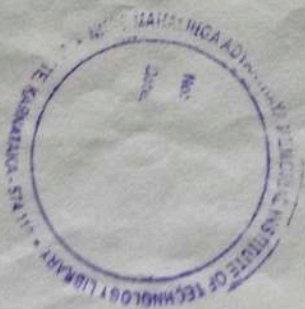


- 2 c) Obtain the reduction formula for  $\int \cos^n x dx$ . Hence
- 3 evaluate  $\int_0^{\frac{\pi}{2}} \cos^n x dx$ .
- 7 L2 5 1
- a) i) Evaluate  $\int_0^{\infty} x^6 e^{-x} dx$  using Gamma function
- ii) Evaluate  $\int_0^1 x^3 (1-x)^2 dx$  using Beta and Gamma functions.
- 6 L1 5 1
- 3 b) Find the volume of the solid generated by revolving the cardioid
- $r = a (1 + \cos \theta)$  about the initial line
- 7 L2 5 2
- 3 c) Find the surface area of the solid generated by revolving the
- astroid  $x = a \sin^3 t$ ,  $y = a \cos^3 t$  about the x-axis
- 7 L2 5 1
- 3 Bloom's Taxonomy, L\* Level: CO\* Course Outcome; PO\* Program Outcome

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- c) Obtain the Maclaurin's expansion of  $\log(1+x)$  upto three non-vanishing terms.

## Unit - III

5. a) Find the extreme values of  $u = x^2 + y^2 + 12x - 6$   
 b) If  $u$  is a homogeneous function of degree  $n$  in  $x$  and  $y$ , then

prove that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = nu$

ii) If  $U = \log \left( \frac{x^4 + y^4}{x+y} \right)$  then prove that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 3$

- c) If  $U = e^x \sin(yz)$  where  $x=t^2, y=t-1, z=\frac{1}{t}$ , find  $\frac{du}{dt}$  at  $t=2$

6. a) Find the directional derivative of  $\phi = x^2yz + 4xz^2$  at the point  $(1, 2, -1)$  in the direction of vector  $2i - j - 2k$

- b) Find the angle between the surfaces  $x^2 + y^2 + z^2 = 5$  and  $z = x^2 + y^2 + 1$  at  $(0, 1, 2)$

- c) Establish the following identities:

i)  $\nabla \cdot \nabla \phi = \nabla^2 \phi$  ii)  $\nabla \cdot (\nabla \times \vec{F}) = 0$

## Unit - IV

7. a) Evaluate  $\int_0^1 \int_0^2 \int_1^2 x^2 yz \, dx \, dy \, dz$

- b) Change the order of integration and hence evaluate

$\int_0^1 \int_{\sqrt{1-x^2}}^{\sqrt{1-x^2}} y^2 \, dy \, dx$

- c) Find the area of the Cardioid  $r = a(1 + \cos \theta)$ .

8. a) Evaluate  $\int_0^1 \int_0^2 e^{x^2} \, dy \, dx$

- b) Show that the area between the parabolas

$y^2 = 4ax$  and  $x^2 = 4ay$  is  $\frac{16}{3}a^2$

- c) By changing to polar co-ordinates evaluate

$\int_0^{\sqrt{a^2-y^2}} \int_0^{\sqrt{a^2-x^2}} (x^2 + y^2) \, dx \, dy$

## Unit - V

9. a) Evaluate  $\int_0^{\pi} \frac{1}{(1+x^2)^2} \, dx$

- b) Prove that  $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$  with usual notations.



**NMAM INSTITUTE OF TECHNOLOGY, NITTE**  
(An Autonomous Institution affiliated to VTU, Belagavi)

**First Semester B.E. (Credit System) Degree Examinations**  
**Supplementary Examinations – July 2019**

Max. Marks: 100

**Note: Answer Five full questions choosing One full question from each Unit**

a) Find the rank of the following matrix using elementary row

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13

$$x + y + z = 3$$

7 L2 1 2

$$\begin{bmatrix} 1 & 4 \\ 3 & 2 \end{bmatrix}$$

7111

$$y_1 = x_1 + x_2 + 3x_3; \quad y_2 = x_1 + 3x_2 - 3x_3; \quad y_3 = -2x_1 - 4x_2 - 4x_3$$

741

7 L2 1

i) State Comparison test

ii) Test the convergence of the following series

$$\frac{1}{2} + \frac{2}{3} + \frac{3}{8}$$
$$\sum_{n=0}^{\infty} \left( \frac{nx}{n+1} \right) x > 0$$

4  
5  
6

227

6. a) If  $u = f\left(\frac{y-x}{xy}, \frac{z-x}{xz}\right)$ , show that  $x^2 \frac{\partial u}{\partial x} + y^2 \frac{\partial u}{\partial y} + z^2 \frac{\partial u}{\partial z} = 0$
- b) Expand  $x^2y + 3y - 2$  at the point  $(1, -2)$  using Taylor's theorem upto terms of 2<sup>nd</sup> degree.
- c) The period of a simple pendulum is  $T = 2\pi\sqrt{l/g}$ . Find the maximum error in T due to the possible error upto 1% in l and 2.5% in g.

6 L1 4  
7 L2 3

Fir

## Unit - IV

tion: 3 Hours

Note: Answer

7. a) Evaluate  $\int_0^1 \int_x^{\sqrt{x}} (x^3 + y^2) dx dy$
- b) Find the volume of the sphere  $x^2 + y^2 + z^2 = a^2$  using triple integral.
- c) Evaluate  $\int_0^\infty \int_0^\infty e^{-(x^2+y^2)} dx dy$  by changing the polar coordinates.
8. a) Evaluate  $\int_{-c}^c \int_{-b}^b \int_{-a}^a (x^2 + y^2 + z^2) dx dy dz$
- b) Find the area of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  in the 1<sup>st</sup> quadrant.
- c) Evaluate  $\int_0^1 \int_x^{\sqrt{x}} xy dy dx$  by changing the order of integration.

6 L1 4  
7 L2 4  
7 L1 4  
6 L1 4  
7 L2 4  
7 L1 4

- a) Find the re  
transforma  
 $\begin{bmatrix} 1 & 2 \\ 2 & 1 \\ 3 & 2 \\ 0 & 1 \end{bmatrix}$
- b) Test for co  
by Gauss  
 $\begin{bmatrix} 1 & 4 \\ 3 & 2 \end{bmatrix}$
- c) Find the ei  
 $\begin{bmatrix} 1 & 4 \\ 3 & 2 \end{bmatrix}$

## Unit - V

9. a) Find the volume of the solid generated by revolving one arch of the cycloid  $x = a(\theta + \sin \theta)$ ,  $y = a(1 + \cos \theta)$  about the X-axis.
- b) Prove that  $\beta(m, n) = \frac{\sqrt{\pi} \Gamma(n)}{\sqrt{m} \Gamma(m)}$  with usual notations.
- c) Obtain the reduction formula for  $\int \sin^n x dx$  and hence evaluate  $\int_0^{\pi/2} \sin^n x dx$ .
10. a) Prove that  $\int_0^{\pi/2} \frac{d\theta}{\sqrt{\sin \theta}} \int_0^{\pi/2} \sqrt{\sin \theta} d\theta = \pi$
- b) Evaluate  $\int_0^a x^4 \sqrt{a^2 - x^2} dx$  by using Beta & Gamma functions.
- c) Find the surface area of the solid generated by the revolution of the cardioid  $r = a(1 - \cos \theta)$  about the initial line.

6 L1 5a)  
7 L1 5b)  
7 L1 5c)  
6 L1 5  
7 L1 5  
7 L1 5

BT\* Bloom's Taxonomy, L\* Level; CO\* Course Outcome, PO\* Program Outcome

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- a) State an  
in  $[0, \pi]$
- b) State Ca  
 $\frac{1}{1+\sqrt{2}}$
- c) Obtain T  
degree t



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# NIMAM INSTITUTE OF TECHNOLOGY, NITTE

(An Autonomous Institution affiliated to VTU, Belagavi)  
**First Semester B.E. (Credit System) Degree Examinations**

November - December 2019

19MA101 - ENGINEERING MATHEMATICS - I

Max. Marks: 100

Duration: 3 Hours

Note: Answer Five full questions choosing One full question from each Unit.

## Unit - I

Marks BT\* CO\* PO\*

1. a) Find the rank of the matrix using elementary row transformation.

$$\begin{bmatrix} 1 & 1 & 1 & 6 \\ 1 & -1 & 2 & 5 \\ 3 & 1 & 1 & 8 \\ 2 & -2 & 3 & 7 \end{bmatrix}$$

6 L\*1 1 1

- b) Test for consistency and solve the system of equations by Gauss elimination method.

$$2x + y + 4z = 12, \quad 4x + 11y - z = 33, \quad 8x - 3y + 2z = 20.$$

7 L3 1 2

- c) Diagonalize the matrix

$$\begin{bmatrix} -19 & 7 \\ -42 & 16 \end{bmatrix}$$

7 L2 1 2

2. a) Find the eigen values and eigen vectors of the matrix

$$\begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$$

7 L3 1 2

- b) Show that the transformation  $y_1 = 2x_1 + x_2 + x_3$ ,  $y_2 = x_1 + x_2 + 2x_3$ ,  $y_3 = x_1 - 2x_3$  is regular. Find the inverse transformation.

7 L1 1 1

- c) Reduce the quadratic form  $3x^2 + 5y^2 + 3z^2 - 2yz + 2zx - 2xy$  to the canonical form.

6 L1 1 1

## Unit - II

3. a) i) State D'Alembert's ratio test.

ii) Test the convergence of the series  $1 + \frac{2!}{2z} + \frac{3!}{3z^2} + \dots \infty$

6 L3 2 1

- b) State and prove Lagrange's mean value theorem.

7 L1 2 1

- c) Expand  $\log_e(1+x)$  by using Maclaurin's series upto 4<sup>th</sup> degree terms.

7 L1 2 1

4. a) Verify Cauchy's mean value theorem for the functions

$$f(x) = e^x, g(x) = e^{-x} \text{ in } [a, b]$$

6 L1 2 2

- b) Expand  $\tan^{-1}x$  at  $x = 1$  upto 3<sup>rd</sup> degree term.

7 L1 2 1

- c) Discuss the convergence of the series  $\frac{x}{1.3} + \frac{x^2}{3.5} + \frac{x^3}{5.7} + \dots$

7 L3 2

## Unit - III

5. a) If  $\tan u = \frac{x^3+y^3}{x-y}$ , prove that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u$

6 L1 3 1

- b) If  $u = x + 3y^2$ ,  $v = 4x^2yz$ ,  $w = 2z^2 - xy$ . Then find

7 L1 3 1

- c) A rectangular box open at the top is to have a volume of 32 cubic units. What must be the dimensions of the box so that the total surface area of the box is a minimum?

7 L3 3 2

P.T.O.