

Computer Vision

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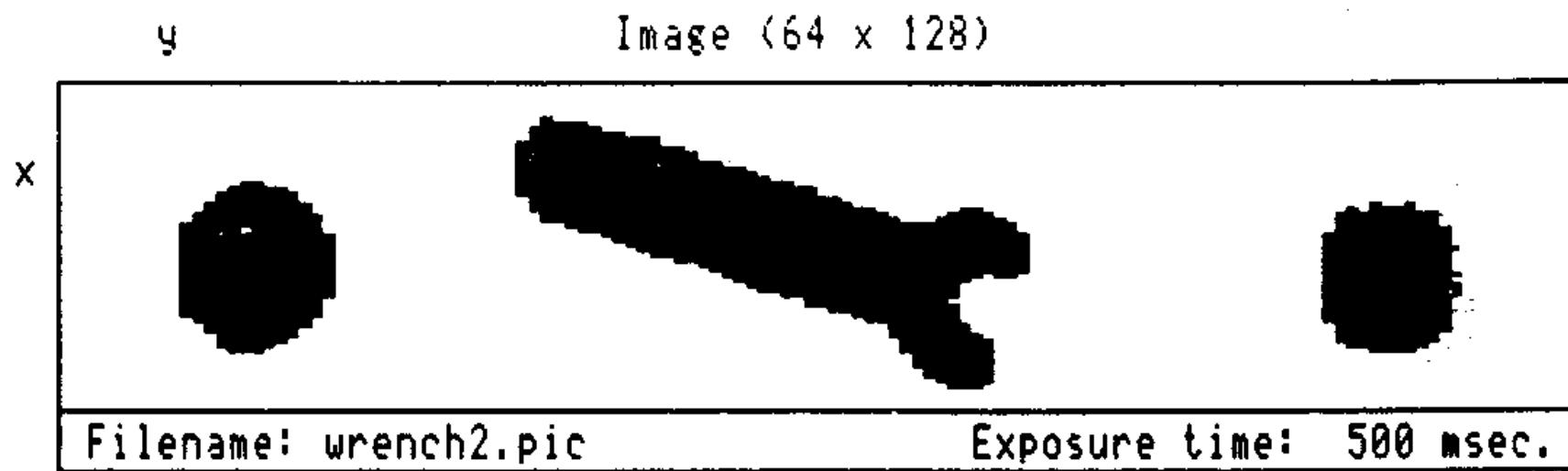
Machine vision, computer vision, vision

- Machine vision is concerned with the sensing of vision data and its interpretation by a computer.
- Three main steps for using vision data:
 - Sensing and digitizing image data.
 - Image processing and analysis
 - Applications

Coordinates of points in space?

- Robot programs need to contain the coordinates of important points e.g. part location, assembly location, location to place a part.
- Locate the part before picking up.
- Inspection of parts.
- Assembly

Find the required part ?



Why Use Vision?

- Cost reduction
- To find randomly placed parts
- To verify part type
- To inspect part
- Affordable
- Maintainable



Robots & Vision vs. People

ACTION	MACHINE	PERSON
Speed	Extremely Fast	Medium
Accuracy	High	Varies
Repeatability	High	Varies
Interpretation	Fixed	High

Applications

- Find locations
- Measure parts
- Verify presence
- Inspections
- Robot guidance

Robotic Vision Process Types

- Fixed camera vision
 - Single camera
 - Multiple cameras
 - High-speed



Robotic Vision Process Types



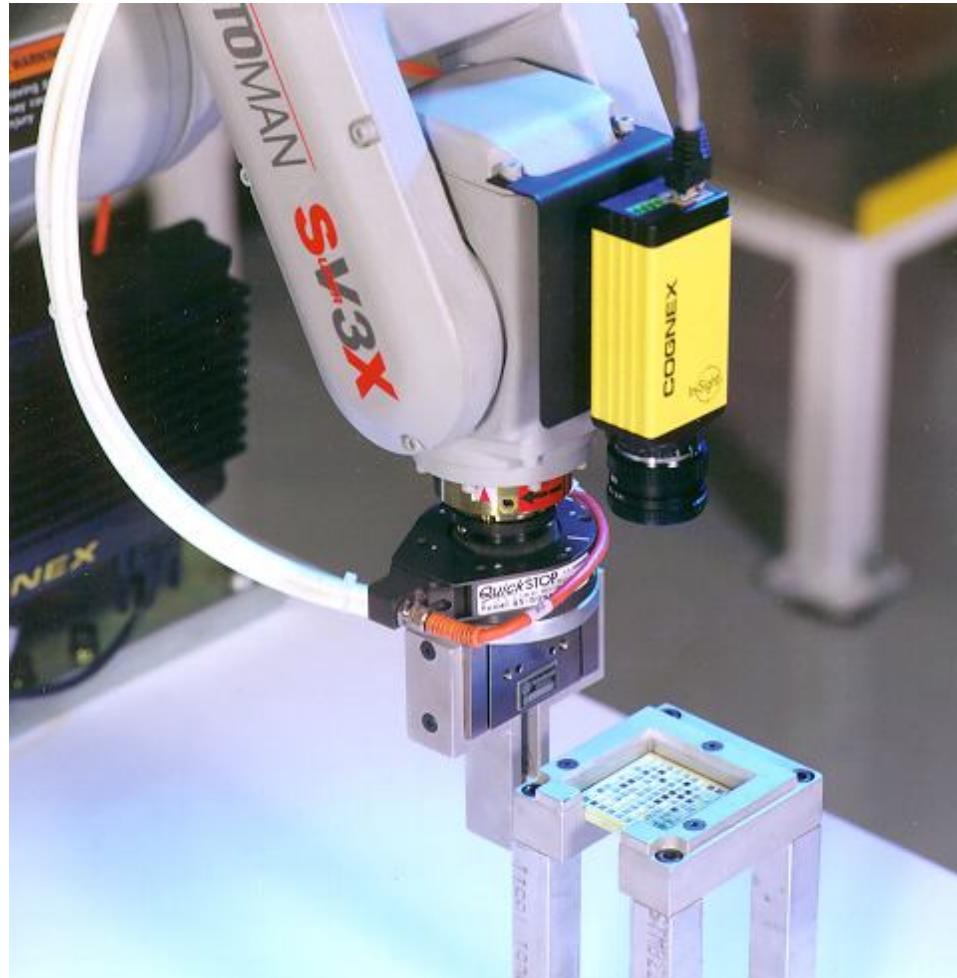
- Robot-mounted vision
 - Single field of view - tight access/multiple parts/clearance
 - Multiple field of view - low cycle time requirements

Flexible Feeding & Conveyor Tracking

- Conveyor-fed parts
- Vision finding
- Part staging for next operation



Part Finding/Inspection



Typical Part

- Task
 - Locate the part and determine:
 - X and Y location
 - Flat on the D hole
 - Place the part on a assembly or shipping tray



Vision Code

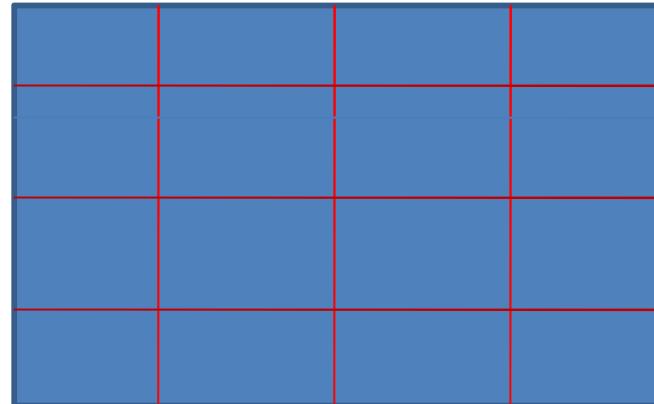
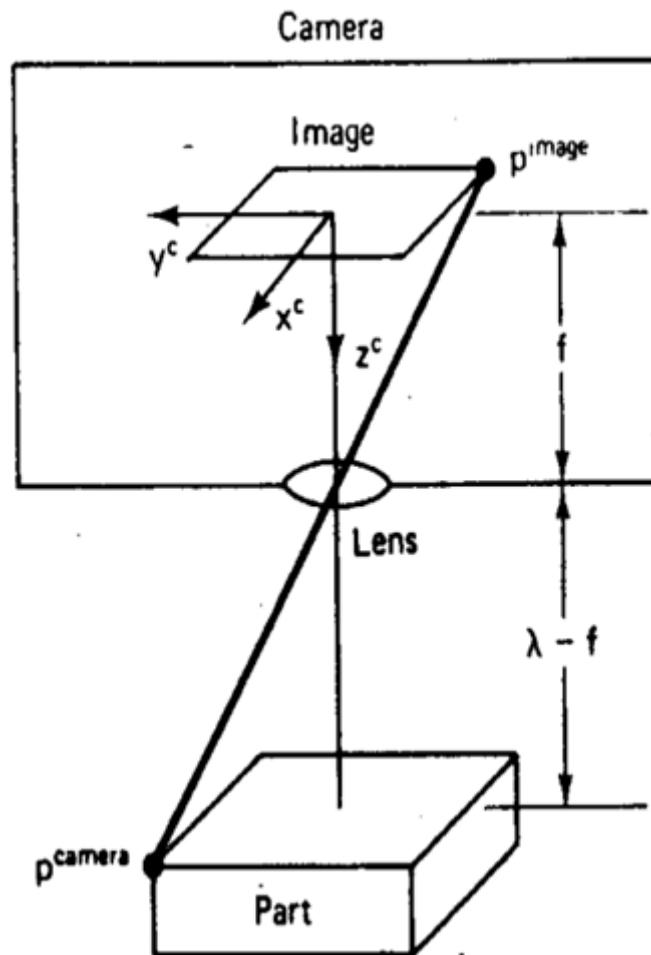
- Tools
 - Cognex Insight
 - Spreadsheet programming
 - Pattern matching
 - Radial rulers
 - Download P-point to controller through RS232 link



Low-cost Vision-based Quality Inspection

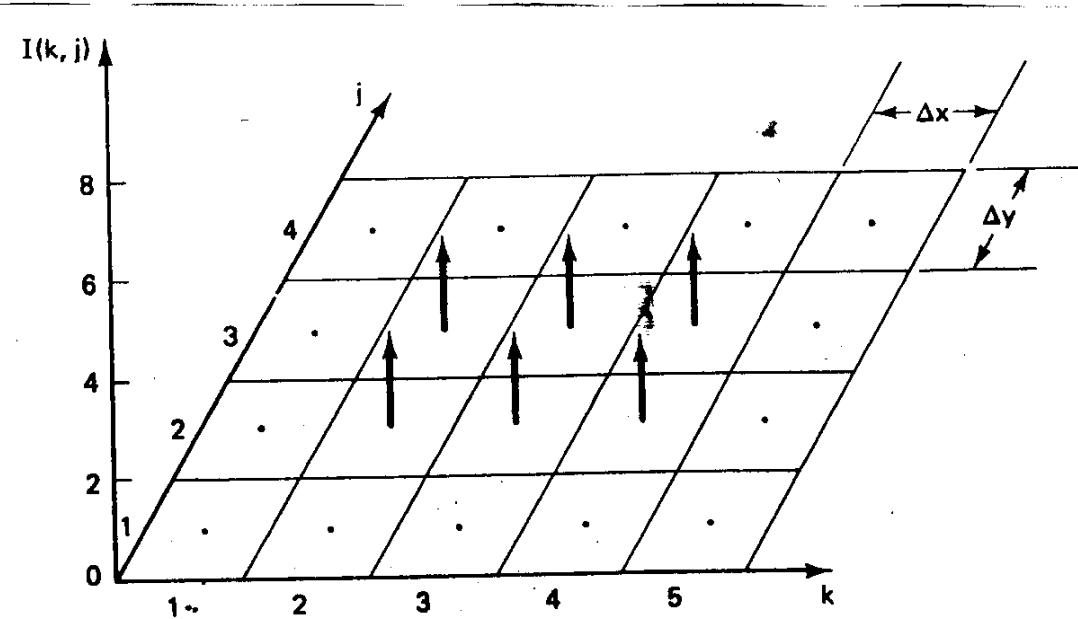
Mithun George Jacob

Working of a camera CCD



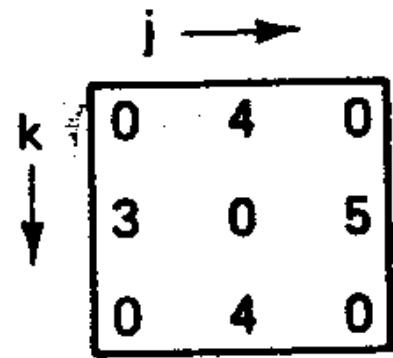
- **Image plane**
- **Each sensing unit is a Pixel**
- **Light can be converted to black/white or colour in each pixel before recording**

CCD Camera



$$I_a(k, j) \triangleq \frac{\int_0^{\Delta x} \int_0^{\Delta y} i[(k - 1)\Delta x + x, (j - 1)\Delta y + y] dy dx}{\Delta x \Delta y}$$

Template matching



$$\rho = \sum_{k=1}^n \sum_{j=i}^n I(k+x, j+y) - T(k, j)$$

		y →		
x ↓				
2	1	0	0	3
0	0	5	0	0
0	4	0	6	0
1	0	5	0	0

Figure 8-4 A 4×5 image.

As the template is 3×3 and the image 4×5 , the possible translations are $0 \leq x \leq 2$ and $0 \leq y \leq 2$. From Eq. (8-2-1), the performance index values corresponding to the possible translations of the template are:

$$\rho(0, 0) = 8$$

$$\rho(0, 1) = 32$$

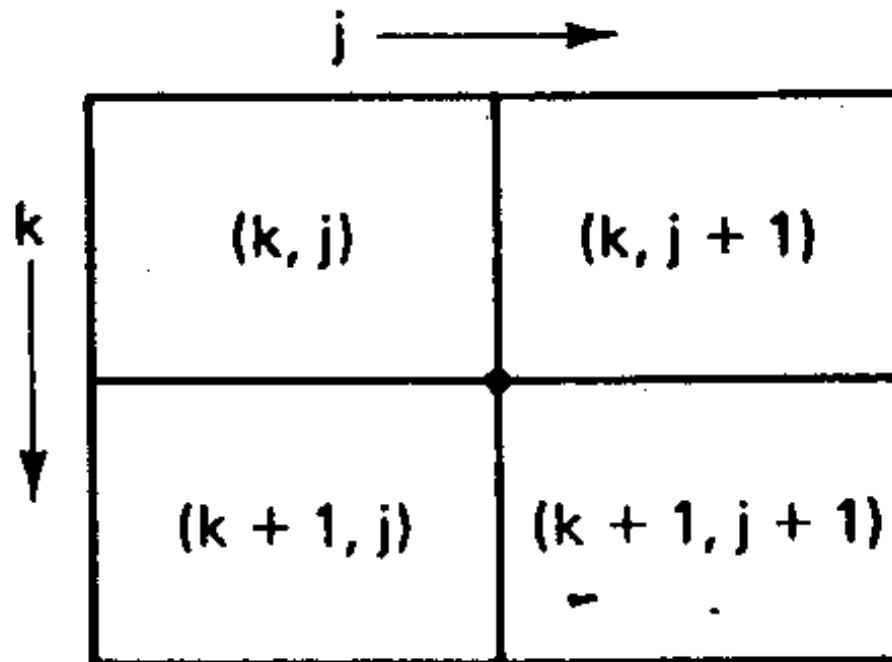
$$\rho(0, 2) = 16$$

$$\rho(1, 0) = 30$$

$$\rho(1, 1) = 4$$

$$\rho(1, 2) = 32$$

Edge detection



$$\nabla I_1(k, j) \triangleq \frac{[I(k + 1, j) - I(k, j)] + [I(k + 1, j + 1) - I(k, j + 1)]}{2\Delta x}$$

$$\nabla I_2(k, j) \triangleq \frac{[I(k, j + 1) - I(k, j)] + [I(k + 1, j + 1) - I(k + 1, j)]}{2\Delta y}$$

Corner point detection

0	1	1
0	1	1
0	0	0

1	1	1
0	1	0
0	0	0

1	1	0
1	1	0
0	0	0

1	0	0
1	1	0
1	0	0

0	0	0
1	1	0
1	1	0

0	0	0
0	1	0
1	1	1

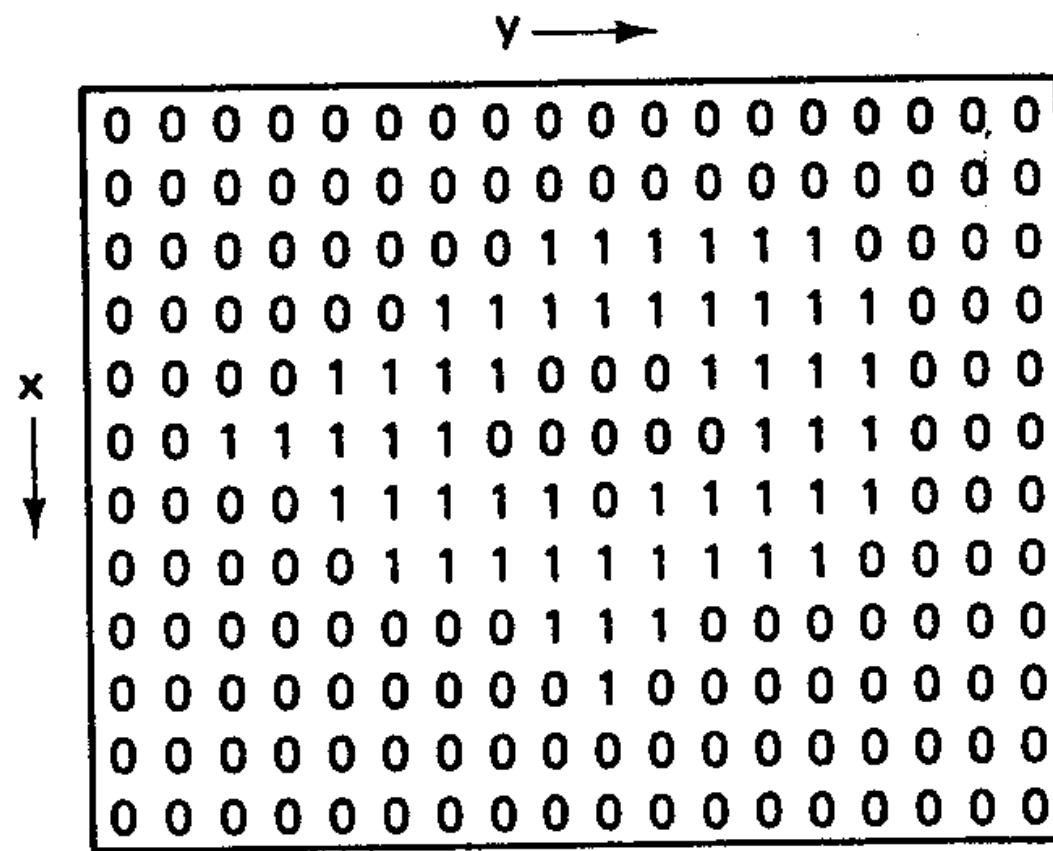
0	0	0
0	1	1
0	1	1

0	0	1
0	1	1
0	0	1

Compression / encoding

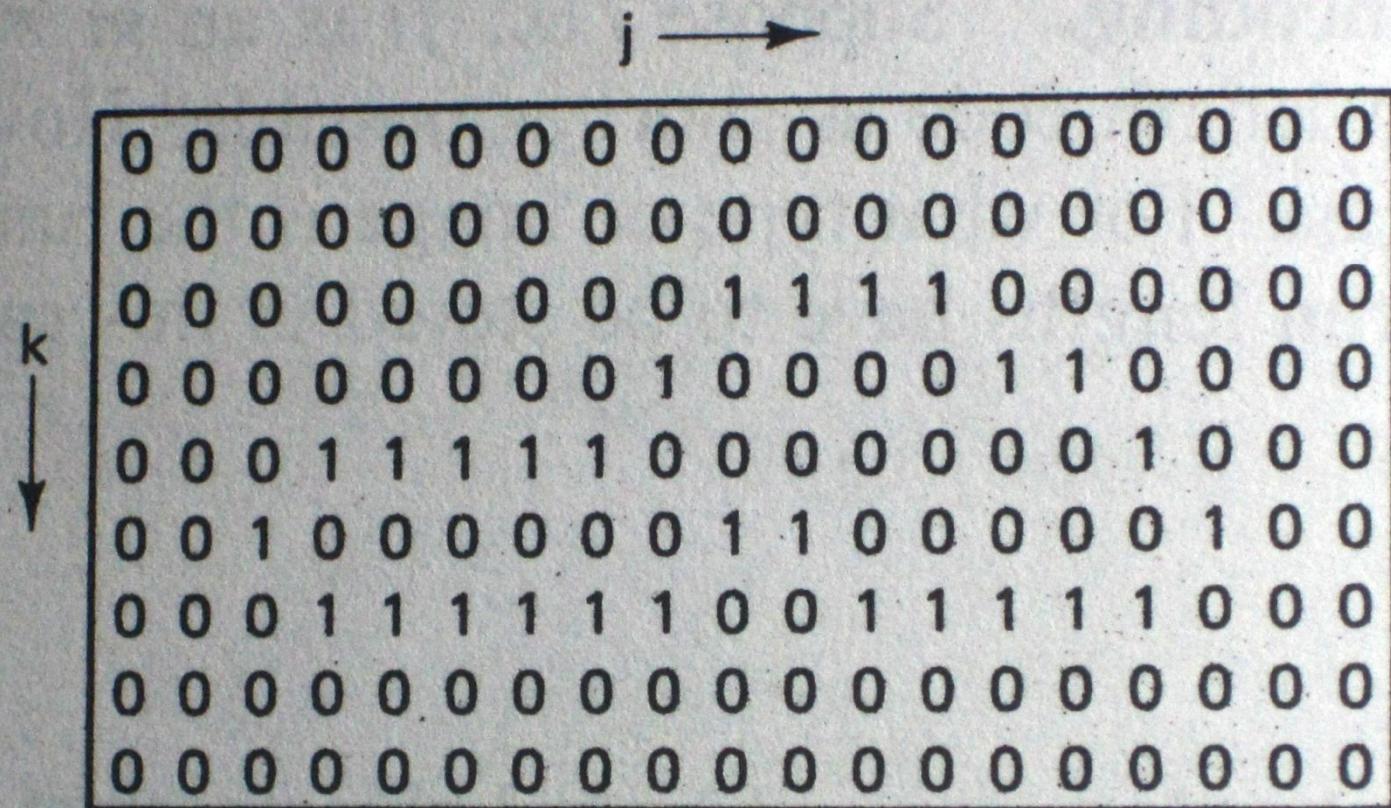
- Large number of pixels will result in a very large image file size.
- Storing will require a lot of space.
- Before storing the digital image is encoded or compressed.

Encoding – Run Length



Line descriptor

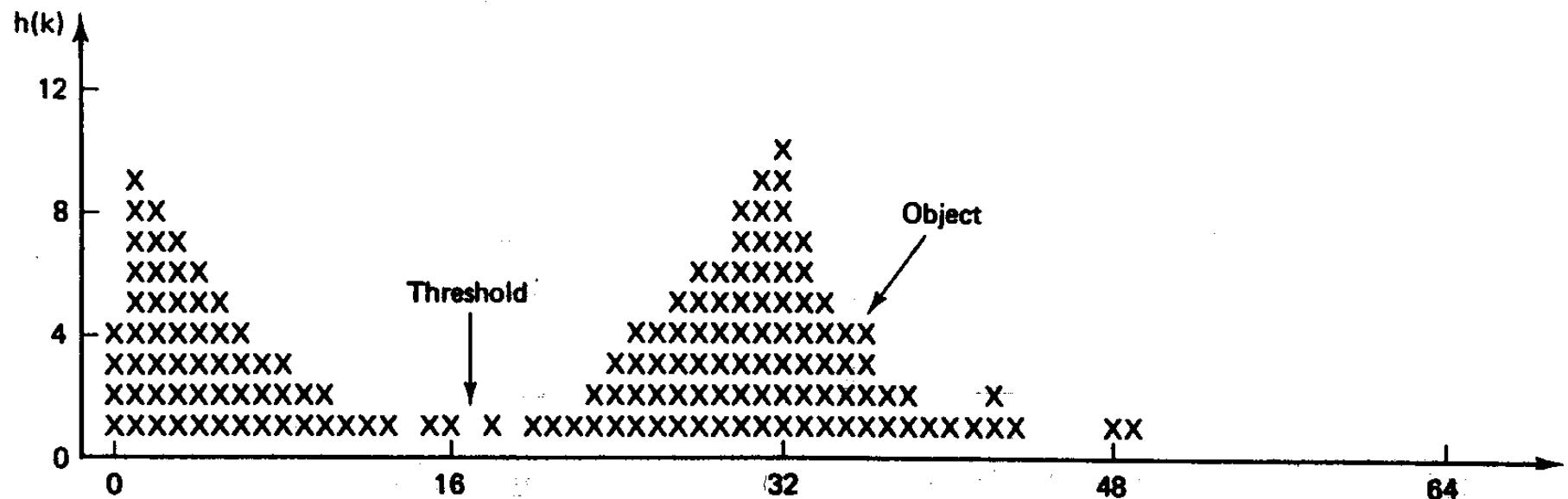
3	2	1
4	p	0
5	6	7



traversing counterclockwise. Then the length of t and the chain code of the boundary is:

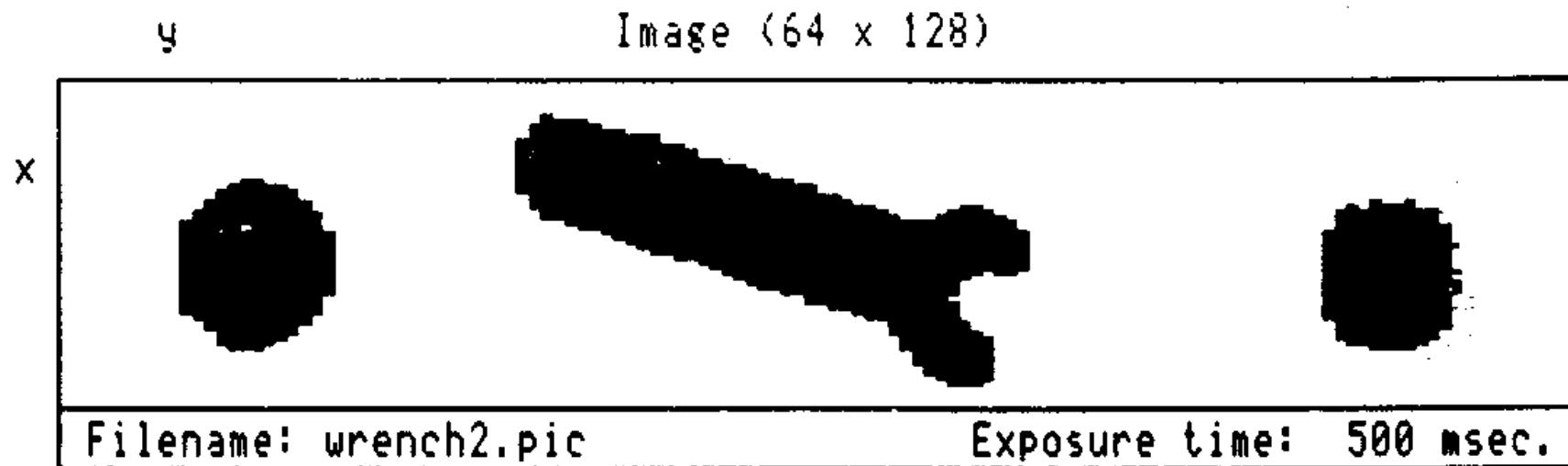
$$a = [3, 3, 4, 3, 4, 4, 4, 5, 5, 4, 4, 4, 4, 4, 5, 7,$$

Segmentation – Thresholding to distinguish between object and background

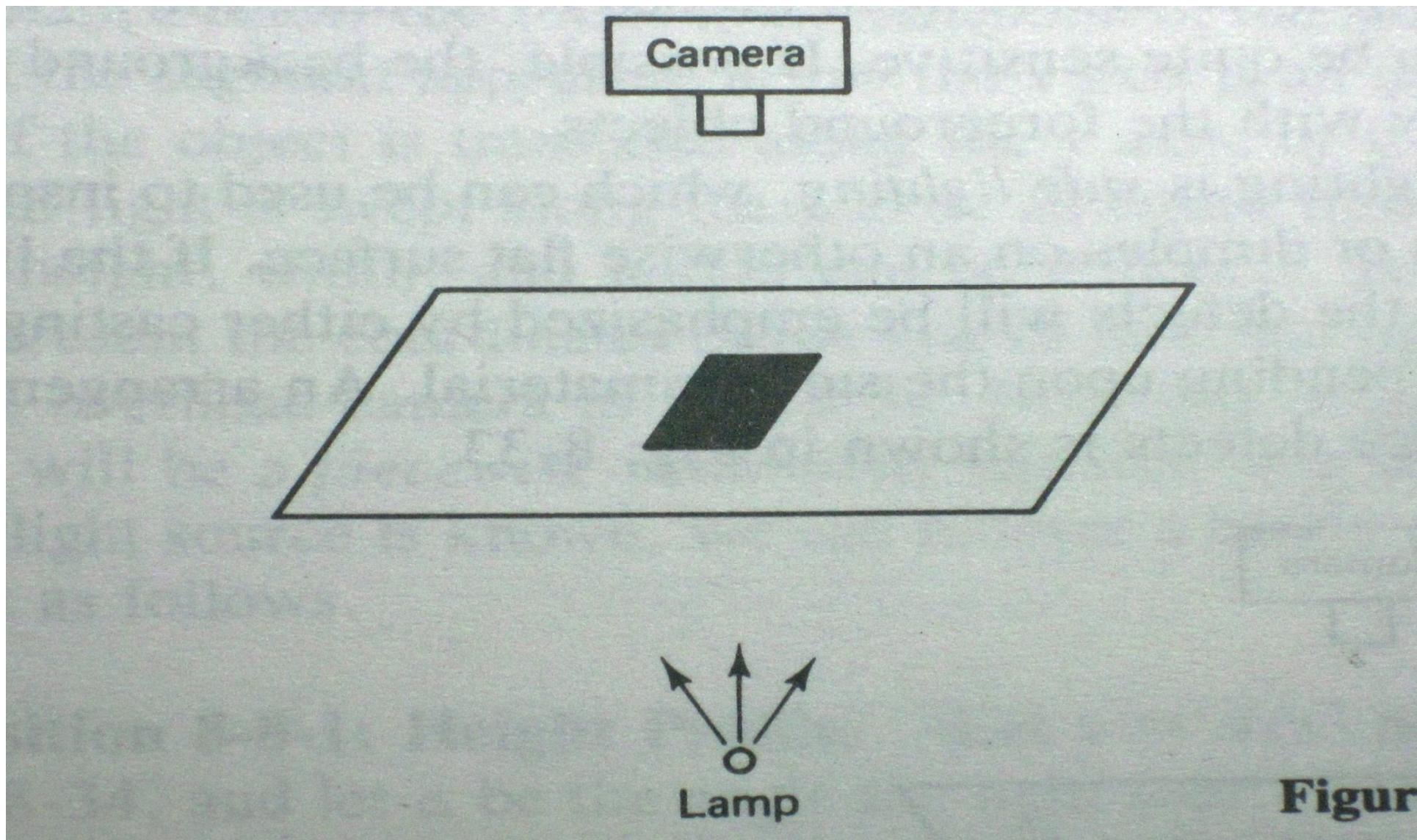


Detection of objects on conveyor

- Shrink operator
- Swell operator

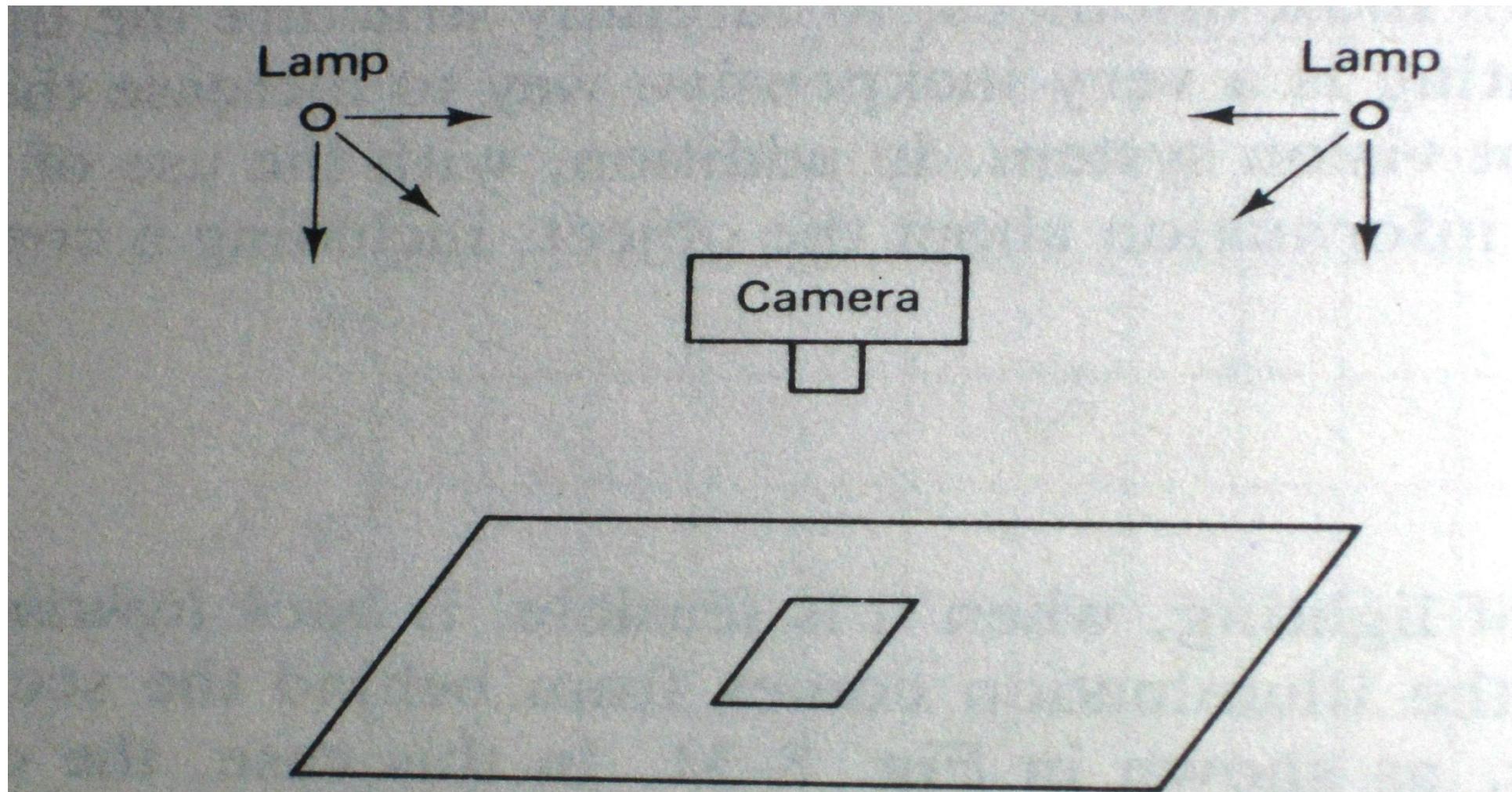


Lighting



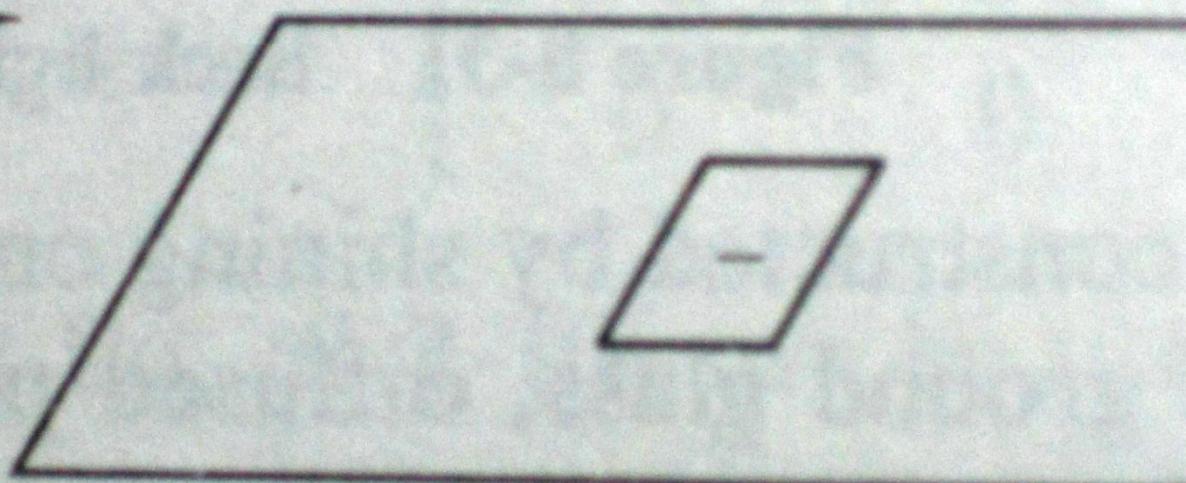
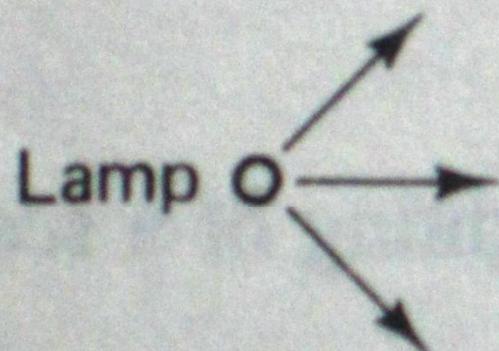
Figur

Double lighting

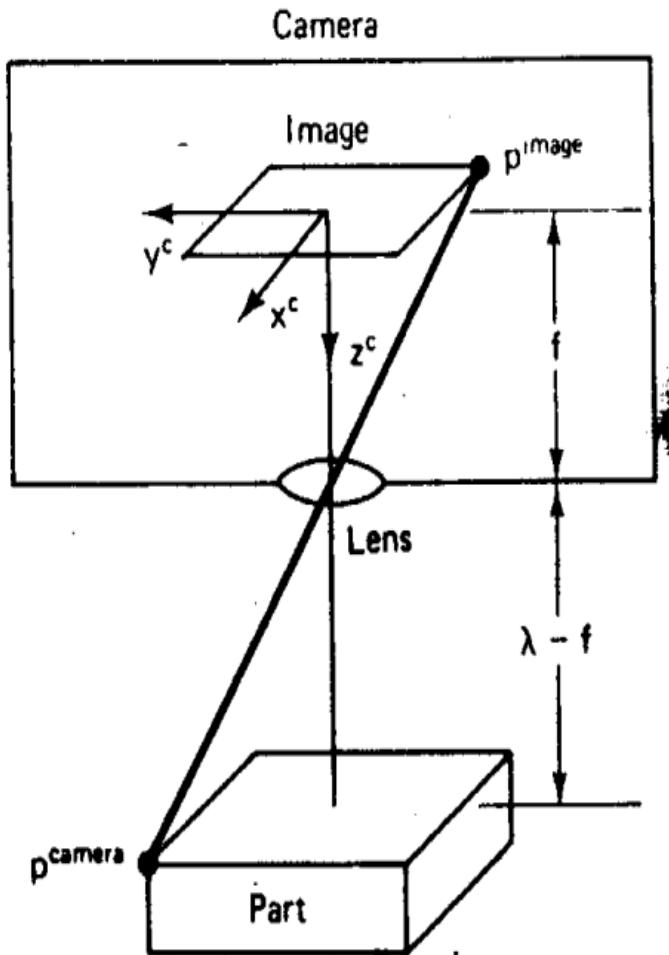


There are several forms of front lighting, such as

Camera



Perspective transformation



$$-\frac{p_1^{image}}{f} = \frac{p_1^{camera}}{p_3^{camera} - f}$$

$$-\frac{p_2^{image}}{f} = \frac{p_2^{camera}}{p_3^{camera} - f}$$

$$p_3^{image} = 0$$

Conversion from world coordinate to image coordinate

$$p^{\text{image}} = \begin{bmatrix} -\frac{fp_1^{\text{camera}}}{p_3^{\text{camera}} - f} \\ -\frac{fp_2^{\text{camera}}}{p_3^{\text{camera}} - f} \\ 0 \end{bmatrix}$$

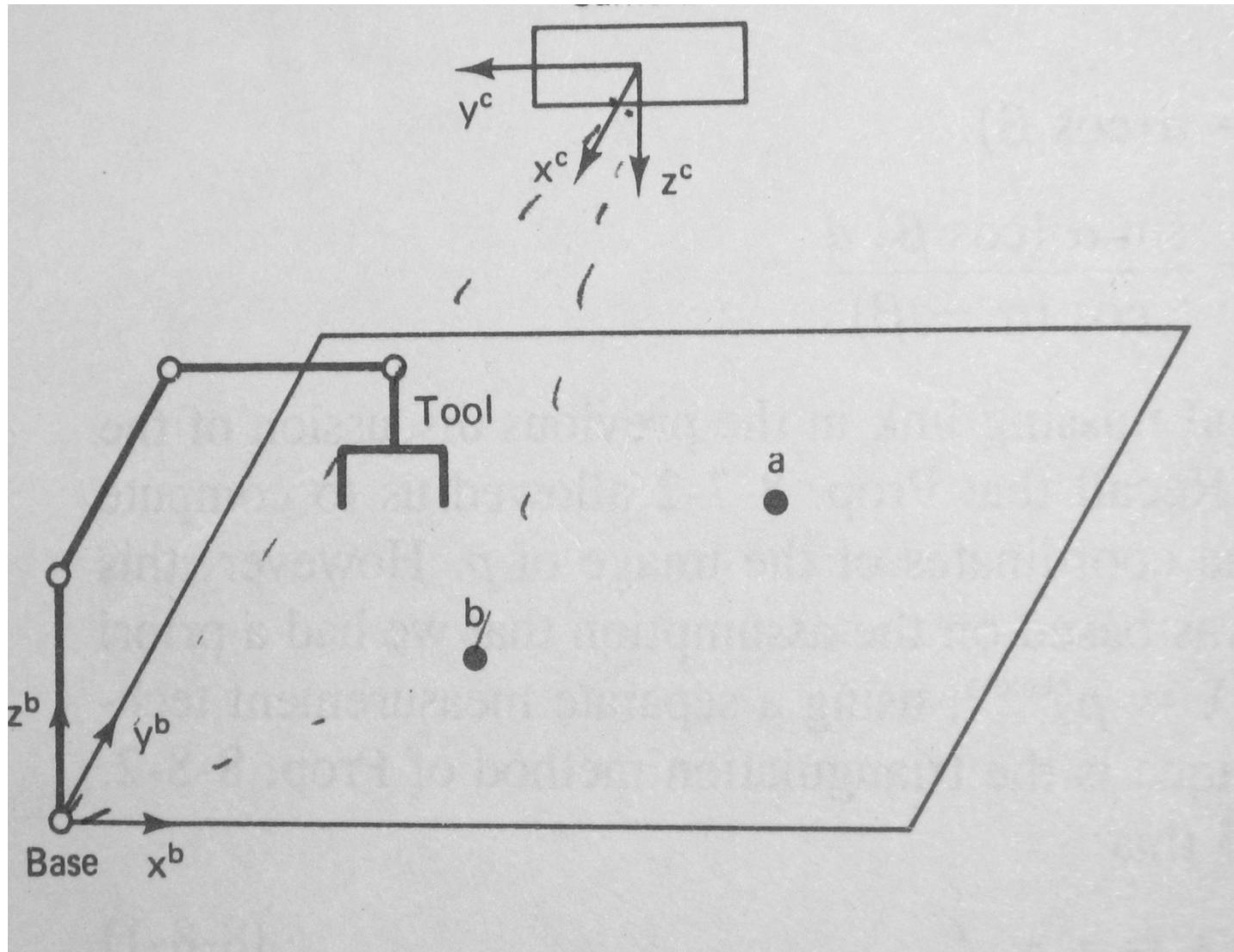
Inverse transform

$$T_{\text{camera}}^{\text{image}}(\lambda) = \left[\begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & f & \frac{f\lambda}{f - \lambda} \\ \hline 0 & 0 & 1 & \frac{f}{f - \lambda} \end{array} \right]$$

Proof. Using Eq. (8-7-4) and the general properties of homogeneous coordinates:

$$\begin{aligned} T_{\text{camera}}^{\text{image}}(\lambda) p^{\text{image}} &= \left[\begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & f & \frac{f\lambda}{f - \lambda} \\ \hline 0 & 0 & 1 & \frac{f}{f - \lambda} \end{array} \right] \begin{bmatrix} p_1^{\text{image}} \\ p_2^{\text{image}} \\ 0 \\ 1 \end{bmatrix} \\ &= \left[p_1^{\text{image}}, p_2^{\text{image}}, \frac{f\lambda}{f - \lambda}, \frac{f}{f - \lambda} \right]^T \\ &= \left[\frac{(f - \lambda)p_1^{\text{image}}}{f}, \frac{(f - \lambda)p_2^{\text{image}}}{f}, \lambda, 1 \right]^T \\ &= [p_1^{\text{camera}}, p_2^{\text{camera}}, p_3^{\text{camera}}, 1]^T \\ &= p^{\text{camera}} \end{aligned}$$

Camera calibration – before using a camera



Unknown X₀, Y₀, Z₀

$$T_{\text{camera}}^{\text{base}} = \left[\begin{array}{ccc|c} 0 & -1 & 0 & x_0 \\ -1 & 0 & 0 & y_0 \\ 0 & 0 & -1 & z_0 \\ \hline 0 & 0 & 0 & 1 \end{array} \right]$$

$$T_{\text{image}}^{\text{base}} = T_{\text{image}}^{\text{camera}} T_{\text{camera}}^{\text{base}}$$

$$= T_{\text{image}}^{\text{camera}} [T_{\text{base}}^{\text{camera}}]^{-1}$$

$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -1/f & 1 \end{bmatrix} \begin{bmatrix} 0 & -1 & 0 & x_0 \\ -1 & 0 & 0 & y_0 \\ 0 & 0 & -1 & z_0 \\ 0 & 0 & 0 & 1 \end{bmatrix}^{-1}$$

$$= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -1/f & 1 \end{bmatrix} \begin{bmatrix} 0 & -1 & 0 & y_0 \\ -1 & 0 & 0 & x_0 \\ 0 & 0 & -1 & z_0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & -1 & 0 & y_0 \\ -1 & 0 & 0 & x_0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1/f & (f - z_0)/f \end{bmatrix} \begin{bmatrix} a_1 \\ a_2 \\ \vdots \\ a_n \end{bmatrix}$$

$$f(y_0 - a_2) = a_1^{\text{image}}(f - z_0)$$

$$f(x_0 - a_1) = a_2^{\text{image}}(f - z_0)$$

$$f(y_0 - b_2) = b_1^{\text{image}}(f - z_0)$$

$$f(x_0 - b_1) = b_2^{\text{image}}(f - z_0)$$

$$z_0 = f \left[1 + \frac{(a_2 - b_2)}{a_1^{\text{image}} - b_1^{\text{image}}} \right]$$

$$y_0 = a_2 + \frac{(f - z_0)a_1^{\text{image}}}{f}$$

$$x_0 = a_1 + \frac{(f - z_0)a_2^{\text{image}}}{f}$$

$$\begin{aligned}
T_{\text{image}}^{\text{base}} &= T_{\text{image}}^{\text{camera}} T_{\text{camera}}^{\text{base}} \\
&= T_{\text{image}}^{\text{camera}} [T_{\text{base}}^{\text{camera}}]^{-1} \\
&= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -1/f & 1 \end{bmatrix} \begin{bmatrix} 0 & -1 & 0 & x_0 \\ -1 & 0 & 0 & y_0 \\ 0 & 0 & -1 & z_0 \\ 0 & 0 & 0 & 1 \end{bmatrix}^{-1} \\
&= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & -1/f & 1 \end{bmatrix} \begin{bmatrix} 0 & -1 & 0 & y_0 \\ -1 & 0 & 0 & x_0 \\ 0 & 0 & -1 & z_0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\
&= \begin{bmatrix} 0 & -1 & 0 & y_0 \\ -1 & 0 & 0 & x_0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1/f & (f - z_0)/f \end{bmatrix} \quad (8-9-2)
\end{aligned}$$

We can now equate the image coordinates a^{image} with the inferred image coordinates, $T_{\text{image}}^{\text{base}}a$. This can also be done for test point b , and the result, after simplification, is:

$$f(y_0 - a_2) = a_1^{\text{image}}(f - z_0) \quad (8-9-3)$$

$$f(x_0 - a_1) = a_2^{\text{image}}(f - z_0) \quad (8-9-4)$$

$$f(y_0 - b_2) = b_1^{\text{image}}(f - z_0) \quad (8-9-5)$$

$$f(x_0 - b_1) = b_2^{\text{image}}(f - z_0) \quad (8-9-6)$$