Surprise test for 23/3/2021

Problem 1

$$(q_0, aabbab, Z_0) \vdash (q_0, abbab, aZ_0) \vdash (q_0, bbab, aaZ_0)$$

 $\vdash (q_0, bab, baaZ_0) \vdash^* (q_0, bab, SaZ_0)$
 $\vdash (q_0, ab, bSaZ_0) \vdash^* (q_0, ab, SZ_0) \vdash (q_0, b, aSZ_0)$
 $\vdash (q_0, \Lambda, baSZ_0) \vdash^* (q_0, \Lambda, SSZ_0) \vdash^* (q_0, \Lambda, SZ_0)$
 $\vdash (q_1, \Lambda, Z_0) \vdash (q_2, \Lambda, Z_0)$

Draw the derivation tree for aabbab

Problem 2

Let G be the CFG with productions $S \to S + T \mid T$ $T \to [S] \mid a$. Both parts of the question refer to the moves made by the nondeterministic bottom-up PDA NB(G) in the process of accepting the input string [a + [a]].

- a. If the configuration at some point is $(q_0, + [a]]$, $S[Z_0)$, what is the configuration one move later?
- b. If the configuration at some point is $(q_0, + [a]], T[Z_0)$, what is the configuration one move later?

Problem 3

Consider the CFG with productions

$$S \rightarrow S_1$$
\$ $S_1 \rightarrow S_1 + T \mid T$ $T \rightarrow T * F \mid F$
 $F \rightarrow \lceil S_1 \rceil \mid a$

- a. Write the CFG obtained from this one by eliminating left recursion.
- Give a transition table for a DPDA that acts as a top-down parser for this language.
