

1, 2, 3

1) Let  $X$  be a metric space. Prove or disprove the following statement: Every compact subset of  $X$  is bounded.

■

**2)** Let  $X$  be a finite metric space. What can you say about the open subsets, closed subsets, and compact subsets of  $X$ ?

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**3)** Let  $a$  and  $b$  be irrational real numbers such that  $a < b$ , and consider the following subset of the rational numbers:

$$A = \{q \in \mathbb{Q} : a < q < b\}.$$

View  $\mathbb{Q}$  as a metric space with the usual metric.

- a. Is  $A$  an open subset of  $\mathbb{Q}$ ?
- b. Is  $A$  a closed subset of  $\mathbb{Q}$ ?
- c. Is  $A$  a compact subset of  $\mathbb{Q}$ ?

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