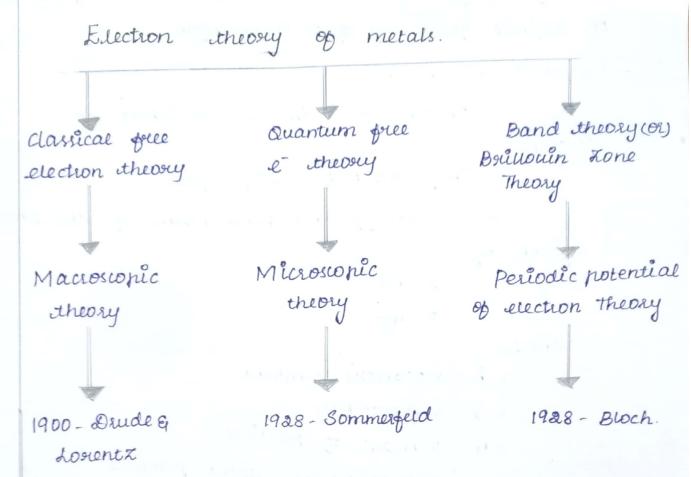
unit - 4 Basic Quantum Physics.



Success of classical free electron theory: * St verifies ohm's daw

* It explain electrical and thermal

conductivity of metals

* It is used to douve wiedemann-

Franx law.

* The optical proporties of metals can be explained using this theory.

Failure of classical free electron theory

* It is macroscopic theory

* It cannot be explained compton, photo-electric effect, naramagnetism, ferromagnetism, etc,...

It is photon (or) discrete energy values in the form of small packets (or) bundles (or) quantas of definite prequency of or wavelength

Properties of photon

* Photons are similar to that of electrons

* They do not ionize gas

* The energy and momentum of the photon is given by.

E=hy

P = mc

where

* h -> planch's constant

* > prequency

*m -> mass of particle

* c -> velocity of light particle

De-Broglie (or) Matter waves

* The waves associated with the matter particles are called matter waves (or) de-Borogue waves $\lambda = \frac{h}{b}$ or $\lambda = \frac{h}{mv}$

Properties

* Matter waves are not electromagnetic waves. particle * lighter will have high wavelength

* Particles moving with less verocity

will have high wavelength

* The Velocity of a matter is not a constant.

other forms of de-Brogue wavelength i) de-Broque wavelength interms of Energy W.K.T

 $KE = \frac{1}{2} mv^2 \longrightarrow (0)$

multiple 'm' on both side

$$Em = \frac{1}{2}m^2v^2$$

 $m^2v^2 = gEm$

 $mv = \sqrt{2Em} \longrightarrow (2)$

. . de - Boiogue wavelength $\lambda = \frac{h}{\sqrt{amE}}$ (: $\lambda = \frac{h}{mv}$)

(ii) de-Broglie wavelength interms of voltage

kinetic energy of particle = 1 mv2 ____ (4)

w.k.T energy = $ev \rightarrow (5)$

equating equation (4) & (5)

1 mv2 = eV -> (b)

multiple in on both side

= m2 v2 = eV.m

m2v2 = ameV

mv = Vamer -> (7)

we know that

.: de-Boroglie wavelength $\lambda = \frac{h}{m}$ (8)

sub eqn (7) in (8)

de-Brogue wavelength $\lambda = \frac{h}{\sqrt{2mev}} \longrightarrow (9)$

(ii) de Broglie wavelength interms of temperature. when a particle like neutron is in theormal equilibrium at temperature T, other they nossess Maxwell distribution of velocity.

kinetic Energy Ek = 1 mvims - (10)

Where

Vms -> 91001 mean square velocity of particle Energy = 3 kBT -> (11)

where

kg -> Boltzmann constant

Equating eqn (10) & (11)

2 mv2 = 3 kBT

multiple m'on both side

m2v2 = 3m kgT

mv = \3mkBT -> (2)

Sub egn (12) in (8)

i. de - Boiogue wavelength 1 = h

Schroedinger wave equation

Time undependent Time dependent

It is described the wave nature of

particle in mathematical form.

Schroedinger:

Time Independent wave equation

classical dipperential equation $\frac{\partial^2 \psi}{\partial x^2} + \frac{\partial^2 \psi}{\partial y^2} + \frac{\partial^2 \psi}{\partial x^2} = \frac{1}{V^2} \frac{\partial^2 \psi}{\partial t^2} \longrightarrow 0$ where, $\nabla^2 \psi = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial x^2}$ (Laplación operator) $abla^2 \psi = \frac{1}{2} \frac{\partial^2 \psi}{\partial x^2} \longrightarrow (2)$ y → wave quinction V -> wave verocity solution of equation (2) $\psi = \psi_0 e^{-lwt}$ (3) Dipp eqn (3) w.r.t't' $\frac{\partial \Psi}{\partial t} = \Psi_0 e^{-i\omega t} (-i\omega)$ Again dits w.r.t 't' $\frac{\partial^2 \psi}{\partial t^2} = \psi_0 e^{-i\omega t} (-i\omega) (-i\omega)$ = 40 e-iwt (i2w2) $\frac{\partial^2 \psi}{\partial L^2} = -\omega^2 \psi \longrightarrow (4) \quad (i = -1)$ Sub egn (4) in (2) V= 4 = - as 4 $\nabla^2 \psi + \frac{\omega^2}{v^2} \psi = 0 \longrightarrow (5)$ we know that W = 278 frequency 8 = V $\omega = 2\pi v$ W = 2T

Squaring on both side
$$\frac{w^2}{V^2} = \frac{4\pi^2}{\lambda^2} \longrightarrow (6)$$
Sub eqn (6) in eqn (5)
$$\nabla^2 \psi + \frac{4\pi^2}{\lambda^2} \psi = 0 \longrightarrow (7)$$
By using $De - Bowglie (\lambda)$

$$\lambda = \frac{h}{mV}$$
Squaring on both side
$$\lambda^2 = \frac{h^2}{m^2 V^2} \longrightarrow (8)$$
Sub eqn (8) in (7)
$$\nabla^2 \psi + \frac{4\pi^2}{h^2/m^2 V^2} \psi = 0 \longrightarrow (9)$$

$$Total energy = potential energy + kinetic energy$$

$$E = V + \frac{1}{2}mV^2$$

$$D(E-V) = mV^2$$

$$D(E-V) = mV^2$$

$$D(E-V) = m^2 V^2 \longrightarrow (9)$$
Sub eqn (10) in (9)

$$\nabla^{2} \psi + 4 \pi^{2} \cdot 2 m (E-V) \psi = 0 \longrightarrow (1)$$

$$h^{2}$$

$$h = \frac{h}{2 \pi}$$

$$h^{2} = \frac{h^{2}}{4 \pi^{2}}$$

$$E\psi = -\frac{\hbar^2}{2m} \nabla^2 \psi + \nu \psi$$

schwedinger time dependent equation:

The solution of classical diffe eqn

diff eqn (1) with respect to 't'

Angular frequency w=2TT2

$$\frac{\partial \psi}{\partial t} = -22\pi \gamma \psi \longrightarrow (2)$$

photon energy £ = h2

$$\gamma = \frac{E}{h}$$

$$\frac{\partial \psi}{\partial t} = -i 2\pi \left(\frac{E}{h}\right) \psi \qquad (ih = 2\pi h)$$

$$\frac{\partial \psi}{\partial t} = -\frac{iE\psi}{\hbar}$$

$$\frac{\partial \psi}{\partial t} = -i \frac{E}{\hbar} \psi \longrightarrow (3)$$

multiple 'i' on both side

in
$$\frac{\partial \Psi}{\partial t} = \mathcal{E} \Psi \longrightarrow (4)$$

Schrondinger time independent equation

$$E \psi = -\frac{\hbar^2}{2m} \nabla^2 \psi + \nabla \psi \longrightarrow (5)$$

it
$$\frac{\partial \Psi}{\partial t} = -\frac{\hbar^2}{2m} \nabla^2 \Psi + V \Psi$$

$$\left(i\hbar \frac{\partial}{\partial t}\right) \Psi = \left(-\frac{\hbar^2}{2m} \nabla^2 + V\right) \Psi$$

ET = HY

Eψ = Energy operator

Hψ = Hamiltonian operator.

Compton Effect

* The beam of x- mays is scattered by a substance at now atomic number by the scattered radiation consists of two components

* Same frequency (or) wavelength

* lower frequency (or) higher wave length

* The changing wavelength of scattered Hadiation is known as compton shift

$$\Delta \lambda = \frac{h}{moc} (1 - \cos 0)$$

Before

$$E = h v$$
 $P = h v$
 $P = h v$
 $P = h v$
 $P = h v$
 $P = m c^2$
 $P = m v$

Recover of election

	Before		apter	
	photon	Electron	photon	Electron
Energy	hz	Mo C ²	h 22'	Mc ²
momentum x - axis	nog	0		mv cos¢
momentum Y-axis	0	0	hr sino	-mv sind

Before collision

Energy of Incident ? + hy
photon

Energy of electron at ? = moc2 sest

= h2+ moc2 ->(1) Total energy

After collision

The energy of scattered photon = ha!

The energy of scattered electron = mc2

Total energy = h2'+mc2 ->(2)

Applying Law of conservation of energy

egn (1) = egn (2)

h8+ moc2 = h2'+ mc2

 $mc^2 = hy + moc^2 - hy'$

mc2 = h(y- 2') + moc2 -> (3)

Before collision

Momentum of photon - x axis = h8

Momentum of electron - yaxis = 0

Total momentum = $hP + 0 \longrightarrow (H)$

After collision

Momentum of scattered photon- 3 = hy coso

Momentum of electron - x axis = mv cos o

Total momentum = $\frac{h^2}{c}$ cos 0 + mv cos $\phi \rightarrow (5)$

Applying law of conservation of momentum:

egn (H) = eqn (5)

 $\frac{hy}{h} = \frac{hy'}{\cos \theta} + mv \cos \phi$

 $\frac{hy}{c} - \frac{hy}{coso} = my \cos \phi$

h (2-8'000) = mv cos \$

h(8-8' coso) = mev cos \$ (6)

Before collision

Momentum of photon along y-axis = 0

Momentum of electron along y-axis = 0

Total Momentum = 0 - (7)

After collision

Momentum of scattered photon? - hy sino

Momentum of electron = mv sin o

Total momentum = hy sino - mysing - 18)

Applying law of conservation of momentum. egn (7) = egn (8) $0 = \frac{h g'}{sino} - m v sin \phi$ $mv \sin \phi = \frac{h v}{s} \sin \phi$ mcv sind = h2' sino ->(9) square and add eqn (9) & (6) $m^2c^2v^2sin^2\phi + m^2c^2v^2cos\phi = h^2p^2sin^2o + h^2(2-2)coso)^2$ m²c²v² [sin² + cos o] = h²p'2sin²0 + h² (p²+p'2os²0 -288' (030) = h2812 sin20+ h282+ h28120520-2122 1000 = h2 212 [sin20+ cos20] + h222 - 2h 22' LOSO m2c2v2 = h2[212+22-288'coso] Egn (3) => square on both side (mc2)2 = [h(2-21) + moc2]2 $m^2 c^4 = h^2 (2-2)^2 + m_0^2 c^4 + 2h(2-2) m_0 c^2$ egn (11) - egn (10) m2c4-m2c2v2=h2(8-21)2+m62c4+2h(8-21)moc2 -h2(2+212-222'coso) m2c2[c2-V2] = h2(22+212 2221) + mo2 64+ 2h(2-21)moc2-h222-h2212+ 2 h2 p2 4050

 $=h^{2}y^{2}+h^{2}y^{2}-2h^{2}yy'+m_{0}^{2}c^{4}+2h(y-y')$ $m_{0}c^{2}-h^{2}y^{2}-h^{2}y^{2}+2h^{2}yy'\cos\theta$

 $m^2c^2(c^2-v^2) = -2h^2yy'[1-coso] + 2h(y-y')moc^2+$

Relativity mass gormula

 $m_0^2 c 4$ $\longrightarrow (12)$

$$m = \frac{m_0}{\sqrt{(1-\frac{V^2}{C^2})}}$$
 $m^2 = \frac{m_0^2 C^2}{C^2 - V^2}$

 $m^2(c^2-V^2) = m_0^2c^2$

multiple c'on both side

 $m^2c^2(c^2-V^2)=m_0^2c^4\longrightarrow (13)$

sub eqn (13) in eqn (12)

moc4 = - 2h2 22'[1-coso]+2h(2-2') moc2+ moc4

2k222'[1-1050]=2h(2-2')moc2

h 28'[1- coso] = moc2(2-21)

$$\frac{h}{moc^2} (1-\omega so) = \frac{1}{\gamma^2} - \frac{1}{\gamma^2} \longrightarrow (14)$$

egn (14) => multiple 'c' on both side

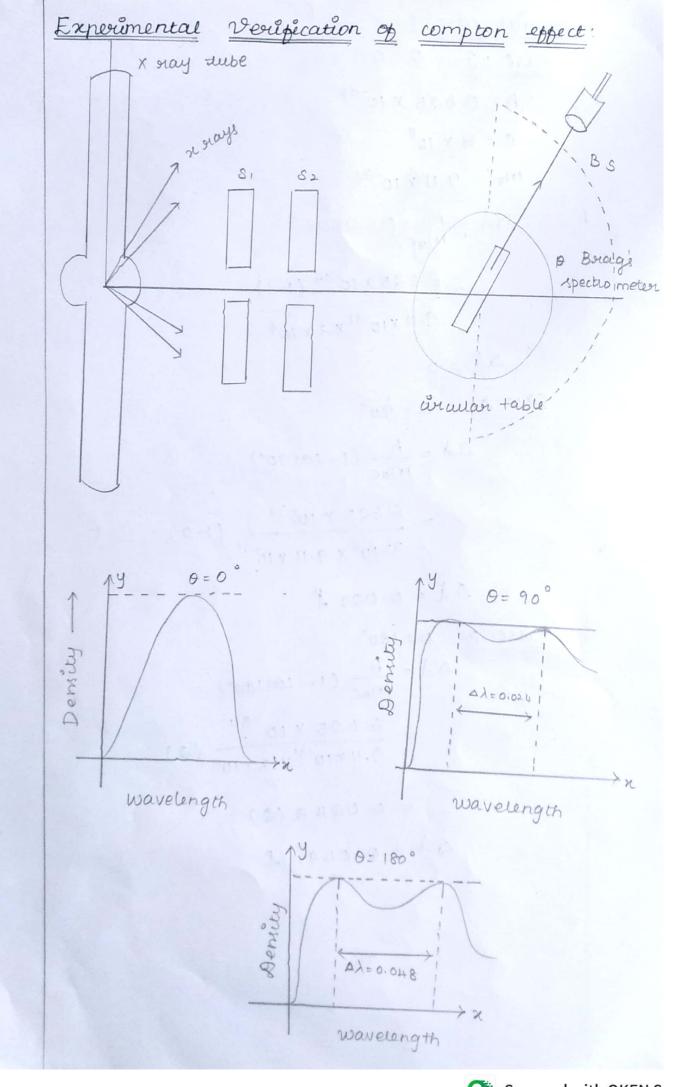
$$\frac{hc}{moc^2} (1 - \cos 0) = \frac{c}{2^i} - \frac{c}{2^i} \quad \left(\frac{c}{2^i} = \lambda; \frac{c}{2^i} = \lambda' \right)$$

$$\lambda' - \lambda = \frac{h}{m_0 c} (1 - coso)$$

$$\Delta \lambda = \frac{h}{m_{oc}} (1 - \cos o)$$

Special case:

$$all : J = 0$$
 $black : J = 0$
 $black :$



Application of schroedinger wave equation ID-potential box. Boundary condition, X=0 V= 00 -> U V= a x=1 $V=\infty \longrightarrow (2)$ The ID - Schroedinger time independent wave equation - $\frac{d^2\psi}{dx^2} + \frac{2m}{h^2} (E-V) \psi = 0 \longrightarrow (3)$ since potential energy V=0 from egn (3) $\frac{d^2 \psi}{dx^2} + \frac{am}{h^2} E \psi = 0$ det $k^2 = \frac{2mE}{\hbar^2} \rightarrow (4)$ $\frac{d^2\psi}{dx^2} + k^2\psi = 0 \longrightarrow (5)$ The solution of equation (5) $\Upsilon(n) = \varnothing \sin kx + B \cos kx \rightarrow (6)$ Boundary wondition -1 x=0 V=0 from equation (6) ψ(x) = A sink(x) + B cosk(x) 0 = 0+ B(1) B = 0 Boundary condition - 2 X=L V=00 B=0 Y(N)=0 MARIATE MARIATER A.

from egn (6)

Y(x) = A sin k(x) + B cos k(x)

0 = A sink(e) + 0

.: A sinkl

Since

A +0

sinkl=0

we know that

sin nTT=0

sinkl = sinnTT

Kd= nTT

 $k = \frac{n\pi}{l} \rightarrow (8)$

sub eqn (1) & (8) in eqn (6)

 $V(x) = A \sin\left(\frac{n\pi x}{\epsilon}\right) \longrightarrow (9)$

Energy of the particle (electron)

from eqn (4)

 $k^2 = \frac{2mF}{h^2}$

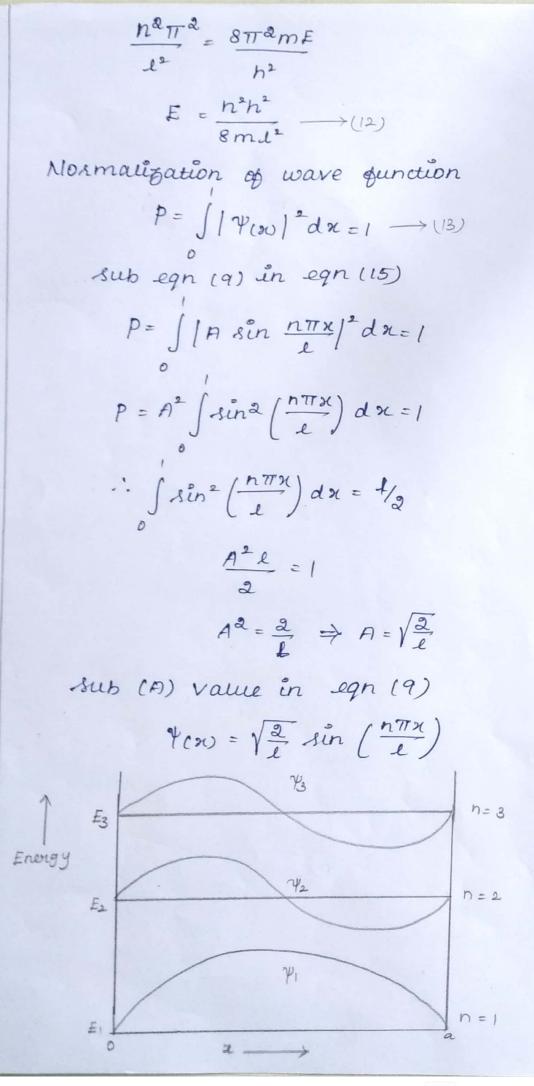
 $k^2 = \frac{2mE}{h^2} \Rightarrow \frac{2mE.4\pi^2}{h^2}$

 $k^2 = 8\pi^2 mE \longrightarrow (10)$

squaring equation (8)

K2 = 12772

comparing equation (10) & (11)



Probability Density

+ st is denoted as p(x,t) dx which means the probability that the particle will be between position & and x+dx at time t.

* A mobability density describes how likely it is that a particle will be in particular position at a parieular time.

We know that $4n = \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi x}{a}\right)$

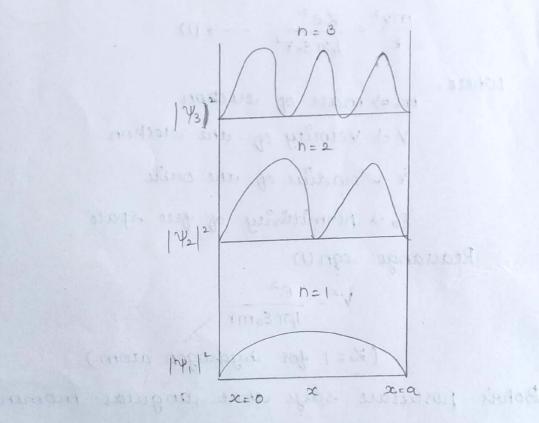
* probability of finding the particle between positions & and 2+ dx is given by

$$P(x) = |Y_n|^2 dx = \frac{2}{a} \sin^2\left(\frac{n\pi x}{a}\right) dx$$

.: probability density, $p(x) = \frac{2}{a} \sin^2(\frac{n\pi x}{a})$

* For n=1 (lowest energy state), x= a

* For n=& (next energy state), x = a & 3a



2 Cooverpondence principle

In 1932 Niels Bohr proposed a correspondence principle of the strong strong some printing they saw

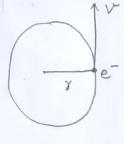
Statement I have no school him a standing

The principle states that for large quantum numbers, quantum physics, gives the same results as those of classical physics.

Proop

According to classical electro-magnetic theory, an electron sevolving in a circular osibil radiates electro-magnetic waves. The frequency of em wave is equal to the frequency of siesolution of election (") the second of the publication !

centrépetal force of 2 columbic attraction resolving electron J between electron & ______



$$\frac{mv^2}{\gamma} = \frac{\chi e^2}{4\pi\epsilon_0 \gamma^2} \longrightarrow (1)$$

where, m => mass of electron V -> verocity of the electron r > radius of the orbit Es > permittivity of free space

Reassange egn (1)

$$V^2 = \frac{e^2}{4\pi \varepsilon_0 m r}$$

(Z=1 for hydrogen atom)

Borris postulate says that angular momentum quantized

i.e., mur= hh - x(2)

squaring on both sides, we have $m^2v^2r^2 = \frac{n^2h^2}{4\pi^2} \longrightarrow (4)$

sub eqn (2) in (4)

$$Y = \frac{n^2h^2\mathcal{E}_0}{\pi me^2} \longrightarrow (5)$$

The frequency of sevolution of election

$$f = \frac{V}{2\pi r} \longrightarrow (6)$$

sub v from eqn(2)

$$f = \frac{1}{2\pi} \frac{e}{\sqrt{4\pi \varepsilon_{omr}}} \longrightarrow (7)$$

sub r from egn (5)

$$= \frac{1}{2\pi} \cdot \frac{e}{\left(4\pi \varepsilon_{om}\right)^{1/2} \left(\frac{h^2 h^2 \varepsilon_{o}}{\pi m e^2}\right)^{3/2}}$$

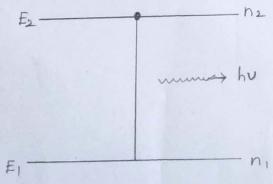
$$f = \frac{me^4}{4 \, \epsilon_n^2 h^3} \cdot \frac{1}{h^3} \longrightarrow (8)$$

According to Bohr's theory, the radiation is emitted when electron jumbs between energy devels.

The frequency of radiation is given by

$$V = \frac{me^{\frac{1}{8}}}{8 e_0^2 h^3} \left(\frac{1}{h_1^2} - \frac{1}{n_2^2} \right) \longrightarrow (9)$$

where n₁ & n₂ are the quantum number coversponding to lower and higher energy severs



1. Physical significance of wave function:

I is a complex quantity

It relates the particles and the wave Statistically

It give the information about the particle behaviour

> Is y* y dx=1 particle present III 4* 4 dx = 0 particle absent

2. What is mean by degenerate and nondegenerate states?

Degenerate

we have same energy eigen value but dipperent eigen function it is known as degenerate state:

Example:

412, Y112

Non-degenerate

we have same energy eigen value and eigen function it is known as nondegenerate state

Example:

Y111, 4222.

3. Depine Eigen values and Eigen function Eigen Values:

It is defined as energy of the particle and is denoted by the letter En Eigen function

It is defined as wave function of the particle and is denoted by the letter yn

4. What is compton wavelength? Give its value The shift in wavelength coversponding to the scattering 90° cauld compton wavelength

we know compton shipt

Cercifore Land California Craws

and a money of the residence of the

$$\Delta \lambda = \frac{h}{m_{oc}} (1 - coso)$$

$$\Delta \lambda = \frac{6.685 \times 10^{-34}}{3 \times 10^8 \times 9.11 \times 10^{-31}} (1-0)$$