



$$t_1 = 0.01$$

$$t_2 = 0.99$$

(From calculating new weight of w_{11} , I have marked the chain rule path)

$$h_{1in} = w_{11}x_1 + w_{21}x_2 + w_{31}x_3 + b_1 = 0.377$$

$$h_{1out} = \text{Act}((h_1)_{in}) = 0.593$$

$$h_{2in} = w_{12}x_1 + w_{22}x_2 + w_{32}x_3 + b_2 = 0.39$$

$$h_{2out} = \text{Act}((h_2)_{in}) = 0.596$$

$$(y_1)_{in} = h_{1out} * w_{h11} + h_{2out} * w_{h21} + b_3 = 1.105$$

$$(y_1)_{out} = \text{Act}((y_1)_{in}) = 0.751$$

$$y_{2in} = h_{1out} * w_{h12} + h_{2out} * w_{h22} + b_4 = 1.224$$

$$y_{2out} = \text{Act}((y_2)_{in}) = 0.772$$

$$\begin{aligned} \text{Error}_{total} &= \frac{1}{2} \left[(\text{target} - y_{out})^2 \right] = \frac{1}{2} \left[(t_1 - y_{1out})^2 + (t_2 - y_{2out})^2 \right] \\ &= \frac{1}{2} \left[(0.01 - 0.751)^2 + (0.99 - 0.772)^2 \right] \\ &= 0.2983 \end{aligned}$$

$$(w_{h11})_{new} = (w_{h11})_{old} - \eta \frac{\partial \text{Error}_{total}}{\partial w_{h11}}$$

$$\begin{aligned}\frac{\partial E_{\text{Total}}}{\partial w_{h1}} &= \frac{\partial E_{\text{Total}}}{\partial y_{1\text{out}}} * \frac{\partial y_{1\text{out}}}{\partial y_{1\text{in}}} * \frac{\partial y_{1\text{in}}}{\partial w_{h1}} \\ &= (y_{1\text{out}} - t_1) * y_{1\text{out}} (1 - y_{1\text{out}}) * h_{1\text{out}} \\ &= 0.651 * 0.751 * 0.249 * 0.593 \\ &= 0.0721\end{aligned}$$

$$\begin{aligned}(w_{h1})_{\text{new}} &= (w_{h1})_{\text{old}} - \eta \frac{\partial E_{\text{Total}}}{\partial w_{h1}} \\ &= 0.40 - 0.5 * 0.0721 \\ &= 0.40 - 0.036 \\ &= 0.364\end{aligned}$$

$$(w_{h12})_{\text{new}} = \frac{\partial E_{\text{Total}}}{\partial y_{2\text{out}}} * \frac{\partial y_{2\text{out}}}{\partial y_{2\text{in}}} * \frac{\partial y_{2\text{in}}}{\partial w_{h12}}$$

$$\begin{aligned}(w_{11})_{\text{new}} &= \frac{\partial E_{\text{Total}}}{\partial y_{1\text{out}}} * \frac{\partial y_{1\text{out}}}{\partial y_{1\text{in}}} * \frac{\partial y_{1\text{in}}}{\partial h_{1\text{out}}} * \frac{\partial h_{1\text{out}}}{\partial h_{1\text{in}}} * \frac{\partial h_{1\text{in}}}{\partial w_{11}} \\ &+ \frac{\partial E_{\text{Total}}}{\partial y_{2\text{out}}} * \frac{\partial y_{2\text{out}}}{\partial y_{2\text{in}}} * \frac{\partial y_{2\text{in}}}{\partial h_{1\text{out}}} * \frac{\partial h_{1\text{out}}}{\partial h_{1\text{in}}} * \frac{\partial h_{1\text{in}}}{\partial w_{11}}\end{aligned}$$

$$\begin{aligned}\Rightarrow & (y_{1\text{out}} - t_1) * y_{1\text{out}} (1 - y_{1\text{out}}) * \cancel{h_{1\text{out}}} * (h_{1\text{out}})_{\text{out}} * (1 - h_{1\text{out}})_{\text{out}} * \eta_1 \\ & + (y_{2\text{out}} - t_2) * y_{2\text{out}} (1 - y_{2\text{out}}) * w_{h12} * (h_{1\text{out}})_{\text{out}} * (1 - h_{1\text{out}})_{\text{out}} * \eta_1\end{aligned}$$

$$\Rightarrow (h_{1\text{out}})_{\text{out}} (1 - h_{1\text{out}})_{\text{out}} * \eta_1 \left[(y_{1\text{out}} - t_1) * y_{1\text{out}} (1 - y_{1\text{out}}) + (y_{2\text{out}} - t_2) * y_{2\text{out}} (1 - y_{2\text{out}}) \right]$$

$$\Rightarrow (1)$$

$$w_{11\text{new}} = w_{11\text{old}} - \eta \frac{\partial E}{\partial w_{11\text{old}}}$$

Similarly calculate for w_{31}, w_{22} ?