n-1)$ ,

i.e. it is  $(\sqrt{1+2^{2n-6}} + \sqrt{1+2^{2n-8}} + \dots)$  shorter

3. Ans

$T_r = 20ns$

| k    | n  | w  | $\Theta_{ideal}$ | $W_n$ | $W_s$ | T     |
|------|----|----|------------------|-------|-------|-------|
| 2    | 12 | 2  | 8                | 5     | 2     | 376   |
| 4    | 6  | 4  | 8                | 10    | 4     | 248   |
| 8    | 4  | 8  | 8                | 16    | 8     | 224   |
| 16   | 3  | 16 | 8                | 21    | 16    | 273   |
| 64   | 2  | 32 | 4                | 32    | 32    | 656   |
| 4096 | 1  | 64 | 0.125            | 64    | 64    | 20488 |

The minimal latency occurs when  $n=4$ . However, the latency of 224 ns when  $n=3$  is close enough that it would probably be chosen to gain the packaging and wire length advantages of a lower dimension.