

10-76 A combined gas-steam power cycle is considered. The topping cycle is a gas-turbine cycle and the bottoming cycle is a simple ideal Rankine cycle. The mass flow rate of the steam, the net power output, and the thermal efficiency of the combined cycle are to be determined.

Assumptions 1 Steady operating conditions exist. 2 Kinetic and potential energy changes are negligible. 3 Air is an ideal gas with constant specific heats.

Properties The properties of air at room temperature are $c_p = 1.005 \text{ kJ/kg} \cdot \text{K}$ and $k = 1.4$ (Table A-2).

Analysis (a) The analysis of gas cycle yields

$$T_6 = T_5 \left(\frac{P_6}{P_5} \right)^{(k-1)/k} = (300 \text{ K})(16)^{0.4/1.4} = 662.5 \text{ K}$$

$$\dot{Q}_{\text{in}} = \dot{m}_{\text{air}}(h_7 - h_6) = \dot{m}_{\text{air}} c_p (T_7 - T_6) \\ = (14 \text{ kg/s})(1.005 \text{ kJ/kg} \cdot \text{K})(1500 - 662.5) \text{ K} = 11,784 \text{ kW}$$

$$\dot{W}_{C,\text{gas}} = \dot{m}_{\text{air}}(h_6 - h_5) = \dot{m}_{\text{air}} c_p (T_6 - T_5) \\ = (14 \text{ kg/s})(1.005 \text{ kJ/kg} \cdot \text{K})(662.5 - 300) \text{ K} = 5100 \text{ kW}$$

$$T_8 = T_7 \left(\frac{P_8}{P_7} \right)^{(k-1)/k} = (1500 \text{ K}) \left(\frac{1}{16} \right)^{0.4/1.4} = 679.3 \text{ K}$$

$$\dot{W}_{T,\text{gas}} = \dot{m}_{\text{air}}(h_7 - h_8) = \dot{m}_{\text{air}} c_p (T_7 - T_8) \\ = (14 \text{ kg/s})(1.005 \text{ kJ/kg} \cdot \text{K})(1500 - 679.3) \text{ K} = 11,547 \text{ kW}$$

$$\dot{W}_{\text{net,gas}} = \dot{W}_{T,\text{gas}} - \dot{W}_{C,\text{gas}} = 11,547 - 5,100 = 6447 \text{ kW}$$

From the steam tables (Tables A-4, A-5, and A-6),

$$h_1 = h_f @ 15 \text{ kPa} = 225.94 \text{ kJ/kg}$$

$$v_1 = v_f @ 15 \text{ kPa} = 0.001014 \text{ m}^3/\text{kg}$$

$$w_{\text{pl,in}} = v_1(P_2 - P_1) = (0.001014 \text{ m}^3/\text{kg})(10,000 - 15 \text{ kPa}) \left(\frac{1 \text{ kJ}}{1 \text{ kPa} \cdot \text{m}^3} \right) = 10.12 \text{ kJ/kg}$$

$$h_2 = h_1 + w_{\text{pl,in}} = 225.94 + 10.13 = 236.06 \text{ kJ/kg}$$

$$\left. \begin{array}{l} P_3 = 10 \text{ MPa} \\ T_3 = 400^\circ\text{C} \end{array} \right\} \begin{array}{l} h_3 = 3097.0 \text{ kJ/kg} \\ s_3 = 6.2141 \text{ kJ/kg} \cdot \text{K} \end{array}$$

$$\left. \begin{array}{l} P_4 = 15 \text{ kPa} \\ s_4 = s_3 \end{array} \right\} \begin{array}{l} x_4 = \frac{s_4 - s_f}{s_{fg}} = \frac{6.2141 - 0.7549}{7.2522} = 0.7528 \\ h_4 = h_f + x_4 h_{fg} = 225.94 + (0.7528)(2372.3) = 2011.8 \text{ kJ/kg} \end{array}$$

Noting that $\dot{Q} \cong \dot{W} \cong \Delta \text{ke} \cong \Delta \text{pe} \cong 0$ for the heat exchanger, the steady-flow energy balance equation yields

$$\dot{E}_{\text{in}} - \dot{E}_{\text{out}} = \Delta \dot{E}_{\text{system}} \stackrel{\text{steady}}{\approx} 0 \longrightarrow \dot{E}_{\text{in}} = \dot{E}_{\text{out}}$$

$$\sum \dot{m}_i h_i = \sum \dot{m}_e h_e \longrightarrow \dot{m}_s (h_3 - h_2) = \dot{m}_{\text{air}} (h_8 - h_9)$$

$$\dot{m}_s = \frac{h_8 - h_9}{h_3 - h_2} \dot{m}_{\text{air}} = \frac{c_p (T_8 - T_9)}{h_3 - h_2} \dot{m}_{\text{air}} = \frac{(1.005 \text{ kJ/kg} \cdot \text{K})(679.3 - 420) \text{ K}}{(3097.0 - 236.06) \text{ kJ/kg}} (14 \text{ kg/s}) = 1.275 \text{ kg/s}$$

$$(b) \quad \dot{W}_{T,\text{steam}} = \dot{m}_s (h_3 - h_4) = (1.275 \text{ kg/s})(3097.0 - 2011.5) \text{ kJ/kg} = 1384 \text{ kW}$$

$$\dot{W}_{\text{p,steam}} = \dot{m}_s w_p = (1.275 \text{ kg/s})(10.12 \text{ kJ/kg}) = 12.9 \text{ kW}$$

$$\dot{W}_{\text{net,steam}} = \dot{W}_{T,\text{steam}} - \dot{W}_{\text{p,steam}} = 1384 - 12.9 = 1371 \text{ kW}$$

$$\text{and} \quad \dot{W}_{\text{net}} = \dot{W}_{\text{net,steam}} + \dot{W}_{\text{net,gas}} = 1371 + 6448 = \mathbf{7819 \text{ kW}}$$

$$(c) \quad \eta_{\text{th}} = \frac{\dot{W}_{\text{net}}}{\dot{Q}_{\text{in}}} = \frac{7819 \text{ kW}}{11,784 \text{ kW}} = \mathbf{66.4\%}$$

