

1. Two large plane charge sheets having surface charge densities σ_0 and $-\sigma_0$ are superposed on each other in $x-y$ plane.

- Find the electric and magnetic fields at a point with $z > 0$ in the given frame S .
- Find the surface charge density σ'_+ of the positive charge sheet as seen from the frame S' moving with respect to S at velocity $v\hat{i}$.
- Assuming that the negative charge sheet moves with respect to S' with a velocity $-V\hat{i}$, write the surface charge density of the negative sheet in the frame S' .
- Write the electric and magnetic fields in the frame S' with at points $z' > 0$, using the charge density and the current density calculated in S' .
- Using the field transformation equations write the electric and magnetic fields in S' from those in S .
- Comparing the magnetic field found in (c) and (d) find the expression for V .

(The general equation for velocity addition for motion along $x-x'$ axis is $V = \frac{v_1 + v_2}{1 - v_1 v_2 / c^2}$. This

ensures that in no frame any object can go faster than c)

More problems

1. A particle moves on the x -axis with velocity u_1 as seen from a frame S' . Consider two events: The particle crossing the point x_1' at time t_1' and then crossing x_2' at time t_2' . Find the coordinates and times of occurrence of these events in frame S using Lorentz Transformation equations. Find velocity of the particle as seen from S . As usual, S' moves with respect to S with velocity v in positive x -direction.

2. Consider two line charges, with linear charge densities $+\lambda$ and $-\lambda$, lie along the x -axis. The positive line move at velocity v in $+x$ -direction and the negative line moves at velocity v in $-x$ direction. All this is in the frame S . A point charge q is placed at $(0,0,y)$.

- Find the force F on q as seen in the frame S .
- Write the fields in the frame S' and the force F' on the particle using Coulomb's law and Biot-Savart law.
- Write the force transformation equation in the given situation.