Qunfong Wang

1.

$$\begin{array}{l} \alpha \to \beta \\ \gamma \to \delta \end{array}$$

Augmentation

$$\begin{array}{l} \alpha\gamma \rightarrow \beta\gamma \\ \alpha\gamma \rightarrow \alpha\delta \end{array}$$

$$a\gamma \rightarrow a\delta$$

Union

$$\alpha\gamma\to\beta\gamma\delta$$

Decomposition

$$\alpha\gamma\to\beta\delta$$

$$\alpha \gamma \rightarrow \gamma$$

Trivial
$$\alpha \gamma \rightarrow \gamma$$

$$\alpha\gamma\to\beta\delta$$

$$G = \{ A \to CD, E \to AH \}$$

$$F = \{ A \to C, AC \to D, E \to AD, E \to H \}$$

G to F

Decomposition on

 $A \rightarrow CD$ and $E \rightarrow AH$

Result:

 $A \rightarrow C$

 $E \to H$

 $E \to A$

 $A \to D$

Transitivity on

 $E \rightarrow A$ and

 $A \to D$

Result:

 $E \rightarrow D$

After that union on

 $E \rightarrow D$ and

 $E \to A$

Result:

 $E \to AD$

Decomposition on $A \rightarrow CD$

 $A \rightarrow D$

 $A \to C$

Union on

 $A \to D$

 $A \to C$

Result:

 $AC \rightarrow D$

F to G

Reflexivity

 $AC \rightarrow C$

Given

 $AC \to D$

Union on

 $AC \rightarrow C$

 $AC \to D$

Result:

 $AC \rightarrow CD$

```
Given
A \to C
reflexivity
A \subseteq AC
transitivity on
AC \rightarrow A
AC \rightarrow D
Result:
A \to D
Union
A \rightarrow C
A \rightarrow D
Result:
A \to CD
Given
E \rightarrow AD
Given
E \rightarrow H
Union on:
E \rightarrow AD
E \to H
Result:
E \to ADH
Reflexivity
AH \subseteq ADH
Transivity on:
ADH \rightarrow AD
E \to ADH
Result:
E \rightarrow AH
3.
Select distinct cName
From Pustomer c, Purchase p, Store s
Where p.Cid = c.Cid AND s.Sid = p.Sid AND s.SName = "Albert Heijn";
4.
Select distinct SName
From Store as s1, Store as s2
Where s1.Sid <> s2.Sid AND S1.SName = s2.SName
EXCEPT
Select SName
From Store
Where city = "Eindhoven"
```

List the names and ID's of all the customers who in some store bought the whole stock of a certain product.