

Our aim in the ME623A workshops is to develop a general purpose framework for a Finite Element code in Matlab. The code needs to be structured in a manner so as to take optimum advantage of the generality of the FE structure. This requires a bit of programming discipline.

The following functions, to be coded in Matlab, are designed to guide you to a working code, that, though not completely general, is adequate for solving a large variety of linear elastic problems in 1, 2, or 3 dimensions. All variables described herein are in *italics* and functions are in **typewriter** fonts. Maintain the size of all variables exactly as directed below. The code will be developed over many sessions and a mistake now will lead to trouble later.

We will suggest verification problems that will be useful for checking if a function that you have written actually works properly. Remember a few thumb rules:

1. Never trust your own code, always try to devise problems that can be used to crash test it. You should always try to make your own function crash under some input. Devising problems to test a function that you have written, so as to check when it fails, is one of the most challenging jobs in FE coding.
2. Follow the array dimensions carefully.
3. Insert checks on values based on physical considerations, eg. number of space dimensions cannot be more than 3. An error should be thrown up by the code if the user tries to enter 4.

Here are the steps that we will have to accomplish.

Step 1: The basic variables in a linear elastic FE code are

- (a) Number of nodes in the system: *nnode*
- (b) Number of elements in the system: *nelem*
- (c) Number of different materials in the system: *nmat*
- (d) Number of degrees of freedom per node: *ndof*
- (e) Number of nodes per element: *nperlm*
- (f) Number of space dimensions: *ndim*

Step 2: Input data for an entire analysis is generally read in from a text file. All input data resides in a single text file. This includes nodal coordinates, element connectivity and material property information, input material properties, boundary conditions (free or fixed), boundary condition values, etc. It is a good idea to design your input file such that it has separate sections for each type of data. The task in this step is to

- (a) Design an input file. Decide what goes where, eg. you may first have all nodal coordinates, followed by element connectivity, followed by material properties, nodal forces and then boundary conditions. Remember that you may have to read in more things later. Also remember,
 - i. node numbers will go from 1 : *nnode* and element numbers from 1 : *nelem*.
 - ii. there will be *ndim* values of coordinates for each node
 - iii. there will be *nperlm* values for nodes connected to each element. Also, you might want to read in the material number which the element is made up of, which goes from 1 : *nmat*.
 - iv. boundary conditions can be specified (as zero or non-zero) for all 1 : *nnode* nodes for 1 : *ndof* degrees of freedom. However, only a few nodes will have boundary conditions. The same holds for external forces.
 - v. We will have to input material properties of all 1 : *nmat* + 1 materials in the system. The first entry for each material is the type *mat_type_number*, followed by the values of the requisite properties. Each of these material types will require some number of material constants to be specified. For example, if you have a linear elastic isotropic material you will have to specify E, ν for it, while if an element is a spring element, you specify only one material property, its stiffness. Each material type (eg. for linear elastic, truss, beam bending etc) will be given an unique *mat_type_number*. We will assume that it goes from 1 : 7 i.e. we can have a maximum of seven different material types.

- vi. Thus, you will have to design what is known as a ‘material library’. It is a function that is of the form

$$[num_mat_data] = \text{mat_lib}(mat_type_number)$$

Here *num_mat_data* is the number of data entries that should be read in for a given *mat_type_number*. For instance, if *mat_type_number* = 1 denotes a linear elastic isotropic material, then *num_mat_data* = 2. For transversely isotropic material, it is 5.

- (b) Write a function that has the following structure:

$$[x, conn, bound, force, mate] = \text{read_input}(nnode, nelem, nmat, ndof, nperlm, ndim)$$

Here the output variables are:

- i. *x*(1 : *nnode*, 1 : *ndim*): array containing nodal coordinates
 - ii. *conn*(1 : *nelem*, 1 : (*nperlm* + 1)): array containing material number associated with an element and nodes connected to it.
 - iii. *bound*(1 : *nnode*, 1 : *ndof*): array containing boundary conditions, a dof is assigned 0 if it is free and 1 if it is fixed.
 - iv. *force*(1 : *nnode*, 1 : *ndof*): if a degree of freedom has specified displacement, it will contain the value of the displacement. If it has a specified force, it will contain the value of the force at that dof. Recall that the same dof cannot have both force and displacement specified.
 - v. *mate*(1 : *nelem*, 1 : *nmat*): material number assigned to an element.
 - vi. *matdata*(1 : *nmat*, 1 : *mat_lib*(*mat_type_number*)): property data for the material type.
- (c) Check. One way could be to write an input file for the truss problem done in the class. Is your code able to read all the information in? Is the information being stored in the arrays as you wanted them to be?