
3. Time and Ordering

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- **Introduction**

- Physical clocks

- Logical clocks

Time

- Time is unambiguous in centralized systems
 - System clock keeps time, all entities use this
- No global time on distributed systems
 - Each node has a (crystal-based) system clock
 - Less accurate than atomic clocks
 - Results in **clock skew** (two clocks, two times) and **clock drift** (two clocks, two count rates)
 - Drifts 1 second every 11 days w.r.t. a perfect clock
 - Problem: An event that occurred after another may be assigned an earlier time
 - Use physical and logical clocks to deal with this

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- Introduction

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- Logical clocks

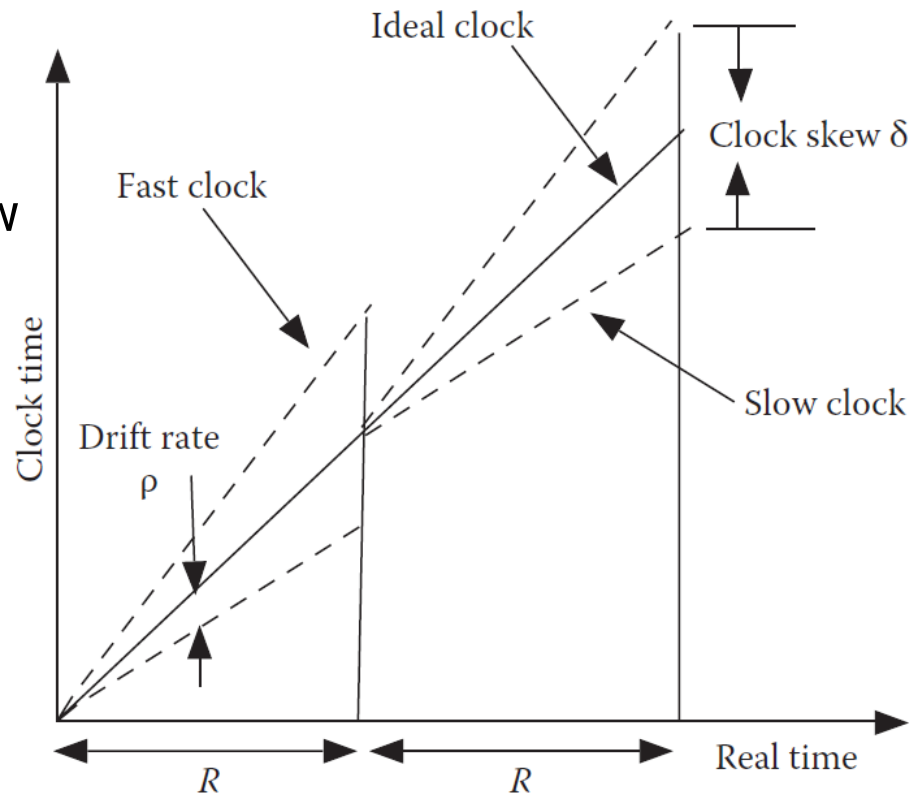
Physical clocks

- Physical clocks allow to synchronize nodes ...
 - i. with a master node (with a UTC receiver)
 - UTC: Universal Coordinated Time is an international standard based on atomic time
 - Broadcasted through short-wave radio and satellite
 - ii. with one another
- ... within a given bound
 - **Perfect** clock synchronization is not feasible
 - Synchronization limited by network jitter and clock drift
 - Typical accuracy of milliseconds

Physical clocks

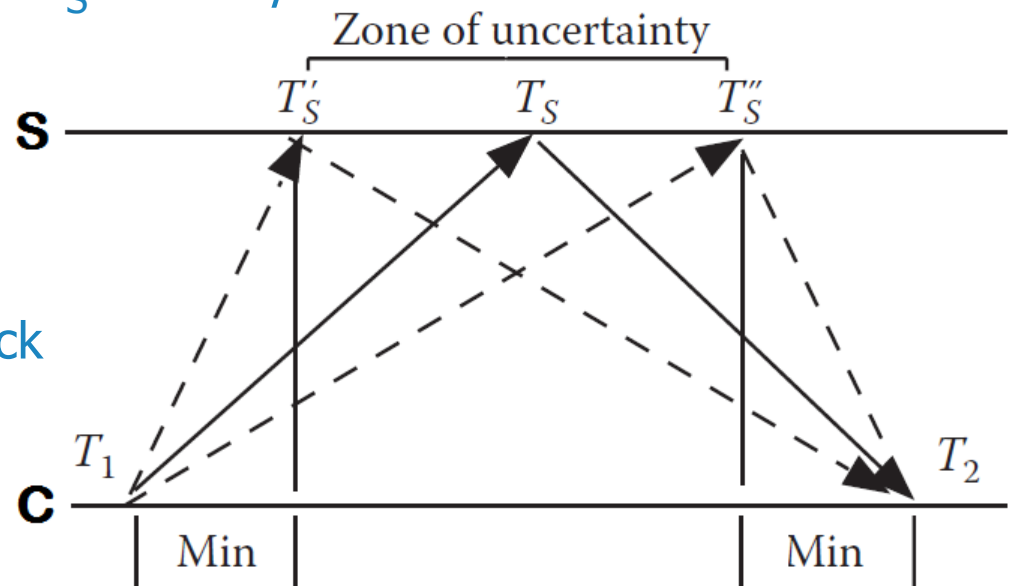
- Synchronize at least every $R < \delta/2\rho$ to limit skew between two clocks to less than δ time units

R : resynchronization interval
 ρ : maximum clock drift rate
 δ : maximum allowed clock skew



Cristian's algorithm

- Synchronize nodes with a server with UTC receiver within a given bound: **External synchronization**
 - Intended for intranets with a UTC-sync server
- 1. Each client asks the time to the server at every R interval
- 2. Client sets the time to $T_s + \text{RTT}/2$
 - RTT: round-trip time
 - $T_2 - T_1$
 - Assumes symmetrical latency
 - Accuracy of client's clock is $\pm(\text{RTT}/2 - \text{Min})$
- NTP is based on a similar concept

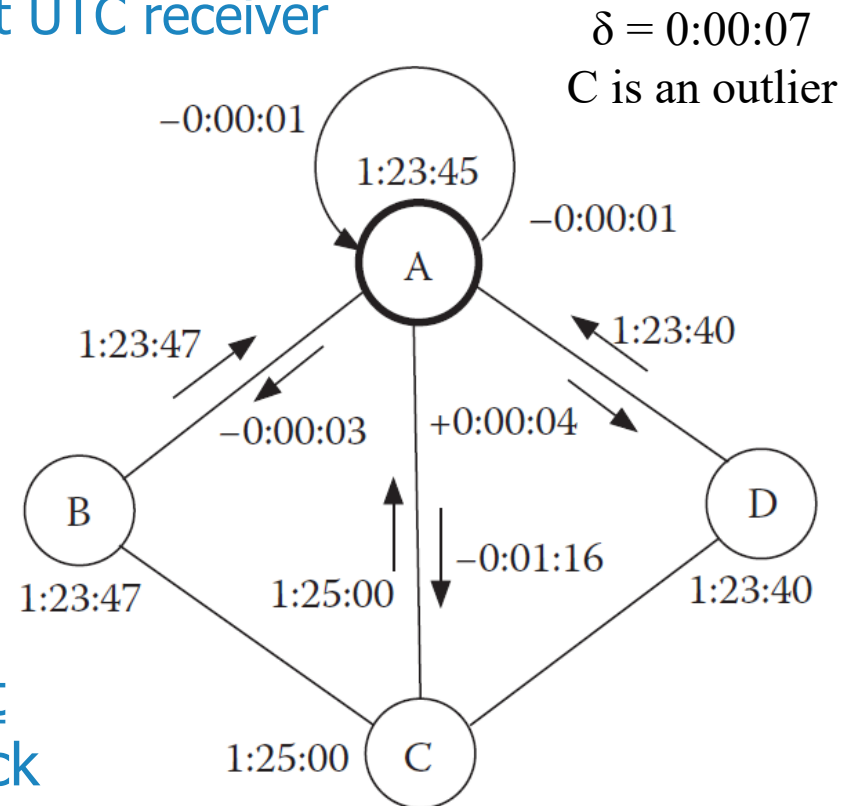


Berkeley algorithm

- Keep clocks synchronized with one another within a given bound: **Internal synchronization**

- Intended for intranets without UTC receiver

- Master polls the clocks of all the slaves at every R interval
 - Adapts them by considering round-trip times
- Master calculates a fault-tolerant average
 - Clocks lying outside the given bound are discarded
- Master sends the adjustment to be made to each local clock



Physical clocks

- Side effects of clock adjustments
 - i. When setting the time forward
 - Some time instants are lost
 - Events scheduled at these times can be affected
 - ii. When setting the time back
 - Monotonicity (time always moves forward) is violated
 - Subsequent events can appear earlier than previous ones
- Workaround: Speed up or slow down local time until the adjustment has been achieved
- Clocks give a real time estimation but cannot deterministically find out the **order** of events

READING REPORT

[Neville-Neil16] Neville-Neil, G.V., *Time Is an Illusion, Lunchtime Doubly So*, Communications of the ACM, Vol. 59, No. 1, pp. 50-55, January 2016

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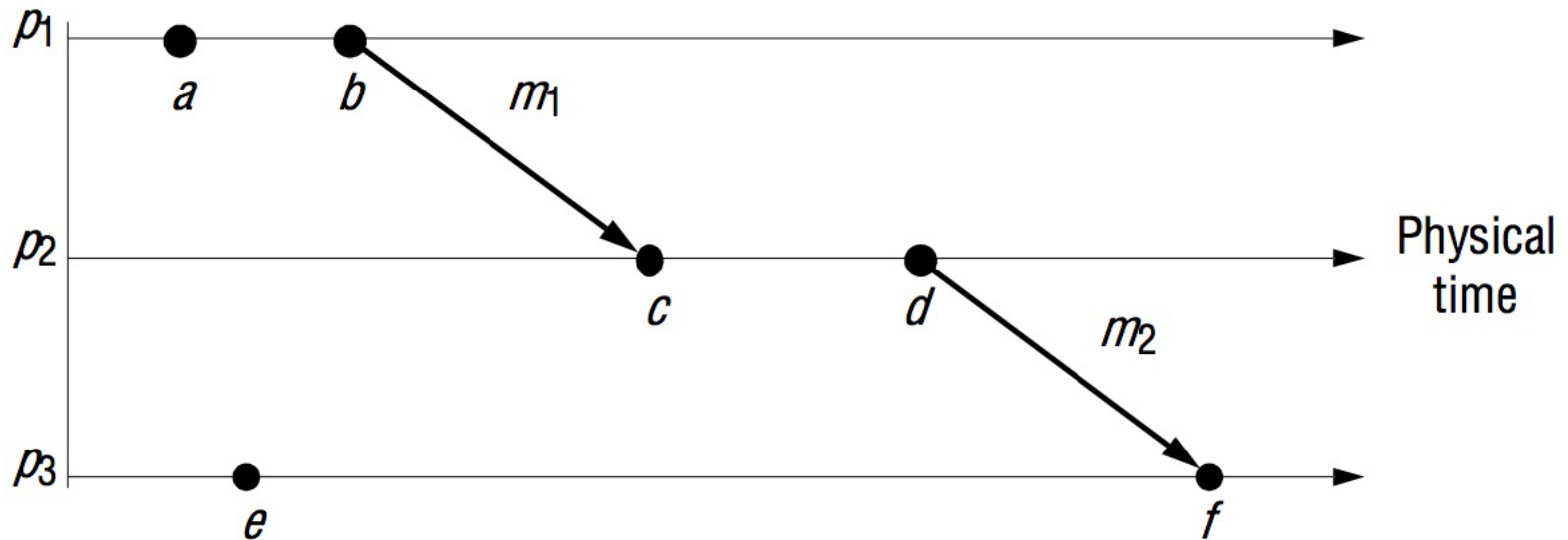
- Introduction
- Physical clocks
- **Logical clocks**

Happened-before relation

- Processes need to know if event 'a' happened before or after event 'b'
 - Agree on the **order** in which events occur rather than the **time** at which they occurred
- The happened-before relation
 - If **a** and **b** are two events in the same process, and **a** comes before **b**, then **a** \rightarrow **b**
 - If **a** is the sending of a message, and **b** is the receipt of that message, then **a** \rightarrow **b**
 - If **a** \rightarrow **b** and **b** \rightarrow **c**, then **a** \rightarrow **c**

Happened-before relation

- Example



$a \rightarrow b, b \rightarrow c, c \rightarrow d, d \rightarrow f, a \rightarrow f$ but $a || e$ (concurrent)

➤ Happened-before relation defines a **partial ordering**

Logical clocks

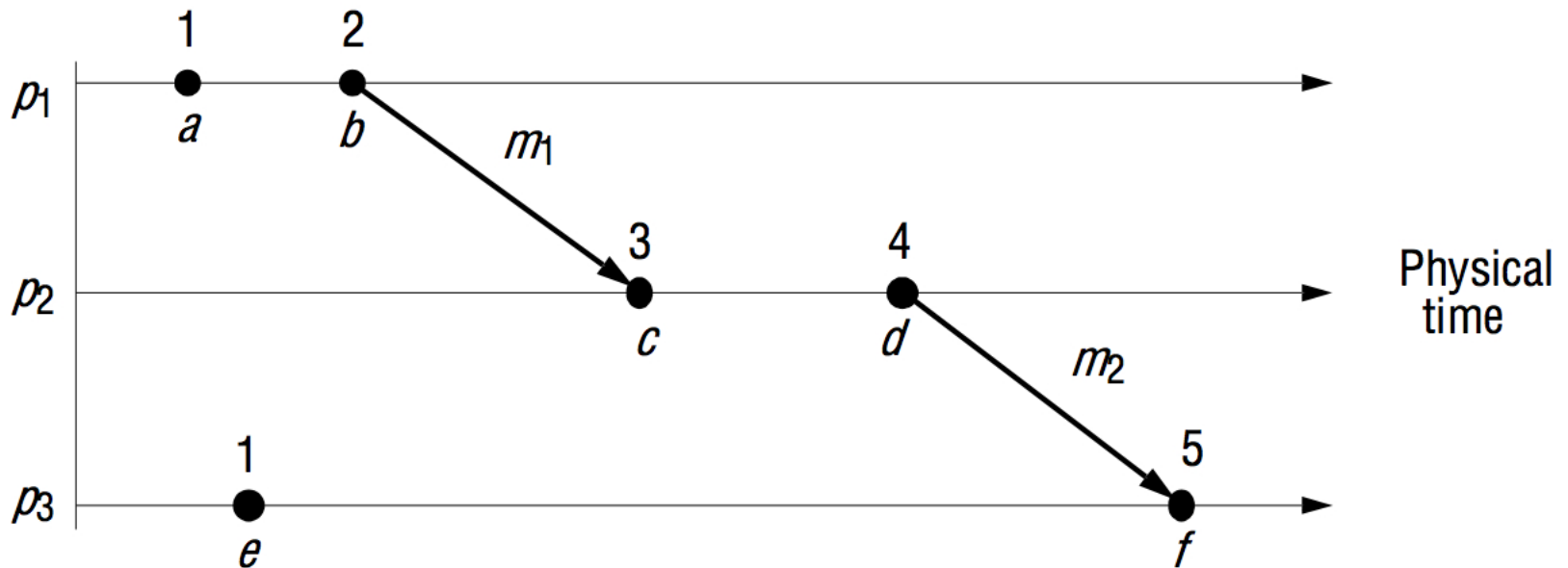
- To capture the happened-before relation, we attach a timestamp $C(e)$ to each event e , satisfying the following properties:
 1. If a and b are two events in the same process, and $a \rightarrow b$, then $C(a) < C(b)$
 2. If a corresponds to sending a message m , and b to the receipt of m , then $C(a) < C(b)$
- How to attach a timestamp to an event when there is no global clock?
 \Rightarrow Use Lamport's logical clocks

Lamport's logical clocks

- Each process P_i maintains a local counter C_i
- C_i is used to attach a timestamp to each event
- C_i is adjusted according to the following rules:
 1. When an event happens at P_i , it increases C_i by 1
 2. When P_i sends message m to P_j , sets $ts(m) = C_i$
 3. When P_j receives m , sets $C_j = \max(C_j, ts(m))$, and then increases by 1

Lamport's logical clocks

- Example



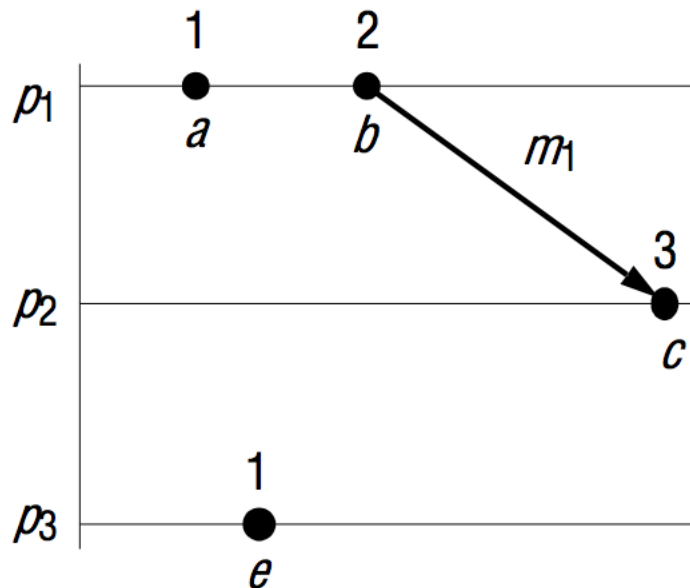
Note that $C(e) < C(b)$ but $b \nparallel e$

Lamport's logical clocks

- Lamport's clocks define a partial order that is consistent with the happened-before relation
 - i.e. it is consistent with causal order
- What if we need totally-ordered clocks?
 - Use Lamport's clocks, but in case two of them are equal, process IDs will be used to break the tie
 - $\{C_i(a), i\} < \{C_j(b), j\}$ iff
 - $C_i(a) < C_j(b)$ OR
 - $C_i(a) = C_j(b)$ AND $i < j$
 - Can be used for instance to order the entry of processes to a critical section

Logical clocks

- Lamport's clocks don't guarantee that if $C(a) < C(b)$ then a causally preceded b ($a \rightarrow b$)



- $C(a) < C(c)$, and ' a ' causally preceded ' c ' ($a \rightarrow c$)
- $C(e) < C(c)$, but ' e ' did not causally precede ' c ' ($c \parallel e$)

⇒ Use vector clocks

Vector clocks

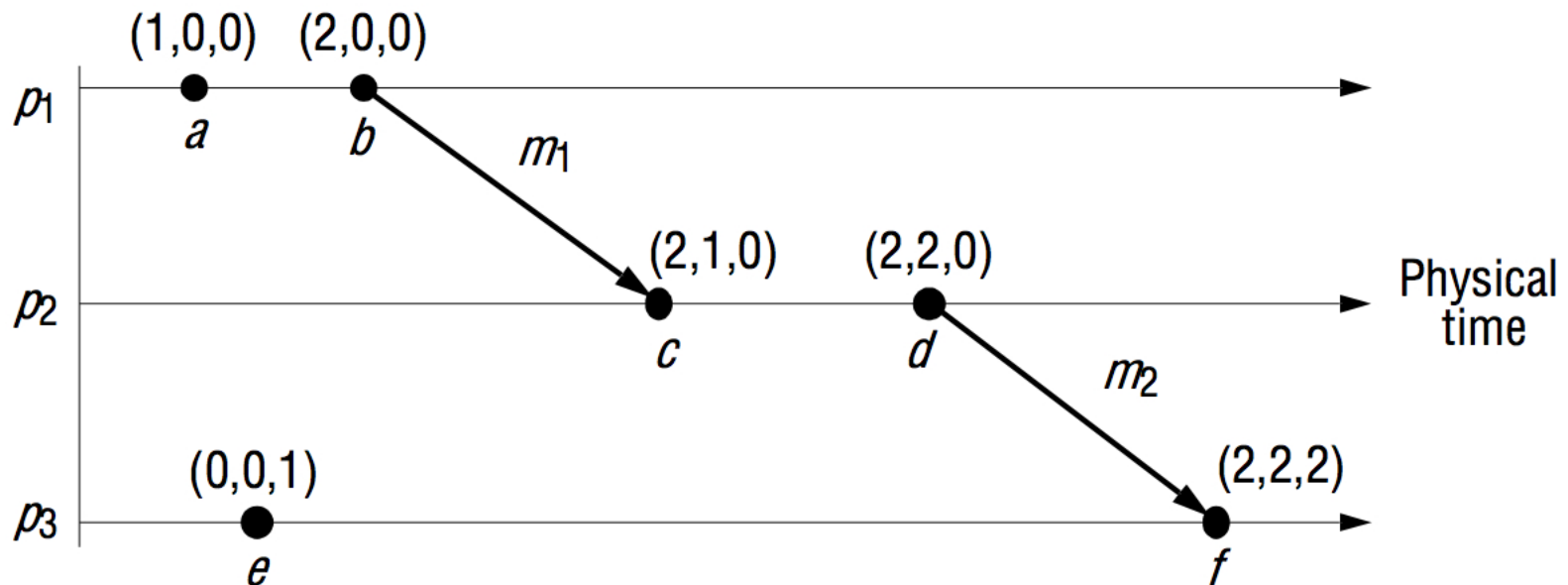
- Each process P_i has an array $VC_i [1...N]$
 - $VC_i [j]$ denotes the number of events that process P_i knows have taken place at process P_j
 - i.e. $VC_i [j]$ is the logical clock of P_j at process P_i
- VC is adjusted as follows:
 1. When P_i sends a message m , it adds 1 to $VC_i [i]$, and sends VC_i with m as vector timestamp $ts(m)$
 2. When P_j receives a message m from P_i , it updates each $VC_j [k]$ to $\max(VC_j [k], ts(m)[k])$, and then increments $VC_j [j]$ by 1

Vector clocks

- Comparing vector clocks to detect causality
($VC(a) < VC(b) \Leftrightarrow a \rightarrow b$)
 - $VC(a) < VC(b)$ iff
 - $VC(a) \leq VC(b)$ & $VC(a) \neq VC(b)$
 - $VC(a) \leq VC(b)$ iff
 - $VC(a)[k] \leq VC(b)[k], k = 1 \dots N$
 - $VC(a) = VC(b)$ iff
 - $VC(a)[k] = VC(b)[k], k = 1 \dots N$

Vector clocks

- Example



Neither $VC(b) \leq VC(e)$ nor $VC(e) \leq VC(b)$, so $b || e$

Summary

- We can synchronize physical clocks, but only within a given bound
- We cannot in general use physical time to find out the order of events
- Use logical clocks to find out events ordering
 - Lamport's clocks: $a \rightarrow b \Rightarrow C(a) < C(b)$
 - Vector clocks: $a \rightarrow b \Leftrightarrow VC(a) < VC(b)$
- Further details:
 - [Tanenbaum]: chapters 6.1 and 6.2
 - [Coulouris]: chapter 14