

21MA101

b) State D'Alembert's ratio test. Test for the convergence of the series

$$\left(\frac{1}{3}\right)^2 + \left(\frac{1.2}{3.5}\right)^2 + \left(\frac{1.2.3}{3.5.7}\right)^2 + \dots \infty.$$

4. a) Test for the convergence of the series

$$1 + \frac{1}{2^2} + \frac{2^2}{3^3} + \frac{3^3}{4^4} + \dots \infty.$$

b) State Cauchy's root test. Test for the convergence of the series

$$\sum \left(1 - \frac{3}{n}\right)^{n^2}.$$

BT\* Bloom's Taxonomy, L\* Level; CO\* Course Outcome; PO\* Program Outcome

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ations: J- T)

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# NMAM INSTITUTE OF TECHNOLOGY, NITTE

(An Autonomous Institution affiliated to VTU, Belagavi)

I Sem B.E. (Credit System) Mid Semester Examinations - I, February 2022

21MA101 – ENGINEERING MATHEMATICS - I

ation: 1 Hour

Max. Marks: 20

Note: Answer any **One** full question from **each Unit**.

## Unit – I

Marks BT\* CO\* PO\*

- a) Find the eigen values and corresponding eigen vectors of the matrix

$$\begin{bmatrix} 1 & 0 & 0 \\ 1 & 2 & 0 \\ 2 & 2 & 3 \end{bmatrix}$$

6 L\*2 1 2

- b) Define rank of a matrix. Also find the rank of the following matrix by elementary row transformation.

$$\begin{bmatrix} 1 & 3 & 4 & -2 \\ 3 & -1 & 2 & 0 \\ 2 & 1 & 3 & -1 \\ 4 & -3 & 1 & 1 \end{bmatrix}$$

4 L1 1 1

- a) Test for consistency and hence solve the following system of equations by Gauss elimination method.

$$x - 3y + 2z = 1$$

$$3x + y + z = 2$$

$$7x - y + 4z = 5$$

5 L2 1 2

- b) Solve the following system of equations by Gauss- Seidel iteration method.

$$27x + 6y - z = 85$$

$$6x + 15y + 2z = 72$$

$$x + y + 54z = 110$$

Start with  $x^{(0)} = y^{(0)} = z^{(0)} = 0$  and carry out three iterations.

5 L1 1 1

## Unit – II

- a) Using the Rayleigh's power method find the largest eigen value and

the corresponding eigen vector of the matrix  $\begin{bmatrix} 4 & 1 & -1 \\ 2 & 3 & -1 \\ -2 & 1 & 5 \end{bmatrix}$ . Take

the initial approximation to the eigen vector as  $[1 \ 0.8 \ 0.8]^T$  and carry out 4 iterations.

5 L2 1 2

P.T.O.