

Apriori Algorithm

- Goal of any organization is to increase the revenue.

- Organizations began mining data relating to frequently bought items. Market basket analysis is one of the key techniques used by large retailers to uncover associations between items.

Example * customers who purchase bread have a 60% likelihood to also purchase Jam
* customers who buy laptops are more likely to purchase laptop bags as well).

** To find association between different items & products that can be sold together which gives in the right product placement

Ex People who buy bread also tend to buy butter & the marketing team at retail store should target customers ~~with~~ to make them buy a third item suppose eggs.

If a customer buys bread & butter & sees a discount offer on eggs, he will be encouraged to spend more & buy the eggs.

Association Rule Mining

The ARM rule can be taught as an if-then relationship just to elaborate on it

$A \Rightarrow B$

If

then

Two ~~sub~~ elements to this rule first is if & second is then.

if is also known as antecedent this is an item or a group of items present in the itemset.

The later is known as consequent

Association Rule Mining algorithm helps the business to make profit.

ARM is all about building the rules

- If you buy A there is a slight possibility or chance that you may buy B also

- This type of relationship in which we can find relationship b/w these two items is known as single cardinality

Measures Association

- Support
- Confidence

$$\text{Support} = \frac{\text{freq}(A, B)}{N}$$

Support is the frequency of or the combination of item A or B. Its basically the frequency of the items we have bought + combination of the items that we have bought

- To filter the items that have been bought less frequently

Confidence

$$\text{Confidence} = \frac{\text{freq}(A, B)}{\text{freq}(A)}$$

It gives us how often the items A & B occur together given the number of the times A occur.

(3)

$$\text{List} = \frac{\text{support}(A \cup B)}{\text{support}(A) \times \text{support}(B)}$$

List is basically the strength of any rule

Denominator gives the independent support value of $A \& B$. This gives us the independent occurrence probability of $A \& B$.

Denominator of List is more, the occurrence of randomness is more.

Ex Transaction at a local market

TID	Items		
T ₁	A	B	C
T ₂	A	C	D
T ₃	B	C	D
T ₄	A	D	E
T ₅	B	C	E

Rules

1. $A \Rightarrow D$

2. $C \Rightarrow A$

3. $A \Rightarrow C$

4. $B \& C \Rightarrow A$

• A gives D
If a person buys A he is most likely to buy D.

Rule	Support	Confidence	List
$A \Rightarrow D$	2/5	2/3	10/9
$C \Rightarrow A$	2/5	2/4	5/6
$A \Rightarrow C$	2/5	2/3	5/6
$B, C \Rightarrow A$	1/5	1/3	5/9

$$= \frac{2}{5} = \frac{2}{5} \times \frac{5}{9} = \frac{\text{List } A \Rightarrow D}{\frac{\text{Support}(A \cup D)}{\text{Support}(A) \times \text{Support}(D)}}$$

Apriori algorithm uses frequent itemsets to generate association rules. It is based on the concept that a subset of a frequent itemset must also be a frequent itemset.

* A frequent itemset is an itemset whose support value is greater than a threshold value.

Example If A & B is a frequent itemset then A & B should be frequent itemsets individually.

min. support = 2

TID	Items
T ₁	1 3 4
T ₂	2 3 5
T ₃	1 2 3 5
T ₄	2 5
T ₅	1 3 5



C1	support
Itemset	
{1}	3
{2}	3
{3}	4
{4}	1
{5}	4

Itemset of size 2

L1	support
Itemset	
{1}	3
{2}	3
{3}	4
{5}	4



C2	support
Itemset	
{1, 2}	1
{1, 3}	3
{1, 5}	2
{2, 3}	2
{2, 5}	3
{3, 5}	3

<u>L2</u>	
<u>Itemset</u>	<u>Support</u>
$\{1,3\}$	3
$\{1,5\}$	2
$\{2,3\}$	2
$\{2,5\}$	3
$\{3,5\}$	3

<u>C3</u>	
<u>Itemset</u>	<u>Support</u>
$\{1,2,3\}$	X
$\{1,2,5\}$	X
$\{1,3,5\}$	2
$\{2,3,5\}$	2

<u>C3</u>	
<u>Itemset</u>	
$\{1,2,3\}, \{1,2\}, \{1,3\}, \{2,3\}$	
$\{1,2,5\}, \{1,2\}, \{1,5\}, \{2,5\}$	
$\{1,3,5\}, \{1,5\}, \{1,3\}, \{3,5\}$	
$\{2,3,5\}, \{2,3\}, \{2,5\}, \{3,5\}$	

<u>L3</u>	
<u>Itemset</u>	<u>Support</u>
$\{1,3,5\}$	2
$\{2,3,5\}$	2

In L2?

No

No

Yes

Yes

<u>C4</u>	
<u>Itemset</u>	<u>Support</u>
$\{1,2,3,5\}$	1

for $I = \{1, 3, 5\}$, subsets are $\{1, 3\}, \{1, 5\}, \{3, 5\}, \{1\}, \{3\}, \{5\}$

for $I = \{2, 3, 5\}$ subsets are $\{2, 3\}, \{2, 5\}, \{3, 5\}, \{2\}, \{3\}, \{5\}$

for every subset S of I ,

$$S \rightarrow (I - S) \quad (\text{S recommends } I - S)$$

$$\text{If } \text{Support}(I) / \text{Support}(S) \geq \text{min-conf value}$$

Applying Rules to Dataset L3

Rule 1: $\{1, 3, 5\}$

$$\text{Rule 1: } \{1, 3\} \rightarrow \{1, 3, 5\}$$

$$\begin{aligned} \text{Confidence} &= \frac{\text{Support}(\{1, 3, 5\})}{\text{Support}(\{1, 3\})} \\ &= \frac{2}{3} = 66.66\% > 60\% \quad \text{Rule selected.} \end{aligned}$$

Rule 2 $\{1, 5\} \rightarrow \{1, 3, 5\}$

$$\begin{aligned} \text{Confidence} &= \frac{\text{Support}(\{1, 3, 5\})}{\text{Support}(\{1, 5\})} \\ &= \frac{2}{2} = 100\% > 60\% \end{aligned}$$

Rule 3 $\{3, 5\} \rightarrow \{1, 3, 5\}$

$$\begin{aligned} \text{Confidence} &= \frac{\text{Support}(\{1, 3, 5\})}{\text{Support}(\{3, 5\})} \\ &= \frac{2}{3} = 66.66\% > 60\% \end{aligned}$$

Rule 4 $\{1\} \rightarrow \{1, 3, 5\}$

$$\begin{aligned} \text{Confidence} &= \frac{\text{Support}(\{1, 3, 5\})}{\text{Support}(\{1\})} \\ &= \frac{2}{3} = 66.66\% > 60\% \end{aligned}$$

Rule 5 $\{3\} \rightarrow \{1, 3, 5\}$

$$\begin{aligned} \text{Confidence} &= \frac{\text{Support}(\{1, 3, 5\})}{\text{Support}(\{3\})} \\ &= \frac{2}{4} = 50\% < 60\% \quad \text{Rule rejected} \end{aligned}$$

Rule 6

$$\begin{aligned} \{5\} &\rightarrow \{1, 3, 5\} \\ \text{Confidence} &= \frac{\text{Support}(\{1, 3, 5\})}{\text{Support}(\{5\})} \\ &= \frac{2}{4} = 50\% < 60\% \quad \text{Rule rejected.} \end{aligned}$$