

R09546042__TSA__HW__02

October 10, 2021

0.0.1 import used library

```
[1]: import numpy as np
import matplotlib.pyplot as plt
import pandas as pd
from sklearn.linear_model import LinearRegression
from statsmodels.tsa.holtwinters import ExponentialSmoothing as HWES
```

1 Q1

1.1 a. Explain how you design the disturbance.

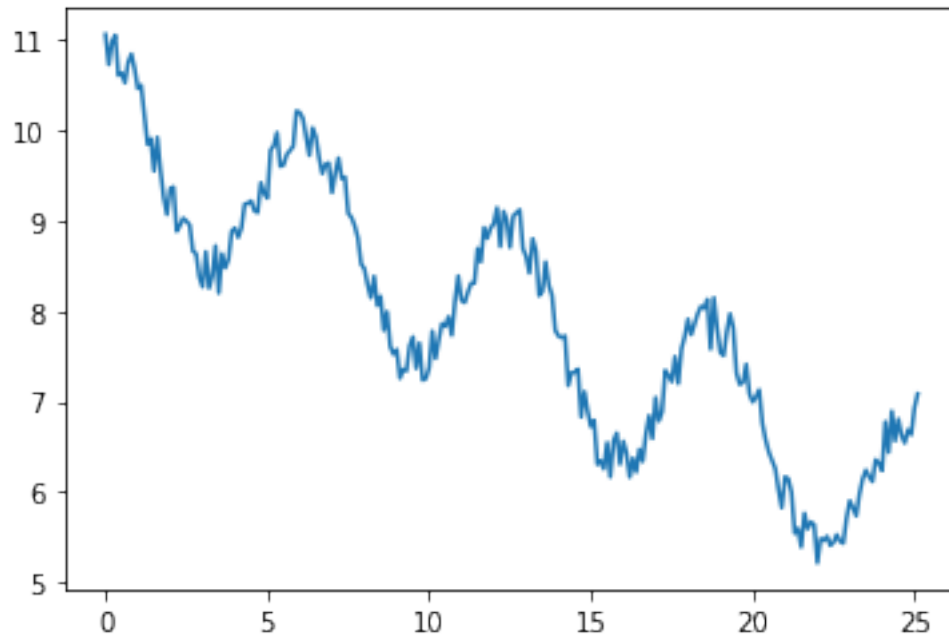
1.1.1 Use `cos()` for changing time-series, $-x/6$ for dwindling trend, 10 as label, and normal distribution($-0.3 \sim 0.3$) for noise.

```
[2]: x = np.arange(0,8*np.pi,0.1)
y = 10+np.cos(x)-x/6

# generate noise
y_noise = []

for i in y:
    n = 0.3
    noise = np.random.uniform(-n,n)
    y_noise.append(i + noise)

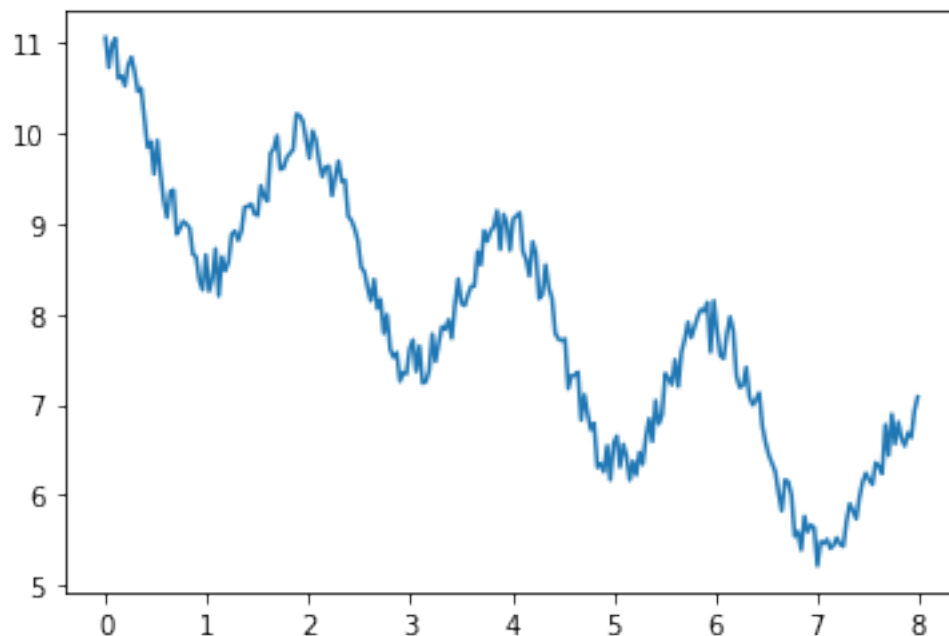
plt.plot(x,y_noise)
plt.show()
```



1.2 b. Identify the number of periods in a season and then deseasonalize the series.

1.2.1 Change x scale into π , making observation easier

```
[3]: plt.plot(x/np.pi,y_noise)
plt.show()
```



1.2.2 As the creator of this time-series, we know that its period is 3.14(by `cos()`), which means there are 3 interger data points in one period.

1.2.3 Leading us to assume period roughly close to 3.

```
[4]: df_original_series = pd.DataFrame({
      'period': x,
      'demand': y_noise
    })

    # include average interger.
    df_interger_series = df_original_series[df_original_series['period'] % 1 == 0]
    df_interger_series['period'] = df_interger_series['period'].div(np.pi).round(1)
    plt.plot(df_interger_series['period'],df_interger_series['demand'],□
      ↪marker='o',markersize=5)

    # deseasonalize
    series_deseasonalization = df_interger_series.loc[:, 'demand'].rolling(3).
      ↪mean().dropna()
    series_deseasonalization=series_deseasonalization.
      ↪drop([series_deseasonalization.index[22],series_deseasonalization.index[23]])

    # deseasonalize dataframe
    df_deseasonalization = pd.DataFrame({
      'Quater': sum([[1,2,3]*8,[1,2]],[]),
      'Period': df_interger_series['period'] ,
      'Demand': df_interger_series['demand'] ,
      'Deseasonalized_Demand': series_deseasonalization
    })
```

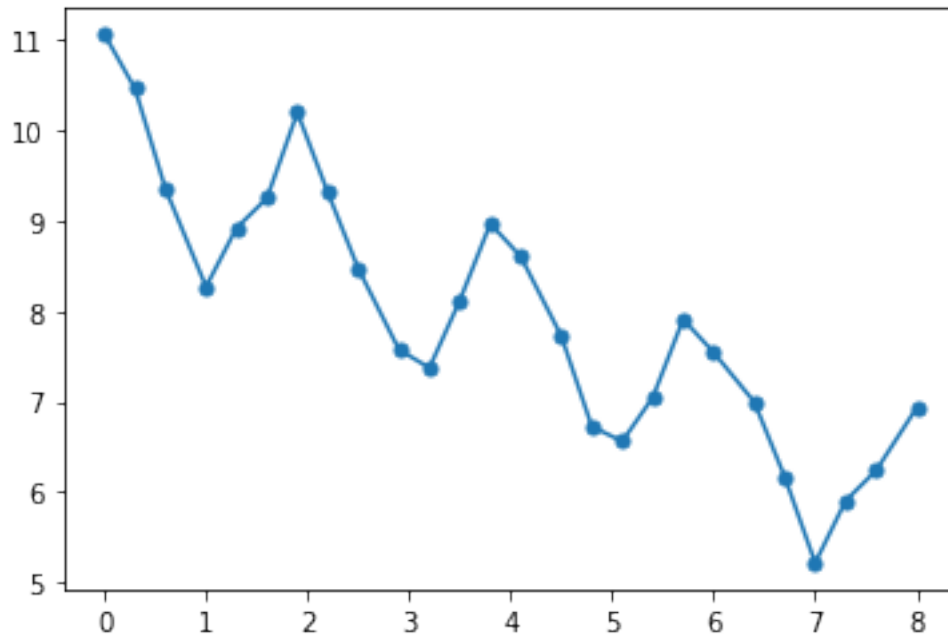
<ipython-input-4-ab869889bd6c>:8: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.

Try using `.loc[row_indexer,col_indexer] = value` instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```
df_interger_series['period'] =
df_interger_series['period'].div(np.pi).round(1)
```



1.3 c. Calculate the seasonality factors

```
[5]: #build up regressing model
reg = LinearRegression().fit(np.asarray(df_deseasonalization.loc[20:230,
    ↳ 'Period']).reshape(-1, 1),
                                df_deseasonalization.loc[:,
    ↳ 'Deseasonalized_Demand']).dropna())
#predict nan value
values = pd.Series(reg.predict(np.asarray(df_deseasonalization.loc[:,
    ↳ 'Period']).reshape(-1,1))))

#fill up nan value
df_deseasonalization.loc[0,['Deseasonalized_Demand']] = values[0]
df_deseasonalization.loc[10,['Deseasonalized_Demand']] = values[10]
df_deseasonalization.loc[240,['Deseasonalized_Demand']] = values[24]
df_deseasonalization.loc[250,['Deseasonalized_Demand']] = values[25]

# calculate seansonality factor
df_deseasonalization.loc[:, 'Seasonality'] = (df_deseasonalization.loc[:,
    ↳ 'Demand'] / df_deseasonalization.loc[:, 'Deseasonalized_Demand'])

df_Seasonality_bar= pd.DataFrame({
    'Quater': sum([[1,2,3]*8,[1,2]],[]),
    'Period': df_interger_series['period'] ,
    'Demand': df_interger_series['demand'] ,
```

```

'Deseasonalized_Demand': series_deseasonalization
})

df_seasonality = df_deseasonalization.groupby(['Quater'], as_index=False).mean()
df_seasonality.loc[:, 'Seasonality_bar'] = df_seasonality.loc[:, 'Seasonality']
df_seasonality = df_seasonality[['Quater', 'Seasonality_bar']]
df_deseasonalization = pd.merge(df_deseasonalization, df_seasonality).
    ↳sort_values('Period')

```

```
[6]: df_deseasonalization
```

```

[6]:   Quater  Period    Demand  Deseasonalized_Demand  Seasonality \
0        1     0.0  11.053918          10.119166      1.092374
9        2     0.3  10.455796           8.455223      1.236608
18       3     0.6   9.349128          10.286280      0.908893
1        1     1.0   8.266442           9.357122      0.883439
10       2     1.3   8.915853           8.843808      1.008146
19       3     1.6   9.245860           8.809385      1.049547
2        1     1.9  10.191551           9.451088      1.078347
11       2     2.2   9.306449           9.581287      0.971315
20       3     2.5   8.466014           9.321338      0.908240
3        1     2.9   7.573053           8.448505      0.896378
12       2     3.2   7.370566           7.803211      0.944555
21       3     3.5   8.116188           7.686602      1.055888
4        1     3.8   8.964254           8.150336      1.099863
13       2     4.1   8.599915           8.560119      1.004649
22       3     4.5   7.721453           8.428541      0.916108
5        1     4.8   6.722205           7.681191      0.875151
14       2     5.1   6.559955           7.001204      0.936975
23       3     5.4   7.043282           6.775147      1.039576
6        1     5.7   7.908110           7.170449      1.102875
15       2     6.0   7.541343           7.497578      1.005837
24       3     6.4   6.994145           7.481199      0.934896
7        1     6.7   6.166982           6.900824      0.893659
16       2     7.0   5.216677           6.125935      0.851572
25       3     7.3   5.902539           5.762066      1.024379
8        1     7.6   6.237170           6.167302      1.011329
17       2     8.0   6.930420           5.959309      1.162957

      Seasonality_bar
0          0.992602
9          1.013624
18         0.979691
1          0.992602
10         1.013624
19         0.979691
2          0.992602

```

11	1.013624
20	0.979691
3	0.992602
12	1.013624
21	0.979691
4	0.992602
13	1.013624
22	0.979691
5	0.992602
14	1.013624
23	0.979691
6	0.992602
15	1.013624
24	0.979691
7	0.992602
16	1.013624
25	0.979691
8	0.992602
17	1.013624

```
[7]: df_seasonality
```

```
[7]:   Quarter  Seasonality_bar
0         1         0.992602
1         2         1.013624
2         3         0.979691
```

1.4 d. Finalize the model and evaluate the performance via MSE and MAPE

```
[8]: # calculate Forecast, Error, Error_Square, MSE, MAPE
df_deseasonalization.loc[:, 'Forecast'] = (reg.predict(np.
    ↳ asarray(df_deseasonalization.loc[:, 'Period']).reshape(-1,1)) *
    ↳ df_deseasonalization.loc[:, 'Seasonality_bar'])
df_deseasonalization.loc[:, 'Error'] = (df_deseasonalization.loc[:,
    ↳ 'Demand'] - df_deseasonalization.loc[:, 'Forecast'])
df_deseasonalization.loc[:, 'Error_Square'] = (df_deseasonalization.loc[:,
    ↳ 'Error'] * df_deseasonalization.loc[:, 'Error'])
MSE = df_deseasonalization['Error_Square'].sum() / len(df_deseasonalization)
MAPE = ((abs(df_deseasonalization.loc[:, 'Error']) / abs(df_deseasonalization.
    ↳ loc[:, 'Demand'])).sum()) * 100 / len(df_deseasonalization)

print("Time-Series Model:")
print("MSE:", MSE.round(3))
print("MAPE:", MAPE.round(3))
```

```
Time-Series Model:
MSE: 0.524
```

MAPE: 7.853

1.5 e. Use the static model to predict , = 25, ... , 30. Use the “true” model to simulate 25, ... , 30 and calculate the MSE and MAPE accordingly.

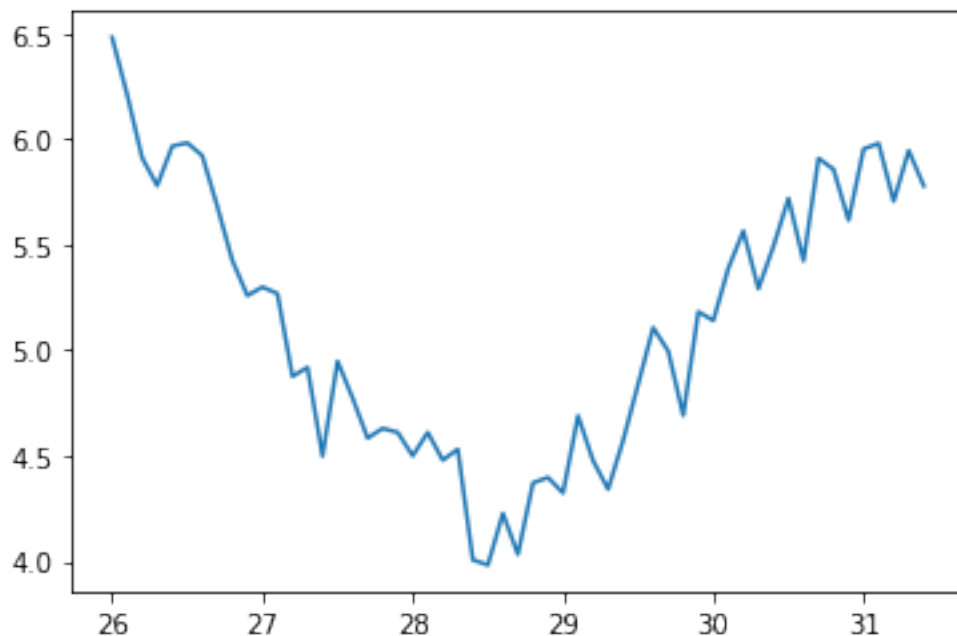
1.5.1 Construct further more data points(y=26~31)

```
[9]: x = np.arange(26.0,10*np.pi,0.1)
y = 10+np.cos(x)-x/6

y_noise = []

for i in y:
    n = 0.3
    noise = np.random.uniform(-n,n)
    y_noise.append(i + noise)

plt.plot(x,y_noise)
plt.show()
```



1.5.2 Predicting while using true model

```
[10]: #true model
df_true_model = pd.DataFrame({
    'Period': x,
    'Demand': y_noise,
```

```

        'Forecast':y,
    })
df_true_model.loc[:, 'Error'] = (df_true_model.loc[:, 'Demand']-df_true_model.
    ↳loc[:, 'Forecast'])
df_true_model.loc[:, 'Error_Square'] = (df_true_model.loc[:,
    ↳'Error']*df_true_model.loc[:, 'Error'])
MSE = df_true_model['Error_Square'].sum()/len(df_true_model)
MAPE = ((abs(df_true_model.loc[:, 'Error']) / abs(df_true_model.loc[:,
    ↳'Demand'])).sum()*100/len(df_true_model)

print("True Model(y=26~31):")
print("MSE:",MSE.round(3))
print("MAPE:",MAPE.round(3))

```

True Model(y=26~31):
MSE: 0.031
MAPE: 3.02

1.5.3 Predicting while using constructed model

```

[11]: #time-series model
df_time_series_model = pd.DataFrame({
    'Period': x,
    'Demand': y_noise
})

df_interger_series = df_time_series_model[df_time_series_model['Period'].
    ↳round(1) % 1.0 == 0]
df_interger_series['Period'] = df_interger_series['Period'].div(np.pi).round(1)
plt.plot(df_interger_series['Period'],df_interger_series['Demand'],
    ↳marker='o',markersize=5)

df_time_series_deseasonalization= pd.DataFrame({
df_time_series_deseasonalization = pd.
    ↳merge(df_interger_series,df_deseasonalization, how="outer").
    ↳sort_values('Period')
df_time_series_deseasonalization.loc[:, 'Quater']=sum([[1,2,3]*10,[1,2]],[])

df_time_series_deseasonalization=df_time_series_deseasonalization.
    ↳drop(['Seasonality_bar'], axis=1)
df_time_series_deseasonalization = pd.
    ↳merge(df_time_series_deseasonalization,df_seasonality,how = "outer").
    ↳sort_values('Period')

```



```

df_time_series_deseasonalization.loc[:, 'Forecast'] = (reg.predict(np.
    ↳asarray(df_time_series_deseasonalization.loc[:, 'Period']).reshape(-1,1)) *
    ↳df_time_series_deseasonalization.loc[:, 'Seasonality_bar'])
df_time_series_deseasonalization.loc[:, 'Error'] =
    ↳(df_time_series_deseasonalization.loc[:,
    ↳'Demand']-df_time_series_deseasonalization.loc[:, 'Forecast'])
df_time_series_deseasonalization.loc[:, 'Error_Square'] =
    ↳(df_time_series_deseasonalization.loc[:,
    ↳'Error']*df_time_series_deseasonalization.loc[:, 'Error'])
MSE = df_time_series_deseasonalization['Error_Square'].sum()/
    ↳len(df_time_series_deseasonalization)
MAPE = ((abs(df_time_series_deseasonalization.loc[:, 'Error']) /
    ↳abs(df_time_series_deseasonalization.loc[:, 'Demand'])).sum()*100/
    ↳len(df_deseasonalization))

print("Time-Series Model(y=26~31):")
print("MSE:",MSE.round(3))
print("MAPE:",MAPE.round(3))

```

Time-Series Model(y=26~31):

MSE: 0.536

MAPE: 10.853

<ipython-input-11-c8e5766bbe8b>:9: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.

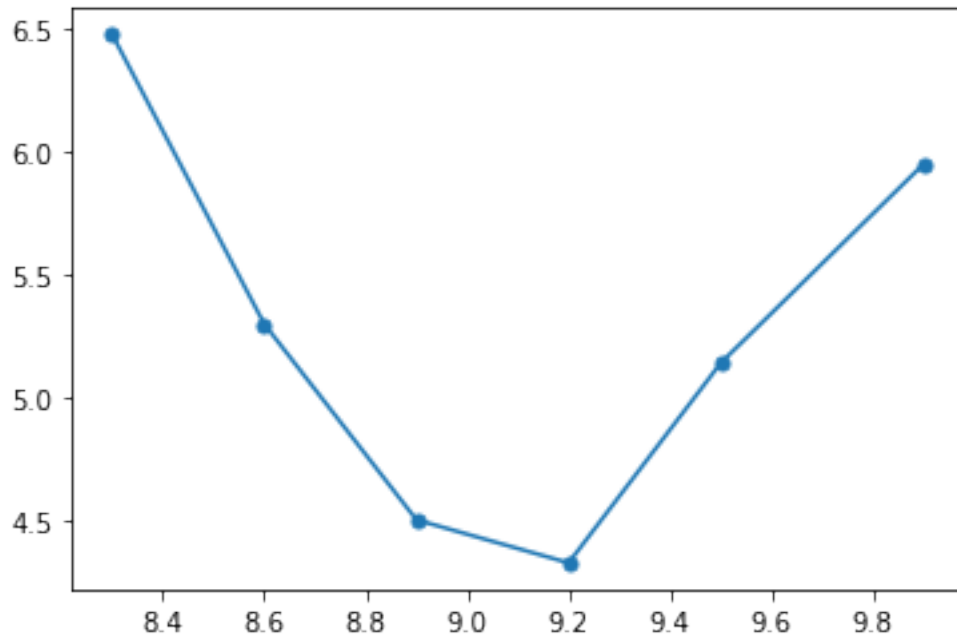
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```

df_interger_series['Period'] =
df_interger_series['Period'].div(np.pi).round(1)

```



1.6 f. Modify the disturbance in (a) to change series (can be more or less fluctuating). Re-run the questions (b)-(d). What can you conclude when comparing to the results in (d) with the previous disturbance.

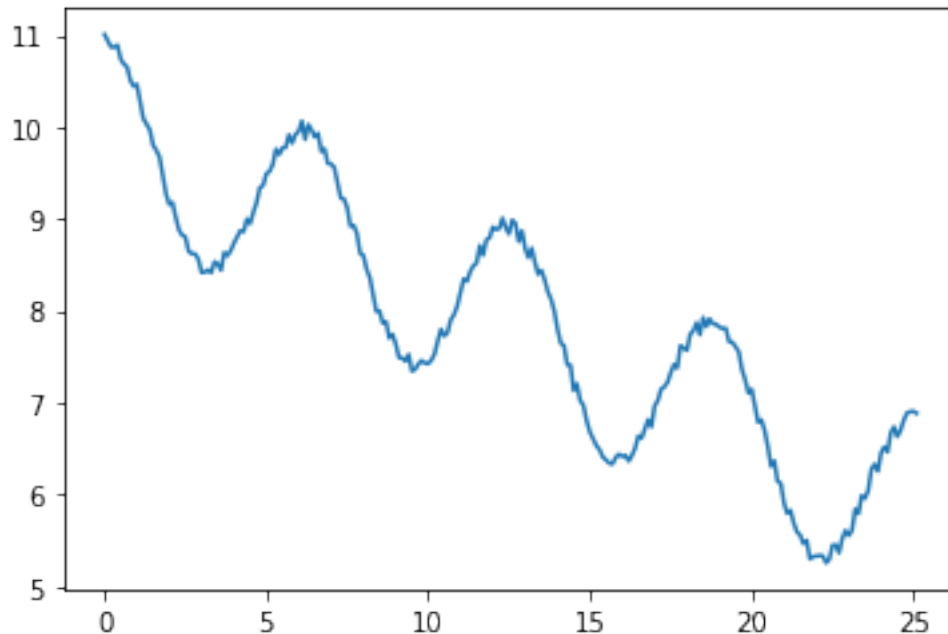
1.6.1 Change noise factor from 0.3 to 0.1.

```
[12]: x = np.arange(0,8*np.pi,0.1)
      y = 10+np.cos(x)-x/6

      y_noise = []

      for i in y:
          n = 0.1
          noise = np.random.uniform(-n,n)
          y_noise.append(i + noise)

      plt.plot(x,y_noise)
      plt.show()
```



```
[13]: df_original_series = pd.DataFrame({
        'period': x,
        'demand': y_noise
    })

    # include average interger.
    df_interger_series = df_original_series[df_original_series['period'] % 1 == 0]
    df_interger_series['period'] = df_interger_series['period'].div(np.pi).round(1)
    plt.plot(df_interger_series['period'],df_interger_series['demand'],□
        ↪marker='o',markersize=5)

    # deseasonalize
    series_deseasonalization = df_interger_series.loc[:, 'demand'].rolling(3).
        ↪mean().dropna()
    series_deseasonalization=series_deseasonalization.
        ↪drop([series_deseasonalization.index[22],series_deseasonalization.index[23]])

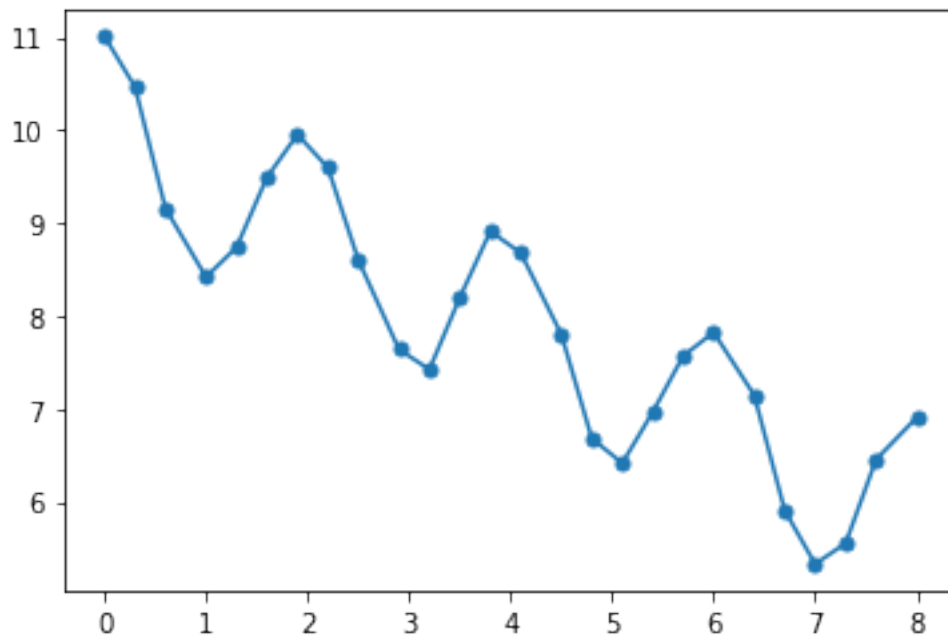
    # deseasonalize dataframe
    df_deseasonalization = pd.DataFrame({
        'Quater': sum([[1,2,3]*8,[1,2]],[]),
        'Period': df_interger_series['period'] ,
        'Demand': df_interger_series['demand'] ,
        'Deseasonalized_Demand': series_deseasonalization
    })
```

<ipython-input-13-ab869889bd6c>:8: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using `.loc[row_indexer,col_indexer] = value` instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```
df_interger_series['period'] =  
df_interger_series['period'].div(np.pi).round(1)
```



```
[14]: #build up regressing model  
reg = LinearRegression().fit(np.asarray(df_deseasonalization.loc[20:230,␣  
    ↳ 'Period']).reshape(-1, 1),  
                             df_deseasonalization.loc[:,␣  
    ↳ 'Deseasonalized_Demand']).dropna())  
#predict nan value  
values = pd.Series(reg.predict(np.asarray(df_deseasonalization.loc[:,␣  
    ↳ 'Period']).reshape(-1,1)))  
  
df_deseasonalization.loc[0,['Deseasonalized_Demand']] = values[0]  
df_deseasonalization.loc[10,['Deseasonalized_Demand']] = values[10]  
df_deseasonalization.loc[240,['Deseasonalized_Demand']] = values[24]  
df_deseasonalization.loc[250,['Deseasonalized_Demand']] = values[25]  
  
# calculate seansonality factor  
df_deseasonalization.loc[:, 'Seasonality'] = (df_deseasonalization.loc[:,␣  
    ↳ 'Demand'] / df_deseasonalization.loc[:, 'Deseasonalized_Demand'])
```

```

df_Seasonality_bar= pd.DataFrame({
    'Quater': sum([[1,2,3]*8,[1,2]],[]),
    'Period': df_interger_series['period'] ,
    'Demand': df_interger_series['demand'] ,
    'Deseasonalized_Demand': series_deseasonalization
})

df_seasonality = df_deseasonalization.groupby(['Quater'], as_index=False).mean()
df_seasonality.loc[:, 'Seasonality_bar'] = df_seasonality.loc[:, 'Seasonality']
df_seasonality = df_seasonality[['Quater', 'Seasonality_bar']]

df_deseasonalization = pd.merge(df_deseasonalization,df_seasonality).
    ↪sort_values('Period')

```

```

[15]: df_deseasonalization.loc[:, 'Forecast'] = (reg.predict(np.
    ↪asarray(df_deseasonalization.loc[:, 'Period']).reshape(-1,1)) *
    ↪df_deseasonalization.loc[:, 'Seasonality_bar'])
df_deseasonalization.loc[:, 'Error'] = (df_deseasonalization.loc[:,
    ↪'Demand']-df_deseasonalization.loc[:, 'Forecast'])
df_deseasonalization.loc[:, 'Error_Squire'] = (df_deseasonalization.loc[:,
    ↪'Error']*df_deseasonalization.loc[:, 'Error'])
MSE = df_deseasonalization['Error_Squire'].sum()/len(df_deseasonalization)
MAPE = ((abs(df_deseasonalization.loc[:, 'Error']) / abs(df_deseasonalization.
    ↪loc[:, 'Demand'])).sum()*100/len(df_deseasonalization))

print("Time-Series Model(less disturbance):")
print("MSE:",MSE.round(3))
print("MAPE:",MAPE.round(3))

```

Time-Series Model(less disturbance):
MSE: 0.546
MAPE: 8.679

1.6.2 In this disturbance data simulation, we have better performance in both MSE and MAPE than previous model

2 Q2

2.0.1 rearrange the data

```

[16]: x = np.arange(0,8*np.pi,0.1)
y = 10+np.cos(x)-x/6

y_noise = []

for i in y:
    n = 0.3

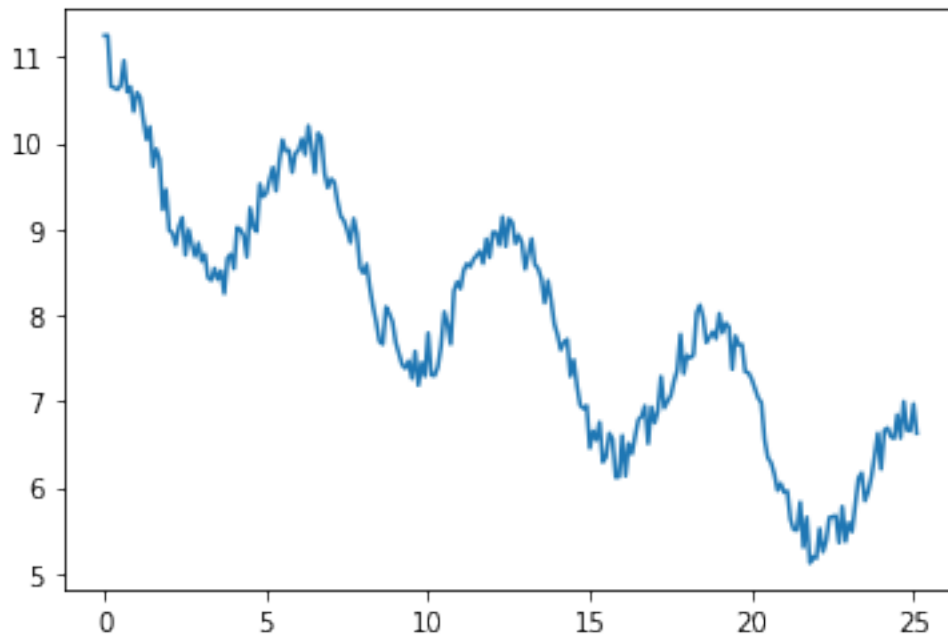
```

```

noise = np.random.uniform(-n,n)
y_noise.append(i + noise)

plt.plot(x,y_noise)
plt.show()

```



```

[17]: df_original_series = pd.DataFrame({
        'Period': x,
        'Demand': y_noise
    })

    # include average interger.
    df_interger_series = df_original_series[df_original_series['Period'] % 1 == 0]
    df_interger_series['Period'] = df_interger_series['Period'].div(np.pi).round(1)
    plt.plot(df_interger_series['Period'],df_interger_series['Demand'],□
        ↪marker='o',markersize=5)

```

<ipython-input-17-e09ded7e73c9>:8: SettingWithCopyWarning:
 A value is trying to be set on a copy of a slice from a DataFrame.
 Try using .loc[row_indexer,col_indexer] = value instead

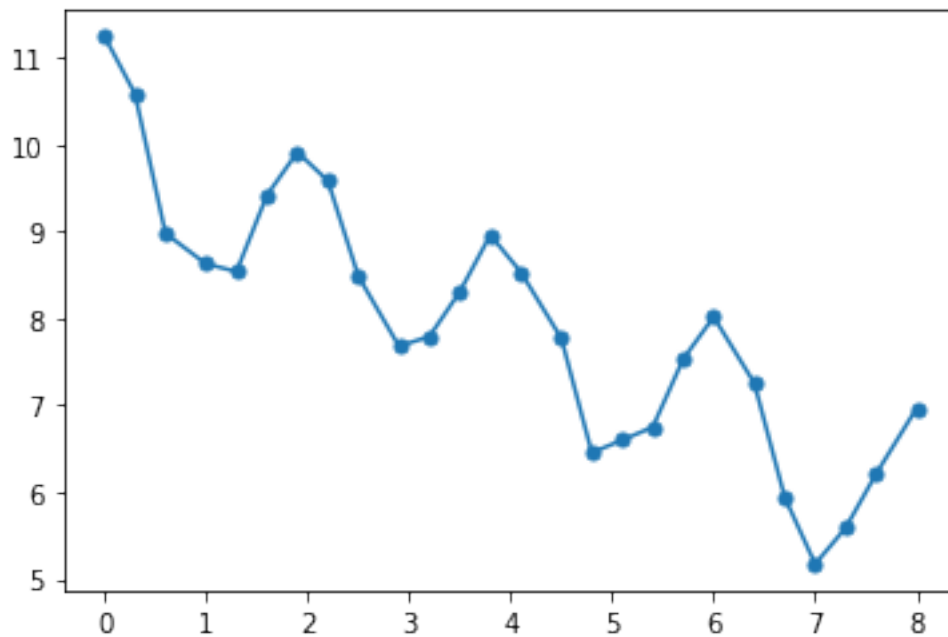
See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```

    df_interger_series['Period'] =
    df_interger_series['Period'].div(np.pi).round(1)

```

[17]: [<matplotlib.lines.Line2D at 0x16ba3c51f10>]



```
[18]: # train the data with Holt-Winters algorithms with statsmodels module.
HWES_model = HWES(df_interger_series.loc[:, 'Demand'], seasonal_periods=3,
    ↪trend='add', seasonal='mul')
HWES_fit_report = HWES_model.fit()
print(HWES_fit_report.summary())
```

ExponentialSmoothing Model Results

```
=====
Dep. Variable:          Demand    No. Observations:          26
Model:          ExponentialSmoothing    SSE          13.224
Optimized:          True    AIC          -3.578
Trend:          Additive    BIC          5.229
Seasonal:          Multiplicative    AICC          7.672
Seasonal Periods:          3    Date:          Sun, 10 Oct 2021
Box-Cox:          False    Time:          22:34:05
Box-Cox Coeff.:          None
=====
```

```
=
      coeff          code    optimized
-----
-
smoothing_level    1.0000000    alpha
True
smoothing_trend    4.8631e-13    beta
```

True		
smoothing_seasonal	1.5746e-09	gamma
True		
initial_level	7.1094084	1.0
True		
initial_trend	-0.1086316	b.0
True		
initial_seasons.0	1.6064587	s.0
True		
initial_seasons.1	1.6246751	s.1
True		
initial_seasons.2	1.5939570	s.2
True		

-

C:\Users\TerryYang\anaconda3\envs\TENSORFLOW\lib\site-packages\statsmodels\tsa\base\tsa_model.py:578: ValueWarning: An unsupported index was provided and will be ignored when e.g. forecasting.
 warnings.warn('An unsupported index was provided and will be'

C:\Users\TerryYang\anaconda3\envs\TENSORFLOW\lib\site-packages\statsmodels\tsa\holtwinters\model.py:427: FutureWarning: After 0.13 initialization must be handled at model creation
 warnings.warn(