

# Smart Materials – II

*(Piezoelectric materials)*



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# Contents

- History of Piezoelectricity
- Piezoelectric Materials
- How to prepare a Piezoceramic Actuator?
- Constitutive Relationship
- Piezoceramic Polymers & Composites
- Bimorphs & Piezostacks



# History of Piezoelectricity

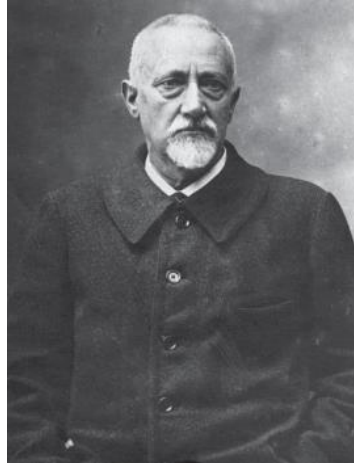
- **Piezoelectricity** : Electricity from Pressure was discovered by Pierre and Jacques Curie in 1880.
- Contemporary: **Contact Electricity** – Static Electricity generated from Friction.
- **Pyroelectricity**: Electricity generated from crystals while heating.



# Who's who in Piezoelectricity?

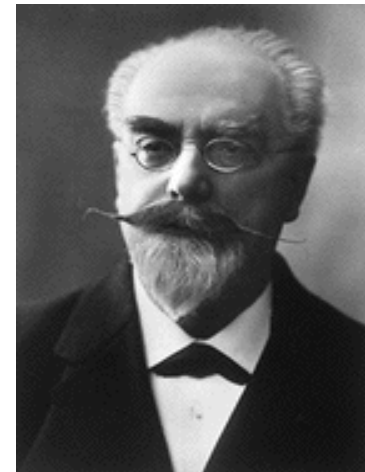


**Pierre Curie (1859-1906),  
Nobel Prize in Physics, 1903**



**Paul-Jacques Curie (1856-1941)**

## **Direct Piezoelectric Effect (1880)**



**Gabriel Lippmann (1845-1921),  
Nobel Prize in Physics, 1908**

## **Reverse Piezoelectric Effect (1881)**

Source: Wikipedia



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# Piezoelectricity – Time Line

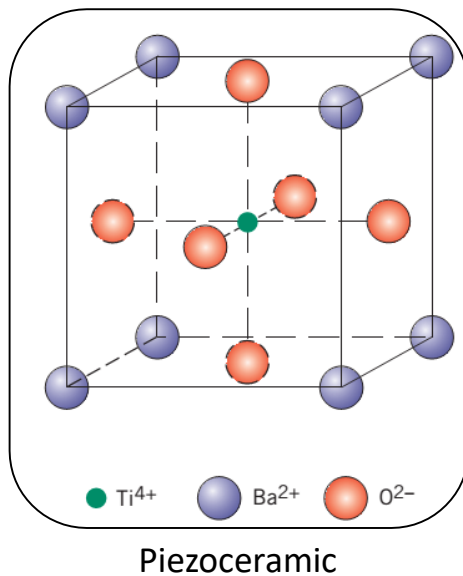
- The effect observed by **Pierre and Jacque Curie** is called as Direct Piezoelectric Effect (Hankel 1881).
- The direct effect was found in Zinc Blende, Boracite, Tourmaline, Quartz, Cane Sugar and Rochelle Salt.
- The reverse effect was theoretically predicted by Lippman (1881) and experimentally confirmed by Voight in 1894.
- First application – Langvein (1917) in Sonar Transducer (composite made of steel plate & quartz) – later Ceramic Phonograph, Ceramic Electret Microphone.



# Piezoelectricity in Perovskites (1949-60)

Perovskite: A Ternary (3 Component structure)

Example:  $\text{BaTiO}_3$  a common piezoelectric material



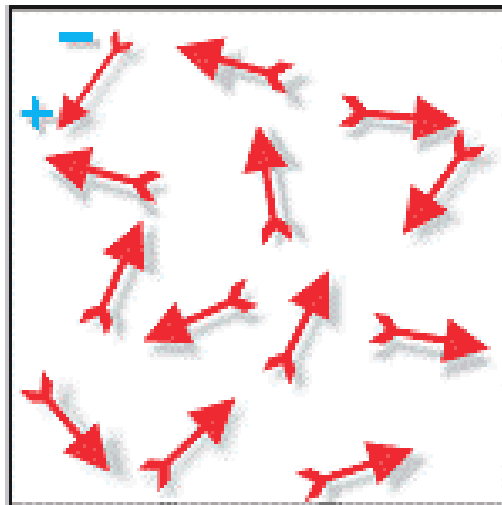
Tetragonal Symmetry with Dipole moment  
below Curie Temperature

**Similar material: PZT family, LiNb family, PbNb family, YMn family,  $(\text{NH}_4)\text{Cd}$  family (1970--)**

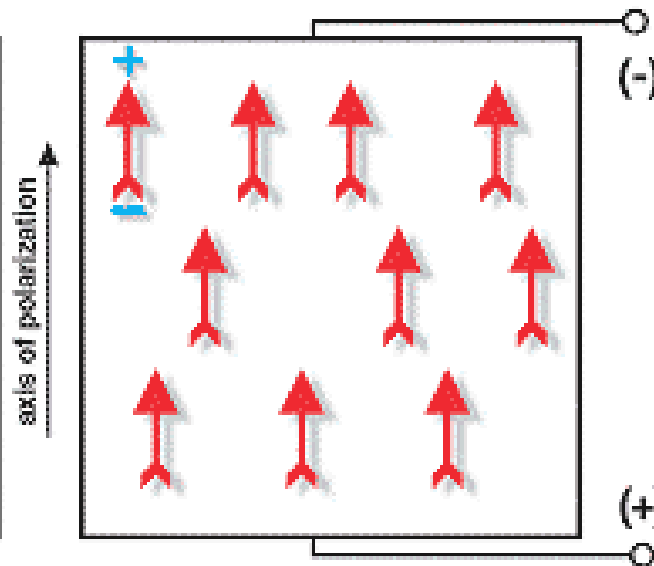


# Polarization of Piezoelectric Material

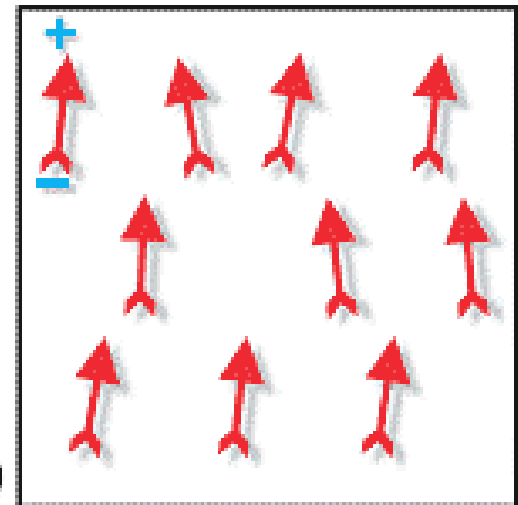
(a) random orientation of polar domains prior to polarization



(b) polarization in DC electric field



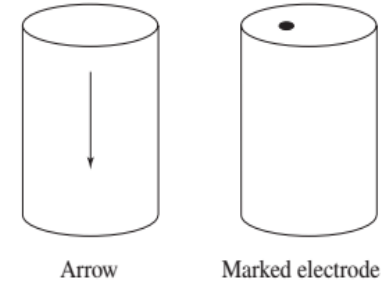
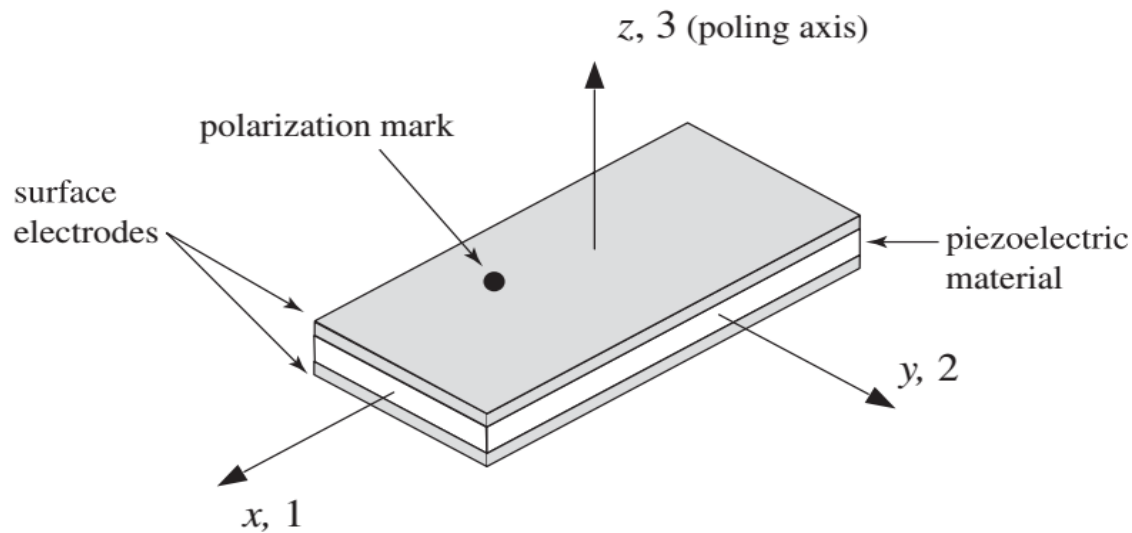
(c) remanent polarization after electric field removed



Reference: [https://www.pc-control.co.uk/piezoelectric\\_effect.htm](https://www.pc-control.co.uk/piezoelectric_effect.htm)

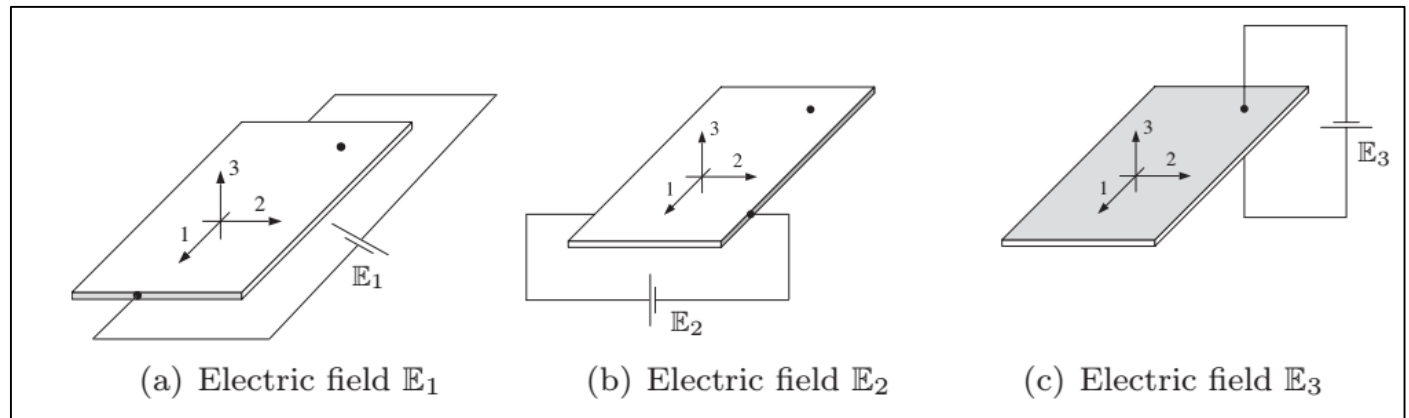


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***Polarization direction***

**Definition of co-ordinate axes and poling direction for a piezoceramic sheet**



***Possible electric field directions for a piezoceramic sheet***

**Source:** Smart Structures Theory by I. Chopra and J.Sirohi (2013)



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# Constitutive Equation of Piezoelectricity

$$D = dX + \varepsilon^X E \leftarrow \text{Direct Effect}$$



$$x = S^E X + dE \leftarrow \text{Converse Effect}$$



$X$  – Stress (N/m<sup>2</sup>)

$x$ - Strain

$D$  - Electric displacement / flux density (C/m<sup>2</sup>)

$S$  – Compliance (m<sup>2</sup>/N),

$E$  - Electric field intensity (V/m or N/C)

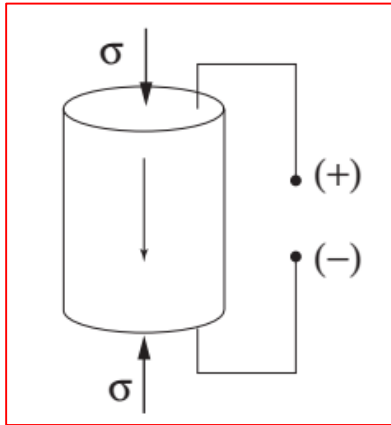
$\varepsilon$  - Permittivity (F/m)

$d$  - Piezoelectric constant (C/N or m/V)

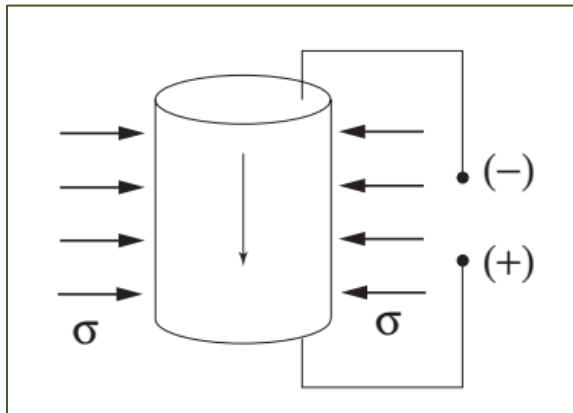
Superscripts denote the measurement of **permittivity at constant stress** and **compliance at constant electric field intensity**



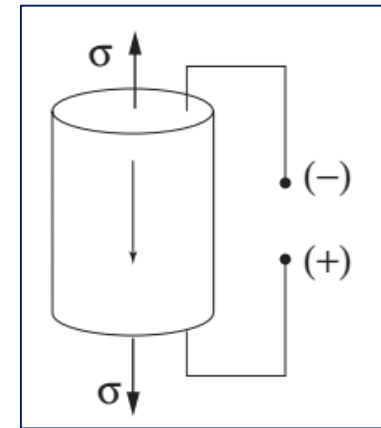
# Direct piezoelectric effect



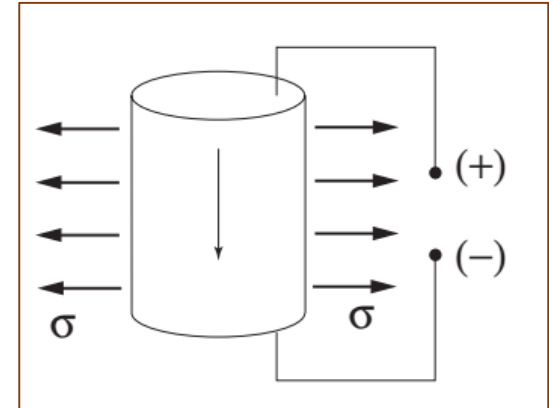
**Compressive stress along the polarization direction generates a voltage of the same polarity as the poling voltage**



**Compressive stress perpendicular to polarization direction generates a voltage of opposite polarity to the poling voltage**



**Tensile stress along the polarization direction generates a voltage of polarity opposite to that of the poling voltage**



**Tensile stress perpendicular to the polarization direction generates a voltage of the same polarity as the poling voltage**

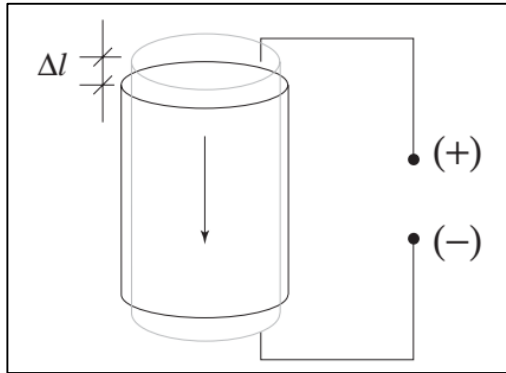
Source: Smart Structures Theory by I. Chopra and J. Sirohi (2013)



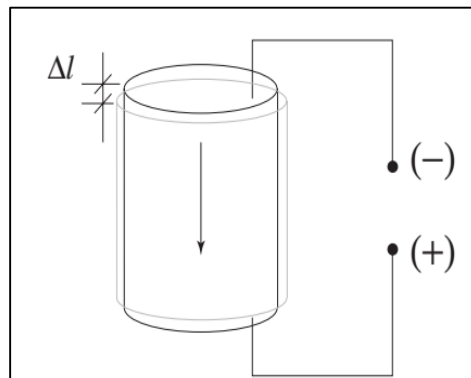
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# Converse piezoelectric effect

## Effect of applied voltage on change in dimensions



Voltage of the same polarity as the poling voltage causes an extension along the poling direction and contraction perpendicular to the poling direction



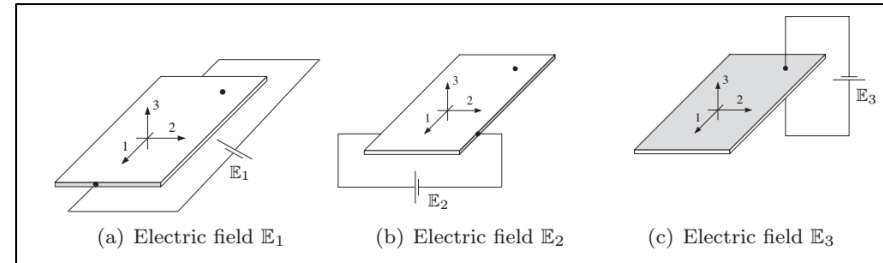
Voltage of the opposite polarity as the poling voltage causes a contraction along the poling direction and extension perpendicular to the poling direction

**Source:** Smart Structures Theory by I. Chopra and J.Sirohi (2013)



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# Piezoelectric constant



$$d_{ki}^d = \frac{\text{charge generated in } k\text{-direction}}{\text{mechanical stress applied in } i\text{-direction}}$$

Unit : Coulomb/Newton



$$d_{ik}^c = \frac{\text{strain induced in } i\text{-direction}}{\text{electric field applied in } k\text{-direction}}$$

Unit : metre/Volt

For most practical purpose,  $d^d = d$  and  $d^c = d^T$ , T= transpose of matrix  
Thus, m/V is equivalent to C/N

**Electro-mechanical coupling coefficient**

$$k_{ij} = \sqrt{\frac{\text{Mechanical energy stored in direction } j}{\text{Electrical energy applied in direction } i}}$$

$$= \sqrt{\frac{\text{Electrical energy stored in direction } j}{\text{Mechanical energy applied in direction } i}}$$

Source: Smart Structures Theory by I. Chopra and J.Sirohi (2013)



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# Commercial Piezoelectric Material Property Set

Prop.	Unit	BaTiO <sub>3</sub>	PZT-A	PZT-B	PbNb <sub>2</sub> O <sub>6</sub>	LiNbO <sub>3</sub>	PbTiO <sub>3</sub>
$\rho$	Mg/m <sup>3</sup>	5.7	7.9	7.7	5.9	4.6	7.1
$k_{31}$		0.21	0.33	0.39	0.04	0.02	0.05
$k_{33}$		0.49	0.68	0.72	0.38	0.17	0.35
$d_{31}$	pC/N <sup>-1</sup>	79	119	234	11	.85	7.4
S	μm <sup>2</sup> /N	8.6	12.2	14.5	29	5.8	11



# A few observations

- PZT family has highest piezoelectric coupling.
- Curie Point: PZT family 220-315°C,  
Li family 600-1200°C
- Instead of polycrystalline Piezoceramics, a single cut PMN could give  $k_{33} = 0.92$  and  $d_{33} = 2070$  pC/N



# Piezoelectric Polymer

- $\text{PVF}_2$  (Poly Vinylidene Fluoride) a semi-crystalline polymer consist of long-chain molecules with the repeat unit of  $\text{CF}_2\text{CH}_2$
- Form I PVDF (all trans) shows all chain oriented parallel to the axis of the unit cell and the dipoles pointing in the same direction
- $d_{31}$  : 4.2-19 pC/N (for PZT  $\sim 234$ )
- $K_{31}$  : 3-14.7%
- $E$  : 1.6 – 3.8 GPa



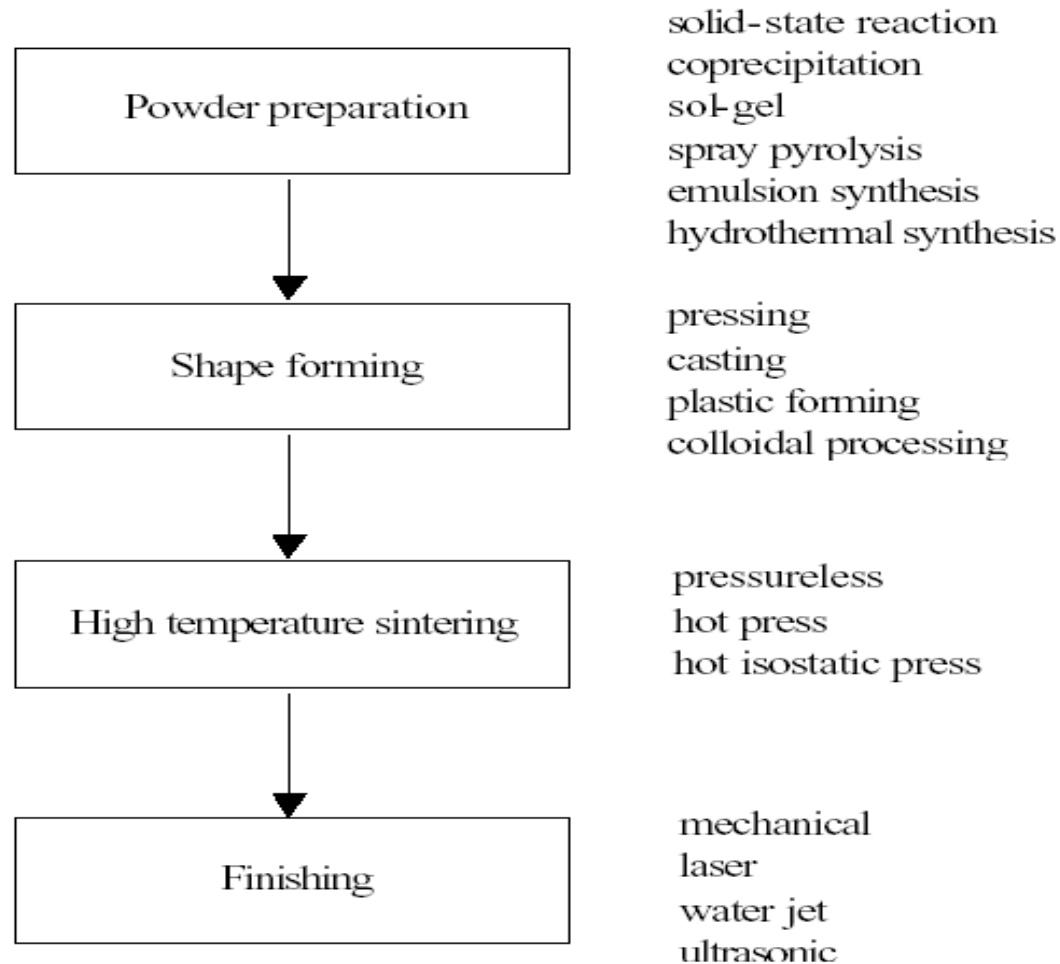
# How to prepare a Piezoceramic Actuator?

- Start with fine powders of component metal oxides (PZT or Barium Titanate family) e.g.. for PZT you need  $\text{PbO}$ ,  $\text{ZrO}_2$  and  $\text{TiO}_2$  powders.
- Mix them in fixed proportions.
- Use an organic binder.
- Form into specific shapes.
- Heat for a specific time and specified temperature 650-800°C
- Cool – apply electrode (sputtering).
- Polarize the sensor/actuator using a DC electric field.





# 4 steps for Powder Processing

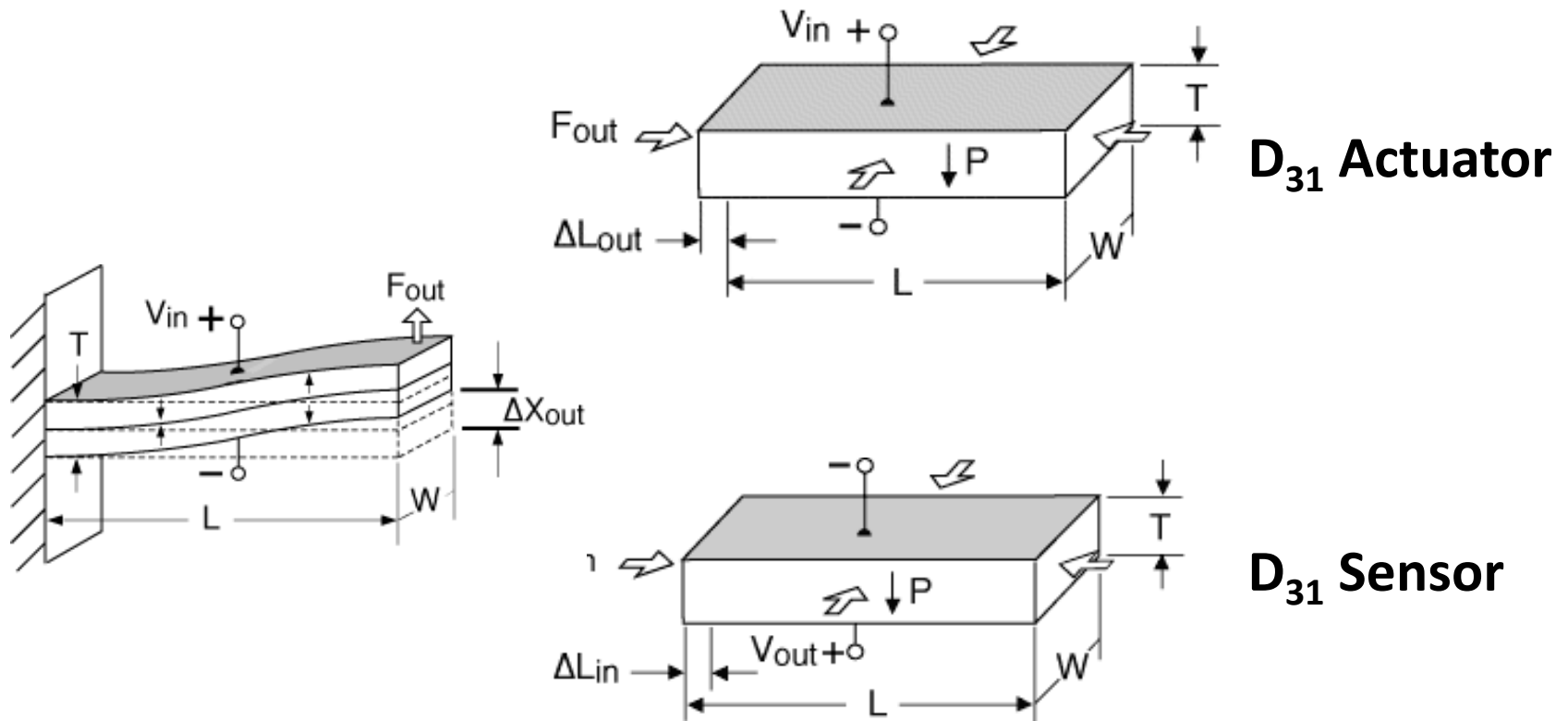


# Piezoelectric Composite

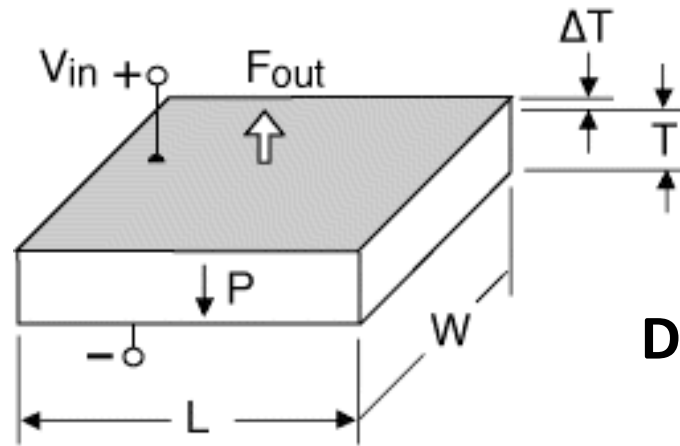
- Composite made of a polymer and PZT
- Polymer phase – lower density, permittivity and increased elastic compliance.
- Smaller PZT particles (5-10  $\mu\text{m}$ ) in Polyurethane (PU) matrix.
- Larger 120 $\mu\text{m}$  particles in a silicone rubber matrix.
- Skinner et.al: Smaller particles generate series connectivity, while larger generate parallel connectivity.



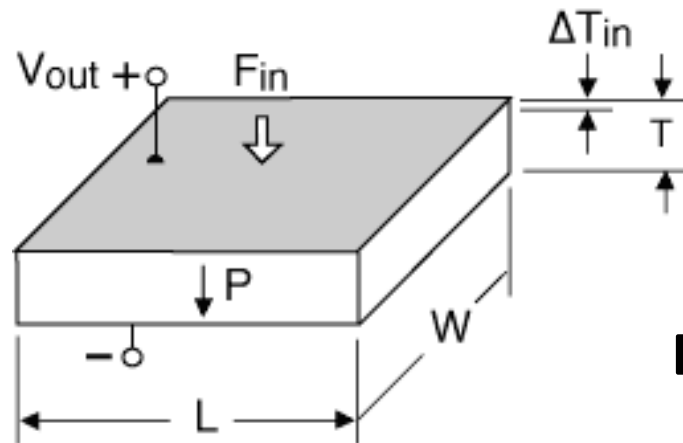
# Applications: Bimorph



# PIEZOSTACK



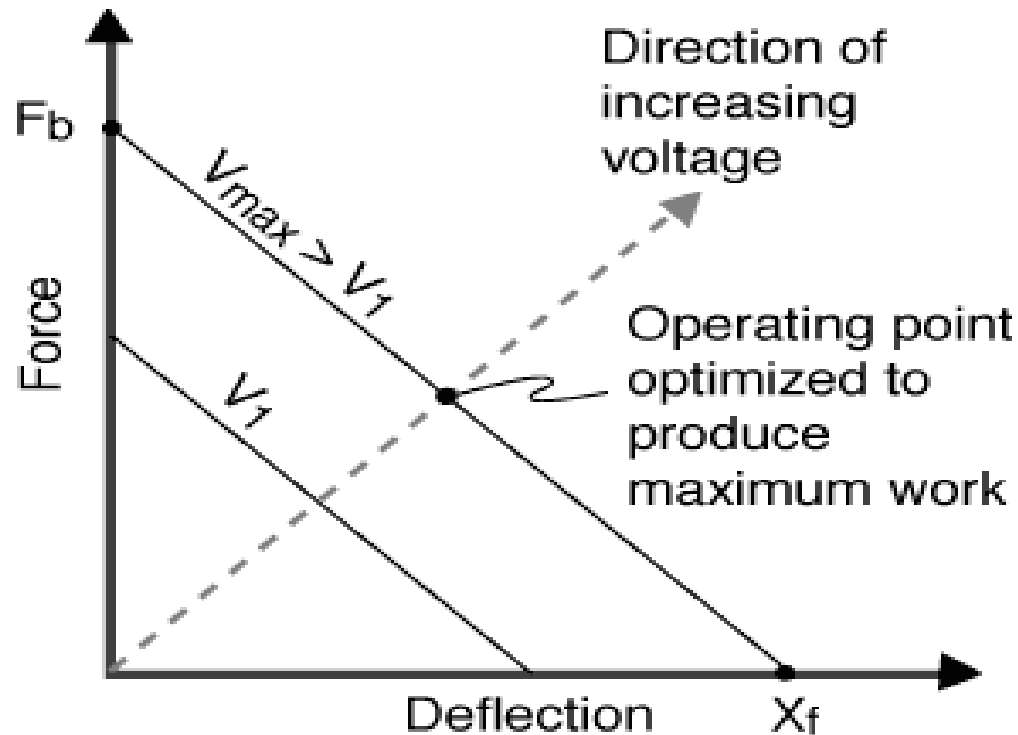
**$D_{33}$  Actuator**



**$D_{33}$  Sensor**



# Operating Point



***Actuator load line***

**Source:** Smart Structures Theory by I. Chopra and J. Sirohi

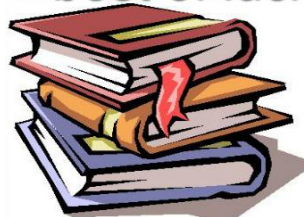


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In the **next lecture**, we will learn about

- ✓ Magnetostrictive materials
- ✓ Constitutive Equations
- ✓ Different effects of Magnetostriction

best of luck



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