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Bsee 19047

$$\text{Q1 } x(t) = \begin{cases} 1.5 & 0 \leq t < 1 \\ -1.5 & 1 \leq t < 2 \end{cases} \quad \omega_0 = \pi \quad T = \frac{2\pi}{\omega_0} = 2 \quad \omega = \frac{2\pi}{T}$$

$$a_k = \frac{1}{T} \int_0^T x(t) e^{-jk\omega t} dt$$

$$= \frac{1}{2} \int_0^1 1.5 e^{-jk\pi t} dt - \frac{1}{2} \int_1^2 1.5 e^{-jk\pi t} dt$$

$$= \frac{1}{2} (1.5) \frac{e^{-jk\pi t}}{-jk\pi} \Big|_0^1 - \frac{1}{2} (1.5) \frac{e^{-jk\pi t}}{-jk\pi} \Big|_1^2$$

$$= \frac{1.5}{2} \frac{e^{-jk\pi} - 1}{-jk\pi} - \frac{1.5}{2} \frac{e^{-2jk\pi} - e^{-jk\pi}}{-jk\pi}$$

$$a_k = \frac{3}{2k\pi j} (1 - e^{-jk\pi}) \Rightarrow \frac{3}{k\pi} e^{-jk(\pi/2)} \sin\left(\frac{k\pi}{2}\right) = a_k$$

$$a_0 = \frac{1}{2} \int_0^1 1.5 dt - \frac{1}{2} \int_1^2 1.5 dt = 0$$

Q: - 2 $x(t) = e^{-3t} \sin 2t$

solve

$$x(j\omega) = \int_{-\infty}^{\infty} x(t) e^{-j\omega t} dt$$

$$x(j\omega) = \int_{-\infty}^{\infty} (e^{-3t} \sin 2t) e^{-j\omega t} dt$$

$$= \int (\sin 2t) e^{t(-3-j\omega)}$$

$$= \frac{1/2j}{3-2j+j\omega} - \frac{1/2j}{3+2j-j\omega}$$

$$X(j\omega) = \frac{2}{(3+2j)^2 + 2^2} = \frac{2}{4+9+4j-4} = \frac{2}{9+4j}$$