= (1+a+...an) as Has ar --- ar

$$D = \begin{vmatrix} 1 & 2 & 1 \\ 2 & 3 & 3 \\ 1 & 1 & -2 \end{vmatrix} = -6 + 6 + 2 - 3 + 8 - 3 = 4$$

$$D_{1} = \begin{vmatrix} 1 & 2 & 1 \\ 2 & 3 & 3 \\ 1 & 1 & -2 \end{vmatrix} = -6 + 6 + 2 + 3 - 3 + 4 - 3 = -3$$

$$D_{2} = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 3 & 3 \\ 1 & 1 & -2 \end{vmatrix} = 3 + 2 + 6 - 3 - 3 - 4 = 1$$

$$D_{3} = \begin{vmatrix} 1 & 2 & 3 \\ 2 & 3 & 3 \\ 1 & 1 & 1 \end{vmatrix} = 3 + 2 + 6 - 3 - 3 - 4 = 1$$

$$x_1 = \frac{5}{4} \quad x_2 = \frac{3}{4} \quad x_3 = \frac{3}{4}$$

2.
$$C_{11} = \begin{vmatrix} 1 & 0 \\ -1 & 1 \end{vmatrix} = 1$$
 $C_{12} = -\begin{vmatrix} 1 & 0 \\ 2 & 1 \end{vmatrix} = -1$ $C_{13} = \begin{vmatrix} 1 & 1 \\ 2 & -1 \end{vmatrix} = -3$.
 $C_{21} = -\begin{vmatrix} 1 & 2 \\ -1 & 1 \end{vmatrix} = -3$ $C_{22} = \begin{vmatrix} 0 & 2 \\ 2 & 1 \end{vmatrix} = 4$ $C_{23} = -\begin{vmatrix} 0 & 1 \\ 2 & -1 \end{vmatrix} = -2$.
 $C_{31} = \begin{vmatrix} 1 & 2 \\ 1 & 0 \end{vmatrix} = -2$ $C_{32} = -\begin{vmatrix} 0 & 2 \\ 1 & 0 \end{vmatrix} = -2$ $C_{33} = \begin{vmatrix} 0 & 1 \\ 1 & 1 \end{vmatrix} = -1$.
 $C_{31} = \begin{vmatrix} 1 & 2 \\ 1 & 0 \end{vmatrix} = -2$ $C_{32} = -\begin{vmatrix} 0 & 2 \\ 1 & 0 \end{vmatrix} = -2$ $C_{33} = \begin{vmatrix} 0 & 1 \\ 1 & 1 \end{vmatrix} = -1$.
 $C_{31} = \begin{vmatrix} 1 & 2 \\ 1 & 0 \end{vmatrix} = -2$ $C_{32} = -\begin{vmatrix} 0 & 2 \\ 1 & 0 \end{vmatrix} = -2$ $C_{33} = \begin{vmatrix} 0 & 1 \\ 1 & 1 \end{vmatrix} = -1$.

$$D = \begin{vmatrix} \lambda & 1 & 1 \\ 1 & \lambda & 1 \end{vmatrix} = 0. \quad \therefore \quad \lambda^3 + \lambda + \lambda - \lambda - \lambda - \lambda = \lambda^3 - \lambda = 0.$$

$$\therefore \quad \lambda = 0 \neq 1 \neq -1.$$

界4题范原来原证明.

$$\begin{vmatrix} a_{1} & a_{2} & a_{3} & \cdots & a_{n} \\ a_{1}^{2} & a_{2}^{2} & a_{3}^{2} & \cdots & a_{n} \\ a_{n}^{2} & a_{2}^{2} & a_{3}^{2} & \cdots & a_{n} \end{vmatrix} = \begin{vmatrix} a_{2} - a_{1} & \cdots & a_{n} - a_{n} \\ 0 & a_{2}^{2} - a_{2}a_{1} & \cdots & a_{n}^{2} - a_{n}a_{1} \\ \vdots & \vdots & \vdots & \vdots \\ 0 & a_{2}^{n-1} & a_{2}^{n-2} & a_{3}^{n-1} & \cdots & a_{n}^{n-2} \\ 0 & a_{2}^{n-1} & a_{2}^{n-2} & a_{1} & a_{n}^{n-1} & a_{n}^{n-2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} & a_{n}^{n-2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} & a_{n}^{n-2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} & a_{n}^{n-2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} & a_{n}^{n-2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} - a_{n}^{n-2} a_{1} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} - a_{n}^{n-2} a_{1} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} - a_{n}^{n-2} a_{1} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{n}^{n-1} - a_{n}^{n-2} a_{1} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{2}^{n-1} - a_{2}^{n-2} a_{1} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{2}^{n-1} - a_{2}^{n-2} a_{2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{2}^{n-1} - a_{2}^{n-2} a_{2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{2}^{n-1} - a_{2}^{n-2} a_{2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{2}^{n-1} - a_{2}^{n-2} a_{2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-2} a_{1} & a_{2}^{n-1} - a_{2}^{n-2} a_{2} \\ 0 & a_{2}^{n-1} - a_{2}^{n-1} - a_{2}^{n-1} - a_{2}^{n-1} \\ 0 & a_{2}^{n-1} - a_{2}^{n-1} - a_{2}^{n-1} - a_{2}^{n-1} - a_{2}^{n-1} \\ 0 & a_{2}^{n-1} - a_{2}^{n-1$$

$$= (a_2 - a_1)(a_3 - a_1)(a_0 - a_1) - (a_n - a_1) \begin{vmatrix} a_1 & \cdots & a_n \\ a_n & \cdots & a_n \end{vmatrix}$$