R09546042_TSA_HW_02

October 10, 2021

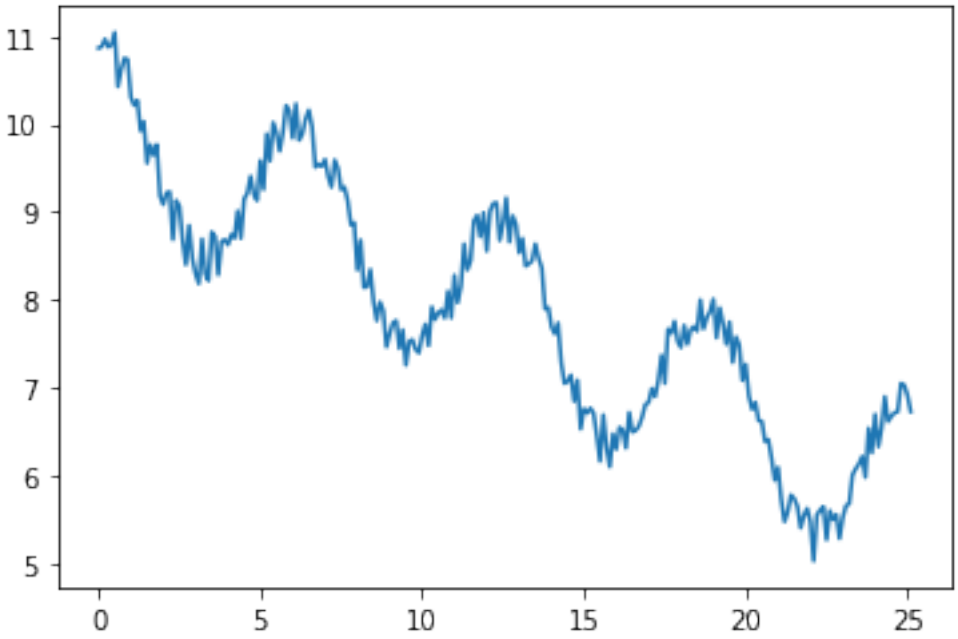
[57]:
```
import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
from sklearn.linear_model import LinearRegression
from statsmodels.tsa.holtwinters import ExponentialSmoothing as HWES
```

1 Q1

1.1 a.

use cos() for waving time-series, -x/6 for dwindling trend, and normal distribution for noise.

[58]:
```
x = np.arange(0,8*np.pi,0.1)   # start,stop,step
y = 10+np.cos(x)-x/6

y_noise = []

for i in y:
    n = 0.3
    noise = np.random.uniform(-n,n)
    y_noise.append(i + noise)

plt.plot(x,y_noise)
plt.show()
```



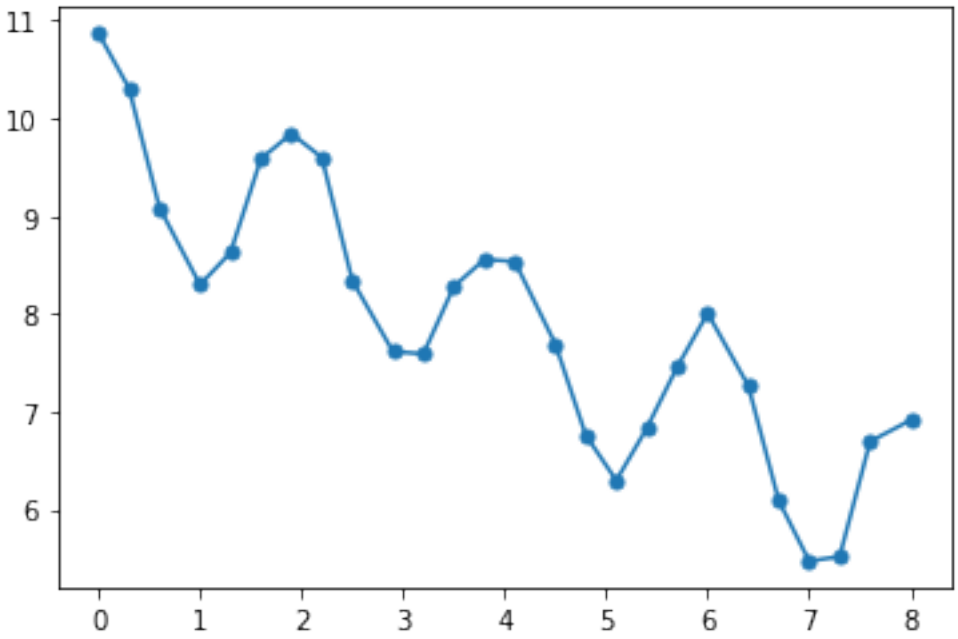
1.2 b

period is 3.14, close to 3.

[59]:
```
df_original_series = pd.DataFrame({
    'period': x,
    'demand': y_noise
})

# include average interger.
df_interger_series = df_original_series[df_original_series['period'] % 1 == 0]
df_interger_series['period'] = df_interger_series['period'].div(np.pi).round(1)
plt.plot(df_interger_series['period'],df_interger_series['demand'],␣
 ↪marker='o',markersize=5)

# deseasonalize
series_deseasonalization = df_interger_series.loc[:, 'demand'].rolling(3).
 ↪mean().dropna()
series_deseasonalization=series_deseasonalization.
 ↪drop([series_deseasonalization.index[22],series_deseasonalization.index[23]])

# deseasonalize dataframe
df_deseasonalization = pd.DataFrame({
    'Quater': sum([[1,2,3]*8,[1,2]],[]),
    'Period': df_interger_series['period'] ,
    'Demand': df_interger_series['demand'] ,
```

```
    'Deseasonalized_Demand': series_deseasonalization
})
```

```
<ipython-input-59-ab869889bd6c>:8: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
  df_interger_series['period'] =
df_interger_series['period'].div(np.pi).round(1)
```



translate x axis to # of pi

1.2.1 c

[60]:
```
#build up regressing model
reg = LinearRegression().fit(np.asarray(df_deseasonalization.loc[20:230,␣
 ↪'Period']).reshape(-1, 1),
                             df_deseasonalization.loc[:,␣
 ↪'Deseasonalized_Demand'].dropna())
#predict nan value
values = pd.Series(reg.predict(np.asarray(df_deseasonalization.loc[:,␣
 ↪'Period']).reshape(-1,1)))

df_deseasonalization.loc[0,['Deseasonalized_Demand']] = values[0]
```

```
df_deseasonalization.loc[10,['Deseasonalized_Demand']] = values[10]
df_deseasonalization.loc[240,['Deseasonalized_Demand']] = values[24]
df_deseasonalization.loc[250,['Deseasonalized_Demand']] = values[25]

# calculate seansonality factor
df_deseasonalization.loc[:, 'Seasonality'] = (df_deseasonalization.loc[:,␣
↪'Demand'] / df_deseasonalization.loc[:, 'Deseasonalized_Demand'])

df_Seasonality_bar= pd.DataFrame({
    'Quater': sum([[1,2,3]*8,[1,2]],[]),
    'Period': df_interger_series['period'] ,
    'Demand': df_interger_series['demand'] ,
    'Deseasonalized_Demand': series_deseasonalization
})

df_seasonality = df_deseasonalization.groupby(['Quater'], as_index=False).mean()
df_seasonality.loc[:, 'Seasonality_bar'] = df_seasonality.loc[:, 'Seasonality']
df_seasonality = df_seasonality[['Quater','Seasonality_bar']]

df_deseasonalization = pd.merge(df_deseasonalization,df_seasonality).
↪sort_values('Period')
```

[61]:
```
df_deseasonalization
```

[61]:

	Quater	Period	Demand	Deseasonalized_Demand	Seasonality	\
0	1	0.0	10.867433	10.022446	1.084310	
9	2	0.3	10.307763	8.407980	1.225950	
18	3	0.6	9.086565	10.087254	0.900797	
1	1	1.0	8.297640	9.230656	0.898922	
10	2	1.3	8.627718	8.670641	0.995050	
19	3	1.6	9.585892	8.837084	1.084735	
2	1	1.9	9.843057	9.352223	1.052483	
11	2	2.2	9.598873	9.675941	0.992035	
20	3	2.5	8.340692	9.260874	0.900638	
3	1	2.9	7.615876	8.518480	0.894042	
12	2	3.2	7.591517	7.849361	0.967151	
21	3	3.5	8.279429	7.828941	1.057541	
4	1	3.8	8.556947	8.142631	1.050882	
13	2	4.1	8.536198	8.457525	1.009302	
22	3	4.5	7.692330	8.261825	0.931069	
5	1	4.8	6.759370	7.662633	0.882121	
14	2	5.1	6.298355	6.916685	0.910603	
23	3	5.4	6.830760	6.629495	1.030359	
6	1	5.7	7.458044	6.862386	1.086800	
15	2	6.0	8.007461	7.432088	1.077417	
24	3	6.4	7.266487	7.577331	0.958977	
7	1	6.7	6.091357	7.121768	0.855315	

```
16        2     7.0   5.474414                6.277419     0.872080
25        3     7.3   5.519303                5.695025     0.969145
8         1     7.6   6.696175                6.188090     1.082107
17        2     8.0   6.914511                5.986282     1.155059
```

```
    Seasonality_bar
0          0.987442
9          1.022739
18         0.979158
1          0.987442
10         1.022739
19         0.979158
2          0.987442
11         1.022739
20         0.979158
3          0.987442
12         1.022739
21         0.979158
4          0.987442
13         1.022739
22         0.979158
5          0.987442
14         1.022739
23         0.979158
6          0.987442
15         1.022739
24         0.979158
7          0.987442
16         1.022739
25         0.979158
8          0.987442
17         1.022739
```

1.2.2 d

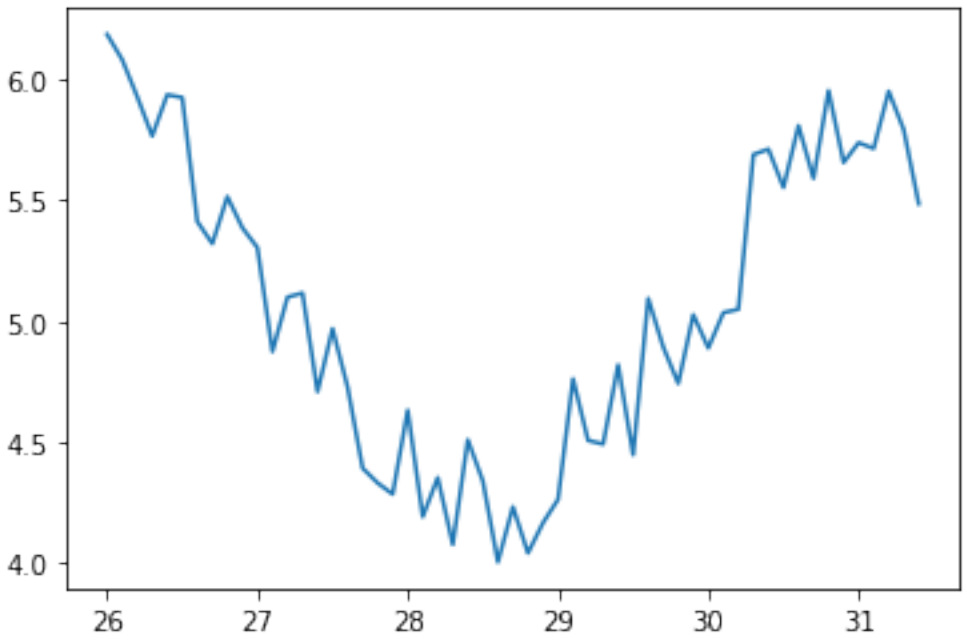
[62]:
```
df_deseasonalization.loc[:, 'Forecast'] =  (reg.predict(np.
 ↪asarray(df_deseasonalization.loc[:, 'Period']).reshape(-1,1)) *␣
 ↪df_deseasonalization.loc[:, 'Seasonality_bar'])
df_deseasonalization.loc[:, 'Error'] =  (df_deseasonalization.loc[:,␣
 ↪'Demand']-df_deseasonalization.loc[:, 'Forecast'])
df_deseasonalization.loc[:, 'Error_Squre'] =  (df_deseasonalization.loc[:,␣
 ↪'Error']*df_deseasonalization.loc[:, 'Error'])
MSE = df_deseasonalization['Error_Squre'].sum()/len(df_deseasonalization)
MAPE = ((abs(df_deseasonalization.loc[:, 'Error']) / abs(df_deseasonalization.
 ↪loc[:, 'Demand'])).sum())*100/len(df_deseasonalization)

print("MSE:",MSE.round(3))
```

```
print("MAPE:",MAPE.round(3))
```

```
MSE: 0.523
MAPE: 8.641
```

1.2.3 e

[63]:
```
x = np.arange(26.0,10*np.pi,0.1)
y = 10+np.cos(x)-x/6

y_noise = []

for i in y:
    n = 0.3
    noise = np.random.uniform(-n,n)
    y_noise.append(i + noise)

plt.plot(x,y_noise)
plt.show()
```



[64]:
```
#true model
df_true_model = pd.DataFrame({
    'Period': x,
    'Demand': y_noise,
    'Forecast':y,
})
```

```
df_true_model.loc[:, 'Error'] =  (df_true_model.loc[:, 'Demand']-df_true_model.
 ↪loc[:, 'Forecast'])
df_true_model.loc[:, 'Error_Squre'] =  (df_true_model.loc[:,␣
 ↪'Error']*df_true_model.loc[:, 'Error'])
MSE = df_true_model['Error_Squre'].sum()/len(df_true_model)
MAPE = ((abs(df_true_model.loc[:, 'Error']) / abs(df_true_model.loc[:,␣
 ↪'Demand'])).sum())*100/len(df_true_model)

print("MSE:",MSE.round(3))
print("MAPE:",MAPE.round(3))
```

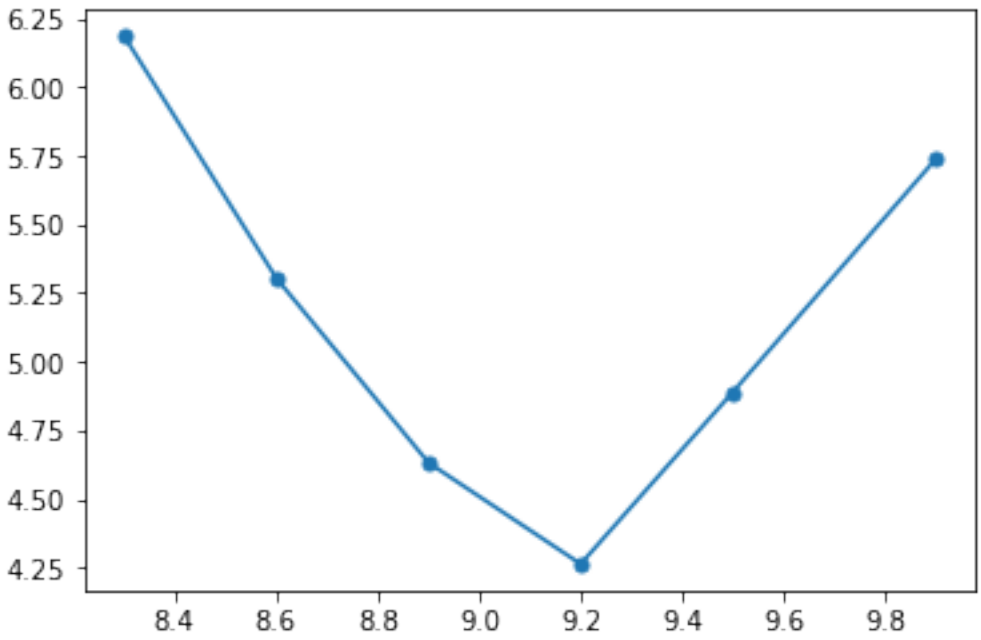
```
MSE: 0.035
MAPE: 3.28
```

[66]:
```
#time-series model
df_time_series_model = pd.DataFrame({
    'Period': x,
    'Demand': y_noise
})


df_interger_series = df_time_series_model[df_time_series_model['Period'].
 ↪round(1) % 1.0 == 0]
df_interger_series['Period'] = df_interger_series['Period'].div(np.pi).round(1)
plt.plot(df_interger_series['Period'],df_interger_series['Demand'],␣
 ↪marker='o',markersize=5)

df_time_series_deseasonalization= pd.DataFrame({   })
df_time_series_deseasonalization = pd.
 ↪merge(df_interger_series,df_deseasonalization, how="outer").
 ↪sort_values('Period')
df_time_series_deseasonalization.loc[:,'Quater']=sum([[1,2,3]*10,[1,2]],[])

df_time_series_deseasonalization=df_time_series_deseasonalization.
 ↪drop(['Seasonality_bar'], axis=1)
df_time_series_deseasonalization = pd.
 ↪merge(df_time_series_deseasonalization,df_seasonality,how = "outer").
 ↪sort_values('Period')

df_time_series_deseasonalization.loc[:, 'Forecast'] =  (reg.predict(np.
 ↪asarray(df_time_series_deseasonalization.loc[:, 'Period']).reshape(-1,1)) *␣
 ↪df_time_series_deseasonalization.loc[:, 'Seasonality_bar'])
df_time_series_deseasonalization.loc[:, 'Error'] = ␣
 ↪(df_time_series_deseasonalization.loc[:,␣
 ↪'Demand']-df_time_series_deseasonalization.loc[:, 'Forecast'])
```

```
df_time_series_deseasonalization.loc[:, 'Error_Squre'] = ␣
 ↪(df_time_series_deseasonalization.loc[:,␣
 ↪'Error']*df_time_series_deseasonalization.loc[:, 'Error'])
MSE = df_time_series_deseasonalization['Error_Squre'].sum()/
 ↪len(df_time_series_deseasonalization)
MAPE = ((abs(df_time_series_deseasonalization.loc[:, 'Error']) /␣
 ↪abs(df_time_series_deseasonalization.loc[:, 'Demand'])).sum())*100/
 ↪len(df_deseasonalization)

print("MSE:",MSE.round(3))
print("MAPE:",MAPE.round(3))
```

```
MSE: 0.513
MAPE: 11.534
```

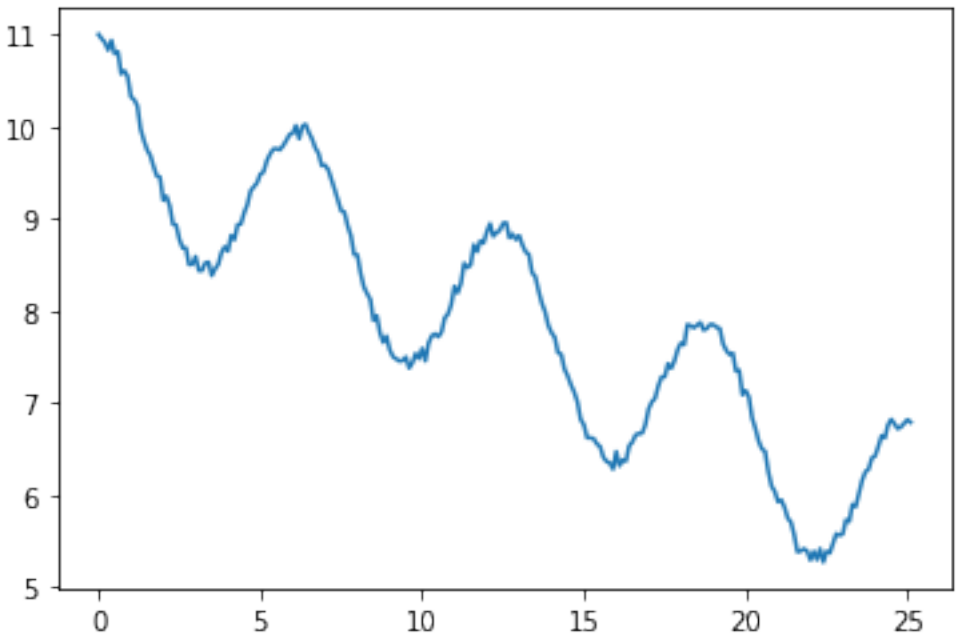
```
<ipython-input-66-45637702f052>:9: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
  df_interger_series['Period'] =
df_interger_series['Period'].div(np.pi).round(1)
```



1.2.4 f

change noise factor to 0.1 only, 3 time less than previous data

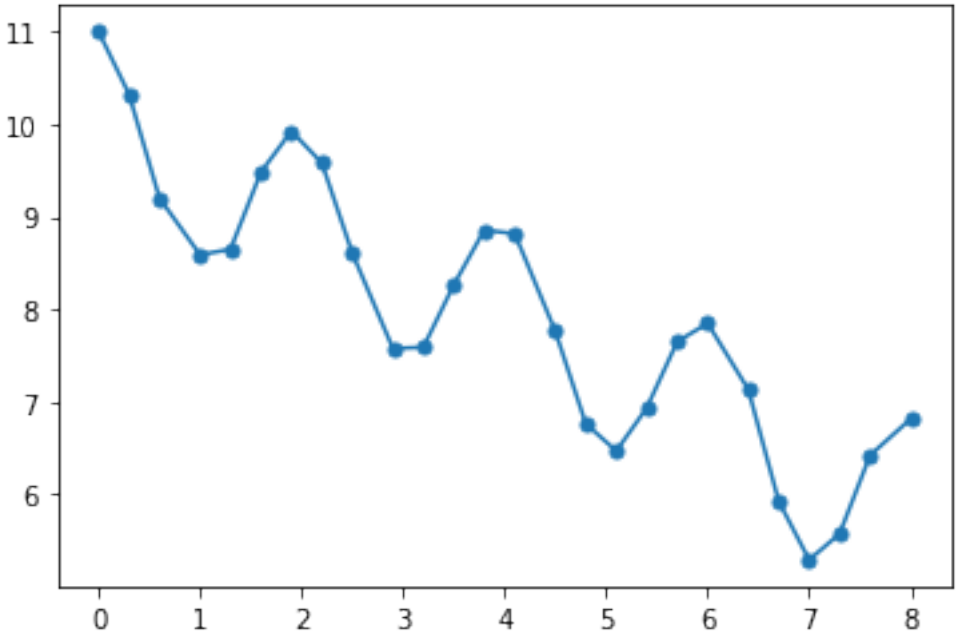
[67]:
```
x = np.arange(0,8*np.pi,0.1)   # start,stop,step
y = 10+np.cos(x)-x/6

y_noise = []

for i in y:
    n = 0.1
    noise = np.random.uniform(-n,n)
    y_noise.append(i + noise)

plt.plot(x,y_noise)
plt.show()
```



[68]:
```
df_original_series = pd.DataFrame({
    'period': x,
    'demand': y_noise
})

# include average interger.
df_interger_series = df_original_series[df_original_series['period'] % 1 == 0]
df_interger_series['period'] = df_interger_series['period'].div(np.pi).round(1)
plt.plot(df_interger_series['period'],df_interger_series['demand'],␣
 ↪marker='o',markersize=5)

# deseasonalize
```

```
series_deseasonalization = df_interger_series.loc[:, 'demand'].rolling(3).
 ↪mean().dropna()
series_deseasonalization=series_deseasonalization.
 ↪drop([series_deseasonalization.index[22],series_deseasonalization.index[23]])

# deseasonalize dataframe
df_deseasonalization = pd.DataFrame({
    'Quater': sum([[1,2,3]*8,[1,2]],[]),
    'Period': df_interger_series['period'] ,
    'Demand': df_interger_series['demand'] ,
    'Deseasonalized_Demand': series_deseasonalization
})
```

```
<ipython-input-68-ab869889bd6c>:8: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
  df_interger_series['period'] =
df_interger_series['period'].div(np.pi).round(1)
```



[69]:
```
#build up regressing model
reg = LinearRegression().fit(np.asarray(df_deseasonalization.loc[20:230,␣
 ↪'Period']).reshape(-1, 1),
```

```
                              df_deseasonalization.loc[:,␣
 ↪'Deseasonalized_Demand'].dropna())
#predict nan value
values = pd.Series(reg.predict(np.asarray(df_deseasonalization.loc[:,␣
 ↪'Period']).reshape(-1,1)))

df_deseasonalization.loc[0,['Deseasonalized_Demand']] = values[0]
df_deseasonalization.loc[10,['Deseasonalized_Demand']] = values[10]
df_deseasonalization.loc[240,['Deseasonalized_Demand']] = values[24]
df_deseasonalization.loc[250,['Deseasonalized_Demand']] = values[25]

# calculate seansonality factor
df_deseasonalization.loc[:, 'Seasonality'] = (df_deseasonalization.loc[:,␣
 ↪'Demand'] / df_deseasonalization.loc[:, 'Deseasonalized_Demand'])

df_Seasonality_bar= pd.DataFrame({
    'Quater': sum([[1,2,3]*8,[1,2]],[]),
    'Period': df_interger_series['period'] ,
    'Demand': df_interger_series['demand'] ,
    'Deseasonalized_Demand': series_deseasonalization
})

df_seasonality = df_deseasonalization.groupby(['Quater'], as_index=False).mean()
df_seasonality.loc[:, 'Seasonality_bar'] = df_seasonality.loc[:, 'Seasonality']
df_seasonality = df_seasonality[['Quater','Seasonality_bar']]

df_deseasonalization = pd.merge(df_deseasonalization,df_seasonality).
 ↪sort_values('Period')
```

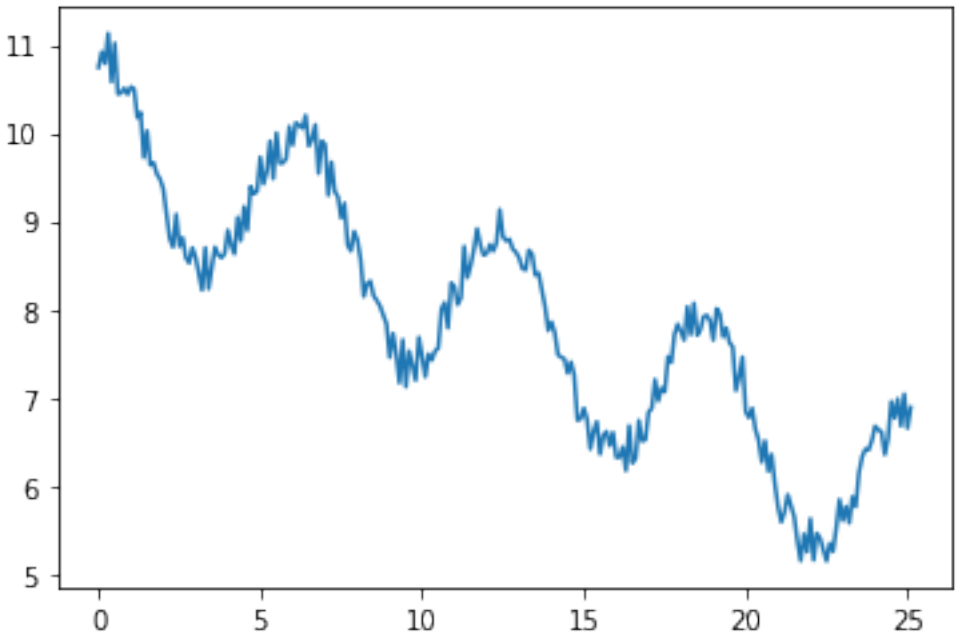
[70]:
```
df_deseasonalization.loc[:, 'Forecast'] =  (reg.predict(np.
 ↪asarray(df_deseasonalization.loc[:, 'Period']).reshape(-1,1)) *␣
 ↪df_deseasonalization.loc[:, 'Seasonality_bar'])
df_deseasonalization.loc[:, 'Error'] =  (df_deseasonalization.loc[:,␣
 ↪'Demand']-df_deseasonalization.loc[:, 'Forecast'])
df_deseasonalization.loc[:, 'Error_Squre'] =  (df_deseasonalization.loc[:,␣
 ↪'Error']*df_deseasonalization.loc[:, 'Error'])
MSE = df_deseasonalization['Error_Squre'].sum()/len(df_deseasonalization)
MAPE = ((abs(df_deseasonalization.loc[:, 'Error']) / abs(df_deseasonalization.
 ↪loc[:, 'Demand'])).sum())*100/len(df_deseasonalization)

print("MSE:",MSE.round(3))
print("MAPE:",MAPE.round(3))
```

```
MSE: 0.515
MAPE: 8.447
```

in this simulation, we have better performance in both MSE and MAPE

2 Q2

[71]:
```
x = np.arange(0,8*np.pi,0.1)   # start,stop,step
y = 10+np.cos(x)-x/6

y_noise = []

for i in y:
    n = 0.3
    noise = np.random.uniform(-n,n)
    y_noise.append(i + noise)

plt.plot(x,y_noise)
plt.show()
```

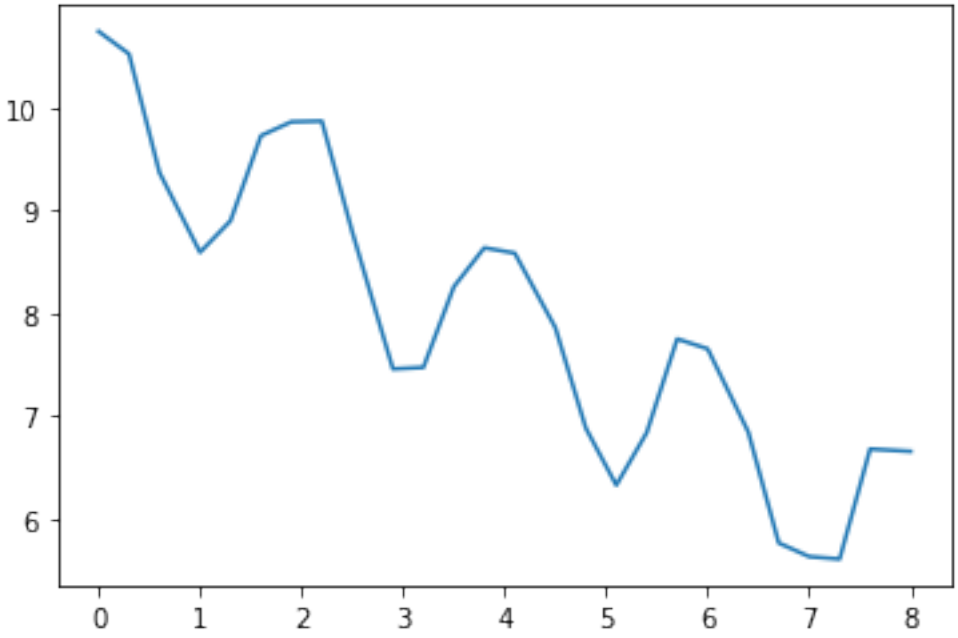


[72]:
```
df_original_series = pd.DataFrame({
    'Period': x,
    'Demand': y_noise
})

# include average interger.
df_interger_series = df_original_series[df_original_series['Period'] % 1 == 0]
df_interger_series['Period'] = df_interger_series['Period'].div(np.pi).round(1)
plt.plot(df_interger_series['Period'],df_interger_series['Demand'])
```

```
<ipython-input-72-bbe5da21f942>:8: SettingWithCopyWarning:
```

```
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
  df_interger_series['Period'] =
df_interger_series['Period'].div(np.pi).round(1)
```

[72]: `[<matplotlib.lines.Line2D at 0x1ee3dc94100>]`



[73]:
```
# train the data with Holt-Winters algorithms with statsmodels module.
HWES_model = HWES(df_interger_series.loc[:, 'Demand'], seasonal_periods=8,␣
 ↪trend='add', seasonal='mul')
HWES_fit_report = HWES_model.fit()
print(HWES_fit_report.summary())
```

```
                       ExponentialSmoothing Model Results
==============================================================================
Dep. Variable:                    Demand   No. Observations:                   26
Model:             ExponentialSmoothing   SSE                             11.221
Optimized:                         True   AIC                              2.152
Trend:                         Additive   BIC                             17.249
Seasonal:                Multiplicative   AICC                            40.334
Seasonal Periods:                     8   Date:                 Sun, 10 Oct 2021
Box-Cox:                          False   Time:                         03:13:49
Box-Cox Coeff.:                    None
```

```
================================================================================
=
                          coeff                 code              optimized
--------------------------------------------------------------------------------
-
smoothing_level            1.0000000               alpha
True
smoothing_trend           3.5816e-14                beta
True
smoothing_seasonal        1.4901e-08               gamma
True
initial_level              8.1211206                 l.0
True
initial_trend             -0.1204870                 b.0
True
initial_seasons.0          1.3426997                 s.0
True
initial_seasons.1          1.3198900                 s.1
True
initial_seasons.2          1.3150706                 s.2
True
initial_seasons.3          1.3339039                 s.3
True
initial_seasons.4          1.3653020                 s.4
True
initial_seasons.5          1.3973825                 s.5
True
initial_seasons.6          1.3933601                 s.6
True
initial_seasons.7          1.3725840                 s.7
True
--------------------------------------------------------------------------------
-

C:\Users\TerryYang\anaconda3\envs\TENSORFLOW\lib\site-
packages\statsmodels\tsa\base\tsa_model.py:578: ValueWarning: An unsupported
index was provided and will be ignored when e.g. forecasting.
  warnings.warn('An unsupported index was provided and will be'
C:\Users\TerryYang\anaconda3\envs\TENSORFLOW\lib\site-
packages\statsmodels\tsa\holtwinters\model.py:427: FutureWarning: After 0.13
initialization must be handled at model creation
  warnings.warn(
```