ALGT - The manual

Pieter Vander Vennet

Contents

Overview

This document gives an overview of the ALGT-tool. First, a general overview of what the tool does is given and why it was developed. Second, a hands-on tutorial develops a Simply Typed Functional Language (STFL). Thirdly, the reference manual gives an in-depth overview of the possibilities and command line flags. Fourth, some concepts and algorithms are explained more thoroughly, together with properties they use. And at last, the dynamize and gradualize options are explained in depth, as these are what the master dissertation is about.

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What is ALGT?

ALGT (Automated Language Generation Tool ¹) is a tool to formally specify any programming language. This is done by first declaring a syntax, using BNF, and then declaring semantics by introducing logical deduction rules, such as evaluation or typing rules. Eventually, properties can be introduced which can be tested. Of course, these can be run.

The tool is kept as general as possible, so any language can be modelled.

2.1 Declaring the syntax

For a full reference on syntax, see the reference manual on syntax.

2.1.1 Simple booleans

A program is nothing more then a string of a specific form. To describe strings of an arbitrary structure, BNF² can be used.

The syntax of our programming language is defined in the **Syntax**section of *STFL.language*:

```
1 STFL
3 ******
4 5 # A Simply Typed Functional Language
6 7 Syntax
8 =======
```

What do we write here? Let's start with declaring the boolean values True and False. We express how these can be parsed by writing bool ::= "True" | "False". This tells the tool that a syntactic form named bool exists and it is either True of False. Note the double quotes, these are important to indicate that we want this string literally. The | epxresses that it can choose between those forms.

STFL.language now looks like:

```
1 2 STFL
3 ******
4 5 # A Simply Typed Functional Language
6 7 Syntax
8 =======
9 10 bool ::= "True" | "False"
```

Lets try running this! Create examples.stfl, which contains:

 $^{^{1}}$ Note the similarity of ALGT and AGT. The tool started its life as AGT, based on the paper $Abstracting\ Gradual\ Typing$. When it became more general, another name and acronym was chosen.

²Backus-Naur-form, as introduced by John Backus in the ALGOL60-report.

```
1 | True 2 | False
```

We can parse these by running (in your terminal) ./ALGT STFL.language examples.stfl bool -1. The first argument is the language file, the second the examples, the bool tells ALGT what syntactic rule to parse. The -1 flag expresses that each line should be treated individually.

If all went well, you should get the following output:

```
# "True" was parsed as:
True bool.0
# "False" was parsed as:
False bool.1
```

The most interesting part here is that True has been parsed with bool.0, thus the first choice of the bool-form, while False has been parsed with the second form.

2.1.2 If-statements

Now, let's add expressions of the form If True Then False Else True. We define a new syntactic form: expr ::= "If" bool "Then" bool "Else" bool. This tell ALGT that an expression starts with a literal If, is followed by a bool (so either True or False), is followed by a literal Then, . . . The tool uses the double quotes " to distinguish between a literal string and another syntactic form.

STFL.language now looks like:

```
1
2
     STFL
3
4
   # A Simply Typed Functional Language
5
6
7
     Syntax
8
9
10
            ::= "True" | "False"
   bool
            ::= "If" bool "Then" bool "Else" bool
11
```

This captures already some example expressions. Let's add If True Then False Else True to examples.stfl:

```
1 | True
2 | False
3 | If True Then False Else True
```

Let's run our tool, this time with ./ALGT STFL.language examples.stfl expr -1

```
"examples.stfl (line 0)" (line 1, column 1):
unexpected "T"
expecting "If"
Could not parse expression of the form expr
"examples.stfl (line 1)" (line 1, column 1):
unexpected "F"
expecting "If"
Could not parse expression of the form expr
"examples.stfl (line 2)" (line 1, column 4):
unexpected "T"
expecting "If"
Could not parse expression of the form expr
```

Oops! Seems like our parser now always wants to see a If in the beginning, and can't handle True anymore. Perhaps we should tell that a bool is a valid expression to:

³Don't worry about spaces and tabs, we deal with them. If you want need to parse stuff like "duizendeneen" or whitespace sensitive languages, please refer to the reference manual

```
6 expr ::= "If" bool "Then" bool "Else" bool
7 | bool
```

Lets see what this gives:

```
+ If expr.0
| True bool.0
| Then expr.0
| False bool.1
| Else expr.0
| True bool.0
```

Looks a lot better! The third example shows clearly how the expression falls apart in smaller pieces. What with a nested If?

If If True Then False Else True Then True Else False clearly can't be parsed, as the condition should be a bool, according to our current syntax.

Well, we can just write expr instead of bool in our syntax:

```
1 expr ::= "If" expr "Then" expr "Else" expr 2 | bool
```

Running this gives

```
If True Then False Else True Then True Else False" was parsed as:
             expr.0
             expr.0
   Ιf
             bool.0
   True
   Then
             expr.0
   False
             bool.1
   Else
             expr.0
   True
             bool.0
Then
             expr.0
True
             bool.0
Else
             expr.0
False
             bool.1
```

This clearly shows how the parse trees are nested. This can be rendered too:⁴

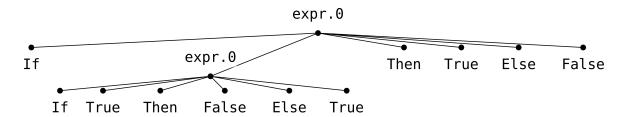


Figure 2.1: ParseTree of a nested condition⁵

2.1.3 Adding numbers, subtyping and forbidden left recursion

Time to spice things up with numbers. To make things easier, integers are built in as Number. It's good practice to introduce a new syntactic rule for them:

```
1 | int ::= Number
```

As an int is a valid expression, we add it to the expr form:

```
1 | expr ::= "If" expr "Then" expr "Else" expr 2 | bool 3 | int
```

Note that every int now also is an expr, just as every bool is an expr. This typing relationship can be visualized with ALGT STFL.language -lsvg Subtyping.svg⁶:

 $^{^4\}mathrm{These}$ images can be created with ALGT STLF.language examples.stfl -l --ptsvg Outputname

 $^{^5\}mathrm{These}$ images can be created with ALGT STLF.language examples.stfl -l --ptsvg Outputname

⁶Creating this svg might take a long time for complicated syntaxes, as ALGT calculates the ordering of labels resulting in the least intersecting lines.

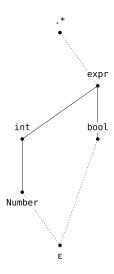


Figure 2.2: Subtyping relation of STFL.language

Now that numbers have been added, let's run this with a number as example:

1 42

should give

```
# "42" was parsed as:
42 Number.0
```

So far, so good! Time to add addition:

```
1 | expr ::= "If" expr "Then" expr "Else" expr 2 | bool 3 | int
```

expr "+" expr

We add some example:

```
1 | 20 + 22
2 | 1 + 2 + 3
```

And run it:

```
Error:
While checking file STFLrec.language:
While checking the syntax:
Potential infinite left recursion detected in the syntax.
Left cycles are:
expr -> expr
```

Oops! Looks like we did something wrong. What is this left recursion? Whenever the parser wants to parse an expression, it tries every choice from left to right. This means that whenever it tries to parse expr, it should first try to parse expr. That's not really helpfull, so the parser might get in an infinite loop then.

Not allowing left recursion also means that no loops in the subtypings occur. In other words, the subtyping relationship is a lattice.

The solution to this problem is splitting expr in two parts: a term with simple elements in front, and expr with advanced forms:

Let's retry this:

```
Error:

While checking file STFLWrongOrder.language:

While checking the syntax:

While checking for dead choices in expr:

The choice 'term "+" expr' will never be parsed.

The previous choice 'term' will already consume a part of it.

Swap them and you'll be fine.
```

What went wrong this time? The parser tries choice after choice. When parsing 20 + 22 against expr ::= term | term "+" term, it'll first try term (and not term "+" term). It successfully parses 20 against the lonely term, thus the input string + 22 is left. The parser doesn't know what to do with this leftover part, so we get an error.

To fix this, we change the order:

```
1 | expr ::= term "+" expr | term
```

When we try again, we get:

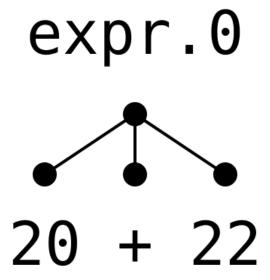


Figure 2.3: Parsetree of 20+22

2.1.4 Lambda expressions

The lambda expression is the last syntactic form we'd like to add. Recall that these look like (x : Int . x + 1).

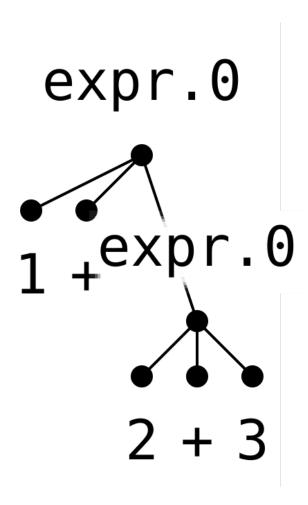


Figure 2.4: Parsetree of 1 + 2 + 3

Variables

The first thing we should deal with, are variables. A builtin is provided for those, namely Identifiers, matching all words starting with a lowercase (matching [a-z][a-zA-ZO-9]*). Let's introduce them in our syntax:

```
1 | var ::= Identifier
```

A var is valid in expressions too, e.g. in the expression x + 1, so we want to add it to our term:

Types

The second ingredient we still need, are types, to annotated the input types. Valid types, for starters, are Bool and Int.

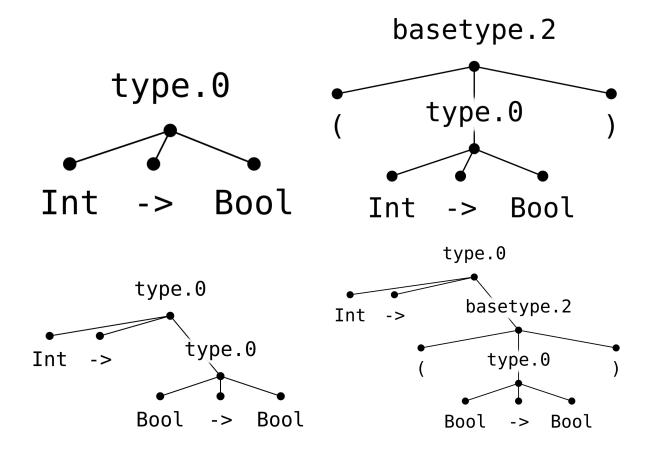
But what is the type of $(\x : Int . x + 1)$? It's something that takes an Int and gives back an Int. We type this as Int -> Int.

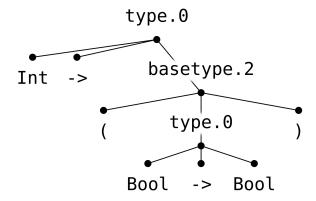
And what is the type of a function, taking another function as an argument? That would be, for example, (Int -> Int) -> Int, meaning we need to add a form with parentheses.

Recalling the trouble we had with left recursion and ordering, we write type as following:

```
1 | basetype::= "Bool" | "Int" | "(" type ")"
2 | type ::= basetype "->" type | basetype
```

Some examples of types are:





2.1.5 Lambda expressions

Now we have what we need to define lambda expressions. As they act as a term, we add it there:

Backslash is the escape character, so use two of them to represent a single backslash. We can also apply arguments to a lambda expression. We expand expr:

```
1 | expr ::= term "+" expr
2 | term expr
3 | term
```

2.1.6 What about nonsensical input?

With the current syntax, expresions as If 5 Then True else False, True + 5, True 5 or (x : Int : x + 1) True can be written. We allow these forms to be parsed, as the next stage of the compiler (the typechecker) will catch these errors. How to construct this, will be explained in a following section.

2.1.7 Recap

Our STFL.language contains

```
1
2
    STFL
3
4
   # A Simply Typed Functional Language
5
6
7
    Syntax
8
   basetype::= "Bool" | "Int" | "(" type ")"
10
            ::= basetype "->" type | basetype
11
12
            ::= "True" | "False"
13
   bool
14
   int
            ::= Number
15
            ::= Identifier
   var
16
17
            ::= term "+" expr
    expr
18
            | term expr
19
            | term
20
21
            ::= "If" expr "Then" expr "Else" expr
22
23
            | "(" "\\" var ":" type "." expr ")"
24
            | bool
```

```
25 | int
26 | var
```

Our examples.stfl contains

We run this with

- \bullet ALGT STFL.language examples.stfl expr -1 to show the parsetrees
- ullet ALGT STFL.language examples.stfl expr -1 --ptsvg SVGnames to render the parsetrees as SVG
- ALGT STFL.language --lsvg SVGname.svg to visualize the subtyping relationship.

2.2 Functions

For a full reference, see the reference manual on functions.

2.2.1 Domain and codomain

It'll come in handy later on to be able to calculate the *domain* and *codomain* of a function type. The *domain* of a function is the type it gives as output.

Table 2.1: Examples of domain and codomain

Function ty	pe dom c	od
Int -> Bool	Int	Bool
(Int -> Bool)	Int	Bool
<pre>Int -> Bool -> Bool</pre>	Int	Bool -> Bool
<pre>Int -> (Bool -> Bool)</pre>	Int	Bool -> Bool
(Int -> Bool) -> Bool	<pre>Int -> Bool</pre>	Bool
Int	Undefined	Undefined
Bool	Undefined	Undefined

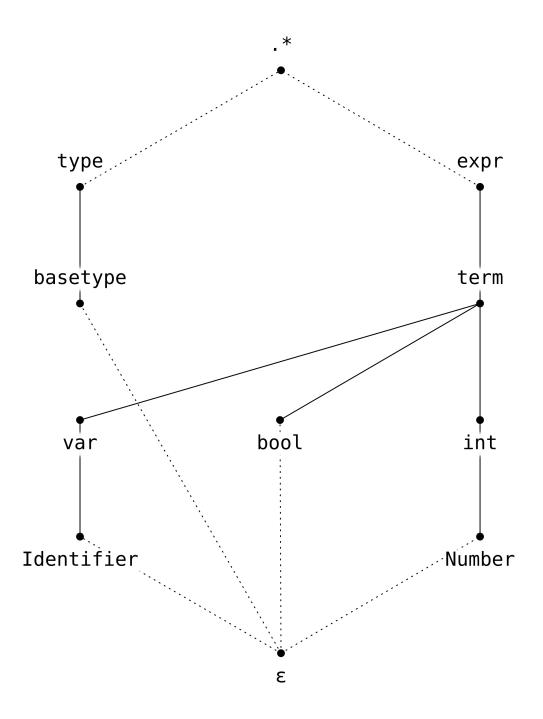


Figure 2.5: The final subtyping relationship of STFL. language $\,$

2.2.2 The function section

We add a new header to STFL.language:

In this function section, we can define the function *domain* in the following way:

```
1 | domain : type -> type 2 | domain(T1 "->" T2) = T1
```

So, what is going on here? Let's first take a look to the first line:

```
1 | domain : type -> type
```

The domain is the name of the function. The type -> type indicates what syntactic form is taken as input (a type) before the -> and what is given as output (again a type). You probably noticed the similarity between the types declared in our own STFL and this declaration. This is intentional. This is quite meta, don't get confused!



Figure 2.6: Relevant XKCD (by Randall Munroe, #917)

2.2.3 Pattern matching

Let's have look at the body of the function:

```
1 | domain(T1 "->" T2) = T1
```

What happens if we throw in Int -> Bool? Remember that this is parsed as a tree, with three leafs. Notice that there are three elements in the pattern match too: a variable T1, a literal -> and a variable T2. These leafs are matched respectively:

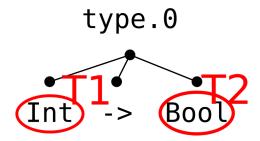


Figure 2.7: Pattern matching in action

The same principle applies with more advanced inputs:

We thus always bind T1 to the part before the top-level ->, in other words: we always bind the input type (or domain type) to T1. As that is exactly what we need, we return it!

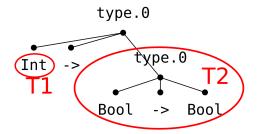


Figure 2.8: Pattern matching in action (more advanced)

2.2.4 Missing cases

This already gives us the most important part. However, what should we do if the first argument is a function type (e.g. (Int -> Bool) -> Bool)?

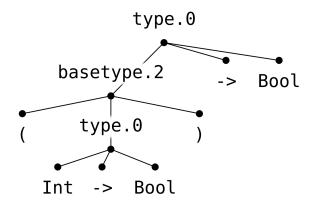


Figure 2.9: Typetree of function argument

This will match the pattern T1 "->" T2 as following:

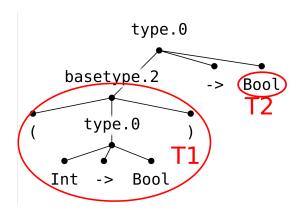


Figure 2.10: Typetree of function argument, matched

We see that T1 includes the (and), which we don't want. We simply solve this by adding a extra clause:

```
1 | domain : type -> type
2 | domain(("(" T1 ")") "->" T2) = T1
3 | domain(T1 "->" T2) = T1
```

We expect that the part *before* the arrow now is surrounded by parens. Note that we put parens once without double quotes and once with. These parens capture this part of the parsetree and match

it against the patterns inside the parens, as visible in the green ellipse:

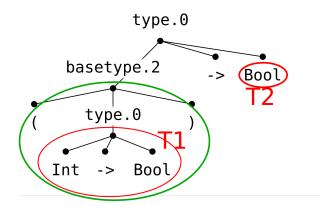


Figure 2.11: Recursive pattern matching

2.2.5 Recursion

There is a last missing case, namely if the entire type is wrapped in parens.

We match a type between parens, and then calculate its domain simply by calling the domain function again.

2.2.6 Clause determination

As you can see, there are three clauses now. What clause is executed?

Simply put, when the function is evaluated, the arguments are pattern matched against the first clause. If this pattern match succeeds, the expression on the right hand side is returned. Do the arguments not match the patterns? Then the next clause is considered.

In other words, clauses are tried **from top to bottom** and tested. The first clause of which the patterns match, is executed.

When no clauses match, an error message is given.

2.2.7 Executing functions

Let's put this to a test. We can calculate the domain of our examples.

Create a file typeExamples.stfl, with contents

Run this with ALGT STFL.language typeExamples.stfl type -1 -f domain:

```
While checking file STFL.language:
   Warning:
   While checking the totality of function "domain":
   Following calls will fall through:
        domain("Bool")
        domain("Int")
```

```
"Int -> Bool" applied to domain
# "(Int -> Bool)" applied to domain
Int
# "Int -> Bool -> Bool" applied to domain
# "Int -> (Bool -> Bool)" applied to domain
# "(Int -> Bool) -> Bool" applied to domain
Int -> Bool
# "Int" applied to domain
Not a single clause of domain matched:
  While pattern matching clause 0:
       In Pattern matching clause 0 with arguments: (Int)
       In domain(Int)
      FT: Could not pattern match '"Int"' over '"(" T ")"'
  While pattern matching clause 1:
       In Pattern matching clause 1 with arguments: (Int)
       In domain(Int)
      FT: Could not pattern match '"Int"' over '("(" T1 ")") "->" T2'
  While pattern matching clause 2:
       In Pattern matching clause 2 with arguments: (Int)
       In domain(Int)
      FT: Could not pattern match '"Int"' over 'T1 "->" T2'
 "Bool" applied to domain
Not a single clause of domain matched:
  While pattern matching clause 0:
       In Pattern matching clause 0 with arguments: (Bool)
       In domain(Bool)
      FT: Could not pattern match '"Bool"' over '"(" T ")"'
  While pattern matching clause 1:
       In Pattern matching clause 1 with arguments: (Bool)
       In domain (Bool)
      FT: Could not pattern match '"Bool"' over '("(" T1 ")") "->" T2
  While pattern matching clause 2:
       In Pattern matching clause 2 with arguments: (Bool)
       In domain (Bool)
      FT: Could not pattern match '"Bool"' over 'T1 "->" T2'
```

What does this output tell us?

For starters, we get a warning that we forgot two cases, namely Bool and Int. For some functions this is a problem, but domain is not defined for those values. Note that a bunch of other tests are builtin as well.⁷

Then, we see an overview for each function what result it gives (or an error message if the pattern matches failed).

If you want more information about the behaviour of a function, specify --ia or --ifa Function-to-analyze to get a clause-per-clause overview:

 $^{^7}$ We'll silently ignore these warnings for the rest of the tutorial with flag --no-checks

```
Clause:
    domain("(" T ")") = domain(T)
 Possible inputs at this point:
 # (type)
 Possible results:
 0 ("(" type(0/1/2:1) ")"): basetype/2 --> type( (Function call - ID not retrieva
  Analysis of clause 1
 Clause:
   domain(("(" T1 ")") "->" T2)
                              = T1
 Possible inputs at this point:
 # ("Bool")
    ("Int")
 # ((basetype "->" type))
 Possible results:
 1 (("(" type(0/0:0/2:1) ")"): basetype/2 "->" type(0/0:2)): type/0 --> type(0/0:2)
   Analysis of clause 2
   domain(T1 "->" T2)
                             = T1
 Possible inputs at this point:
 # ("Bool")
 # ("Int")
# (("Bool" "->" type))
# (("Int" "->" type))
 Possible results:
    ("Bool" "->" type(0/0:2)): type/0 --> "Bool" : "basetype" ("Int" "->" type(0/0:2)): type/0 --> "Int" : "basetype"
Falthrough
("Bool")
("Int")
```

2.2.8 Codomain

codomain can be implemented analogously:

```
1 codomain : type -> type
2 codomain("(" T ")") = codomain(T)
```

```
3 codomain(T1"->" ("(" T2 ")")) = T2
4 codomain(T1 "->" T2) = T2
```

2.3 Building the typechecker

Now that we have some experience with natural deduction, we can slay the next dragon: the typechecker! For those unfamiliar, the typechecker looks at the expression and determines the type of it and halts on inconsistencies, such as 1 + True or If True Then 0 Else False, ...

we will build a single rule for each syntactic choice of expr; thu a rule for:

- The constants True and False
- The constant Numbers
- Typing plus
- Typing If ... Then ... Else ...
- Typing lambda's (\x : T . e)
- Typing variables x
- Typing application

2.3.1 The typing environment

Before where start, how should we type a variable, such as x? Of course, this depends on the environment. In the lambda (\x : Int . x), x should be typed as a Int, while in the lambda (\x : Bool . x), this x clearly is a Bool.

We could type the inner expressions by substituting a simple default value in the expression, and then typing it. However, this doesn't scale to more advanced languages.

The other, more general solution is keeping track of the type of each variable. We declare a simple list to keep track of the types in the Syntax Section:

The typing represents a data entry, whereas the typingEnvironment can contain zero or more of these data entries, thus keeping track of the variable types.

The typing relation is often denoted with a uppercase gamma, Γ . We will follow this convention⁸.

2.3.2 The typing relation

We're all set now! What should our typing relation look like? First, we'll want to take a typingRelation as input, together with an expr. This should be enough to calculate the type of the expression.

In other words, the type of the relation is typingRelation (in), expr (in), type (out). In the acadical world, this is often given the symbol \vdash 9, pronounced entails or out of this environment follows this typing. So, our declaration becomes:

```
1\mid (\vdash) : typingEnvironment (in), expr (in), type (out) Pronounced as "entails typing"
```

2.3.3 Typing constants True and False

It's pretty easy to type constants, such as 42 and True. Let us start with typing the constant True.

If this looks magical: we take the typing environment as input (but don't use it), pattern match on a literal True and return the known type Bool.

We can do the same for False:

⁸Type Ctrl+Shift+U 0393 on linux to input Gamma. On Windows, hold down Alt and type + 0393.

⁹Type Ctrl+Shift+U 22a2 on linux to input entails. On Windows, hold down Alt and type + 22a2.

2.3.4 Typing constant Numbers

Our next challenge is giving a type to Ints. Making a single rule for each number is a bit hard, especially because there is an infinite amount of them...

However, we can simply fix this by adding a predicate, checking that our input is a number:

```
1  n:int
2  ----- [Tnumber]
3  Γ ⊢ n, "Int"
```

Remember that our predicates are written above the line.

2.3.5 Typing against an empty environment

Let's try to run our typing relation, with ./ALGT STFL.language expr -l -r -

```
# Could not apply relation \vdash to the input "True", because: While trying to proof that (\vdash) is applicable to "True": Expected 2 arguments to relation \vdash, but only got 1
```

Well, that didn't work. The tool expects two arguments; but only one is provided...

To solve this, we declare yet another relation, in which we type an expression against an empty environment:

```
1  n:int
2  ----- [Tnumber]
3  Γ ⊢ n, "Int"
```

Retrying with the new relation (./ALGT STFL.language examples.stfl expr -1 -r ::) gives us:

```
# If True Then False Else True applied to ::

# Proof weight: 6, proof depth: 3

{} \rangle True, Bool \{} \rangle False, Bool \{} \rangle True, Bool Tl = Bool = Tr

{} \rangle If True Then False Else True, Bool

If True Then False Else True :: Bool
```

2.3.6 Typing plus

Another expression we'll want to type are additions.

Of course, this will always return an Int, but there is more. True + False is not valid, whereas 1 + 1 can be typed. In other words, we have to check that the arguments to + are both numbers.

We could thus type + as following:

This works for 1 + 2, but not for 1 + (2 + 3), as (2 + 3) is *not* a syntactic form that is a literal Number. It can be typed as Int though, so we can generalize our predicates by using the typing relationship recursively:

Looks good! Time to give this a try:

2.3.7 Typing If

It is pretty straightforward that the condition should be a Bool, which already gives a draft of the rule:

We also want to make sure that both e1 and e2 are correctly typed, so we recursively typecheck them:

But what type should we return? The type of e1 or e2?

Consider expression If True Then O Else False. Evaluating this yields O. However, expression If False Then O Else False would yield False. In other words, depending on the runtime value of the condition, we might get a different type.

That's not behaviour we want. The types of e1 and e2 should be the same to function correctly. We add a predicate to check this:

Now we can also return a type; as T1 and T2 are the same, we just pick one:

All done! Time to give it a try:

2.3.8 Typing lambda's

Typing lambda's is a bit complicated. Remember that a lambda such as (\x : T . e) means that, given x of type T as input argument, it gives back expression e with x replaced.

This gives us quite some clues about what to do.

Let's start with the skeleton of the rule:

```
1 | ???

2 | ----- [TLambda]

3 | Γ | "(" "\\" x ":" T1 "." e ")", ???
```

Of course, we'll want to type e jus as well. Not only to check wether it is correct, but also because we'll need it's type later on:

This is close to what we want, but there is a catch though: in the expression e, we know that x has the type T1. We should pass this knowledge to the typing of e, by adding it to the typing environment Γ :

So far, so good! The only question remaining is what type we should return. We know we have input of type T1 and output of type T2. Thats where our -> comes into play: the entire lambda has type T1 -> T2!

There is a little technicality into play here though: T1 might be some complicated type, such as Int -> Bool - meaning we expect a *function* as input argument. If we would write Int -> Bool -> T2, that would be read as funcion taking *two* arguments: first a Int, followed by a Bool. Not quite the same thus.

The fix for this is simple: add parentheses. The type of a lambda is $(T1) \rightarrow T2$.

Typing this out as rule yields:

Note that an extra pair of parentheses was added; one pair is between double quotes, denoting that this should be added in the parse tree; the other pair just groups them together to help the tool build the parsetree.

2.3.9 Typing variables

Before we can see typing of lambda's live, we need to take another hurdle: typing variables.

You'll probably think it'll be a lot of work to design the searching behaviour, but luckily, there is a special construction that does exactly that. Remember the evaluation context? We can use this builtin here too:

```
1 | 2 | ------ [Tx] | 3 | Γ[x ":" T] | -x, T
```

Quite succint! If you're a bit puzzled about its workings, we stated to ALGT that it should search a typing of x, where x is exactly the name of the variable we want to type.

At this point, we can finally type a single lambda:

2.3.10 Typing application

The typechecker is nearly complete, only a single syntactic form can't be typed yet: application of the form function argument.

How can we tackle this problem? For starters, we'll have to type the function and argument

A function has a determined input argument, also known as the *domain* of the function. To be well typed, the domain should match the type of the argument exactly. But how can we get this argument? Luckily, we created a function earlier on that calculates exactly that! We can simply use domain and check that it's result equals TArg:

Nearly done! Only question left is what type we should return.

This is pretty straighforward too, as we earlier made the function codomain which exactly calculates the return type of TFunc

All finished now, except for trying of course:

2.4 Evaluator and typechecker: recap

Our declared relations are:

The definition of those relations are:

```
1
   Rules
2
    ======
4
5
6
7
    \mathtt{expr0} \to \mathtt{expr1}
                                              [EvalCtx]
8
9
    expr[expr0] \rightarrow expr[expr1]
10
11
12
13
    n1:Number
                             n2:Number
                                ----- [EvalPlus]
14
    n1 "+" n2 \rightarrow !plus(n1, n2)
15
16
17
18
20
                                                         [EvalIfTrue]
     "If" "True" "Then" e1 "Else" e2 
ightarrow e1
21
22
23
                                                         [EvalIfFalse]
24
     "If" "False" "Then" e1 "Else" e2 
ightarrow e2
25
26
27
28
     ("(" "\\" var ":" type "." e ")") arg 
ightarrow !subs:expr(var, arg, e)
29
30
31
32
33
34
    i:int
35
                                      [CanonInt]
36
     (√) i
37
38
39
    b:bool
                                      [CanonBool]
40
     (√) b
41
42
43
44
45
46
    (√) e
                                      [BigStepBase]
47
48
49
    	ext{e0} 
ightarrow 	ext{e1} \qquad 	ext{e1} 
ightarrow 	ext{e2}
50
                                     [BigStepRec]
51
52
    e0 →* e2
53
54
55
56
58 "{}" ⊢ e, T
```

```
59 | ----- [TEmptyCtx]
60
      e :: T
 61
62
63
64
                                [TboolTrue]
65
      \Gamma \vdash "True", "Bool"
66
67
 68
 69
                                 [TboolFalse]
     \Gamma \vdash "False", "Bool"
70
71
 72
73
     n:int
 74
     -----
                                [Tnumber]
 75
     \Gamma \vdash \mathtt{n}, "Int"
 76
 77
 78
 79
80
81
82
83
                                [Tx]
84
85
     \Gamma[ x ":" T ] \vdash x, T
86
87
 88
     \Gamma \vdash \mathtt{n1}, "Int" \Gamma \vdash \mathtt{n2}, "Int"
                                                                     [TPlus]
89
90
     \Gamma \vdash n1 "+" n2, "Int"
91
92
     \Gamma \vdash c, "Bool" \Gamma \vdash e1, Tl \Gamma \vdash e2, Tr Tl = Tr : type
93
94
                                                 -----[TIf]
     \Gamma \vdash "If" c "Then" e1 "Else" e2, Tl
95
96
97
98
     (x ":" T1) "," \Gamma \vdash e, T2
99
100
                                            ----- [TLambda]
      \Gamma \vdash "(" "\\" x ":" T1 "." e ")", ( "(" T1 ")") "->" T2
101
102
103
104
     \Gamma \vdash e1, Tfunc \Gamma \vdash e2, Targ Targ = domain(Tfunc) : type
105
106
                                                                                [Tapp]
107 \Gamma \vdash e1 e2, codomain(Tfunc)
```

Running the relation :: on all our examples with flags ./ALGT STFL.language True False If True Then False Else True If If gives:

```
False :: Bool
# If True Then False Else True applied to ::
# Proof weight: 6, proof depth: 3
\{\} \vdash True, Bool \{\} \vdash False, Bool \{\} \vdash True, Bool Tl = Bool = Tr
\{\} \vdash If True Then False Else True, Bool
If True Then False Else True :: Bool
# 42 applied to ::
# Proof weight: 3, proof depth: 3
42 : int
{} ⊢ 42, Int
42 :: Int
# 20 + 22 applied to ::
# Proof weight: 6, proof depth: 4
20 : int 22 : int
\{\}\ \vdash\ 20\ , Int \{\}\ \vdash\ 22\ , Int
{} ⊢ 20 + 22, Int
20 + 22 :: Int
# 1 + 2 + 3 applied to ::
# Proof weight: 9, proof depth: 5
                2 : int 3 : int
1 : int {} ⊢ 2, Int {} ⊢ 3, Int
\{\} \vdash 1, Int \{\} \vdash 2 + 3, Int
\{\} \vdash 1 + 2 + 3, Int
1 + 2 + 3 :: Int
# (\x: Int . x + 1) 41 applied to :: # Proof weight: 10, proof depth: 6
                            1 : int
```

2.5 Syntax Styling

As a bonus, syntax styling is supported out of the box just as well! While this is not a fundamental aspect of a programming language, it is quite fun - and important when presenting.

(\ cond : Bool . If cond Then 41 + 1 Else 0) True

- Terminal
- \bullet White
- \bullet WhiteFlat

Reference manual

3.1 General

A language is defined in a .language-file. It starts (optionally) with a title:

Comments start with a # and can appear quasi everywhere.

```
egin{array}{c|c} 1 & & & \\ 2 & \# & \text{This is a comment} \end{array}
```

Syntax, functions, relations, ... are all defined in their own sections:

A section header starts with an upper case, is underlined with = and followed by a blank line.

3.2 Syntax

All syntax is defined in the Syntax section. It consists out of BNF-rules, of the form

```
1 | name ::= "literal" | choice | seq1 seq2
```

Choices might be written on multiple lines, as long as at least one tab precedes them:

```
1 | name ::= choice1 | choice2
2 | choice3
```

3.2.1 Literals

A string that should be matched exactly, is enclosed in " (double quotes). Some characters can be escaped with a backslash, namely:

Table 3.1: Escape sequences

	Sequence	Result	
\n	ne	ewline	
\t	ta	ıb	
\"	do	double quote	
\\	ba	ackslash	

3.2.2 Parsing order

Rules are parsed **left to right**, in other words, choices are tried in order. No backtracking happens when a choice is made; the parser is a *recursive descent parser*. This has two drawbacks: left recursion results in an infinite loop and the ordering of choices does matter.

```
# Left recursion, error message.
expr ::= expr "+" int

# 'int' already consumes a part of 'int + int', error message
expr ::= int | int "+" int

# Common part extraction, error message
# Correct
expr ::= int "+" int | int
```

3.2.3 Builtin syntactic forms

Some syntactic forms are already provided for your convenience, namely:

Builtin Meaning Regex Matches an identifier Identifier [a-z][a-zA-Z0-9]*Number Matches an (negative) integer. Integers parsed by -?[0-9]* this might be passed into the builtin arithmetic functions. Matches a single character, whatever it is, including Any newline characters Matches a lowercase letter Lower [a-z] Upper Matches an uppercase letter [A-Z]Matches an digit Digit [0-9] Matches a hexadecimal digit [0-9a-fA-F] Hex Matches a double quote delimted string, returns the String "([^"\]|\"|\\)*" value including the double quotes Matches a double quote delimeted string, returns "([^"\]|\"|\\)*" StringUnescthe value without the double quotes Matches a single character that is not a newline. LineChar [^\n] This includes: Matches a '(', which will dissapear in the parsetree Par0 (Matches a ')', which will dissapear in the parsetree ParC)

Table 3.2: Builtin syntax

3.2.4 Subtyping relationship

A syntactic form equals a (possibly infinite) set of strings. By using a syntactic form \mathtt{a} as choice in other syntactic form \mathtt{b} , \mathtt{a} will be a subset of be, giving the natural result that \mathtt{a} is a subtype of \mathtt{b} .

In the following examle, bool and int are both subsets of expr. This can be visualised with the --lsvg Output.svg-flag.

```
1 bool ::= "True" | "False"
2 int ::= Number
3 expr ::= ... | bool | int
```

3.2.5 Whitespace in sequences

Whitespace (the characters " ","\t"), is parsed by default (and ignored completely). If you want to parse a whitespace sensitive language, use other symbols to declare the rule:

Table 3.3: Whitespace modes

	Operator Meaning
::=	Totally ignore whitespace
~~=	Parse whitespace for this rule only
//=	Parse whitespace for this rule and all recursively called rules

This gives rise to the following behaviour:

Table 3.4: Whitespace mode examples

Syntax	Matching String	
a ::= "b" "c" x	b с x y	
x ::= "x" "y"	bcxy	
	b\tc\tx\ty	
	b c\txy	
a ~~= "b" "c" x	bcx y	
x ::= "x" "y"	bcxy	
	bcx\ty	
a //= "b" "c" x	bcxy	
x ::= "x" "y"		

3.2.6 Grouping sequences

Sometimes, you'll want to group an entire rule as a token (e.g. comments, an identifier, ...) Add a \$ after the assignment to group it.

```
1 text ::= LineChar line | LineChar
2 commentLine ::= $ "#" text "\n"
3
4 customIdentifier ::= $ Upper Number
```

When such a token is used in a pattern or expression, the contents of this token are parsed against this rule:

```
1 | f : customIdentifier -> statement
2 | f("X10") = "X9" "# Some comment"
```

3.3 Functions

3.3.1 Patterns and expressions

Functions transform their input. A function is declared by first giving its type, followed by one or more clauses:

When an input is given, arguments are pattern matched against the patterns on between parentheses. If the match succeeds, the expression on the right is given. If not, the next clause is given.

Note that using the same variable multiple times is allowed, this will only work if these arguments are the same:

```
1 | f(a, a) = ...
```

Recursion can be used just as well:

```
1 \mid f("a" a) = f(a)
```

This is purely functional, heavily inspired on Haskell.

Possible expressions

Expr	Name	As expression
x	Variable	Recalls the parsetree associated with this variable
_	Wildcard	Not defined
42	Number	This number
"Token"	Literal	This string
<pre>func(arg0, arg1,)</pre>	Function call	Evaluate this function
!func:type(arg0,)	Builtin function call	Evaluate this builtin function, let it return a type
(expr or pattern:type)	Ascription	Checks that an expression is of a type. Bit useless
e[expr or pattern]	Evaluation context	Replugs expr at the same place in e. Only works if e was created with an evaluation context
a "b" (nested)	Sequence	Builds the parse tree

Possible patterns

Expr	As pattern	
x	Captures the argument as the name. If multiple are used in the same pattern, the captured arguments should be the same or the match fails.	
_	Captures the argument and ignores it	
42	Argument should be exactly this number	
"Token"	Argument should be exactly this string	
<pre>func(arg0, arg1,)</pre>	Evaluates the function, matches if the argument equals the result. Can only use variables which are declared left of this pattern	
!func:type(arg0,)	Evaluates the builtin function, matches if the argument equals the result. Can only use variables which are declared left of this pattern	
(expr or pattern:type)	Check that the argument is an element of type	
e[expr or pattern]	Matches the parsetree with e, searches a subpart in it matching pattern	
a "b" (nested)	Splits the parse tree in the appropriate parts, pattern matches the subparts	

3.3.2 Typechecking

Equality

```
1 | 2 | Syntax | 3 | ======= 4 | 5 | a | ::= ... | 6 | b | ::= ... | 7 | c | ::= a | b | d
```

```
8
9 Functions
10 =========
11
12 f : a -> b -> c
13 f(x, x) = x
```

When equality checks are used in the pattern matching, the variable will be typed as the smallest common supertype of both types. If such a supertype does not exist, an error message is given.

Note that using a supertype might be a little too loose, but won't normally happen in real-world examples.

In the given example, x will be typed as c, the common super type. In this example, x might also be a d, while this is not possible for the input. This can be solved by splitting of $a \mid b$ as a new rule.

3.3.3 Totality- and liveabilitychecks

Can be disabled with --no-check, when they take to long.

3.3.4 Higher order functions and currying?

Are not possible for now (v 0.1.26.4). Perhaps in a future version or when someone really needs it and begs for it.

3.3.5 Builtin functions

name	Descr	Arguments
plus	Gives a sum of all arguments (0 if none given)	Number* -> Number
min	Gives the first argument, minus all the other	Number -> Number* -> Number
	arguments	
mul	Multiplies all the arguments. (1 if none given)	Number* -> Number
div	Gives the first argument, divided by the product of	Number -> Number* -> Number
	the other arguments. (Integer division, rounded	
	down))	
mod	Gives the first argument, module the product of the	Number -> Number* -> Number
	other arguments.	
neg	Gives the negation of the argument	Number -> Number
equal	Checks that all the arguments are equal. Gives 1 if	.* -> .* -> Number
	so, 0 if not.	
error	Stops the function, gives a stack trace. When used in	.** → ε
	a rule, this won't match a predicate	
subs	(expression to replace, to replace with, in this	.* -> .* -> .*
	expression) Replaces each occurrence of the first	
	expression by the second, in the third argument.	
	You'll want to explictly type this one, by using	
	subs:returnType("x", "41", "x + 1")	
group	Given a parsetree, flattens the contents of the	.* -> StringUnesc
	parsetree to a single string	

3.4 Relations and Rules

3.5 Properties

3.6 Command line flags

Used concepts and algorithms

4.1 Automated description of an arbitrary language

4.1.1 Invariants and checks

No common choices No left recursion -> lattice properties Left consumption (expr | expr "+" ...) -> error msg

- 4.1.2 Lattices
- 4.1.3 Parser interpretation
- 4.2 Abstract representation of an arbitrary language

Abstract interpretation stuff

- 4.2.1 Representation
- 4.2.2 Subtraction
- 4.3 Functions
- 4.4 Natural deduction representation
- 4.5 Algorithms
- 4.5.1 Minimal typecheck
- 4.5.2 Liveability check
- 4.5.3 Dead clauses check
- 4.5.4 Abstract interpretation
- 4.5.5 Rule inputs and output calculation

Dynamization and gradualization

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A short list of usefull unicode characters.

On Linux, press Left-Ctrl + Shift + U together, then type the hexcode.

On Windows, press

6.1 Character | Name | Hexcode

 Γ | Gamma | 393 \rightarrow | Right-Arrow | 2192 \checkmark | Checkmark | 2713 \vdash | Entails, vdash | 22a2 γ | Lowercase gamma | 03b3 ε | Epsilon | 025b λ | Lowercase Lambda | 03bb \vee | Disjunction | 2228 \wedge | Conjunction | 2227 \Rightarrow | Double-Right-Arrow | 21d2