ALGT - The manual

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# Overview

This document gives an overview of the ALGT-tool. First, a general overview of what the tool does is given and why it was developed. Second, a hands-on tutorial develops a Simply Typed Functional Language (STFL). Thirdly, the reference manual gives an in-depth overview of the possibilities and command line flags. Fourth, some concepts and algorithms are explained more thoroughly, together with properties they use. And at last, the dynamize and gradualize options are explained in depth, as these are what the master dissertation is about.

This documentation is about version 0.1.25 (Total quickcheck), generated on 2017-3-13.

## What is ALGT?

ALGT (Automated Language Generation Tool  $^1$ ) is a tool to formally specify any programming language. This is done by first declaring a syntax, using BNF, and then declaring semantics by introducing logical deduction rules, such as evaluation or typing rules. Eventually, properties can be introduced which can be tested. Of course, these can be run.

The tool is kept as general as possible, so any language can be modelled.

 $<sup>^1\</sup>mathrm{Note}$  the similarity of ALGT and AGT . The tool started its life as AGT, based on the paper Abstracting~Gradual~Typing. When it became more general, another name and acronym was chosen.

# Tutorial: developing a simple programming language

We will develop a programming language which can work with booleans and integers. Apart from doing basic arithmetic, we can also use anonymous functions.

Example programs are:

```
1  True
2  False
3  If True Then False Else True
4  If If True Then False Else True Then True Else False
5  42
6  20 + 22
7  1 + 2 + 3
8  (\x : Int . x + 1) 41
```

The expression ( $\x : Int . x + 1$ ) is a lambda expression. This is an anonymous function, taking one argument - named x- of type Int. When applied (e.g. ( $\x : Int . x + 1$ ) 41, the expression right of the . is returned, with the variable x substituted by the argument, becoming 41 + 1.

#### 3.1 Setting up a language

A language is declared inside a .language file 1. Create STFL.language, and put a title in it:

```
1 STFL
3 ******
4 5 # A Simply Typed Functional Language
```

You can put comments wherever you want after a #, e.g. to give some explanation about the language

#### 3.2 Declaring the syntax

For a full reference on syntax, see the reference manual on syntax.

#### 3.2.1 Simple booleans

A program is nothing more then a string of a specific form. To describe strings of an arbitrary structure, BNF<sup>2</sup> can be used.

The syntax of our programming language is defined in the **Syntax**section of *STFL.language*:

<sup>&</sup>lt;sup>1</sup>Actually, the extension doesn't matter at all.

<sup>&</sup>lt;sup>2</sup>Backus-Naur-form, as introduced by John Backus in the ALGOL60-report.

```
1 STFL
3 ******
4 
5 # A Simply Typed Functional Language
6 
7 Syntax
8 =======
```

What do we write here? Let's start with declaring the boolean values True and False. We express how these can be parsed by writing bool ::= "True" | "False". This tells the tool that a syntactic form named bool exists and it is either True of False. Note the double quotes, these are important to indicate that we want this string literally. The | epxresses that it can choose between those forms.

STFL.language now looks like:

```
STFL

******

# A Simply Typed Functional Language

Syntax

=======

bool ::= "True" | "False"
```

Lets try running this! Create examples.stfl, which contains:

```
1 True 2 False
```

We can parse these by running (in your terminal) ./ALGT STFL.language examples.stfl bool -1. The first argument is the language file, the second the examples, the bool tells ALGT what syntactic rule to parse. The -1 flag expresses that each line should be treated individually.

If all went well, you should get the following output:

```
# "True" was parsed as:
True bool.0
# "False" was parsed as:
False bool.1
```

The most interesting part here is that True has been parsed with bool.0, thus the first choice of the bool-form, while False has been parsed with the second form.

#### 3.2.2 If-statements

Now, let's add expressions of the form If True Then False Else True. We define a new syntactic form: expr ::= "If" bool "Then" bool "Else" bool. This tell ALGT that an expression starts with a literal If, is followed by a bool (so either True or False), is followed by a literal Then, ... The tool uses the double quotes " to distinguish between a literal string and another syntactic form.

STFL.language now looks like:

```
1
2
     STFL
3
4
   # A Simply Typed Functional Language
5
6
7
     Syntax
8
9
10
            ::= "True" | "False"
            ::= "If" bool "Then" bool "Else" bool
11
```

This captures already some example expressions. Let's add If True Then False Else True to examples.stfl:

<sup>&</sup>lt;sup>3</sup>Don't worry about spaces and tabs, we deal with them. If you want need to parse stuff like "duizendeneen" or whitespace sensitive languages, please refer to the reference manual

```
1 | True
2 | False
3 | If True Then False Else True
```

Let's run our tool, this time with ./ALGT STFL.language examples.stfl  ${\bf expr}$  -1

Oops! Seems like our parser now always wants to see a If in the beginning, and can't handle True anymore. Perhaps we should tell that a bool is a valid expression to:

Lets see what this gives:

```
+ If expr.0

| True bool.0

| Then expr.0

| False bool.1

| Else expr.0

| True bool.0
```

Looks a lot better! The third example shows clearly how the expression falls apart in smaller pieces. What with a nested If?

If If True Then False Else True Then True Else False clearly can't be parsed, as the condition should be a bool, according to our current syntax.

Well, we can just write expr instead of bool in our syntax:

```
1 expr ::= "If" expr "Then" expr "Else" expr
2 | bool
```

Running this gives

```
If True Then False Else True Then True Else False" was parsed as:
             expr.0
             expr.0
   Τf
   True
             bool.0
   Then
             expr.0
             bool.1
   False
   Else
             expr.0
             bool.0
   True
Then
             expr.0
             bool.0
True
Else
             expr.0
False
             bool.1
```

This clearly shows how the parse trees are nested. This can be rendered too:<sup>4</sup>

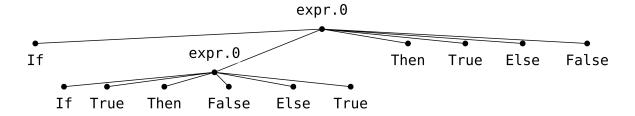


Figure 3.1: ParseTree of a nested condition<sup>5</sup>

<sup>&</sup>lt;sup>4</sup>These images can be created with ALGT STLF.language examples.stfl -l --ptsvg Outputname

<sup>&</sup>lt;sup>5</sup>These images can be created with ALGT STLF.language examples.stfl -l --ptsvg Outputname

#### 3.2.3 Adding numbers, subtyping and forbidden left recursion

Time to spice things up with numbers. To make things easier, integers are built in as Number. It's good practice to introduce a new syntactic rule for them:

```
1 | int ::= Number
```

As an int is a valid expression, we add it to the expr form:

```
1 | expr ::= "If" expr "Then" expr "Else" expr 2 | bool 3 | int
```

Note that every int now also is an expr, just as every bool is an expr. This typing relationship can be visualized with ALGT STFL.language -lsvg Subtyping.svg $^6$ :

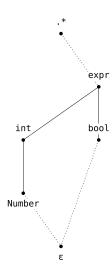


Figure 3.2: Subtyping relation of STFL.language

Now that numbers have been added, let's run this with a number as example:

1 42

should give

```
# "42" was parsed as:
42 Number.0
```

So far, so good! Time to add addition:

```
1 | expr ::= "If" expr "Then" expr "Else" expr 2 | bool 3 | int
```

expr "+" expr

We add some example:

```
1 | 20 + 22
2 | 1 + 2 + 3
```

And run it:

```
Error:
While checking file STFLrec.language:
While checking the syntax:
Potential infinite left recursion detected in the syntax.
Left cycles are:
expr -> expr
```

<sup>&</sup>lt;sup>6</sup>Creating this svg might take a long time for complicated syntaxes, as ALGT calculates the ordering of labels resulting in the least intersecting lines.

Oops! Looks like we did something wrong. What is this left recursion? Whenever the parser wants to parse an expression, it tries every choice from left to right. This means that whenever it tries to parse expr, it should first try to parse expr. That's not really helpfull, so the parser might get in an infinite loop then.

Not allowing left recursion also means that no loops in the subtypings occur. In other words, the subtyping relationship is a lattice.

The solution to this problem is splitting expr in two parts: a term with simple elements in front, and expr with advanced forms:

Let's retry this:

```
Error:

While checking file STFLWrongOrder.language:

While checking the syntax:

While checking for dead choices in expr:

The choice 'term "+" expr' will never be parsed.

The previous choice 'term' will already consume a part of it.

Swap them and you'll be fine.
```

What went wrong this time? The parser tries choice after choice. When parsing 20 + 22 against expr ::= term | term "+" term, it'll first try term (and not term "+" term). It successfully parses 20 against the lonely term, thus the input string + 22 is left. The parser doesn't know what to do with this leftover part, so we get an error.

To fix this, we change the order:

```
1 | expr ::= term "+" expr
2 | term
```

When we try again, we get:

#### 3.2.4 Lambda expressions

The lambda expression is the last syntactic form we'd like to add. Recall that these look like (x : Int . x + 1).

#### Variables

The first thing we should deal with, are variables. A builtin is provided for those, namely Identifiers, matching all words starting with a lowercase (matching [a-z][a-zA-ZO-9]\*). Let's introduce them in our syntax:

```
1 | var ::= Identifier
```

A var is valid in expressions too, e.g. in the expression x + 1, so we want to add it to our term:

```
1 | term | ::= "If" expr "Then" expr "Else" expr | bool | int | var
```

# expr.0

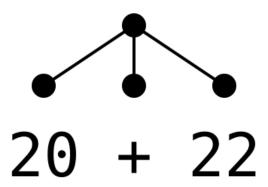


Figure 3.3: Parsetree of 20+22

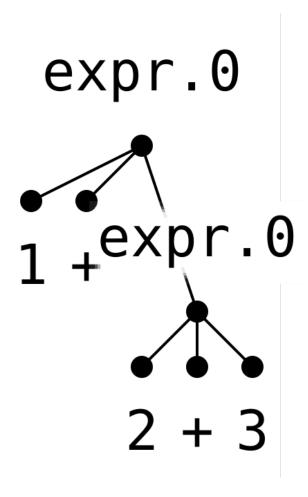


Figure 3.4: Parsetree of 1 + 2 + 3

#### Types

The second ingredient we still need, are types, to annotated the input types. Valid types, for starters, are Bool and Int.

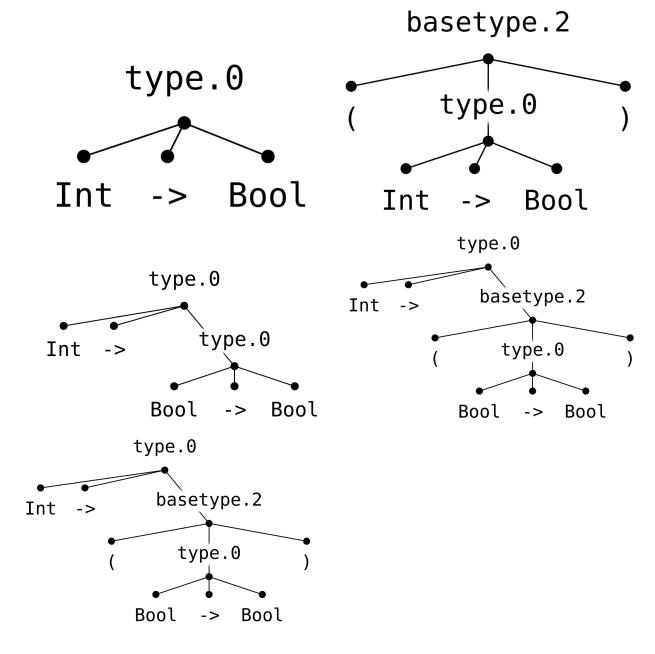
But what is the type of  $(\x : Int . x + 1)$ ? It's something that takes an Int and gives back an Int. We type this as Int -> Int.

And what is the type of a function, taking another function as an argument? That would be, for example, (Int -> Int) -> Int, meaning we need to add a form with parentheses.

Recalling the trouble we had with left recursion and ordering, we write type as following:

```
basetype::= "Bool" | "Int" | "(" type ")"
type ::= basetype "->" type | basetype
```

Some examples of types are:



#### 3.2.5 Lambda expressions

Now we have what we need to define lambda expressions. As they act as a term, we add it there:

Backslash is the escape character, so use two of them to represent a single backslash. We can also apply arguments to a lambda expression. We expand expr:

```
1 | expr ::= term "+" expr
2 | term expr
3 | term
```

#### 3.2.6 What about nonsensical input?

With the current syntax, expresions as If 5 Then True else False, True + 5, True 5 or (x : Int : x + 1) True can be written. We allow these forms to be parsed, as the next stage of the compiler (the typechecker) will catch these errors. How to construct this, will be explained in a following section.

#### 3.2.7 Recap

Our STFL.language contains

```
2
    STFL
3
4
    # A Simply Typed Functional Language
5
6
7
    Syntax
8
9
10
    basetype::= "Bool" | "Int" | "(" type ")"
            ::= basetype "->" type | basetype
11
12
            ::= "True" | "False"
   bool
13
14
    int
            ::= Number
15
    var
            ::= Identifier
16
17
    expr
            ::= term "+" expr
            | term expr
18
19
            | term
20
21
22
            ::= "If" expr "Then" expr "Else" expr
23
            | "(" "\\" var ":" type "." expr ")"
            | bool
24
25
            | int
            | var
```

Our examples.stfl contains

```
True
False
If True Then False Else True
If If True Then False Else True Then True Else False
20 + 22
11 + 2 + 3
(\x : Int . x + 1) 41
```

We run this with

- ALGT STFL.language examples.stfl expr -1 to show the parsetrees
- ALGT STFL.language examples.stfl expr -1 --ptsvg SVGnames to render the parsetrees as SVG
- ALGT STFL.language --lsvg SVGname.svg to visualize the subtyping relationship.

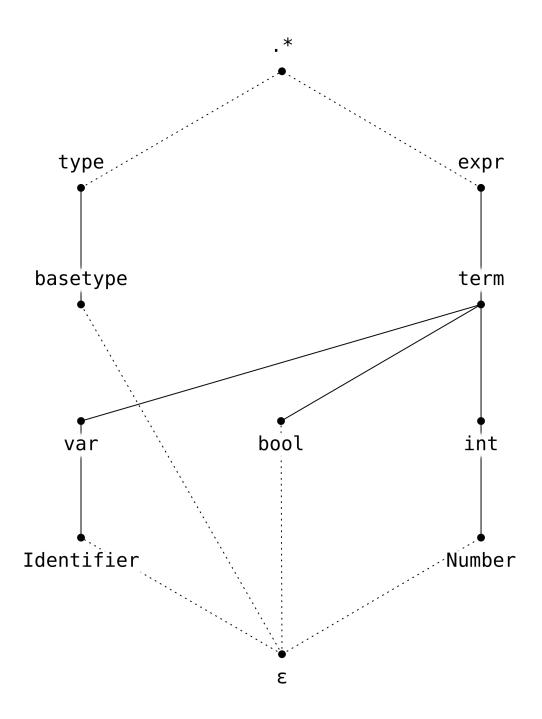


Figure 3.5: The final subtyping relationship of STFL. language  $\,$ 

#### 3.3 Functions

For a full reference on syntax, see the reference manual on functions.

#### 3.3.1 Domain and codomain

It'll come in handy later on to be able to calculate the *domain* and *codomain* of a function type. The *domain* of a function is the type it can handle as input. The *codomain* of a function is the type it gives as output.

Table 3.1: Examples of domain and codomain

Function type	dom	$\operatorname{cod}$
Int -> Bool	Int	Bool
(Int -> Bool)	Int	Bool
<pre>Int -&gt; Bool -&gt; Bool</pre>	Int	Bool -> Bool
<pre>Int -&gt; (Bool -&gt; Bool)</pre>	Int	Bool -> Bool
(Int -> Bool) -> Bool	<pre>Int -&gt; Bool</pre>	Bool -> Bool
Int	Undefined	Undefined
Bool	Undefined	Undefined

Now, let's define these functions!

#### 3.3.2 The function section

We add a new header to STFL.language:

```
1 Functions 2 ========
```

In this function section, we can define the function *dom* in the following way:

```
1 | domain : type -> type 2 | domain(T1 "->" T2) = T1
```

So, what is going on here? Let's first take a look to the first line:

```
1 \mid \mathtt{domain} : type -> type
```

The domain is the name of the function. The type -> type indicates what syntactic form is taken as input (a type) before the -> and what is given as output (again a type).



Figure 3.6: Relevant XKCD (by Randall Munroe, #917)

#### 3.3.3 Pattern matching

Let's have look at the body of the function:

```
1 | domain(T1 "->" T2) = T1
```

What happens if we throw in Int -> Bool? Remember that this is parsed as a tree, with three leafs. Notice that there are three elements in the pattern match to: a variable T1, a literal -> and a variable T2. These leafs are matched respectively:

The same principle applies with more advanced inputs:

We thus always bind T1 to the part before the top-level ->, in other words: we always bind the input type (or domain type) to T1. As that is exactly what we need, we return it!

#### 3.3.4 Missing cases

This already gives us the most important part. However, what should we do if the first argument type is a function? e.g. (Int -> Bool) -> Bool:

This will match the pattern T1 "->" T2 as following:

We see that  $\tau_1$  includes the ( and ), which we don't want. We simply solve this by adding a extra clause:

# type.0

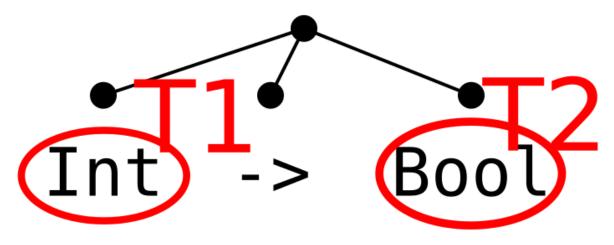


Figure 3.7: Pattern matching in action

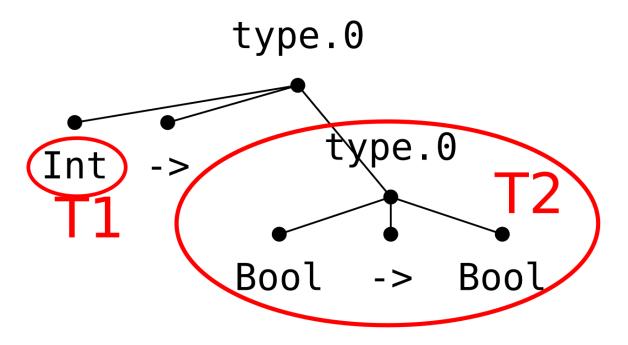


Figure 3.8: Pattern matching in action (more advanced)

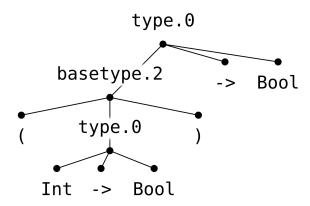


Figure 3.9: Typetree of function argument

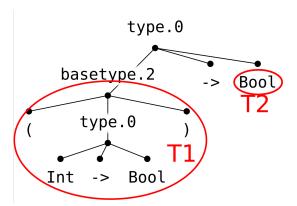


Figure 3.10: Typetree of function argument, matched

We expect that the part *before* the arrow now is surrounded by parens. Note that we put parens once without double quotes and once with. These parens capture this part of the parsetree and match it against the patterns inside the parens, as visible in the green ellipse:

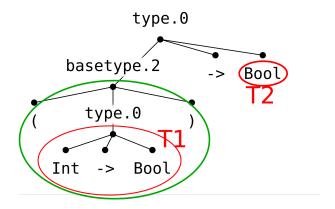


Figure 3.11: Recursive pattern matching

#### 3.3.5 Recursion

There is a last missing case, namely if the entire type is wrapped in parens.

We match a type between parens, and then calculate its domain simply by calling the domain function again.

#### 3.3.6 Clause determination

As you can see, there are two clauses now. How do we now what clause is executed?

Simply put, when the function is evaluated, the arguments are pattern matched against the first clause. If this pattern match succeeds, the expression on the right hand side is returned. Do the arguments not match the patterns? Then the next clause is considered.

In other words, clauses are tried from top to bottom and tested. The first clause of which the patterns match, is executed.

When no clauses match, an error message is given.

#### 3.3.7 Executing functions

Let's put this to a test. We can calculate the domain of our examples.

Create a file typeExamples.stfl, with contents

 $\operatorname{Run}$  this with ALGT STFL.language type Examples.stfl type -1 -f domain:

```
While checking file STFL.language:
  Warning:
    While checking the totality of function "domain":
      Following calls will fall through:
        domain("Bool")
        domain("Int")
# "Int -> Bool" applied to domain
# "(Int -> Bool)" applied to domain
# "Int -> Bool -> Bool" applied to domain
Int
# "Int -> (Bool -> Bool)" applied to domain
Int
# "(Int -> Bool) -> Bool" applied to domain
Int -> Bool
# "Int" applied to domain
Not a single clause of domain matched:
  While pattern matching clause 0:
       In Pattern matching clause 0 with arguments: (Int)
       In domain(Int)
      FT: Could not pattern match '"Int", over '"(" T ")",
  While pattern matching clause 1:
       In Pattern matching clause 1 with arguments: (Int)
       In domain(Int)
      FT: Could not pattern match '"Int", over '("(" T1 ")") "->" T2'
  While pattern matching clause 2:
       In Pattern matching clause 2 with arguments: (Int)
       In domain(Int)
      FT: Could not pattern match '"Int"' over 'T1 "->" T2'
# "Bool" applied to domain
Not a single clause of domain matched:
  While pattern matching clause 0:
       In Pattern matching clause 0 with arguments: (Bool)
       In domain(Bool)
      FT: Could not pattern match '"Bool"' over '"(" T ")"'
  While pattern matching clause 1:
       In Pattern matching clause 1 with arguments: (Bool)
       In domain(Bool)
      FT: Could not pattern match '"Bool"' over '("(" T1 ")") "->" T2'
  While pattern matching clause 2:
       In Pattern matching clause 2 with arguments: (Bool)
       In domain(Bool)
      FT: Could not pattern match '"Bool"' over 'T1 "->" T2'
```

What does this output tell?

For starters, we get a warning that we forgot two cases, namely Bool and Int. For some functions this is a problem, but domain is not defined for those values. Note that a bunch of other tests are builtin as well.

Then, we see an overview for each function what result it gives (or an error message if the pattern matches failed).

<sup>&</sup>lt;sup>7</sup>We'll silently ignore these warnings for the rest of the tutorial with flag --no-checks

If you want more information about the behaviour of a function, specify --ia or --ifa Function-to-analyze to get a clause-per-clause overview:

```
Analysis of domain : type -> type
_____
    Analysis of clause 0
   Clause:
     domain("(" T ")") = domain(T)
   Possible inputs at this point:
   # (type)
   Possible results:
      ("(" type(0/1/2:1) ")"): basetype/2 --> type( (Function call - ID not retrieva
    Analysis of clause 1
   Clause:
     domain(("(" T1 ")") "->" T2)
   Possible inputs at this point:
   # ("Bool")
      ("Int")
      ((basetype "->" type))
   Possible results:
   1 (("(" type(0/0:0/2:1) ")"): basetype/2 "->" type(0/0:2)): type/0
                                                                               --> type((
    Analysis of clause 2
   Clause:
     domain(T1 "->" T2) = T1
   Possible inputs at this point:
   # ("Bool")
   # ("Int")
# (("Bool" "->" type))
# (("Int" "->" type))
   Possible results:
     ("Bool" "->" type(0/0:2)): type/0 --> "Bool" : "basetype" ("Int" "->" type(0/0:2)): type/0 --> "Int" : "basetype"
  Falthrough
```

```
("Bool")
("Int")
```

#### 3.3.8 Codomain

codomain can be implemented totally analogously:

#### 3.4 Relations and Rules: building the evaluator

While we could build an function which evaluates our programming languages, language designers love natural deduction more. Don't worry if you never heard about that before, we'll explain it right away!

#### 3.4.1 Declaring relation "evaluation"

First, we declare a new section inside our STFL.language, with a relation declaration inside:

```
1 Relations

2 ===========

3 (→) : expr (in), expr (out) Pronounced as "small step"
```

Let us break this line down.

The first part,  $(\rightarrow)$ , says that we declare a relation with name  $\rightarrow$ . Except from some builtin symbols, you can use whatever string you want, including unicode<sup>8</sup>. If you don't want to use the unicode-arrow for this tutorial, you can replace  $\rightarrow$  by ->.

The second part, : expr (in), expr (out) states that this is a relation between two expr. As example, 2 + 3, 5 will be in ( $\rightarrow$ ) or written more conventionally  $2 + 3 \rightarrow 5$ .

What about the (in) and (out) parts? These are to help the computer. Given 2 + 3, it's pretty easy for the computer to calculate 5. Given 5, the computer can't magically deduce that this was computed by calculating 2 + 3, especially because an infinite amount of possible calculations might lead to the result 5. We call this the *mode* of the argument.

The last part, Pronounced as "evaluation" defines a name for the relation. It's just an extra, to help users of your language to know what a relation is supposed to do or to help them searching it on a search engine.

Note that the goal of  $\rightarrow$  is to make a small, fundamental step - just one addition or simplification, e.g.  $1 + 2 + 3 \rightarrow 1 + 5$ . We'll design another relation later on which will give us the end result immediatly, giving us 6.

#### 3.4.2 Defining relation "evaluation"

#### Simple deduction rules: If

Defining relations works with one or more rules.

We start with a simple one:

How should you read this rule? The part under the line says that this is part of the relation; in other words; "If" "True" "Then" e1 "Else" e2 will evaluate to e1. This is equivalent to writing the function eval("If" "True" "Then" e1 "Else" e2) = e1.

<sup>&</sup>lt;sup>8</sup>to enter an unicode character on a linux machine, type Left-Ctrl + Shift + U, release, and type the hexcode of the desired character, e.g. 2192 to get the right-arrow. On windows, hold down Alt and type + 2192.

The part on the right of the line [EvalIfTrue] gives the name of the rule. You can put there pretty much everything you want.

Analogously, you can add a rule for If False:

This is already enough to run our third example. To run a relation, specify -r <name-of-relation>, thus ./ALGT STFL.language examples.stfl expr -l -r  $\rightarrow$ :

```
# If True Then False Else True applied to →
# Proof weight: 1, proof depth: 1

------ [EvalIfTrue]
If True Then False Else True → False
```

#### Deduction rules with predicates: plus

How do we add numbers? We can add a deduction rule just as well for this:

First, take a look at the bottom line. The left part is straightforward; we match a parsetree with form n1 + n2. But what is this !plus(n1, n2). It's a function call with arguments n1 and n2. The exclamation mark ! indicates that this is a builtin function.

In other words, this rule indicates that 1 + 2 should be evaluated with !plus(1,2), giving three.

There is a catch, though. !plus has type Number -> Number (recall, this means that plus takes two Numbers and gives us a Number in return). We can't pass in other types, or it would fail. We thus have to check that we get correct input for this rule. To do this, we have those predicates on top: n1:Number (read this as n1 is of syntactic form Number) and n2:Number.

Let give this a run!

We can see that our simple example, 20 + 22 neatly gives us the answer<sup>9</sup>. The other example, 1 + 2 + 3 however, fails. Note that it gives a detailed overview of what rules it attempted to apply and why those rules failed.

<sup>&</sup>lt;sup>9</sup>Luckily, your computer didn't have to run for 10 million years. And it conveniently gave the question too, so that we wouldn't forget it.

#### If with complicated conditions

But what with our fourth example, If If True Then False Else True Then True Else False? The condition itself as an If-expression as well.

Herefore we introduce a more complicated rule:

The part above the line should be read as a condition. It states that, whenever condo evaluates to cond1, then we can evaluate the bigger expression.

#### Evaluation contexts for congruence rules

However, there is a way to write this even shorter:

The part expr[expr0] will search, within the expression we want to evaluate, a nested expression that satisfies the conditions. In other words, it will search in the parsetree (If (If True Then False Else False) Then True Else False a part that can be evaluated (e.g. If True Then False Else False).

The evaluated expression will then be put back in the original, bigger parsetree at the same location. Make sure to name the nested expr expro, thus syntactic-form-name followed by a number. That's how the tool figures out what kind of parsetree to search for.

As a bonus, it'll also solve our 1 + 2 + 3!

These proofs are getting a bit harder to read, but always start from the bottom if you get lost.

It basically states that 1 + (2 + 3) makes a step to 1 + 5, because of rule EvalCtx; this rule could be used because 2 + 3 evaluates to 5.

The proof for that part of the relation is given more on top, by rule EvalPlus, which could be invoked because both 2 and 3 are Numbers.

#### Application

As last, we'd like to apply functions, such as ( $\x : Int . x + 1$ ) 41.

Our intution is that, given something as ( $\x$ : someType . someExpr) someArg, we want to evaluate this to someExpr, where we replace every x in someExpr. However, a builtin function does exactly that: !subs. This gives us the following rule:

#### 3.4.3 Evaluation-relation: recap

Our evaluation rule is defined as:

```
2
    Relations
3
4
    (
ightarrow : expr (in), expr (out) Pronounced as "small step"
5
6
7
8
    Rules
9
10
11
12
    \mathtt{expr0} \to \mathtt{expr1}
                                              [EvalCtx]
13
14
     expr[expr0] → expr[expr1]
15
16
17
                            n2:Number
18
    n1:Number
            -----[EvalPlus]
19
20
    n1 "+" n2 \rightarrow !plus(n1, n2)
21
22
23
24
25
                                                        [EvalIfTrue]
26
     "If" "True" "Then" e1 "Else" e2 
ightarrow e1
27
28
                                                        [EvalIfFalse]
29
     "If" "False" "Then" e1 "Else" e2 
ightarrow e2
30
31
32
33
   ("(" "\\" var ":" type "." e ")") arg 
ightarrow !subs:expr(var, arg, e)
```

#### 3.4.4 Is canonical

It is usefull to known when an expression is *canonical*, thus is fully evaluated. This can be simply stated by a relation taking just one argument and *giving no output*<sup>10</sup>. It would contain exactly the Numbers, True and False.

First, the declaration in the Relations-section:

 $<sup>^{10}\</sup>mathrm{Mathematicians}$  would call this a set.

#### 3.4.5 Bigstep

Of course, when we input 1 + 2 + 3, we would like te get 6, and not 1 + 5. For this, we can define a second relation,

First, let us declare this:

```
1\mid(	o\!\!*) : expr (in), expr (out) Pronounced as "big step"
```

First, the basecase. If something is canonical, we are done and just return that unchanged. We express this as following:

```
1 (\( \sigma \) e \( ----- \) [BigStepBase] \( e \rightarrow \) e
```

What if we are not done? That means that we can make a single step,  $e0 \rightarrow e1$  and that we calculate this e1 to its canonical from e2 with the relation itself!

So, we finally did it! Time to see our examples in all their glory!

```
# True applied to →*

# Proof weight: 3, proof depth: 3

True : bool
------ [CanonBool]
(✓) True
------ [BigStepBase]

True →* True
```

```
# If True Then False Else True applied to →*

# Proof weight: 5, proof depth: 4

False : bool

(√) False

If True Then False Else True → False False →* False

If True Then False Else True →* False
```

```
# 20 + 22 applied to →*

# Proof weight: 7, proof depth: 4

42 : int
-----
20 : Number 22 : Number (√) 42
-----
20 + 22 → 42 42 →* 42
------
20 + 22 →* 42
```

#### 3.5 Building the typechecker

Now that we have the evaluator and some experience, we can slay the next dragon: the typechecker! For those unfamiliar, the typechecker looks at the expression and determines the type of it and halts on inconsistencies, such as 1 + True or If True Then 0 Else False, ...

we will build a single rule for each syntactic choice of expr; thu a rule for:

- The constants True and False
- The constant Numbers
- Typing plus
- Typing If ... Then ... Else ...
- Typing lambda's ( $\x$  : T . e)
- Typing variables x
- Typing application

#### 3.5.1 The typing environment

Before where start, how should we type a variable, such as x? Of course, this depends on the environment. In the lambda (\\x : Int . x), x should be typed as a Int, while in the lambda (\\x : Bool . x), this x clearly is a Bool.

We could type the inner expressions by substituting a simple default value in the expression, and then typing it. This however, doesn't scale to more advanced languages.

The other, more general solution is keeping track of the type of each variable. We declare a simple list to keep track of the types in the Syntax Section:

```
typing ::= var ":" type
typingEnvironment ::= typing "," typingEnvironment | "{}"
```

The typing represents a data entry, whereas the typingEnvironment can contain zero or more of these data entries, thus keeping track of the variable types.

The typing relation will often be denoted with a uppercase gamma,  $\Gamma$  (U+0393).

#### 3.5.2 The typing relation

We're all set now! What should our typing relation look like? First, we'll want to take a typingRelation as input, together with an expr. This should be enough to calculate the type of the expression.

In other words, the type of the relation is typingRelation (in), expr (in), type (out). In the acadical world, this is often given the symbol  $\vdash$  <sup>11</sup>, pronounced entails or out of this environment follows this typing. So, our declaration becomes:

```
|\cdot| : typingEnvironment (in), expr (in), type (out) Pronounced as "entails typing"
```

#### 3.5.3 Typing constants True and False

It's pretty easy to type constants, such as 42 and True.

Let us start with typing the constant True.

If this look a bit magical: we take the typing environment as input, left of the ⊢, pattern match on a literl True and return the known type Bool.

We can do the same for False:

#### 3.5.4 Typing constant Numbers

Our next challenge is giving a type to Ints. Make a single rule for each number is a bit hard, given that there are infinite many of them...

However, we can simply fix this by adding a predicate, checking that our input is a number:

```
1 n:int
2 ----- [Tnumber]
3 Γ ⊢ n, "Int"
```

Remember that our predicates are written above the line.

#### 3.5.5 Typing against an empty environment

Let's try to run our typing relation, with ./ALGT STFL.language expr -l -r -

```
# Could not apply relation \vdash to the input "True", because: While trying to proof that (\vdash) is applicable to "True": Expected 2 arguments to relation \vdash, but only got 1
```

Well, that didn't work. The tool expects two arguments; but only one is provided...

To solve this, we declare yet another relation, in which we type an expression against an empty environment:

<sup>11</sup> Type Ctrl+Shift+U 22a2 on linux to input this character. On Windows, hold down Alt and type + 22a2.

```
1 n:int
2 ----- [Tnumber]
3 Γ ⊢ n, "Int"
```

Retrying with the new relation (./ALGT STFL.language True False If True Then False Else True If If True Then False Else gives us:

#### 3.5.6 Typing plus

Another expression we'll want to type are additions.

Of course, this will always return an Int, but there is more. True + False is not valid, whereas 1 + 1 can be typed. In other words, we have to check that the arguments to + are both numbers.

We could thus type plus as following:

This works for 1 + 2, but not for 1 + (2 + 3), as (2 + 3) is *not* a syntactic form that is a literal Number. It can be typed as Int though, so we can generalize our predicates by using the typing relationship recursively:

Looks good! Time to give this a try:

#### 3.5.7 Typing If

It is pretty straightforward that the condition of our If should be Bool, which already gives a draft of the rule:

We also want to make sure that both e1 and e2 are correctly typed, so we recursively typecheck them:

But what type should we return? The type of e1 or e2?

Consider expression If True Then O Else False. Evaluating this for one step, would yield O. However, expression If False Then O Else False would yield False. In other words, depending on the runtime value of the condition, we might get a different type.

That's not behaviour we want. The types of e1 and e2 should be the same to function correctly. We add a predicate to check this:

Now we can also return a type; as T1 and T2 are the same, we just pick one:

All done! Time to give it a try:

#### 3.5.8 Typing lambda's

Typing lambda's is a bit complicated. Remember that a lambda such as  $(\x : T . e)$  means that, given x of type T as input argument, it gives back expression e with x replaced.

This gives us quite some clues about what to do.

Let's start with the skeleton of the rule:

```
1 | ???
2 |----- [TLambda]
3 | Γ |- "(" "\\" x ":" T1 "." e ")", ???
```

Of course, we'll want to type <code>e</code> jus as well. Not only to check wether it is correct, but also because we'll need it's type later on:

This is close to what we want, but there is a catch though: in the expression e, we know that x has the type T1. We should pass this knowledge to the typing of e, by adding it to the typing environment  $\Gamma$ :

So far, so good! The only question remaining is what type we should return. We know we have input of type T1 and output of type T2. Thats where our -> comes into play: the entire lambda has type T1 -> T2!

There is a little technicality into play here though: T1 might be some complicated type, such as Int -> Bool - meaning we expect a *function* as input argument. If we would write Int -> Bool -> T2, that would be read as funcion taking *two* arguments: first a Int, followed by a Bool. Not quite the same thus.

The fix for this is simple: add parentheses. The type of a lambda is  $(T1) \rightarrow T2$ .

Typing this out as rule yields:

Note that an extra pair of parentheses was added; one pair is between double quotes, denoting that this should be added in the parse tree; the other pair just groups them together to help the tool build the parsetree.

#### 3.5.9 Typing variables

Before we can see typing of lambda's live, we need to take another hurdle: typing variables.

You'll probably think it'll be a lot of work to design the searching behaviour, but luckily, there is a special construction builtin that does exactly that. Remember the evaluation context? We can put this to work here too:

```
1 | 2 | ------ [Tx] | 3 | Γ[x":"T] | -x, T
```

Quite succint! If you're a bit puzzled about it's workins, we stated to ALGT that it should search a typing of x, where x is exactly the name of the variable we want to type.

At this point, we can finally type a single lambda:

#### 3.5.10 Typing application

The typechecker is nearly complete, only a single syntactic form can't be typed yet: application of the form function argument.

How can we tackle this problem? For starters, we'll have to type the function and argument

A function has a determined input argument, also known as the *domain* of the function. To be well typed, the domain should match the type of the argument exactly. But how can we get this argument?

Luckily, we created a function earlier on that calculates exactly that! We can simply use that and check that it's result equals TArg:

Nearly done! Only question left is what type we should return.

This is pretty straighforward too, as we earlier made the function codomain which exactly calculates the return type of TFunc

All finished now, except for trying of course:

#### 3.6 Evaluator and typechecker: recap

Our declared relations are:

```
1
                          Relations
     2
     3
                                                                             : expr (in), expr (out)

: expr (in), expr (out)

Pronounced as "big step"

Pronounced as "is capanical as "
    4
                         (\rightarrow)
     5
                          (→*)
                                                                                : expr (in)
                                                                                                                                                                                                                                                                                                         Pronounced as "is canonical"
    6
    7
                                                                             : typingEnvironment (in), expr (in), type (out) Pronounced as "entails typing"
    9
10
                         (::)
                                                                              : expr (in), type (out) Pronounced as "type in empty context"
11
                                                                             : type (in), type (in) Pronounced as "equals"
12
```

The definition of those relations are:

```
12
           er n2:Number
----- [EvalPlus]
n2 \rightarrow !plus(n1, n2)
13
   n1:Number
14
   n1 "+" n2 \rightarrow !plus(n1, n2)
15
16
17
18
19
                                             [EvalIfTrue]
20
    "If" "True" "Then" e1 "Else" e2 
ightarrow e1
21
22
23
   -----
                                             [EvalIfFalse]
24
25
    "If" "False" "Then" e1 "Else" e2 
ightarrow e2
26
27
28
     -----[EvalLamApp]
    ("(" "\\" var ":" type "." e ")") arg \rightarrow !subs:expr(var, arg, e)
29
30
31
32
33
34
   (i:int)
35
                          [CanonInt]
36
    (√) i
37
38
39
   (b:bool)
                      [CanonBool]
40
41
    (√) b
42
43
44
45
46
   (√) e
                        [BigStepBase]
47
48
49
   50
                              [BigStepRec]
51
52
   e0 →* e2
53
54
55
56
57
   58
59
    e :: T
60
61
62
63
64
   \Gamma \vdash "True", "Bool"
65
66
67
68
                       [TboolFalse]
69
   \Gamma \vdash "False", "Bool"
70
71
72
73
   n:int
                       [Tnumber]
74
   \Gamma \vdash \mathtt{n}, "Int"
75
76
77
78
79
80
```

```
82
83
 84
      -----
                            [Tx]
     \Gamma[ x ":" T ] \vdash x, T
85
86
87
     \Gamma \vdash \mathtt{n1} , "Int" \Gamma \vdash \mathtt{n2} , "Int"
88
 89
                                                              [TPlus]
     \Gamma \vdash n1 "+" n2, "Int"
90
91
92
     \Gamma \vdash \mathtt{c}, "Bool" \Gamma \vdash \mathtt{e1}, Tl \Gamma \vdash \mathtt{e2}, Tr Tl == Tr
93
                                        ----- [TIf]
94
95
     \Gamma \vdash "If" c "Then" e1 "Else" e2, Tl
96
97
98
     (x ":" T1) "," \Gamma \vdash e, T2
99
100
                                 ----- [TLambda]
101
     \Gamma \vdash "(" "\\" x ":" T1 "." e ")", ( "(" T1 ")") "->" T2
102
103
104
    \Gamma \vdash e1, Tfunc \Gamma \vdash e2, Targ Targ == domain(Tfunc)
105
                                              -----[Tapp]
106
     \Gamma \vdash e1 e2, codomain(Tfunc)
107
108
109
110
111
112
113
114
     T1 = T2 : type
     ----- [EqBase]
115
116
     T1 == T2
117
118
    T1 == T2
119
      ----- [EqParL]
120
     "(" T1 ")" == T2
121
122
     T1 == T2
123
     ----- [EqParR]
124
     T1 == "(" T2 ")"
125
126
127
    Ta1 == Ta2
                   Tb1 == Tb2
128
               -----[EqArrow]
129 | -----
130 Ta1 "->" Tb1 == Ta2 "->" Tb2
```

Running the relation :: on all our examples with flags ./ALGT STFL.language True False If True Then False Else True If If gives:

```
{} ⊢ False, Bool
False :: Bool
# If True Then False Else True applied to ::
# Proof weight: 7, proof depth: 4
                                                         T1 = Bool = T2
{} ⊢ True, Bool {} ⊢ False, Bool {} ⊢ True, Bool Bool == Bool
\{\} \vdash If True Then False Else True, Bool
If True Then False Else True :: Bool
# 42 applied to ::
# Proof weight: 3, proof depth: 3
42 : int
\{\} \vdash 42, Int
42 :: Int
# 20 + 22 applied to ::
# Proof weight: 6, proof depth: 4
20 : int
              22 : int
\{\}\ \vdash\ 20\ , Int \{\}\ \vdash\ 22\ , Int
{} ⊢ 20 + 22, Int
                -----
20 + 22 :: Int
# 1 + 2 + 3 applied to ::
# Proof weight: 9, proof depth: 5
               2 : int 3 : int
1 : int {} + 2, Int {} + 3, Int
{} ⊢ 1, Int {} ⊢ 2 + 3, Int
\{\} \vdash 1 + 2 + 3, Int
1 + 2 + 3 :: Int
# (\x : Int . x + 1) 41 applied to ::
# Proof weight: 11, proof depth: 6
```

```
1 : int

x : Int , {} \( \) x : Int x : Int x : Int , {} \( \) 1, Int

x : Int , {} \( \) x + 1, Int

41 : int

T1 = Int = T2

{} \( \) ( \) x : Int . x + 1 ) 41, Int

( \) x : Int . x + 1 ) 41 :: Int
```

#### 3.7 Properties

The last fundamental part of our language are it's properties.

Arbitrary properties can be stated just as rules can.

ALGT will check that these properties hold, by trying a bunch of random examples, effectively quickchecking your language implementation.

Most languages are concerned about two important properties: preservation and progress.

#### 3.7.1 Stating Preservation

Preservation is the property that, when an expression e0 of type T is evaluated, the new expression e1 is still of type T. Without this property, our typechecker would be useless...

Now, we can state this property in the Properties-section of the file:

This is the same as a rule in a relation: given the predicates (e0 :: T and e0  $\rightarrow$ e1), the consequent (e1 :: T) can always be proven.

As our implementation is correct, we can just run our program as following, and see it did try to proof us wrong:

```
Done quickchecking property Preservation with 8 examples
# Language file parsed. No action specified, see -h or --manual to specify other options
```

We can ask ALGT to try more examples, with the --quickcheck-runs NUMBER-OF-RUNS flag:

```
Done quickchecking property Preservation with 25 examples # Language file parsed. No action specified, see -h or --manual to specify other options
```

Note that we can also run these properties on our own examples, with --test-property NAME OF PROPERTY --ppp or --test-all-properties --ppp. By default, property proofs are not printed (as they tend to be long), --ppp says to Print the Property Proofs.

```
# (/) e0

True : bool
----- [CanonBool]
(/) True
```

#### 3.7.2 Stating progress

Another important property is *progress*. This states that, if an expression is well-typed, it either is in canonical form (a simple value) or we can evaluate for another step.

This is quite an important check to, as it means we can't have a *stuck* state, in which the evaluation doesn't know how to progress. Turing complete programming language (which **STFL** is *not*) might get stuck in a infinite loop though, but it is because a certain expression would yield exactly the same expression, but with at least some steps in between.

This property can be stated as following:

Here, *choice* is used in the consequent: given the predicates (e0 :: T), at least one of the choices must be proven:

```
Property Preservation holds for given examples
Property successfull
# Property Preservation proven by failing predicate with assignment {e0 --> True}:
  # Success: e0 :: T
  # Failed: e0 \rightarrow e1
  e0 
ightarrow e1 failed because:
  While trying to proof that (\rightarrow) is applicable to "True":
    Not a single rule matched:
    While trying to intepret the rule EvalCtx with True:
      Evaluation contexts only searching within a parse tree and don't handle literals
    While trying to intepret the rule EvalPlus with True:
        FT: Could not pattern match '"True"' over 'n1 "+" n2'
    While trying to intepret the rule EvalIfTrue with True:
        FT: Could not pattern match '"True"' over '"If" "True" "Then" e1 "Else" e2'
    While trying to intepret the rule EvalIfFalse with True:
        FT: Could not pattern match '"True"' over '"If" "False" "Then" e1 "Else" e2'
    While trying to intepret the rule EvalLamApp with True:
        FT: Could not pattern match '"True"' over '("(" "\\" var ":" type "." e ")") arg'
```

Does ALGT find counterexamples for this property?

```
Done quickchecking property Progress with 8 examples
# Language file parsed. No action specified, see -h or --manual to specify other options
```

Phew! No counterexamples found! Our language is probably sound.

#### 3.7.3 Disabling quickchecks and symbolic checks

If the quickchecks take to long, you can disable them, using --quickcheck-runs 0. When the other checks takes to long (such as minimal typing of functions, liveability and totality), add --no-check to disable them all

#### 3.8 Properties

#### 3.9 Recap: used command line arguments

## Reference manual

#### 4.1 General

A language is defined in a .language-file. It starts (optionally) with a title:

Comments start with a # and can appear quasi everywhere.

```
1 2 # This is a comment
```

Syntax, functions, relations, ... are all defined in their own sections:

```
1 | Syntax 3 | =======
```

A section header starts with an upper case, is underlined with = and followed by a blank line.

#### 4.2 Syntax

All syntax is defined in the Syntax section. It consists out of BNF-rules, of the form

```
1 | name ::= "literal" | choice | seq1 seq2
```

Choices might be written on multiple lines, as long as at least one tab precedes them:

```
1 | name ::= choice1 | choice2 | choice3
```

#### 4.2.1 Literals

A string that should be matched exactly, is enclosed in " (double quotes). Some characters can be escaped with a backslash, namely:

Table 4.1: Escape sequences

Sequence	Result
\n	newline
\t	tab
\"	double quote
\\	backslash

#### 4.2.2 Parsing order

Rules are parsed **left to right**, in other words, choices are tried in order. No backtracking happens when a choice is made; the parser is a *recursive descent parser*. This has two drawbacks: left recursion results in an infinite loop and the ordering of choices does matter.

```
# Left recursion, error message.
expr ::= expr "+" int

# 'int' already consumes a part of 'int + int', error message
expr ::= int | int "+" int

# Common part extraction, error message
# Correct
expr ::= int "+" int | int
```

#### 4.2.3 Builtin syntactic forms

Some syntactic forms are already provided for your convenience, namely:

Builtin Meaning Regex Matches an identifier Identifier [a-z][a-zA-Z0-9]\*Number Matches an (negative) integer. Integers parsed by -?[0-9]\* this might be passed into the builtin arithmetic functions. Matches a single character, whatever it is, including Any newline characters Matches a lowercase letter Lower [a-z] Matches an uppercase letter [A-Z]Upper Matches an digit Digit [0-9] Matches a hexadecimal digit [0-9a-fA-F] Hex Matches a double quote delimited string, returns the String "([^"\]|\"|\\)\*" value including the double quotes Matches a double quote delimeted string, returns "([^"\]|\"|\\)\*" StringUnescthe value without the double quotes Matches a single character that is not a newline. LineChar [^\n] This includes: Matches a '(', which will dissapear in the parsetree Par0 ( Matches a ')', which will dissapear in the parsetree ParC )

Table 4.2: Builtin syntax

#### 4.2.4 Subtyping relationship

A syntactic form equals a (possibly infinite) set of strings. By using a syntactic form  $\mathtt{a}$  as choice in other syntactic form  $\mathtt{b}$ ,  $\mathtt{a}$  will be a subset of be, giving the natural result that  $\mathtt{a}$  is a subtype of  $\mathtt{b}$ .

In the following examle, bool and int are both subsets of expr. This can be visualised with the --lsvg Output.svg-flag.

#### 4.2.5 Whitespace in sequences

Whitespace (the characters " ","\t"), is parsed by default (and ignored completely). If you want to parse a whitespace sensitive language, use other symbols to declare the rule:

Table 4.3: Whitespace modes

Operator	Meaning
::=	Totally ignore whitespace
~~=	Parse whitespace for this rule only
//=	Parse whitespace for this rule and all recursively called rules

This gives rise to the following behaviour:

Table 4.4: Whitespace mode examples

Syntax	Matching String	
a ::= "b" "c" x	b с x y	
x ::= "x" "y"	bcxy	
	b\tc\tx\ty	
	b c\txy	
a ~~= "b" "c" x	bcx y	
x ::= "x" "y"	bcxy	
	bcx\ty	
a //= "b" "c" x	bcxy	
x ::= "x" "y"		

#### 4.2.6 Grouping sequences

Sometimes, you'll want to group an entire rule as a token (e.g. comments, an identifier, ...) Add a \$ after the assignment to group it.

```
1 text ::= LineChar line | LineChar
2 commentLine ::= $ "#" text "\n"
3
4 customIdentifier ::= $ Upper Number
```

When such a token is used in a pattern or expression, the contents of this token are parsed against this rule:

```
1 | f : customIdentifier -> statement
2 | f("X10") = "X9" "# Some comment"
```

#### 4.3 Functions

#### 4.3.1 Patterns and expressions

Functions transform their input. A function is declared by first giving its type, followed by one or more clauses:

When an input is given, arguments are pattern matched against the patterns on between parentheses. If the match succeeds, the expression on the right is given. If not, the next clause is given.

Note that using the same variable multiple times is allowed, this will only work if these arguments are the same:

```
1 | f(a, a) = ...
```

Recursion can be used just as well:

```
1 \mid f("a" a) = f(a)
```

This is purely functional, heavily inspired on Haskell.

#### Possible expressions

Expr	Name	As expression
x	Variable	Recalls the parsetree associated with this variable
_	Wildcard	Not defined
42	Number	This number
"Token"	Literal	This string
<pre>func(arg0, arg1,)</pre>	Function call	Evaluate this function
!func:type(arg0,)	Builtin function call	Evaluate this builtin function, let it return a type
(expr or pattern:type)	Ascription	Checks that an expression is of a type. Bit useless
e[expr or pattern]	Evaluation context	Replugs expr at the same place in e. Only works if e was created with an evaluation context
a "b" (nested)	Sequence	Builds the parse tree

#### Possible patterns

Expr	As pattern
x	Captures the argument as the name. If multiple are used in the same pattern, the captured arguments should be the same or the match fails.
_	Captures the argument and ignores it
42	Argument should be exactly this number
"Token"	Argument should be exactly this string
<pre>func(arg0, arg1,)</pre>	Evaluates the function, matches if the argument equals the result. Can only use variables which are declared left of this pattern
!func:type(arg0,)	Evaluates the builtin function, matches if the argument equals the result. Can only use variables which are declared left of this pattern
(expr or pattern:type)	Check that the argument is an element of type
e[expr or pattern]	Matches the parsetree with e, searches a subpart in it matching pattern
a "b" (nested)	Splits the parse tree in the appropriate parts, pattern matches the subparts

#### 4.3.2 Typechecking

#### Equality

```
1 | 2 | Syntax | 3 | ====== 4 | 5 | a | ::= ... | 6 | b | ::= ...
```

When equality checks are used in the pattern matching, the variable will be typed as the smallest common supertype of both types. If such a supertype does not exist, an error message is given.

Note that using a supertype might be a little too loose, but won't normally happen in real-world examples.

In the given example, x will be typed as c, the common super type. In this example, x might also be a d, while this is not possible for the input. This can be solved by splitting of  $a \mid b$  as a new rule.

#### 4.3.3 Totality- and liveabilitychecks

Can be disabled with --no-check, when they take to long.

#### 4.3.4 Higher order functions and currying?

Are not possible for now (v 0.1.25). Perhaps in a future version or when someone really needs it and begs for it.

#### 4.3.5 Builtin functions

name	Descr	Arguments
plus	Gives a sum of all arguments (0 if none given)	Number* -> Number
min	Gives the first argument, minus all the other arguments	Number -> Number* -> Number
mul	Multiplies all the arguments. (1 if none given)	Number* -> Number
div	Gives the first argument, divided by the product of the other arguments. (Integer division, rounded down))	Number -> Number* -> Number
mod	Gives the first argument, module the product of the other arguments.	Number -> Number* -> Number
neg	Gives the negation of the argument	Number -> Number
equal	Checks that all the arguments are equal. Gives 1 if so, 0 if not.	.* -> .* -> Number
error	Stops the function, gives a stack trace. When used in a rule, this won't match a predicate	.** → <i>ε</i>
subs	(expression to replace, to replace with, in this expression) Replaces each occurence of the first expression by the second, in the third argument. You'll want to explictly type this one, by using subs:returnType("x", "41", "x + 1")	.* -> .* -> .*
group	Given a parsetree, flattens the contents of the parsetree to a single string	.* -> StringUnesc

#### 4.4 Relations and Rules

#### 4.5 Properties

#### 4.6 Command line flags

# Used concepts and algorithms

# Dynamization and gradualization

## Thankword

#### Thanks to

- Christophe Scholliers
- Ilion Beyst, for always being up to date, giving ideas, spotting bugs at first sight, implementing Nederlands and his enthousiasm in general
- Isaura Claeys, for proofreading and finding a lot of typos