

Polymeric Structure



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Contents

- ✓ Concept of molecular weight
- ✓ Chemistry of polymers
- ✓ % Crystallinity
- ✓ Tacticity in polymers



Molecular Weight

- The molecular weight distribution is **important in thermoplastics**.
- In **thermosets**, a gelled network of essentially **infinite molecular weight** is formed, so the idea of a "molecular weight distribution" is **non-sensical**.

Two ways:-

- a) Number average molecular weight (M_n): **Total weight of all the polymer molecules in a sample, divided by the total number of polymer molecules in a sample.**

$$\text{Number average molecular weight, } \overline{M}_n = \frac{\sum M_i N_i}{\sum N_i}$$

Where, M_i = molecular weight of i_{th} polymer chain;
 N_i = number of chains of that molecular weight.

- b) Weighted average molecular weight (M_w): **It's based on the fact that a bigger molecule contains more of the total mass of the polymer sample than the smaller molecules do.**

$$\text{Weighted average molecular weight, } \overline{M}_w = \frac{\sum M_i^2 N_i}{\sum M_i N_i}$$

More appropriate



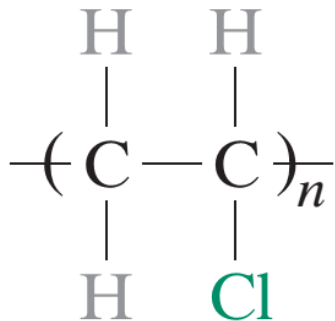
Degree of Polymerization

$$DP = \frac{\bar{M}_n}{m}$$

where, \bar{M}_n = Number average molecular weight
 m = repeat unit molecular weight (no. of atoms x atomic wt.)

Example: Suppose for **Polyvinyl chloride**, $\bar{M}_n = 21,150$ g/mol
 Then, repeat unit molecular weight, $m = 2 \times 12 + 3 \times 1 + 1 \times 35$
 $= 62$ g/mol

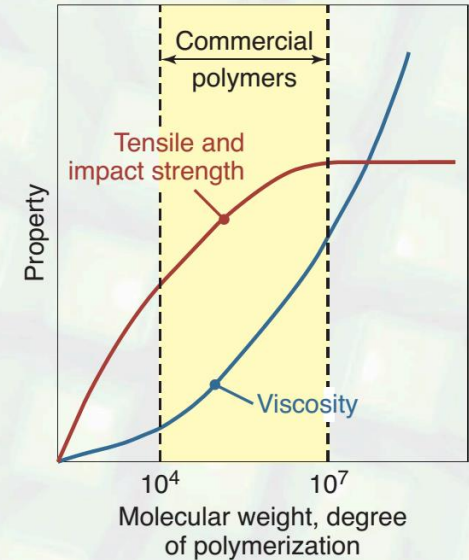
$$DP = \frac{21,150}{62} = 341$$



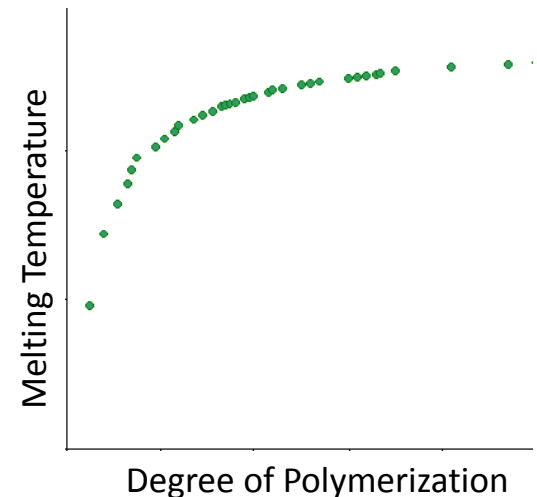
PVC

Repeat unit contains – 2 carbon, 3 hydrogen and 1 chlorine atom

Effect of Molecular Weight



Reference: Kalpakjian, Schmid - Manufacturing Processes for Engineering Materials, 5th ed.

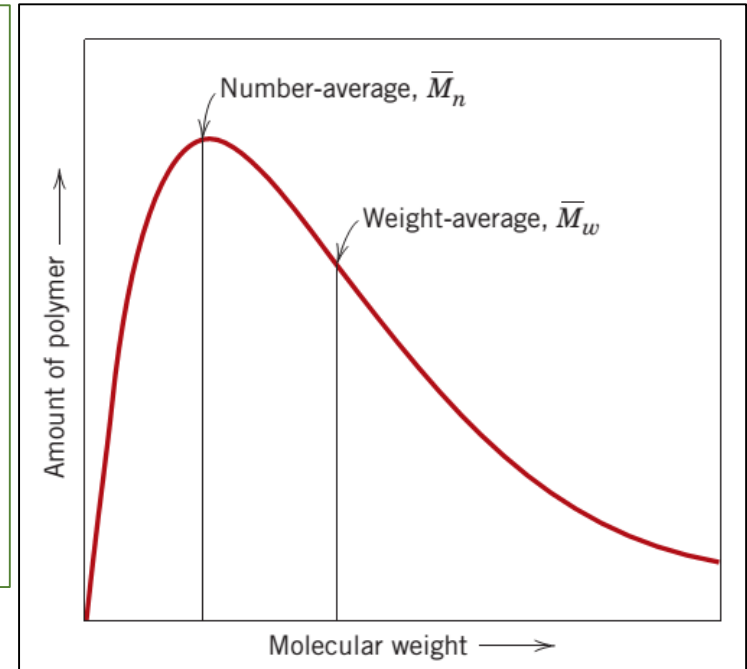


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Polydispersity Index

$$\text{Polydispersity index, PI} = \frac{M_w}{M_n}$$

- The larger the polydispersity index, the broader the molecular weight.
- Monodisperse polymer, where all the chain lengths are equal (such as a protein) has an $\text{PI} = 1$.
- Step polymerization reactions typically yield values of $\text{PI} \approx 2.0$
- Chain polymerization reactions yield values between $\text{PI} = 1.5 - 20$.



Distribution of molecular weights for a typical polymer



Example

No. of molecules (N_i)	Mass of each molecule (M_i) (g/mol)	Total mass of each type of molecule, ($N_i M_i$) in g/mol	$M_i^2 N_i$
1	800,000	800,000	6.4×10^{11}
3	750,000	2250,000	16.8×10^{11}
5	700,000	3500,000	24.5×10^{11}
8	650,000	5200,000	33.8×10^{11}
10	600,000	6000,000	36×10^{11}
13	550,000	7150,000	39.3×10^{11}
20	500,000	10,000,000	50×10^{11}
13	450,000	5850,000	26.3×10^{11}
10	400,000	4000,000	16×10^{11}
8	350,000	2800,000	98×10^{11}
5	300,000	1500,000	4.5×10^{11}
3	250,000	750,000	18.75×10^{11}
1	200,000	200,000	0.4×10^{11}
$\sum N_i = 100$		$\sum M_i N_i = 50,000,000$ (Total mass)	$\sum M_i^2 N_i = 370.75 \times 10^{11}$

$$\text{Number average molecular weight, } \overline{M}_n = \frac{\sum M_i N_i}{\sum N_i}$$

$$= \frac{50,000,000}{100} = 500,000 \text{ g/mol}$$

$$\text{Weighted average molecular weight, } \overline{M}_w = \frac{\sum M_i^2 N_i}{\sum M_i N_i}$$

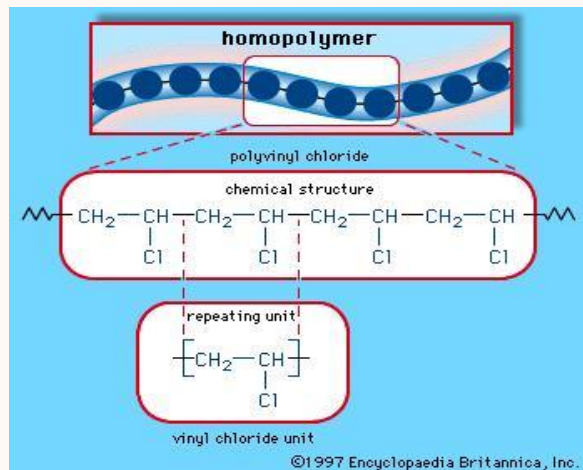
$$= \frac{370.75 \times 10^{11}}{50,000,000} = 741,500 \text{ g/mol}$$

$$\text{Polydispersity index, } PI = \frac{M_w}{M_n} = 1.48$$

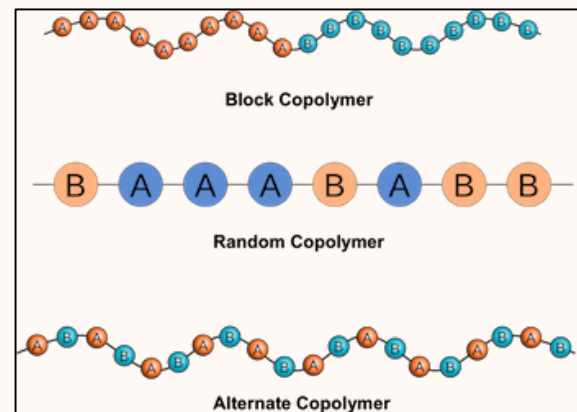


Chemistry of Polymer molecules

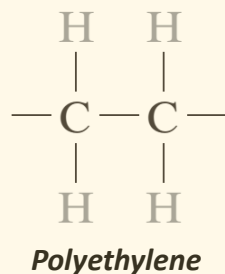
- When all the mers are the same, the molecule is called a **Homo-polymer**.



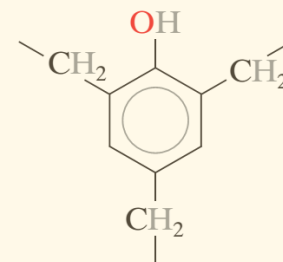
- When there is more than one type of mer present, the molecule is a **Co-polymer**.



- Mer units that have **2 active bonds** to connect with **other mers** are called **bi-functional**.



- Mer units that have **3 active bonds** to connect with other mers are called **tri-functional**. They form 3-D molecular network structures.

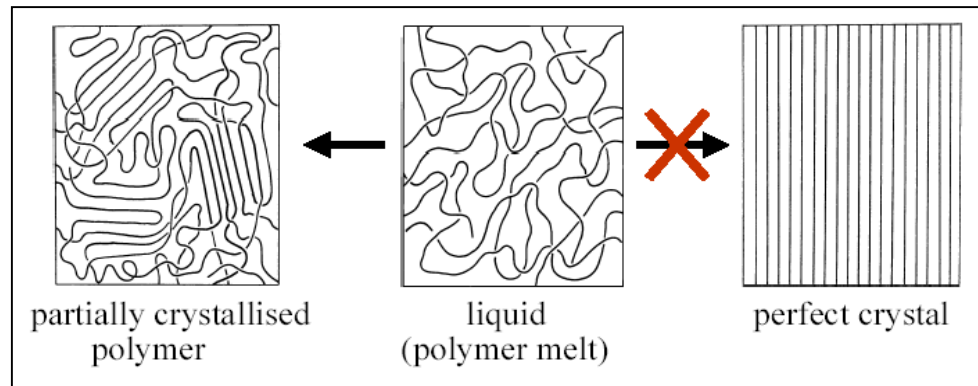


Phenol-formaldehyde (Bakelite)



Possible Physical States for Polymer Materials

Traditional classification of physical states (gases, liquids, crystals) is not informative for polymer materials.

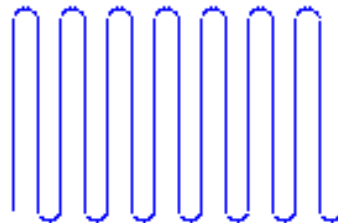
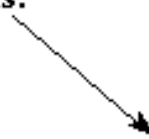


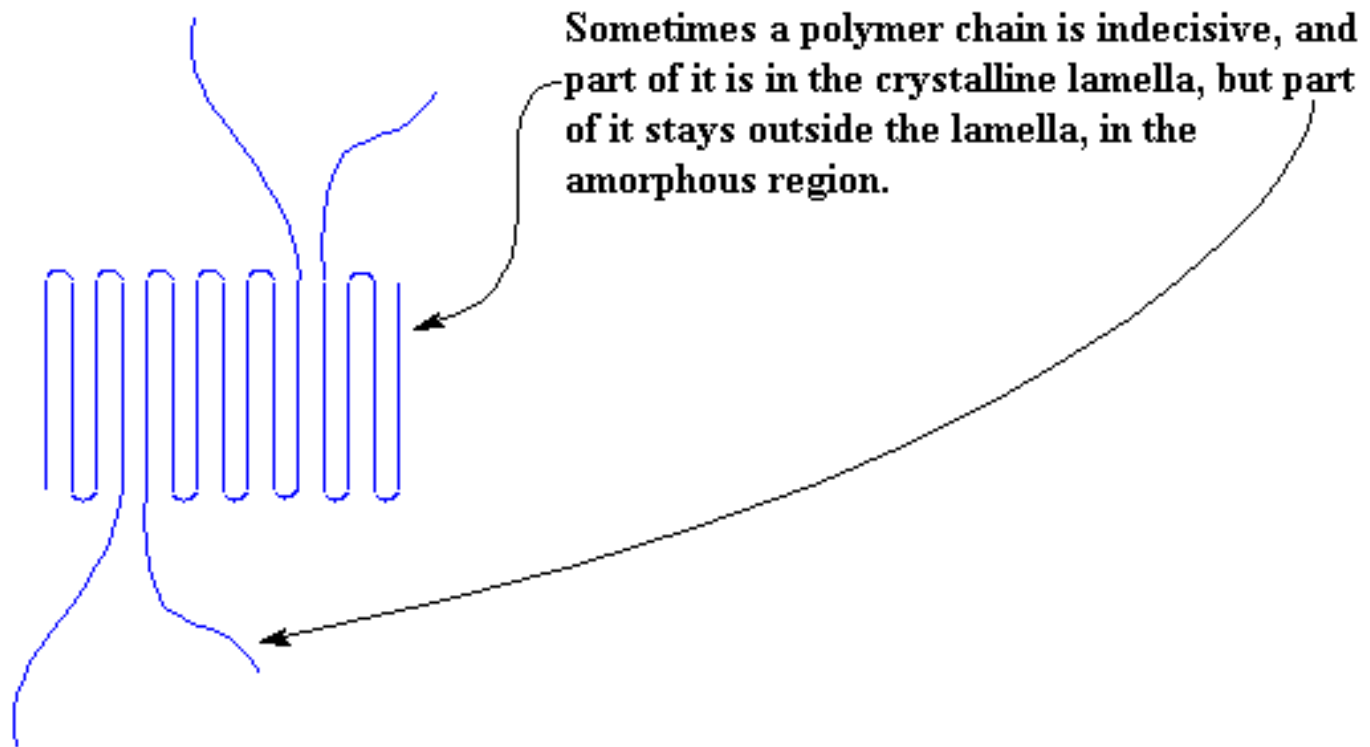
Classification of polymer materials:-

- ❖ Partially crystalline state
- ❖ Viscoelastic State (polymer melt)
- ❖ Highly elastic state (e.g. Rubbers)
- ❖ Glassy state (e.g. Organic glasses from poly(styrene), poly(methylmethacrylate), poly(vinyl chloride))

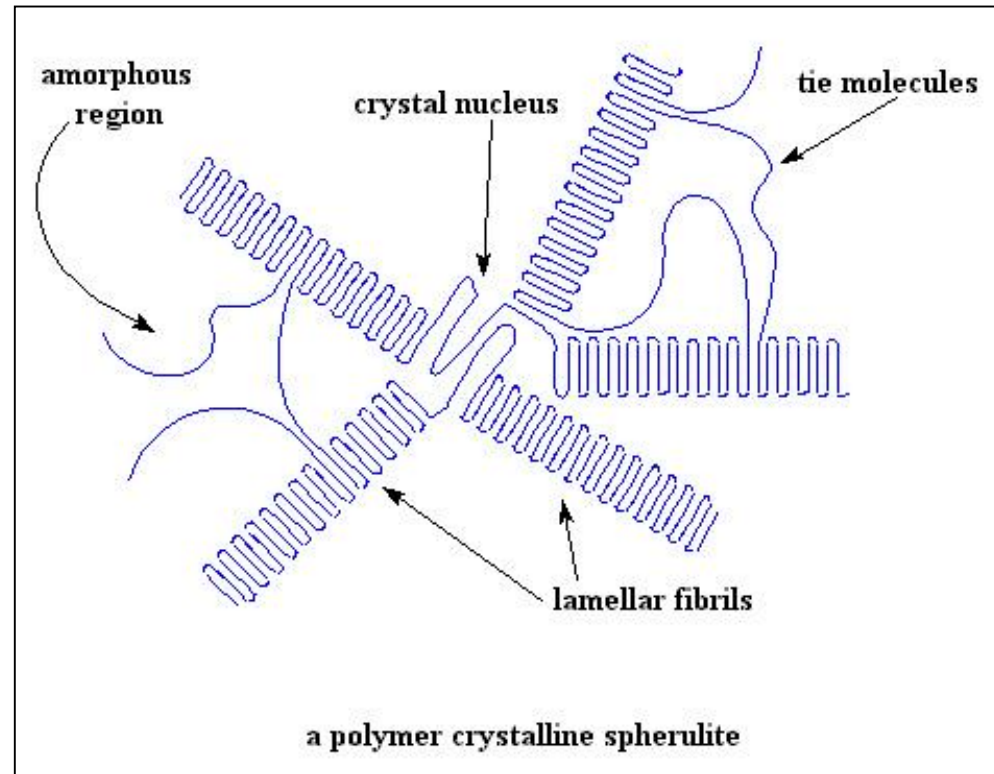


Most polymers don't stretch out fully, like this. Instead, they fold back on themselves after going straight for a short distance, like this.





- ✓ Lamella grow like the spokes of a bicycle wheel from a central nucleus.
- ✓ The whole assembly is called a *Spherulite*. In a sample of a crystalline polymer weighing only a few grams, there are many billions of Spherulites.



Crystallinity

Crystalline region: Orderly arrangement of molecular chains.

- ✓ **High crystallinity** means - **higher density, more strength, higher resistance** to both dissolution and softening by heating.

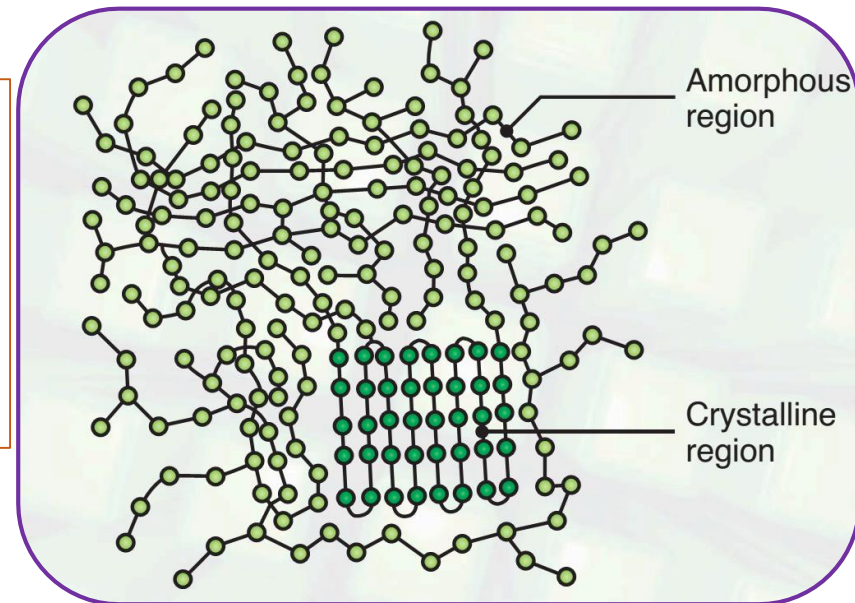
Degree of crystallinity in Polymers

- Ranges from completely amorphous to about 95% crystalline.
- Metal specimens are almost always entirely crystalline.
- Ceramics are either totally crystalline or totally non-crystalline.

For same material & molecular weight

$$\rho_{\text{crystalline polymer}} > \rho_{\text{amorphous polymer}}$$

(due to close packing)



Remember: No polymer is 100% crystalline

Reference: Kalpakjian, Schmid - Manufacturing Processes for Engineering Materials, 5th ed.



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Crystallinity dependence

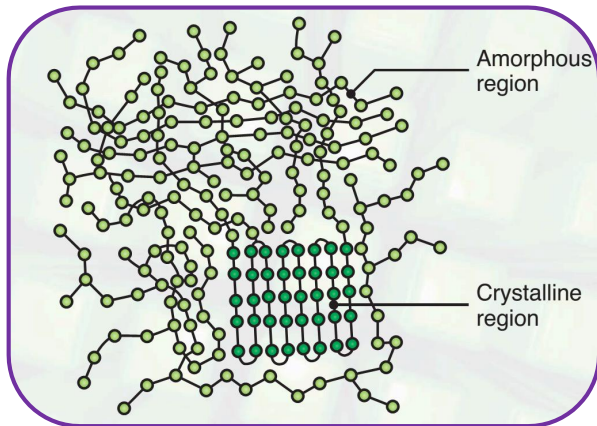
Degree of crystallinity is affected by:-

✓ **Rate of cooling during solidification**

- More the rapid cooling – lesser the time for alignment – poorer the crystallinity.

✓ **Chain configuration**

- More the side branching & cross linking - more the restriction to prevent the chain alignment – lesser the crystallinity .
- Thus, linear polymer have high degree of crystallinity.
- Most network and crosslinked polymers are almost totally amorphous.



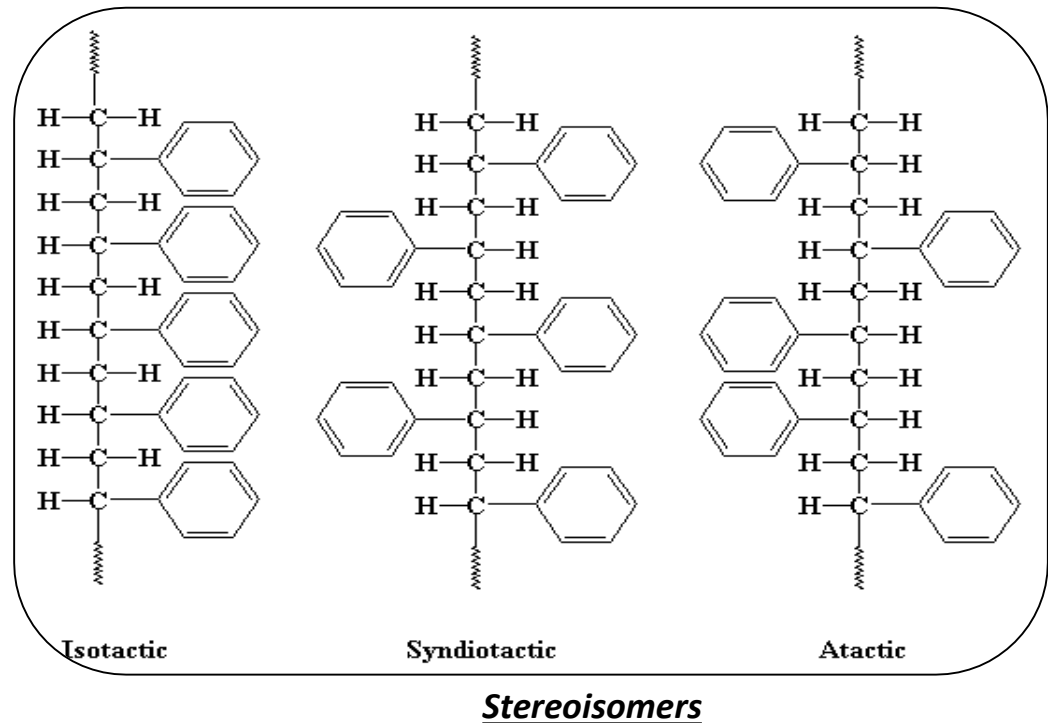
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Tacticity in Polymers

- ✓ Different atomic configurations for the same composition.
- ✓ Tacticity is the way pendant groups are arranged along the backbone chain of a polymer.
- ✓ Isotactic & Syndiotactic – **regular geometry facilitates** fitting of adjacent chain, thus **more crystalline**.
- ✓ **Atactic** – Poorly Crystalline due to **irregularity of side group**.
- ✓ Also, larger the side-bonded groups of atoms - the less is the tendency for crystallization.



Some Highly Crystalline Polymers:

- ✓ Polypropylene
- ✓ Syndiotactic polystyrene
- ✓ Nylon
- ✓ Kevlar and Nomex

Some Highly Amorphous Polymers

- ✓ Poly(methyl-methacrylate), PMMA
- ✓ Atactic polystyrene
- ✓ Polycarbonate
- ✓ Polyisoprene



% Crystallinity

$$\% \text{ Crystallinity} = \frac{\rho_c(\rho_s - \rho_a)}{\rho_s(\rho_c - \rho_a)} \times 100$$

where, ρ_s : Density of specimen

ρ_a : Density of the totally amorphous polymer,

ρ_c : Density of the perfectly crystalline polymer

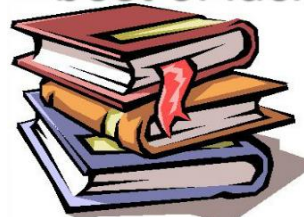
The values of ρ_s , ρ_a and ρ_c are measured by experimental means.



In the **next lecture**, we will learn about:

- ✓ Glass Transition temperature (T_g)
- ✓ Experimental methods to determine T_g
- ✓ Factors affecting T_g

best of luck



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