# **Homework-6 Solutions**

**Q 5-76** Hot water stream is mixed with a cold water stream. For a specified mixture temperature, the mass flow rate of cold water is to be determined.

**Assumptions 1** Steady operating conditions exist. **2** The mixing chamber is well-insulated so that heat loss to the surroundings is negligible. **3** Changes in the kinetic and potential energies of fluid streams are negligible. **4** Fluid properties are constant. **5** There are no work interactions.

**Properties** Noting that  $T < T_{\text{sat }@250 \text{ kPa}} = 127.41^{\circ}\text{C}$ , the water in all three streams exists as a compressed liquid, which can be approximated as a saturated liquid at the given temperature. Thus,

$$h_1 \cong h_{f@.80^{\circ}C} = 335.02 \text{ kJ/kg}$$
  
 $h_2 \cong h_{f@.20^{\circ}C} = 83.915 \text{ kJ/kg}$   
 $h_3 \cong h_{f@.42^{\circ}C} = 175.90 \text{ kJ/kg}$ 

**Analysis** We take the mixing chamber as the system, which is a control volume. The mass and energy balances for this steady-flow system can be expressed in the rate form as

Mass balance:

$$\dot{m}_{\rm in} - \dot{m}_{\rm out} = \Delta \dot{m}_{\rm system}^{70 \text{ (steady)}} = 0 \longrightarrow \dot{m}_1 + \dot{m}_2 = \dot{m}_3$$

Energy balance:

$$\underline{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}} = \underbrace{\Delta \dot{E}_{\text{system}}}^{\rlap{$\not$$} 0 \text{ (steady)}}_{\text{Rate of net energy transfer by heat, work, and mass}} = 0$$
Rate of change in internal, kinetic, potential, etc. energies

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

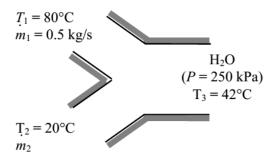
$$\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3 \quad \text{(since } \dot{Q} = \dot{W} = \Delta \text{ke} \cong \Delta \text{pe} \cong 0)$$

Combining the two relations and solving for  $\dot{m}_2$  gives

$$\dot{m}_1 h_1 + \dot{m}_2 h_2 = (\dot{m}_1 + \dot{m}_2) h_3$$
$$\dot{m}_2 = \frac{h_1 - h_3}{h_3 - h_2} \dot{m}_1$$

Substituting, the mass flow rate of cold water stream is determined to be

$$\dot{m}_2 = \frac{(335.02 - 175.90) \text{ kJ/kg}}{(175.90 - 83.915) \text{ kJ/kg}} (0.5 \text{ kg/s}) = \mathbf{0.865} \text{ kg/s}$$



### **Q** 5-120

An evacuated bottle is surrounded by atmospheric air. A valve is opened, and air is allowed to fill the bottle. The amount of heat transfer through the wall of the bottle when thermal and mechanical equilibrium is established is to be determined.

**Assumptions:** 1 This is an unsteady process since the conditions within the device are changing during the process, but it can be analyzed as a uniform-flow process since the state of fluid at the inlet remains constant. 2 Air is an ideal gas with variable specific heats. 3 Kinetic and potential energies are negligible. 4 There are no work interactions involved. 5 The direction of heat transfer is to the air in the bottle (will be verified).

**Properties:** The gas constant of air is 0.287 kPa.m3/kg.K (Table A-1).

**Analysis:** We take the bottle as the system, which is a control volume since mass crosses the boundary. Noting that the microscopic energies of flowing and non-flowing fluids are represented by enthalpy h and internal energy u, respectively, the mass and energy balances for this uniform-flow system can be expressed as

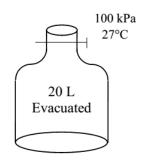
Mass balance:

$$m_{\rm in} - m_{\rm out} = \Delta m_{\rm system} \rightarrow m_i = m_2 \quad (\text{since } m_{\rm out} = m_{\rm initial} = 0)$$

Energy balance:

$$\underbrace{E_{\text{in}} - E_{\text{out}}}_{\text{Net energy transfer}} = \underbrace{\Delta E_{\text{system}}}_{\text{Change in internal, kinetic, potential, etc. energies}}$$

$$Q_{\text{in}} + m_i h_i = m_2 u_2 \quad (\text{since } W \cong E_{\text{out}} = E_{\text{initial}} = ke \cong pe \cong 0)$$



Combining the two balances:

$$Q_{\rm in} = m_2 (u_2 - h_i)$$

where

$$m_2 = \frac{P_2 V}{RT_2} = \frac{(100 \text{ kPa})(0.020 \text{ m}^3)}{(0.287 \text{ kPa} \cdot \text{m}^3/\text{kg} \cdot \text{K})(300 \text{ K})} = 0.02323 \text{ kg}$$

$$T_i = T_2 = 300 \text{ K} \xrightarrow{\text{Table A-17}} \frac{h_i = 300.19 \text{ kJ/kg}}{u_2 = 214.07 \text{ kJ/kg}}$$

Substituting,

$$Q_{\text{in}} = (0.02323 \text{ kg})(214.07 - 300.19) \text{ kJ/kg} = -2.0 \text{ kJ}$$

or

$$Q_{\text{out}} = 2.0 \text{ kJ}$$

**Discussion** The negative sign for heat transfer indicates that the assumed direction is wrong. Therefore, we reverse the direction.

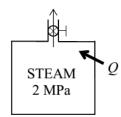
### **Q** 5-122

A rigid tank initially contains superheated steam. A valve at the top of the tank is opened, and vapor is allowed to escape at constant pressure until the temperature rises to 500°C. The amount of heat transfer is to be determined.

Assumptions 1 This is an unsteady process since the conditions within the device are changing during the process, but it can be analyzed as a uniform-flow process by using constant average properties for the steam leaving the tank. 2 Kinetic and potential energies are negligible. 3 There are no work interactions involved. 4 The direction of heat transfer is to the tank (will be verified).

**Properties** The properties of water are (Tables A-4 through A-6)

$$\begin{split} P_1 &= 2 \text{ MPa} \quad \big\} \; \boldsymbol{v}_1 = 0.12551 \, \text{m}^3/\text{kg} \\ T_1 &= 300 \, ^{\circ}\text{C} \quad \big\} \; u_1 = 2773.2 \, \text{kJ/kg}, \quad h_1 = 3024.2 \, \text{kJ/kg} \\ P_2 &= 2 \, \text{MPa} \quad \big\} \; \boldsymbol{v}_2 = 0.17568 \, \text{m}^3/\text{kg} \\ T_2 &= 500 \, ^{\circ}\text{C} \quad \big\} \; u_2 = 3116.9 \, \text{kJ/kg}, \quad h_2 = 3468.3 \, \text{kJ/kg} \end{split}$$



**Analysis:** We take the tank as the system, which is a control volume since mass crosses the boundary. Noting that the microscopic energies of flowing and non-flowing fluids are represented by enthalpy h and internal energy u, respectively, the mass and energy balances for this uniformflow system can be expressed as

Mass balance:

$$m_{\rm in} - m_{\rm out} = \Delta m_{\rm system} \rightarrow m_e = m_1 - m_2$$

Energy balance:

$$\begin{array}{ll} E_{\rm in} - E_{\rm out} &= \Delta E_{\rm system} \\ \text{Net energy transfer} \\ \text{by heat, work, and mass} & \text{Change in internal, kinetic,} \\ Q_{\rm in} - m_e h_e &= m_2 u_2 - m_1 u_1 \text{ (since } W \cong ke \cong pe \cong 0) \end{array}$$

The state and thus the enthalpy of the steam leaving the tank is changing during this process. But for simplicity, we assume constant properties for the exiting steam at the average values. Thus,

$$h_e \cong \frac{h_1 + h_2}{2} = \frac{3024.2 + 3468.3 \text{ kJ/kg}}{2} = 3246.2 \text{ kJ/kg}$$

The initial and the final masses in the tank are

$$m_1 = \frac{\mathbf{V}_1}{\mathbf{v}_1} = \frac{0.2 \text{ m}^3}{0.12551 \text{ m}^3/\text{kg}} = 1.594 \text{ kg}$$
  
 $m_2 = \frac{\mathbf{V}_2}{\mathbf{v}_2} = \frac{0.2 \text{ m}^3}{0.17568 \text{ m}^3/\text{kg}} = 1.138 \text{kg}$ 

Then from the mass and energy balance relations,

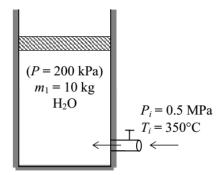
$$m_e = m_1 - m_2 = 1.594 - 1.138 = 0.456 \text{ kg}$$
  
 $Q_{in} = m_e h_e + m_2 u_2 - m_1 u_1$   
 $= (0.456 \text{ kg})(3246.2 \text{ kJ/kg}) + (1.138 \text{ kg})(3116.9 \text{ kJ/kg}) - (1.594 \text{ kg})(2773.2 \text{ kJ/kg})$   
 $= 606.8 \text{ kJ}$ 

## O 5-123

Assumptions 1 This is an unsteady process since the conditions within the device are changing during the process, but it can be analyzed as a uniform-flow process since the state of fluid at the inlet remains constant. 2 The expansion process is quasi-equilibrium. 3 Kinetic and potential energies are negligible. 3 There are no work interactions involved other than boundary work. 4 The device is insulated and thus heat transfer is negligible.

**Properties** The properties of steam are (Tables A-4 through A-6)

$$\begin{split} P_1 &= 200 \text{ kPa} \\ x_1 &= 0.6 \end{split} \} h_1 = h_f + x_1 h_{fg} \\ &= 504.71 + 0.6 \times 2201.6 = 1825.6 \text{ kJ/kg} \\ P_2 &= 200 \text{ kPa} \\ \text{sat. vapor} \end{split} \} h_2 = h_{g@200 \text{ kPa}} = 2706.3 \text{ kJ/kg} \\ P_i &= 0.5 \text{ MPa} \\ T_i &= 350 ^{\circ} \text{C} \end{split} \} h_i = 3168.1 \text{ kJ/kg} \end{split}$$



*Analysis* (a) The cylinder contains saturated vapor at the final state at a pressure of 200 kPa, thus the final temperature in the cylinder must be

$$T_2 = T_{\text{sat } @ 200 \text{ kPa}} = 120.2 ^{\circ}\text{C}$$

(b) We take the cylinder as the system, which is a control volume since mass crosses the boundary. Noting that the microscopic energies of flowing and non-flowing fluids are represented by enthalpy h and internal energy u, respectively, the mass and energy balances for this uniform-flow system can be expressed as

Mass balance: 
$$m_{\text{in}} - m_{\text{out}} = \Delta m_{\text{system}} \rightarrow m_i = m_2 - m_1$$

Energy balance:

$$\underbrace{E_{\text{in}} - E_{\text{out}}}_{\text{Net energy transfer}} = \underbrace{\Delta E_{\text{system}}}_{\text{Change in internal, kinetic, potential, etc. energies}}$$

$$m_i h_i = W_{\text{b.out}} + m_2 u_2 - m_1 u_1 \text{ (since } Q \cong ke \cong pe \cong 0)$$

Combining the two relations gives

$$0 = W_{\text{b,out}} - (m_2 - m_1)h_i + m_2u_2 - m_1u_1$$

or,

$$0 = -(m_2 - m_1)h_i + m_2h_2 - m_1h_1$$

since the boundary work and  $\Delta U$  combine into  $\Delta H$  for constant pressure expansion and compression processes. Solving for  $m_2$  and substituting,

$$m_2 = \frac{h_i - h_1}{h_i - h_2} m_1 = \frac{(3168.1 - 1825.6) \text{ kJ/kg}}{(3168.1 - 2706.3) \text{ kJ/kg}} (10 \text{ kg}) = 29.07 \text{ kg}$$

Thus,

$$m_i = m_2 - m_1 = 29.07 - 10 = 19.07 \text{ kg}$$

#### **Q 5-140**

**Assumptions 1** This is an unsteady process since the conditions within the device are changing during the process, but it can be analyzed as a uniform-flow process assuming that the state of fluid leaving the device remains constant. **2** Kinetic and potential energies are negligible.

**Properties** The initial properties of R-134a are (Tables A-11 through A-13)

$$P_1 = 1.2 \text{ MPa}$$
  
 $T_1 = 120 ^{\circ}\text{C}$   $\begin{cases} v_1 = 0.02423 \text{ m}^3/\text{kg} \\ u_1 = 325.03 \text{ kJ/kg} \\ h_1 = 354.11 \text{ kJ/kg} \end{cases}$ 

**Analysis:** We take the tank as the system, which is a control volume since mass crosses the boundary. Noting that the microscopic energies of flowing and non-flowing fluids are represented by enthalpy h and internal energy u, respectively, the mass and energy balances for this uniform-flow system can be expressed as

Mass balance: 
$$m_{\rm in} - m_{\rm out} = \Delta m_{\rm system} \rightarrow m_e = m_1 - m_2$$

Energy balance:

$$\underbrace{E_{\text{in}} - E_{\text{out}}}_{\text{Net energy transfer}} = \underbrace{\Delta E_{\text{system}}}_{\text{Change in internal, kinetic, potential, etc. energies}}$$

$$\underbrace{C_{\text{hange in internal, kinetic, potential, etc. energies}}_{\text{potential, etc. energies}}$$

$$\underbrace{W_{\text{hin}} - m_e h_e}_{\text{e}} = m_2 u_2 - m_1 u_1 \text{ (since } Q \cong ke \cong pe \cong 0)}_{\text{out}}$$

The initial mass and the relations for the final and exiting masses are

$$m_1 = \frac{\mathbf{V}_1}{\mathbf{v}_1} = \frac{0.8 \text{ m}^3}{0.02423 \text{ m}^3/\text{kg}} = 33.02 \text{ kg}$$

$$m_2 = \frac{\mathbf{V}_2}{\mathbf{v}_2} = \frac{0.5 \text{ m}^3}{v_2}$$

$$m_e = m_1 - m_2 = 33.02 - \frac{0.5 \text{ m}^3}{v_2}$$



Noting that the spring is linear, the boundary work can be determined from

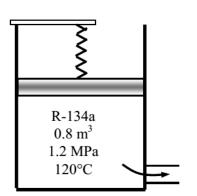
$$W_{\text{b,in}} = \frac{P_1 + P_2}{2} (\mathbf{V}_1 - \mathbf{V}_2) = \frac{(1200 + 600) \text{ kPa}}{2} (0.8 - 0.5) \text{m}^3 = 270 \text{ kJ}$$

Substituting the energy balance,

$$270 - \left(33.02 - \frac{0.5 \,\mathrm{m}^3}{\mathbf{v}_2}\right) h_e = \left(\frac{0.5 \,\mathrm{m}^3}{\mathbf{v}_2}\right) u_2 - (33.02 \,\mathrm{kg})(325.03 \,\mathrm{kJ/kg}) \qquad \text{(Eq. 1)}$$

where the enthalpy of exiting fluid is assumed to be the average of initial and final enthalpies of the refrigerant in the cylinder. That is,

$$h_e = \frac{h_1 + h_2}{2} = \frac{(354.11 \,\text{kJ/kg}) + h_2}{2}$$



Final state properties of the refrigerant (h2, u2, and v2) are all functions of final pressure (known) and temperature (unknown). The solution may be obtained by a trial-error approach by trying different final state temperatures until Eq. (1) is satisfied. Or solving the above equations simultaneously using an equation solver with built-in thermodynamic functions such as EES, we obtain

$$T_2 = 96.8$$
°C,  $m_e = 22.47$  kg,  $h_2 = 336.20$  kJ/kg,  
 $u_2 = 307.77$  kJ/kg,  $v_2 = 0.04739$  m<sup>3</sup>/kg,  $m_2 = 10.55$  kg