

# EXERCISE SHEET 26 <SELECTED QUESTION>

②  $\mu = 33$

$\sigma = 2$

$$\frac{x - \mu}{\sigma} = \frac{35 - 33}{2}$$

$$= 1$$

$$\Pr(X > 35) = 1 - \Pr(Z \leq 1)$$

$$= 1 - 0.8413$$

$$= 0.1587 //$$

① a)  $\Pr(Z < z) = 0.1020$

$$z = -2.3 //$$

b)  $\Pr(Z \geq c) = 0.0102$

$$c = -2.32 //$$

c)  $\Pr(-2 \leq Z \leq 2) = \Pr(Z \leq 2) - \Pr(Z \leq -2)$

$$= 0.9772 - 0.0228$$

$$= 0.9544 //$$

d)  $\Pr(-z \leq Z \leq z) = 0.4108$

$$0.4108 = \Pr(Z \leq z) - \Pr(Z \leq -z)$$

$$\text{BTAE } z = 0.54 //$$

③ a)  $\mu = 1000, \sigma = 200$

$$\frac{x - \mu}{\sigma} = \frac{700 - 1000}{200}$$

$$= -1.5$$

$$\Pr(Z \leq -1.5) = 0.0668$$

$$= 6.68\% //$$

b)  $\Pr(Z \leq h) = 0.1003$

$$h = -1.28$$

$$\frac{x-1000}{200} = -1.28$$

$$x = 744 \text{ hours} //$$

⑤ a)  $\mu=5, \Pr(X>7)=0.1056$

$$\frac{7-5}{\sigma} = 1.25$$

$$\sigma = \frac{2}{1.25}$$

$$\sigma = 1.6 //$$

b)  $\Pr(X < 3.992)$

$$\frac{3.992-5}{1.6} = -0.63$$

$$\Pr(Z < -0.63) = 0.2643$$

c)  $\Pr(X < 3.992 | X < 7) = \frac{\Pr(X < 3.992)}{\Pr(X < 7)}$

$$= \frac{0.2643}{1 - \Pr(X < 7)}$$

$$= \frac{0.2643}{1 - 0.1056}$$

$$= 0.2955 //$$

⑦  $\mu=30 \quad \sigma=6$

cost: \$40

sell: \$60

refund: \$30 (< 24 months)

Let  $X$  = lifetime of car battery

If  $X < 24$ :

$$\$60 - \$40 - \$30 = -\$10$$

If  $X \geq 24$ :

$$\$60 - \$40 = \$20$$

$$\Pr(X < 24) = \Pr\left(\frac{X-30}{6} < \frac{24-30}{6}\right)$$

$$= \Pr(Z < -1)$$

$$= 0.1587$$

$$\begin{aligned}\Pr(X > 24) &= 1 - \Pr(X < 24) \\ &= 1 - 0.1587 \\ &= 0.8413\end{aligned}$$

$$\begin{aligned}\text{Mean profit} &= 0.1587 \times (-10) + 0.8413 \times 20 \\ &= \$15.24 \text{ (2dp)} //\end{aligned}$$

$$\textcircled{6} \text{ d) } \Pr(X > x) = 0.8023$$

$$0.8023 = 1 - \Pr(X \leq x)$$

$$\Pr(X \leq x) = 0.1977 = \Pr(Z \leq z)$$

$$z = -0.85$$

$$\frac{x - 5}{1.6} = -0.85$$

$$x = 3.64 //$$