

1) BGW protocol.

$$p = 11, \quad S_1 = 3 + 5x \quad t = 2$$

$$S_2 = 4 + 2x$$

$$f(x) = S_1 * S_2 = 12 + 26x + 10x^2$$

Now

$$\underline{\underline{2t - 1 = 3}}$$

$$f(1) = 4 + 11 = 15$$

$$f(2) = 104 + 11 = 115$$

$$f(3) = 180 + 11 = 191$$

So,

$$A = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 4 & 9 \end{bmatrix}$$

$$\text{So, } A^{-1} = \begin{bmatrix} 3 & -5/2 & 1/2 \\ -3 & 4 & -1 \\ 1 & -3/2 & 1/2 \end{bmatrix}$$

$$h_1(x) = 8 * 6 + x = 4 + x$$

Shares $\rightarrow \{5, 6, 7\}$

$$h_2(x) = 13 * 8 + x = 5 + x$$

Shares $\rightarrow \{6, 7, 8\}$

$$h_3(x) = 18 * 10 + x = 4 + x$$

Shares $\rightarrow \{5, 6, 7\}$

$$h(n) = \varphi_1 h_1(n) + \varphi_2 h_2(n) + \varphi_3 h_3(n)$$

$$h(1) = 3 \times 5 + 6(-3) + 5$$

$$= 2$$

$$h(2) = 3 \times 6 + (-3) \times 7 + 6$$

$$= 3$$

So, we get (1, 2) & (2, 3)

Using Lagrange theorem,

$$\text{Sol}^n = \frac{2 \times -2}{(1-2)} + \frac{3(-1)}{(2-1)}$$

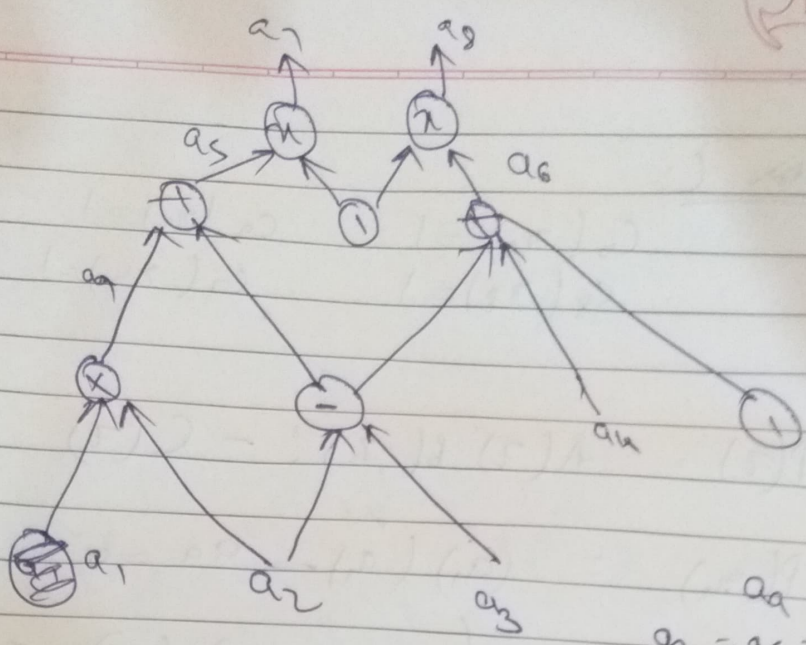
$$= 4 + (-3)$$

$$= \boxed{1}$$

$$S_1 S_2 = 12 \times 11 = \boxed{1}$$

\therefore The protocol was demonstrated and verified.

2. >



$$a_5 = a_1 a_2$$

$$a_7 = a_5 = a_1 a_2 + a_2 - a_3$$

$$a_8 = a_6 = a_2 - a_3 + a_4$$

3 AND nodes : π_1, π_8, π_9
 \uparrow : a_1, a_2, a_3, a_4] assignment

$$I(\pi) = \deg(3)$$

$$= (\pi - \pi_1)(\pi - \pi_8)(\pi - \pi_9) \rightarrow 1$$

for A:

$$A_0(\pi_8) = 1 \quad A_9(\pi_7) = 1$$

$$A_1(\pi_8) = 1$$

$$A_2(\pi_7) = 1$$

$$A_3(\pi_9) = -1$$

for B:

$$B_0(\pi_7) = 1$$

$$B_2(\pi_8) = 1$$

$$B_3(\pi_8) = -1$$

$$B_4(\pi_8) = 1$$

For C :

$$C_0(\pi_8) = 1$$

$$C_9(\pi_7) = 1$$

$$C_8(\pi_8) = 1$$

$$C_7(\pi_7) = 1$$

$$P(z) = A(z) B(z) - C(z)$$

$$P(\pi_9) = (a_1)(a_9) - a_9 = 0$$

$$P(\pi_7) = (a_1 - a_7 + a_9)(1) - a_7 = 0$$

$$P(\pi_8) = (1)(a_2 - a_8 + a_9) - (1 + a_8) = 0$$

we use lagrange now to find $P(z)$

$$z(z) = (z - \pi_7)(z - \pi_8)(z - \pi_9)$$

4.7 pragma solidity 0.6.8;

```
import "@openzeppelin/contracts/math/SafeMath.sol";
import " " " " Interfaces/ IItem.sol";
// Interface has price stock & name
```

```

Contract OnlineMarket {
    using SafeMath for uint256;
    address owner;
    Item public item;
address
    struct Item {
        uint id;
        string name;
    }
}

```

1) Mapping between item and price
mapping (Item \Rightarrow unit) price vob;
2) mapping between item & stock
mapping (Item \Rightarrow unit) stock vob;
mapping (address \Rightarrow unit) paid by user;

Function OnlineMarket () {
 owner = msg.Sender;
}

```

function Price (wint NewPrice, wint id, string
                name, wint stocknum)
// set new price for item first check num
require (msg.sender == owner);
priceVal (Item (id, name)) = NewPrice

```

```

    stockVal (Item (id, name)) = stockVal;
}

```

b)

```

function Buy (int quant, int id, string name)
{
    require (quant * item (id, name) > msg.value;
    paidBy User (msg.sender) += msg.value;
    stockVal (Item (id, name)) = quant;
    owner.send (msg.value);
}
require (quant <= Item (id, name));

```

~~function Buy (int quant, string name)~~

c) A possible attack that can take place is that there can be simultaneous ordering by two people due to same time ordering by two people.

- Payable function can be used to exploit and void the contracts.

- Reentrance vulnerability is also an issue.

$$3.7 \quad N = 5 \times 11 = 55$$

$$G = \{a: x^2 = a \pmod{N}\}$$

when that set $(G, * \pmod{N})$ is cyclic group.

Now, we need perfect squares, so, it is quadratic residue.

~~$$x^2 \in \{1, 4, 9, 16, 25, 36, 49\}$$~~

$$x^2 \in \{1, 4, 9, 16, 25, 36, 49, \dots\}$$

Therefore, we can have 'a' as,

$$a \in \{1, 4, 5, 9, 11, 14, 15, 16, 20, 25, 26, 31, 34, 36, 44, 45, 49\}$$

(\because Done using code)

Hence

$$\text{Cyclic Group } G = \{1, 4, 5, 9, 11, 14, 15, 16, 20, 25, 26, 31, 34, 36, 44, 45, 49\}$$

But, we are unable to find the generator, hence, NO Generator