Problem sheet -5

1. Write suitable grammars for the given languages. Also list three valid and invalid strings for each language

(a)
$$L = \{a^n b^m : n \le m + 3\}.$$

(b)
$$L = \{a^n b^m : n \neq m - 1\}.$$

(c)
$$L = \{a^n b^m : n \neq 2m\}.$$

(d)
$$L = \{a^n b^m : 2n \le m \le 3n\}.$$

(e)
$$L = \{w \in \{a, b\}^* : n_a(w) \neq n_b(w)\}.$$

(f)
$$L = \{w \in \{a, b\}^* : n_a(v) \ge n_b(v), \text{ where } v \text{ is any prefix of } w\}.$$

(g)
$$L = \{w \in \{a,b\}^* : n_a(w) = 2n_b(w) + 1\}.$$

2. Find the language generated by the grammars given below

$$S \to AB|\lambda$$
,

$$A \rightarrow aB$$
,

$$B \rightarrow Sb$$
.

3.

$$S \rightarrow aaB$$
.

$$A \rightarrow bBb|\lambda$$
,

$$B \rightarrow Aa$$
.

4. Write suitable grammar for the following C constructs.

Consult a book on C for formal defintions of the following constructs.

- (a) literal
- (b) for statement
- (c) if-else statement
- (d) do statement
- (e) compound statement
- (f) return statement
