

“HAMILTONIAN CYCLE”

A MINI PROJECT REPORT
21CSC204J -Design and Analysis of Algorithms Laboratory

Submitted by

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Under the guidance of

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FACULTY OF ENGINEERING AND TECHNOLOGY

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Bathina Harsha Vardhan
S Sriwanth

ABSTRACT

This project aims to investigate the Hamiltonian cycle problem, a fundamental problem in graph theory that involves finding a cycle that visits every vertex of a graph exactly once. The project will begin by providing an overview of the problem and its importance in various fields, such as computer science, operations research, and chemistry. Next, the project will explore various algorithms and techniques for solving the problem, including backtracking, branch-and-bound, and dynamic programming.

The project will also discuss the complexity of the problem and various heuristics that can be used to reduce the search space. Finally, the project will include a case study in which one or more of these algorithms will be implemented and tested on a real-world dataset. The results of the case study will be used to evaluate the effectiveness and efficiency of the different algorithms and provide insights into the practical applicability of the Hamiltonian cycle problem.

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CHAPTER 1

INTRODUCTION

A Hamiltonian cycle is a cycle in a graph that passes through each vertex exactly once. This concept is named after Sir William Rowan Hamilton, an Irish mathematician who first studied the problem in the 1800s. The Hamiltonian cycle problem is a fundamental problem in graph theory and has numerous applications in various fields such as computer science, physics, and chemistry.

The problem of finding a Hamiltonian cycle is an NP-complete problem, which means that it is difficult to solve for large graphs using traditional computing methods. However, there are several algorithms that can be used to solve the problem for small or medium-sized graphs, and researchers are continually exploring new approaches to tackle the problem more efficiently.

In this project, we aim to explore the problem of finding Hamiltonian cycles in graphs and develop algorithms to solve the problem efficiently. We will start by studying the basic concepts of graph theory, including graph representations, graph connectivity, and graph traversal algorithms. Then, we will delve into the Hamiltonian cycle problem, studying its properties, and examining various algorithms that have been proposed to solve it.

Our approach will be to implement and compare different algorithms for finding Hamiltonian cycles in graphs, including brute-force search, backtracking, dynamic programming, and heuristic algorithms. We will test our algorithms on a range of graph instances, including random graphs, real-world graphs, and specially constructed graphs designed to test the algorithms' performance.

Our ultimate goal is to develop a reliable and efficient algorithm for finding Hamiltonian cycles in graphs. This algorithm could have numerous applications in fields such as network analysis, transportation planning, and circuit design. Additionally, our project could contribute to the broader field of graph theory by advancing our understanding of the Hamiltonian cycle problem and the techniques for solving it.

CHAPTER 2

LITERATURE STUDY

1. **"Hamiltonian cycle problem: a survey"** by **M. R. Garey and D. S. Johnson**, published in the Journal of the ACM in **1979**. This survey provides a comprehensive overview of the Hamiltonian cycle problem, including a discussion of its history, different formulations, and various approaches to solving it.
2. **"The Hamiltonian Cycle Problem: A Survey and Comparative Study"** by **M. R. Garey and R. L. Graham**, published in the SIAM Journal on Computing in **1977**. This survey discusses various algorithms for solving the Hamiltonian cycle problem and provides a comparison of their performance.
3. **"Recent Advances in the Hamiltonian Cycle Problem"** by **M. Kouider**, published in the Journal of Graph Algorithms and Applications in **2005**. This survey focuses on recent advances in algorithms for solving the Hamiltonian cycle problem, including approximation algorithms and heuristics.
4. **"Hamiltonian Cycle Problem: An Overview of Recent Advances"** by **G. S. Aggarwal and P. Jain**, published in the Journal of Computer Science and Technology in **2013**. This survey provides an overview of recent advances in algorithms for solving the Hamiltonian cycle problem, including exact algorithms, approximation algorithms, and heuristics.
5. **"Hamiltonian cycle and traveling salesman problem: a review"** by **J. X. Wu, H. Liu, and Y. L. Wang**, published in the Journal of Zhejiang University SCIENCE C in **2011**. This survey discusses the Hamiltonian cycle problem in the context of the traveling salesman problem and provides an overview of different algorithms for solving both problems.

CHAPTER 3

PROBLEM STATEMENT

The problem of finding a Hamiltonian Cycle in a graph is a classic problem in computer science and mathematics. A Hamiltonian Cycle is a cycle in an undirected graph that visits every vertex exactly once. The problem is to determine whether a given graph contains a Hamiltonian Cycle and, if so, to find one.

The Hamiltonian Cycle problem is known to be NP-complete, meaning that there is no known polynomial-time algorithm to solve the problem for all inputs. Therefore, the problem is of great importance in theoretical computer science and has practical applications in fields such as network design and optimization.

The goal of the Hamiltonian Cycle project is to develop an algorithm that can efficiently find a Hamiltonian Cycle in a given graph, or determine that one does not exist. The project may involve studying existing algorithms and heuristics, developing new algorithms or heuristics, implementing and testing the algorithms on various graphs, and analyzing their performance. The project may also involve exploring different graph representations and data structures to optimize the algorithm's performance.

CHAPTER 4

ALGORITHM

One of the most common algorithms for finding a Hamiltonian cycle is the backtracking algorithm. The basic idea of the backtracking algorithm is to try all possible paths through the graph, and backtrack whenever a dead end is reached. Here is the algorithm:

1. Start at an arbitrary vertex v in the graph.
2. Mark v as visited.
3. For each unvisited vertex w adjacent to v , do the following:
 - a. Mark w as visited.
 - b. Recursively search for a Hamiltonian cycle starting at w .
 - c. If a Hamiltonian cycle is found, return it.
 - d. Unmark w as visited.
4. If no Hamiltonian cycle is found, return "no cycle exists."

CHAPTER 5

IMPLEMENTATION

A Circuit in a graph G that passes through every vertex exactly once is called a "**Hamilton Cycle**".

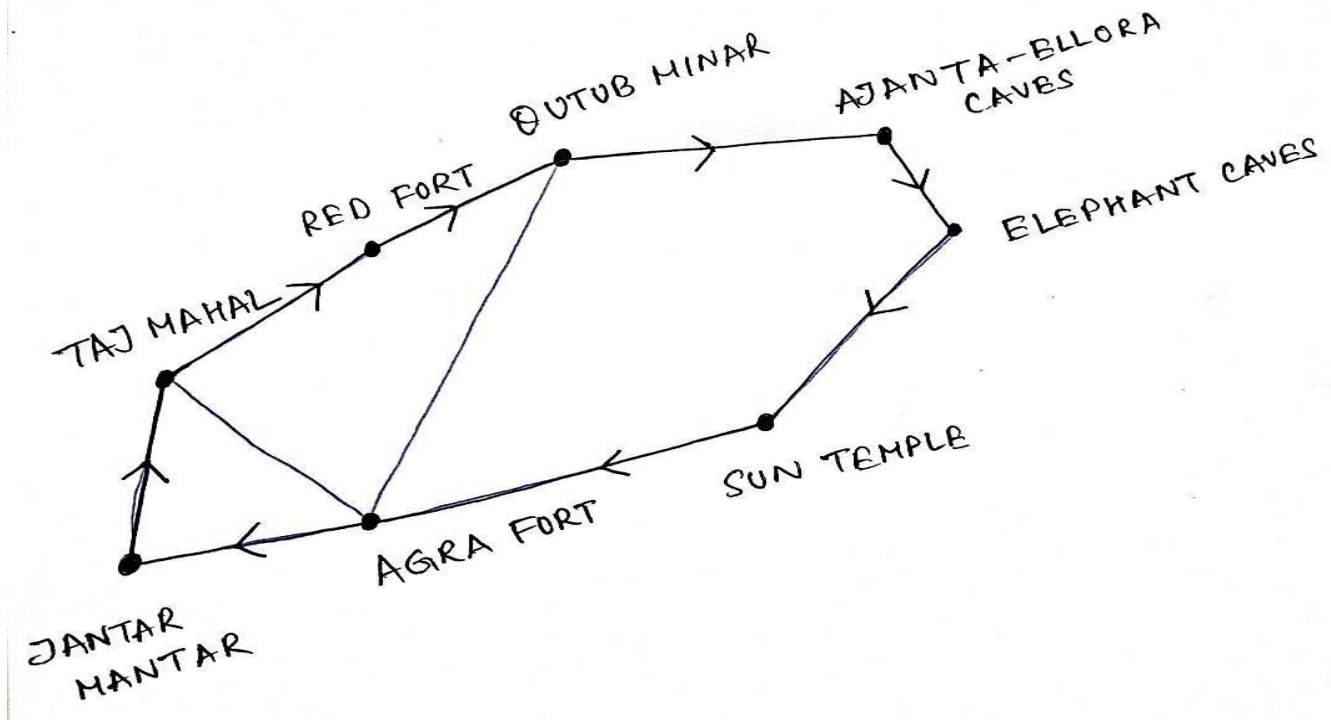
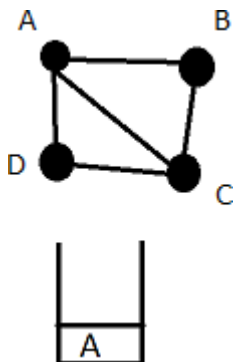


Fig 5.1 Hamilton Cycle

The route depicted starting from Taj Mahal and ending in there is an example of "Hamilton Cycle".

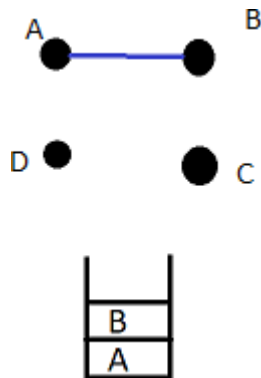
Given a graph G , we need to find the Hamilton Cycle

Step 1: Initialize the array with the starting vertex

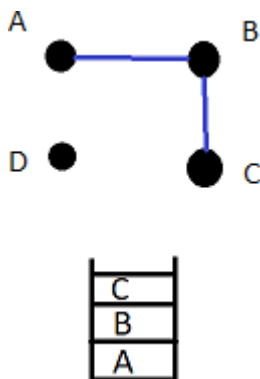


Step 2: Search for adjacent vertex of the topmost element (here it's adjacent element of A

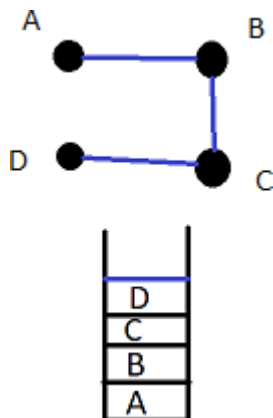
i.e., B, C and D). We start by choosing B and insert in the array.



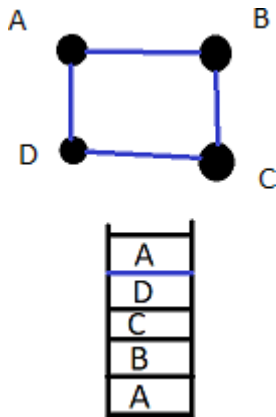
Step 3: The topmost element is now B which is the current vertex. We again search for the adjacent vertex (here C) since C has not been traversed, we add in the list.



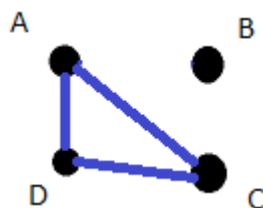
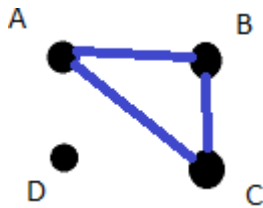
Step 4: The current vertex is now C; we see the adjacent vertex from here. We get D and B, inserting D into the array as B has already been considered.



Step 5: The current vertex is now D since it is a Hamilton Cycle, we need to get back to the starting vertex (which is A). Thus, a Hamilton Cycle of the given graph is **A -> B -> C -> D -> A**.



The Hamilton Path covering all the vertexes. Another Cycle can be $A \rightarrow D \rightarrow C \rightarrow B \rightarrow A$. In another case, if we would have chosen C in Step 2, we would end up getting stuck. We would have to traverse a vertex more than once which is not the property of a *Hamilton Cycle*.



- **Hamilton's "A Voyage Round the World Puzzle"**

Inspired from a game called the "Iconian puzzle", a dodecahedron containing 20 vertices which denotes a city and the edges denotes the routes (as shown in the Fig. (a)). The object of the puzzle was to start at a city and travel along the edges of the dodecahedron, visiting each of other 19 cities exactly once and end back at the first city. The cycle or the circuit thus obtained is (Fig. (b)):

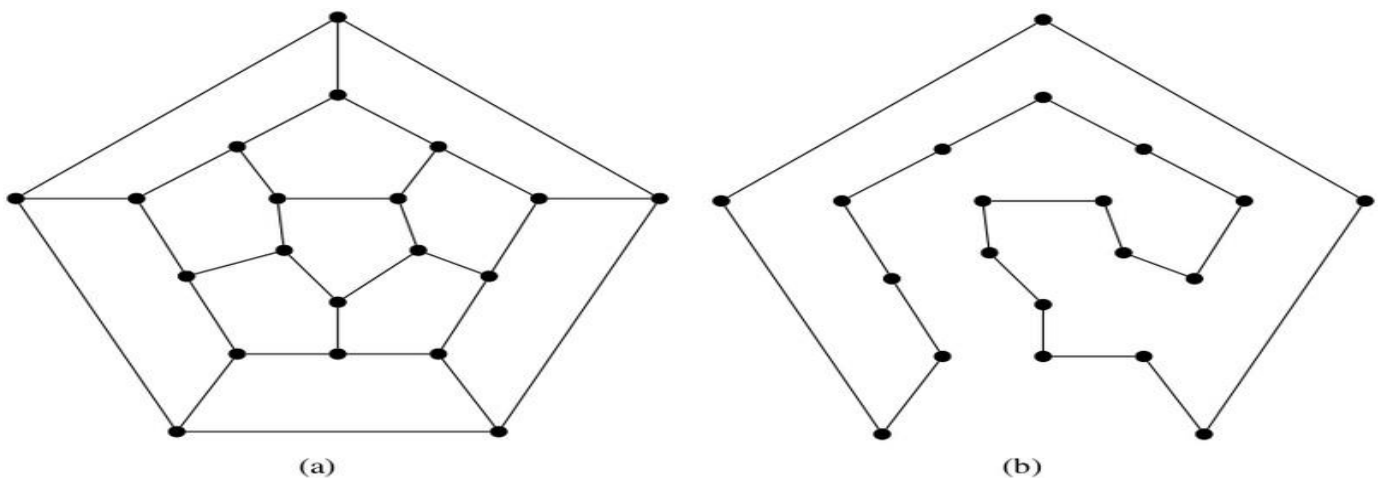


Fig 5.2 A Voyage Round the World Puzzle

CHAPTER 6

CONCLUSION

The conclusion of a Hamiltonian Cycle project would depend on the goals and objectives of the project, as well as the findings and results obtained during the research.

A Hamiltonian Cycle project could involve studying the properties and characteristics of Hamiltonian cycles in graphs, developing algorithms to find Hamiltonian cycles in different types of graphs, or analyzing the complexity of Hamiltonian cycle problems.

In any case, the conclusion of a Hamiltonian Cycle project should summarize the key findings and insights obtained during the project. This could include a discussion of the strengths and limitations of the approach used, any interesting observations or patterns discovered, and suggestions for future research directions.

Additionally, the conclusion could discuss the potential practical applications of Hamiltonian cycles, such as in network optimization, graph theory, or computer science. Ultimately, the conclusion should tie together the various aspects of the project and provide a clear and concise summary of the project's contributions to the field.

CHAPTER 7

FUTURE ENHANCEMENT

There are several possible future enhancements that can be made for a Hamiltonian Cycle project, depending on the specific goals and requirements of the project. Here are some ideas:

1. **Performance optimization:** One potential enhancement is to improve the efficiency of the algorithm used to find Hamiltonian cycles. There are many ways to do this, such as using a more sophisticated graph traversal algorithm, or implementing parallel processing to speed up the computations.
2. **Visualization:** Another possible enhancement is to develop a visualization tool to help users better understand the graphs and cycles. This could involve creating interactive visualizations that allow users to explore the graph and cycle in different ways, or using 3D graphics to make the visualization more engaging.
3. **User interface improvements:** A third enhancement could involve improving the user interface of the application, making it more intuitive and user-friendly. This could include adding features such as drag and drop functionality for adding nodes and edges to the graph, or implementing keyboard shortcuts to make the application more efficient to use.
4. **Integration with other tools:** Another possible enhancement is to integrate the Hamiltonian Cycle project with other tools or platforms. For example, the application could be integrated with a database of graphs, or with a machine learning algorithm that can help predict the likelihood of a graph having a Hamiltonian cycle.
5. **Additional features:** Finally, the project could be enhanced by adding additional features that expand its functionality. For example, the application could be extended to support other types of graph problems, such as finding Eulerian cycles, or it could include a solver for the Traveling Salesman Problem.

CHAPTER 8

APPENDIX

Source Code:

Hamiltonian Cycle Problem

```
#include <iostream>
#include <cstdio>
#include <cstdlib>
#define N 5
using namespace std;
void displaytheSolution(int path[]);
bool isSafe(int n, bool g[N][N], int path[], int pos) {
    if (g[path[pos-1]][n] == 0)
        return false;
    for (int i = 0; i < pos; i++)
        if (path[i] == n)
            return false;
    return true;
}
bool hamiltonianCycle(bool g[N][N], int path[], int pos) {
    //If all vertices are included in Hamiltonian Cycle
    if (pos == N) {
        if (g[path[pos-1]][path[0]] == 1)
            return true;
        else
            return false;
    }
    for (int n = 1; n < N; n++) {
        if (isSafe(n, g, path, pos)) { //Check if this vertex can be added to Hamiltonian Cycle
            path[pos] = n;
            //recur to construct rest of the path
            if (hamiltonianCycle(g, path, pos+1) == true)
                return true;
            path[pos] = -1; //remove vertex if it doesn't lead to the solution
        }
    }
    return false;
}
bool hamCycle(bool g[N][N]) {
    int *path = new int[N];
```

```

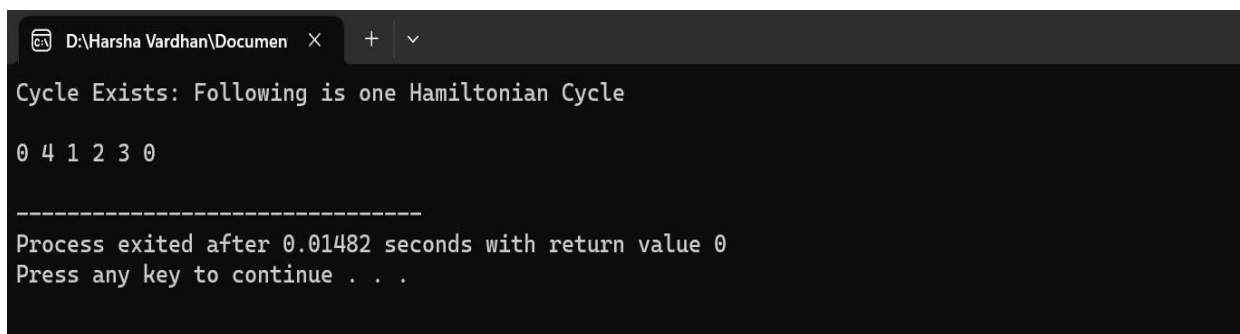
    for (int i = 0; i < N; i++)
        path[i] = -1;
    path[0] = 0;
    if (hamiltonianCycle(g, path, 1) == false) {
        cout<<"\nCycle does not exist"<<endl;
        return false;
    }
    displaytheSolution(path);
    return true;
}

void displaytheSolution(int p[]) {
    cout<<"Cycle Exists:";
    cout<<" Following is one Hamiltonian Cycle \n"<<endl;
    for (int i = 0; i < N; i++)
        cout<<p[i]<<" ";
    cout<<p[0]<<endl;
}

int main() {
    bool g[N][N] = {{0, 1, 0, 1, 1},
                    {0, 0, 1, 1, 0},
                    {0, 1, 0, 1, 1},
                    {1, 1, 1, 0, 1},
                    {0, 1, 1, 0, 0},
                    };
    hamCycle(g);
    return 0;
}

```

Output:



The screenshot shows a terminal window with a dark background. The title bar at the top indicates the file path 'D:\Harsha Vardhan\Documen' and has standard window controls. The output text is as follows:

```

Cycle Exists: Following is one Hamiltonian Cycle

0 4 1 2 3 0

-----
Process exited after 0.01482 seconds with return value 0
Press any key to continue . . .

```

REFERENCES

1. "Hamiltonian cycle problem: a survey" by M. R. Garey and D. S. Johnson, published in the Journal of the ACM in 1979.
2. "The Hamiltonian Cycle Problem: A Survey and Comparative Study" by M. R. Garey and R. L. Graham, published in the SIAM Journal on Computing in 1977.
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5. "Hamiltonian cycle and traveling salesman problem: a review" by J. X. Wu, H. Liu, and Y. L. Wang, published in the Journal of Zhejiang University SCIENCE C in 2011.