

### Quiz #3

1.

$$(a) P_Y(y) = \sum_{x=1}^4 P_{X,Y}(x,y) = \frac{e}{y!} \sum_{x=1}^4 x^y = \frac{e}{y!} (1 + 2^y + 3^y + 4^y).$$

$$(b) P_{X|Y}(x|1) = \frac{P_{X,Y}(x,1)}{P_Y(1)} = \frac{e x}{10e} = \frac{1}{10} x.$$

$$(c) P(X > 2 | Y=1) = \sum_{x=3}^4 P_{X|Y}(x|1)$$

$$= \frac{1}{10} (3 + 4) = 0.7.$$

$$(d) E[X | Y=1] = \sum_{x=1}^4 x P_{X|Y}(x|1)$$

$$= \cancel{e} \left( \frac{1}{10} + \frac{4}{10} + \frac{9}{10} + \frac{16}{10} \right)$$

$$= 3.$$