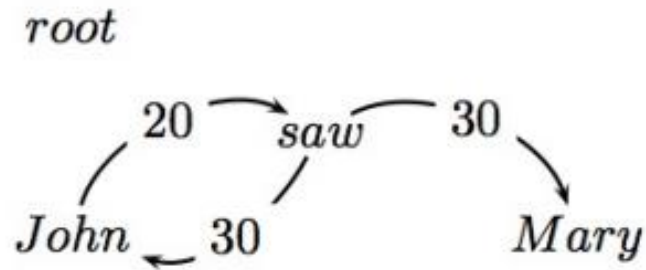
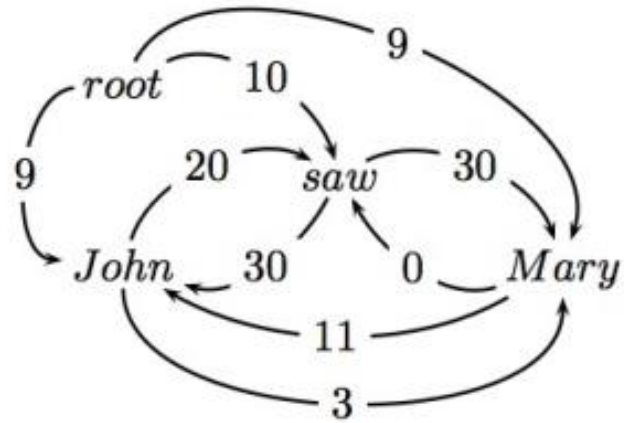


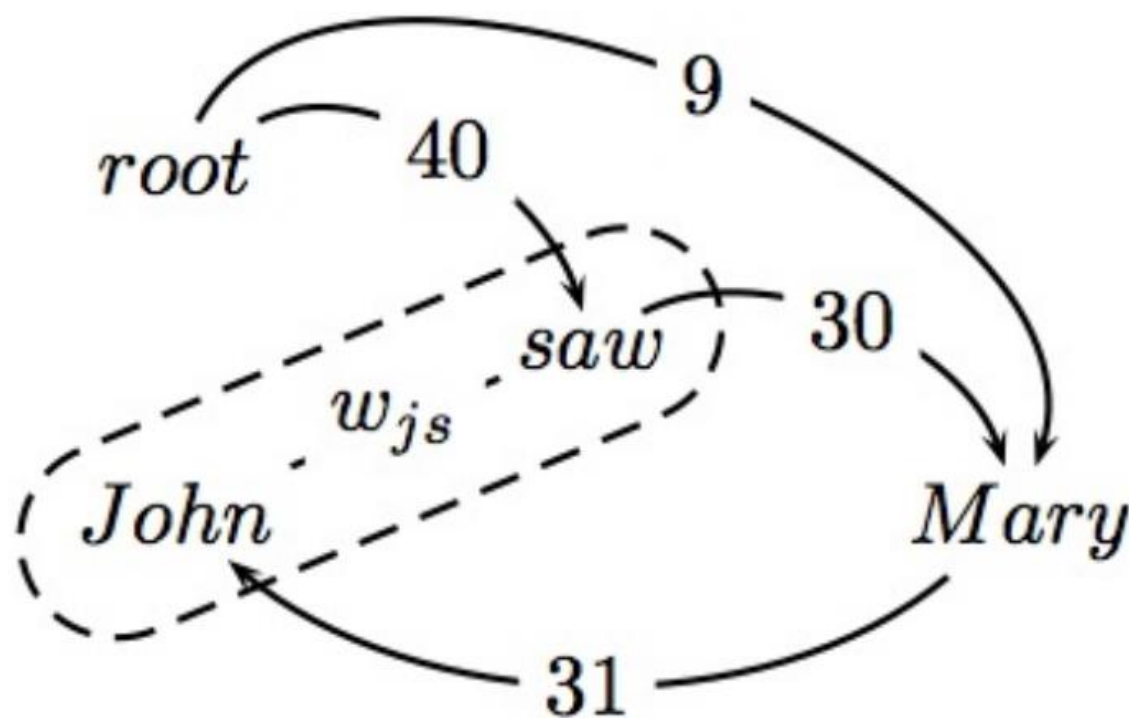


# Chu-Liu-Edmonds

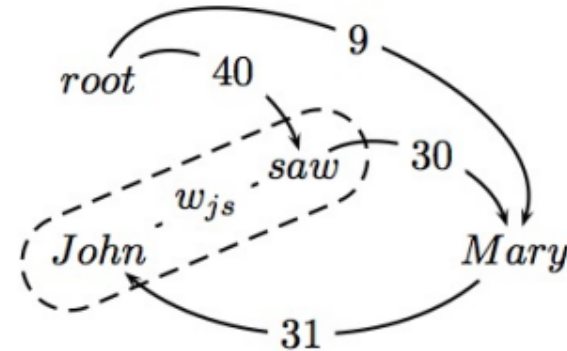
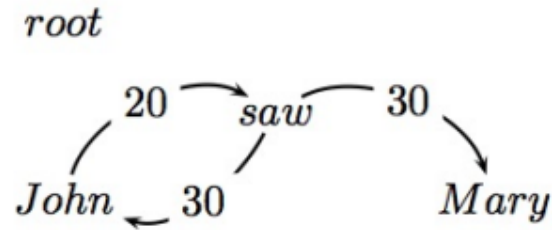
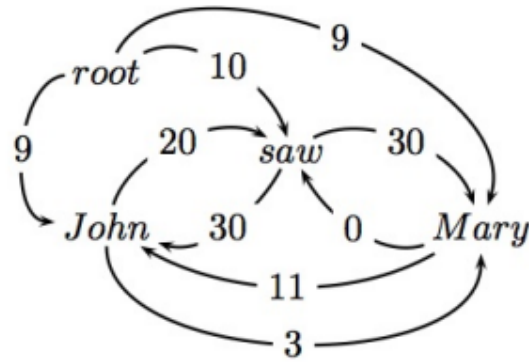


## Chu-Liu-Edmonds

- ▶ If not a tree, identify cycle and contract
- ▶ Recalculate arc weights into and out-of cycle



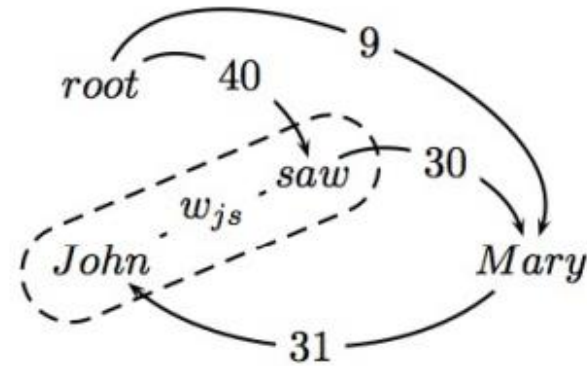
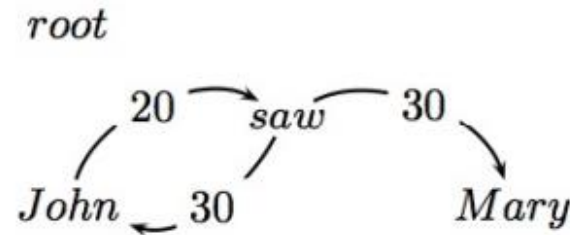
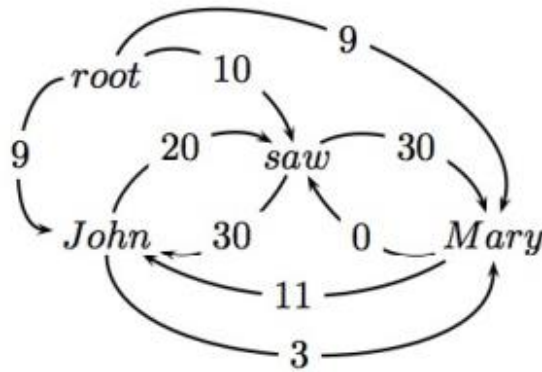
# Chu-Liu-Edmonds



## ► Outgoing arc weights

- Equal to the max of outgoing arc over all vertexes in cycle
- e.g., *John* → *Mary* is 3 and *saw* → *Mary* is 30

# Chu-Liu-Edmonds



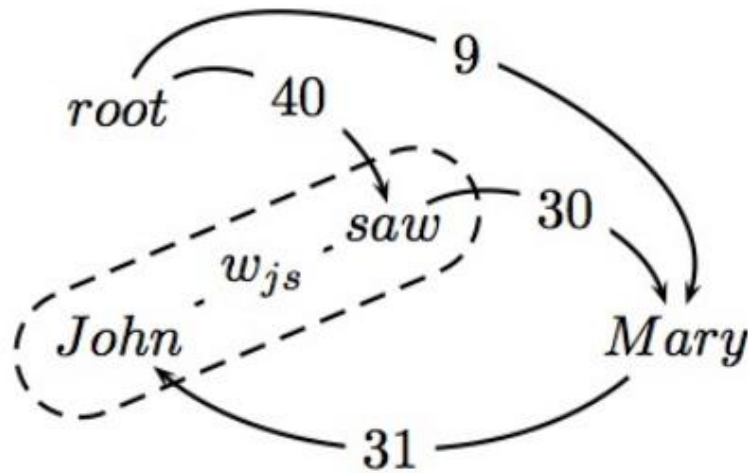
## ► Incoming arc weights

- Equal to the weight of best spanning tree that includes head of incoming arc, and all nodes in cycle
- *root* → *saw* → *John* is 40 (\*\*)
- *root* → *John* → *saw* is 29

# Chu-Liu-Edmonds

## Theorem

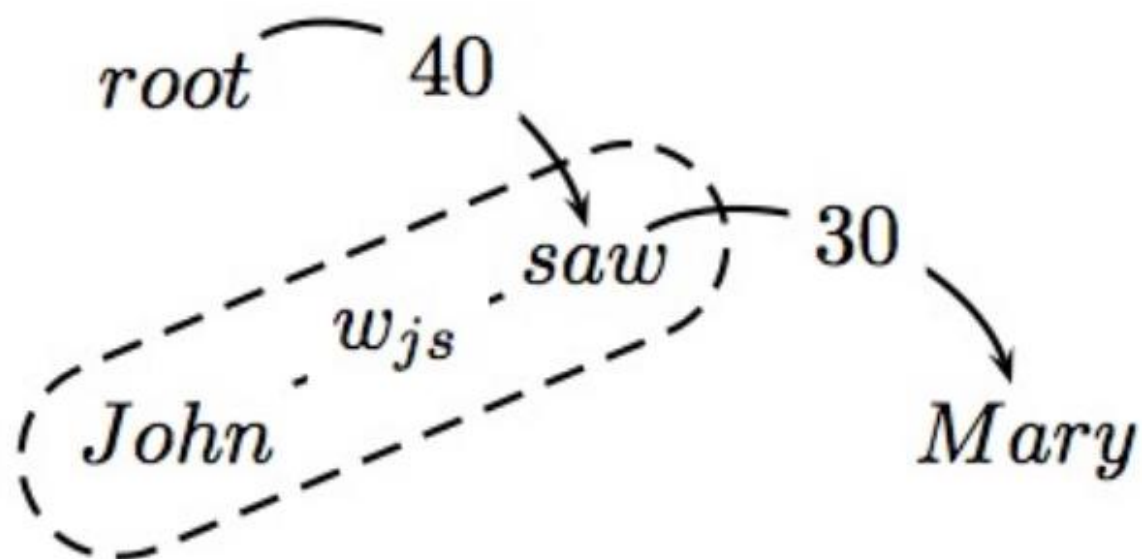
The weight of the MST of this contracted graph is equal to the weight of the MST for the original graph



- Therefore, recursively call algorithm on new graph

# Chu-Liu-Edmonds

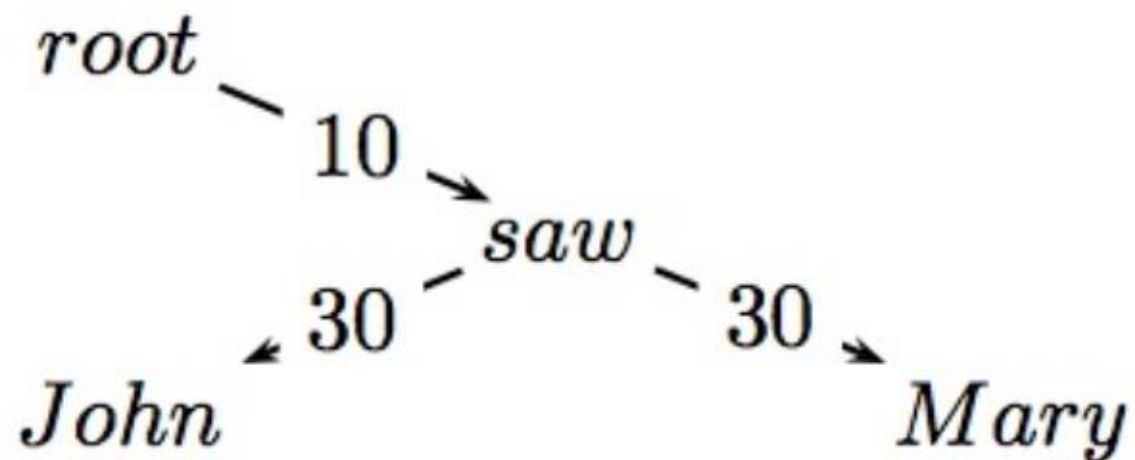
- ▶ This is a tree and the MST for the contracted graph!!



- ▶ Go back up recursive call and reconstruct final graph

# Chu-Liu-Edmonds

- ▶ This is the MST!!





# Learning weights of the graph

- Use training dataset
- Define features
- Step1: Construct a graph with all arcs
- Step2: initialize a weight vector based on number of features,  $w(0)$
- Step3: find feature vector for every arc
- Step 4: find weight of every arc  $w_{ij}(k)$ , by multiplying feature vector of the arc and the weight vector  $w(i)$
- Step5: Apply CLE algo. To find MST  $G'$
- Step6: update the  $w(i+1)=w(i)+f(G_t)-f(G')$
- Step7: Iterate

Suppose you are training MST Parser for dependency and the sentence, “John saw Mary” occurs in the training set. Also, for simplicity, assume that there is only one dependency relation, “rel”. Thus, for every arc from word  $w_i$  to  $w_j$ , your features may be simplified to depend only on words  $w_i$  and  $w_j$  and not on the relation label. Below is the set of features

f 1 :  $\text{pos}(w_i) = \text{Noun}$  and  $\text{pos}(w_j) = \text{Noun}$

f 2 :  $\text{pos}(w_i) = \text{Verb}$  and  $\text{pos}(w_j) = \text{Noun}$

f 3 :  $w_i = \text{Root}$  and  $\text{pos}(w_j) = \text{Verb}$

f 4 :  $w_i = \text{Root}$  and  $\text{pos}(w_j) = \text{Noun}$

f 5 :  $w_i = \text{Root}$  and  $w_j$  occurs at the end of sentence

f 6 :  $w_i$  occurs before  $w_j$  in the sentence

f 7 :  $\text{pos}(w_i) = \text{Noun}$  and  $\text{pos}(w_j) = \text{Verb}$

The feature weights before the start of the iteration are: {3, 20, 15, 12, 1, 10, 20}.

Determine the weights after an iteration over this example.

a) [3, 19, 11, 15, 3, 12, 19]

b) [3, 20, 13, 10, 3, 11, 21]

c) [4, 20, 15, 10, 1, 7, 21]

d) [3, 19, 16, 11, 1, 9, 19]