

# Logit Mixing Training for More Reliable and Accurate Prediction

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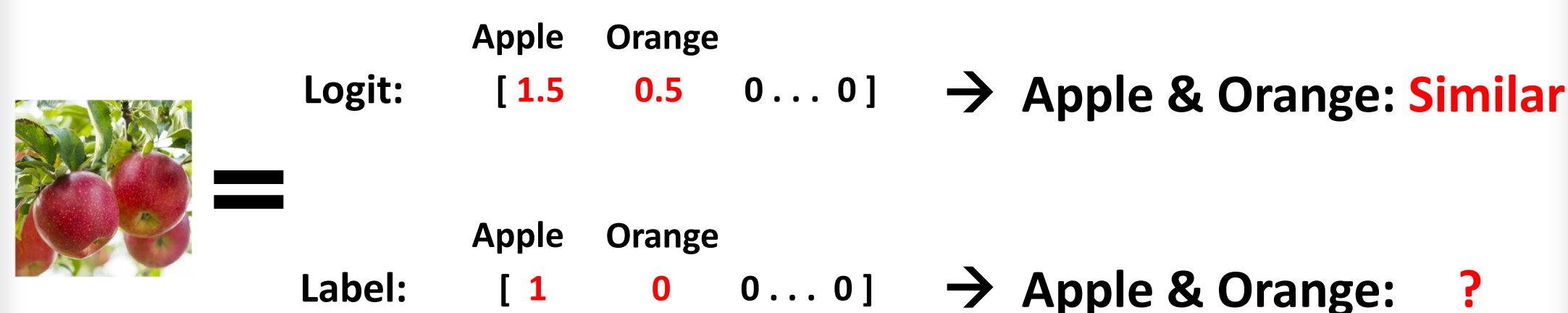
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## Motivation & Goal

- Problem:** DNNs are **poor at understanding inter-class relationship** because model training strictly enforces to predict the **one-hot labels**.
- Goals:** We devise DNNs to utilize inter-class relationships by **rejecting improbable classes**.
- Key idea :** We **adopt logits as weak supervision** for learning inter-class relationship.

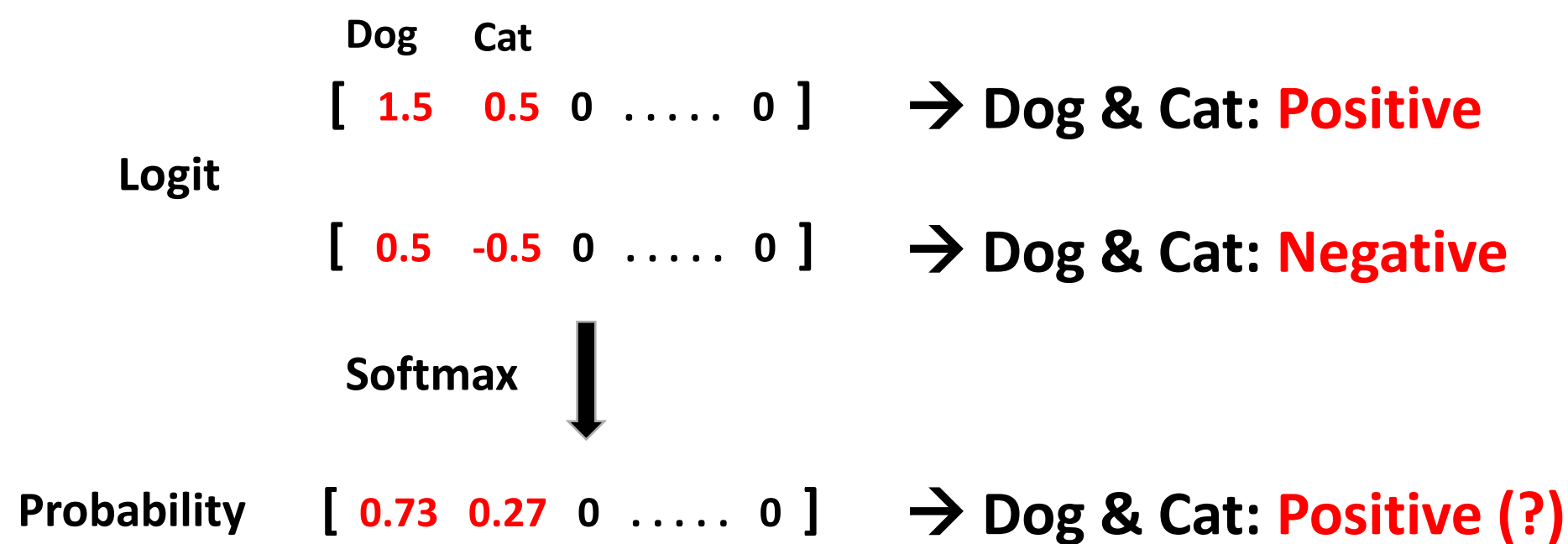
## Logit vs. One-hot Labels

- Logits** can reveal the inter-class relationship while one-hot labels **do not provide any relationship** between classes.



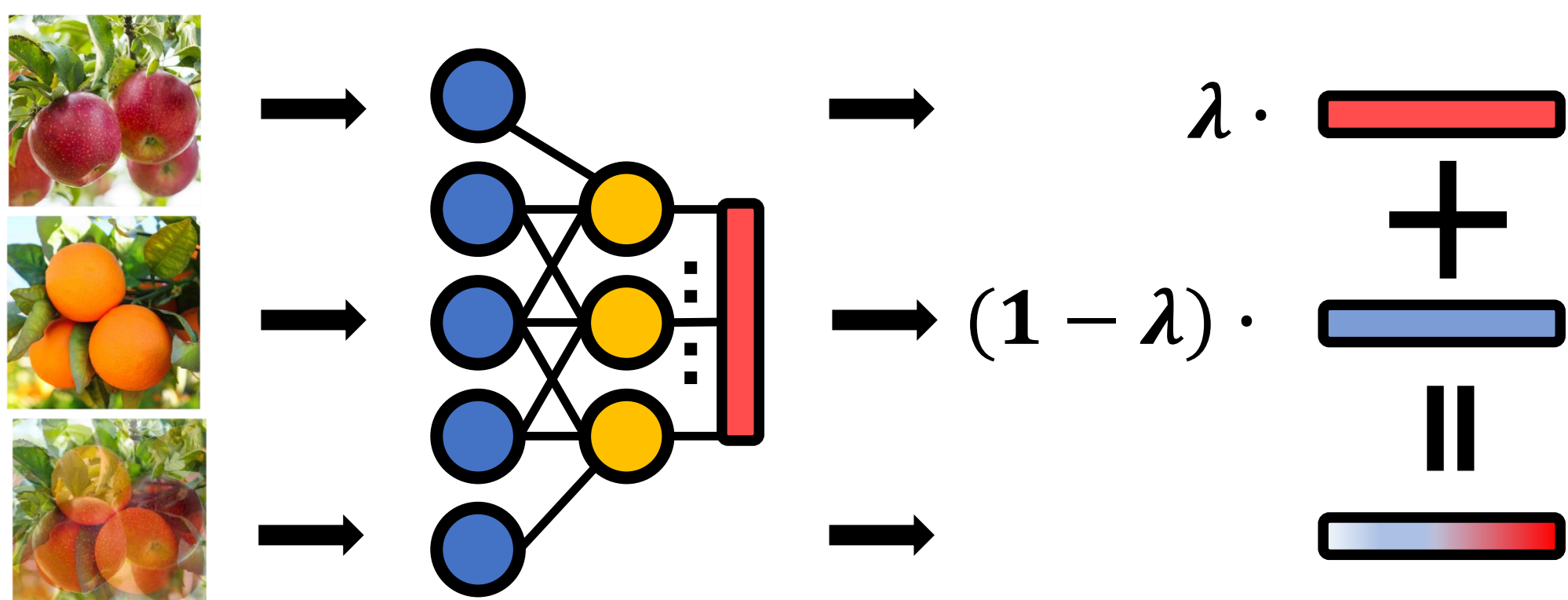
## Logits vs. Probability Vector

- Probability vector** (a.k.a post-softmax output) can capture the positive inter-class relationship, however, it can distort the true relationship.



## Method

$$\lambda \cdot \text{Apple} + (1 - \lambda) \cdot \text{Orange} = \text{Mixed Fruit}$$



$$\mathcal{L}_{sim} = \|(\lambda f(x_1) + (1 - \lambda)f(x_2)) - f(x_{mix})\|_2$$

## Objective Function

Similarity loss  $\mathcal{L}_{sim} = \|(\lambda f(x_1) + (1 - \lambda)f(x_2)) - f(x_{mix})\|_2$

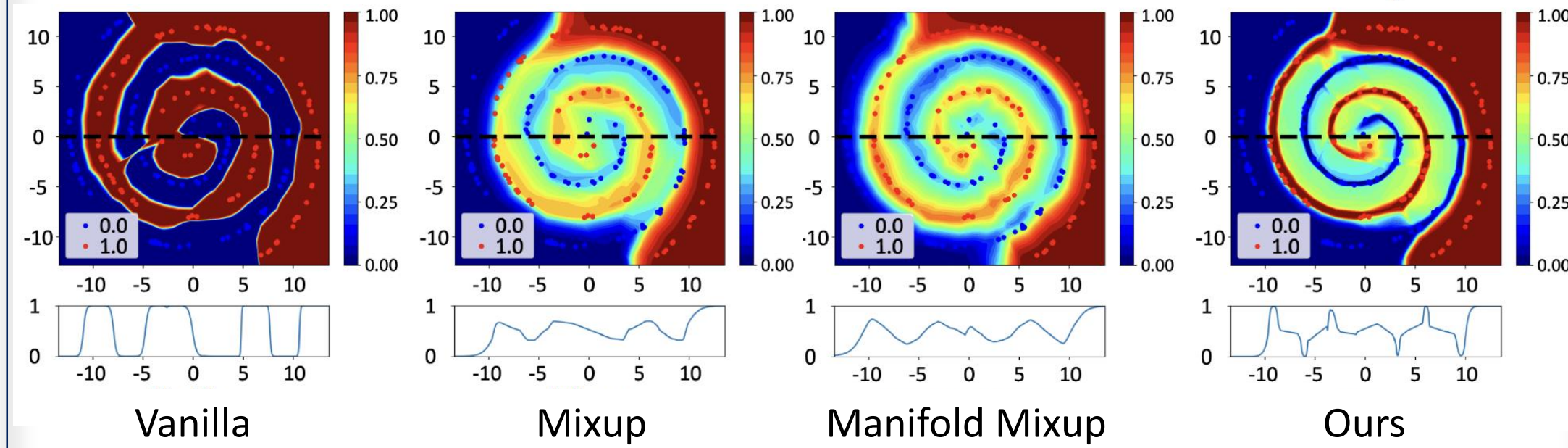
Cross-entropy with original labels  $\mathcal{L}_{cls} = \mathcal{H}(\tilde{y}_1, y_1) + \mathcal{H}(\tilde{y}_2, y_2)$

Cross-entropy with mixed labels  $y_{mix} = \lambda y_1 + (1 - \lambda)y_2$

$$\mathcal{L}_{mix} = \lambda \mathcal{H}(\tilde{y}_{mix}, y_1) + (1 - \lambda) \mathcal{H}(\tilde{y}_{mix}, y_2)$$

## Experimental Results

### Toy Example



### Ablation Study on Losses

| Name                  | Loss  | Accuracy(%)         |
|-----------------------|---|---------------------|
| Vanilla               | $\mathcal{L}_{cls}$   | 78.32 ± 0.07        |
| Mixup                 | $\mathcal{L}_{mix}$   | 79.82 ± 0.08        |
| LogitMix <sub>m</sub> | $\mathcal{L}_{cls} + \mathcal{L}_{sim} + \mathcal{L}_{mix}$ | <b>81.59 ± 0.09</b> |
| (-) Mixup             | $\mathcal{L}_{cls} + \mathcal{L}_{sim}$                     | 80.11 ± 0.09        |
| (-) Cross entropy     | $\mathcal{L}_{mix} + \mathcal{L}_{sim}$                     | 80.51 ± 0.08        |
| (-) Similarity loss   | $\mathcal{L}_{mix} + \mathcal{L}_{cls}$                     | 80.08 ± 0.49        |

### Image Classification

| Dataset      | Network      | Metric | Vanilla | Mixup        | LogitMix <sub>m</sub> | CutMix       | LogitMix <sub>c</sub> | PuzzleMix | LogitMix <sub>p</sub> |
|--------------|--------------|--------|---------|--------------|-----------------------|--------------|-----------------------|-----------|-----------------------|
| CIFAR100     | VGG16        | Acc    | 74.30   | 75.02        | 76.22 (+1.20)         | 75.34        | 76.10 (+0.76)         | 75.92     | <b>76.38</b> (+0.46)  |
|              |              | ECE    | 0.176   | 0.060        | <b>0.035</b> (-0.025) | 0.051        | 0.062 (+0.011)        | 0.121     | 0.100 (-0.021)        |
|              |              | OE     | 0.154   | 0.035        | <b>0.025</b> (-0.010) | 0.022        | <b>0.008</b> (-0.014) | 0.011     | 0.049 (+0.038)        |
|              | ResNet50     | Acc    | 78.32   | 79.82        | 81.59 (+1.77)         | 80.57        | 81.02 (+0.45)         | 82.57     | <b>83.76</b> (+1.19)  |
|              |              | ECE    | 0.087   | 0.040        | <b>0.014</b> (-0.026) | 0.078        | 0.073 (-0.005)        | 0.092     | 0.215 (+0.123)        |
|              |              | OE     | 0.073   | 0.028        | <b>0.003</b> (-0.025) | 0.064        | 0.060 (-0.004)        | 0.015     | <b>0.000</b> (-0.015) |
|              | ResNeXt50    | Acc    | 79.18   | 81.10        | 81.63 (+0.53)         | 81.16        | 81.46 (+0.30)         | 81.40     | <b>82.13</b> (+0.73)  |
|              |              | ECE    | 0.069   | 0.042        | <b>0.021</b> (-0.021) | 0.059        | 0.032 (-0.027)        | 0.092     | 0.220 (+0.128)        |
|              |              | OE     | 0.057   | 0.001        | <b>0.000</b> (-0.001) | 0.047        | 0.023 (-0.024)        | 0.017     | 0.001 (-0.016)        |
|              | MobileNetV2  | Acc    | 69.69   | 69.98        | 73.90 (+3.92)         | 68.82        | 69.91 (+1.09)         | 75.77     | <b>75.99</b> (+0.22)  |
|              |              | ECE    | 0.061   | 0.091        | <b>0.048</b> (-0.043) | 0.050        | 0.049 (-0.001)        | 0.097     | 0.100 (+0.003)        |
|              |              | OE     | 0.042   | <b>0.000</b> | <b>0.000</b> (0.000)  | <b>0.000</b> | <b>0.000</b> (0.000)  | 0.022     | 0.009 (-0.013)        |
|              | ShuffleNetV2 | Acc    | 72.17   | 74.17        | 75.53 (+1.36)         | 73.60        | 73.73 (+0.13)         | 76.18     | <b>76.75</b> (+0.57)  |
|              |              | ECE    | 0.079   | 0.060        | 0.042 (-0.018)        | <b>0.016</b> | 0.023 (+0.007)        | 0.126     | 0.094 (-0.032)        |
|              |              | OE     | 0.060   | <b>0.000</b> | <b>0.000</b> (-0.000) | 0.002        | <b>0.000</b> (-0.002) | 0.014     | 0.001 (-0.013)        |
| TinyImageNet | ResNet50     | Acc    | 66.6    | 68.34        | <b>70.71</b> (+2.37)  | 69.08        | 69.87 (+0.79)         | 69.71     | 70.15 (+0.44)         |
|              |              | ECE    | 0.098   | 0.032        | 0.030 (-0.002)        | <b>0.029</b> | 0.034 (+0.005)        | 0.121     | 0.131 (+0.010)        |
|              |              | OE     | 0.076   | 0.022        | 0.010 (-0.012)        | 0.015        | <b>0.005</b> (-0.010) | 0.012     | 0.012 (0.000)         |
|              | MobileNetV2  | Acc    | 57.62   | 59.55        | 62.12 (+2.57)         | 53.54        | 57.66 (+4.12)         | 64.08     | <b>65.30</b> (+1.22)  |
|              |              | ECE    | 0.073   | 0.091        | <b>0.032</b> (-0.059) | 0.094        | 0.082 (-0.012)        | 0.112     | 0.104 (-0.008)        |
|              |              | OE     | 0.045   | 0.019        | <b>0.000</b> (-0.019) | <b>0.000</b> | <b>0.000</b> (0.000)  | 0.034     | 0.016 (-0.018)        |
| ILSVRC2015   | ResNet50     | Acc    | 76.13   | 77.37        | 78.38 (+1.01)         | 78.43        | <b>78.51</b> (+0.08)  | 75.63     | 77.47 (+1.84)         |
|              |              | ECE    | 0.370   | 0.041        | 0.028 (-0.013)        | 0.028        | <b>0.020</b> (-0.008) | 0.120     | 0.117 (-0.003)        |
|              |              | OE     | 0.030   | 0.003        | <b>0.001</b> (-0.002) | 0.029        | 0.029 (0.000)         | 0.053     | 0.056 (+0.003)        |

### Text Classification / Regression

| Model   | MNLI-mm      | QQP          | QNLI         | SST-2        | CoLA         | STS-B        | MRPC         | RTE          | Average      |
|---|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|
| BERT <sub>BASE</sub> [Devlin et al., 2018]        | <b>84.73</b> | <b>91.25</b> | 91.43        | <b>93.12</b> | 57.82        | 89.43        | <b>87.75</b> | 68.95        | 83.06        |
| Mixup on BERT <sub>BASE</sub> [Sun et al., 2020]  | 84.29        | 91.15        | 91.36        | <b>93.12</b> | 58.82        | 89.44        | 87.50        | 67.87        | 82.94        |
| LogitMix on BERT <sub>BASE</sub>                  | <b>84.73</b> | <b>91.25</b> | <b>91.58</b> | <b>93.12</b> | <b>58.85</b> | <b>89.45</b> | 87.50        | <b>70.04</b> | <b>83.32</b> |
|   | (0.00)       | (0.00)       | (+0.15)      | (0.00)       | (+0.03)      | (+0.01)      | (-0.25)      | (+1.09)      | (+0.26)      |
| BERT <sub>LARGE</sub> [Devlin et al., 2018]       | 85.99        | 90.20        | 92.20        | 92.89        | 60.88        | 89.9         | 87.75        | 73.29        | 84.14        |
| Mixup on BERT <sub>LARGE</sub> [Sun et al., 2020] | 86.02        | 90.09        | 92.42        | 92.66        | 61.86        | <b>90.02</b> | 88.24        | 73.29        | 84.33        |
| LogitMix on BERT <sub>LARGE</sub>                 | <b>86.10</b> | <b>90.95</b> | <b>92.60</b> | <b>93.58</b> | <b>63.89</b> | 89.98        | <b>89.22</b> | <b>74.37</b> | <b>85.09</b> |
|   | (+0.08)      | (+0.75)      | (+0.18)      | (+0.69)      | (+2.03)      | (-0.04)      | (+0.98)      | (+1.08)      | (+0.76)      |

## Conclusion

- We propose to utilize logits for the better understanding on the inter-class relationship.
- We analyze the effect of three different losses and the robustness for the choice of the hyperparameter.
- We verify that our LogitMix can be combined with various mixing-based augmentation methods.
- We show that LogitMix effectively improves the classification and the calibration performance for image and text datasets.

## References

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