

リメディアル数学 (化学システム工学科) ——— 第1回 2024/4/24 略解

指数・対数

問題 1.

(1) 1.

(2) $\frac{1}{16}$.

(3) $\frac{1}{1024}$.

(4) $7^{5+(-4)} = 7$.

(5) $5^{8-5} = 5^3 = 125$.

(6) $2^{-3 \times 2} = 2^{-6} = \frac{1}{64}$.

(7) $3^{-4} \times 5^{-2} = \frac{1}{2025}$.

別解: $(3^2 \times 5)^{-2} = 45^{-2} = \frac{1}{2025}$

問題 2.

(1) $\sqrt[3]{121}$.

(2) $\frac{1}{\sqrt[3]{5}}$.

(3) $2\sqrt[3]{3}$.

(4) $\sqrt[3]{5^4} = 5\sqrt[3]{5}$.

(5) $\sqrt[3]{18}\sqrt[3]{15} = \sqrt[3]{2 \times 3^2} \sqrt[3]{3 \times 5} = 3\sqrt[3]{10}$.

(6) $(2^5)^{\frac{1}{5}} = 2$.

(7) $\left(\frac{1}{3^4}\right)^{\frac{1}{4}} = \frac{1}{3}$.

(8) $\frac{\sqrt[4]{243}}{\sqrt[4]{3}} = \frac{3^{\frac{5}{4}}}{3^{\frac{1}{4}}} = 3^{\frac{5}{4}-\frac{1}{4}} = 3$.

(9) $((2^3)^{\frac{1}{4}})^{\frac{1}{3}} = 2^{3 \times \frac{1}{4} \times \frac{1}{3}} = 2^{\frac{1}{4}}$.

(10) $17^{\frac{1}{2}} \div 17^{\frac{5}{6}} \times 17^{\frac{1}{3}} = 17^{\frac{1}{2}-\frac{5}{6}+\frac{1}{3}} = 17^0 = 1$.

(11) $13^{\frac{2}{3}} \div 13^{\frac{1}{6}} \times 13^{\frac{1}{2}} = 13^{\frac{2}{3}-\frac{1}{6}+\frac{1}{2}} = 13$.

問題 3.

(1) 3.

(2) -4.

(3) 0.

(4) 5.

(5) -2.

(6) -2.

(7) $\frac{1}{4}$.

(8) $\frac{\log_3 9}{\log_3 \sqrt{3}} = \frac{2}{\frac{1}{2}} = 4$.

(9) $\log_{15}(3 \times 5) = 1$.

(10) $\log_2 \frac{40}{5} = 3$.

(11) $\log_5 \frac{24 \times 54}{6^3} = \log_5 6$.

(12) $\log_3 5 \times \frac{\log_3 27}{\log_3 5} = 3$.

三角関数の値

問題 4.

(1) $\frac{5}{6}\pi$.

(2) $\frac{5}{3}\pi$.

(3) 180° .

(4) 330° .

問題 5.

(1) $\sin \theta = \frac{\sqrt{3}}{2}, \cos \theta = \frac{1}{2}, \tan \theta = \sqrt{3}$.

(2) $\sin \theta = -\frac{1}{\sqrt{2}}, \cos \theta = \frac{1}{\sqrt{2}}, \tan \theta = -1$.

(3) $\sin \theta = 0, \cos \theta = 1, \tan \theta = 0$.

(4) $\sin \theta = 1, \cos \theta = 0, \tan \theta$ は定義されない.

方程式

問題 6.

(1) $x = \pm i$.

(2) $x = \pm \frac{\sqrt{6}}{4}i$.

(3) 解の公式より $x = \sqrt{5} \pm i$.

(4) $\sqrt{6-2\sqrt{5}} = \sqrt{5}-1$ より $x = \pm(\sqrt{5}-1)i$.

(5) $x^4 + x^2 - 12 = (x^2 + 4)(x^2 - 3)$ より $x = \pm 2i, \pm \sqrt{3}$.

(6) $x^3 - 8 = (x - 2)(x^2 + 2x + 4)$ より $x = 2, -1 \pm \sqrt{3}i$.

(7) $x^3 - 4x^2 + 2x + 3 = (x - 3)(x^2 - x - 1)$ より $x = 3, \frac{1 \pm \sqrt{5}}{2}$.

(8) $x^4 + x^2 + 1 = (x^2 + 1)^2 - x^2$
 $= (x^2 + x + 1)(x^2 - x + 1)$ より
 $x = \frac{-1 \pm \sqrt{3}i}{2}, \frac{1 \pm \sqrt{3}i}{2}$.

問題 7.

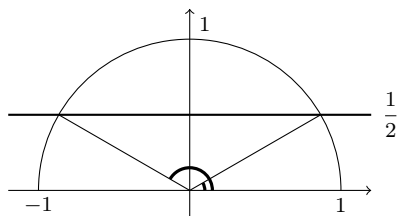
(1) $3^{3x} = 3^2$ より $3x = 2$, つまり $x = \frac{2}{3}$.

(2) $2^{2x} = 2^{x+1}$ より $2x = x + 1$, つまり $x = 1$.

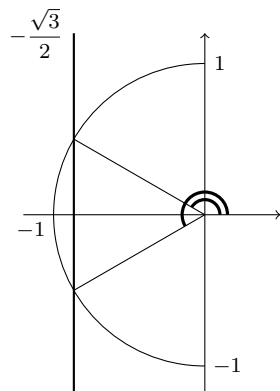
(3) $x = 9$.

(4) $x = \left(\frac{1}{4}\right)^{-\frac{3}{2}} = 8$.

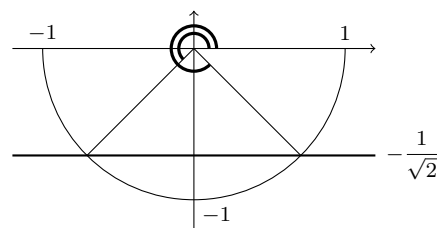
(5) $\sin \theta = \frac{1}{2}$ より, $\theta = \frac{\pi}{6}, \frac{5}{6}\pi$.



(6) $\cos \theta = -\frac{\sqrt{3}}{2}$ より, $\theta = \frac{5}{6}\pi, \frac{7}{6}\pi$.



(7) $\sin \theta = -\frac{1}{\sqrt{2}}$ より, $\theta = \frac{5}{4}\pi, \frac{7}{4}\pi$.



(8) $\theta = \frac{\pi}{4}, \frac{5}{4}\pi$.

