

**Import statement**

```
1 from math import pi
2 tau = 2 * pi
```

**Assignment statement**

**Code (left):**

Statements and expressions  
Red arrow points to next line.  
Gray arrow points to the line just executed

**Frames (right):**

A name is bound to a value  
In a frame, there is at most one binding per name

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(-2)
```

**Built-in function**

**User-defined function**

**Global frame**

**Intrinsic name of function called**

**Local frame**

**Formal parameter bound to argument**

**Return value**

**Return value is not a binding!**

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(square(3))
```

**Global frame**

**f1: square [parent=Global]**

**f2: square [parent=Global]**

**Return value**

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

**Evaluation rule for call expressions:**

1. Evaluate the operator and operand subexpressions.
2. Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

**Applying user-defined functions:**

1. Create a new local frame with the same parent as the function that was applied.
2. Bind the arguments to the function's formal parameter names in that frame.
3. Execute the body of the function in the environment beginning at that frame.

**Execution rule for def statements:**

1. Create a new function value with the specified name, formal parameters, and function body.
2. Its parent is the first frame of the current environment.
3. Bind the name of the function to the function value in the first frame of the current environment.

**Execution rule for assignment statements:**

1. Evaluate the expression(s) on the right of the equal sign.
2. Simultaneously bind the names on the left to those values, in the first frame of the current environment.

**Execution rule for conditional statements:**

- Each clause is considered in order.
1. Evaluate the header's expression.
  2. If it is a true value, execute the suite, then skip the remaining clauses in the statement.

**Evaluation rule for or expressions:**

1. Evaluate the subexpression <left>.
2. If the result is a true value v, then the expression evaluates to v.
3. Otherwise, the expression evaluates to the value of the subexpression <right>.

**Evaluation rule for and expressions:**

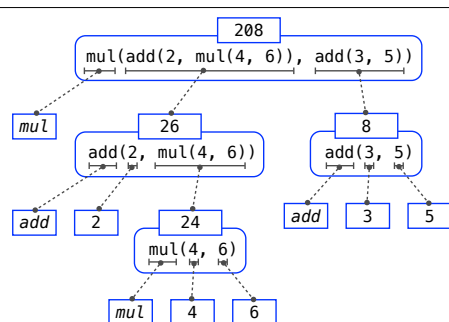
1. Evaluate the subexpression <left>.
2. If the result is a false value v, then the expression evaluates to v.
3. Otherwise, the expression evaluates to the value of the subexpression <right>.

**Evaluation rule for not expressions:**

1. Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

**Execution rule for while statements:**

1. Evaluate the header's expression.
2. If it is a true value, execute the (whole) suite, then return to step 1.



**Defining:**

**Formal parameter**

**Return expression**

**Def statement**

```
>>> def square(x):
    return mul(x, x)
```

**Body (return statement)**

**Call expression:** square(2+2)

**operator:** square

**function:** func square(x)

**operand:** 2+2

**argument:** 4

**Calling/Applying:**

**Argument**

**Intrinsic name**

**Return value**

```
4 square(x):
    return mul(x, x)
```

**Return value** 16

```
1 def f(x, y):
2     return g(x)
3
4 def g(a):
5     return a + y
6
7 result = f(1, 2)
```

**Global frame**

**f1: f [parent=Global]**

**f2: g [parent=Global]**

**Error**

**"y" is not found**

**"y" is not found**

- An environment is a sequence of frames
- An environment for a non-nested function (no def within def) consists of one local frame, followed by the global frame

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(4)
```

**Global frame**

**f1: square [parent=Global]**

**Return value** 16

A call expression and the body of the function being called are evaluated in different environments

```
def fib(n):
    """Compute the nth Fibonacci number, for N >= 1."""
    pred, curr = 0, 1 # Zeroth and first Fibonacci numbers
    k = 1 # curr is the kth Fibonacci number
    while k < n:
        pred, curr = curr, pred + curr
        k = k + 1
    return curr
```

```
def cube(k):
    return pow(k, 3)

def summation(n, term):
    """Sum the first n terms of a sequence.

    >>> summation(5, cube)
    225
    """
    total, k = 0, 1
    while k <= n:
        total, k = total + term(k), k + 1
    return total
```

**Function of a single argument (not called term)**

**A formal parameter that will be bound to a function**

**Sum the first n terms of a sequence.**

**The cube function is passed as an argument value**

**The function bound to term gets called here**

**0 + 1<sup>3</sup> + 2<sup>3</sup> + 3<sup>3</sup> + 4<sup>3</sup> + 5<sup>3</sup>**

**Pure Functions**

```
-2 abs(number):
    2
```

```
2, 10 pow(x, y):
    1024
```

**Non-Pure Functions**

```
-2 print(...):
    None
```

**display "-2"**

**Compound statement**

**Clause**

```
<header>:
    <statement>
    <statement>
    ...
```

**Suite**

**<separating header>:**

```
<statement>
<statement>
...

```

```
def abs_value(x):
    1 statement,
    3 clauses,
    3 headers,
    3 suites,
    2 boolean
    contexts
    if x > 0:
        return x
    elif x == 0:
        return 0
    else:
        return -x
```

**Higher-order function:** A function that takes a function as an argument value or returns a function as a return value

**Nested def statements:** Functions defined within other function bodies are bound to names in the local frame

