


ME341A
Heat and Mas Transfer
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Introduction to Radiation Heat Transfer


by
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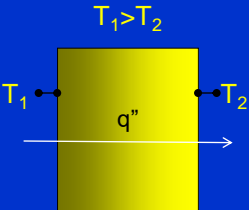
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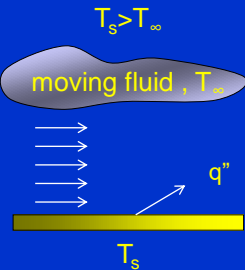


Modes of heat transfer

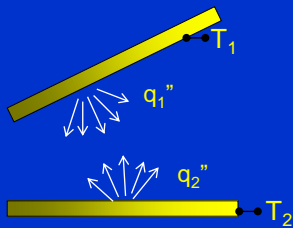
CONDUCTION


$$\dot{Q} = k \cdot A \cdot \frac{\Delta T}{\Delta x}$$

CONVECTION


$$\dot{Q} = h \cdot A \cdot \Delta T$$

RADIATION


$$\dot{Q} = \sigma \cdot \varepsilon \cdot A \cdot (T^4 - T_{\infty}^4)$$


MIXED MODE HEAT TRANSFER

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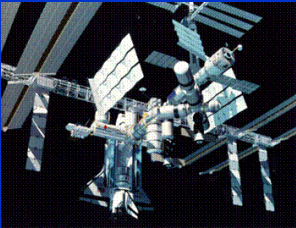
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Examples: Space, Furnaces, heat treatment....




Space thermal management



Heat treatment furnaces



Bread Furnaces




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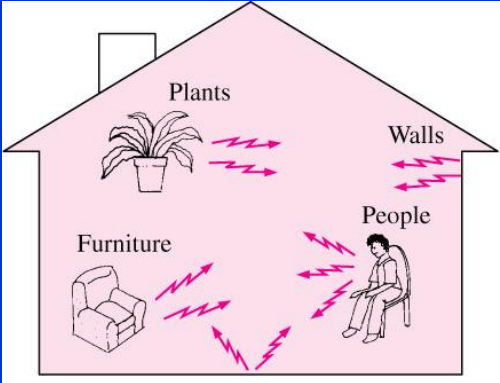
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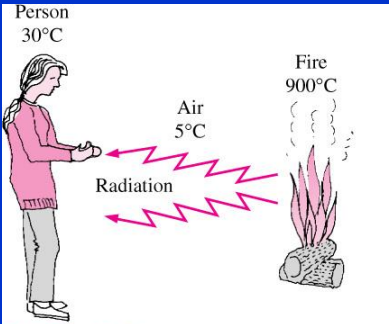
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Everything around us emits radiation



Plants
Walls
Furniture
People



Person
30°C
Air
5°C
Fire
900°C
Radiation

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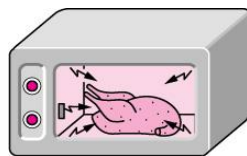
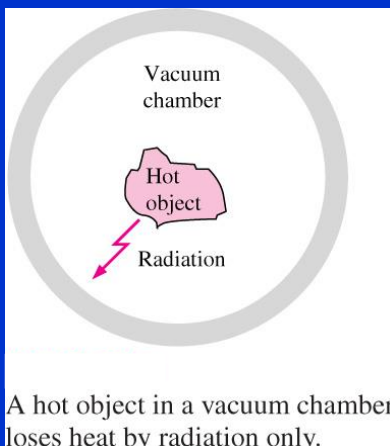
Unlike conduction and convection, heat transfer by radiation can occur between two bodies, even when they are separated by a medium colder than both.

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Radiation exchange: Examples



Food is heated or cooked in a microwave oven by absorbing the electromagnetic radiation energy generated by the magnetron of the oven.



Radiation: Special characteristics


The mechanism of radiation is fundamentally different from conduction and convection.

Here:

- **Electromagnetic theory:** needed to describe the wavelike nature of radiation (Energy and 'pressure' associated with electromagnetic waves)
- **Thermodynamics:** is of course, essential to understand bulk interactions.
- **Quantum mechanics:** is necessary to describe in detail the atomic and molecular processes that occur when radiation is produced within matter and when it is absorbed by matter.
- **Statistical mechanics:** is needed to describe the way in which energy of radiation is distributed over the wavelength spectrum.

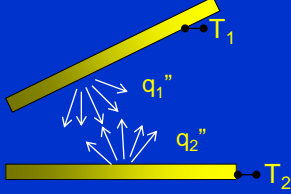
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Radiation: Special characteristics

- Fundamentally different from what we have studied so far
- Conduction and Convection both depend on material medium
- Radiation is an electromagnetic phenomenon--No matter is required
- Rate of energy transfer is proportional to fourth power of temperature difference
- Radiation is long range Phenomena while conduction/convection are short range
- Mixed mode requires integro-differential equations
- Spectral and directional nature of radiation



$$\dot{Q} = \sigma \cdot \varepsilon \cdot A \cdot (T^4 - T_{\infty}^4)$$

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Radiation: Special characteristics

Scales are different!
Conduction and convection are
→ short range, molecular mean free path

Radiation → Long range

Partial differential equations vs integro-diferential equations
(problems involving radiation with conduction/convection)

Behavior of radiative properties is quite complex
→ Spectral and Directional
→ Difficult to measure and show 'erratic behavior'


In contrast, behavior or properties which affect
conduction/convection is rather simple/ 'well-behaved'

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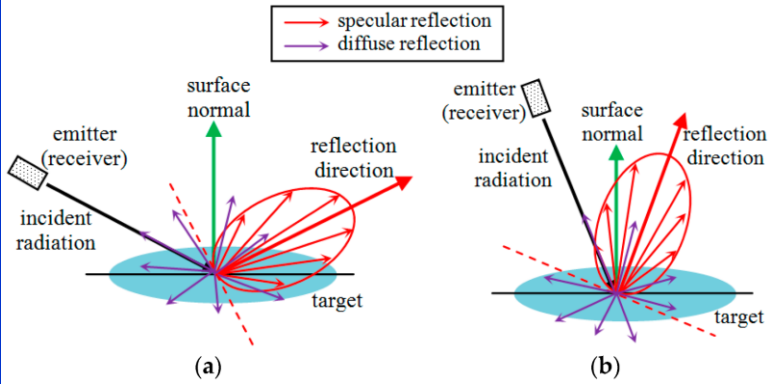
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For example: Specular/Diffuse mirrors




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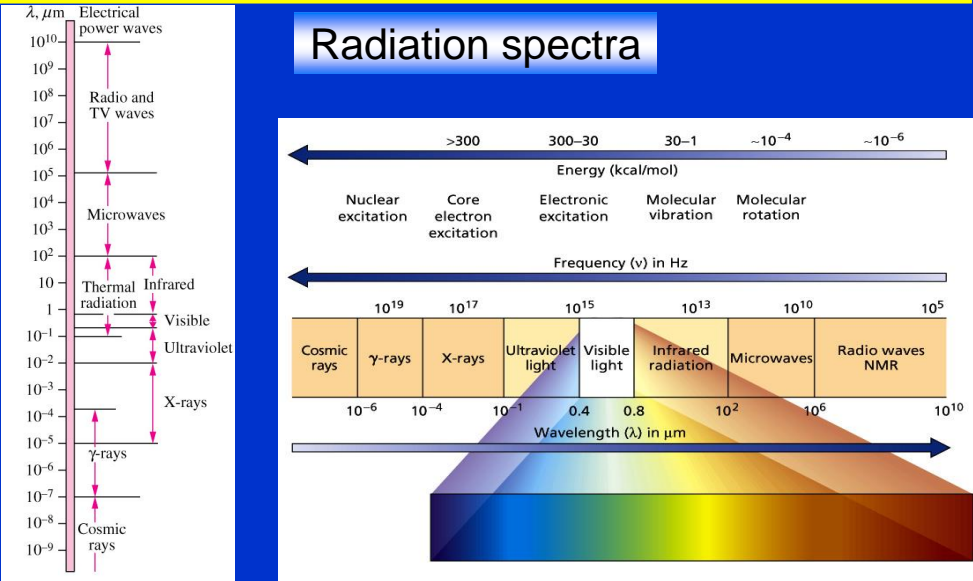
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Radiation spectra




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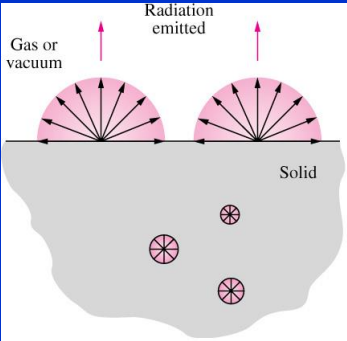
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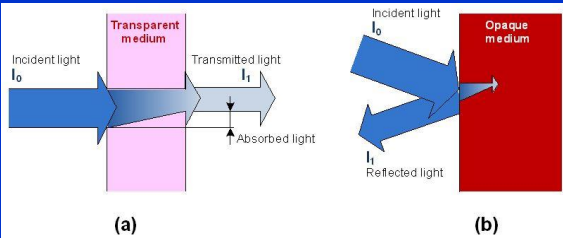
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Radiation in opaque solids



Radiation in opaque solids is considered a surface phenomenon since the radiation emitted only by the molecules at the surface can escape the solid.



(a) (b)

Transmissivity (τ)

Reflectivity (ρ)

Absorptivity (α)


$$\tau + \rho + \alpha = 1$$

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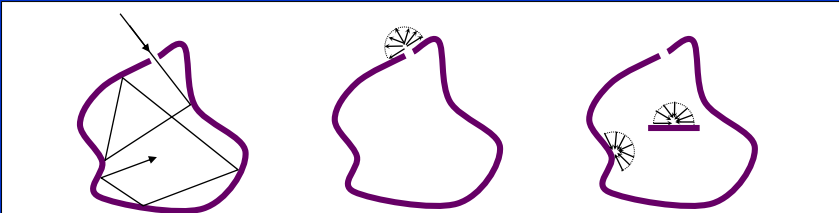
Concept of a black body

A black body is an ideal surface having the following properties

1. It absorbs all incident radiation, regardless of wavelength and direction

2. For a prescribed temperature and wavelength, no surface can emit energy more than a blackbody

3. Although the radiation emitted by a blackbody is a function of wavelength and temperature, it is independent of the direction. Hence, the blackbody is a diffuse emitter



Isothermal surface

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Black body characteristics


- A black body is an idealized physical body that absorbs all incident electromagnetic radiation, regardless of frequency or angle of incidence.
- A **white body** is one that reflects all incident rays completely and uniformly in all directions.
- A black body in thermal equilibrium (that is, at a constant temperature) emits electromagnetic radiation called black-body radiation.
- The radiation is emitted according to **Planck's law**, meaning that it has a spectrum that is determined by the temperature alone, not by the body's shape or composition.
- An ideal black body in thermal equilibrium has two notable properties:
 - It is an ideal emitter: at every frequency, it emits as much or more thermal radiative energy as any other body at the same temperature.
 - It is a **diffuse** emitter: the energy is radiated isotropically, independent of direction.

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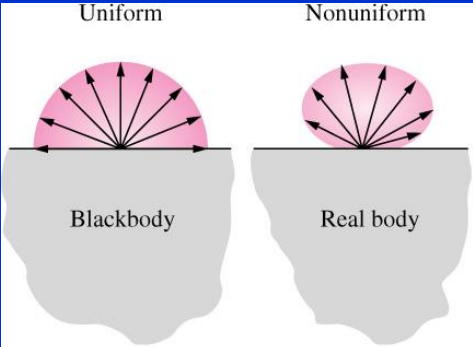
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Concept of a black body

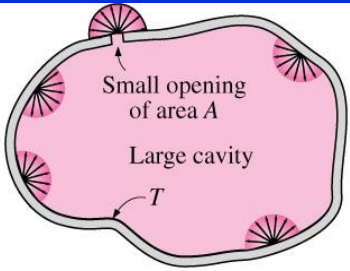
Uniform

Nonuniform



Blackbody

Real body




A large isothermal cavity at temperature T with a small opening of area A closely resembles a blackbody of surface area A at the same temperature.

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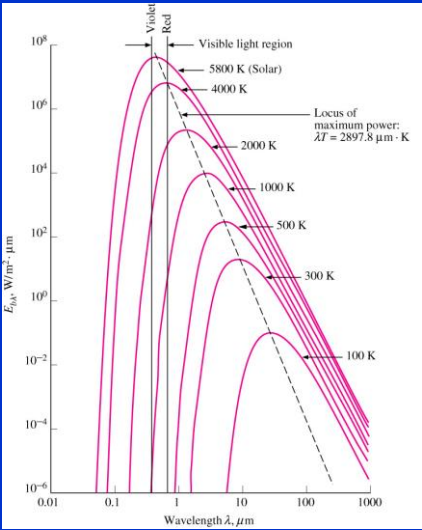
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Emissive power of a black body



Emittance or **Emissive power** is the total amount of thermal energy emitted per unit area per unit time for all possible wavelengths.

Emissivity of a body at a given temperature is the ratio of the total emissive power of a body to the total emissive power of a perfectly black body at that temperature.


Spectral → fn(λ)

Directional → fn (angle of incidence)

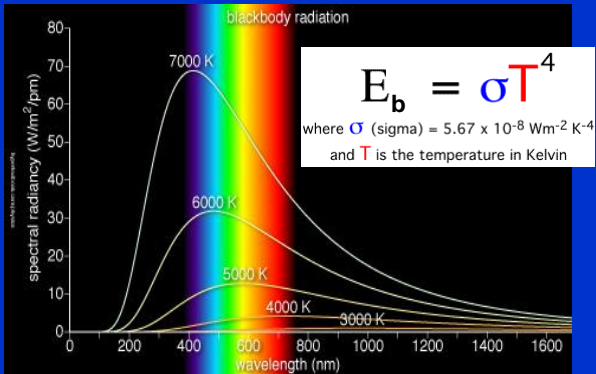
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Stephan Boltzmann Law



The radiation energy emitted by a black body per unit time and per unit surface area, E_b , is called as the **blackbody emissive power**.


↓

Proportional to the fourth power of the absolute temperature

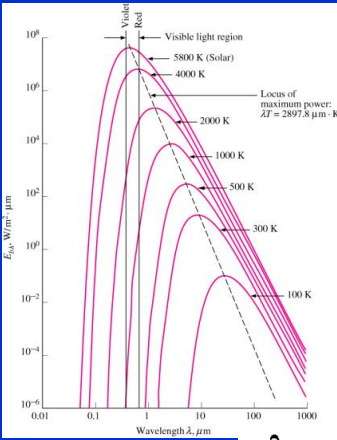
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Planks Law and implications



- Emitted radiation is a continuous function of wavelength.
- At any wavelength, the amount of emitted radiation increases with temperature
- As the temperature increases, the curves shift to the left, to the shorter wavelengths. A larger fraction of the radiation is emitted at shorter wavelengths at higher temperatures.
- Solar radiation → 5800 K

$$E(\lambda, T) = \frac{2hc^2 \pi}{\lambda^5} \cdot \frac{1}{e^{\left(\frac{hc}{\lambda kT}\right)} - 1} = E_{b, \lambda}$$

h = Planck's constant = $6.626 \times 10^{-34} \text{ J} \cdot \text{s}$
 c = speed of light = $2.997925 \times 10^8 \text{ m / sec}$
 λ = wavelength (m)
 k = Boltzmann's constant = $1.381 \times 10^{-23} \text{ J/K}$
 T = temperature (K)

Wien's Law

$$\lambda_{\max} = C/T$$


where C is a constant equal to 2897
and T is the temperature in Kelvin

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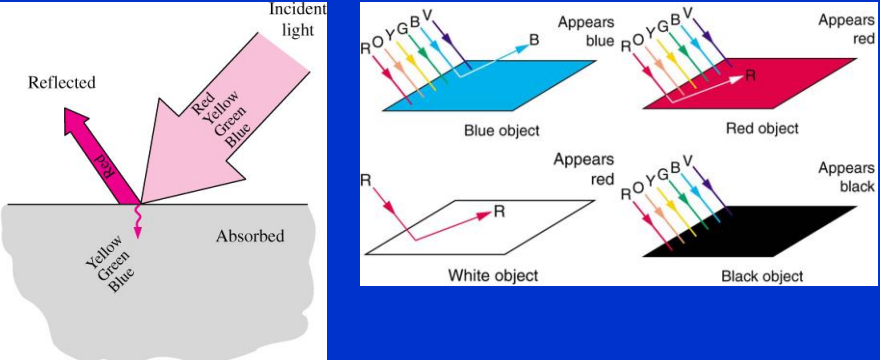
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Color of an object: due to selective reflection



For objects below about 800 K, the colour of the object is not due to emission (emission is dominated by infra-red), it is due to selective reflection of a particular wavelength

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Color of an object: due to emission

Temperature (°C)
550
630
680
740
770
800
850
900
950
1000
1100
1200
1300

Infra-red camera
> 0.8 micrometer

Hot steel ingot

Electric heater

Objects beyond 1000K
emit visible radiation

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Solar radiation spectrum

Spectral Irradiance ($\text{W/m}^2/\text{nm}$)

Wavelength (nm)

UV Visible Infrared →

Sunlight at Top of the Atmosphere

5250°C Blackbody Spectrum

Radiation at Sea Level

Absorption Bands


O_3 O_2 H_2O H_2O H_2O CO_2 H_2O

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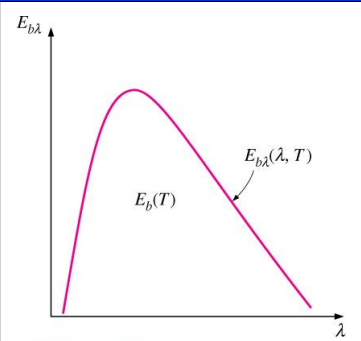
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Relation between laws of radiation



On an $E_{b\lambda}$ - λ chart, the area under a curve for a given temperature represents the total radiation energy emitted by a blackbody at that temperature.


- Stephan-Boltzmann Law is obtained by integrating the Planks Law over the entire range of wavelengths
- That is: the integration of the spectral black body emissive power $E_{b,\lambda}$ over the entire wavelength spectrum gives the total black body emissive power E_b

$$\int_0^\infty E(\lambda, T) d\lambda = \int_0^\infty \left\{ \frac{2hc^2}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda kT}} - 1} \right\} d\lambda$$
$$E_b(T) = \frac{2hc^2\pi^4}{15\left[\frac{hc}{k}\right]^4} T^4 = \sigma T^4$$

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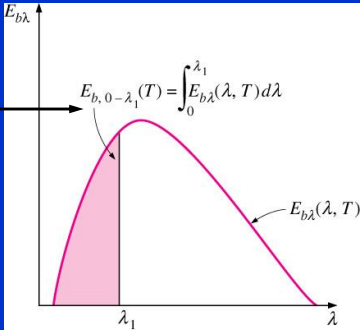
Band emissive power

The radiation energy emitted by a blackbody per unit area over a wavelength band $\lambda = 0$ to λ_1 is determined by this integral

$$E_{b, 0-\lambda_1}(T) = \int_0^{\lambda_1} E_{b\lambda}(\lambda, T) d\lambda$$

However, a closed form solution is not possible with the limits 0 to any arbitrary λ_1
(Only $\lambda_1 = \infty$ is possible, as we did earlier)

Only numerical integration is possible which is rather tedious to perform every time




On an $E_{b\lambda}$ - λ chart, the area under the curve to the left of the $\lambda = \lambda_1$ line represents the radiation energy emitted by a blackbody in the wavelength range $0-\lambda_1$ for the given temperature.

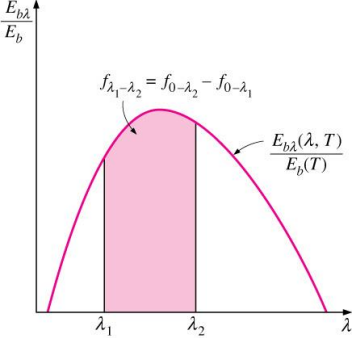
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Black body radiation function



Graphical representation of the fraction of radiation emitted in the wavelength band from λ_1 to λ_2 .

λT ($\mu\text{m} \cdot \text{K}$)	$f_{0-\lambda}$
200	0.000000
400	0.000000
600	0.000000
800	0.000016
1,000	0.000321
1,200	0.002134
1,400	0.007790
1,600	0.019718
1,800	0.039341
2,000	0.066728
2,200	0.100888
2,400	0.140256
2,600	0.183120
2,800	0.227897
2,898	0.250108

$$f_{\lambda}(T) = \frac{\int_0^{\lambda} E_{b\lambda}(\lambda, T) d\lambda}{\sigma T^4}$$

The above function represents the fraction of the radiation emitted from a blackbody at temperature T in the wavelength band $0 - \lambda$

The fraction of the radiation energy emitted by a black body at temperature T over a finite wavelength band is:


$$f_{\lambda_1-\lambda_2}(T) = f_{\lambda_2}(T) - f_{\lambda_1}(T)$$

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Why an incandescent bulb is inefficient



HIGHLY INEFFICIENT

- White filament $\approx 2500\text{ K}$
- Visible spectrum $0.4\text{ }\mu\text{m}$ to $0.76\text{ }\mu\text{m}$
- $\lambda_1 T = 0.4 \times 2500 = 1000\text{ }\mu\text{mK} \rightarrow$ hence, $f_{\lambda_1} = 0.000321$
- $\lambda_2 T = 0.76 \times 2500 = 1900\text{ }\mu\text{mK} \rightarrow$ hence, $f_{\lambda_2} = 0.053035$
- 0.03 percent of radiation is emitted at wavelengths less than $0.4\text{ }\mu\text{m}$ and 5.3 percent at wavelengths less than $0.76\text{ }\mu\text{m}$
- Hence, the fraction of the radiation emitted between these two wavelengths is:
- $f_{\lambda_1-\lambda_2} = f_{\lambda_2} - f_{\lambda_1} = 0.053035 - 0.000321 = 0.0527135$

Only about 5% of the total emission radiated by the filament is in the visible spectrum. The rest 95% is all primarily infrared.


From Wiens law, the peak emission occurs at a wavelength of $1.16\text{ }\mu\text{m}$ [$(\lambda T)_{\text{max power}} = 2897.7$]

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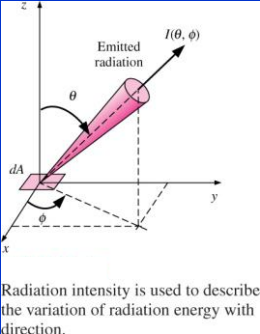
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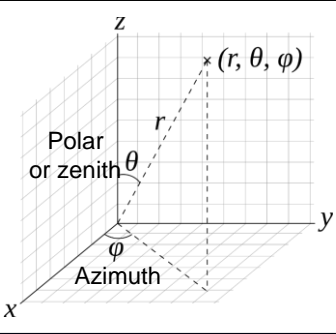
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Radiation intensity in spherical coordinate system



Radiation intensity is used to describe the variation of radiation energy with direction.



- Radiation is emitted by all parts of a plane surface into the hemisphere above the surface.
- The directional distribution of the emitted (or incident) radiation is usually not uniform.
- Therefore, we need a quantity that describes the magnitude of radiation emitted (or incident) in a specified direction in space.


This quantity is called as Radiation Intensity, denoted by I

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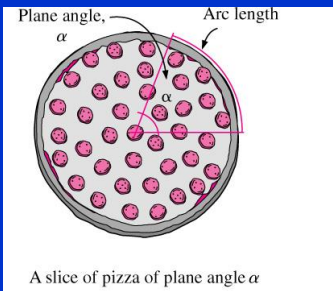
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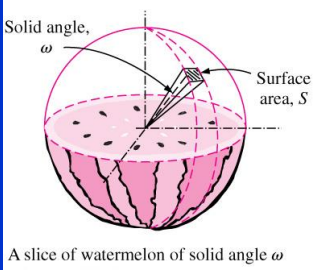
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Plane angle vs Solid Angle



A slice of pizza of plane angle α



A slice of watermelon of solid angle ω

$$\text{Plane Angle} = \frac{\text{Arc}}{\text{Radius}} \quad \text{radians}$$

- For a circle of unit radius, the length of the arc is equivalent to the plane angle which it subtends; both are 2π for a complete circle of radius $r = 1$

$$\text{Solid Angle} = \frac{\text{Surface Area}}{(\text{Radius})^2} \quad \text{steradians}$$


- For a sphere of unit radius, the area on the surface of a sphere is equivalent to the solid angle which it subtends; both are 4π for a complete circle of radius $r = 1$

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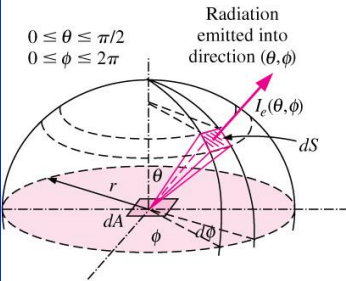
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Solid angle for a hemisphere

The emission of radiation from a differential surface element into the surrounding hemispherical space through a differential solid angle



$0 \leq \theta \leq \pi/2$
 $0 \leq \phi \leq 2\pi$

Radiation emitted into direction (θ, ϕ)

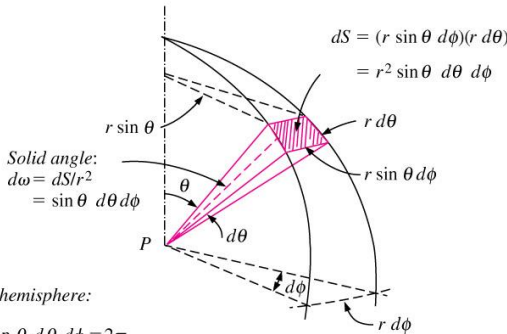
$I_e(\theta, \phi)$

dS

dA

θ

ϕ



$dS = (r \sin \theta d\phi)(r d\theta)$
 $= r^2 \sin \theta d\theta d\phi$

$r \sin \theta$

$r d\theta$

$r \sin \theta d\phi$

P

θ

$d\theta$

$d\phi$

$r d\phi$

Solid angle:
 $d\omega = dS/r^2$
 $= \sin \theta d\theta d\phi$

Solid angle for a hemisphere:
$$\omega = \int d\omega = \int_{\theta=0}^{\pi/2} \int_{\phi=0}^{2\pi} \sin \theta d\theta d\phi = 2\pi$$


Hemisphere

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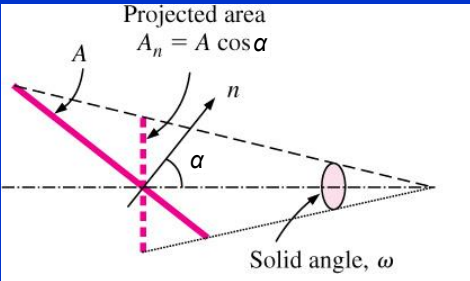
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Generalized viewing angle



Projected area
 $A_n = A \cos \alpha$

A

n

α

Solid angle, ω

Radiation intensity is based on the projected area, and thus the calculation of radiation emission from a surface involves the projection of the surface

HENCE

In general, the differential solid angle $d\omega$ subtended by a differential surface area dA when viewed from a point at a distance r from dA is expressed as

$$d\omega = \frac{dA_n}{r^2} = \frac{dA \cdot \cos(\alpha)}{r^2}$$

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Intensity of emitted radiation

- The radiation intensity of the emitted radiation $I_e(\theta, \varphi)$ is defined as the rate at which radiation energy dQ_e is emitted in the (θ, φ) direction per unit area normal to this direction and per unit solid angle about this direction.

$$I_e(\theta, \varphi) = \frac{d\dot{Q}}{dA \cos(\theta) \cdot d\omega} = \frac{d\dot{Q}}{dA \cos(\theta) \cdot \sin(\theta) d\theta d\varphi}$$

W/(m²·sr)
- The radiation flux for emitted radiation is the emissive power E, which can be expressed in the differential form as:

$$dE = \frac{d\dot{Q}}{dA} = I_e(\theta, \varphi) \cos(\theta) \cdot \sin(\theta) d\theta d\varphi$$
- The emissive power from the surface into the hemisphere surrounding it can be determined by integration:

$$E = \int_{hemisphere} dE = \int_{\varphi=0}^{2\pi} \int_{\theta=0}^{\pi/2} I_e(\theta, \varphi) \cos(\theta) \cdot \sin(\theta) d\theta d\varphi$$


W/m²

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Averaging of quantities

Naming	Depends on		For example
	Wavelength	Angle (θ, φ)	Intensity
Spectral-Directional	Yes	Yes	$I_{\lambda,e}(\lambda, \theta, \varphi, T)$
Total-Directional	No (Averaged)	Yes	$I_e(\theta, \varphi, T)$
Spectral-Hemispherical	Yes	No (Averaged)	$I_{\lambda,e}(\lambda, T)$
Total-Hemispherical	No (Averaged)	No (Averaged)	$I_e(T)$

Diffused Systems (no dependency on the angle)

$$E = \int_{hemisphere} dE = \int_{\varphi=0}^{2\pi} \int_{\theta=0}^{\pi/2} I_e(\theta, \varphi) \cdot \cos(\theta) \cdot \sin(\theta) d\theta d\varphi = \pi I_e$$

Since a black body is a diffused emitter


$$E_b = \pi I_b = \sigma T^4$$

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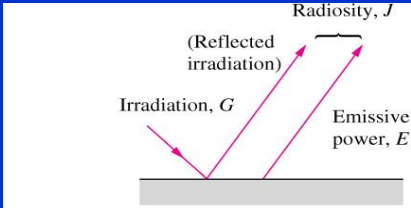
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Radiation fluxes

Corresponding intensities are defined as:

- $E \rightarrow I_e$
- $G \rightarrow I_i$
- $R \rightarrow I_r$
- $J = (E+R) \rightarrow I_{e+r}$
- Again there are four possibilities depending on whether the intensities are dependent on frequency (specular) and direction.
- If the intensities are diffuse $I = \text{constant}$, then:
 - $E = \pi I_e$
 - $G = \pi I_i$
 - $R = \pi I_r$
 - $J = \pi I_{e+r}$




The three kinds of radiation flux (in W/m^2): emissive power, irradiation, and radiosity.

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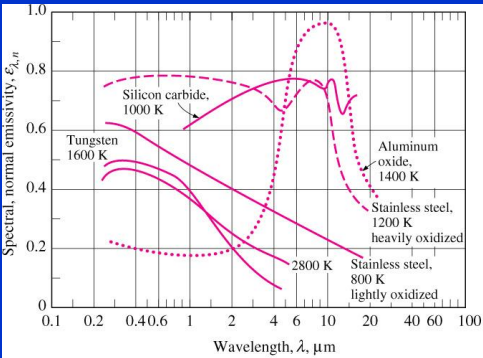
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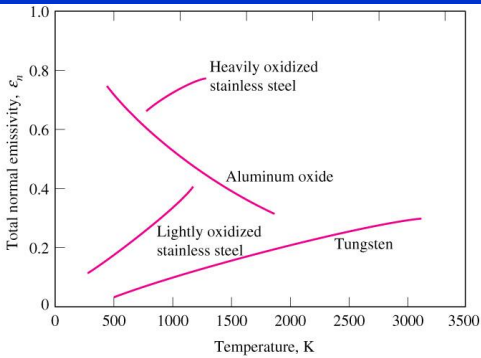
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Spectral and directional nature of emissivity



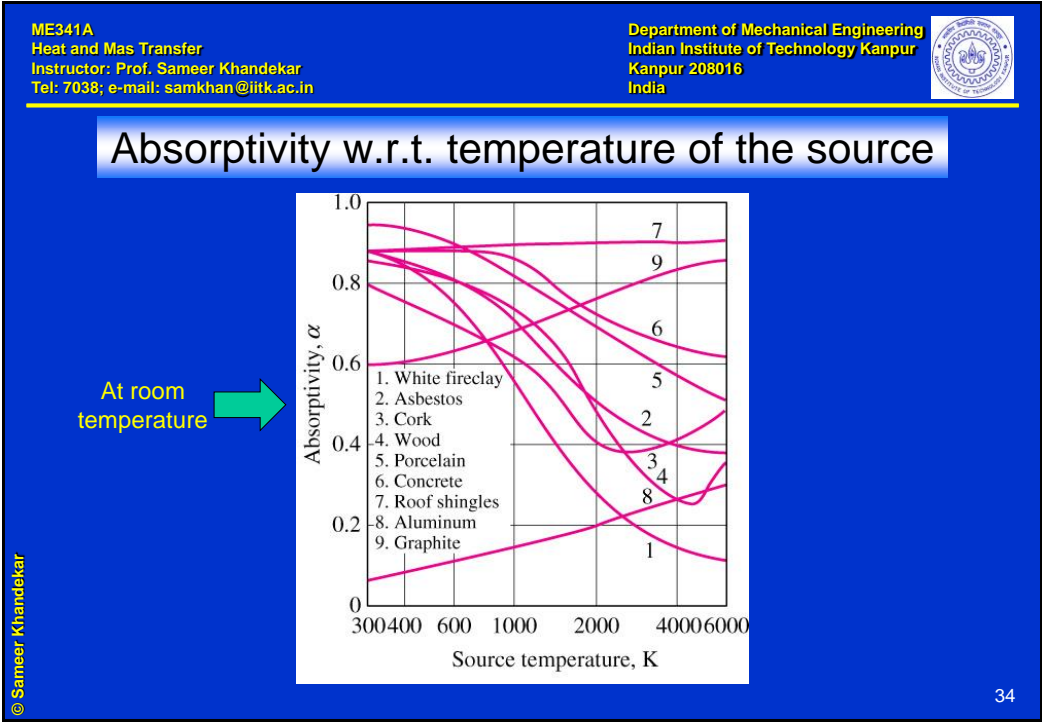
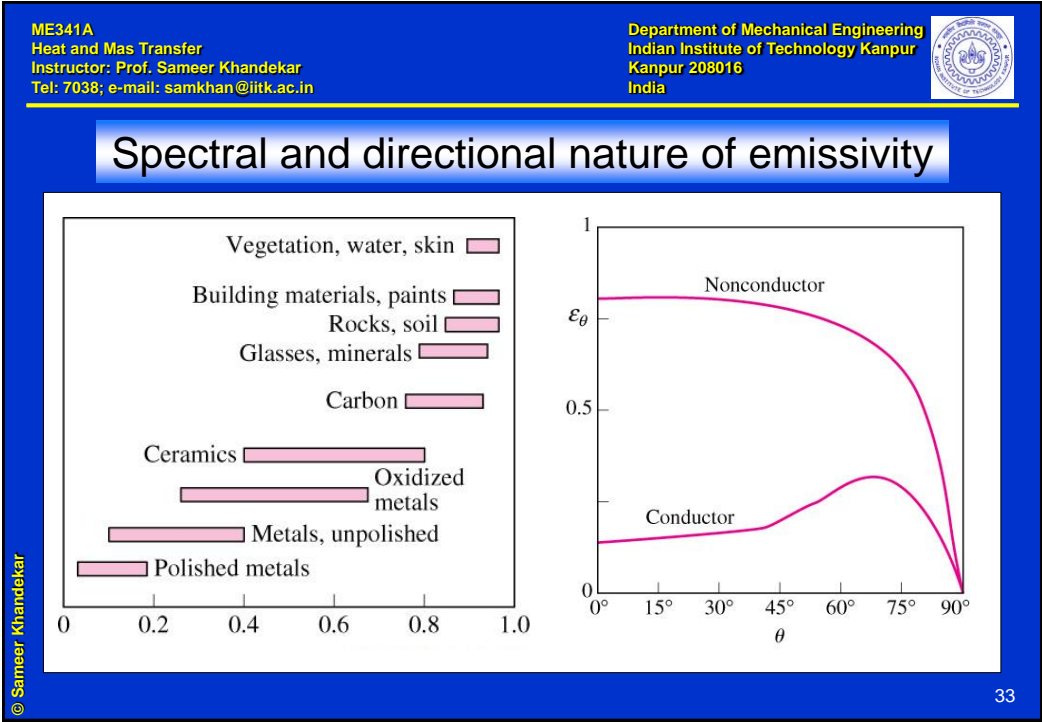
(a)



(b)

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Real surfaces: Diffuse and Grey approximations

Real surface:
 $\epsilon_\theta \neq \text{constant}$
 $\epsilon_\lambda \neq \text{constant}$

Diffuse surface:
 $\epsilon_\theta = \text{constant}$

Gray surface:
 $\epsilon_\lambda = \text{constant}$

Diffuse, gray surface:
 $\epsilon = \epsilon_\lambda = \epsilon_\theta = \text{constant}$

Real materials emit energy at a fraction of black-body energy levels. A black body in thermal equilibrium has an emissivity of $\epsilon = 1.0$.

(a) ϵ_λ vs λ (b) E_λ vs λ

Most first order engineering calculations for radiation are done with this assumption

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Real or Gray Bodies/surfaces

- Real materials emit energy at a fraction of black-body energy levels.
- By definition, a black body in thermal equilibrium has an emissivity of $\epsilon = 1.0$.
- A source with lower emissivity independent of frequency is often referred to as a **gray body**


Monochromatic Emissive Power E_λ in $\text{W/m}^2 \mu\text{m}$ vs Wavelength λ in μm

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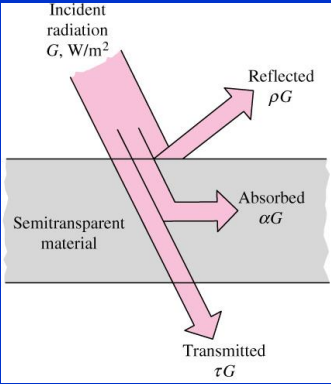
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Absorptivity, Reflectivity and Transmissivity



Semi-Transparent Material

$$\alpha = \frac{\text{Absorbed radiation}}{\text{Incident radiation}} = \frac{G_{abs}}{G} \mid (0 \leq \alpha \leq 1)$$
$$\rho = \frac{\text{Reflected radiation}}{\text{Incident radiation}} = \frac{G_{ref}}{G} \mid (0 \leq \rho \leq 1)$$
$$\tau = \frac{\text{Transmitted radiation}}{\text{Incident radiation}} = \frac{G_{tran}}{G} \mid (0 \leq \tau \leq 1)$$
$$G_{abs} + G_{ref} + G_{tran} = G \quad \text{For opaque surfaces:}$$

Hence $\alpha + \rho = 1$


$$\alpha + \rho + \tau = 1$$

Here too, we can define spectral, directional, total, hemispherical (four types) of quantities

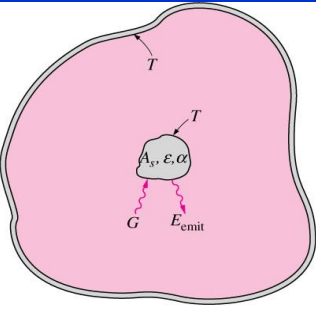
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Kirchhoff's law



The small body contained in a large isothermal enclosure used in the development of Kirchhoff's law.

The total hemispherical emissivity of a surface at temperature T is equal to its total hemispherical absorptivity for radiation coming from a black body at the same temperature.


- The radiation incident on any part of the surface of the small body is equal to the radiation emitted by a black body at temperature T .
- Hence, $G = E_b(T) = \sigma T^4$
- $G_{abs} = \alpha G = \alpha \cdot \sigma T^4$
- The radiation emitted by the small body is $E_{emit} = \epsilon \cdot \sigma T^4$

Considering that the small body is in thermal equilibrium with the enclosure, applying energy equation, we get $\epsilon(T) = \alpha(T)$.

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End of Lecture

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