ME-231A

Practice Problem Set-3 Answers

P1. (a) m=0.530 kg/s (b) exit area=38.7cm²

P2. (a)
$$\frac{\partial \rho}{\partial t} = -1440 kg / m^3 s$$
 (b) $\rho(t) = \rho_o \left(\frac{1}{1 + Vt / L_o} \right)$

P3. (a) 11/4 (b) 11/4

P4.
$$\vec{V} = \omega r \frac{z}{h} \hat{e}_{\theta}$$

P5. (a) $\psi = -C \ln r + C_1$ (b) $Q = -0.0547 \text{ m}^3/\text{s.m}$

P6.
$$u = U - \left(\frac{\omega \sin \omega t}{2 - \cos \omega t}\right) x$$

P8. (a) $V_y = e^{-x} \sinh y, \psi = e^{-x} \sinh y + y + const$

(b)
$$V_y = V_o \left(\frac{y^2}{ax^2} - \frac{2y^3}{3a^2x^3} \right), \psi = V_o \left(\frac{y^2}{ax} - \frac{y^3}{3a^2x^2} \right) + const$$

P9. (a) Yes (b)
$$p = p_a - \frac{1}{2}\rho(2x^2y^2 + x^4 + y^4)$$

P11.
$$w = \frac{\rho g}{2\mu} (h^2 - x^2)$$

P12. (a)
$$u_x^A = \frac{\mu_B V}{\mu_A H_B + \mu_B H_A} y$$
 (b) $u_x^B = V - \frac{\mu_A V}{\mu_A H_B + \mu_B H_A} (H_A + H_B - y)$

P13. (a)
$$C = \frac{\rho g \sin \theta}{2\mu}$$
 (b) $Q = \frac{\rho g h^3 \sin \theta}{3\mu}$

P14. Velocity profile and Pressure gradient

$$u = -\frac{h^2}{\mu} \frac{dp}{dx} (y - \frac{1}{2}y^2) + \frac{Ch}{\mu} y, \text{ where } y = y/h$$

$$\frac{dp}{dx} = \frac{3}{2} \frac{C}{h}$$

P15. Velocity profile for water and oil are:

$$V_{y,w} = \rho_w g(xh - x^2/2) / \mu_w + \rho_o ghx / \mu_w$$

$$V_{y,o} = \rho_o g (2 xh - x^2 / 2) / \mu_o + \rho_o g h^2 (\frac{1}{2} \mu_o \rho_w / \mu_w \rho_o + \mu_o / \mu_w - \frac{3}{2}) / \mu_o$$

P16. Velocity profile:

$$(\rho g/2\mu) [(R-h)^2 \ln R/r - (R^2-r^2)/2]$$

P17. Velocity profile:

$$(\rho g R^2 / 4\mu) [(1-r^2 / R^2) + 2(R_1 / R)^2 \ln(r / R)]$$

P18. Velocity profile

$$u_{\theta} = \frac{R_i^2 \omega_i}{R_o^2 - R_i^2} \left(\frac{R_o^2}{r} - r \right)$$