

# ALGT - The manual

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# Chapter 1

## Overview

This document gives an overview of the *ALGT*-tool. First, a general overview of what the tool does is given and why it was developed. Second, a hands-on tutorial develops a Simply Typed Functional Language (STFL). Thirdly, the reference manual gives an in-depth overview of the possibilities and command line flags. Fourth, some concepts and algorithms are explained more thoroughly, together with properties they use. And at last, the `dynamize` and `gradualize` options are explained in depth, as these are what the master dissertation is about.

This documentation is about version **0.2** (`Demo time!`), generated on 2017-3-21 .



# Chapter 2

## What is ALGT?

*ALGT* (*Automated Language Generation Tool* <sup>1</sup>) is a tool to formally specify any programming language. This is done by first declaring a syntax, using BNF, and then declaring semantics by introducing logical deduction rules, such as evaluation or typing rules. Eventually, properties can be introduced which can be tested. Of course, these can be run.

The tool is kept as general as possible, so any language can be modelled.

### 2.1 Declaring the syntax

For a full reference on syntax, see the reference manual on syntax.

#### 2.1.1 Simple booleans

A program is nothing more than a string of a specific form. To describe strings of an arbitrary structure, *BNF* <sup>2</sup> can be used.

The syntax of our programming language is defined in the **Syntax** section of *STFL.language*:

```
1  STFL
2  *****
3
4
5  # A Simply Typed Functional Language
6
7  Syntax
8  =====
```

What do we write here? Let's start with declaring the boolean values `True` and `False`. We express how these can be parsed by writing `bool ::= "True" | "False"`. This tells the tool that a syntactic form named `bool` exists and it is either `True` or `False`. Note the double quotes, these are important to indicate that we want this string literally. The `|` expresses that it can choose between those forms.

*STFL.language* now looks like:

```
1  STFL
2  *****
3
4
5  # A Simply Typed Functional Language
6
7  Syntax
8  =====
9
10 bool    ::= "True" | "False"
```

Lets try running this! Create `examples.stfl`, which contains:

---

<sup>1</sup>Note the similarity of *ALGT* and *AGT*. The tool started its life as *AGT*, based on the paper *Abstracting Gradual Typing*. When it became more general, another name and acronym was chosen.

<sup>2</sup>Backus-Naur-form, as introduced by John Backus in the ALGOL60-report.

```

1 True
2 False

```

We can parse these by running (in your terminal) `./ALGT STFL.language examples.stfl bool -1`. The first argument is the language file, the second the examples, the `bool` tells ALGT what syntactic rule to parse. The `-1` flag expresses that each line should be treated individually.

If all went well, you should get the following output:

```

# "True" was parsed as:
True    bool.0
# "False" was parsed as:
False   bool.1

```

The most interesting part here is that `True` has been parsed with `bool.0`, thus the first choice of the `bool`-form, while `False` has been parsed with the second form.

## 2.1.2 If-statements

Now, let's add expressions of the form `If True Then False Else True`. We define a new syntactic form: `expr ::= "If" bool "Then" bool "Else" bool`.<sup>3</sup> This tells *ALGT* that an expression starts with a literal `If`, is followed by a `bool` (so either `True` or `False`), is followed by a literal `Then`, ... The tool uses the double quotes `"` to distinguish between a literal string and another syntactic form.

*STFL.language* now looks like:

```

1
2 STFL
3 *****
4
5 # A Simply Typed Functional Language
6
7 Syntax
8 =====
9
10 bool    ::= "True" | "False"
11 expr    ::= "If" bool "Then" bool "Else" bool

```

This captures already some example expressions. Let's add `If True Then False Else True` to *examples.stfl*:

```

1 True
2 False
3 If True Then False Else True

```

Let's run our tool, this time with `./ALGT STFL.language examples.stfl expr -1`

```

"examples.stfl (line 0)" (line 1, column 1):
unexpected "T"
expecting "If"
Could not parse expression of the form expr
"examples.stfl (line 1)" (line 1, column 1):
unexpected "F"
expecting "If"
Could not parse expression of the form expr
"examples.stfl (line 2)" (line 1, column 4):
unexpected "T"
expecting "If"
Could not parse expression of the form expr

```

Oops! Seems like our parser now always wants to see a `If` in the beginning, and can't handle `True` anymore. Perhaps we should tell that a `bool` is a valid expression to:

```

1
2 Syntax
3 =====
4
5 bool    ::= "True" | "False"

```

<sup>3</sup>Don't worry about spaces and tabs, we deal with them. If you want need to parse stuff like "duizendeneen" or whitespace sensitive languages, please refer to the reference manual



```

6 | expr    ::= "If" bool "Then" bool "Else" bool
7 |         | bool

```

Lets see what this gives:

```

+ | If      expr.0
  | True    bool.0
  | Then    expr.0
  | False   bool.1
  | Else    expr.0
  | True    bool.0

```

Looks a lot better! The third example shows clearly how the expression falls apart in smaller pieces. What with a nested If?

If If True Then False Else True Then True Else False clearly can't be parsed, as the condition should be a `bool`, according to our current syntax.

Well, we can just write `expr` instead of `bool` in our syntax:

```

1 | expr    ::= "If" expr "Then" expr "Else" expr
2 |         | bool

```

Running this gives

```

# "If If True Then False Else True Then True Else False" was parsed as:
+ | If      expr.0
  | + If    expr.0
    | | True bool.0
    | | Then expr.0
    | | False bool.1
    | | Else expr.0
    | | True bool.0
    | Then expr.0
    | True bool.0
    | Else expr.0
    | False bool.1

```

This clearly shows how the parse trees are nested. This can be rendered too:<sup>4</sup>

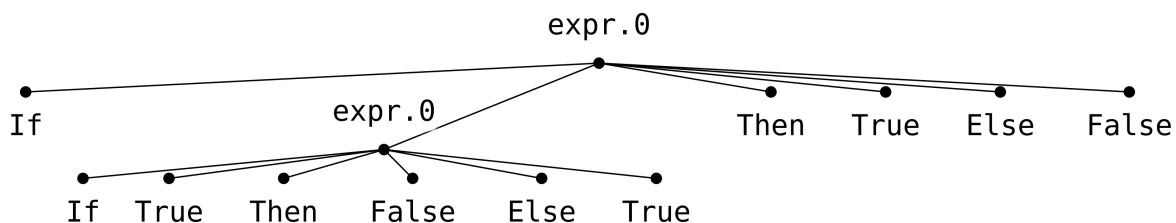


Figure 2.1: ParseTree of a nested condition<sup>5</sup>

### 2.1.3 Adding numbers, subtyping and forbidden left recursion

Time to spice things up with numbers. To make things easier, integers are built in as `Number`. It's good practice to introduce a new syntactic rule for them:

```

1 | int     ::= Number

```

As an `int` is a valid expression, we add it to the `expr` form:

```

1 | expr    ::= "If" expr "Then" expr "Else" expr
2 |         | bool
3 |         | int

```

Note that every `int` now also is an `expr`, just as every `bool` is an `expr`. This typing relationship can be visualized with `ALGT STFL.language -lsvg Subtyping.svg`<sup>6</sup> :

<sup>4</sup>These images can be created with `ALGT STFL.language examples.stfl -l --ptsvg Outputname`

<sup>5</sup>These images can be created with `ALGT STFL.language examples.stfl -l --ptsvg Outputname`

<sup>6</sup>Creating this svg might take a long time for complicated syntaxes, as ALGT calculates the ordering of labels resulting in the least intersecting lines.

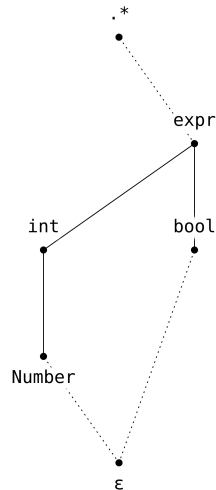


Figure 2.2: Subtyping relation of STFL.language

Now that numbers have been added, let's run this with a number as example:

```
1 | 42
```

should give

```
# "42" was parsed as:
42    Number.0
```

So far, so good! Time to add addition:

```
1 | expr    ::= "If" expr "Then" expr "Else" expr
2 |         | bool
3 |         | int
```

expr "+" expr

We add some example:

```
1 | 20 + 22
2 | 1 + 2 + 3
```

And run it:

```
Error:
While checking file STFLrec.language:
  While checking the syntax:
    Potential infinite left recursion detected in the syntax.
    Left cycles are:
      expr -> expr
```

Oops! Looks like we did something wrong. What is this left recursion? Whenever the parser wants to parse an expression, it tries every choice from left to right. This means that whenever it tries to parse `expr`, it should first try to parse `expr`. That's not really helpfull, so the parser might get in an infinite loop then.

Not allowing left recursion also means that no loops in the subtypings occur. In other words, the subtyping relationship is a lattice.

The solution to this problem is splitting `expr` in two parts: a `term` with simple elements in front, and `expr` with advanced forms:

```
1 | expr    ::= term
2 |         | term "+" expr
3 | term    ::= "If" expr "Then" expr "Else" expr
4 |         | bool
5 |         | int
```

Let's retry this:

```

Error:
  While checking file STFLWrongOrder.language:
    While checking the syntax:
      While checking for dead choices in expr:
        The choice 'term "+" expr' will never be parsed.
        The previous choice 'term' will already consume a part of it.
        Swap them and you'll be fine.

```

What went wrong this time? The parser tries choice after choice. When parsing `20 + 22` against `expr ::= term | term "+" term`, it'll first try `term` (and not `term "+" term`). It successfully parses `20` against the lonely `term`, thus the input string `+ 22` is left. The parser doesn't know what to do with this leftover part, so we get an error.

To fix this, we change the order:

```

1 | expr    ::= term "+" expr
2 |       | term

```

When we try again, we get:

```

# "20 + 22" was parsed as:
+ 20      Number.0
| +       expr.0
| 22      Number.0
# "1 + 2 + 3" was parsed as:
+ 1       Number.0
| +       expr.0
| + 2     Number.0
| | +     expr.0
| | 3     Number.0

```

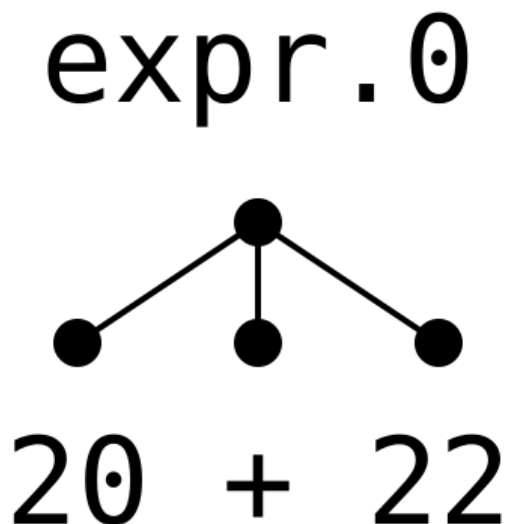


Figure 2.3: Parsetree of `20+22`

#### 2.1.4 Lambda expressions

The lambda expression is the last syntactic form we'd like to add. Recall that these look like `(\x : Int . x + 1)`.

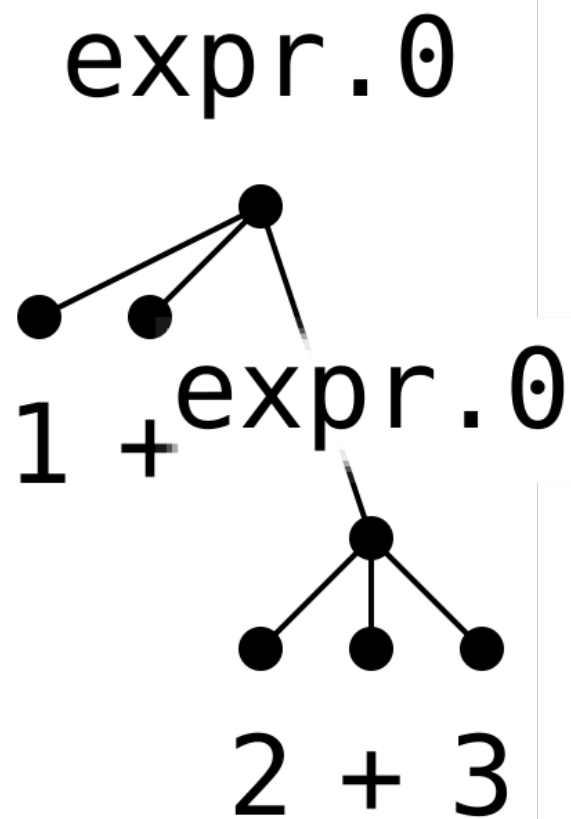


Figure 2.4: Parsetree of  $1 + 2 + 3$

## Variables

The first thing we should deal with, are variables. A builtin is provided for those, namely `Identifiers`, matching all words starting with a lowercase (matching `[a-z][a-zA-Z0-9]*`). Let's introduce them in our syntax:

```
1 | var      ::= Identifier
```

A `var` is valid in expressions too, e.g. in the expression `x + 1`, so we want to add it to our `term`:

```
1 | term      ::= "If" expr "Then" expr "Else" expr
2 |           | bool
3 |           | int
4 |           | var
```

## Types

The second ingredient we still need, are types, to annotated the input types. Valid types, for starters, are `Bool` and `Int`.

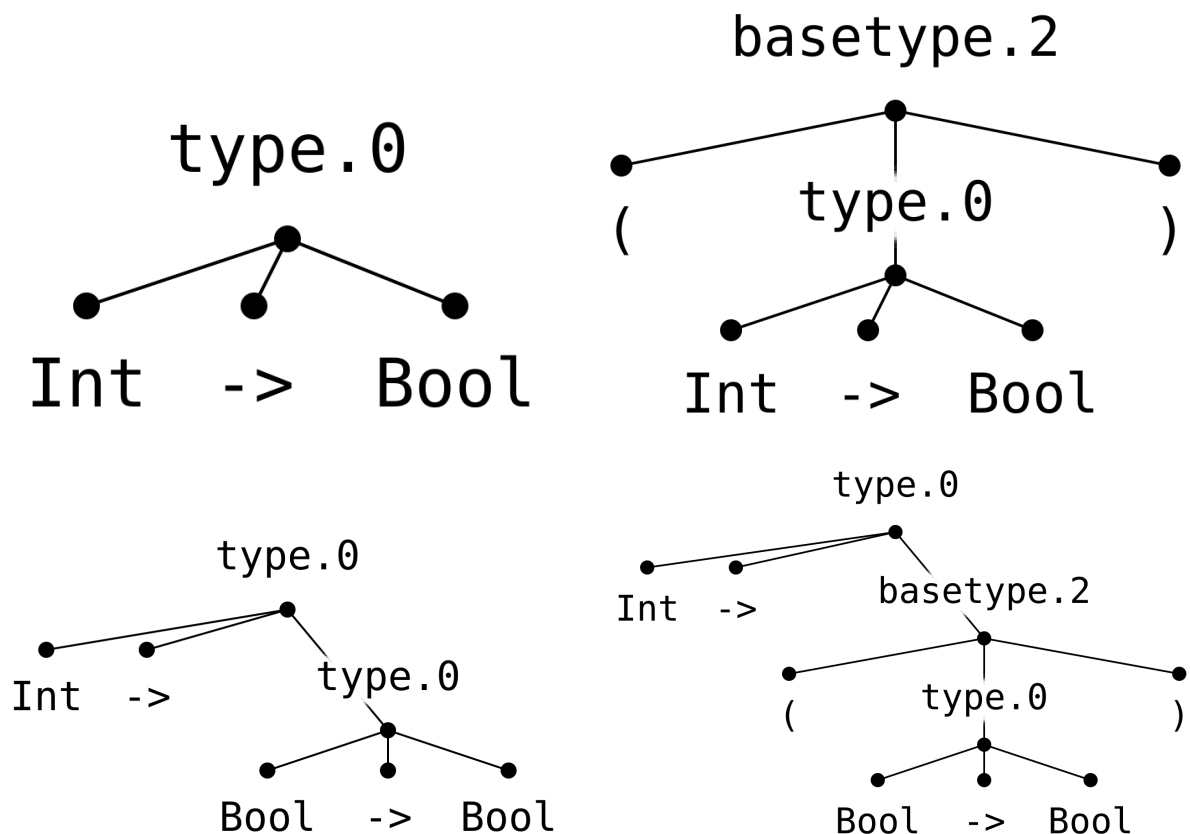
But what is the type of  $(\lambda x : \text{Int} . x + 1)$ ? It's something that takes an `Int` and gives back an `Int`. We type this as `Int -> Int`.

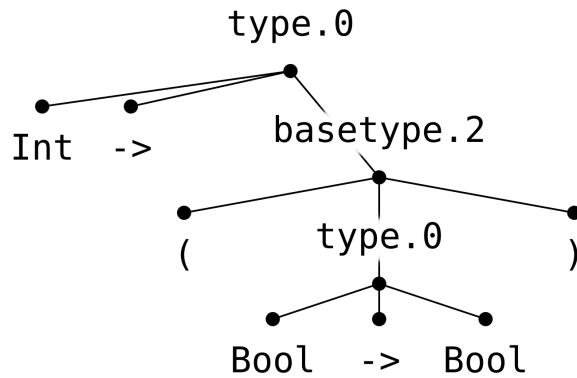
And what is the type of a function, taking another function as an argument? That would be, for example, `(Int -> Int) -> Int`, meaning we need to add a form with parentheses.

Recalling the trouble we had with left recursion and ordering, we write `type` as following:

```
1 | basetype ::= "Bool" | "Int" | "(" type ")"
2 | type     ::= basetype "->" type | basetype
```

Some examples of types are:





### 2.1.5 Lambda expressions

Now we have what we need to define lambda expressions. As they act as a term, we add it there:

```

1 term    ::= "If" expr "Then" expr "Else" expr
2          | "(" "\\\" var ":" type "." expr ")"
3          | bool
4          | int
5          | var

```

Backslash is the escape character, so use two of them to represent a single backslash.

We can also apply arguments to a lambda expression. We expand `expr`:

```

1 expr    ::= term "+" expr
2          | term expr
3          | term

```

### 2.1.6 What about nonsensical input?

With the current syntax, expressions as `If 5 Then True else False, True + 5, True 5 OR (\x : Int : x + 1) True` can be written. We allow these forms to be parsed, as the next stage of the compiler (the typechecker) will catch these errors. How to construct this, will be explained in a following section.

### 2.1.7 Recap

Our *STFL.language* contains

```

1
2 STFL
3 *****
4
5 # A Simply Typed Functional Language
6
7 Syntax
8 =====
9
10 basetype ::= "Bool" | "Int" | "(" type ")"
11 type    ::= basetype "->" type | basetype
12
13 bool    ::= "True" | "False"
14 int     ::= Number
15 var     ::= Identifier
16
17 expr    ::= term "+" expr
18          | term expr
19          | term
20
21
22 term    ::= "If" expr "Then" expr "Else" expr
23          | "(" "\\\" var ":" type "." expr ")"
24          | bool

```

```

25 | int
26 | var

```

Our *examples.stfl* contains

```

1 True
2 False
3 If True Then False Else True
4 If If True Then False Else True Then True Else False
5 42
6 20 + 22
7 1 + 2 + 3
8 (\x : Int . x + 1) 41

```

We run this with

- `ALGT STFL.language examples.stfl expr -l` to show the parsetrees
- `ALGT STFL.language examples.stfl expr -l --ptsvg SVGnames` to render the parsetrees as SVG
- `ALGT STFL.language --lsvg SVGname.svg` to visualize the subtyping relationship.

## 2.2 Functions

For a full reference, see the reference manual on functions.

### 2.2.1 Domain and codomain

It'll come in handy later on to be able to calculate the *domain* and *codomain* of a function type. The *domain* of a function is the type it can handle as input. The *codomain* of a function is the type it gives as output.

Table 2.1: Examples of domain and codomain

Function type	dom	cod
<code>Int -&gt; Bool</code>	<code>Int</code>	<code>Bool</code>
<code>(Int -&gt; Bool)</code>	<code>Int</code>	<code>Bool</code>
<code>Int -&gt; Bool -&gt; Bool</code>	<code>Int</code>	<code>Bool -&gt; Bool</code>
<code>Int -&gt; (Bool -&gt; Bool)</code>	<code>Int</code>	<code>Bool -&gt; Bool</code>
<code>(Int -&gt; Bool) -&gt; Bool</code>	<code>Int -&gt; Bool</code>	<code>Bool</code>
<code>Int</code>	<i>Undefined</i>	<i>Undefined</i>
<code>Bool</code>	<i>Undefined</i>	<i>Undefined</i>

Now, let's define these functions!

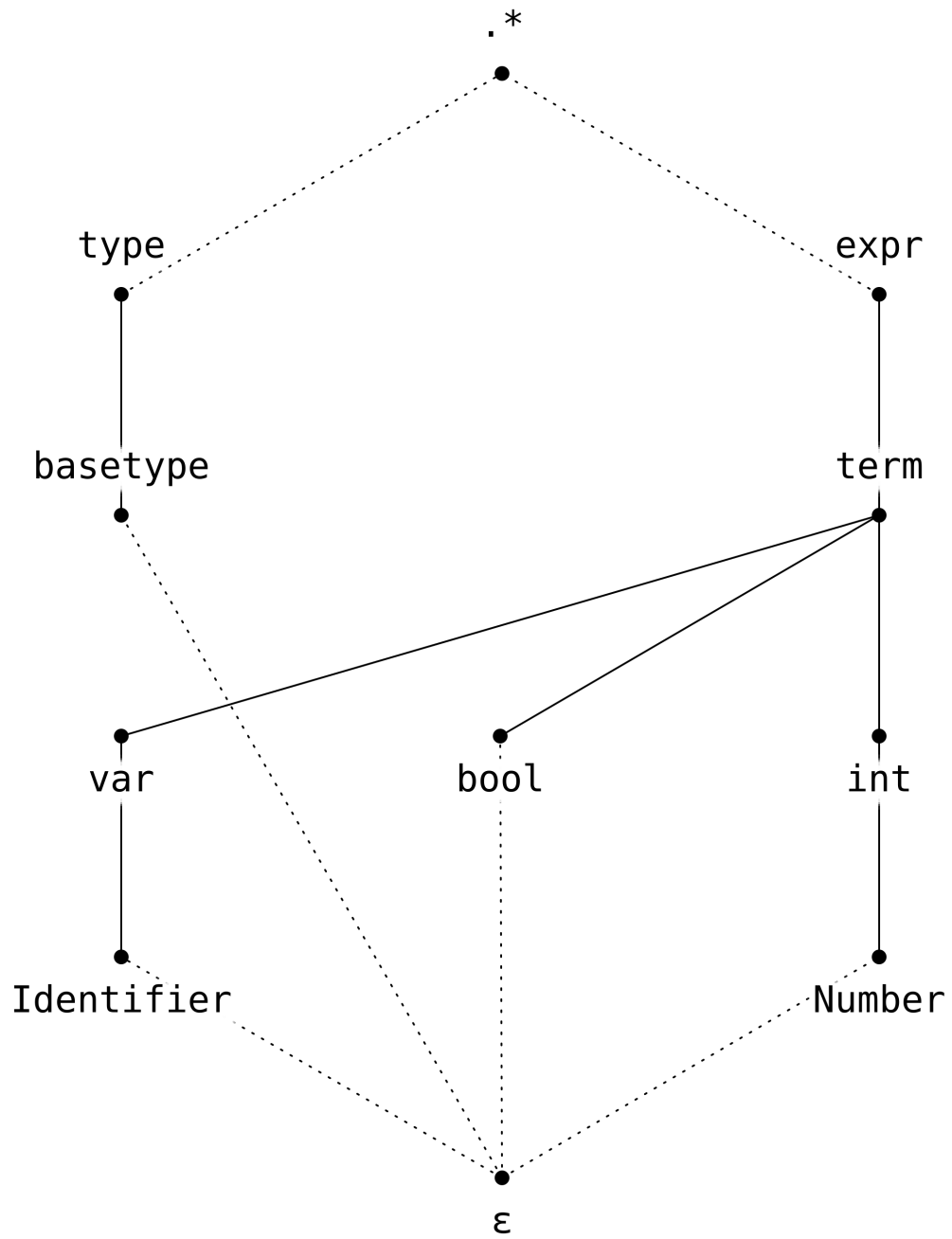


Figure 2.5: The final subtyping relationship of STFL.language



### 2.2.2 The function section

We add a new header to *STFL.language*:

```
1 | Functions
2 | =====
```

In this function section, we can define the function *domain* in the following way:

```
1 | domain : type -> type
2 | domain(T1 "->" T2) = T1
```

So, what is going on here? Let's first take a look to the first line:

```
1 | domain : type -> type
```

The *domain* is the name of the function. The *type -> type* indicates what syntactic form is taken as input (a *type*) before the *->* and what is given as output (again a *type*). You probably noticed the similarity between the types declared in our own STFL and this declaration. This is intentional. This is quite meta, don't get confused!



Figure 2.6: Relevant XKCD (by Randall Munroe, #917)

### 2.2.3 Pattern matching

Let's have look at the body of the function:

```
1 | domain(T1 "->" T2) = T1
```

What happens if we throw in *Int -> Bool*? Remember that this is parsed as a tree, with three leafs. Notice that there are three elements in the pattern match too: a variable *T1*, a literal *->* and a variable *T2*. These leafs are matched respectively:

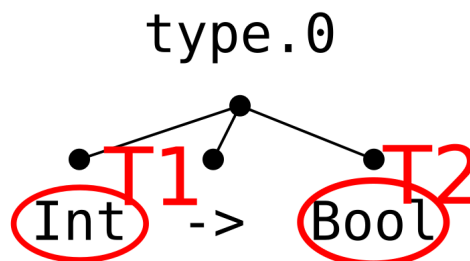


Figure 2.7: Pattern matching in action

The same principle applies with more advanced inputs:

We thus always bind *T1* to the part before the top-level *->*, in other words: we always bind the input type (or domain type) to *T1*. As that is exactly what we need, we return it!

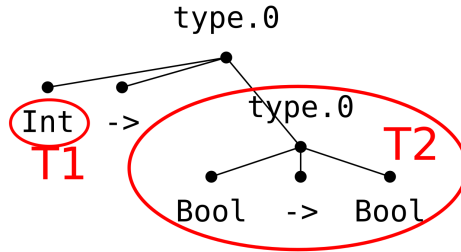


Figure 2.8: Pattern matching in action (more advanced)

#### 2.2.4 Missing cases

This already gives us the most important part. However, what should we do if the first argument is a function type (e.g.  $(\text{Int} \rightarrow \text{Bool}) \rightarrow \text{Bool}$ )?

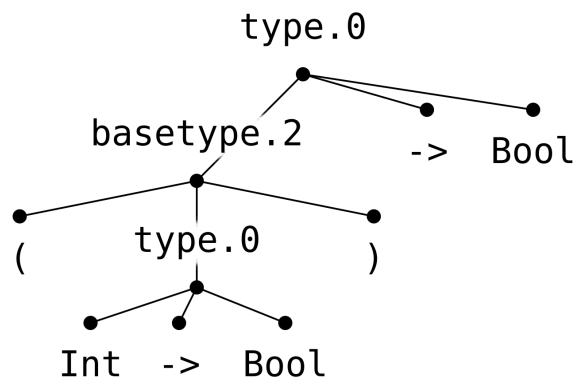


Figure 2.9: Typetree of function argument

This will match the pattern  $T1 \rightarrow T2$  as following:

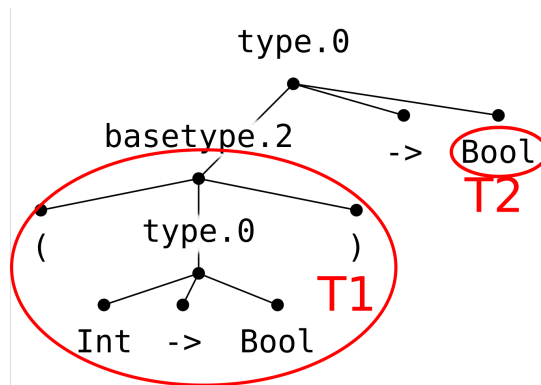


Figure 2.10: Typetree of function argument, matched

We see that  $T1$  includes the  $($  and  $)$ , which we don't want. We simply solve this by adding a extra clause:

```

1 | domain                               : type -> type
2 | domain((" T1 ") "->" T2)             = T1
3 | domain(T1 "->" T2)                   = T1

```

We expect that the part *before* the arrow now is surrounded by parens. Note that we put parens once without double quotes and once with. These parens capture this part of the parsetree and match

it against the patterns inside the parens, as visible in the green ellipse:

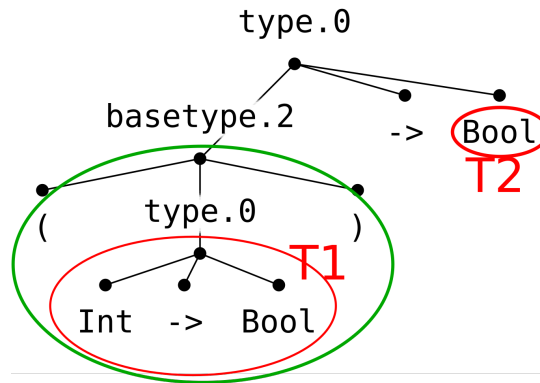


Figure 2.11: Recursive pattern matching

## 2.2.5 Recursion

There is a last missing case, namely if the entire type is wrapped in parens.

We match a type between parens, and then calculate its domain simply by calling the domain function again.

```

1 | domain          : type -> type
2 | domain("(" T ")") = domain(T)
3 | domain("(" T1 ")" "->" T2) = T1
4 | domain(T1 "->" T2) = T1

```

## 2.2.6 Clause determination

As you can see, there are three clauses now. What clause is executed?

Simply put, when the function is evaluated, the arguments are pattern matched against the first clause. If this pattern match succeeds, the expression on the right hand side is returned. Do the arguments not match the patterns? Then the next clause is considered.

In other words, clauses are tried **from top to bottom** and tested. The first clause of which the patterns match, is executed.

When no clauses match, an error message is given.

## 2.2.7 Executing functions

Let's put this to a test. We can calculate the domain of our examples.

Create a file `typeExamples.stfl`, with contents

```

1 | Int -> Bool
2 | (Int -> Bool)
3 | Int -> Bool -> Bool
4 | Int -> (Bool -> Bool)
5 | (Int -> Bool) -> Bool
6 | Int
7 | Bool

```

Run this with `ALGT STFL.language typeExamples.stfl type -l -f domain:`

```

While checking file STFL.language:
Warning:
  While checking the totality of function "domain":
    Following calls will fall through:
      domain("Bool")
      domain("Int")

```

```

# "Int -> Bool" applied to domain
Int

# "(Int -> Bool)" applied to domain
Int

# "Int -> Bool -> Bool" applied to domain
Int

# "Int -> (Bool -> Bool)" applied to domain
Int

# "(Int -> Bool) -> Bool" applied to domain
Int -> Bool

# "Int" applied to domain
Not a single clause of domain matched:
  While pattern matching clause 0:
    In Pattern matching clause 0 with arguments: (Int)
    In domain(Int)
  :
  FT: Could not pattern match 'Int' over '(" T ")'
  While pattern matching clause 1:
    In Pattern matching clause 1 with arguments: (Int)
    In domain(Int)
  :
  FT: Could not pattern match 'Int' over '(" T1 ") -> T2'
  While pattern matching clause 2:
    In Pattern matching clause 2 with arguments: (Int)
    In domain(Int)
  :
  FT: Could not pattern match 'Int' over 'T1 -> T2'

# "Bool" applied to domain
Not a single clause of domain matched:
  While pattern matching clause 0:
    In Pattern matching clause 0 with arguments: (Bool)
    In domain(Bool)
  :
  FT: Could not pattern match 'Bool' over '(" T ")'
  While pattern matching clause 1:
    In Pattern matching clause 1 with arguments: (Bool)
    In domain(Bool)
  :
  FT: Could not pattern match 'Bool' over '(" T1 ") -> T2'
  While pattern matching clause 2:
    In Pattern matching clause 2 with arguments: (Bool)
    In domain(Bool)
  :
  FT: Could not pattern match 'Bool' over 'T1 -> T2'

```

What does this output tell us?

For starters, we get a warning that we forgot two cases, namely `Bool` and `Int`. For some functions this is a problem, but `domain` is not defined for those values. Note that a bunch of other tests are builtin as well.<sup>7</sup>

Then, we see an overview for each function what result it gives (or an error message if the pattern matches failed).

If you want more information about the behaviour of a function, specify `--ia` or `--ifa FUNCTION-TO-ANALYZE` to get a clause-per-clause overview:

```

Analysis of domain : type -> type
=====

Analysis of clause 0

```

<sup>7</sup>We'll silently ignore these warnings for the rest of the tutorial with flag `--no-checks`

```

.....

Clause:
  domain("(" T ")")      = domain(T)

Possible inputs at this point:
# (type)

Possible results:
0  "(" type(0/1/2:1) ")": basetype/2      --> type( (Function call - ID not retrieved)

Analysis of clause 1
.....

Clause:
  domain("(" T1 ") " -> " T2)
                                = T1

Possible inputs at this point:
# ("Bool")
# ("Int")
# ((basetype " -> " type))

Possible results:
1  "(" type(0/0:0/2:1) ")": basetype/2 " -> " type(0/0:2)): type/0      --> type(0

Analysis of clause 2
.....

Clause:
  domain(T1 " -> " T2)      = T1

Possible inputs at this point:
# ("Bool")
# ("Int")
# (("Bool" " -> " type))
# (("Int" " -> " type))

Possible results:
2  ("Bool" " -> " type(0/0:2)): type/0      --> "Bool"      : "basetype"
2  ("Int" " -> " type(0/0:2)): type/0      --> "Int"       : "basetype"

Falthrough
-----

("Bool")
("Int")

```

## 2.2.8 Codomain

codomain can be implemented analogously:

```

1 | codomain      : type -> type
2 | codomain("(" T ")") = codomain(T)

```

```

3 | codomain(T1 "->" ("(" T2 ")")) = T2
4 | codomain(T1 "->" T2)          = T2

```

## 2.3 Building the typechecker

Now that we have some experience with natural deduction, we can slay the next dragon: the typechecker!

For those unfamiliar, the typechecker looks at the expression and determines the type of it and halts on inconsistencies, such as `1 + True Or If True Then 0 Else False`, ...

we will build a single rule for each syntactic choice of `expr`; thus a rule for:

- The constants `True` and `False`
- The constant `Numbers`
- Typing plus
- Typing `If ... Then ... Else ...`
- Typing lambda's ( $\lambda x : T . e$ )
- Typing variables `x`
- Typing application

### 2.3.1 The typing environment

Before where start, how should we type a variable, such as `x`? Of course, this depends on the environment. In the lambda ( $\lambda x : \text{Int} . x$ ), `x` should be typed as a `Int`, while in the lambda ( $\lambda x : \text{Bool} . x$ ), this `x` clearly is a `Bool`.

We could type the inner expressions by substituting a simple default value in the expression, and then typing it. However, this doesn't scale to more advanced languages.

The other, more general solution is keeping track of the type of each variable. We declare a simple list to keep track of the types in the `Syntax` Section:

```

1 | typing          ::= var ":" type
2 | typingEnvironment ::= typing "," typingEnvironment | "{}"

```

The `typing` represents a data entry, whereas the `typingEnvironment` can contain zero or more of these data entries, thus keeping track of the variable types.

The typing relation is often denoted with a uppercase gamma,  $\Gamma$ . We will follow this convention<sup>8</sup>.

### 2.3.2 The typing relation

We're all set now! What should our typing relation look like? First, we'll want to take a `typingRelation` as input, together with an `expr`. This should be enough to calculate the `type` of the expression.

In other words, the type of the relation is `typingRelation (in), expr (in), type (out)`. In the academic world, this is often given the symbol  $\vdash$ <sup>9</sup>, pronounced *entails* or *out of this environment follows this typing*.

So, our declaration becomes:

```

1 | (⊢) : typingEnvironment (in), expr (in), type (out) Pronounced as "entails typing"

```

### 2.3.3 Typing constants True and False

It's pretty easy to type constants, such as `42` and `True`.

Let us start with typing the constant `True`.

```

1 | ----- [TboolTrue]
2 | Γ ⊢ "True", "Bool"

```

If this looks magical: we take the typing environment as input (but don't use it), pattern match on a literal `True` and return the known type `Bool`.

We can do the same for `False`:

<sup>8</sup>Type `Ctrl+Shift+U 0393` on linux to input `Gamma`. On Windows, hold down `Alt` and type `+ 0393`.

<sup>9</sup>Type `Ctrl+Shift+U 22a2` on linux to input `entails`. On Windows, hold down `Alt` and type `+ 22a2`.

```

1 | ----- [TboolFalse]
2 |
3 |  $\Gamma \vdash \text{"False"}, \text{"Bool"}$ 

```

### 2.3.4 Typing constant Numbers

Our next challenge is giving a type to `ints`. Making a single rule for each number is a bit hard, especially because there is an infinite amount of them...

However, we can simply fix this by adding a predicate, checking that our input is a number:

```

1 | n:int
2 | ----- [Tnumber]
3 |  $\Gamma \vdash n, \text{"Int"}$ 

```

Remember that our predicates are written above the line.

### 2.3.5 Typing against an empty environment

Let's try to run our typing relation, with `./ALGT STFL.language expr -l -r  $\vdash$`

```

# Could not apply relation  $\vdash$  to the input "True", because:
While trying to proof that ( $\vdash$ ) is applicable to "True":
Expected 2 arguments to relation  $\vdash$ , but only got 1

```

Well, that didn't work. The tool expects two arguments; but only one is provided...

To solve this, we declare yet another relation, in which we type an expression against an empty environment:

```

1 | n:int
2 | ----- [Tnumber]
3 |  $\Gamma \vdash n, \text{"Int"}$ 

```

Retrying with the new relation (`./ALGT STFL.language examples.stfl expr -l -r ::`) gives us:

```

# True applied to ::
# Proof weight: 2, proof depth: 2

----- [TboolTrue]
{}  $\vdash$  True, Bool
----- [TEmptyCtx]
True :: Bool

# False applied to ::
# Proof weight: 2, proof depth: 2

----- [TboolFalse]
{}  $\vdash$  False, Bool
----- [TEmptyCtx]
False :: Bool

```

```

# If True Then False Else True applied to ::
# Proof weight: 6, proof depth: 3

-----
{}  $\vdash$  True, Bool  {}  $\vdash$  False, Bool  {}  $\vdash$  True, Bool  T1 = Bool = Tr
-----
{}  $\vdash$  If True Then False Else True, Bool
-----
If True Then False Else True :: Bool

```

### 2.3.6 Typing plus

Another expression we'll want to type are additions.

Of course, this will always return an `Int`, but there is more. `True + False` is not valid, whereas `1 + 1` can be typed. In other words, we have to check that the arguments to `+` are both numbers.

We could thus type `+` as following:

1	$n1 : \text{Number} \quad n2 : \text{Number}$	
2	-----	[TPlus]
3	$\Gamma \vdash n1 \text{ "+" } n2, \text{"Int"}$	

This works for `1 + 2`, but not for `1 + (2 + 3)`, as `(2 + 3)` is *not* a syntactic form that is a literal `Number`. It can be typed as `Int` though, so we can generalize our predicates by using the typing relationship recursively:

1	$\Gamma \vdash n1, \text{"Int"} \quad \Gamma \vdash n2, \text{"Int"}$	
2	-----	[TPlus]
3	$\Gamma \vdash n1 \text{ "+" } n2, \text{"Int"}$	

Looks good! Time to give this a try:

```
# 1 + 2 + 3 applied to ::
# Proof weight: 9, proof depth: 5

      2 : int      3 : int
      -----
1 : int      {} ⊢ 2, Int      {} ⊢ 3, Int
-----
{} ⊢ 1, Int      {} ⊢ 2 + 3, Int
-----
{} ⊢ 1 + 2 + 3, Int
-----
1 + 2 + 3 :: Int
```

### 2.3.7 Typing If

It is pretty straightforward that the condition should be a `Bool`, which already gives a draft of the rule:

1	$\Gamma \vdash \text{cond}, \text{"Bool"}$	
2	-----	[TIf]
3	$\Gamma \vdash \text{"If" cond "Then" e1 "Else" e2, ???}$	

We also want to make sure that both `e1` and `e2` are correctly typed, so we recursively typecheck them:

1	$\Gamma \vdash \text{cond}, \text{"Bool"} \quad \Gamma \vdash e1, T1 \quad \Gamma \vdash e2, T2$	
2	-----	[TIf]
3	$\Gamma \vdash \text{"If" cond "Then" e1 "Else" e2, ???}$	

But what type should we return? The type of `e1` or `e2`?

Consider expression `If True Then 0 Else False`. Evaluating this yields `0`. However, expression `If False Then 0 Else False` would yield `False`. In other words, depending on the runtime value of the condition, we might get a different type.

That's not behaviour we want. The types of `e1` and `e2` should be the same to function correctly. We add a predicate to check this:

1	$\Gamma \vdash \text{cond}, \text{"Bool"} \quad \Gamma \vdash e1, T1 \quad \Gamma \vdash e2, T2 \quad T1 = T2$	
2	-----	[TIf]
3	$\Gamma \vdash \text{"If" cond "Then" e1 "Else" e2, ???}$	

Now we can also return a type; as `T1` and `T2` are the same, we just pick one:

1	$\Gamma \vdash c, \text{"Bool"} \quad \Gamma \vdash e1, T1 \quad \Gamma \vdash e2, Tr \quad T1 = Tr : \text{type}$	
2	-----	[TIf]
3	$\Gamma \vdash \text{"If" c "Then" e1 "Else" e2, T1}$	

All done! Time to give it a try:



```
# If True Then False Else True applied to ::
# Proof weight: 6, proof depth: 3

-----
{} ⊢ True, Bool   {} ⊢ False, Bool   {} ⊢ True, Bool   T1 = Bool = Tr
-----
{} ⊢ If True Then False Else True, Bool
-----
If True Then False Else True :: Bool
```

### 2.3.8 Typing lambda's

Typing lambda's is a bit complicated. Remember that a lambda such as  $(\lambda x : T . e)$  means that, *given  $x$  of type  $T$  as input argument, it gives back expression  $e$  with  $x$  replaced.*

This gives us quite some clues about what to do.

Let's start with the skeleton of the rule:

```
1 | ???
2 | ----- [TLambda]
3 | Γ ⊢ "(" "\\ " x ":" T1 "." e ")", ???
```

Of course, we'll want to type  $e$  just as well. Not only to check whether it is correct, but also because we'll need its type later on:

```
1 | Γ ⊢ e, T1
2 | ----- [TLambda]
3 | Γ ⊢ "(" "\\ " x ":" T1 "." e ")", ???
```

This is close to what we want, but there is a catch though: in the expression  $e$ , we know that  $x$  has the type  $T1$ . We should pass this knowledge to the typing of  $e$ , by adding it to the typing environment  $\Gamma$ :

```
1 | (x ":" T1) ", " Γ ⊢ e, T2
2 | ----- [TLambda]
3 | Γ ⊢ "(" "\\ " x ":" T1 "." e ")", ???
```

So far, so good! The only question remaining is what type we should return. We know we have input of type  $T1$  and output of type  $T2$ . That's where our  $\rightarrow$  comes into play: the entire lambda has type  $T1 \rightarrow T2$ !

There is a little technicality into play here though:  $T1$  might be some complicated type, such as  $\text{Int} \rightarrow \text{Bool}$  - meaning we expect a *function* as input argument. If we would write  $\text{Int} \rightarrow \text{Bool} \rightarrow T2$ , that would be read as function taking *two* arguments: first a  $\text{Int}$ , followed by a  $\text{Bool}$ . Not quite the same thus.

The fix for this is simple: add parentheses. The type of a lambda is  $(T1) \rightarrow T2$ .

Typing this out as rule yields:

```
1 | (x ":" T1) ", " Γ ⊢ e, T2
2 | ----- [TLambda]
3 | Γ ⊢ "(" "\\ " x ":" T1 "." e ")", ( "(" T1 ")" "->" T2
```

Note that an extra pair of parentheses was added; one pair is between double quotes, denoting that this should be added in the parse tree; the other pair just groups them together to help the tool build the parsetree.

### 2.3.9 Typing variables

Before we can see typing of lambda's live, we need to take another hurdle: typing variables.

You'll probably think it'll be a lot of work to design the searching behaviour, but luckily, there is a special construction that does exactly that. Remember the evaluation context? We can use this builtin here too:

```
1 | ----- [Tx]
2 | Γ[ x ":" T ] ⊢ x, T
3 |
```

Quite succinct! If you're a bit puzzled about its workings, we stated to ALGT that it should search a typing of  $x$ , where  $x$  is exactly the name of the variable we want to type.

At this point, we can finally type a single lambda:

```
# (\x : Int . x + 1) applied to ::
# Proof weight: 6, proof depth: 5

----- [Tx]          1 : int
x : Int , {} ⊢ x, Int   x : Int , {} ⊢ 1, Int
----- [Tnumber]
x : Int , {} ⊢ x + 1, Int
----- [TPlus]
{} ⊢ ( \ x : Int . x + 1 ), ( Int ) -> Int
----- [TLambda]
( \ x : Int . x + 1 ) :: ( Int ) -> Int
----- [TEmpyCtx]
```

### 2.3.10 Typing application

The typechecker is nearly complete, only a single syntactic form can't be typed yet: application of the form function argument.

How can we tackle this problem? For starters, we'll have to type the function and argument

```
1 | Γ ⊢ func, TFunc   Γ ⊢ arg, TArg
2 | ----- [TApp]
3 | Γ ⊢ func arg, ???
```

A function has a determined input argument, also known as the *domain* of the function. To be well typed, the domain should match the type of the argument exactly. But how can we get this argument?

Luckily, we created a function earlier on that calculates exactly that! We can simply use `domain` and check that it's result equals `TArg`:

```
1 | Γ ⊢ func, TFunc   Γ ⊢ arg, TArg   domain(TFunc) = TArg
2 | ----- [TApp]
3 | Γ ⊢ func arg, ???
```

Nearly done! Only question left is what type we should return.

This is pretty straightforward too, as we earlier made the function `codomain` which exactly calculates the return type of `TFunc`

```
1 | Γ ⊢ e1, Tfunc   Γ ⊢ e2, Targ   Targ = domain(Tfunc) : type
2 | ----- [Tapp]
3 | Γ ⊢ e1 e2, codomain(Tfunc)
```

All finished now, except for trying of course:

```
# (\x : Int . x + 1) 41 applied to ::
# Proof weight: 10, proof depth: 6

----- 1 : int
x : Int , {} ⊢ x, Int   x : Int , {} ⊢ 1, Int
-----
x : Int , {} ⊢ x + 1, Int
-----
{} ⊢ ( \ x : Int . x + 1 ), ( Int ) -> Int
-----
{} ⊢ ( \ x : Int . x + 1 ) 41, Int
-----
( \ x : Int . x + 1 ) 41 :: Int

----- 41 : int
{} ⊢ 41, Int   Targ = Int = domain(Tfunc)
```

## 2.4 Evaluator and typechecker: recap

Our declared relations are:

```

1  Relations
2  =====
3
4  ( $\rightarrow$ )      : expr (in), expr (out)          Pronounced as "small step"
5  ( $\rightarrow^*$ )    : expr (in), expr (out)          Pronounced as "big step"
6  ( $\checkmark$ )     : expr (in)                      Pronounced as "is canonical"
7
8  ( $\vdash$ )       : typingEnvironment (in), expr (in), type (out) Pronounced as "entails typing"
9
10 ( $:::$ )        : expr (in), type (out) Pronounced as "type in empty context"

```

The definition of those relations are:

```

1  Rules
2  =====
3
4
5
6
7  expr0  $\rightarrow$  expr1
8  ----- [EvalCtx]
9  expr[expr0]  $\rightarrow$  expr[expr1]
10
11
12
13  n1:Number          n2:Number
14  ----- [EvalPlus]
15  n1 "+" n2  $\rightarrow$  !plus(n1, n2)
16
17
18
19
20 ----- [EvalIfTrue]
21 "If" "True" "Then" e1 "Else" e2  $\rightarrow$  e1
22
23
24 ----- [EvalIfFalse]
25 "If" "False" "Then" e1 "Else" e2  $\rightarrow$  e2
26
27
28 ----- [EvalLamApp]
29 ("(" "\\\" var ":" type "." e ")") arg  $\rightarrow$  !subs:expr(var, arg, e)
30
31
32
33
34  i:int
35  ----- [CanonInt]
36  ( $\checkmark$ ) i
37
38
39  b:bool
40  ----- [CanonBool]
41  ( $\checkmark$ ) b
42
43
44
45
46  ( $\checkmark$ ) e
47  ----- [BigStepBase]
48  e  $\rightarrow^*$  e
49
50  e0  $\rightarrow$  e1          e1  $\rightarrow^*$  e2
51  ----- [BigStepRec]
52  e0  $\rightarrow^*$  e2
53
54
55
56
57
58  "{}"  $\vdash$  e, T

```

```

59 ----- [TEmptyCtx]
60 e :: T
61
62
63
64 ----- [TboolTrue]
65 Γ ⊢ "True", "Bool"
66
67
68 ----- [TboolFalse]
69 Γ ⊢ "False", "Bool"
70
71
72
73 n:int
74 ----- [Tnumber]
75 Γ ⊢ n, "Int"
76
77
78
79
80
81
82
83 ----- [Tx]
84 Γ[ x ":" T ] ⊢ x, T
85
86
87
88 Γ ⊢ n1, "Int"   Γ ⊢ n2, "Int"
89 ----- [TPlus]
90 Γ ⊢ n1 "+" n2, "Int"
91
92
93 Γ ⊢ c, "Bool"   Γ ⊢ e1, T1       Γ ⊢ e2, Tr       T1 = Tr : type
94 ----- [TIf]
95 Γ ⊢ "If" c "Then" e1 "Else" e2, T1
96
97
98
99 (x ":" T1) ", " Γ ⊢ e, T2
100 ----- [TLambda]
101 Γ ⊢ "(" "\\ x ":" T1 "." e )", ( "(" T1 ")" ) "->" T2
102
103
104
105 Γ ⊢ e1, Tfunc   Γ ⊢ e2, Targ       Targ = domain(Tfunc) : type
106 ----- [Tapp]
107 Γ ⊢ e1 e2, codomain(Tfunc)

```

Running the relation `::` on all our examples with flags `./ALGT STFL.language True False If True Then False Else True If If` gives:

```

# True applied to ::
# Proof weight: 2, proof depth: 2

-----
{} ⊢ True, Bool
-----
True :: Bool

# False applied to ::
# Proof weight: 2, proof depth: 2

-----
{} ⊢ False, Bool

```

```

-----
False :: Bool

# If True Then False Else True applied to ::
# Proof weight: 6, proof depth: 3

-----
{} ⊢ True, Bool  {} ⊢ False, Bool  {} ⊢ True, Bool  T1 = Bool = Tr
-----
{} ⊢ If True Then False Else True, Bool
-----
If True Then False Else True :: Bool

# 42 applied to ::
# Proof weight: 3, proof depth: 3

42 : int
-----
{} ⊢ 42, Int
-----
42 :: Int

# 20 + 22 applied to ::
# Proof weight: 6, proof depth: 4

20 : int      22 : int
-----
{} ⊢ 20, Int  {} ⊢ 22, Int
-----
{} ⊢ 20 + 22, Int
-----
20 + 22 :: Int

# 1 + 2 + 3 applied to ::
# Proof weight: 9, proof depth: 5

      2 : int      3 : int
      -----
1 : int  {} ⊢ 2, Int  {} ⊢ 3, Int
-----
{} ⊢ 1, Int  {} ⊢ 2 + 3, Int
-----
{} ⊢ 1 + 2 + 3, Int
-----
1 + 2 + 3 :: Int

# (λx : Int . x + 1) 41 applied to ::
# Proof weight: 10, proof depth: 6

      1 : int
      -----

```

```

x : Int , {} ⊢ x, Int  x : Int , {} ⊢ 1, Int
-----
x : Int , {} ⊢ x + 1, Int                                41 : int
-----
{} ⊢ ( \ x : Int . x + 1 ), ( Int ) -> Int                {} ⊢ 41, Int  Targ = Int = domain(Tfunc)
-----
{} ⊢ ( \ x : Int . x + 1 ) 41, Int
-----
( \ x : Int . x + 1 ) 41 :: Int

```

## 2.5 Syntax Styling

As a bonus, syntax styling is supported out of the box just as well! While this is not a fundamental aspect of a programming language, it is quite fun - and important when presenting.

### 2.5.1 Declaring the syntax style

The syntax style is defined in a section `Syntax Style` just beneath the actual syntax:

```

1 | Syntax Style
2 | =====

```

You can map a syntactic form onto a style:

```

1 | type          -> "type"
2 | basetype      -> "type"

```

These say that both `type` and `typeTerm` should be rendered with style `type`.

It's also possible to pick a choice of a syntactic form, by choosing the zero-based<sup>10</sup> index:

```

1 | term.0 -> "keyword"

```

This would take the first choice of `term`, thus the one with “If”, “Then” and “Else” and render those as keywords. The nested expressions will be rendered independently.

As a quick reminder, the syntax of `term` is.

```

1 | term      ::= "If"  expr "Then" expr "Else" expr
2 |           | "("  "\\" var ":" type "." expr ")"
3 |           | bool
4 |           | int
5 |           | var

```

The full syntax style is:

```

1 | Syntax Style
2 | =====
3 |
4 | type          -> "type"
5 | basetype      -> "type"
6 |
7 | Identifier    -> "identifier"
8 | Number       -> "constant"
9 | bool         -> "constant"
10 | expr         -> "statement"
11 | term.1       -> "noise"
12 | term.0       -> "keyword"

```

This yields the following result:

```
{( \ cond : Bool . If cond Then 41 + 1 Else 0 ) True }
```

### 2.5.2 Other color schemes

If you don't like the *green-on-black* color scheme, other color schemes are provided as well. Select one with the `--style`-flag.

<sup>10</sup>As all sane computer languages, the first choiced is assigned index 0, the second is index 1, ...

- Terminal
- White
- WhiteFlat

Giving:

Style	Output
White	{( \ cond : Bool . If cond Then 41 + 1 Else 0 ) True}
WhiteFlat	{( \ cond : Bool . If cond Then 41 + 1 Else 0 ) True}
Terminal	{(\ cond : Bool . If cond Then 41 + 1 Else 0 ) True}

You can also define and specify your own color scheme; see the reference manual.





# Chapter 3

## Reference manual

### 3.1 General

A language is defined in a `.language`-file. It starts (optionally) with a title:

```
1
2  Language Name
3  *****
```

Comments start with a `#` and can appear quasi everywhere.

```
1
2  # This is a comment
```

Syntax, functions, relations, ... are all defined in their own sections:

```
1
2  Syntax
3  =====
```

A section header starts with an upper case, is underlined with `=` and followed by a blank line.

### 3.2 Syntax

All syntax is defined in the `Syntax` section. It consists out of `BNF`-rules, of the form

```
1  name      ::= "literal" | choice | seq1 seq2
```

Choices might be written on multiple lines, as long as at least one tab precedes them:

```
1  name      ::= choice1 | choice2
2              | choice3
```

#### 3.2.1 Literals

A string that should be matched exactly, is enclosed in `"` (double quotes). Some characters can be escaped with a backslash, namely:

Table 3.1: Escape sequences

Sequence	Result
<code>\n</code>	newline
<code>\t</code>	tab
<code>\"</code>	double quote
<code>\\</code>	backslash

### 3.2.2 Parsing order

Rules are parsed **left to right**, in other words, choices are tried in order. No backtracking happens when a choice is made; the parser is a *recursive descent parser*. This has two drawbacks: left recursion results in an infinite loop and the ordering of choices does matter.

```

1  # Left recursion, error message.
2  expr    ::= expr "+" int
3
4  # 'int' already consumes a part of 'int + int', error message
5  expr    ::= int | int "+" int
6
7  # Common part extraction, error message
8
9  # Correct
10 expr   ::= int "+" int | int

```

### 3.2.3 Builtin syntactic forms

Some syntactic forms are already provided for your convenience, namely:

Table 3.2: Builtin syntax

Builtin	Meaning	Regex
Identifier	Matches an identifier	<code>[a-z][a-zA-Z0-9]*</code>
Number	Matches an (negative) integer. Integers parsed by this might be passed into the builtin arithmetic functions.	<code>-?[0-9]*</code>
Any	Matches a single character, whatever it is, including newline characters	<code>.</code>
Lower	Matches a lowercase letter	<code>[a-z]</code>
Upper	Matches an uppercase letter	<code>[A-Z]</code>
Digit	Matches an digit	<code>[0-9]</code>
Hex	Matches a hexadecimal digit	<code>[0-9a-fA-F]</code>
String	Matches a double quote delimited string, returns the value including the double quotes	<code>"([^\\" \\\" \\\\)*)"</code>
StringUnesc	Matches a double quote delimited string, returns the value without the double quotes	<code>"([^\\" \\\" \\\\)*)"</code>
LineChar	Matches a single character that is not a newline. This includes :	<code>[^\n]</code>
ParO	Matches a '(', which will dissapear in the parsetree	<code>(</code>
ParC	Matches a ')', which will dissapear in the parsetree	<code>)</code>

### 3.2.4 Subtyping relationship

A syntactic form equals a (possibly infinite) set of strings. By using a syntactic form  $\mathbf{a}$  as choice in other syntactic form  $\mathbf{b}$ ,  $\mathbf{a}$  will be a subset of  $\mathbf{b}$ , giving the natural result that  $\mathbf{a}$  is a subtype of  $\mathbf{b}$ .

In the following example, `bool` and `int` are both subsets of `expr`. This can be visualised with the `--svg` `Output.svg`-flag.

```
1 | bool    ::= "True" | "False"
2 | int     ::= Number
3 | expr    ::= ... | bool | int
```

### 3.2.5 Whitespace in sequences

Whitespace (the characters " ", "\t"), is parsed by default (and ignored completely). If you want to parse a whitespace sensitive language, use other symbols to declare the rule:

Table 3.3: Whitespace modes

Operator	Meaning
::=	Totally ignore whitespace
~~=	Parse whitespace for this rule only
//=	Parse whitespace for this rule and all recursively called rules

This gives rise to the following behaviour:

Table 3.4: Whitespace mode examples

Syntax	Matching String
<code>a ::= "b" "c" x</code>	<code>b c x y</code>
<code>x ::= "x" "y"</code>	<code>bcxy</code> <code>b\tc\tx\ty</code> <code>b c\txy</code> <code>...</code>
<code>a ~~= "b" "c" x</code>	<code>bcx y</code>
<code>x ::= "x" "y"</code>	<code>bcxy</code> <code>bcx\ty</code>
<code>a //= "b" "c" x</code>	<code>bcxy</code>
<code>x ::= "x" "y"</code>	

### 3.2.6 Grouping sequences

Sometimes, you'll want to group an entire rule as a token (e.g. comments, an identifier, ...)

Add a `$` after the assignment to group it.

```

1 | text                ::= LineChar line | LineChar
2 | commentLine        ::= $ "#" text "\n"
3 |
4 | customIdentifier    ::= $ Upper Number

```

When such a token is used in a pattern or expression, the contents of this token are parsed against this rule:

```

1 | f                  : customIdentifier -> statement
2 | f("X10")          = "X9" "#" Some comment "

```

## 3.3 Syntax Style

### 3.3.1 Builtin styles

Select a style with the `--style StyleName` flag.

Style	Terminal	White	WhiteFlat
statement	<code>statement</code>	statement	statement
identifier	<code>identifier</code>	identifier	identifier
type	<code>type</code>	type	type
constant	<code>constant</code>	constant	constant
keyword	<code>keyword</code>	keyword	keyword
special-char	<code>special-char</code>	special-char	special-char
number	<code>number</code>	number	number
float	<code>float</code>	float	float

Style	Terminal	White	WhiteFlat
builtin	<b>builtin</b>	builtin	builtin
variable	<b>variable</b>	variable	variable
preprocessor	<b>preprocessor</b>	preprocessor	preprocessor
comment	<b>comment</b>	comment	comment
noise	<b>noise</b>	noise	noise
header1	<b>header1</b>	header1	header1
header2	<b>header2</b>	header2	header2
header3	<b>header3</b>	header3	header3
header4	<b>header4</b>	header4	header4
header5	<b>header5</b>	header5	header5
header6	<b>header6</b>	header6	header6
emph	<b>emph</b>	emph	emph
bold	<b>bold</b>	bold	bold
url	<b>url</b>	url	url
monospace	<b>monospace</b>	monospace	monospace
hline	<b>hline</b>	hline	hline
note	<b>note</b>	note	note
warning	<b>warning</b>	warning	warning
error	<b>error</b>	error	error
todo	<b>todo</b>	todo	todo
fixme	<b>fixme</b>	fixme	fixme
cursor	<b>cursor</b>	cursor	cursor
linehighlight	<b>linehighlight</b>	linehighlight	linehighlight
selection	<b>selection</b>	selection	selection
linenumbers	<b>linenumbers</b>	linenumbers	linenumbers

### 3.3.2 Creating your own style

Select your own style with `--style Name.style` (the extension `.style` triggers the external style).

A stylefile looks as:

```

1  Name
2  *****
3
4  Constants
5  =====
6
7  # Here come shorthands for often used values, e.g.:
8  black          = #000000
9  stringVal      = "someString"
10 intValue      = 14
11
12 Defaults
13 =====
14
15 # Here come the defaults, thus the general properties for every default line
16
17 # literal assignment uses '='
18 foreground-color = #00ff00
19 # recall of a constant defined in the first section uses ':'
20 background-color : black
21
22 Styles
23 =====
24
25 # The different styles defined. See the matrix for what you might define
26
27 statement
28 -----
29
30 font-style: italic

```

```

31 | keyword (statement)
32 | -----
33 |
34 |
35 | # fallbackstyle between parentheses.
36 | # Attributes not found in this style will be first searched in 'statement'
37 |
38 | font-style: bold

```

### 3.3.3 Supported renderers and attributes

## 3.4 Functions

### 3.4.1 Patterns and expressions

Functions transform their input. A function is declared by first giving its type, followed by one or more clauses:

```

1 | f      : a -> b
2 | f(a, "b") = "c"
3 | f(a, b)  = "d"

```

When an input is given, arguments are pattern matched against the patterns on between parentheses. If the match succeeds, the expression on the right is given. If not, the next clause is given.

Note that using the same variable multiple times is allowed, this will only work if these arguments are the same:

```

1 | f(a, a) = ...

```

Recursion can be used just as well:

```

1 | f("a" a) = f(a)

```

This is purely functional, heavily inspired on Haskell.

### Possible expressions

Expr	Name	As expression
<code>x</code>	Variable	Recalls the parsetree associated with this variable
<code>_</code>	Wildcard	<i>Not defined</i>
<code>42</code>	Number	This number
<code>"Token"</code>	Literal	This string
<code>func(arg0, arg1, ...)</code>	Function call	Evaluate this function
<code>!func:type(arg0, ...)</code>	Builtin function call	Evaluate this builtin function, let it return a type
<code>(expr or pattern:type)</code>	Ascription	Checks that an expression is of a type. Bit useless
<code>e[expr or pattern]</code>	Evaluation context	Replugs <code>expr</code> at the same place in <code>e</code> . Only works if <code>e</code> was created with an evaluation context
<code>a "b" (nested)</code>	Sequence	Builds the parse tree

### Possible patterns

Expr	As pattern
<code>x</code>	Captures the argument as the name. If multiple are used in the same pattern, the captured arguments should be the same or the match fails.

Expr	As pattern
-	Captures the argument and ignores it
42	Argument should be exactly this number
"Token"	Argument should be exactly this string
func(arg0, arg1, ...)	Evaluates the function, matches if the argument equals the result. Can only use variables which are declared left of this pattern
!func:type(arg0, ...)	Evaluates the builtin function, matches if the argument equals the result. Can only use variables which are declared left of this pattern
(expr or pattern:type)	Check that the argument is an element of type
e[expr or pattern]	Matches the parsetree with e, searches a subpart in it matching pattern
a "b" (nested)	Splits the parse tree in the appropriate parts, pattern matches the subparts

### 3.4.2 Typechecking

#### Equality

```

1
2   Syntax
3   =====
4
5   a      ::= ...
6   b      ::= ...
7   c      ::= a | b | d
8
9   Functions
10  =====
11
12  f      : a -> b -> c
13  f(x, x) = x

```

When equality checks are used in the pattern matching, the variable will be typed as the smallest common supertype of both types. If such a supertype does not exist, an error message is given.

Note that using a supertype might be a little *too* loose, but won't normally happen in real-world examples.

In the given example, `x` will be typed as `c`, the common super type. In this example, `x` might also be `a`, while this is not possible for the input. This can be solved by splitting of `a | b` as a new rule.

### 3.4.3 Totality- and liveabilitychecks

Can be disabled with `--no-check`, when they take to long.

### 3.4.4 Higher order functions and currying?

Are not possible for now (v 0.2). Perhaps in a future version or when someone really needs it and begs for it.

### 3.4.5 Builtin functions

name	Descr	Arguments
plus	Gives a sum of all arguments (0 if none given)	Number* -> Number
min	Gives the first argument, minus all the other arguments	Number -> Number* -> Number
mul	Multiplies all the arguments. (1 if none given)	Number* -> Number

name	Descr	Arguments
<code>div</code>	Gives the first argument, divided by the product of the other arguments. (Integer division, rounded down))	<code>Number -&gt; Number* -&gt; Number</code>
<code>mod</code>	Gives the first argument, module the product of the other arguments.	<code>Number -&gt; Number* -&gt; Number</code>
<code>neg</code>	Gives the negation of the argument	<code>Number -&gt; Number</code>
<code>equal</code>	Checks that all the arguments are equal. Gives 1 if so, 0 if not.	<code>. * -&gt; . * -&gt; Number</code>
<code>error</code>	Stops the function, gives a stack trace. When used in a rule, this won't match a predicate	<code>. ** -&gt; <math>\epsilon</math></code>
<code>subs</code>	(expression to replace, to replace with, in this expression) Replaces each occurrence of the first expression by the second, in the third argument. You'll want to explicitly type this one, by using <code>subs:returnType("x", "41", "x + 1")</code>	<code>. * -&gt; . * -&gt; . * -&gt; . *</code>
<code>group</code>	Given a parsetree, flattens the contents of the parsetree to a single string	<code>. * -&gt; StringUnesc</code>

## 3.5 Relations and Rules

## 3.6 Properties

## 3.7 Command line flags





# Chapter 4

## Used concepts and algorithms

### 4.1 Automated description of an arbitrary language

#### 4.1.1 Invariants and checks

No common choices

No left recursion -> lattice properties

Left consumption (expr | expr “+” ...) -> error msg

#### 4.1.2 Lattices

#### 4.1.3 Parser interpretation

### 4.2 Abstract interpretation of an arbitrary language

#### 4.2.1 Representation

#### 4.2.2 Subtraction

### 4.3 Functions

### 4.4 Natural deduction representation

### 4.5 Algorithms

#### 4.5.1 Minimal typecheck

#### 4.5.2 Liveability check

#### 4.5.3 Dead clauses check

#### 4.5.4 Abstract interpretation

#### 4.5.5 Rule inputs and output calculation



## Chapter 5

# Dynamization and gradualization



## Chapter 6

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# Chapter 7

## Unicode characters

A short list of usefull unicode characters.

Character	Name	Hexcode
Γ	Gamma	393
→	Right-Arrow	2192
✓	Checkmark	2713
⊢	Entails, vdash	22a2
γ	Lowercase gamma	03b3
ε	Epsilon	025b
λ	Lowercase Lambda	03bb
∨	Disjunction	2228
∧	Conjunction	2227
⇒	Double-Right-Arrow	21d2

### 7.1 On linux:

1. Press `Left-CTRL + Shift + U`
2. Release all
3. Type the hexcode of the character (e.g. 2192 to get →)

### 7.2 On windows:

1. Hold down `Alt`
2. Type `+` (that is the plus of the numeric keypad)
3. Type the hexcode (e.g. 2192 to get →)
4. Release `Alt`

or alternatively, visit [this excellent guide](#).

### 7.3 On Os X

1. Go to `International system preferences → input menu`
2. Check the box next to “Unicode hex”
3. Switch to unicode input in the menu bar
4. Hold `Alt`, enter the hexadecimal unicode value