

# Rafay Amir

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## Signals & Systems

### Assignment 1

Q:- 1

$$x(t) = 2 \cos(10t+1) - \sin(4t-1)$$

Period of  $\cos x$  and  $\sin x = 2\pi$

$$\cos(10t+1) = \frac{2\pi}{10}$$

$$= \frac{\pi}{5}$$

$$\sin(4t-1) = \frac{2\pi}{4}$$

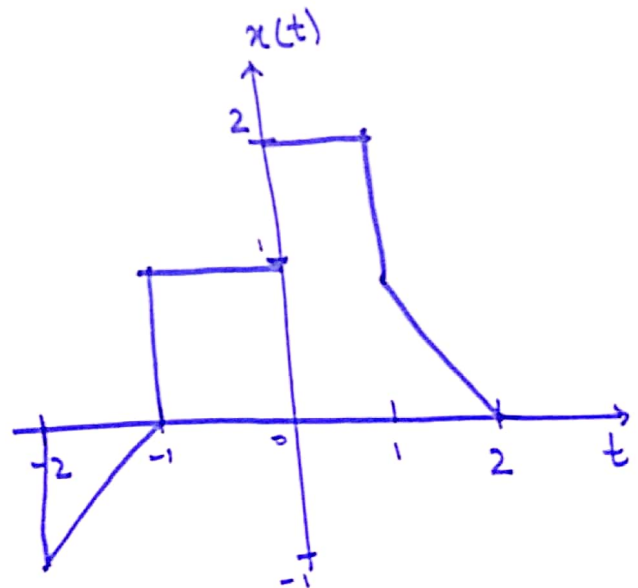
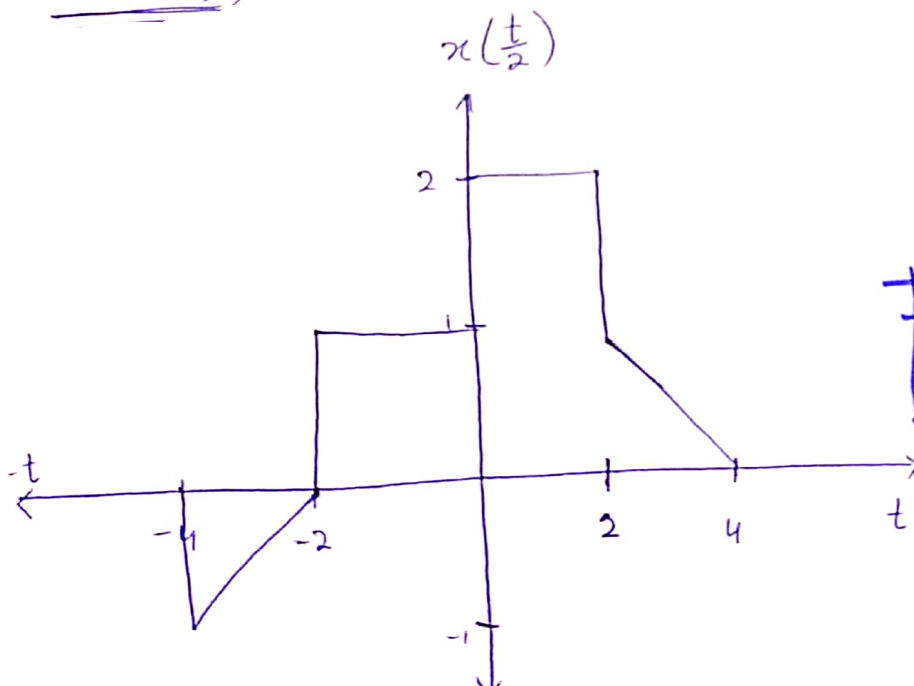
$$= \frac{\pi}{2}$$

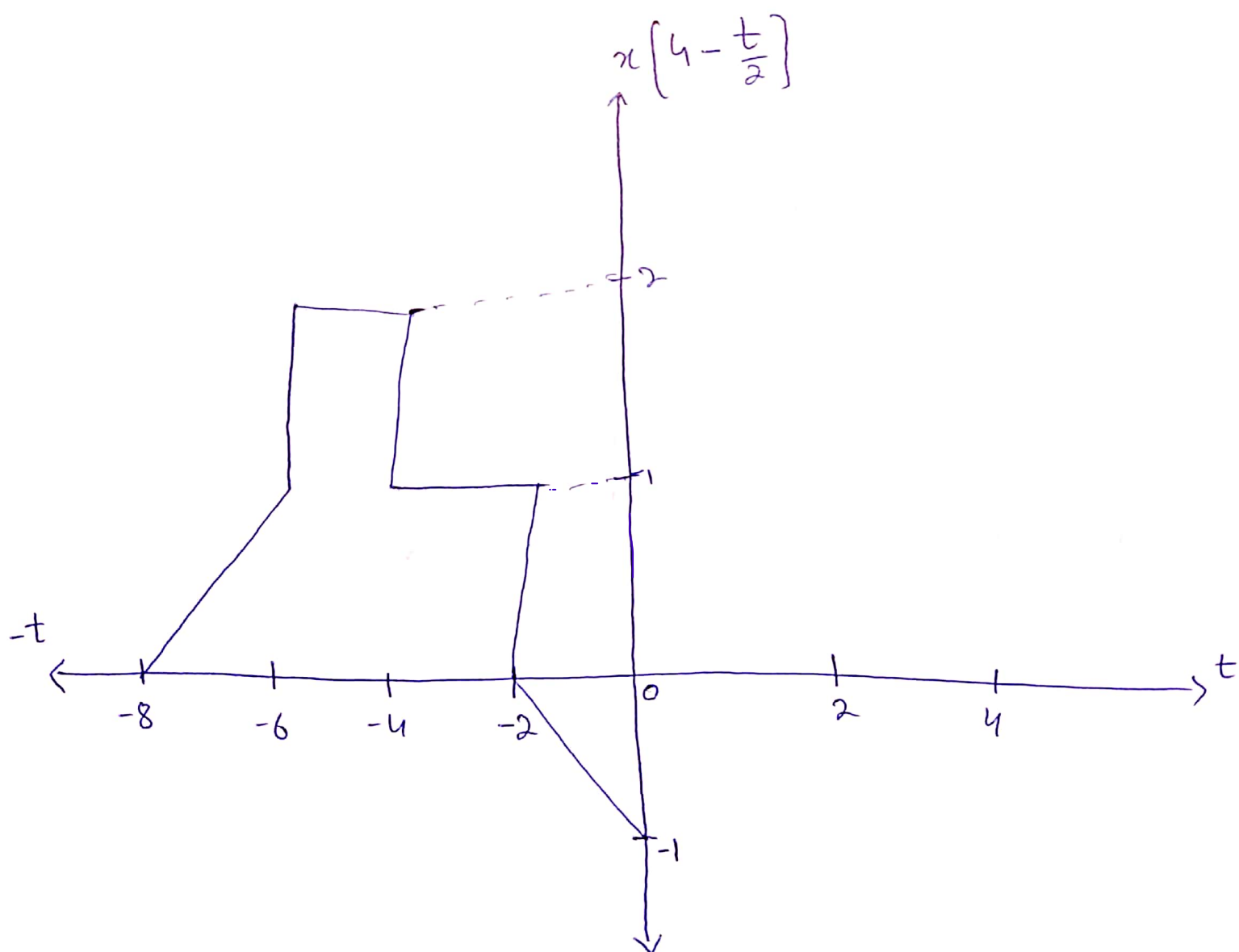
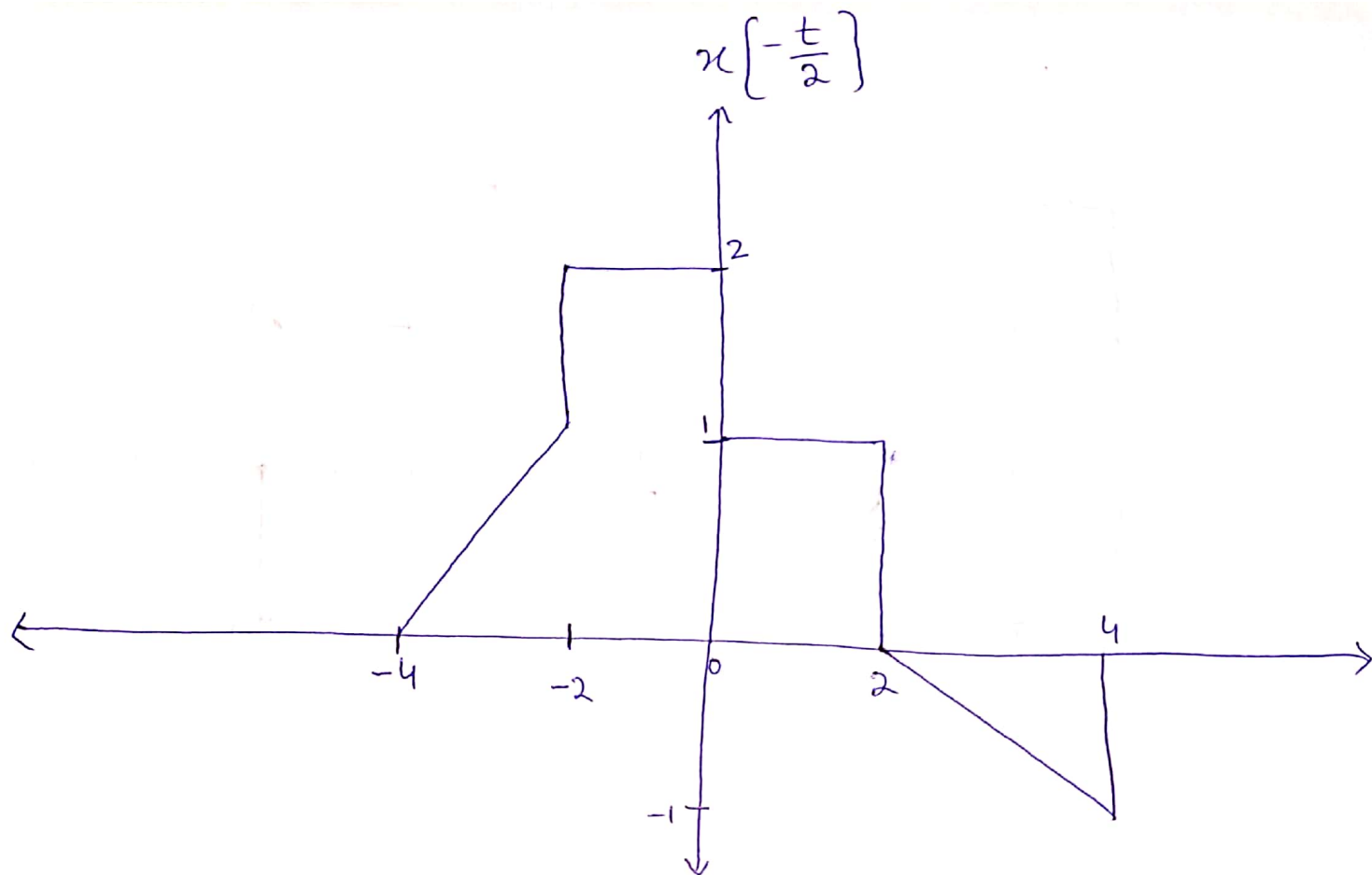
$$\text{LCM of } \frac{\pi}{5} \text{ and } \frac{\pi}{2} = \frac{2\pi}{10} + \frac{5\pi}{10} = \frac{7\pi}{10}$$

Here  $\pi = \pi$  is the LCM of both periods then the combined period of the given function is  $(\pi)$

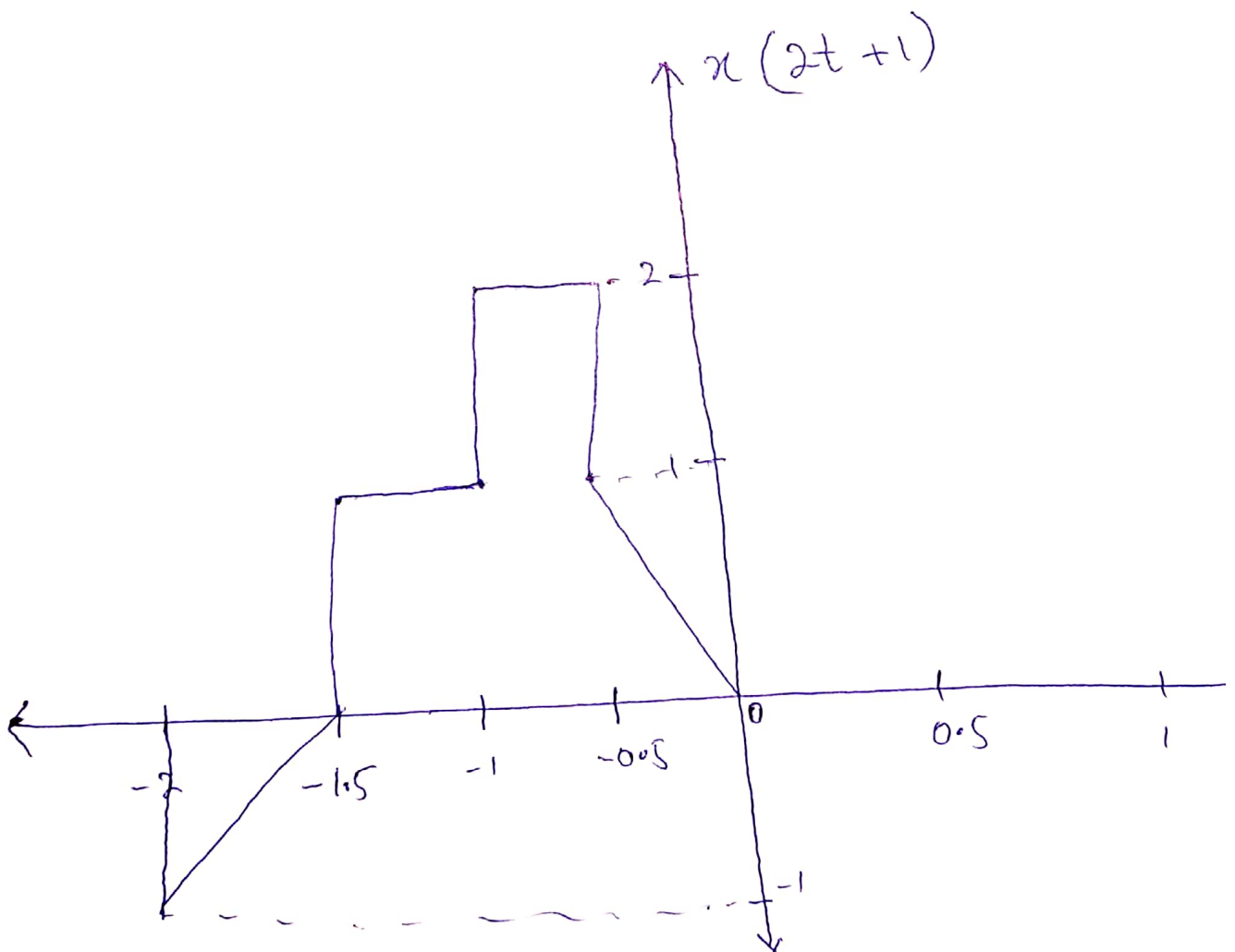
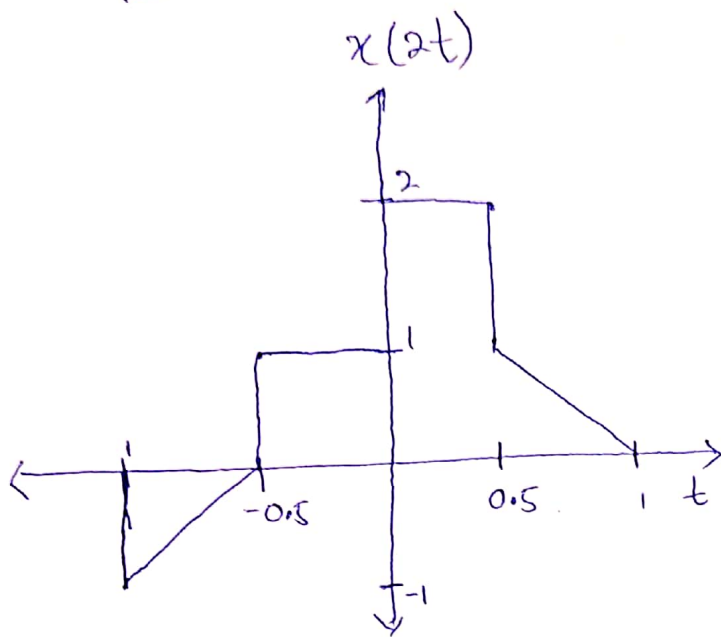
Q:- 2

$$x\left(4 - \frac{t}{2}\right)$$





$x(2t+1)$



Q: 3

$$x(t), y_1(t) = x(2t) \quad , \quad y_2(t) = x(t/2)$$

- ① It is true that if  $x(t)$  is periodic, then  $y_1(t)$  is periodic because  $y_1(t)$  is nothing else but the frequency changed version of the function  $x(t)$ . Here  $y_1(t)$  has half the time period of  $x(t)$  and double the frequency of  $x(t)$ .
- ② It is also true that if  $y_1(t)$  is periodic then  $x(t)$  is periodic while there is a difference between the frequency and time period of these two signals  $x(t)$  and  $y_1(t)$  - period of  $y_1(t) = 2t$  means that the signal  $x(t)$  will complete its duration in double the time of  $y_1(t)$ .
- ③ The statement is still true, if  $x(t)$  is periodic then  $y_2(t)$  will also be periodic with the time period of double the period of  $x(t)$  and half the frequency of  $x(t)$ .
- ④ If  $y_2(t)$  is periodic, then  $x(t)$  will also be periodic while there will be a difference in time period and frequency of both signals -  $y_2(t)$  will be having double the time period and half the frequency as compared to the signal  $x(t)$ .