

Homework-5 Solutions

Q 4-23

A piston-cylinder device contains nitrogen gas at a specified state. The boundary work is to be determined for the isothermal expansion of nitrogen.

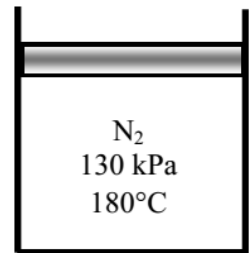
Properties The properties of nitrogen are $R = 0.2968 \text{ kJ/kg}\cdot\text{K}$, $k = 1.4$ (Table A-2a).

Analysis We first determine initial and final volumes from ideal gas relation, and find the boundary work using the relation for isothermal expansion of an ideal gas

$$V_1 = \frac{mRT}{P_1} = \frac{(0.25 \text{ kg})(0.2968 \text{ kJ/kg}\cdot\text{K})(180 + 273 \text{ K})}{(130 \text{ kPa})} = 0.2586 \text{ m}^3$$

$$V_2 = \frac{mRT}{P_2} = \frac{(0.25 \text{ kg})(0.2968 \text{ kJ/kg}\cdot\text{K})(180 + 273 \text{ K})}{80 \text{ kPa}} = 0.4202 \text{ m}^3$$

$$W_b = P_1 V_1 \ln\left(\frac{V_2}{V_1}\right) = (130 \text{ kPa})(0.2586 \text{ m}^3) \ln\left(\frac{0.4202 \text{ m}^3}{0.2586 \text{ m}^3}\right) = \mathbf{16.3 \text{ kJ}}$$

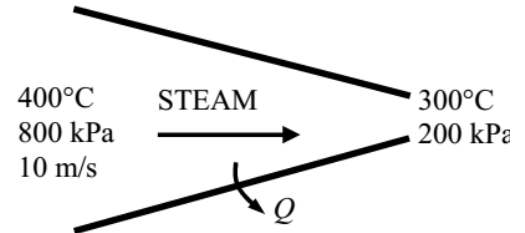


Q 5-34

Heat is lost from the steam flowing in a nozzle. The velocity and the volume flow rate at the nozzle exit are to be determined.

Assumptions 1 This is a steady-flow process since there is no change with time. 2 Potential energy change is negligible. 3 There are no work interactions.

Analysis We take the steam as the system, which is a control volume since mass crosses the boundary. The energy balance for this steady-flow system can be expressed in the rate form as



Energy balance:

$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\dot{\Delta E}_{\text{system}}}_{\text{Rate of change in internal, kinetic, potential, etc. energies}} \stackrel{\text{no (steady)}}{=} 0$$

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m} \left(h_1 + \frac{V_1^2}{2} \right) = \dot{m} \left(h_2 + \frac{V_2^2}{2} \right) + \dot{Q}_{\text{out}} \quad \text{since } \dot{W} \cong \Delta p e \cong 0$$

or

$$h_1 + \frac{V_1^2}{2} = h_2 + \frac{V_2^2}{2} + \frac{\dot{Q}_{\text{out}}}{\dot{m}}$$

The properties of steam at the inlet and exit are (Table A-6)

$$\left. \begin{array}{l} P_1 = 800 \text{ kPa} \\ T_1 = 400^\circ\text{C} \end{array} \right\} \begin{array}{l} v_1 = 0.38429 \text{ m}^3/\text{kg} \\ h_1 = 3267.7 \text{ kJ/kg} \end{array}$$

$$\left. \begin{array}{l} P_2 = 200 \text{ kPa} \\ T_2 = 300^\circ\text{C} \end{array} \right\} \begin{array}{l} v_2 = 1.31623 \text{ m}^3/\text{kg} \\ h_2 = 3072.1 \text{ kJ/kg} \end{array}$$

The mass flow rate of the steam is

$$\dot{m} = \frac{1}{v_1} A_1 V_1 = \frac{1}{0.38429 \text{ m}^3/\text{s}} (0.08 \text{ m}^2)(10 \text{ m/s}) = 2.082 \text{ kg/s}$$

Substituting,

$$3267.7 \text{ kJ/kg} + \frac{(10 \text{ m/s})^2}{2} \left(\frac{1 \text{ kJ/kg}}{1000 \text{ m}^2/\text{s}^2} \right) = 3072.1 \text{ kJ/kg} + \frac{V_2^2}{2} \left(\frac{1 \text{ kJ/kg}}{1000 \text{ m}^2/\text{s}^2} \right) + \frac{25 \text{ kJ/s}}{2.082 \text{ kg/s}}$$

$$\longrightarrow V_2 = \mathbf{606 \text{ m/s}}$$

The volume flow rate at the exit of the nozzle is

$$\dot{V}_2 = \dot{m} v_2 = (2.082 \text{ kg/s})(1.31623 \text{ m}^3/\text{kg}) = \mathbf{2.74 \text{ m}^3/\text{s}}$$

Q 5-54

Argon gas expands in a turbine. The exit temperature of the argon for a power output of 190 kW is to be determined.

Assumptions **1** This is a steady-flow process since there is no change with time. **2** Potential energy changes are negligible. **3** The device is adiabatic and thus heat transfer is negligible. **4** Argon is an ideal gas with constant specific heats.

Properties The gas constant of Ar is $R = 0.2081 \text{ kPa} \cdot \text{m}^3/\text{kg} \cdot \text{K}$. The constant pressure specific heat of Ar is $c_p = 0.5203 \text{ kJ/kg} \cdot ^\circ\text{C}$ (Table A-2a)

Analysis There is only one inlet and one exit, and thus $\dot{m}_1 = \dot{m}_2 = \dot{m}$. The inlet specific volume of argon and its mass flow rate are

$$v_1 = \frac{RT_1}{P_1} = \frac{(0.2081 \text{ kPa} \cdot \text{m}^3/\text{kg} \cdot \text{K})(723 \text{ K})}{1600 \text{ kPa}} = 0.09404 \text{ m}^3/\text{kg}$$

Thus,

$$\dot{m} = \frac{1}{v_1} A_1 V_1 = \frac{1}{0.09404 \text{ m}^3/\text{kg}} (0.006 \text{ m}^2)(55 \text{ m/s}) = 3.509 \text{ kg/s}$$

We take the turbine as the system, which is a control volume since mass crosses the boundary. The energy balance for this steady-flow system can be expressed in the rate form as

$$\underbrace{\dot{E}_{in} - \dot{E}_{out}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\dot{\Delta E}_{system}}_{\text{Rate of change in internal, kinetic, potential, etc. energies}} \overset{\text{No (steady)}}{=} 0$$

$$\dot{E}_{in} = \dot{E}_{out}$$

$$\dot{m}(h_1 + V_1^2/2) = \dot{W}_{out} + \dot{m}(h_2 + V_2^2/2) \quad (\text{since } \dot{Q} \cong \Delta pe \cong 0)$$

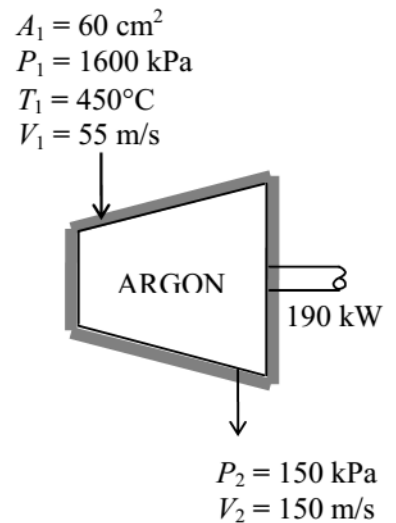
$$\dot{W}_{out} = -\dot{m} \left(h_2 - h_1 + \frac{V_2^2 - V_1^2}{2} \right)$$

Substituting,

$$190 \text{ kJ/s} = -(3.509 \text{ kg/s}) \left[(0.5203 \text{ kJ/kg} \cdot ^\circ\text{C})(T_2 - 450^\circ\text{C}) + \frac{(150 \text{ m/s})^2 - (55 \text{ m/s})^2}{2} \left(\frac{1 \text{ kJ/kg}}{1000 \text{ m}^2/\text{s}^2} \right) \right]$$

It yields

$$T_2 = \mathbf{327^\circ\text{C}}$$



Q 5-57

Air is expanded in an adiabatic turbine. The mass flow rate of the air and the power produced are to be determined.

Assumptions **1** This is a steady-flow process since there is no change with time. **2** The turbine is well-insulated, and thus there is no heat transfer. **3** Air is an ideal gas with constant specific heats.

Properties The constant pressure specific heat of air at the average temperature of $(500+127)/2=314^\circ\text{C}=587\text{ K}$ is $c_p = 1.048\text{ kJ/kg}\cdot\text{K}$ (Table A-2b). The gas constant of air is $R = 0.287\text{ kPa}\cdot\text{m}^3/\text{kg}\cdot\text{K}$ (Table A-1).

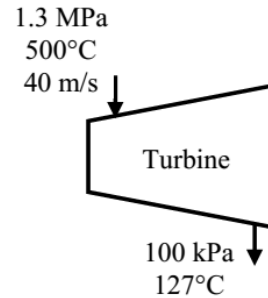
Analysis (a) There is only one inlet and one exit, and thus $\dot{m}_1 = \dot{m}_2 = \dot{m}$. We take the turbine as the system, which is a control volume since mass crosses the boundary. The energy balance for this steady-flow system can be expressed in the rate form as

$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\Delta \dot{E}_{\text{system}}}_{\text{Rate of change in internal, kinetic, potential, etc. energies}} \stackrel{\text{no (steady)}}{=} 0$$

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m} \left(h_1 + \frac{V_1^2}{2} \right) = \dot{m} \left(h_2 + \frac{V_2^2}{2} \right) + \dot{W}_{\text{out}}$$

$$\dot{W}_{\text{out}} = \dot{m} \left(h_1 - h_2 + \frac{V_1^2 - V_2^2}{2} \right) = \dot{m} \left(c_p (T_1 - T_2) + \frac{V_1^2 - V_2^2}{2} \right)$$



The specific volume of air at the inlet and the mass flow rate are

$$\nu_1 = \frac{RT_1}{P_1} = \frac{(0.287\text{ kPa}\cdot\text{m}^3/\text{kg}\cdot\text{K})(500+273\text{ K})}{1300\text{ kPa}} = 0.1707\text{ m}^3/\text{kg}$$

$$\dot{m} = \frac{A_1 V_1}{\nu_1} = \frac{(0.2\text{ m}^2)(40\text{ m/s})}{0.1707\text{ m}^3/\text{kg}} = \mathbf{46.88\text{ kg/s}}$$

Similarly at the outlet,

$$\nu_2 = \frac{RT_2}{P_2} = \frac{(0.287\text{ kPa}\cdot\text{m}^3/\text{kg}\cdot\text{K})(127+273\text{ K})}{100\text{ kPa}} = 1.148\text{ m}^3/\text{kg}$$

$$V_2 = \frac{\dot{m} \nu_2}{A_2} = \frac{(46.88\text{ kg/s})(1.148\text{ m}^3/\text{kg})}{1\text{ m}^2} = 53.82\text{ m/s}$$

(b) Substituting into the energy balance equation gives

$$\begin{aligned} \dot{W}_{\text{out}} &= \dot{m} \left(c_p (T_1 - T_2) + \frac{V_1^2 - V_2^2}{2} \right) \\ &= (46.88\text{ kg/s}) \left[(1.048\text{ kJ/kg}\cdot\text{K})(500-127)\text{ K} + \frac{(40\text{ m/s})^2 - (53.82\text{ m/s})^2}{2} \left(\frac{1\text{ kJ/kg}}{1000\text{ m}^2/\text{s}^2} \right) \right] \\ &= \mathbf{18,300\text{ kW}} \end{aligned}$$

Q 5-67

Steam is throttled from a specified pressure to a specified state. The quality at the inlet is to be determined.

Assumptions **1** This is a steady-flow process since there is no change with time. **2** Kinetic and potential energy changes are negligible. **3** Heat transfer to or from the fluid is negligible. **4** There are no work interactions involved.

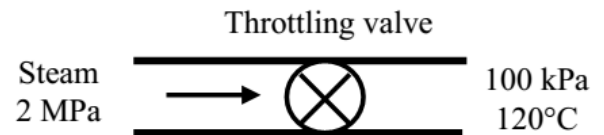
Analysis There is only one inlet and one exit, and thus $\dot{m}_1 = \dot{m}_2 = \dot{m}$. We take the throttling valve as the system, which is a control volume since mass crosses the boundary. The energy balance for this steady-flow system can be expressed in the rate form as

$$\dot{E}_{\text{in}} - \dot{E}_{\text{out}} = \Delta \dot{E}_{\text{system}} \stackrel{\text{no (steady)}}{=} 0$$

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m}h_1 = \dot{m}h_2$$

$$h_1 = h_2$$



Since $\dot{Q} \cong \dot{W} = \Delta \text{ke} \cong \Delta \text{pe} \cong 0$.

The enthalpy of steam at the exit is (Table A-6),

$$\left. \begin{array}{l} P_2 = 100 \text{ kPa} \\ T_2 = 120^\circ\text{C} \end{array} \right\} h_2 = 2716.1 \text{ kJ/kg}$$

The quality of the steam at the inlet is (Table A-5)

$$\left. \begin{array}{l} P_1 = 2000 \text{ kPa} \\ h_1 = h_2 = 2716.1 \text{ kJ/kg} \end{array} \right\} x_1 = \frac{h_2 - h_f}{h_{fg}} = \frac{2716.1 - 908.47}{1889.8} = \mathbf{0.957}$$