Handwritten digit recognition using Python

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Introduction

Machine Learning is "the field of study that gives computers the ability to learn without being explicitly programmed." - Arthur Samuel

Machine Learning has a vast number of application in a number of fields, from computer science all the way to the medical field.

This project focuses on one specific application: image recognition.

The purpose of the project

The aim of this project is to recognize handwritten digits (drawn via a mouse on a canvas).

The stakeholders

This project is only a proof-of-concept. It is aimed at other individuals interested in machine learning, hoping that they might learn a thing or two from it.

System requirements

- RAM: at least 200 MB
- CPU: any CPU made after the year 2000

Theoretical background

Model used

The machine learning model used for this project is: **logistic regression**. The reason why this model was used is because the given application requires classification.

This model, as any other machine learning model, tries to fit the dataset with a polynomial.

Given a dataset and classes A and B, this model can predict with a certain probability that a value X is in class A or class B.

The hypothesis function

The hypothesis function for this model is

$$h_{\theta}(x) = g(\theta^T x)$$

The only difference between this hypothesis function and the linear regression's hypothesis function is the use of the $g(z) = \frac{1}{1+e^{-z}}$ function.

The g function, also known as the sigmoid or logistic function, makes it so that our output is in the (0,1) interval. Otherwise we could not interpret our output as a probability.

The cost function

The cost function J is

$$J(\theta) = -\frac{1}{m} * \left[\sum_{i=1}^{m} y^{(i)} log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) log (1 - h_{\theta}(x^{(i)})) \right]$$

The actual learning part of this algorithm is minimizing this cost function. We take the θ value at the function's minimum and use that for our hypothesis function.

Prediction

If the output of our hypothesis function is > 0.5 then we predict 1, otherwise we predict 0. This means that we can only classify a given value into two classes.

Multiple classes

In our case we need to classify the values in 10 different classes $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$. To solve this, we will have 10 different logistic regression models, one for each digit. This means that we will have 10 different hypothesis functions. To decide in which class to classify the given handwritten digit, we need to evaluate it in all 10 of the hypothesis functions. The digit will be put into the class, where its evaluated value is the highest (it is the most probable that it belongs to that class)

$$\max(h_{\theta}^{0}(x),h_{\theta}^{1}(x),h_{\theta}^{2}(x),h_{\theta}^{3}(x),h_{\theta}^{4}(x),h_{\theta}^{5}(x),h_{\theta}^{6}(x),h_{\theta}^{7}(x),h_{\theta}^{8}(x),h_{\theta}^{9}(x))$$

Illustrative example

This example was taken from Andrew NG's Machine Learning Coursera course, which can be found here We have a dataset with two features: exam1 score and exam2 score and a pass/fail label based on these exam scores. See figure 1

When we minimize the cost function J the θ values we get we can use for the hypothesis function h to predict whether a student will pass, based on his two exam scores. If we were to plot the hypothesis function, it would look as such See figure 2

Here we can clearly see that students with exam scores that would place them in the upper-right part of the plot, have a high chance of passing, while the students in the lower-left corner have a high chance of failing.

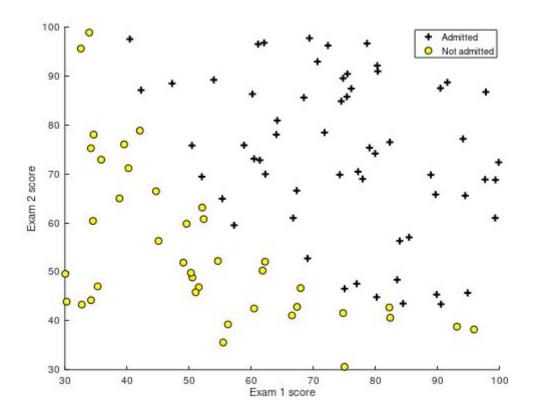


Figure 1: Dataset

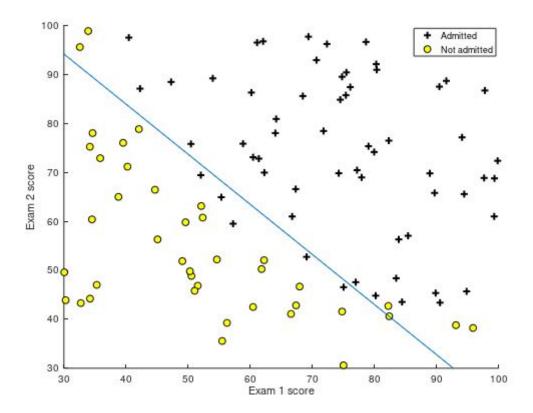


Figure 2: Fitted dataset

Functional requirements

The script should be able to recognize a given handwritten digit with a reasonable accuracy.

Non-functional requirements

The graphical user interface should be simple and easy to use. The following wireframe shows how the GUI was specified to look. See figure 3

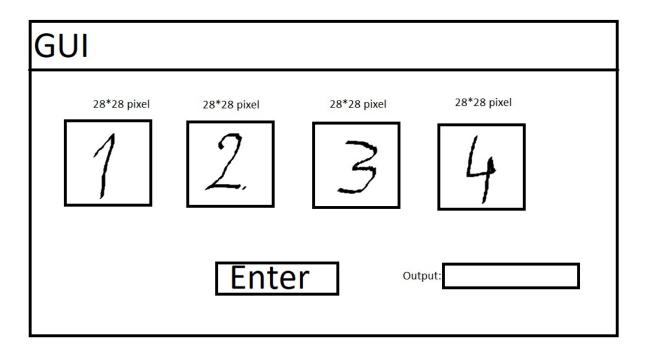


Figure 3: Wireframe

Implementation

Logistic regression applied

System diagram

Our system consists of python scripts. The following system diagram describes its operation. See figure 4

Machine learning

Data formatting

Graphical User Interface

The task was to create a Graphical User Interface (GUI) based on the specified wireframe. The kivy python package was used for achieving this task. The GUI is written in python while also using the features of the kivy language. This script provides the skeleton for the whole project. This is where the other scripts are invoked (formatting.py and evaluate.py).

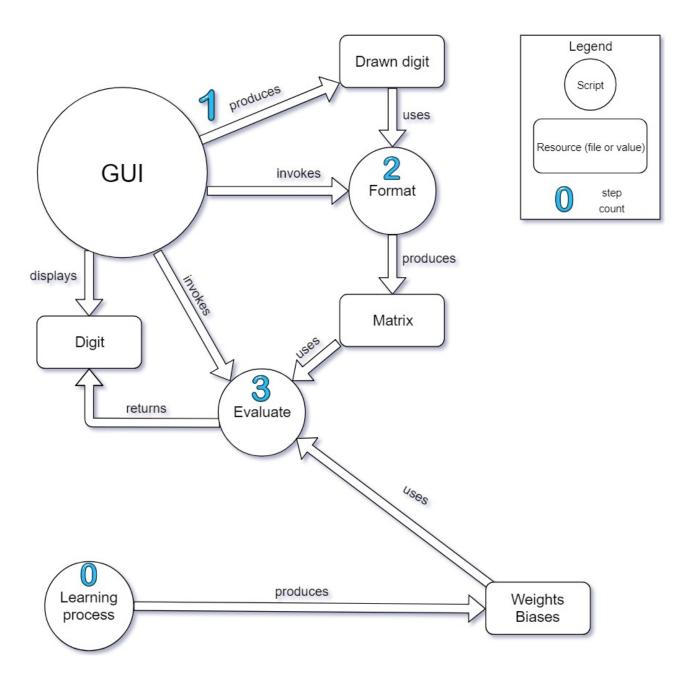


Figure 4: System diagram

This GUI provides three separate canvases to draw on. By clicking the 'Save' button, the drawings on the canvases get converted to png image files and are save to the res folder

User guide

After opening the application, it becomes possible to draw on each of the three canvases. Figure 5

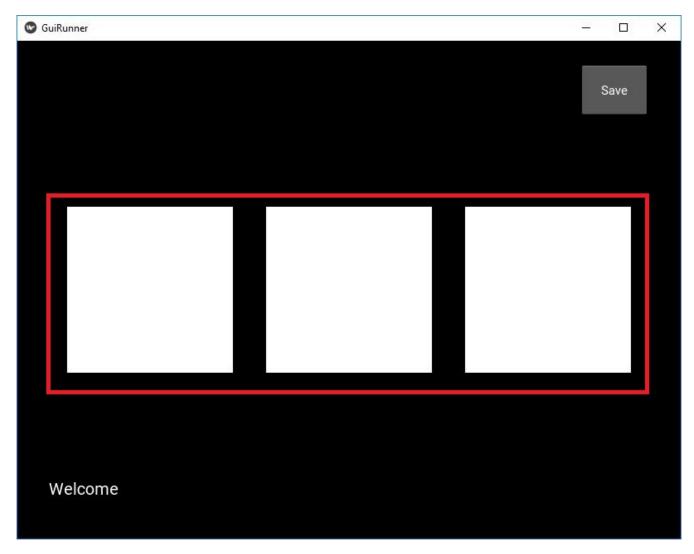


Figure 5: $Opening\ screen$

It is not obligatory to draw on every canvas. After the drawing took place, the 'Save' button should be pushed. Figure 6

After the 'Save' button was pushed, the result gets displayed in the lower-left corner. Figure 7



Figure 6: Save button

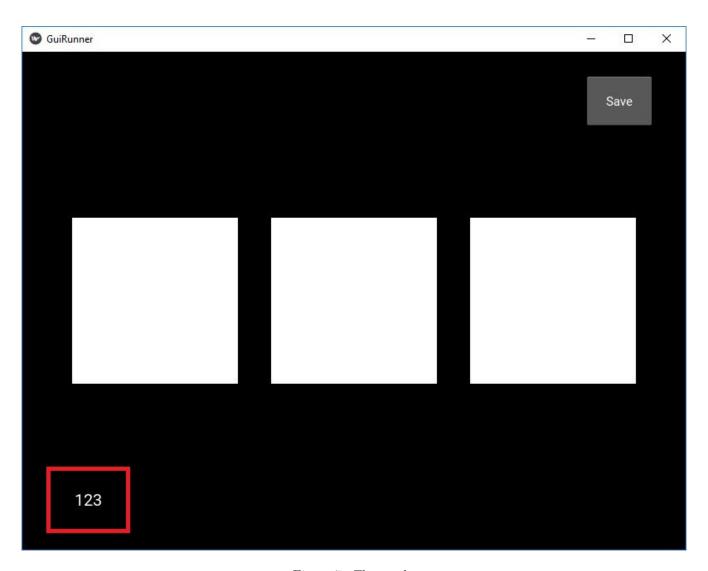


Figure 7: The result