

ESO 201A: Thermodynamics  
2016-2017-I semester

Mass-Energy Analysis: part 3

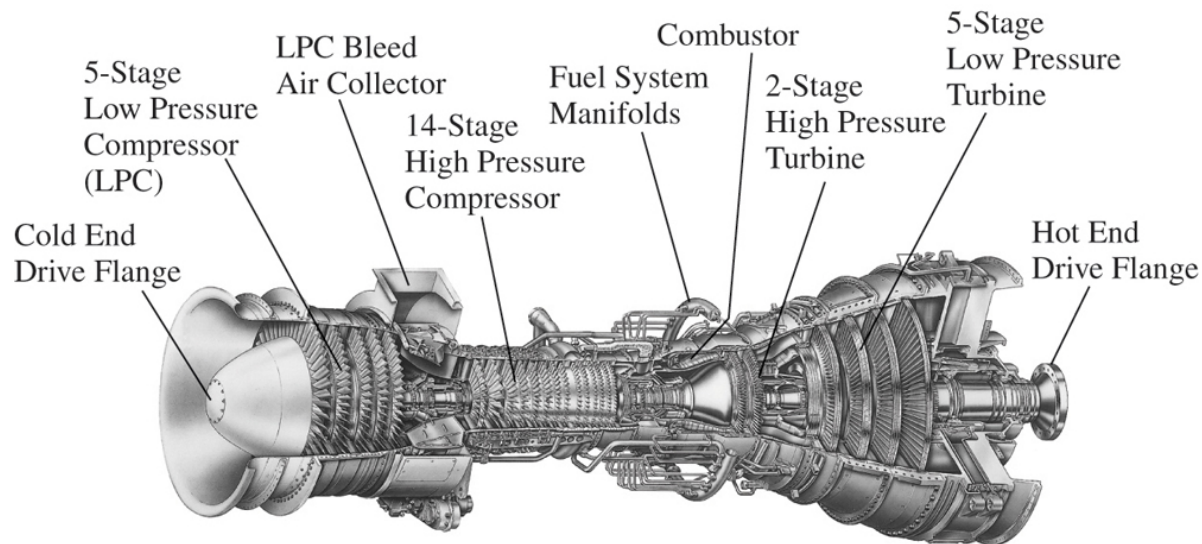
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[home.iitk.ac.in/~jayantks/ESO201/index.htm](http://home.iitk.ac.in/~jayantks/ESO201/index.htm)

# Learning objectives

- Develop the conservation of mass principle.
- Apply the conservation of mass principle to various systems including steady- and unsteady-flow control volumes.
- Apply the first law of thermodynamics as the statement of the conservation of energy principle to control volumes.
- Identify the energy carried by a fluid stream crossing a control surface as the sum of internal energy, flow work, kinetic energy, and potential energy of the fluid and to relate the combination of the internal energy and the flow work to the property enthalpy.
- Solve energy balance problems for common steady-flow devices such as nozzles, compressors, turbines, throttling valves, mixers, heaters, and heat exchangers.
- Apply the energy balance to general unsteady-flow processes with particular emphasis on the uniform-flow process as the model for commonly encountered charging and discharging processes.

## Some Steady Flow-Engineering Devices

Many engineering devices operate essentially under the same conditions for long periods of time. The components of a steam power plant (turbines, compressors, heat exchangers, and pumps), for example, operate nonstop for months before the system is shut down for maintenance. Therefore, these devices can be conveniently analyzed as steady-flow devices.

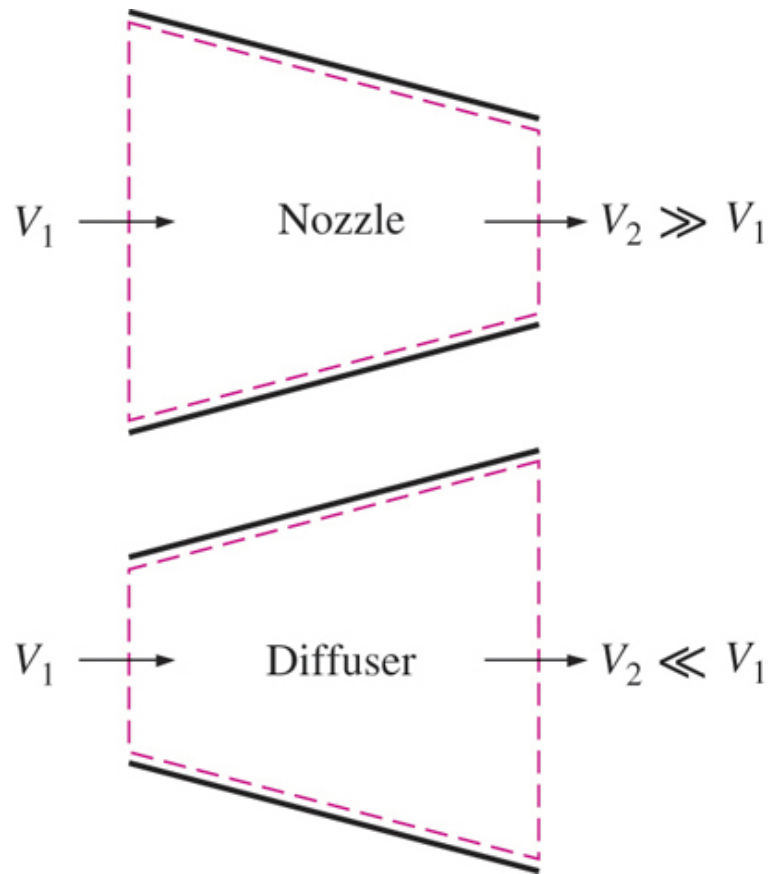


A modern land-based gas turbine used for electric power production. This is a General Electric LM5000 turbine. It has a length of 6.2 m, it weighs 12.5 tons, and produces 55.2 MW at 3600 rpm with steam injection.

| $V_1$ | $V_2$ | $\Delta ke$ |
|-------|-------|-------------|
| m/s   | m/s   | kJ/kg       |
| 0     | 45    | 1           |
| 50    | 67    | 1           |
| 100   | 110   | 1           |
| 200   | 205   | 1           |
| 500   | 502   | 1           |

At very high velocities, even small changes in velocities can cause significant changes in the kinetic energy of the fluid.

# Nozzles and Diffusers



Nozzles and diffusers are shaped so that they cause large changes in fluid velocities and thus kinetic energies.

Nozzles and diffusers are commonly utilized in jet engines, rockets, spacecraft, and even garden hoses.

A **nozzle** is a device that *increases the velocity of a fluid* at the expense of pressure.

A **diffuser** is a device that *increases the pressure of a fluid* by slowing it down.

# Energy balance for a nozzle and diffuser

Steady-flow process

$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\frac{dE_{\text{system}}}{dt}}_{\text{Rate of change in internal, kinetic, potential, etc., energies}} \overset{0 \text{ (steady)}}{=} 0$$

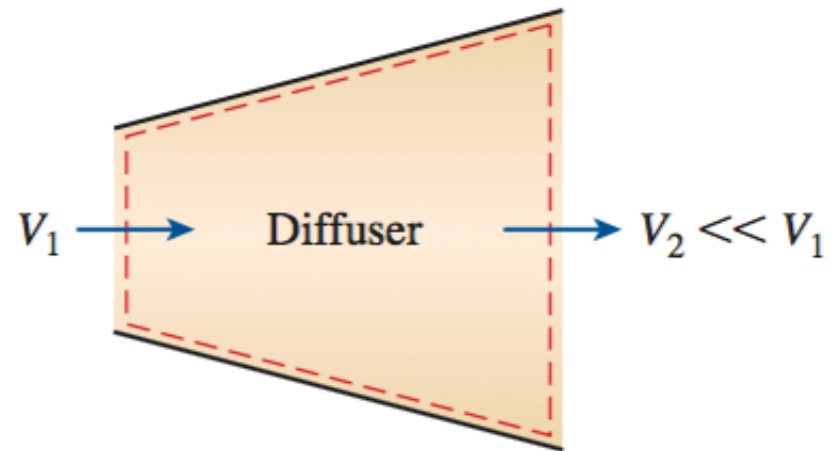
(since  $\dot{Q} \cong 0$ ,  $\dot{W} = 0$ , and  $\Delta pe \cong 0$ )

$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{m} \left( h_1 + \frac{V_1^2}{2} \right) = \dot{m} \left( h_2 + \frac{V_2^2}{2} \right)$$

## Example

Air at  $10^\circ\text{C}$  and  $80\text{ kPa}$  enters the diffuser of a jet engine steadily with a velocity of  $200\text{ m/s}$ . The inlet area of the diffuser is  $0.4\text{ m}^2$ . The air leaves the diffuser with a velocity that is very small compared with the inlet velocity. Determine (a) the mass flow rate of the air and (b) the temperature of the air leaving the diffuser.



# Example

**TABLE A-17**

Ideal-gas properties of air

| $T$<br>K | $h$<br>kJ/kg | $P_r$  | $u$<br>kJ/kg | $v_r$  | $s^\circ$<br>kJ/kg·K |
|----------|--------------|--------|--------------|--------|----------------------|
| 200      | 199.97       | 0.3363 | 142.56       | 1707.0 | 1.29559              |
| 210      | 209.97       | 0.3987 | 149.69       | 1512.0 | 1.34444              |
| 220      | 219.97       | 0.4690 | 156.82       | 1346.0 | 1.39105              |
| 230      | 230.02       | 0.5477 | 164.00       | 1205.0 | 1.43557              |
| 240      | 240.02       | 0.6355 | 171.13       | 1084.0 | 1.47824              |
| 250      | 250.05       | 0.7329 | 178.28       | 979.0  | 1.51917              |
| 260      | 260.09       | 0.8405 | 185.45       | 887.8  | 1.55848              |
| 270      | 270.11       | 0.9590 | 192.60       | 808.0  | 1.59634              |
| 280      | 280.13       | 1.0889 | 199.75       | 738.0  | 1.63279              |
| 285      | 285.14       | 1.1584 | 203.33       | 706.1  | 1.65055              |
| 290      | 290.16       | 1.2311 | 206.91       | 676.1  | 1.66802              |
| 295      | 295.17       | 1.3068 | 210.49       | 647.9  | 1.68515              |
| 298      | 298.18       | 1.3543 | 212.64       | 631.9  | 1.69528              |
| 300      | 300.19       | 1.3860 | 214.07       | 621.2  | 1.70203              |
| 305      | 305.22       | 1.4686 | 217.67       | 596.0  | 1.71865              |
| 310      | 310.24       | 1.5546 | 221.25       | 572.3  | 1.73498              |
| 315      | 315.27       | 1.6442 | 224.85       | 549.8  | 1.75106              |
| 320      | 320.29       | 1.7375 | 228.42       | 528.6  | 1.76690              |

## Turbines and Compressors

**Turbine** drives the electric generator In steam, gas, or hydroelectric power plants.

*As the fluid passes through the turbine, work is done against the blades, which are attached to the shaft. As a result, the shaft rotates, and the turbine produces work.*

**Compressors**, as well as **pumps** and **fans**, are devices used to increase the pressure of a fluid. *Work is supplied to these devices from an external source through a rotating shaft.*

A **fan** increases the pressure of a gas slightly and is mainly used to mobilize a gas.

A **compressor** is capable of compressing the gas to very high pressures.

**Pumps** work very much like compressors except that they handle liquids instead of gases.



## Energy balance for compressor

$$\underbrace{\dot{E}_{\text{in}} - \dot{E}_{\text{out}}}_{\text{Rate of net energy transfer by heat, work, and mass}} = \underbrace{\frac{dE_{\text{system}}}{dt}}_{\text{Rate of change in internal, kinetic, potential, etc., energies}} \overset{0 \text{ (steady)}}{=} 0$$

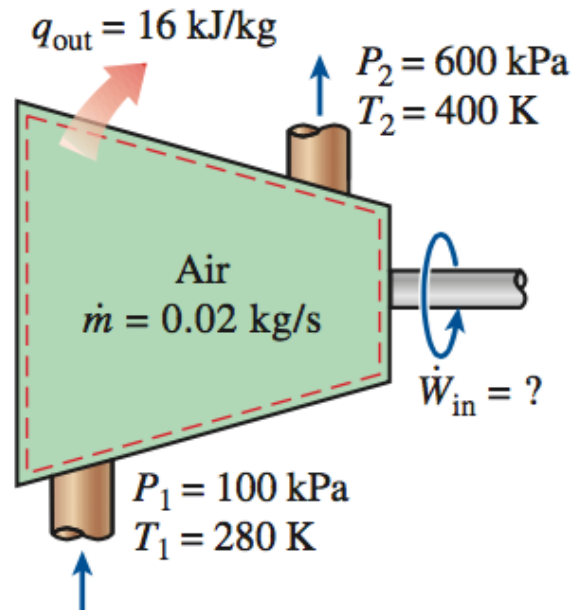
$$\dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\dot{W}_{\text{in}} + \dot{m}h_1 = \dot{Q}_{\text{out}} + \dot{m}h_2 \quad (\text{since } \Delta \text{ke} = \Delta \text{pe} \cong 0)$$

$$\dot{W}_{\text{in}} = \dot{m}q_{\text{out}} + \dot{m}(h_2 - h_1)$$

## Example

Air at 100 kPa and 280 K is compressed steadily to 600 kPa and 400 K. The mass flow rate of the air is 0.02 kg/s, and a heat loss of 16 kJ/kg occurs during the process. Assuming the changes in kinetic and potential energies are negligible, determine the necessary power input to the compressor.



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|----------|--------------|--------|--------------|-------|----------------------|
| 270      | 270.11       | 0.9590 | 192.00       | 688.0 | 1.63004              |
| 280      | 280.13       | 1.0889 | 199.75       | 738.0 | 1.63279              |
| 285      | 285.14       | 1.1584 | 203.33       | 706.1 | 1.65055              |
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| 310      | 310.24       | 1.5546 | 221.25       | 572.3 | 1.73498              |
| 315      | 315.27       | 1.6442 | 224.85       | 549.8 | 1.75106              |
| 320      | 320.29       | 1.7375 | 228.42       | 528.6 | 1.76690              |
| 325      | 325.31       | 1.8345 | 232.02       | 508.4 | 1.78249              |
| 330      | 330.34       | 1.9352 | 235.61       | 489.4 | 1.79783              |
| 340      | 340.42       | 2.149  | 242.82       | 454.1 | 1.82790              |
| 350      | 350.49       | 2.379  | 250.02       | 422.2 | 1.85708              |
| 360      | 360.58       | 2.626  | 257.24       | 393.4 | 1.88543              |
| 370      | 370.67       | 2.892  | 264.46       | 367.2 | 1.91313              |
| 380      | 380.77       | 3.176  | 271.69       | 343.4 | 1.94001              |
| 390      | 390.88       | 3.481  | 278.93       | 321.5 | 1.96633              |
| 400      | 400.98       | 3.806  | 286.16       | 301.6 | 1.99194              |
| 410      | 411.12       | 4.153  | 293.43       | 283.3 | 2.01699              |
| 420      | 421.26       | 4.522  | 300.69       | 266.6 | 2.04142              |

## Next lecture

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