

为级数收敛问题

1. 为级数收敛问题.

$$x(n) = [2, 1, -2] \quad h(n) = [1, 2, -1] \quad y(n) = x(n) * h(n)$$

$$\text{和级数收敛: } y_1 = 2+x-2x^2 \quad y = y_1 \times y_2 = (2+x-2x^2) \times (1+2x-x^2) = 2+5x-2x^2-5x^3+2x^4$$

$$y_2 = 1+2x-x^2$$

$$\therefore y(n) = [2, 5, -2, 5, 2] = x(n) * h(n)$$

2. walsh-hadamard 变换.

$$f = \begin{bmatrix} 1 & 3 & 3 & 1 \\ 1 & 3 & 3 & 1 \\ 1 & 3 & 3 & 1 \\ 1 & 3 & 3 & 1 \end{bmatrix} \quad \text{walsh 变换矩阵} \quad G = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & 1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix}$$

$$\text{① walsh 变换: } w = \frac{1}{N^2} G^T f G = \begin{bmatrix} 0 & 0 & 0 & -4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\text{② Hadamard 变换: } \text{Hadamard 变换矩阵} \quad G = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -1 & 1 & -1 \\ 1 & 1 & -1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix}$$

$$\text{Hadamard 变换: } w = \frac{1}{N^2} G^T f G = \begin{bmatrix} 8 & 0 & 0 & -4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$