Hierarchical spatial modelling for applied population and community ecology

Jeffrey W. Doser, Marc Kéry, Gesa von Hirschheydt 24-27 June 2024



Introduction to hierarchical spatial modeling

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What is spatial data?

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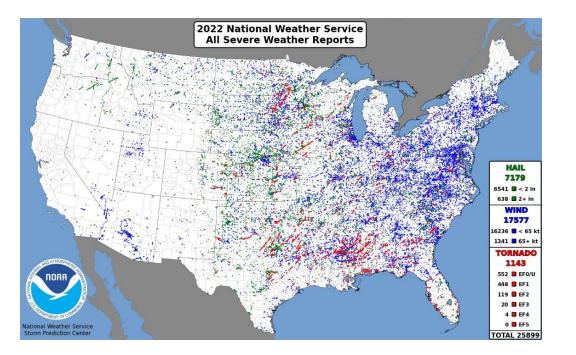
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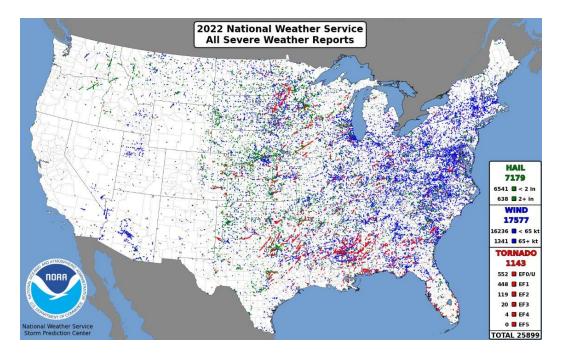
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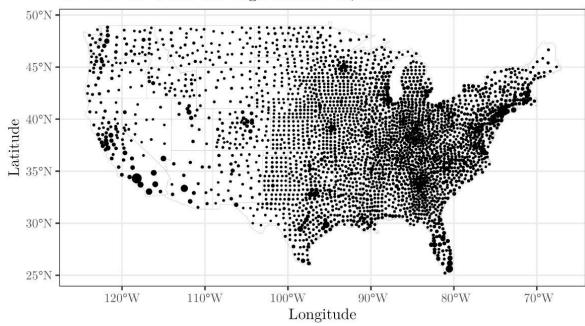
First Law of Geography

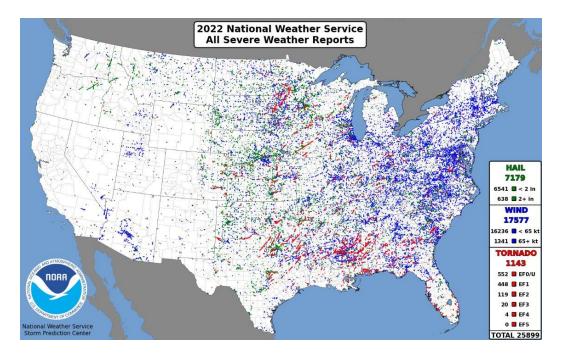
"Everything is related to everything else, but near things are more related than distant things." - Waldo Tobler

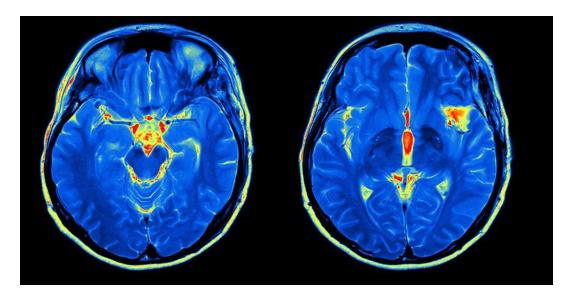




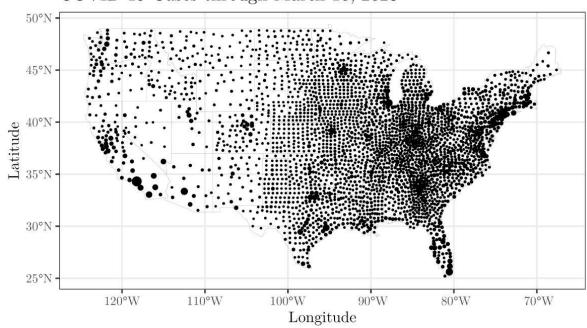
COVID-19 Cases through March 10, 2023

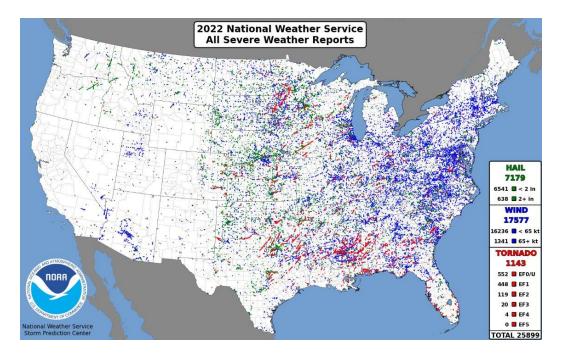


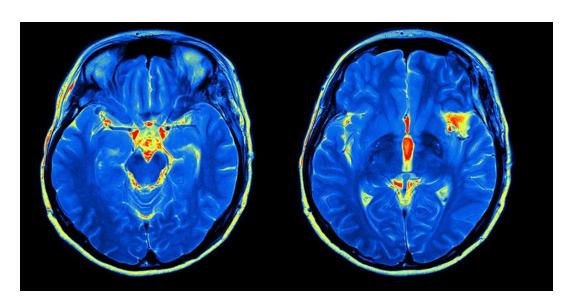




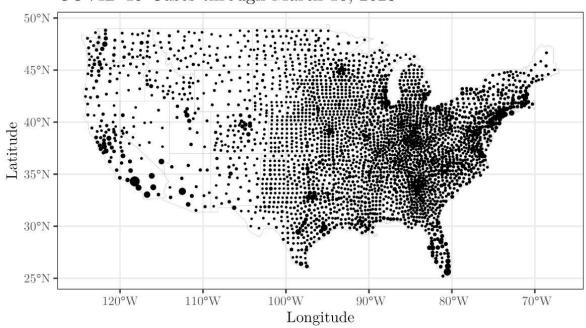
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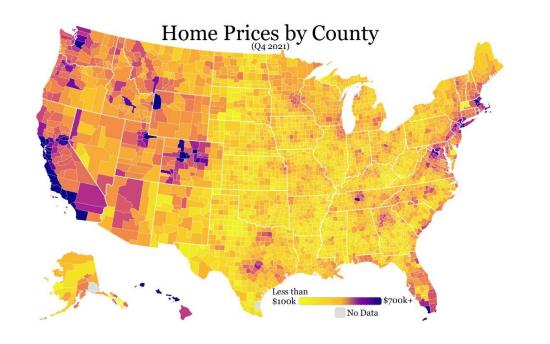






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Three types of spatial data

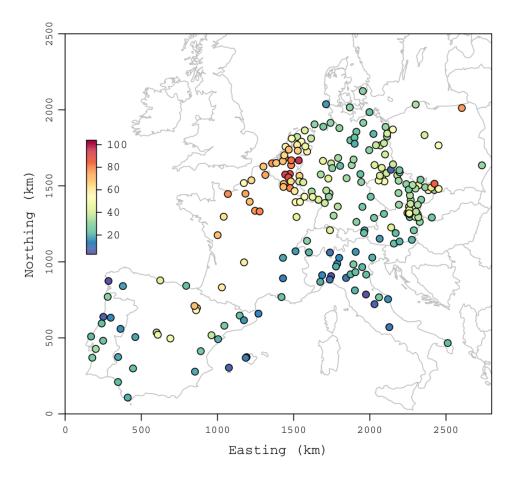
Point-referenced data

Areal data

Point pattern data

Point-referenced data

- Each observation is associated with a location (point)
- Data represents a sample from a continuous spatial domain
- Also referred to as geocoded or geostatistical data

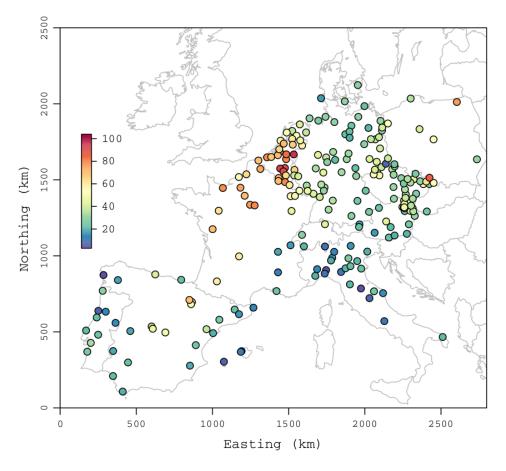


Pollutant levels in Europe in March 2009

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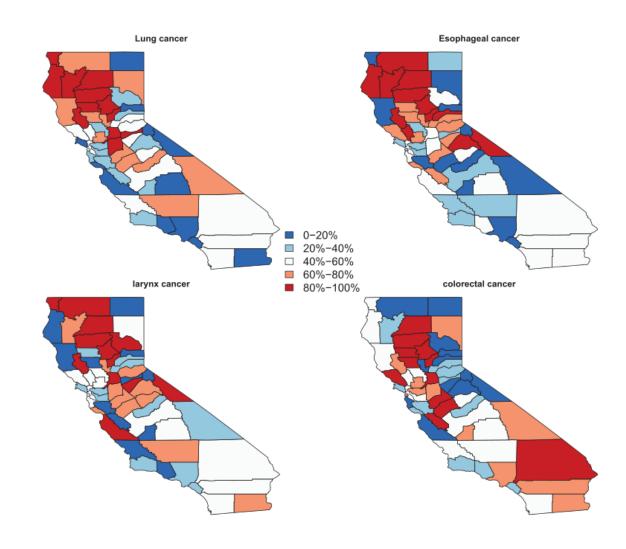
We will focus on methods for point-referenced data.



Pollutant levels in Europe in March 2009

Areal data

- Each observation is associated with an areal unit (of regular or irregular shape)
- Data represents a sample from a discrete spatial domain
- Also referred to as lattice data
- Example: disease incidence rates in California, USA



Gao, Banerjee, Ritz (2022)

Point pattern data

- Locations of the data points themselves are random
- Data set is often just the locations of the points
- Also called point process data
- If there is covariate information along with the points, called a marked point process
- Example: most presence-only data sets



Gelfand and Shirota (2022) Ecological Monographs

Point-referenced spatial modelling

- Modelling of point-referenced data collected at locations referenced by coordinates (e.g., lat-long, Easting-Northing).
- Also relevant for modelling of areal data (e.g., use the areal unit centroid), but not always ideal.
- We will model detection-nondetection and count data using pointreferenced spatial regression models

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 - 4. Area of interest is often large relative to the actual sampled area.

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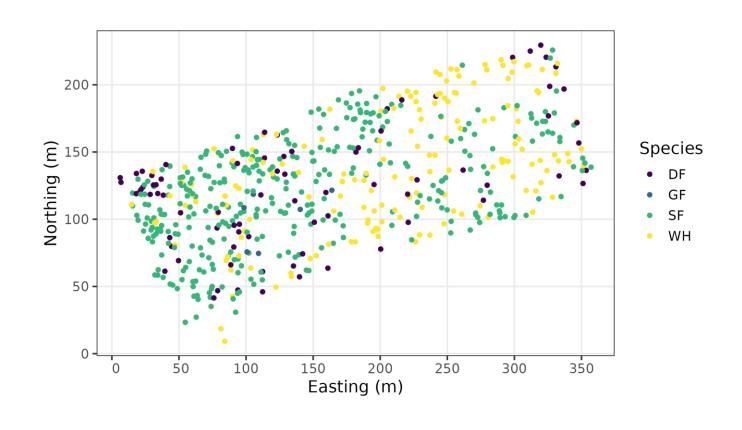
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- Recall our basic assumption that the residuals in a linear model are IID (independent and identically distributed).
- Alternatively, can say that $y(\mathbf{s}_i)$ are conditionally independent given the covariates included in the model.

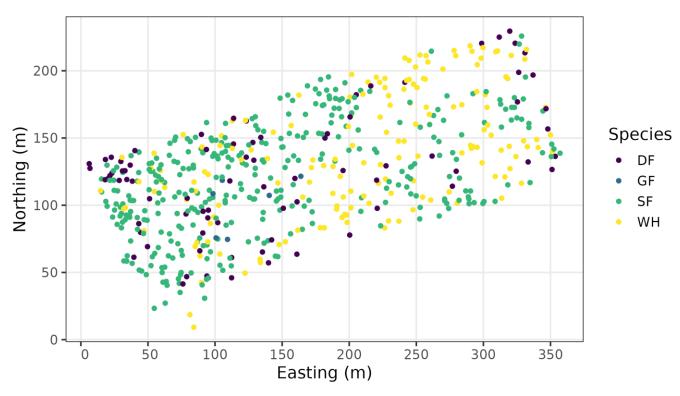
Example: Western Experimental Forest (WEF) data

- 600 trees measured across a 10 ha forest stand in Oregon, USA
- Objective: Predict diameter at breast height (DBH) of all trees across the stand
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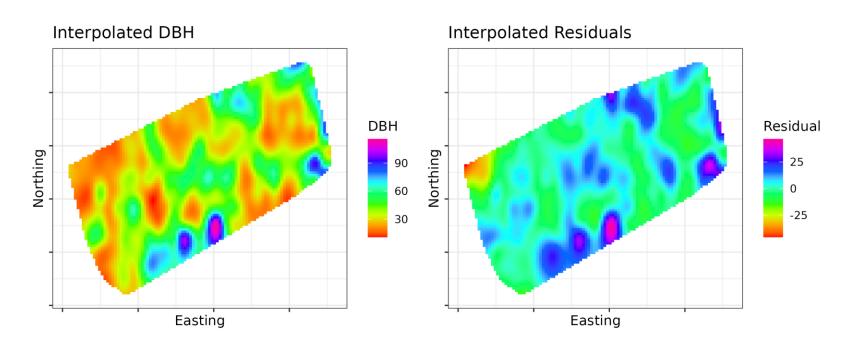
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Classical geostatistics: residual plots

- Surface plots of the residuals help to identify any spatial patterns left unexplained by the covariates
- Local spatial patterns are still evident in residual plots. Basic linear model does not seem sufficient



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- Overall concept: if the sqaured difference between any two data points gets larger as the distance between points increases, this implies a spatial correlation.

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If the value on the left gets larger as the distance between \mathbf{s}_j and \mathbf{s}_k increases, there is spatial correlation.

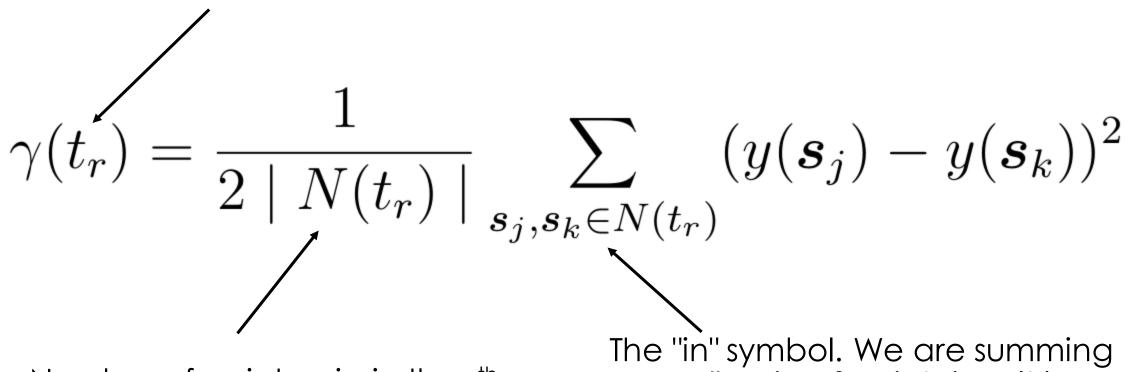
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- 4. Repeat for all intervals to give a set of values across distances that you can use for plotting

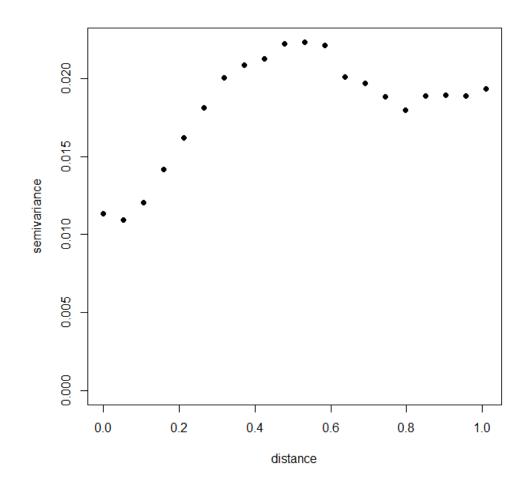
Midpoint of the r^{th} distance bin



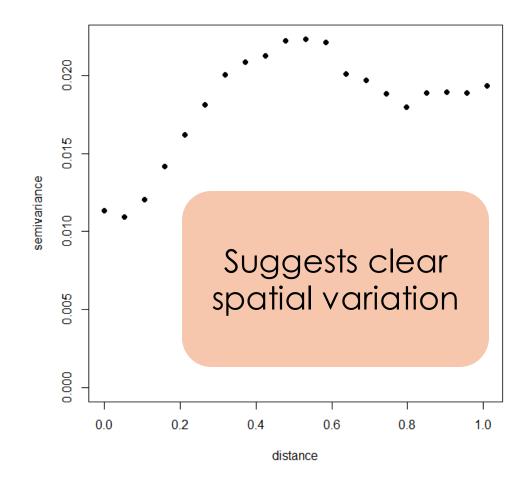
Number of point pairs in the r^{th} distance bin

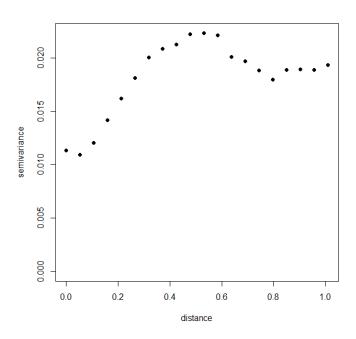
The "in" symbol. We are summing over all pairs of points in $N(t_r)$

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- A flat semivariogram would suggest little spatial variation

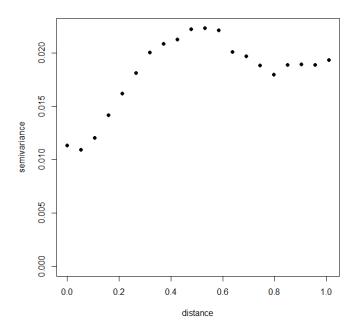


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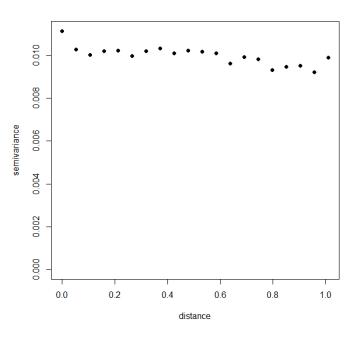




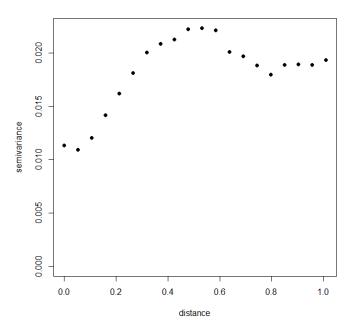
Response variable



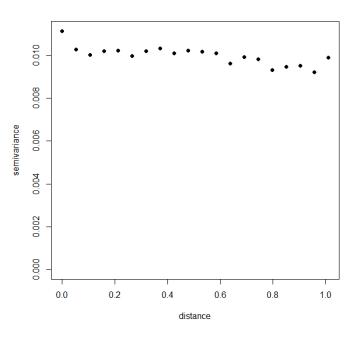
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Residuals



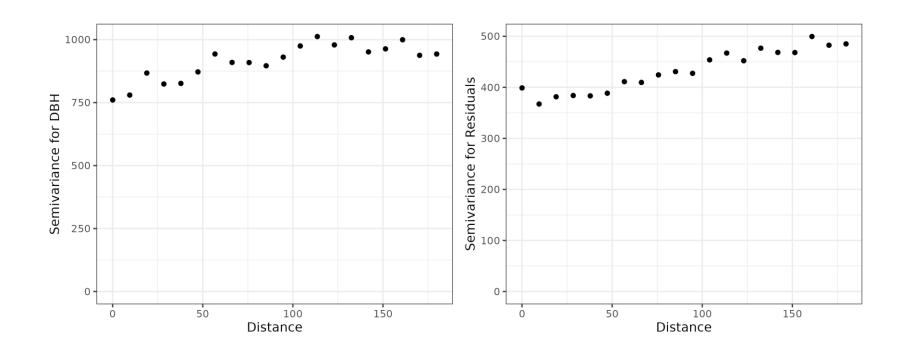
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Residuals

Residuals show little pattern. A simple linear model is adequate.

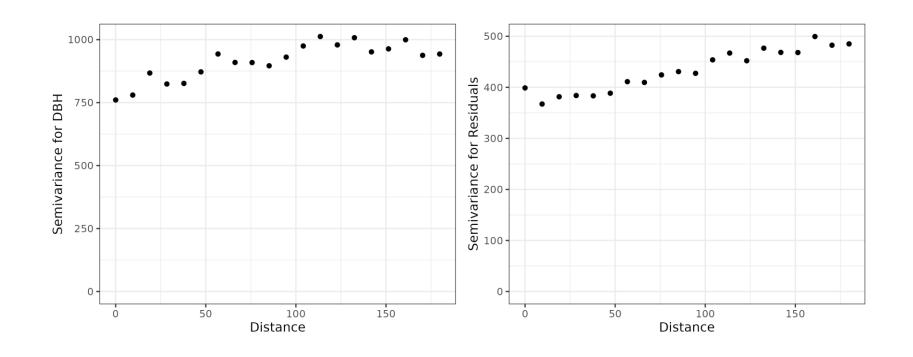
WEF Example



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- Allow us to account for Residual Spatial Autocorrelation (i.e., spatial correlation in the response that is not explained by the covariates)

Spatial random effect

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- How to choose the form of w(s)?
- We want to choose w(s) such that we can easily predict and make smooth maps.
- We will choose w(s) to be a surface.

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- So, what does all this mean for our random effects?

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Spatial covariance matrix

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 - A covariance function

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- We will focus primarily on using the exponential covariance function

Exponential covariance function

 Covariance between site A and site B using exponential covariance function:

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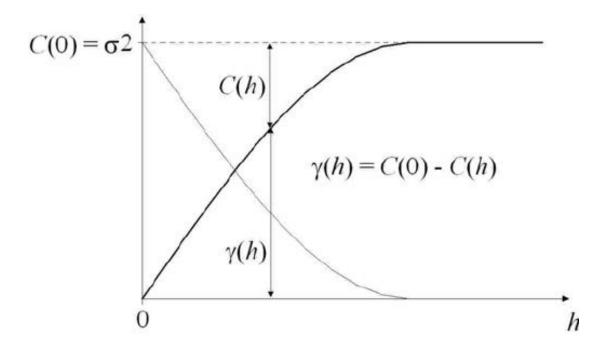
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- ϕ Spatial decay. Controls how quickly the correlation between sites decays across space.
- "Effective spatial range" when using an exponential covariance function. This is the distance at which the spatial correlation between two sites is essentially negligible (0.05)

Covariance functions and semivariograms

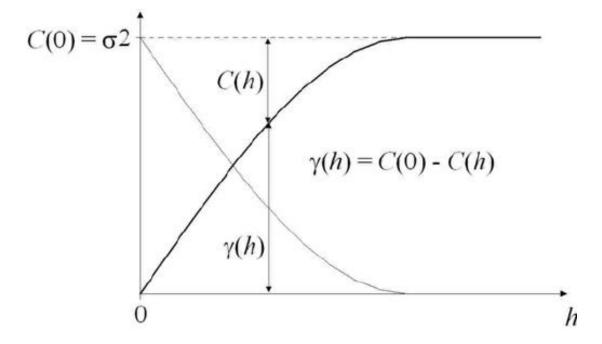
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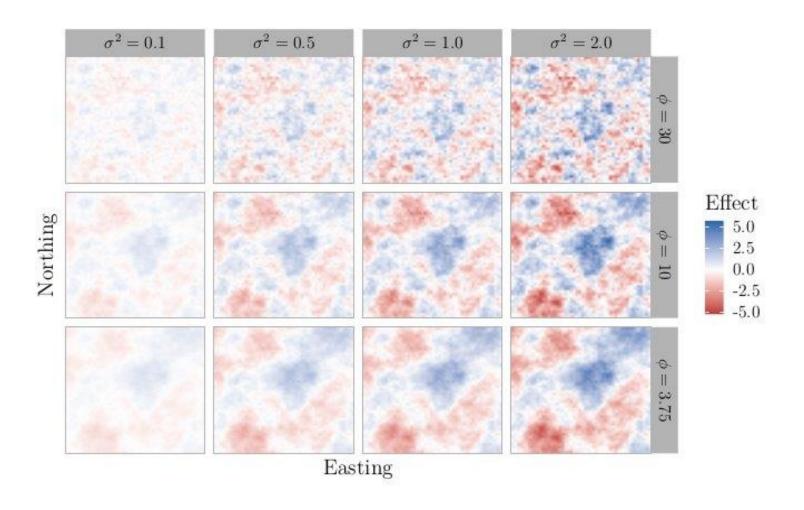
Covariance functions are intuitive: things closer together have higher correlation, things farther away have lower correlation.



Spatial Gaussian processes

$$C(d_{A,B}, \sigma^2, \phi)) = \sigma^2 \exp(-\phi d_{A,B})$$

Maps of the resulting spatial random effects (w) under different parameter values



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> Danie Krige

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- The Bayesian approach is highly preferred (and I promise it's not just me saying that!).
- Frequentist approaches (ML, REML) do not adequately account for uncertainty in the estimates of the spatial variance and spatial decay parameters. Leads to overly precise predictions

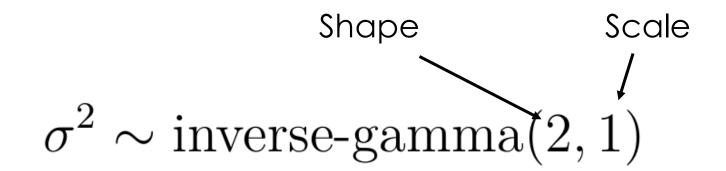
Bayesian spatial linear model

- Assign prior distributions to all parameters and fit the model using MCMC.
- The two spatial parameters (ϕ and σ^2) are notoriously difficult to estimate separately from each other (Zhang, 2004 JASA).
- Priors become important. In spOccupancy and spAbundance, we use the following:
 - ο φ: A mildly informative uniform prior
 - \circ σ^2 : A vague inverse-gamma prior

Default priors on spatial parameters

- Default priors allow the effective spatial range to be anywhere from the maximum inter-site distance in the data set to the minimum inter-site distance.
- Fairly uninformative: allows for broad-scale and fine-scale spatial autocorrelation
- Can be made more informative by changing d_{max} and d_{min} to other values.

Default priors on spatial parameters



- Sets the prior mean of the spatial variance to 1 (moderate amount of spatial variation) with an infinite variance.
- When the shape = 2, the prior variance is infinite and the prior mean is equal to the scale.

Exercise: Western Experimental Forest

2-spatial-linear-model-wef.R





Pros to fitting spatial models

- More accurate predictions at new locations (i.e., more accurate maps)
- More accurate uncertainty estimates
- Visualizing spatial random effects can provide insight on underlying drivers
- Help to generate new hypotheses



Cons to fitting spatial models

- Substantially slower (we will address this shortly).
- Convergence can be difficult to achieve without informative priors on spatial parameters.
- Generally requires more data (i.e., spatial replication) than non-spatial models.
- Spatial confounding



Spatial confounding

- Covariates in your spatial model may be highly correlated with the spatial random effects, which can lead to difficulties when interpreting the covariate effect.
- Same concept as checking correlation between covariates between fitting a model (except one covariate is the spatial random effect).
- Some spatial models try to explicitly eliminate this problem (i.e., restricted spatial regression), but the benefits of this approach are highly debated.

Literature on spatial confounding

General

Adding Spatially-Correlated Errors Can Mess Up the Fixed Effect You Love

James S. Hodges & Brian J. Reich

Pages 325-334 | Received 01 Mar 2010, Published online: 01 Jan 2012



Statistical Practice

On Deconfounding Spatial Confounding in Linear Models

Dale L. Zimmerman 🛂 🕞 & Jay M. Ver Hoef

Pages 159-167 | Received 26 Feb 2021, Accepted 12 Jun 2021, Published online: 26 Jul 2021



Research article

Spatial confounding in Bayesian species distribution modeling

Jussi Mäkinen, Elina Numminen, Pekka Niittynen, Miska Luoto and Jarno Vanhatalo

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- 2. Plot the estimates of the spatial random effect and compare with the covariates. Are they highly correlated?
- 3. Compare estimated effects in spatial model to those in non-spatial model. Are there drastic differences?
- 4. Use more informative priors to reduce the spatial confounding. Read Mäkinen et al. 2022 for specific details.