In[65]:= Clear [
$$\lambda$$
1,  $\lambda$ 2,  $\mu$ a,  $\mu$ b, H, R, cond0, cond1, cond2, cond3] cond0 = 0 <  $\lambda$ 1 && 0 <  $\lambda$ 2 &&  $\lambda$ 1 +  $\lambda$ 2 <  $\mu$ a <  $\mu$ b && 0 < H < R cond1 = R  $\lambda$ 1 - H  $\frac{1}{\mu a - \lambda 1}$  > 0 > R ( $\lambda$ 1 +  $\lambda$ 2) - H  $\frac{1}{\mu a - (\lambda 1 + \lambda 2)}$  cond2 = R  $\lambda$ 1 - H  $\frac{1}{\mu b - \lambda 1}$  < R ( $\lambda$ 1 +  $\lambda$ 2) - H  $\frac{1}{\mu b - (\lambda 1 + \lambda 2)}$  cond3 =  $\frac{1}{\mu b - (\lambda 1 + \lambda 2)}$  >  $\frac{1}{\mu a - \lambda 1}$ 

Out[66]= 0 < 
$$\lambda$$
1 && 0 <  $\lambda$ 2 &&  $\lambda$ 1 +  $\lambda$ 2 <  $\mu$ a <  $\mu$ b && 0 < H < R

Out[67]= R 
$$\lambda$$
1 -  $\frac{H}{-\lambda$ 1 +  $\mu$ a} > 0 > R  $(\lambda$ 1 +  $\lambda$ 2) -  $\frac{H}{-\lambda$ 1 -  $\lambda$ 2 +  $\mu$ a

Out[68]= 
$$R \lambda 1 - \frac{H}{-\lambda 1 + \mu b} < R (\lambda 1 + \lambda 2) - \frac{H}{-\lambda 1 - \lambda 2 + \mu b}$$

Out[69]= 
$$\frac{1}{-\lambda \mathbf{1} - \lambda \mathbf{2} + \mu \mathbf{b}} > \frac{1}{-\lambda \mathbf{1} + \mu \mathbf{a}}$$

In[70]:= FindInstance[cond0,  $\{\lambda 1, \lambda 2, \mu a, \mu b, H, R\}$ ]
FindInstance[cond0 && cond1,  $\{\lambda 1, \lambda 2, \mu a, \mu b, H, R\}$ ]
FindInstance[cond0 && cond1 && cond2,  $\{\lambda 1, \lambda 2, \mu a, \mu b, H, R\}$ ]
res = FindInstance[cond0 && cond1 && cond2 && cond3,  $\{\lambda 1, \lambda 2, \mu a, \mu b, H, R\}$ ]

Out[70]= 
$$\{\{\lambda 1 \rightarrow 1, \lambda 2 \rightarrow 1, \mu a \rightarrow 3, \mu b \rightarrow 4, H \rightarrow 1, R \rightarrow 2\}\}$$

Out[71]= 
$$\left\{\left\{\lambda\mathbf{1}\rightarrow\frac{23}{8}\text{, }\lambda\mathbf{2}\rightarrow\mathbf{1}\text{, }\mu\mathbf{a}\rightarrow\mathbf{4}\text{, }\mu\mathbf{b}\rightarrow\mathbf{5}\text{, }\mathbf{H}\rightarrow\frac{95}{128}\text{, }\mathbf{R}\rightarrow\mathbf{1}\right\}\right\}$$

Out[72]= 
$$\left\{ \left\{ \lambda \mathbf{1} \rightarrow \frac{29}{16}, \ \lambda \mathbf{2} \rightarrow \mathbf{1}, \ \mu \mathbf{a} \rightarrow \mathbf{3}, \ \mu \mathbf{b} \rightarrow \mathbf{4}, \ \mathbf{H} \rightarrow \frac{391}{512}, \ \mathbf{R} \rightarrow \mathbf{1} \right\} \right\}$$

$$\text{Out[73]= } \Big\{ \Big\{ \lambda \mathbf{1} \rightarrow \frac{13}{16} \text{, } \lambda \mathbf{2} \rightarrow \mathbf{2} \text{, } \mu \mathbf{a} \rightarrow \mathbf{3} \text{, } \mu \mathbf{b} \rightarrow \mathbf{4} \text{, } \mathbf{H} \rightarrow \frac{391}{512} \text{, } \mathbf{R} \rightarrow \mathbf{1} \Big\} \Big\}$$

In[155]:= res1 = Last[res]
N[res1, 2]

Out[155]= 
$$\left\{\lambda\mathbf{1} \rightarrow \frac{13}{16}, \ \lambda\mathbf{2} \rightarrow \mathbf{2}, \ \mu\mathbf{a} \rightarrow \mathbf{3}, \ \mu\mathbf{b} \rightarrow \mathbf{4}, \ \mathbf{H} \rightarrow \frac{391}{512}, \ \mathbf{R} \rightarrow \mathbf{1}\right\}$$

$$\text{Out[156]= } \{ \ \lambda \text{1} \rightarrow \text{0.81, } \lambda \text{2} \rightarrow \text{2.0, } \mu \text{a} \rightarrow \text{3.0, } \mu \text{b} \rightarrow \text{4.0, H} \rightarrow \text{0.76, R} \rightarrow \text{1.0} \}$$

In[149]:=

$$\begin{split} & \text{Print} \big[ \text{"Profit} \, (\lambda 1, \mu a) = \text{", N} \big[ \text{R } \, \lambda 1 - \text{H} \, \frac{1}{\mu a - \lambda 1} \, / \text{. res1, 2} \big] \big] \\ & \text{Print} \big[ \text{"Profit} \, (\lambda 1 + \lambda 2, \mu a) = \text{", N} \big[ \text{R } \, (\lambda 1 + \lambda 2) \, - \text{H} \, \frac{1}{\mu a - \left(\lambda 1 + \lambda 2\right)} \, / \text{. res1, 2} \big] \big] \\ & \text{Print} \big[ \text{"Profit} \, (\lambda 1, \mu b) = \text{", N} \big[ \text{R } \, \lambda 1 - \text{H} \, \frac{1}{\mu b - \lambda 1} \, / \text{. res1, 2} \big] \big] \\ & \text{Print} \big[ \text{"Profit} \, (\lambda 1 + \lambda 2, \mu b) = \text{", N} \big[ \text{R} \, \left(\lambda 1 + \lambda 2\right) \, - \text{H} \, \frac{1}{\mu b - \left(\lambda 1 + \lambda 2\right)} \, / \text{. res1, 2} \big] \big] \\ & \text{Print} \big[ \text{"Waiting time} \, (\lambda 1, \mu a) = \, \frac{1}{\mu a - \lambda 1} = \text{", N} \big[ \frac{1}{\mu a - \lambda 1} \, / \text{. res1, 2} \big] \big] \\ & \text{Print} \big[ \text{"Waiting time} \, (\lambda 1 + \lambda 2, \mu b) = \, \frac{1}{\mu b - \left(\lambda 1 + \lambda 2\right)} = \text{", N} \big[ \frac{1}{\mu b - \left(\lambda 1 + \lambda 2\right)} \, / \text{. res1, 2} \big] \big] \end{split}$$

Profit 
$$(\lambda 1, \mu a) = 0.46$$

Profit 
$$(\lambda 1 + \lambda 2, \mu a) = -1.3$$

Profit 
$$(\lambda 1, \mu b) = 0.57$$

Profit 
$$(\lambda 1 + \lambda 2, \mu b) = 2.2$$

Waiting time 
$$(\lambda 1, \mu a) = \frac{1}{\mu a - \lambda 1} = 0.46$$

Waiting time 
$$(\lambda 1 + \lambda 2, \mu b) = \frac{1}{\mu b - (\lambda 1 + \lambda 2)} = 0.84$$